

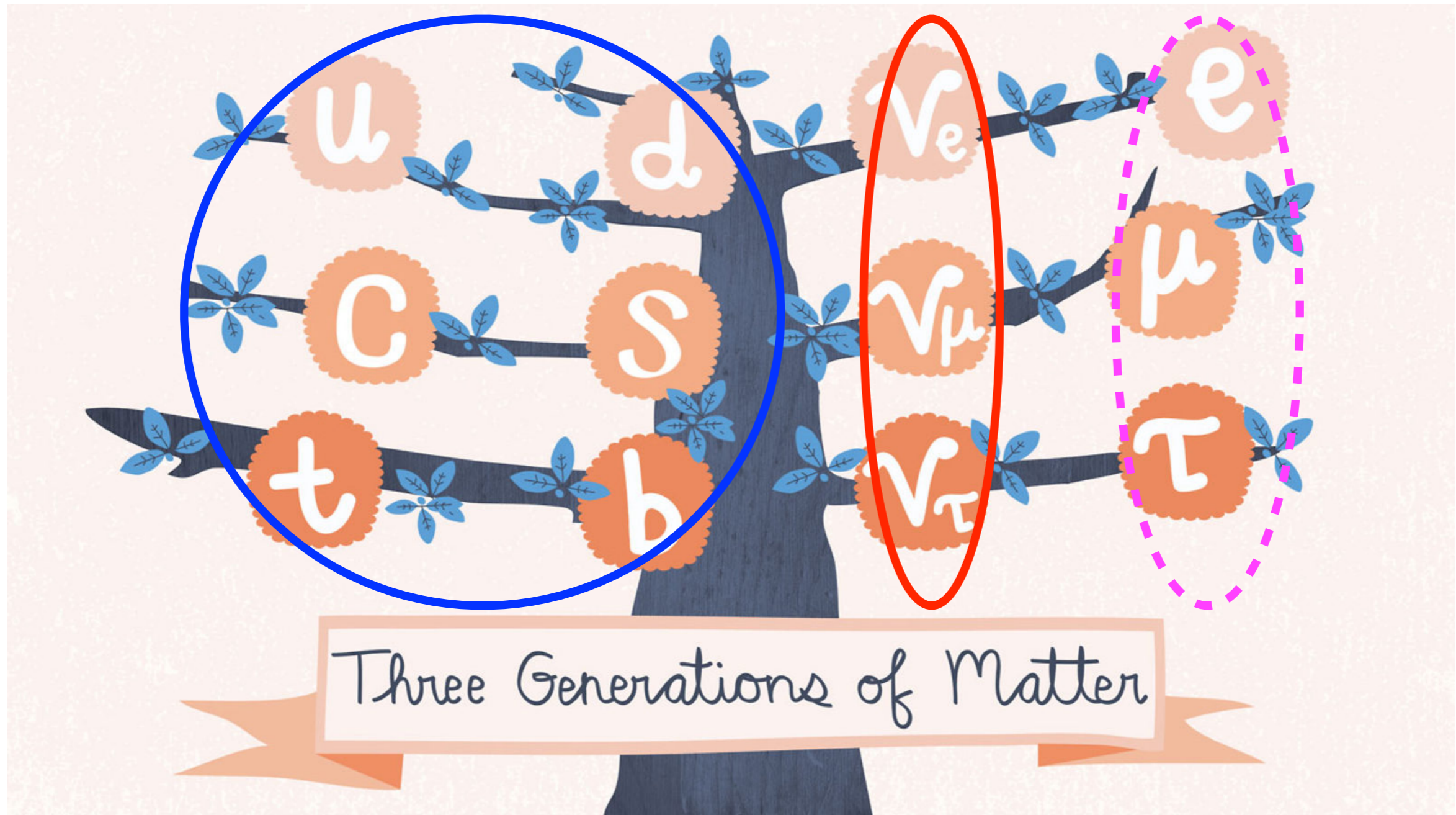
Charged lepton flavor violation

Swagato Banerjee



IPA 2018: Interplay between Particle and Astroparticle physics
8-12 Oct 2018, Cincinnati, OH, USA

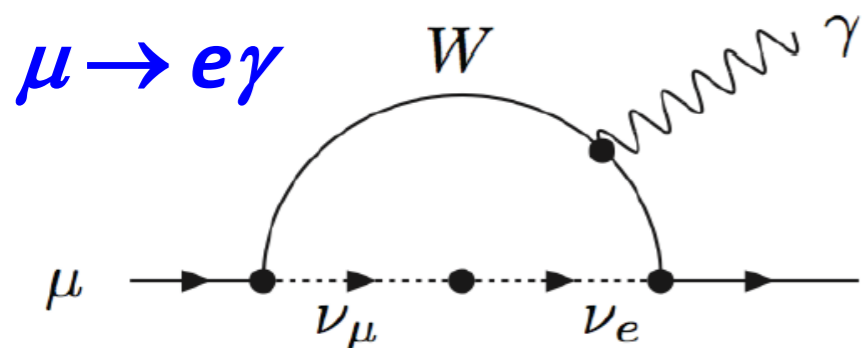
Three Flavors



- Quark - mixing: NP 2008
- Neutrino - oscillations: NP 2002, 2015
- Charged lepton flavor violation: ?

Standard Model (SM)

- Lepton flavor violation (LFV)
 - not forbidden by SM gauge symmetry
 - most new models naturally include LFV vertex
- In SM, LF is conserved for zero degenerate ν masses
- Now we have clear indication that ν 's have finite mass
 \Rightarrow Lepton Flavor is violated in Nature: but by how much?
- SM extended to include finite ν mass and mixing predicts LFV



$$\text{BR}(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{M_W^2} \right|^2 < 10^{-54}$$

... many orders below experimental sensitivity!

- Observation for LFV \Rightarrow unambiguous signature of new physics

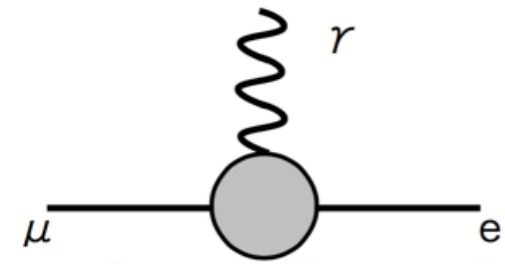
LFV processes

Process	Current Limit	Next Generation exp
$\tau \rightarrow \mu\eta$	BR < 6.5 E-8	
$\tau \rightarrow \mu\gamma$	BR < 6.8 E-8	$10^{-9} - 10^{-10}$ (Belle II)
$\tau \rightarrow \mu\mu\mu$	BR < 3.2 E-8	
$\tau \rightarrow eee$	BR < 3.6 E-8	LHCb, Belle II
$K_L \rightarrow e\mu$	BR < 4.7 E-12	
$K^+ \rightarrow \pi^+e^-\mu^+$	BR < 1.3 E-11	NA62
$B^0 \rightarrow e\mu$	BR < 7.8 E-8	
$B^+ \rightarrow K^+e\mu$	BR < 9.1 E-8	LHCb, Belle II
$\mu^+ \rightarrow e^+\gamma$	BR < 4.2 E-13	10^{-14} (MEG)
$\mu^+ \rightarrow e^+e^+e^-$	BR < 1.0 E-12	10^{-16} (PSI)
$\mu N \rightarrow eN$	$R_{\mu e} < 7.0 E-13$	10^{-17} (Mu2e, COMET)

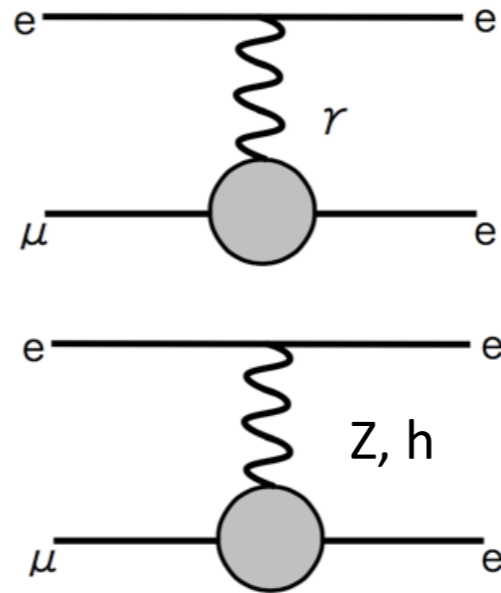
$$R_{\mu e} = \frac{\Gamma(\mu^- + N(A,Z) \rightarrow e^- + N(A,Z))}{\Gamma(\mu^- + N(A,Z) \rightarrow \text{all muon captures})}$$

Muon to electron processes

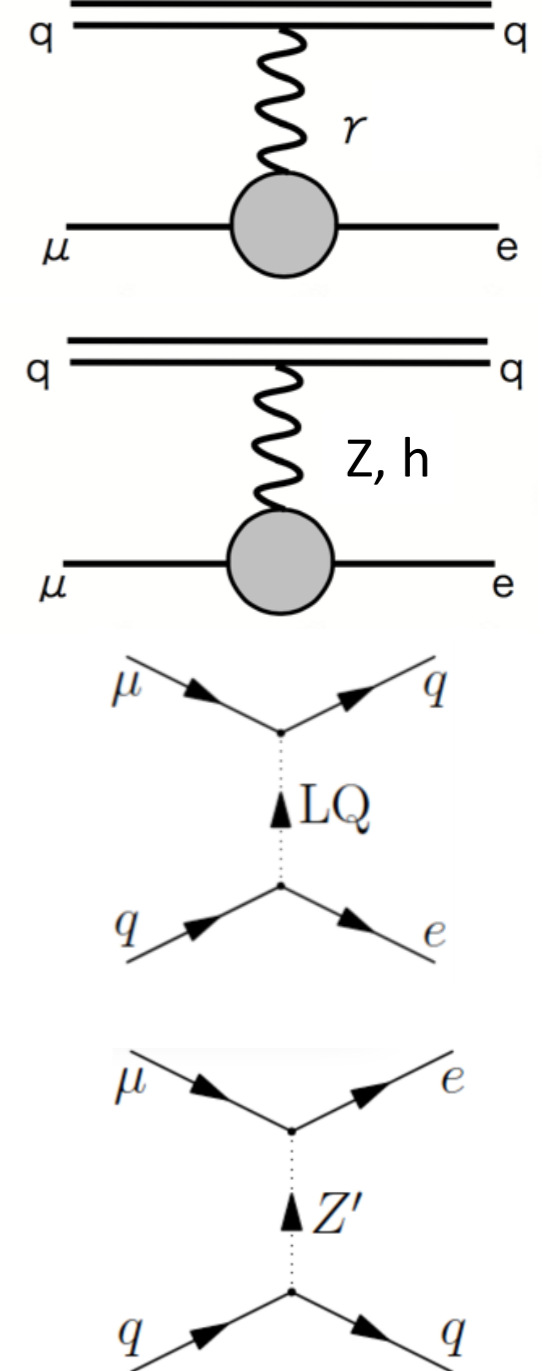
$$\mu^+ \rightarrow e^+ \gamma$$



$$\mu^+ \rightarrow e^+ e^+ e^-$$

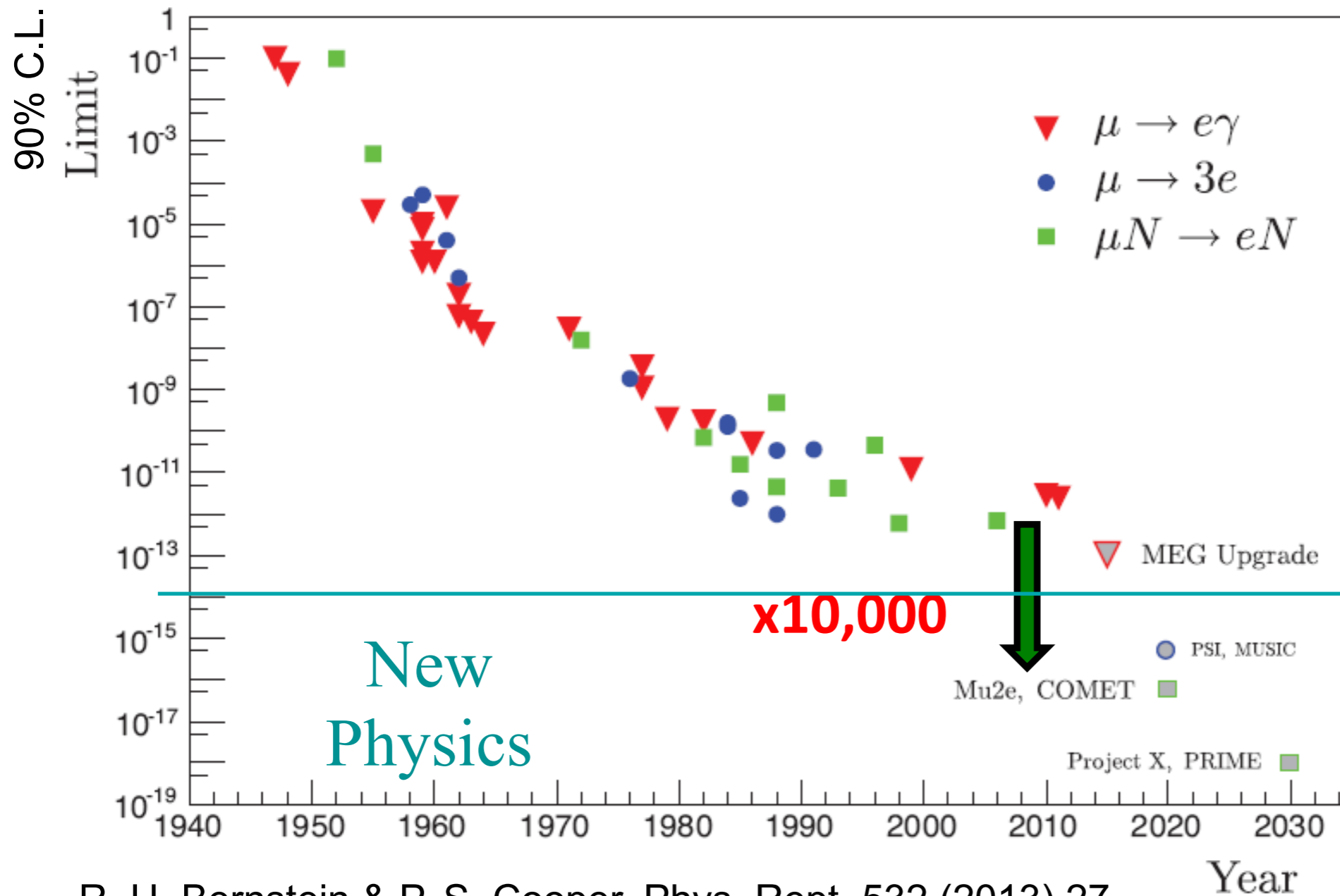


$$\mu^- N \rightarrow e^- N$$



Different channels offer complementary sensitivity.

Muon to electron processes



Current best limits:

MEG-2016

$BR(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$

SINDRUM-1988

$BR(\mu \rightarrow 3e) < 1 \times 10^{-12}$

SINDRUM-II 2006

$R_{\mu e} < 7 \times 10^{-13}$

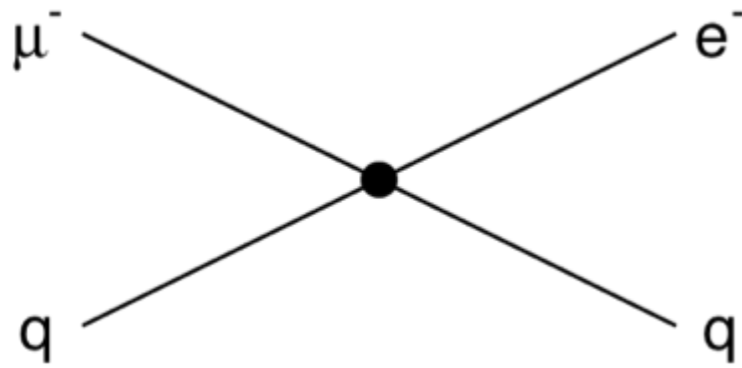
MU2E GOAL

$R_{\mu e} = 6 \times 10^{-17}$

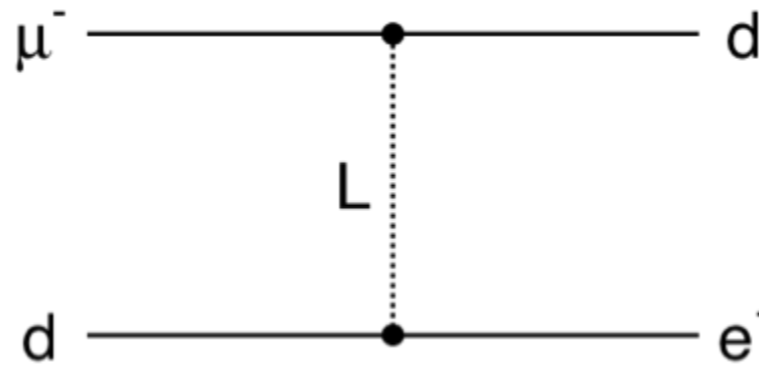
R. H. Bernstein & P. S. Cooper, Phys. Rept. 532 (2013) 27

Beyond SM processes

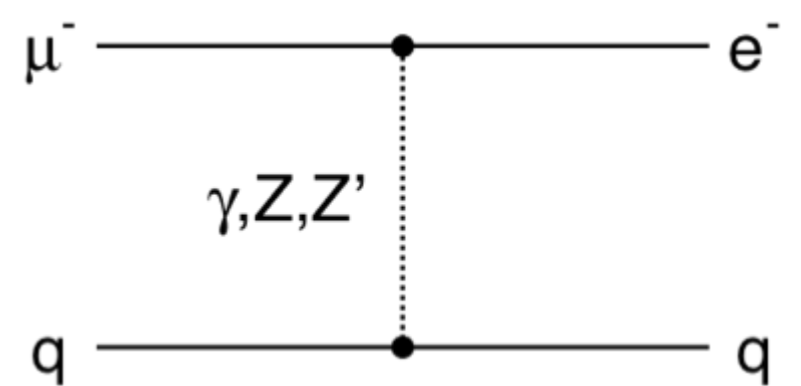
Tree level :



Compositeness

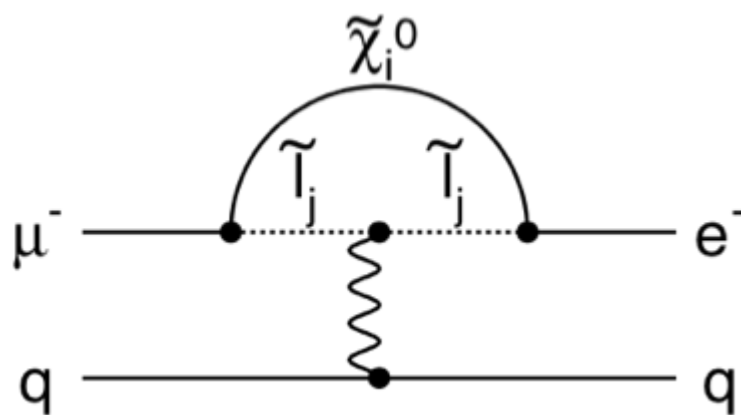


Leptoquarks

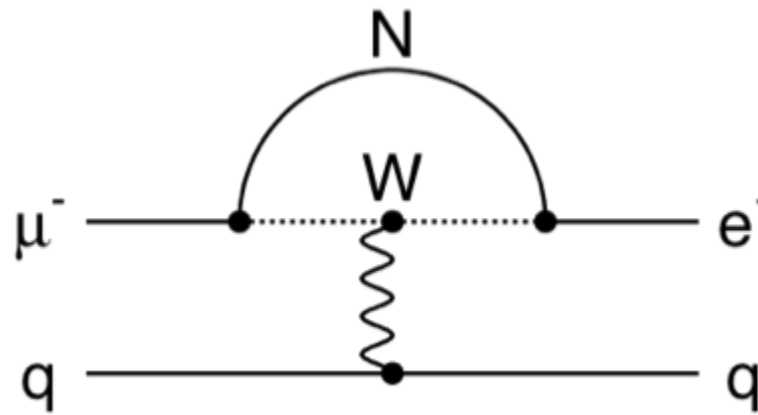


New Heavy Bosons /
Anomalous Couplings

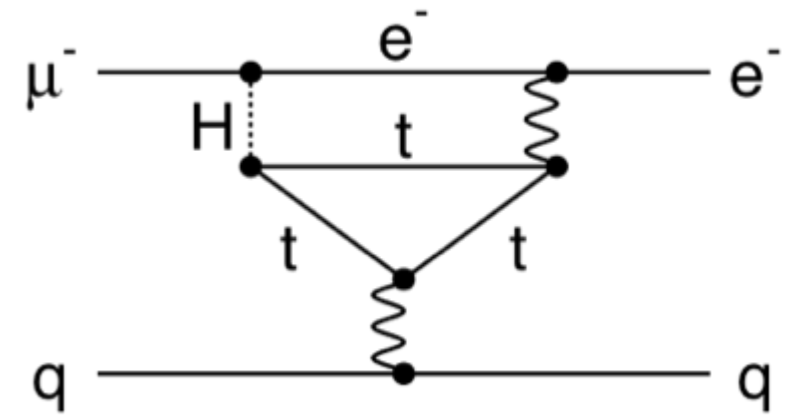
Loop induced :



Supersymmetry



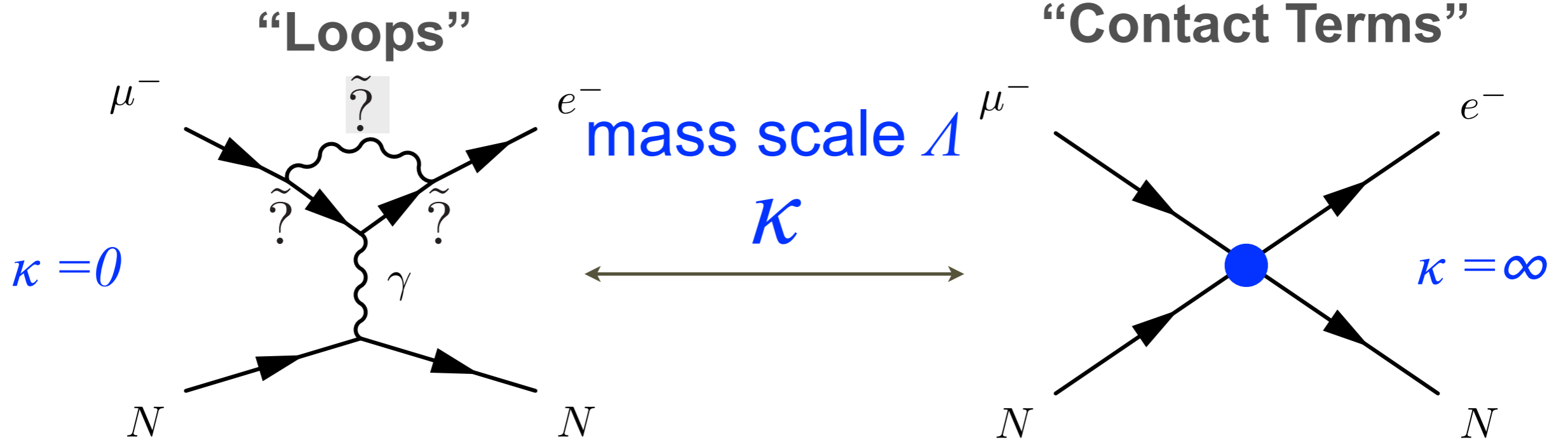
Heavy Neutrinos



Extended higgs models

Effective Lagrangian (\mathcal{L}_{eff})

$$\mathcal{L}_{\text{CLFV}} = \frac{m_\mu}{(\kappa + 1)\Lambda^2} \bar{\mu}_R \sigma_{\mu\nu} e_L F^{\mu\nu} + \frac{\kappa}{(1 + \kappa)\Lambda^2} \bar{\mu}_L \gamma_\mu e_L (\bar{u}_L \gamma_\mu u_L + \bar{d}_L \gamma_\mu d_L)$$



Supersymmetry, Heavy Neutrinos

New Particles at High Mass Scale
(leptoquarks, heavy Z,...)

Contributes to $\mu \rightarrow e\gamma$

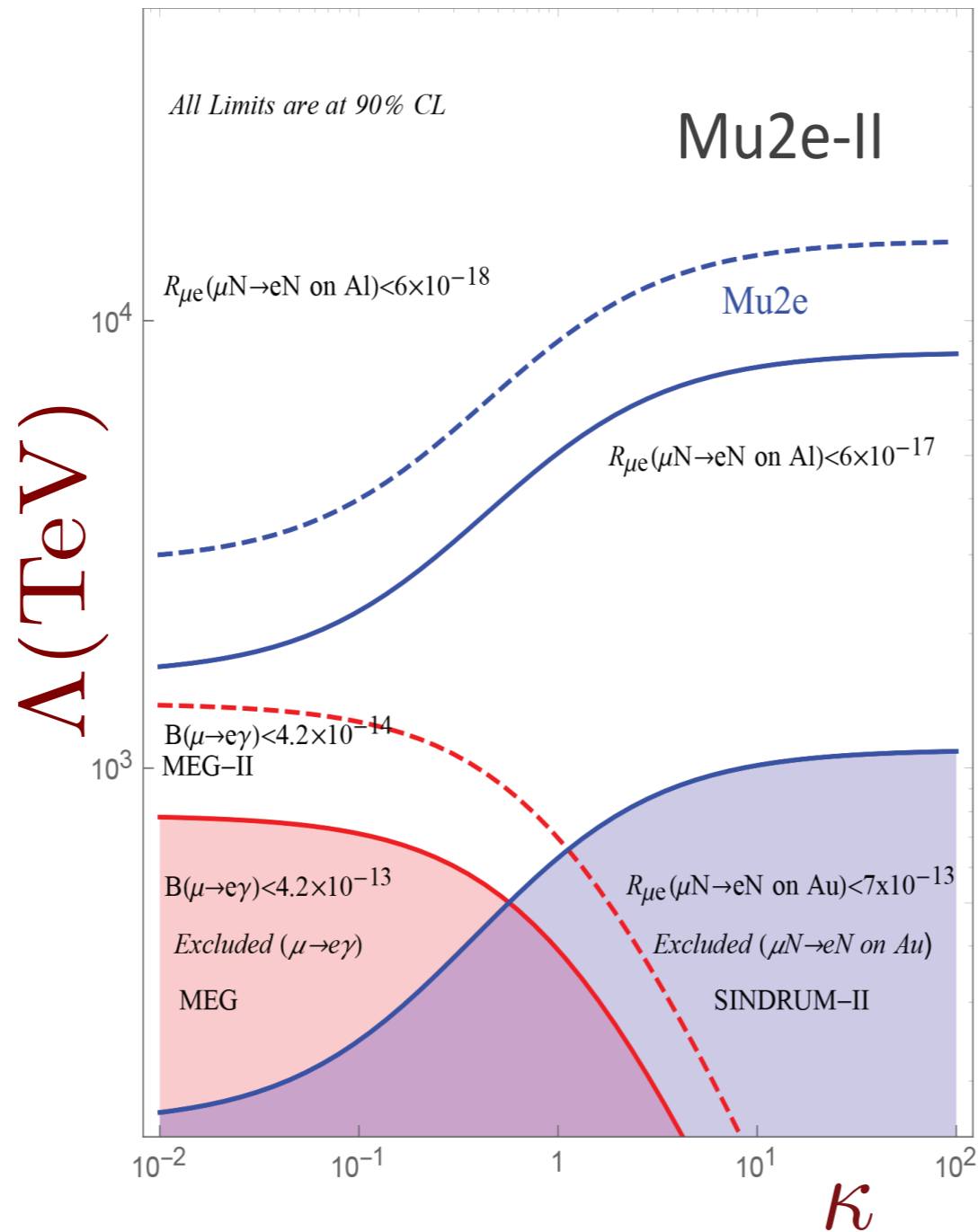
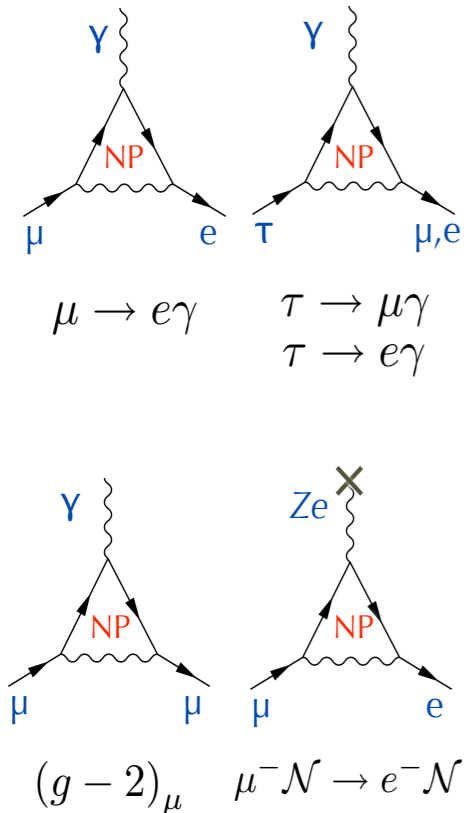
Does not produce $\mu \rightarrow e\gamma$

Scale of new physics

Discovery experiments probing $\sim 10^4$ TeV much beyond LHC

Loop induced :

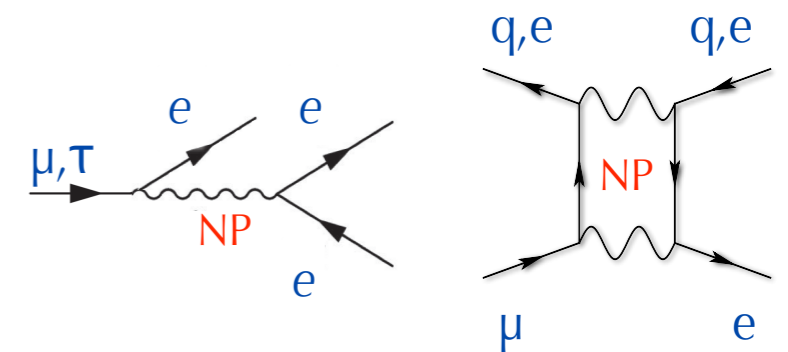
$$\kappa \ll 1$$



Based on A. de Gouvêa, P. Vogel, Prog.Part.Nucl.Phys 71, 75-92 (2013)

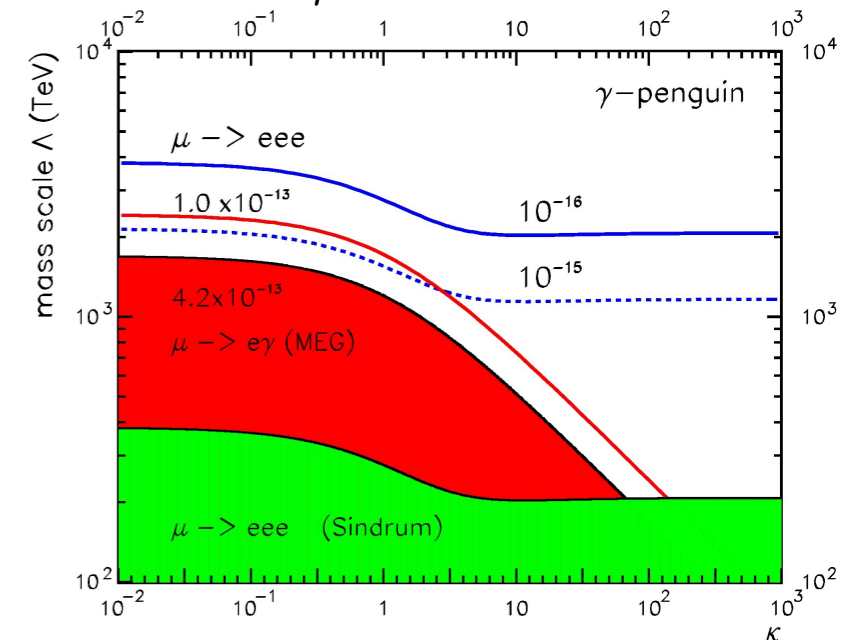
Tree level :

$$\kappa \gg 1$$



$$\mu \rightarrow eee$$

$$\mu^- \mathcal{N} \rightarrow e^- \mathcal{N}$$



Disentangling the nature of LFV

Comparisons between channels are powerful model discriminants

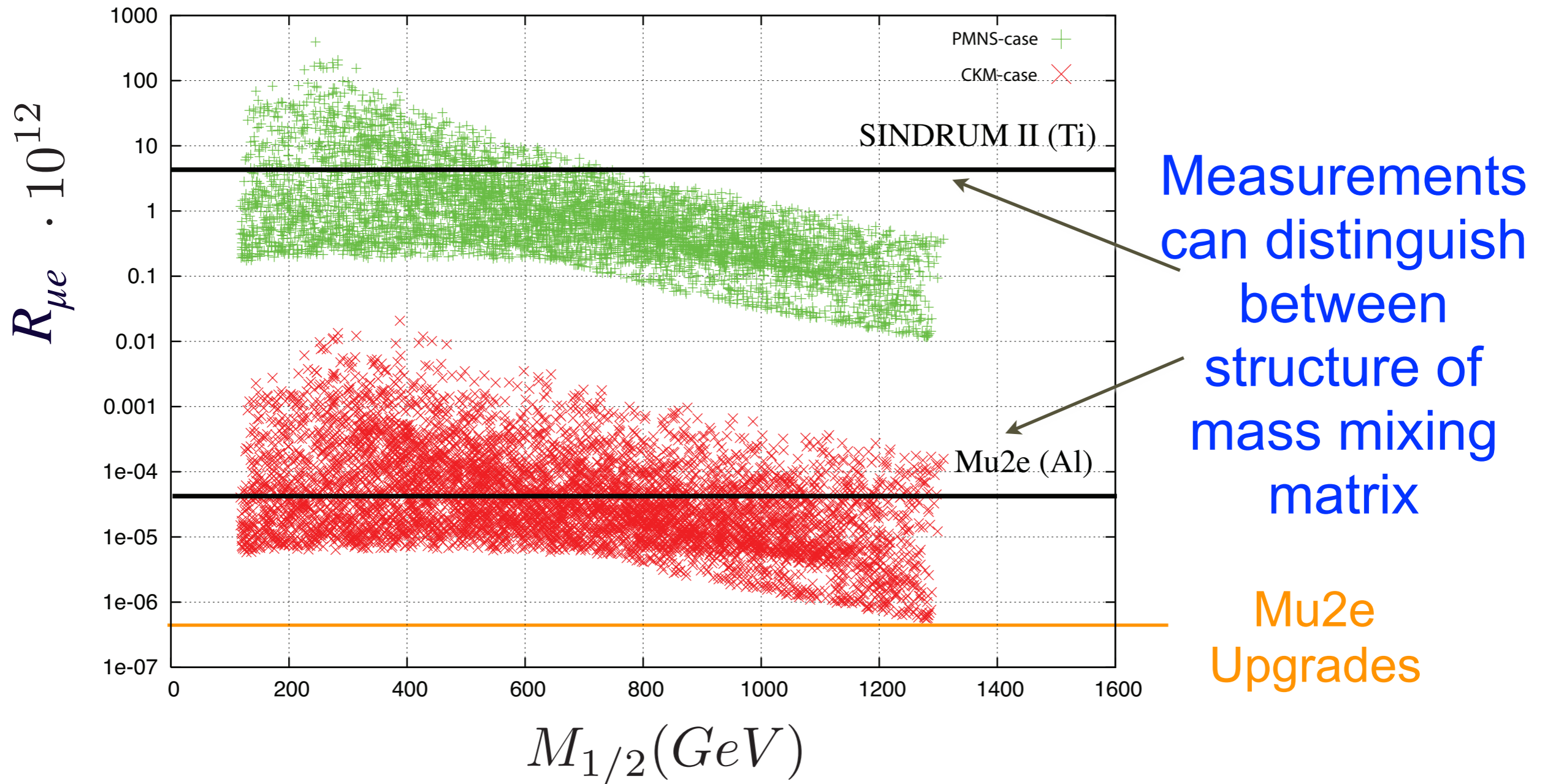
Model	$\mu \rightarrow eee$	$\mu N \rightarrow eN$	$\frac{\text{BR}(\mu \rightarrow eee)}{\text{BR}(\mu \rightarrow e\gamma)}$	$\frac{\text{CR}(\mu N \rightarrow eN)}{\text{BR}(\mu \rightarrow e\gamma)}$
MSSM	Loop	Loop	$\approx 6 \times 10^{-3}$	$10^{-3} - 10^{-2}$
Type-I seesaw	Loop*	Loop*	$3 \times 10^{-3} - 0.3$	0.1–10
Type-II seesaw	Tree	Loop	$(0.1 - 3) \times 10^3$	$\mathcal{O}(10^{-2})$
Type-III seesaw	Tree	Tree	$\approx 10^3$	$\mathcal{O}(10^3)$
LFV Higgs	Loop [†]	Loop* [†]	$\approx 10^{-2}$	$\mathcal{O}(0.1)$
Composite Higgs	Loop*	Loop*	0.05 – 0.5	2 – 20

TABLE VII. – *Pattern of the relative predictions for the $\mu \rightarrow e$ processes as predicted in several models (see the text for details). It is indicated whether the dominant contributions to $\mu \rightarrow eee$ and $\mu \rightarrow e$ conversion are at the tree or at the loop level; Loop* indicates that there are contributions that dominate over the dipole one, typically giving an enhancement compared to Eq. (40, 41). [†] A tree-level contribution to this process exists but it is subdominant.*

L. Calibbi and G. Signorelli,
 Riv. Nuovo Cimento, 41 (2018) 71
[arXiv:1709.00294v2\[hep-ph\]](https://arxiv.org/abs/1709.00294v2)

Disentangling the nature of LFV

μ to e at $\tan \beta = 10$



L. Calibbi, A. Faccia, A. Masiero, S. K. Vempati
Phys.Rev.D74:116002,2006,
[arXiv:hep-ph/0605139v2](https://arxiv.org/abs/hep-ph/0605139v2)

Disentangling the nature of LFV

- Mass of heavy neutrino in Type I Seesaw models:

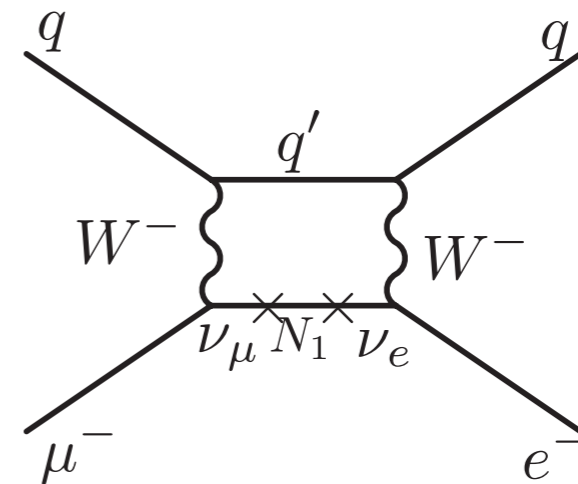
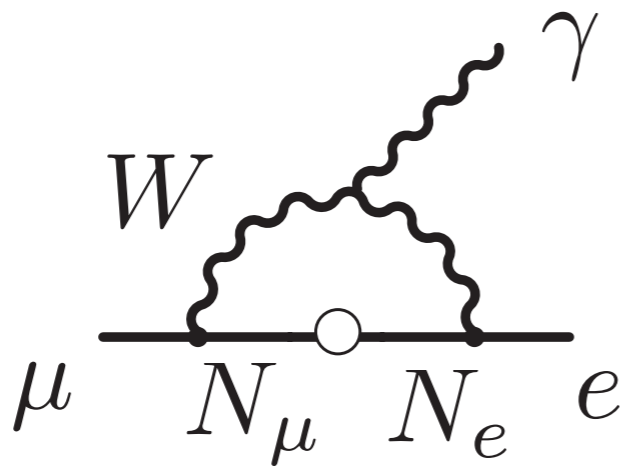
$$\Gamma \propto \frac{\left| \sum_{N_i} U_{N_i \mu} U_{N_i e}^* \right|^2}{M_N^4}$$

$$m_N \leq 6000 \text{ TeV} \left(\frac{10^{-16}}{R_{\mu e}} \right)^{1/4}$$

$$m_N \leq 300 \text{ TeV} \left(\frac{10^{-14}}{\text{BR}(\mu \rightarrow e \gamma)} \right)^{1/4}$$

$$m_N \leq 1000 \text{ TeV} \left(\frac{10^{-14}}{\text{BR}(\mu \rightarrow e e e)} \right)^{1/4}$$

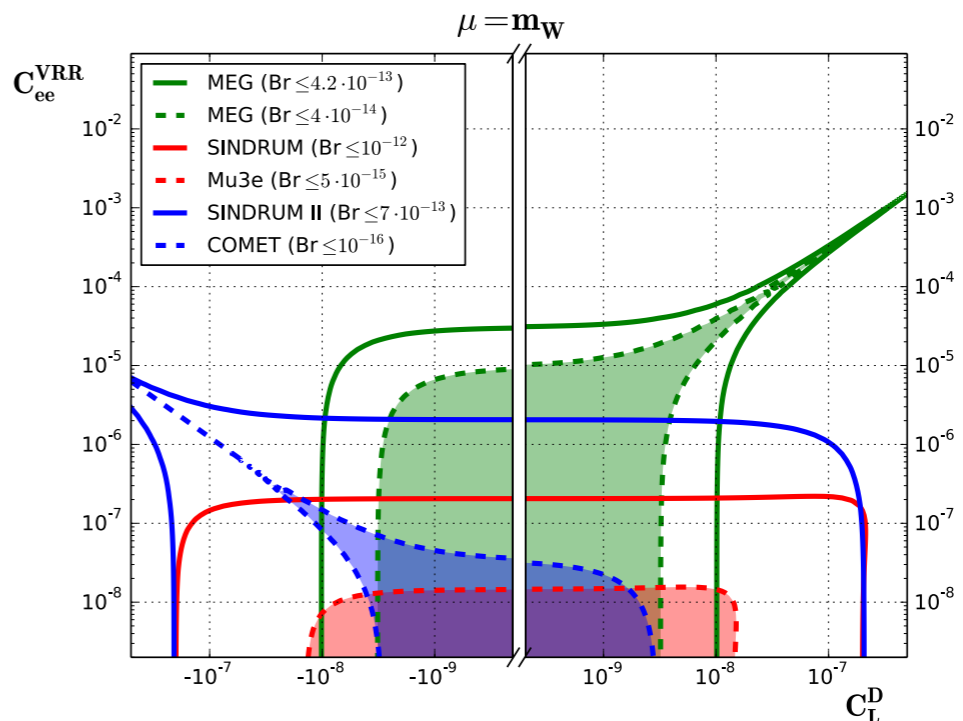
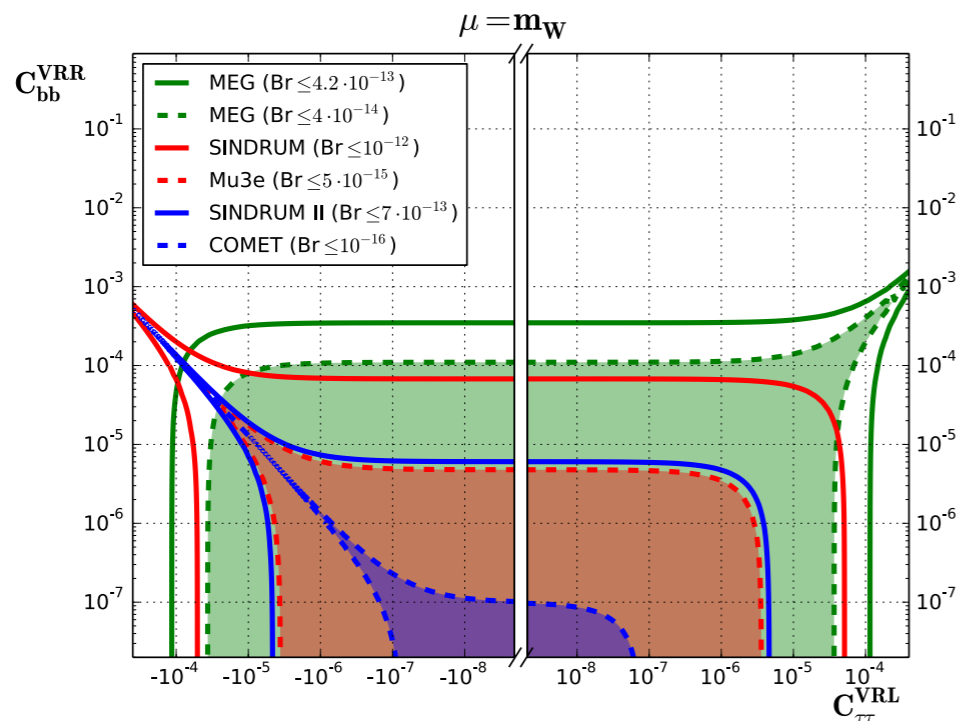
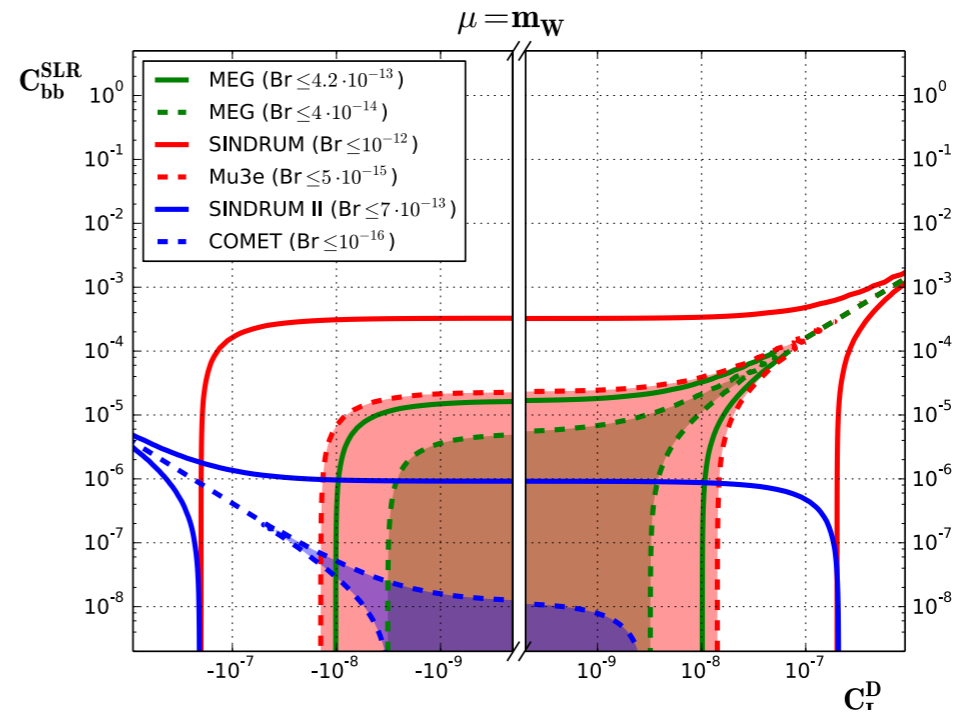
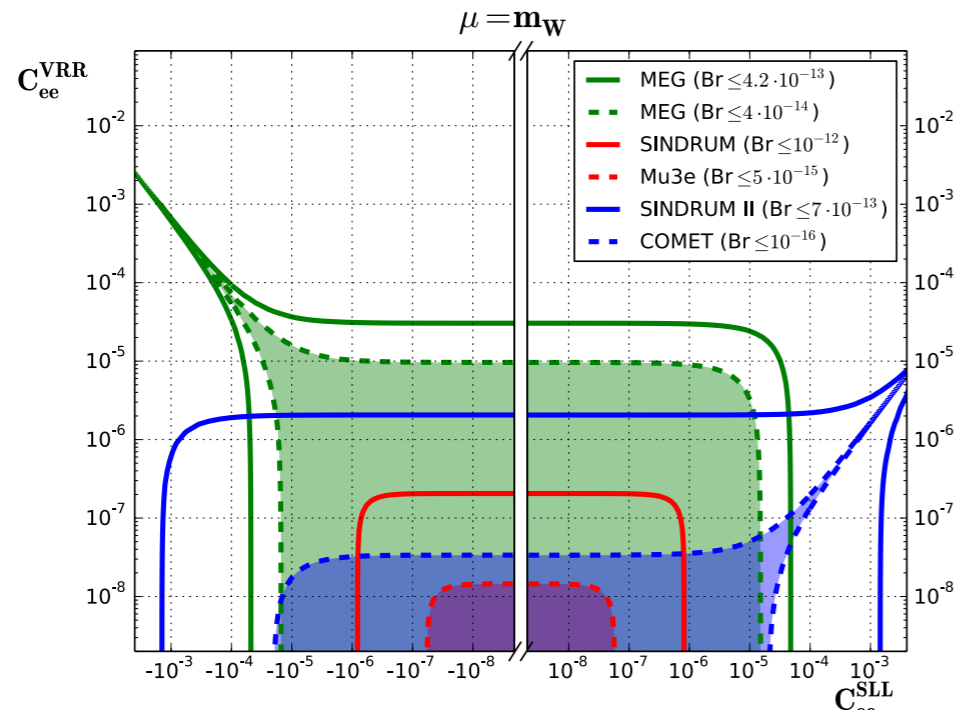
- Left diagram for $\mu \rightarrow e \gamma$, $\mu N \rightarrow e N$, $\mu \rightarrow e e e$; right only for $\mu N \rightarrow e N$



Rodrigo Alonso, Mikael Dhen, Belen Gavela, Thomas Hambye, JHEP01(2013)118, [arXiv:1209.2679v2](https://arxiv.org/abs/1209.2679v2)
 D. N. Dinh, A. Ibarra, E. Molinaro, S. T. Petcov, JHEP08(2012)125, [arXiv:1205.4671v4](https://arxiv.org/abs/1205.4671v4)

Disentangling the nature of LFV

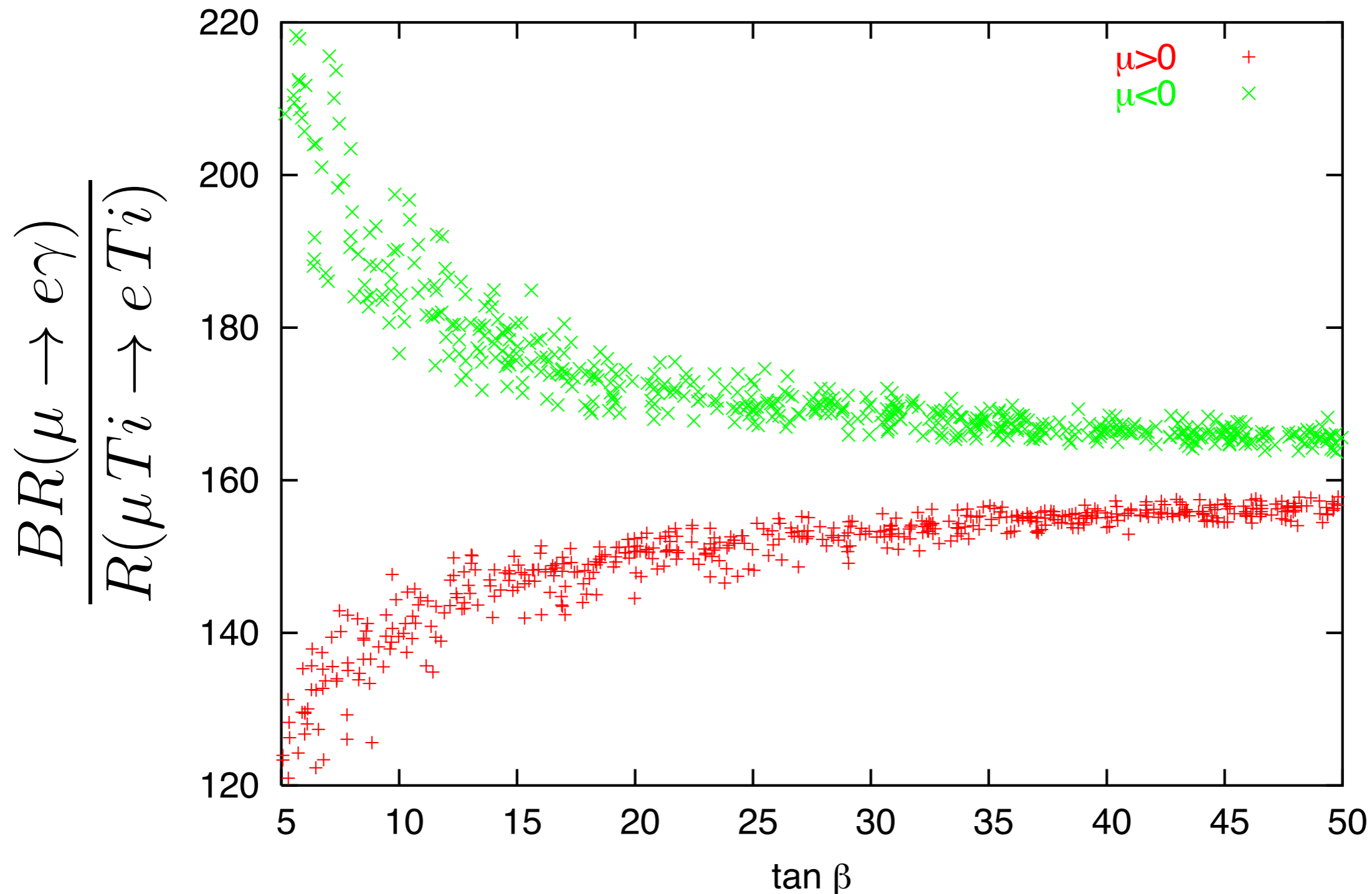
- Wilson coefficients for Vector (V), Scalar (S), Dipole (D) terms in \mathcal{L}_{eff}



Andreas Crivellin, Sacha Davidson, Giovanni Marco Pruna, Adrian Signer
 JHEP05(2017)117, [arXiv:1702.03020v3](https://arxiv.org/abs/1702.03020v3)

Disentangling the nature of LFV

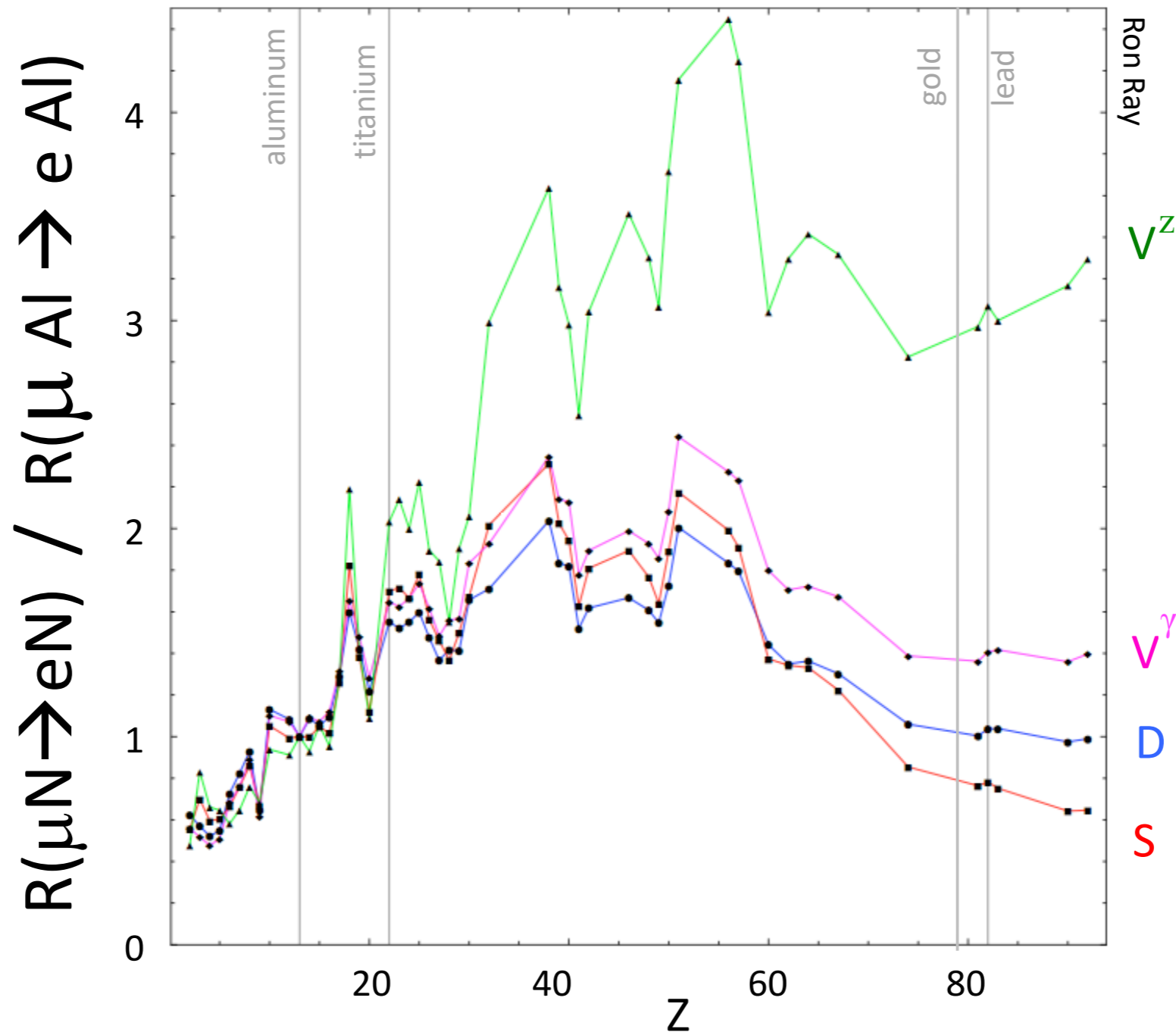
- Constraining $\text{sign}(\mu)$ in mSUGRA with seesaw induced neutrino masses



Carlos E. Yaguna, Int.J.Mod.Phys. A21 (2006) 1283–1289, arXiv:hep-ph/0502014v2

Disentangling the nature of LFV

- Z-dependence of μ to e conversion rates normalized to Aluminum ($Z=13$)



Vincenzo Cirigliano, Ryuichiro Kitano, Yasuhiro Okada, Paula Tuzon
Phys.Rev.D80:013002,2009, [arXiv:0904.0957v1](https://arxiv.org/abs/0904.0957v1) [hep-ph]

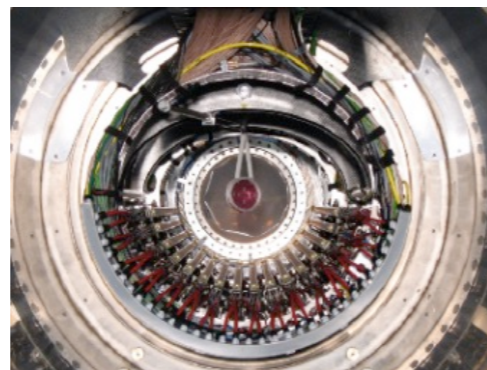
Muon to electron experiments

	$\mu^+ \rightarrow e^+\gamma$	$\mu^-N \rightarrow e^-N$	$\mu^+ \rightarrow e^+e^+e^-$
	MEG (PSI)	Mu2e COMET (FNAL) (JPARC)	Mu3e (PSI)
Now:	4.2×10^{-13} (MEG, 2016)	7×10^{-13} (SINDRUM-II, 2006)	1×10^{-12} (SINDRUM, 1998)
Future:	4×10^{-14}	6×10^{-17}	1×10^{-14}
Timeframe:	2020	2023	2020

Mu3e @PSI



MEG Upgrade @PSI



Mu2e @FNAL



COMET @KEK

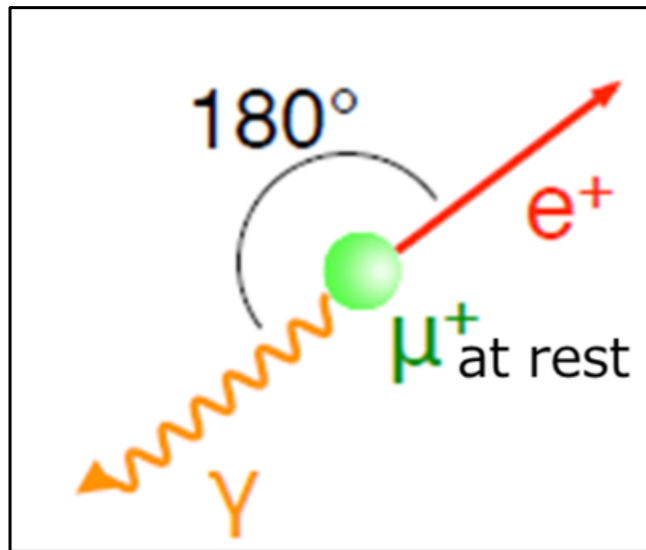


MEG experiment

Signal

Back-to-back $e\gamma$

$$E_e = E_\gamma = m_\mu/2$$

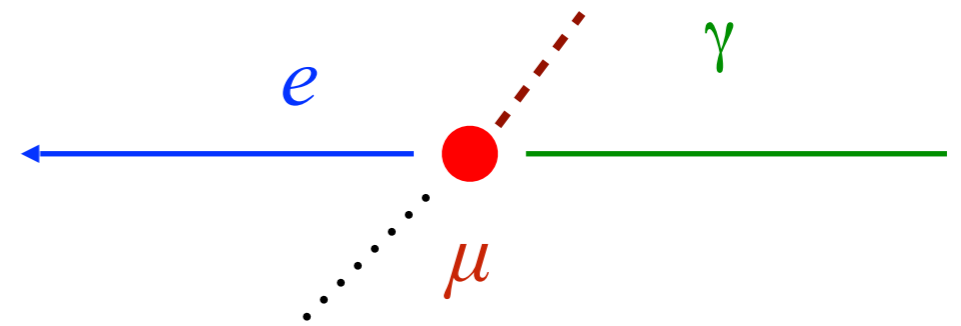


Keys to success:

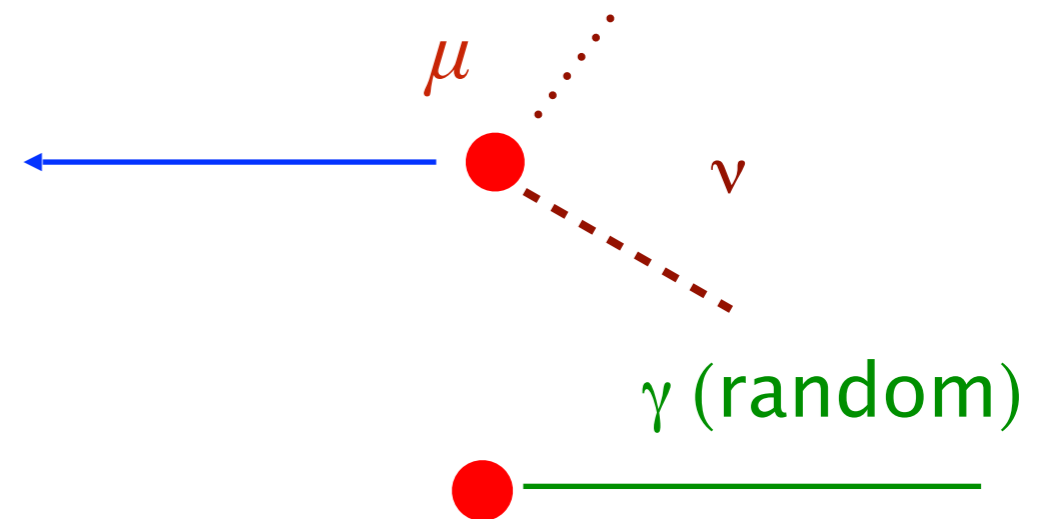
excellent energy, timing,
angular resolutions,
particularly ΔE_γ and $\Delta\theta_{e\gamma}$

Background

correlated $\mu \rightarrow e \gamma \nu \nu$



uncorrelated $\mu \rightarrow e \nu \nu$



MEG results

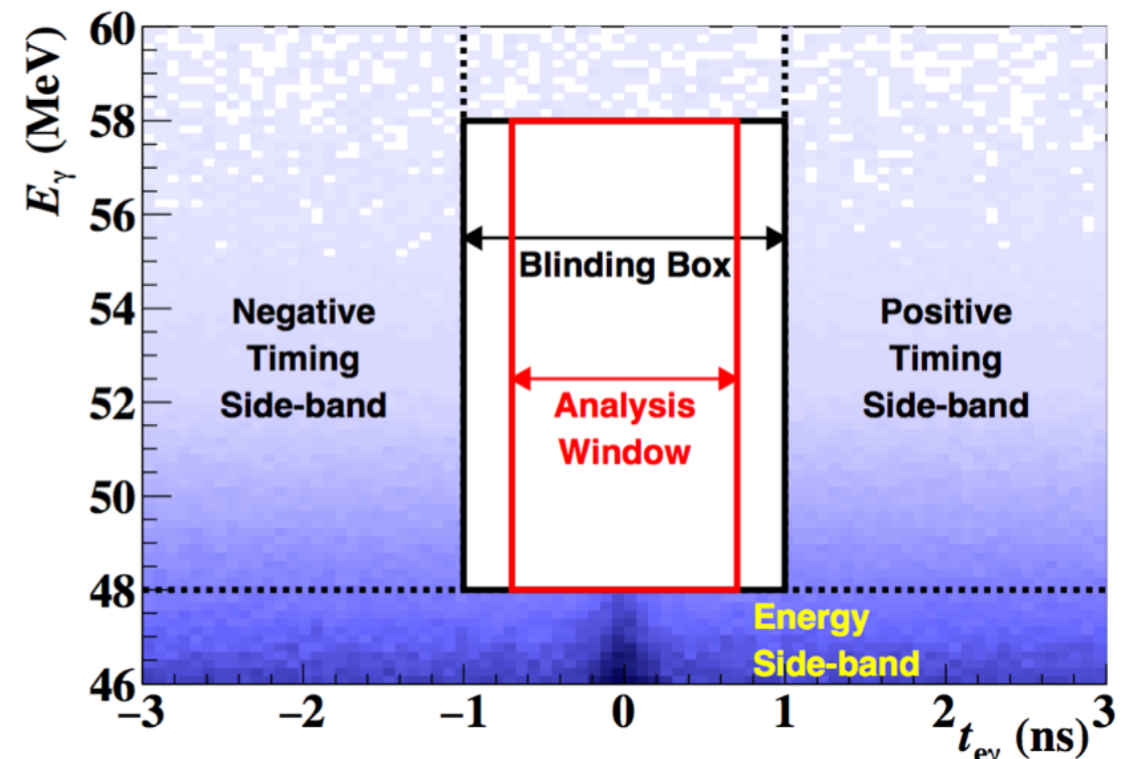
- Published results uses full data set (2009-2013)
 - $\sim 7.5 \times 10^{14}$ stopped μ^+

Utilizes 5 variables

- E_e, E_γ
- $t_{e\gamma} = t_e - t_\gamma$
- $\theta_{e\gamma}$
- $\phi_{e\gamma}$

Blind Analysis

Full Likelihood fit to data



$$\text{Best fit } \text{BF}(\mu^+ \rightarrow e^+\gamma) = -2.2 \times 10^{-13}$$

$$\text{BF}(\mu^+ \rightarrow e^+\gamma) < 4.2 \times 10^{-13} \text{ @ 90\% CL}$$
$$(< 5.3 \times 10^{-13} \text{ expected})$$

Eur. Phys. J. C76 (2016) 434 [arXiv:1605.05081]

Muon to electron conversion experiments

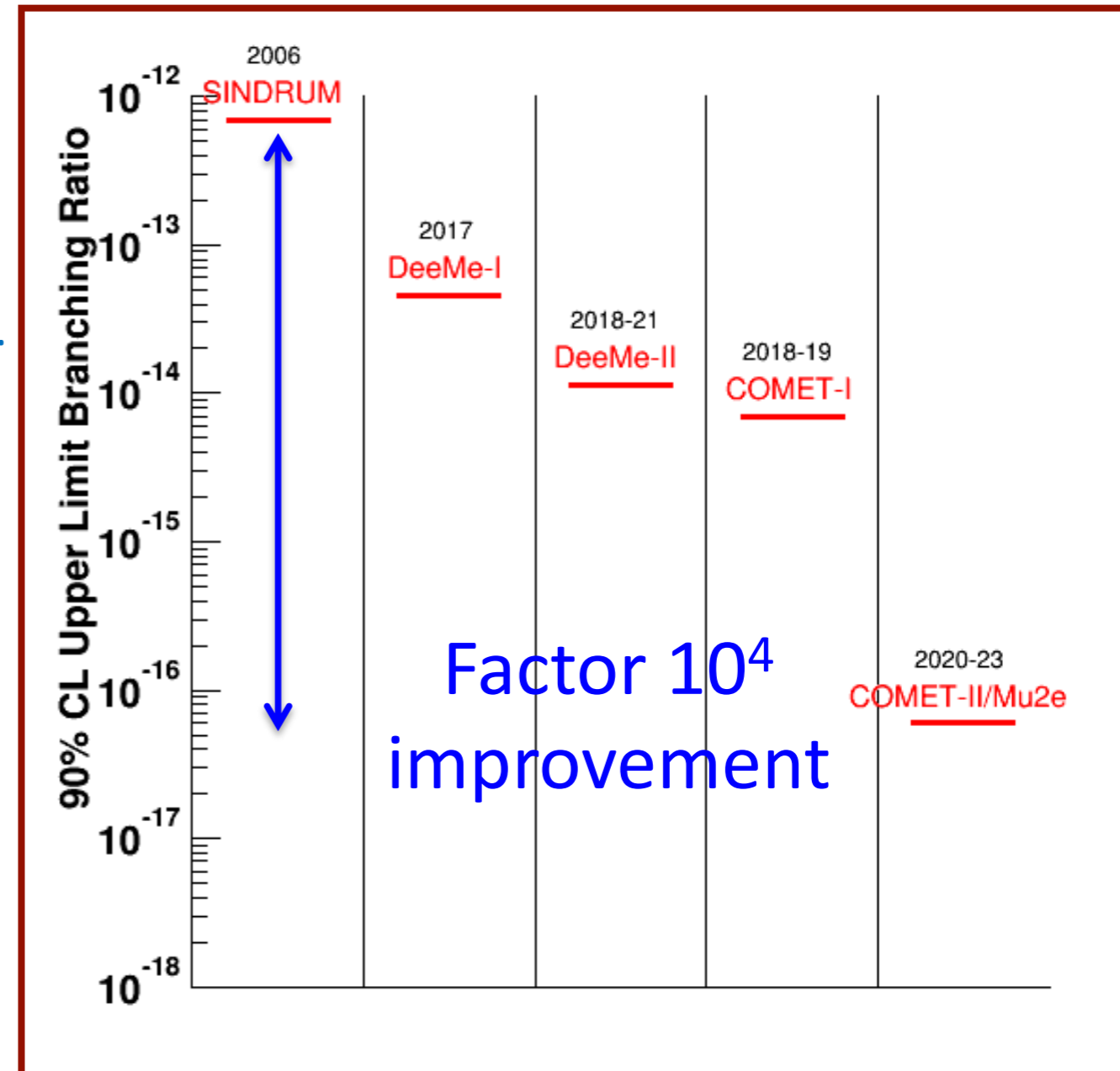
Current State-of-the-art (@ 90% CL) :

$$R_{\mu e} = \frac{\Gamma(\mu^- \text{ Au} \rightarrow e^- \text{ Au})}{\Gamma(\mu^- \text{ Au capture})} < 7 \times 10^{-13}$$

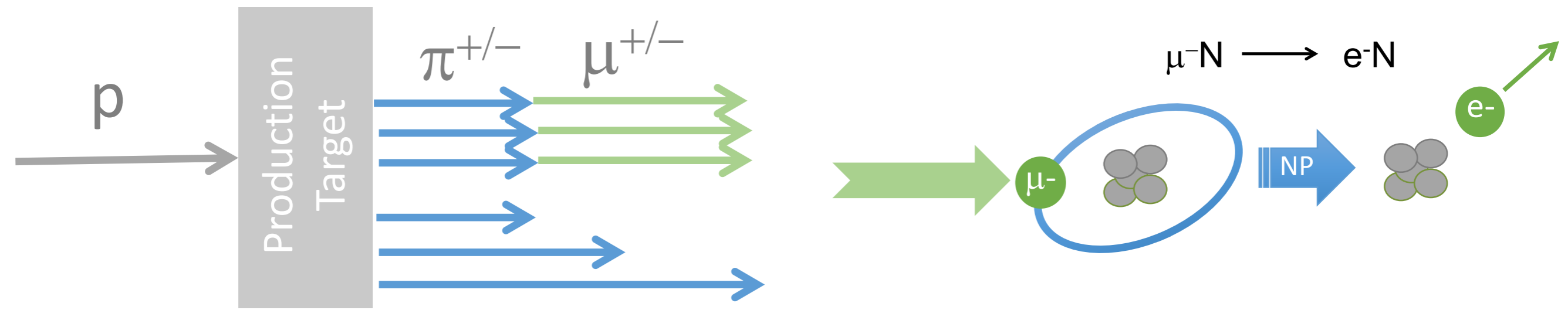
W. Bertl, et al. (SINDRUM-II) Eur. Phys. J. C47 (2006) 337.

Next generation experiments:

- DeeMee (J-PARC, 3 GeV) x10
- Mu2e (Fermilab) x10,000
- COMET (J-PARC, 8 GeV)
 - Phase-I x10-100
 - Phase-II x10,000

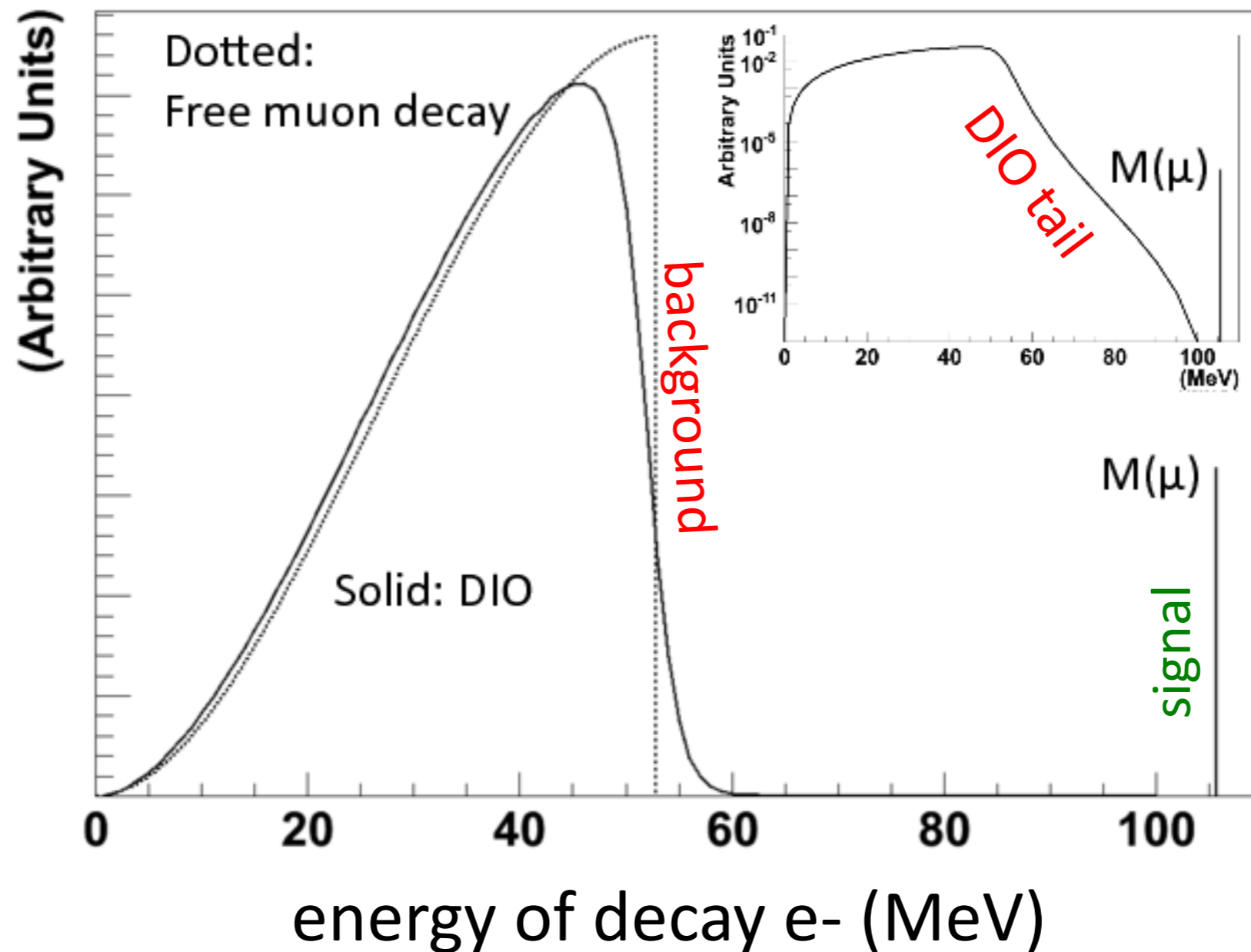


Muon to electron conversion experiments



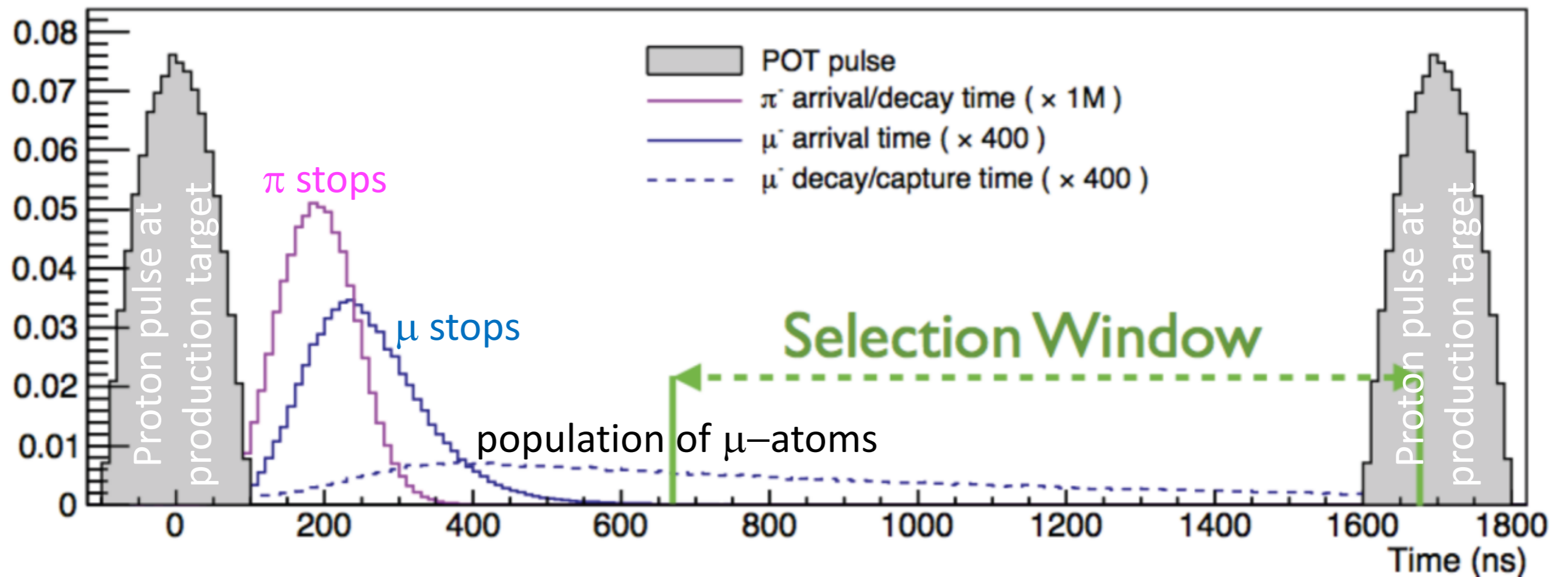
- **Stopped μ^- is captured in atomic orbit**
 - Quickly (\sim fs) cascades to 1s state
- **Bohr radius ~ 20 fm** (for aluminum)
 - Significant overlap of μ^- and N wavefunctions
 - Lifetime of the μ -atom \sim few 100 ns for stopping targets of interest
- **Once in orbit, 3 things can happen**
 - Decay : $\mu^- N_{(A,Z)} \rightarrow e^- \nu \nu N_{(A,Z)}$ (background) [39% in Al target]
 - Capture : $\mu^- N_{(A,Z)} \rightarrow \nu N^*_{(A, Z-1)}$ (normalization) [61% in Al target]
 - Conversion : $\mu^- N_{(A,Z)} \rightarrow e^- N_{(A,Z)}$ (signal) $E_e = m_\mu - E_{\text{binding}} - E_{\text{recoil}} = 104.9$ MeV [in Al]

Background from decay in orbit (DIO)



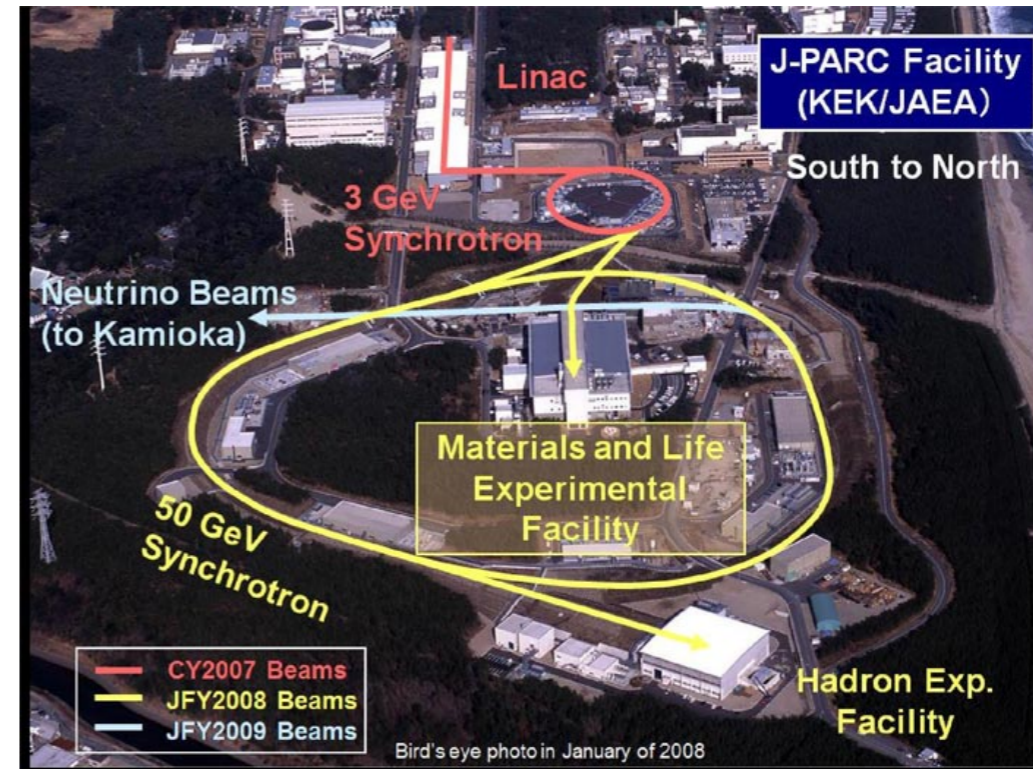
- E_e follows the Michel spectrum... but with a long tail from nuclear recoil $E_{\max} = E_{\mu e}$
 - Requires excellent σ_p (<200 keV/c) & FWHM < 1 MeV/c to suppress

Background from radiative pion capture (RPC)



- Pions that survive to the stopping target are promptly captured on the nucleus
 - few% of the time, radiate γ with $E_\gamma \sim m_\mu$
 - Suppressed by 10^9 - 10^{10} with pulsed proton beam and utilizing a delayed search window while maintaining a high efficiency for signal ($\sim 50\%$)

Proton beams for Mu2e and COMET

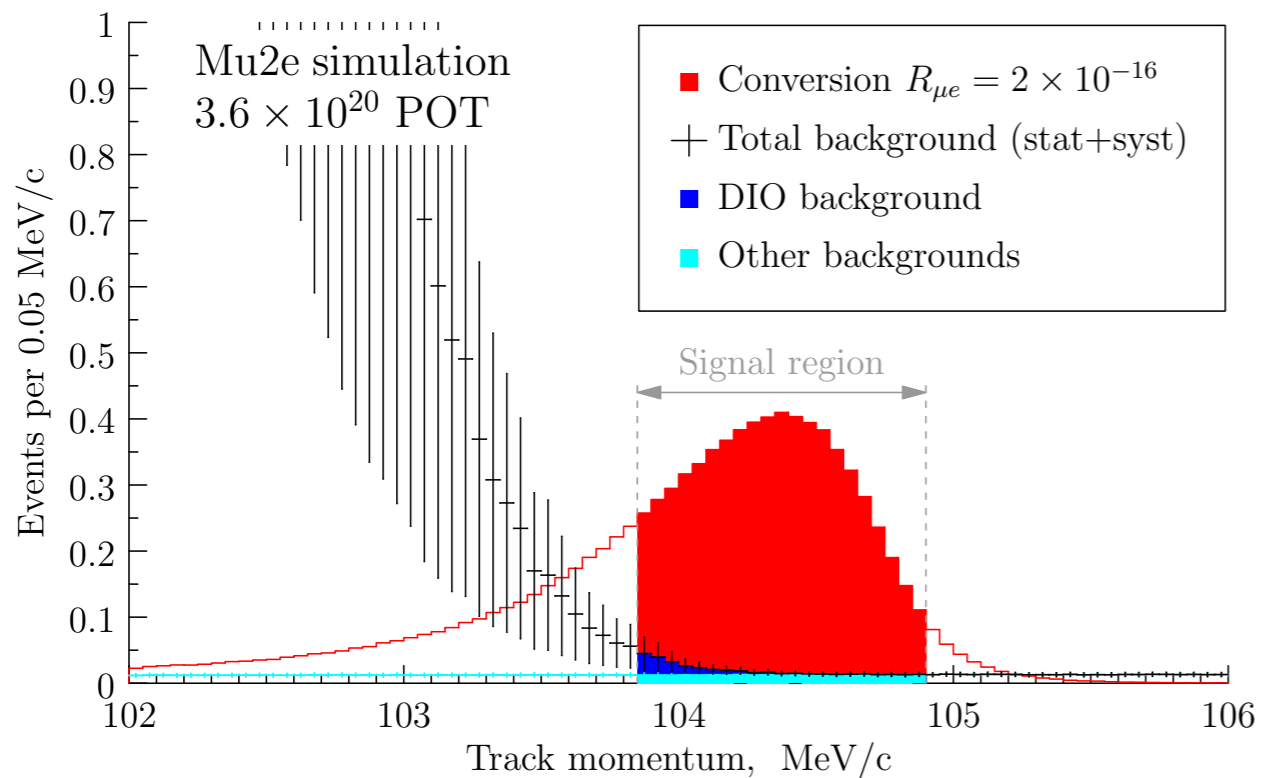


- 8kW of 8 GeV protons
 - 10^{10} stop μ^-/s
- Protons delivered in pulses
 - 4×10^7 protons per pulse
 - spaced by 1695 ns.
- Mu2e will run simultaneously with NOvA and short baseline neutrino experiments

- Utilize 8 GeV protons
 - Phase I : 3 kW ; 10^{8-9} stop μ^-/s
 - Phase II: 56 kW ; 10^{11} stop μ^-/s
- Protons delivered in pulses
 - spaced by 1100 ns.
- COMET will share beam time with T2K

Mu2e Sensitivity [COMET Phase II is similar]

**Typical Signal [SUSY at 10^{-15} :]
40 events vs 0.4 bkg**



Background compositions

Category	Source	Events
	μ Decay in Orbit	0.14
Intrinsic	Radiative μ Capture	<0.01
	Radiative π Capture	0.02
	Beam electrons	<0.01
	μ Decay in Flight	<0.01
Late Arriving Beam	π Decay in Flight	<0.01
	Anti-proton induced	0.04
Miscellaneous	Cosmic Ray induced	0.21
Total Background		0.41

(assuming $6.7E17$ stopped muons in $6E7$ s of beam time)

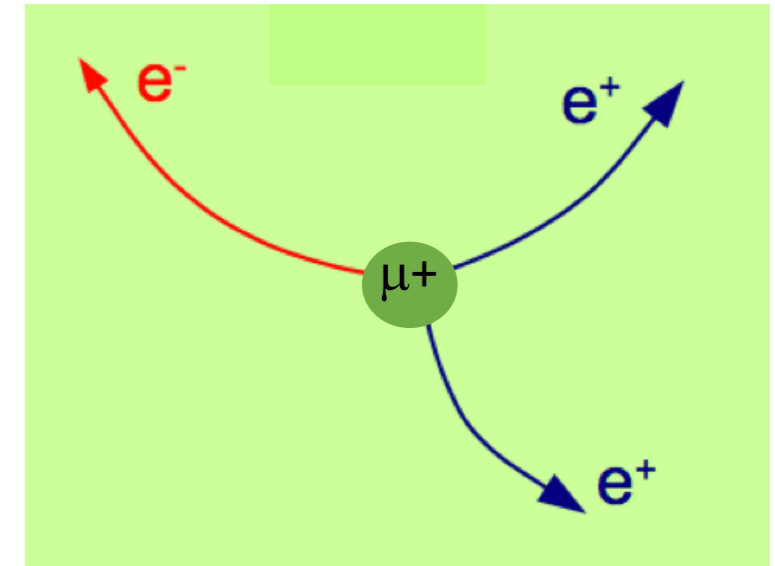
- Full Geant4 simulation and reconstruction, background overlaid with signal
- Discovery sensitivity accomplished with 3 years of running and suppressing backgrounds to < 0.4 event total: 2×10^{-16} [5σ significance]
- Single event sensitivity 3×10^{-17}
- Null signal upper limit 8×10^{-17} @ 90% C.L.

Muon to three electrons experiment

Current State-of-the-art (@ 90% CL) :

$$BF(\mu^+ \rightarrow e^+e^+e^-) < 1 \times 10^{-12}$$

U. Bellgardt, et al. (SINDRUM) Nucl.Phys. B299 (1988) 1.



Next generation experiments:

– Mu3e (PSI)

- Phase Ia x20
- Phase Ib x400
- Phase II x10,000

Muon to three electrons experiment

Signal

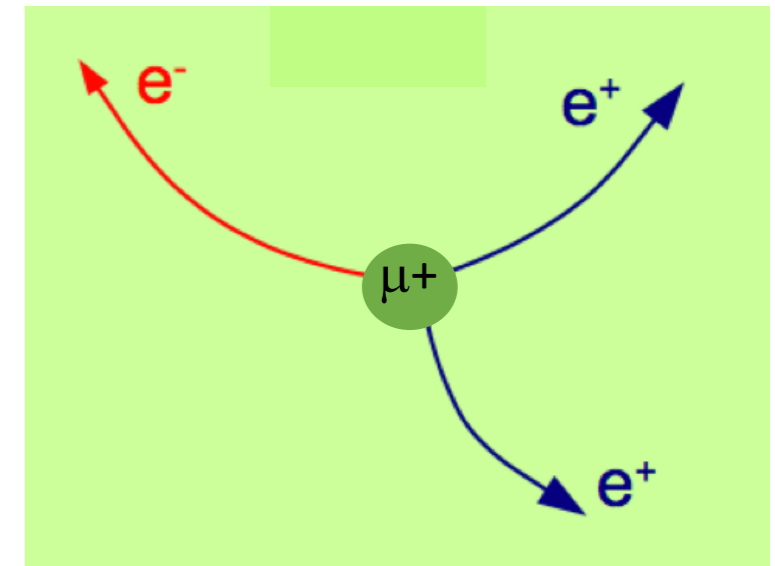
$$\Sigma p = 0$$

$$E_e < m_\mu/2$$

$$\Sigma E_e = m_\mu$$

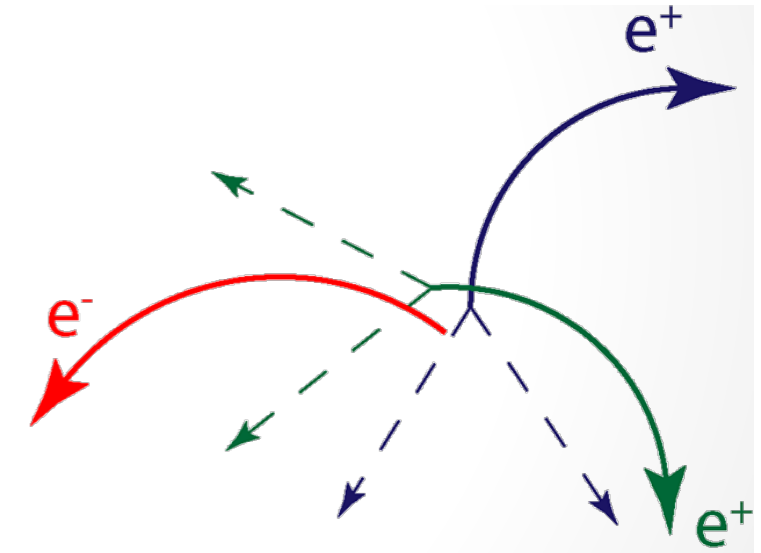
Common vertex

Co-incident in time



Backgrounds

- internal conversion of photon in radiative muon decays
- accidental photons followed by e^-e^+ pair-production

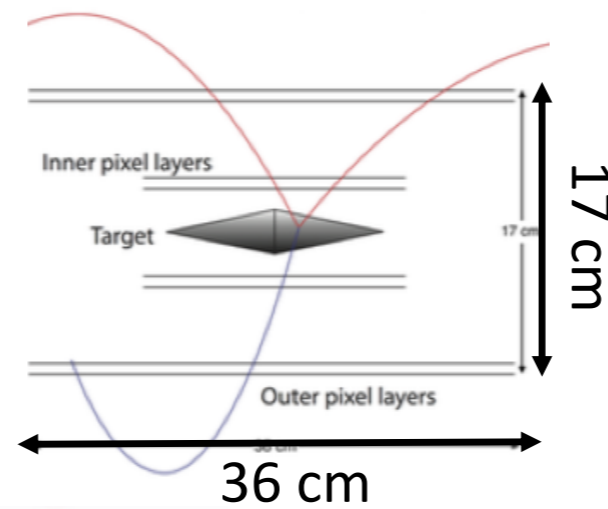


- **Keys to success:** excellent momentum, timing, and vertex resolutions

Phased construction progressively more sensitive

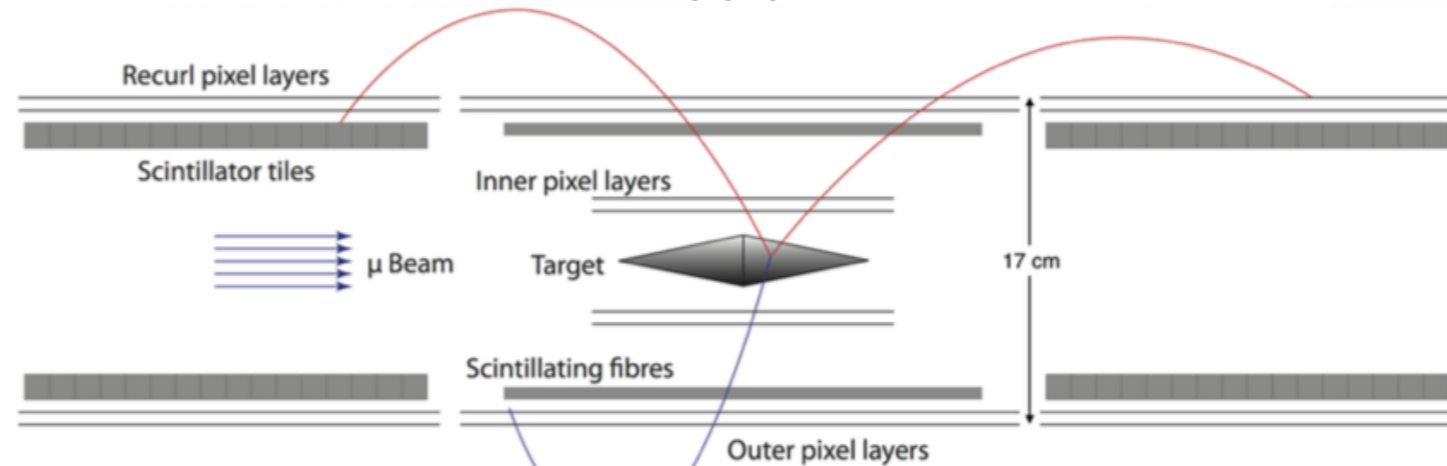
All inside 1T magnetic field

Phase-Ia



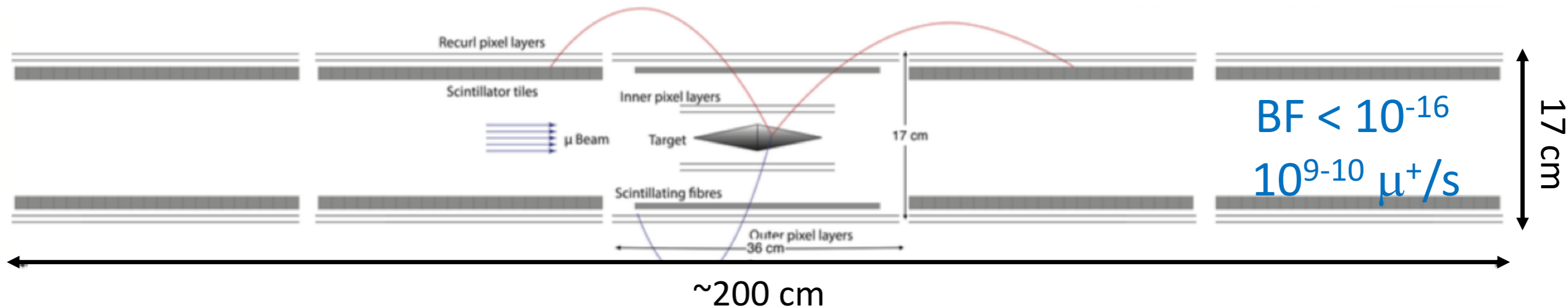
$BF < 10^{-13} - 10^{-14}$
 $10^7 \mu^+/s$

Phase-Ib



$BF < 10^{-14} - 10^{-15}$
 $10^8 \mu^+/s$

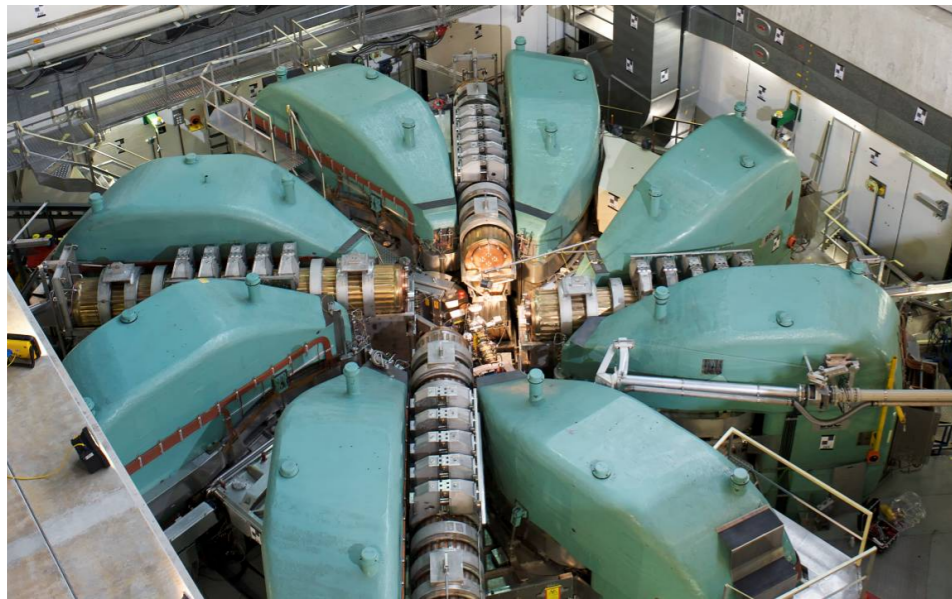
Phase-II



$BF < 10^{-16}$
 $10^9 - 10^{10} \mu^+/s$

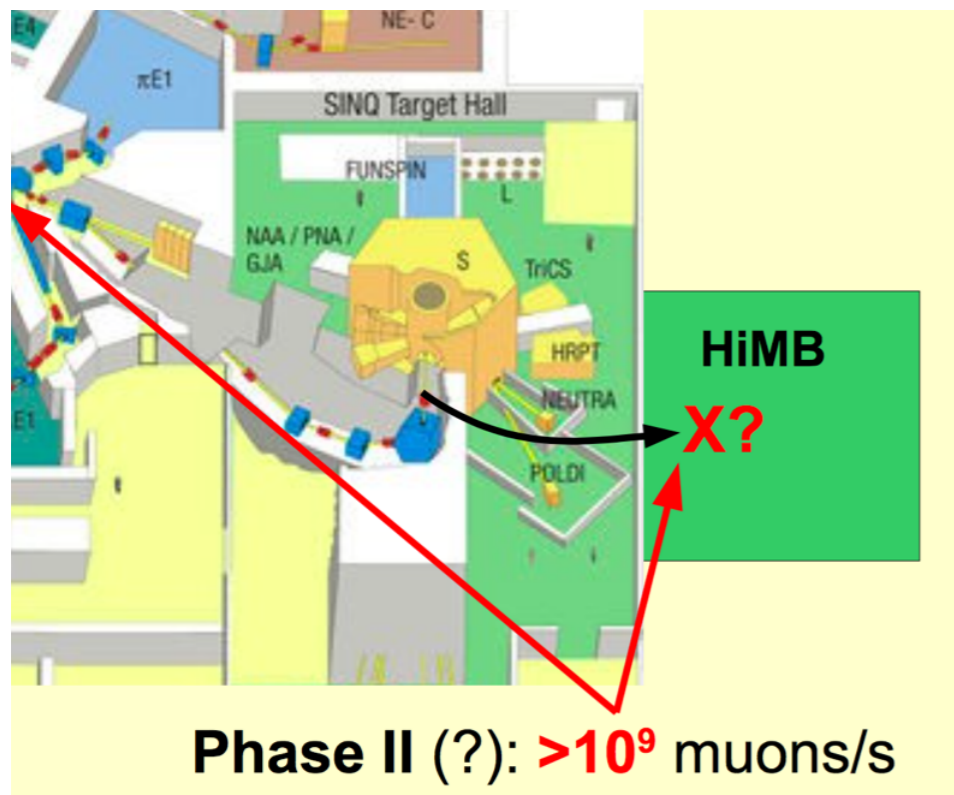
17 cm

Mu3e beam @ PSI



Phase I cyclotron

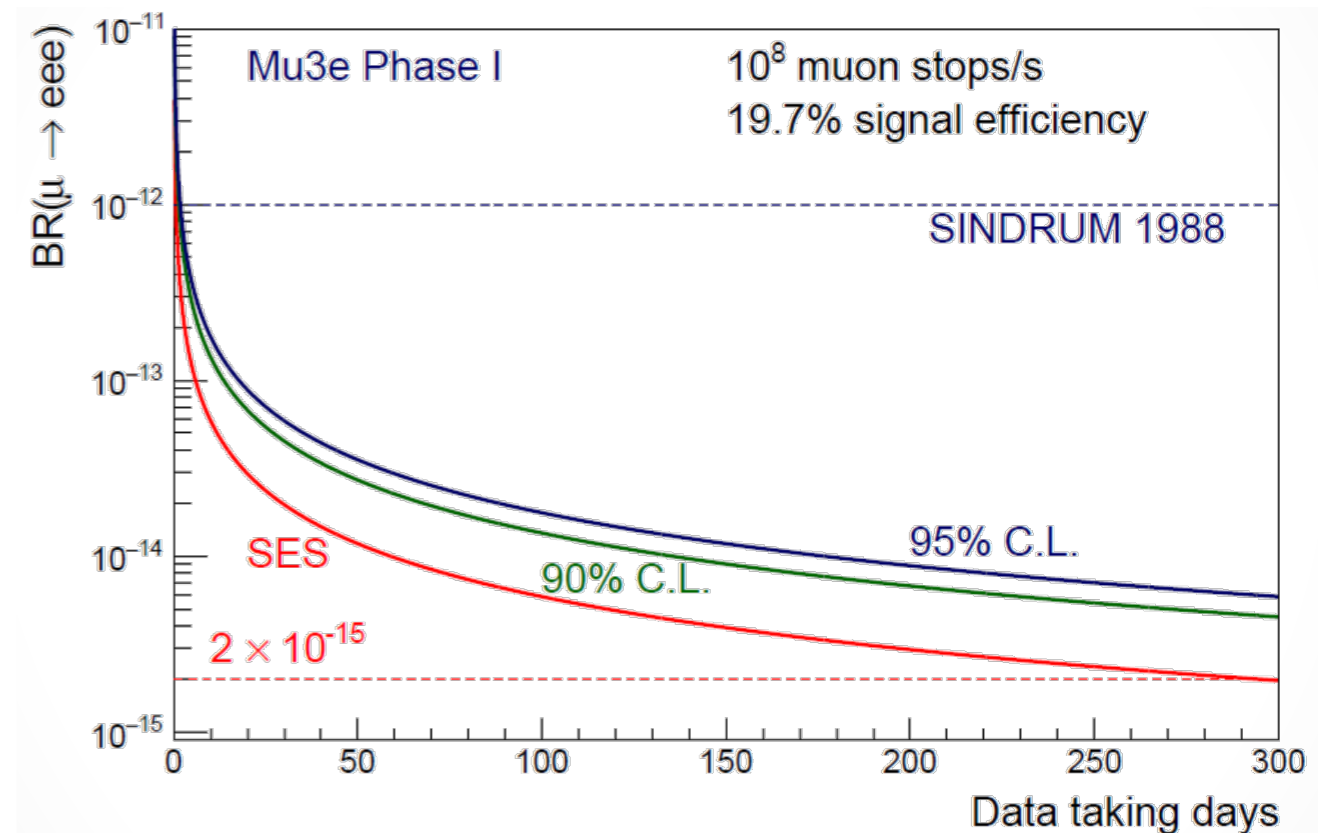
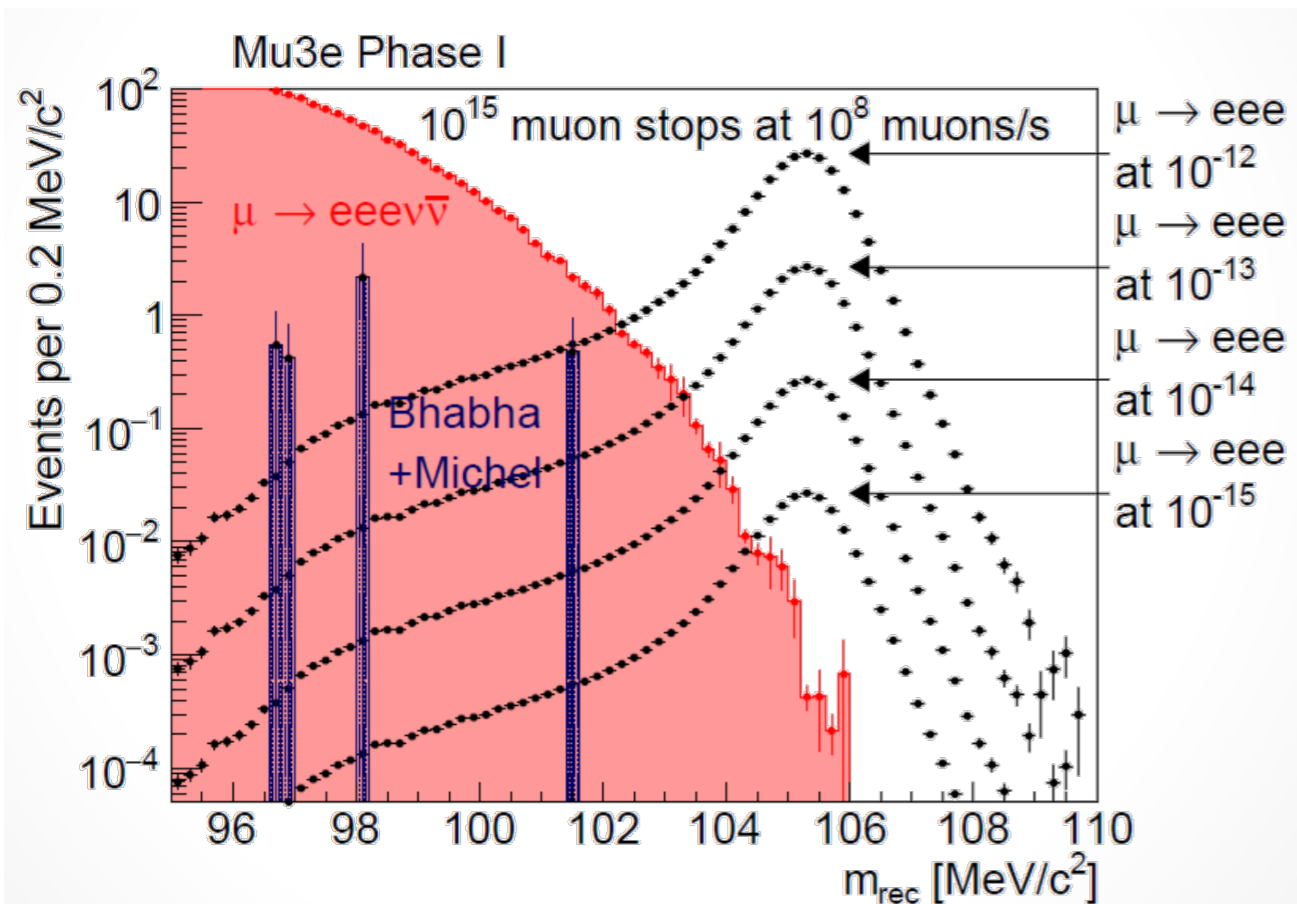
- 1.3 MW of 0.6 GeV protons
- DC muon beam using “surface” muons, $p_\mu \sim 28 \text{ MeV}/c$
- Mu3e will use $10^7 - 10^8 \mu^+/\text{s}$
- Utilizes same beam line as MEG



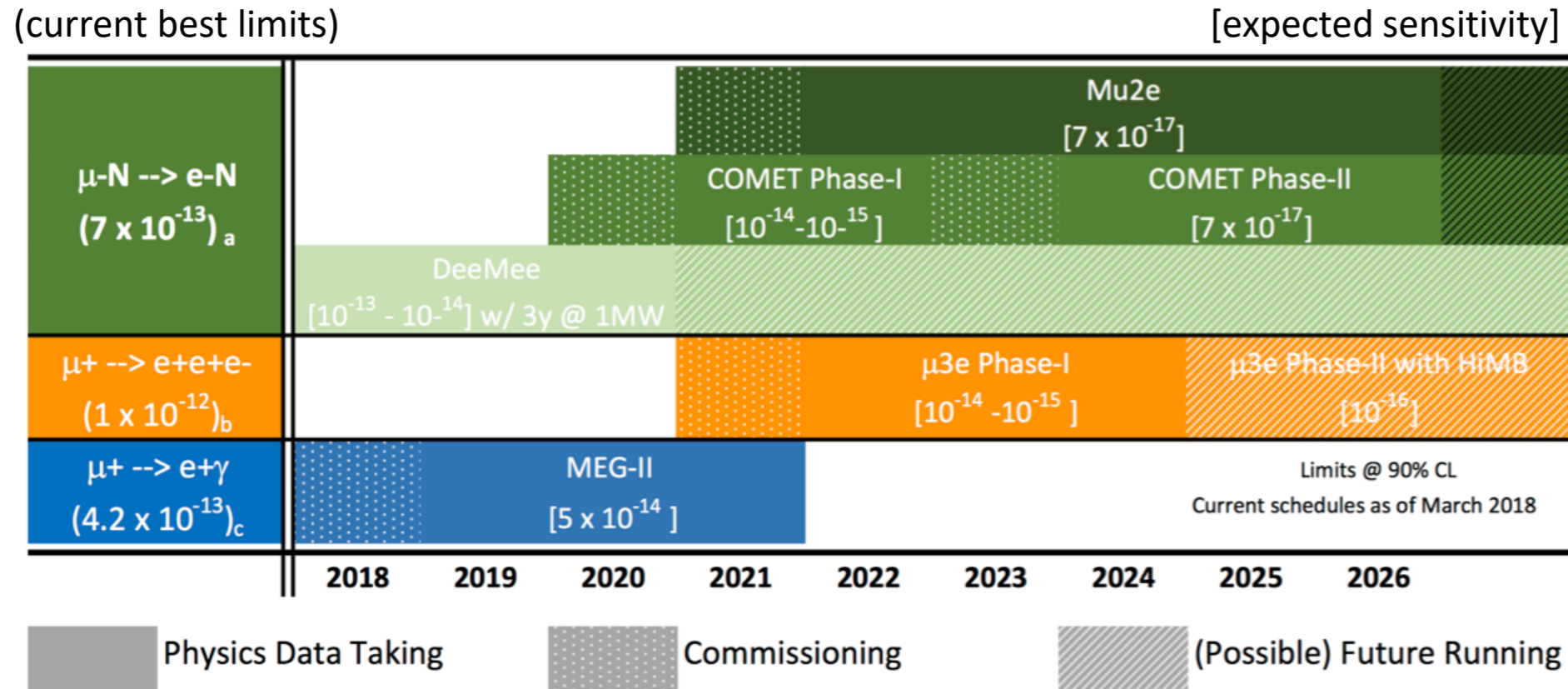
To achieve Phase-II sensitivity requires an upgraded facility at PSI:
High Intensity Muon Beam

Mu3e projections

- **2019** Magnet delivery and detector **construction**
- **2020** Installation and **commissioning** at PSI
- **2021** Data taking at up to a few **$10^8 \mu/s$**



Summary



- Exciting improvements in sensitivity of LFV
- Probe new physics up to 10000 TeV scale
- In case of null observation, further improve sensitivity with:
 - source intensity upgrade
 - detector improvements
- If signal is observed, distinguish models by studying:
 - target nuclei dependence
 - different final states
- Acknowledgements: Many thanks to Douglas Glenzinski & Robert Bernstein