

Relativistic particle scattering and Big Bang Nucleosynthesis

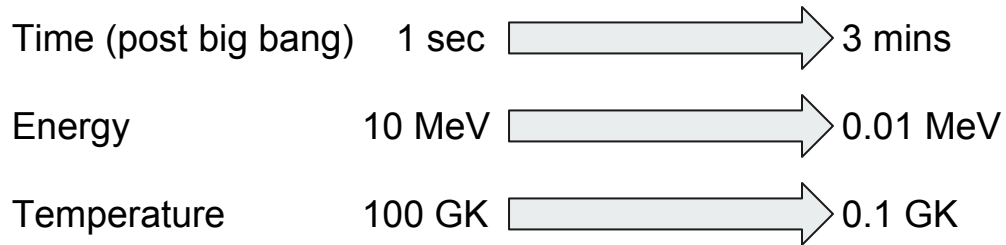
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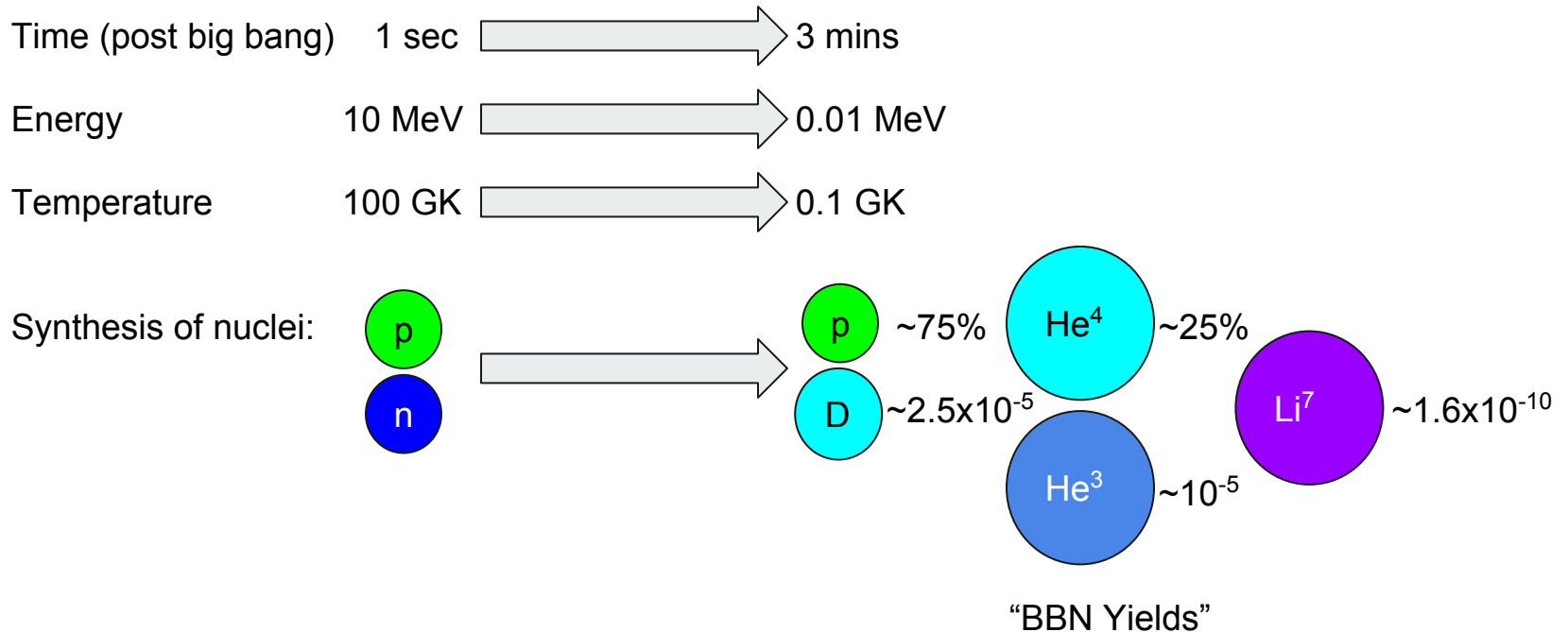
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Intro to “Big Bang Nucleosynthesis” (BBN)



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Reaction rates between two species



$$n_1 n_2 \langle \sigma(v)v \rangle = n_1 n_2 \int v \sigma(v) f(v) dv$$

Reaction rates between two species

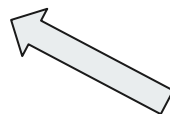

$$n_1 n_2 \langle \sigma(v)v \rangle = n_1 n_2 \int v \sigma(v) f(v) dv$$

$f(v)$: Distribution of the relative velocities of the two nuclei.

Traditionally assumed to be Maxwell-Boltzmann distribution, obtained by approximating Fermi-Dirac.

Thermalization of (charged) nuclei

- At BBN, Nuclei are surrounded by e^+e^- and photons.
- Nuclei thermalize by interacting with e^+e^-
- $f(v)$ should be influenced by these interactions
- e^+e^- are relativistic during BBN and hence follow Maxwell-Jüttner distribution (i.e. relativistic Maxwell-Boltzmann distribution)

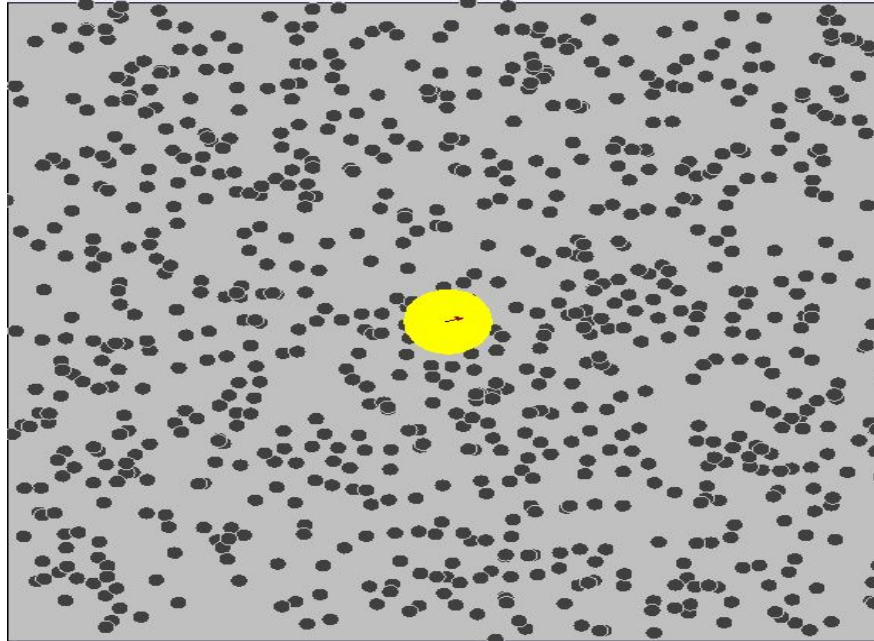


T		$\frac{n_{\pm}}{n_{\gamma}}$	$\frac{\sigma_{\pm}}{\sigma_{\gamma}}$		$\sim \frac{\Gamma_{\pm}}{n_{\gamma} \sigma_{\gamma}}$
T_9	MeV		$\sigma_{\pm} = \pi r_D^2$	$\sigma_{\pm} = \text{Mott X-sec.}$	
11.6	1	1.43	5×10^4	10^5	10^5
1.16	0.1	0.102	10^7	10^5	10^4
0.116	0.01	10^{-13}	2×10^{28}	10^{29}	10^{15}

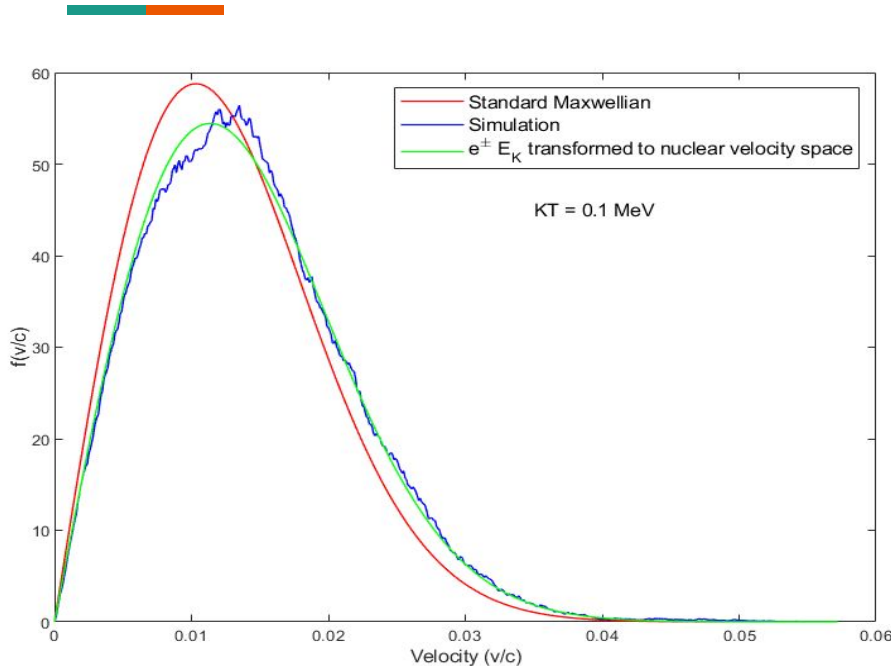
Simulated thermalization with e^+e^-



Nuclei doing random
walks by scattering off
 e^+e^-



Simulated thermalization with e^+e^-



Energy distribution for Nuclei

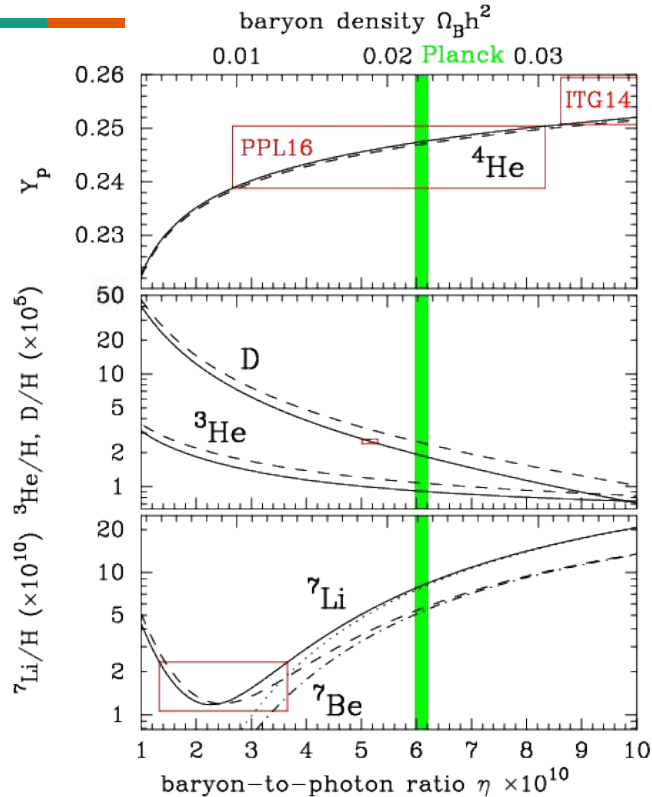
= Energy distribution of e^+e^-

= Maxwell-Jüttner distribution

Transform this M-J distribution to v-space ($f(v)$), update reaction rates and BBN yields.

Velocity distribution for Nuclei (Simulation) compared with classical M-B and e^+e^- M-J(transformed to n v-space).

BBN Yields



Unfortunately, this doesn't solve the Li^7 problem, it worsen's it. But, it is a correction to be accounted for.

Deuterium and Lithium disagree with observational constraints.

“Relativistic Electron Scattering and Big Bang Nucleosynthesis”
Sasankan, Kedia, Kusakabe, Mathews [Submitted]

Summary


 ${}^7\text{Li}$ problem \rightarrow Our research begins:

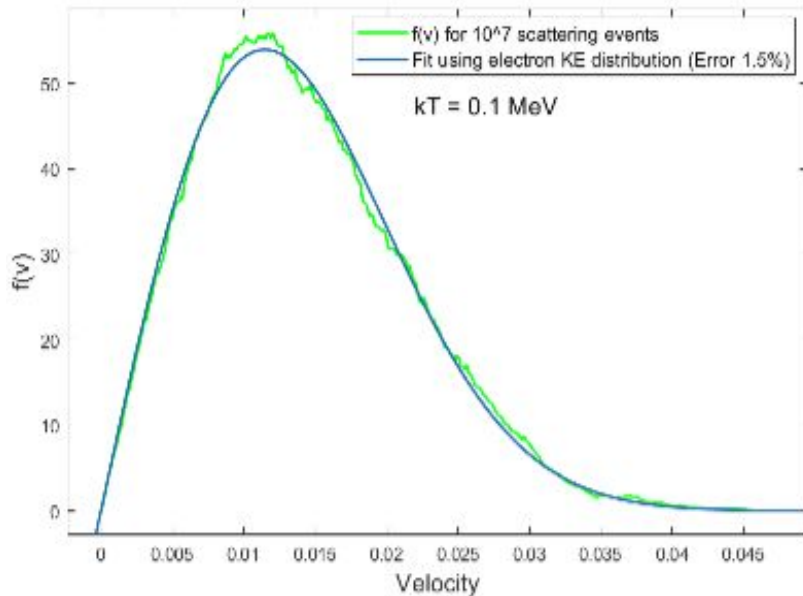
Question: How does a nucleus thermalize?

- Interacts with surroundings
 - Mostly e^+e^- , γ
 - Interacts with e^+e^-
- e^+e^- follow M-Jüttner, not M-Boltzmann
- Simulate thermalization with e^+e^-
- Observed distribution $f_{Nulcei}(E) = f_{e^+e^-}(E) = \text{M-Jüttner distribution}$
 \Rightarrow obtain $f(v) \Rightarrow$ update reaction rates \Rightarrow update BBN yields.

Lithium Problem is probably really a BBN problem

Thank you!

Velocity profile




Maxwell-Jüttner distribution

$$f(\gamma) = \left(\frac{\gamma^2 v m_e}{kT K_2(m_e c^2 / kT)} \right) \frac{1}{\exp[(E_T \pm \mu) / kT] + 1}$$

Relative velocity dist. in terms of nuclear velocity dist.

$$f^{\text{rel}}(\mathbf{v}; T) = \int d\mathbf{V} [f(\mathbf{v}_1) f(\mathbf{v}_2)]_{\mathbf{v}}$$



“Relativistic Electron Scattering and Big Bang Nucleosynthesis” Sasankan, Kedia, Kusakabe, Mathews, PRL[Submitted]. ArXiv preprint : <https://arxiv.org/abs/1810.05976>