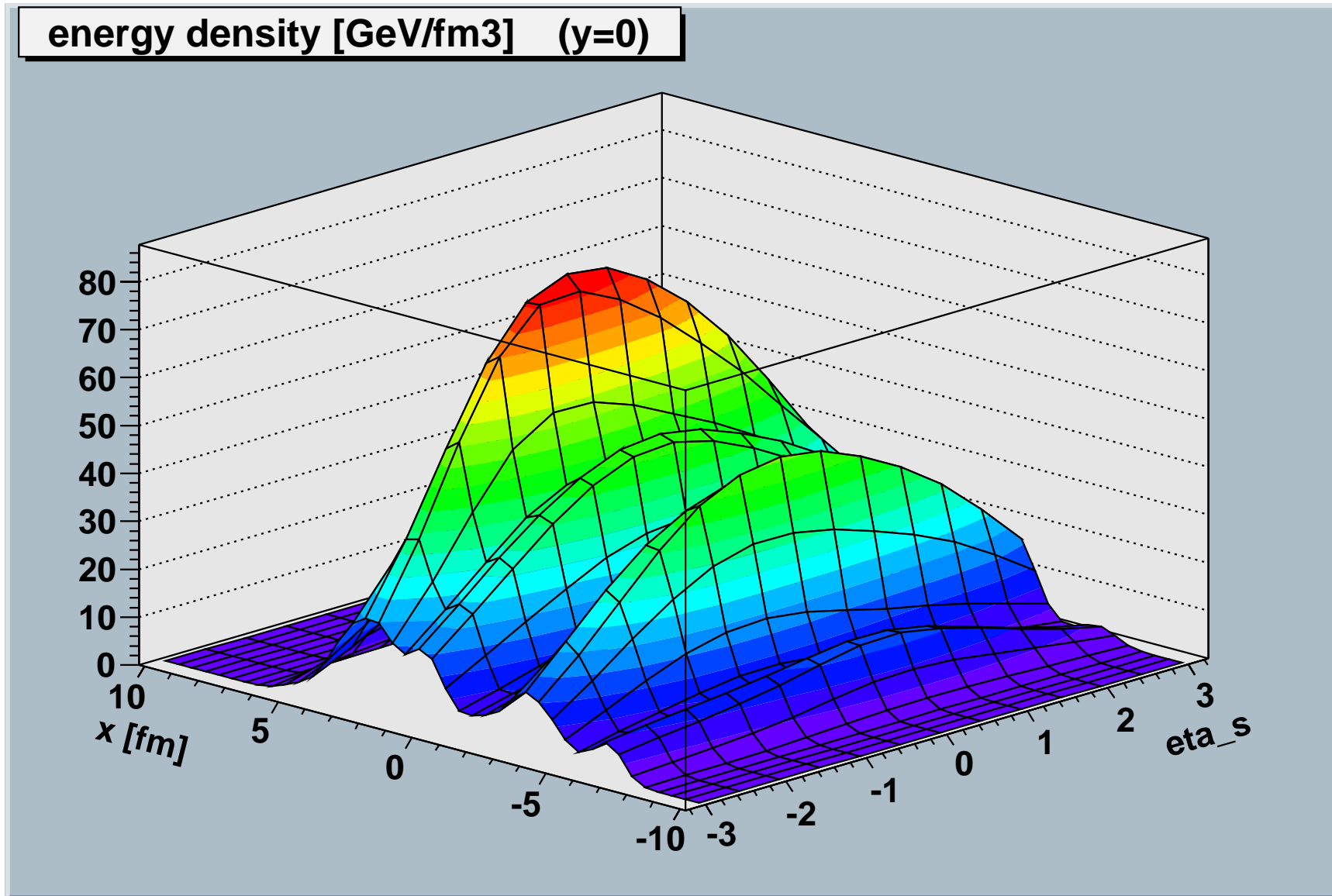


# Multiple Scattering and hydrodynamical evolution in pp@LHC

**Klaus Werner**  
<werner@subatech.in2p3.fr>

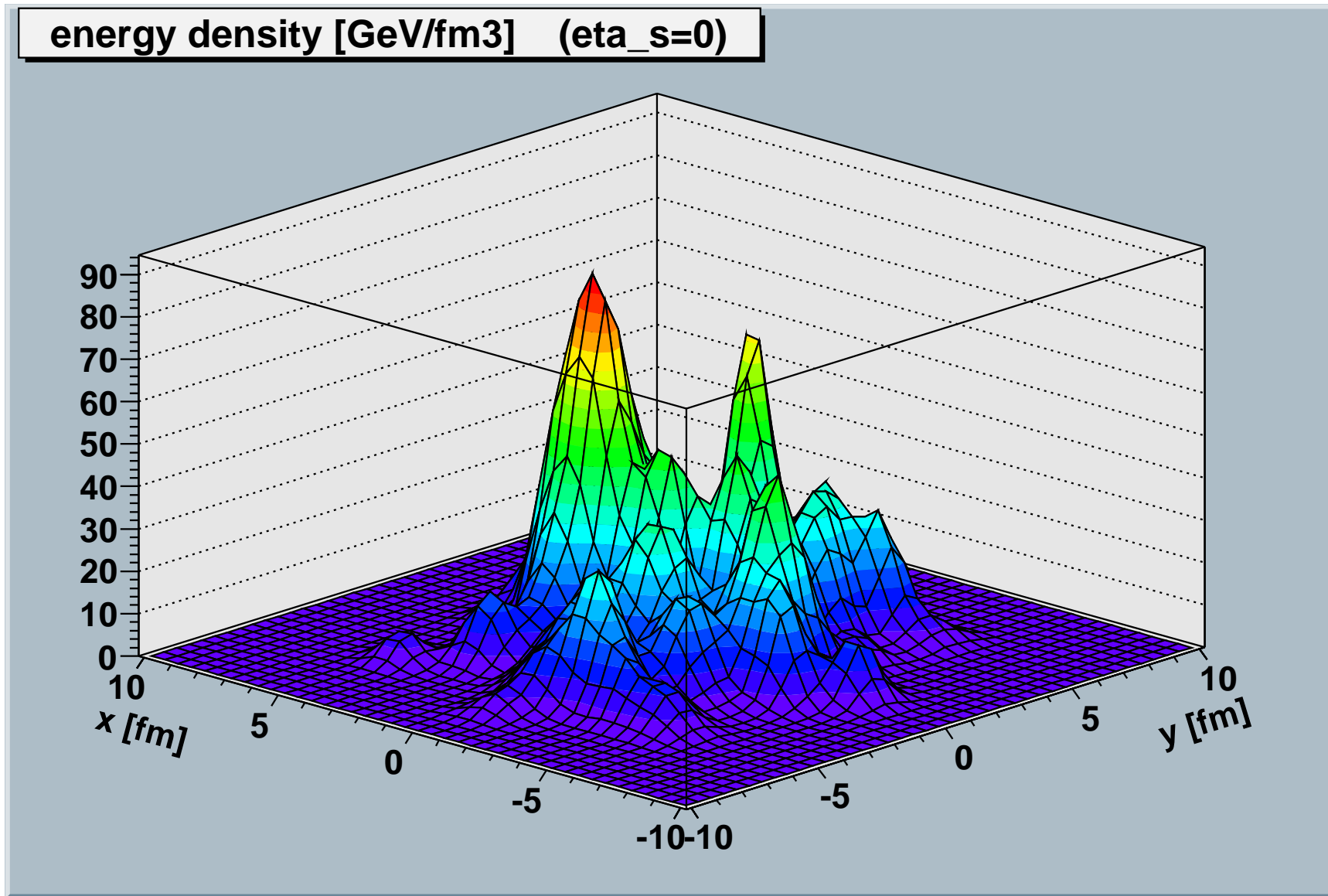
in collaboration with T. Pierog, S. Porteboeuf, T. Hirano, Y. Karpenko, M. Bleicher, S. Haussler

# EPOS energy density (0.6fm/c) central AuAu



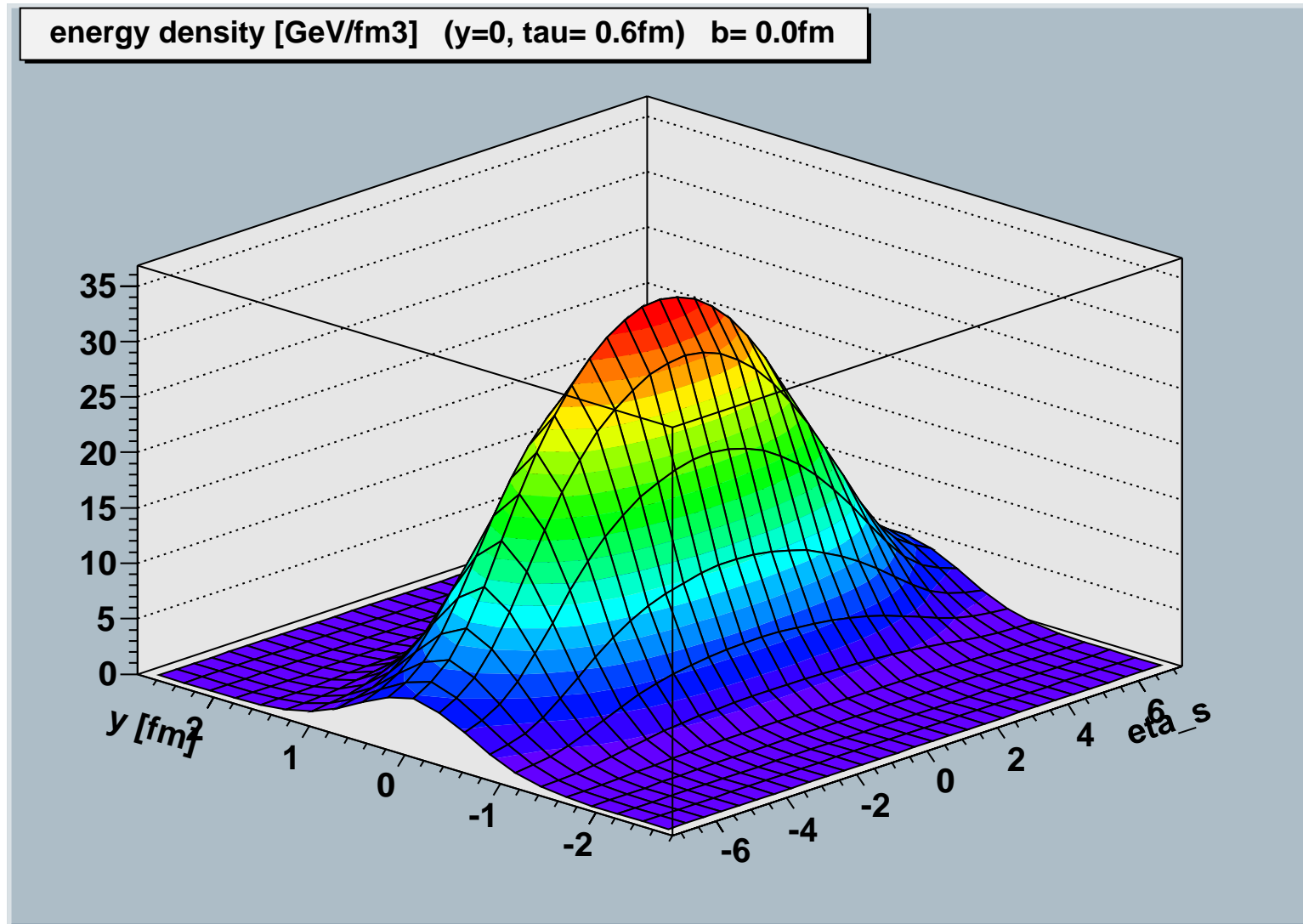
typically several ridges

... in transverse direction



several peaks ( $\hat{=}$  ridges in  $\eta - x$ )

# EPOS energy density (0.6fm/c) “central” pp



single ridge

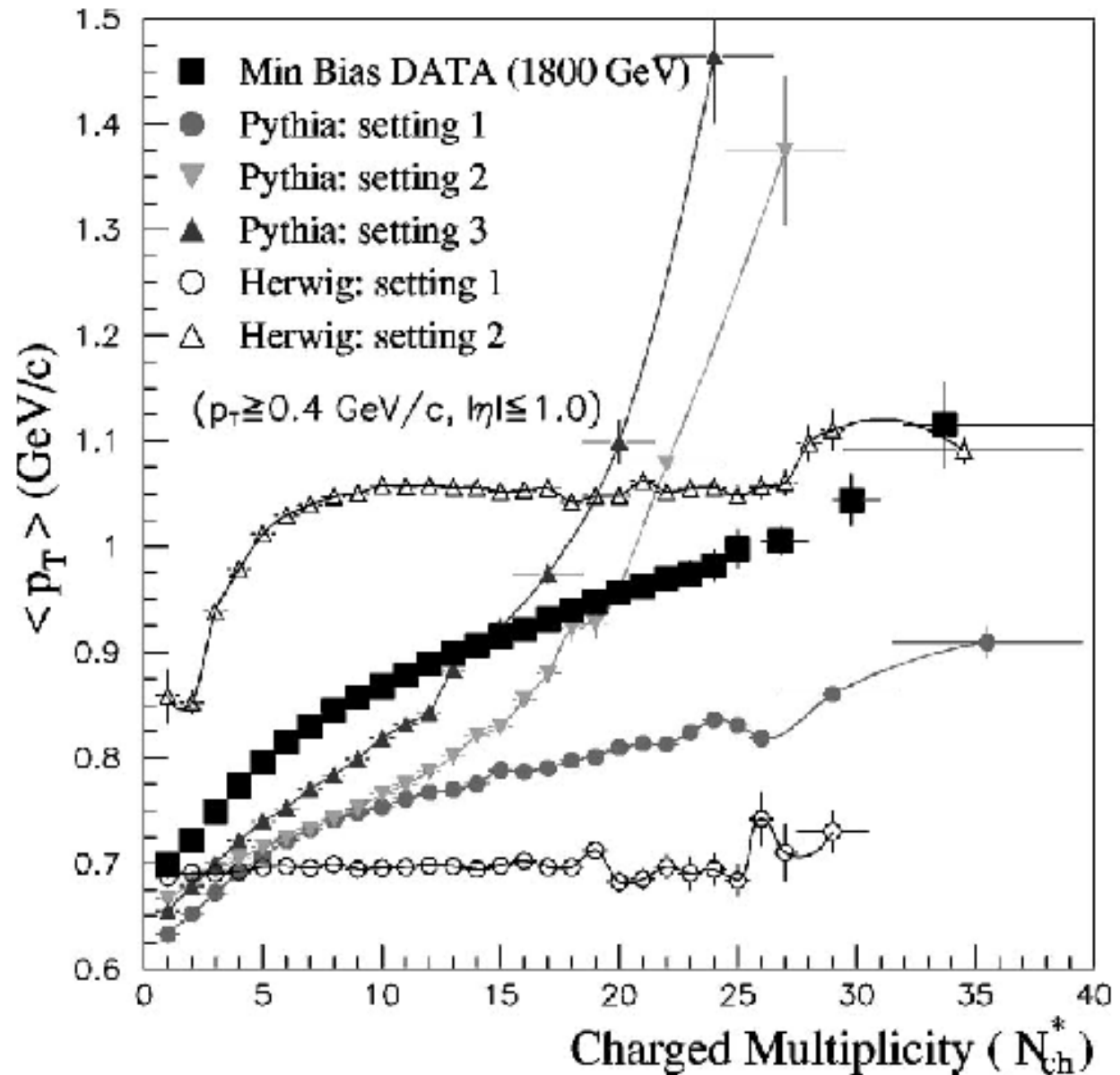
- ▷ Size of the fluctuations in AuAu small, similar to what will be achieved in pp@LHC
- ▷ If hydro is applicable for AuAu@RHIC, it should be so for pp@LHC, if one reaches high energy densities...
- ▷ Here, **multiple scattering** will help !!

# Multiple scattering in pp

pp@1800GeV  
data: CDF

Phys. Rev. D  
Vol 65,  
072005 (2002)

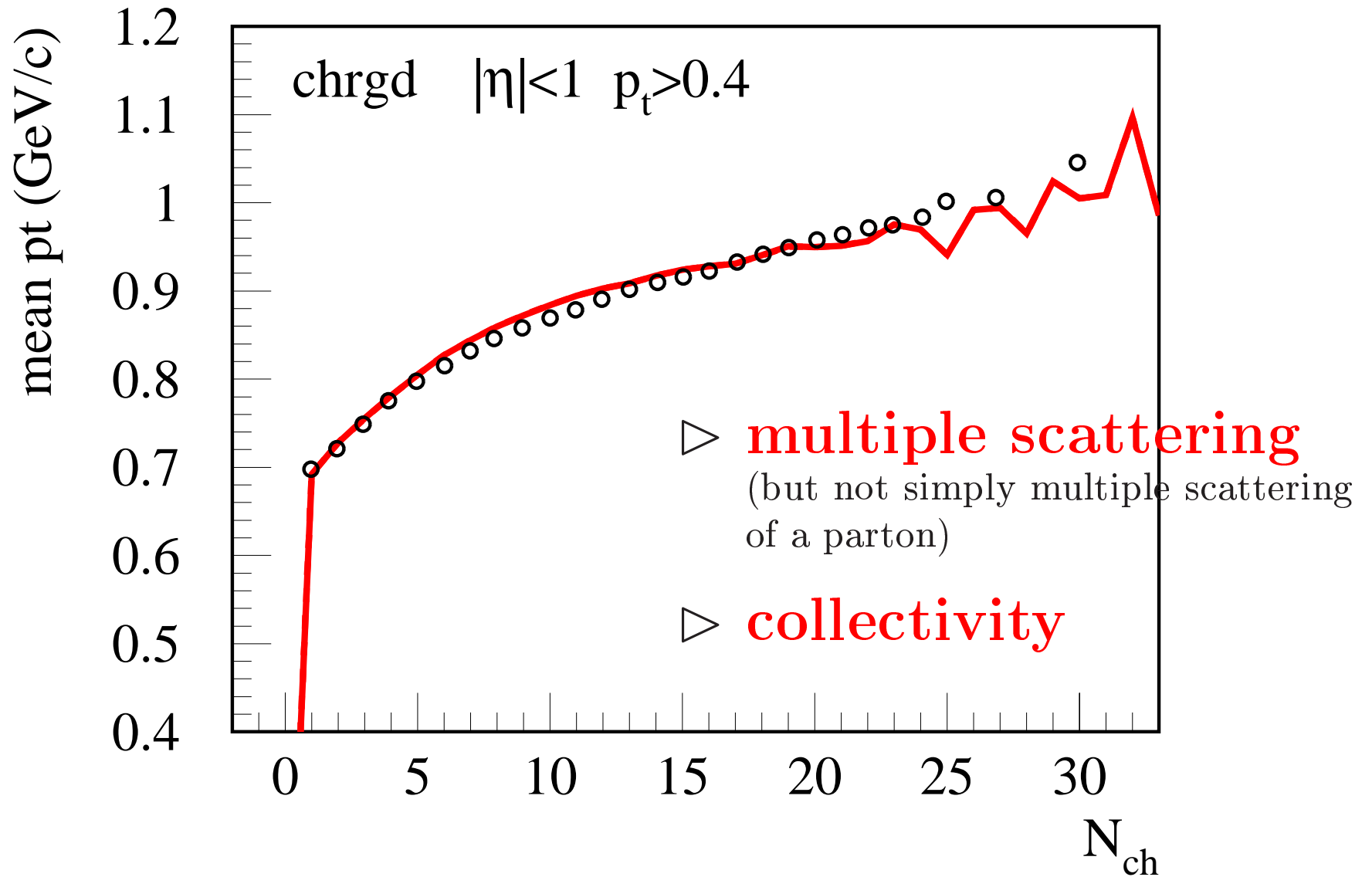
recent activities in  
Pythia community



pp@1800GeV

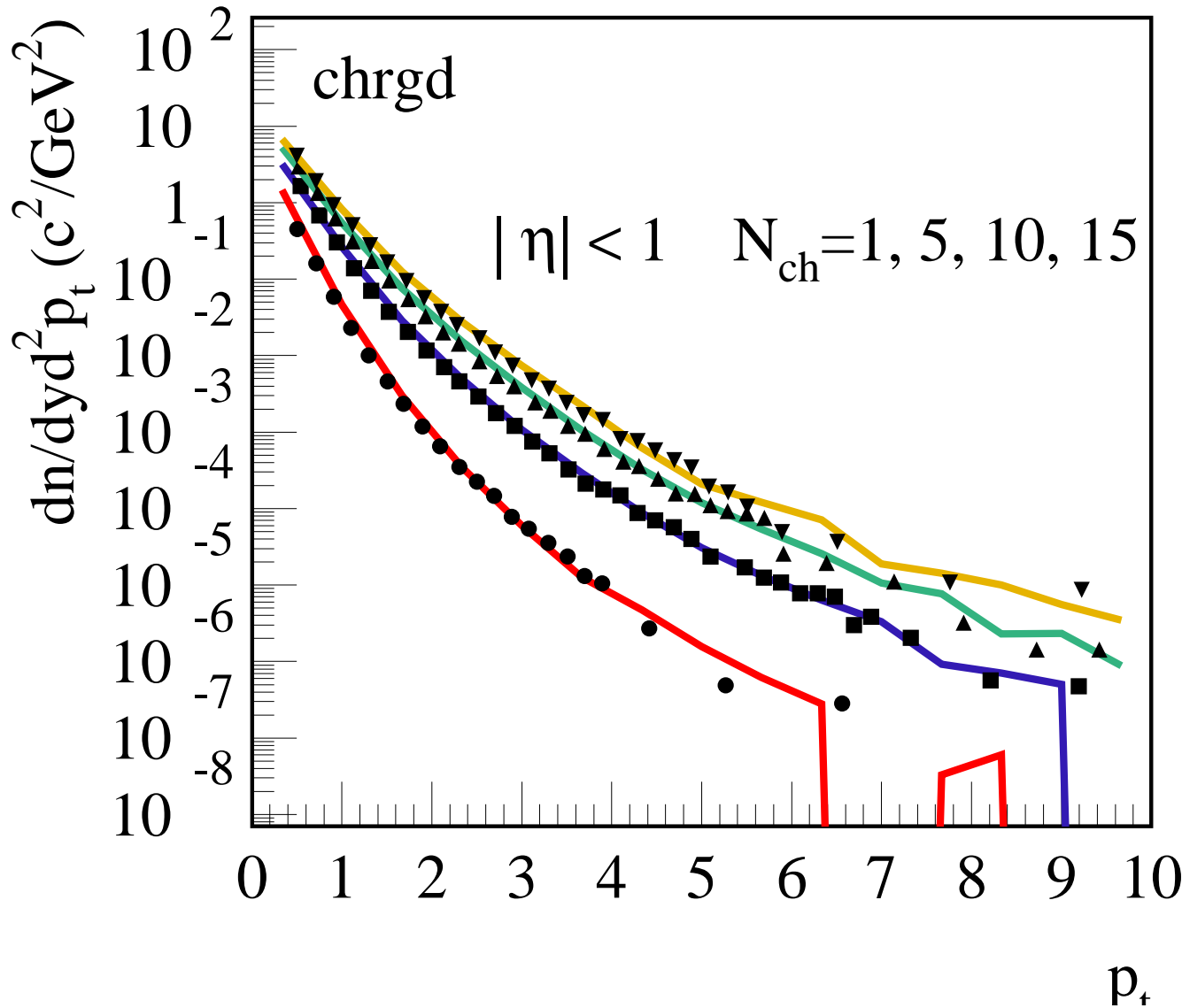
points: CDF

curve EPOS





pp@1800GeV, points: CDF, curves EPOS



In EPOS:

high multiplicity  
related to multiple  
scattering

but multiple scatter-  
ing also favours hard  
scatterings — just  
higher probability

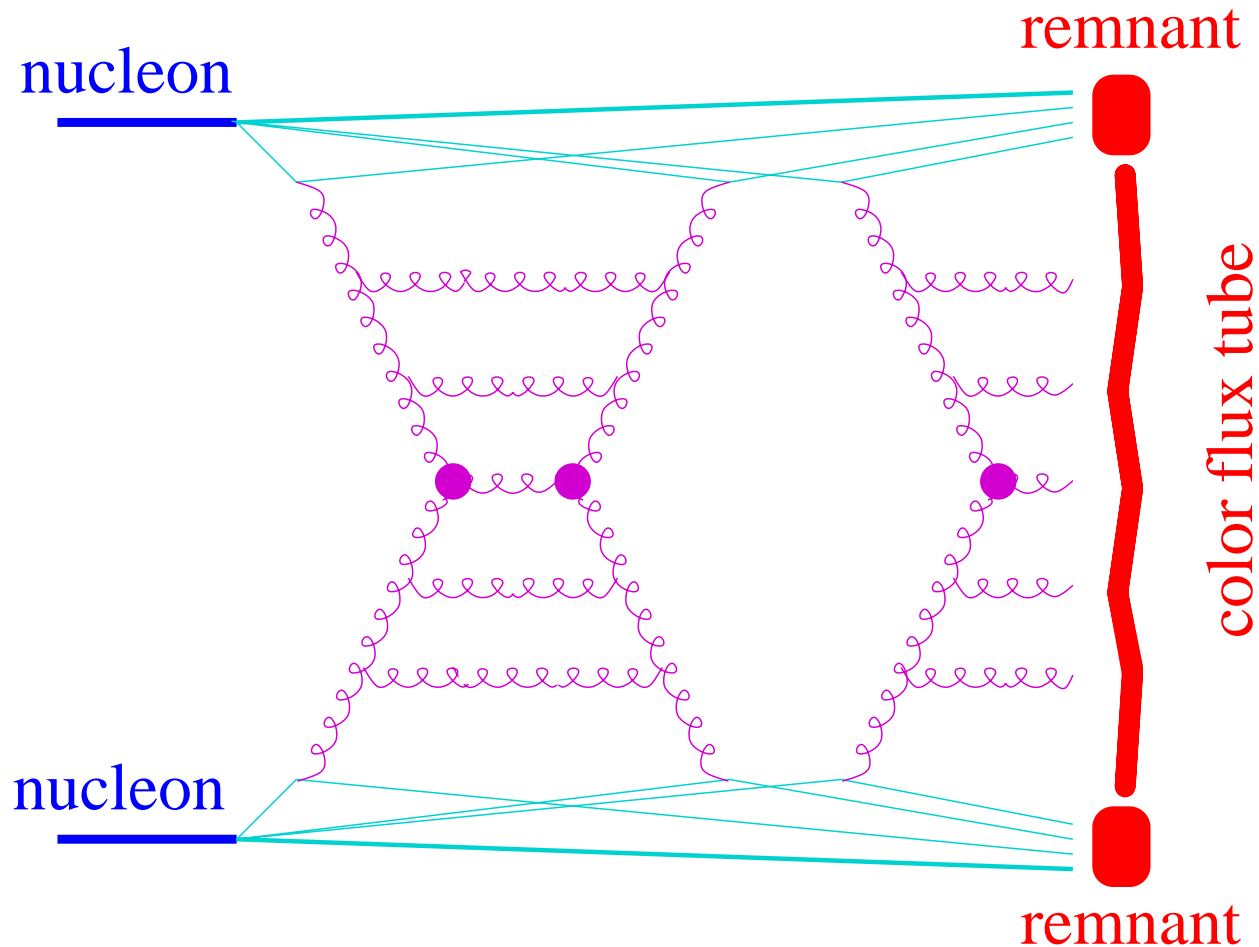
## EPOS: multiple exchange of ladders

Multiple scattering  
with energy sharing

Squaring graphs  
→ cut diagrams  
→ cutting rule techniques

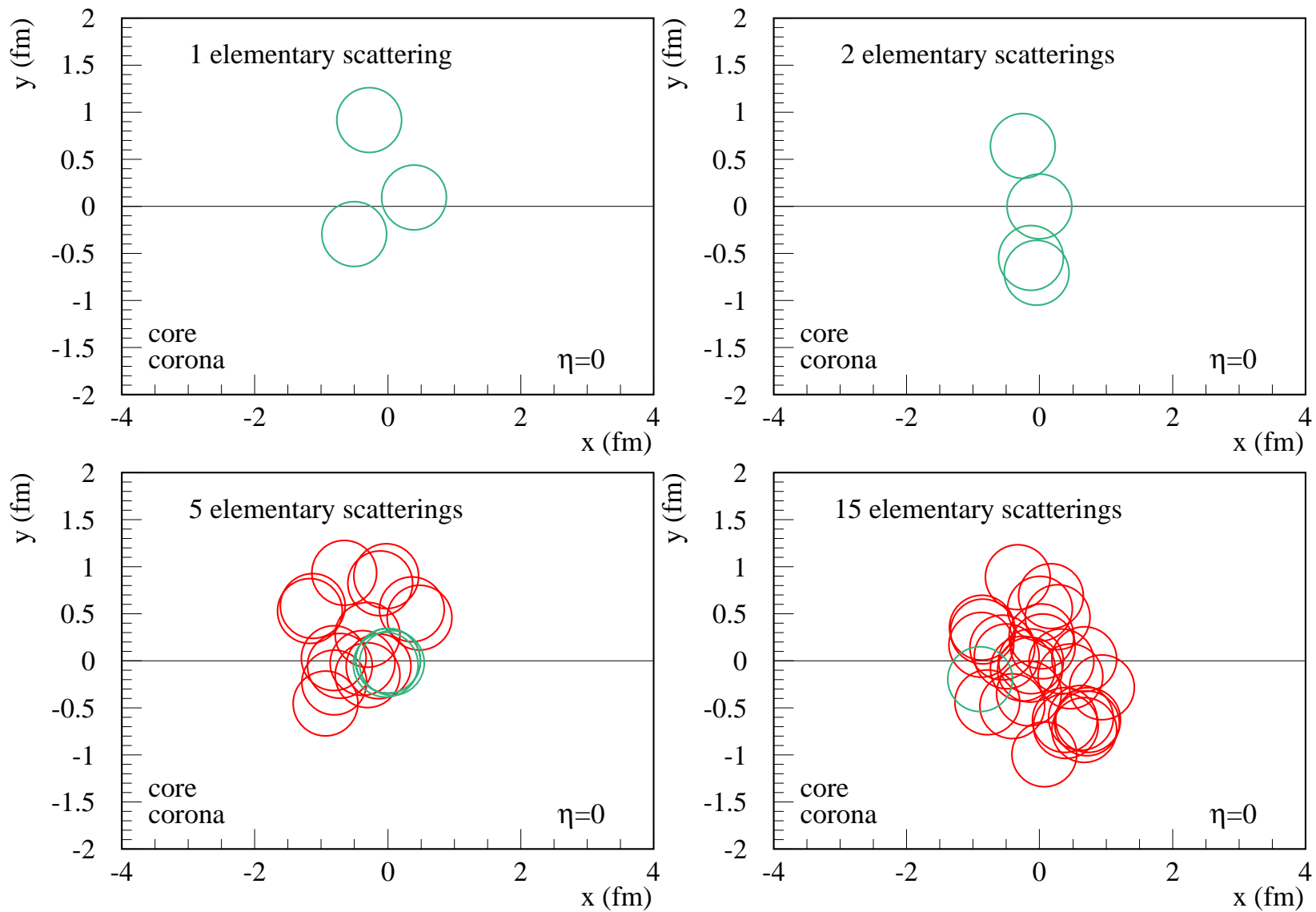
Energy sharing:  
Markov chain  
techniques

Particle production  
from **remnants** and **flux tube** decays (→strings)



Parton-based Gribov-Regge Theory, H. J. Drescher, M. Hladik, S. Ostapchenko, T. Pierog, and K. Werner, Phys. Rept. 350 (2001) 93-289; Parton ladder splitting and the rapidity dependence of  $p_t$  spectra in dAu collisions at RHIC, K. Werner, F.M. Liu, T. Pierog, Phys. Rev. C 74, 044902 (2006)

# Core-corona approach in pp



Core-corona in AA:

- ▷ separation of volume into (central) core and (peripheral) corona part

Completely different in pp:

- ▷ separation of events into two classes: core and corona events

- ▷ Energy density comparable to AuAu@RHIC
- ▷ Size comparable to size of fluctuations in AuAu@RHIC
- ▷ we propose (and we do) for pp:  
hydrodynamical expansion + statistical decay  
based on EPOS flux tube initial conditions –  
**event-by-event**

## Only core used to compute initial conditions for hydrodynamical evolution

at  $\tau_0$  : from space and momentum four-vectors of string segments, we get

- ▷ energy density  $\varepsilon(\vec{x})$ ,
- ▷ flow velocity  $\vec{v}(\vec{x})$
- ▷ net flavor densities  $f(\vec{x})$

H.J. Drescher, S. Ostapchenko,  
 T. Pierog, and K.Werner,  
 hep-ph/0011219,  
 Phys.Rev.C65:054902,2002

$$T^{\mu\nu} = \frac{1}{\Delta V} \sum_{i \in \Delta V} \frac{p_i^\mu p_i^\nu}{p_i^0}$$

$$N_q^\mu = \frac{1}{\Delta V} \sum_{i \in \Delta V} \frac{p_i^\mu}{p_i^0} q_i$$

with

$$p = \int_A^B \left\{ \frac{\partial X(r, t)}{\partial t} dr + \frac{\partial X(r, t)}{\partial r} dt \right\}$$

$$X(r, t) = X_0 + \frac{1}{2} \left[ \int_{r-t}^{r+t} g(\xi) d\xi \right]$$

$A, B$ : two neighboring points on  $X$

$$g(r) = v_k \quad \text{for } r_{k-1} \leq r \leq r_k, \quad 1 \leq k \leq n$$

$$v_k = p_k / p_k^0, \quad r_k = p_k^0 / \kappa$$

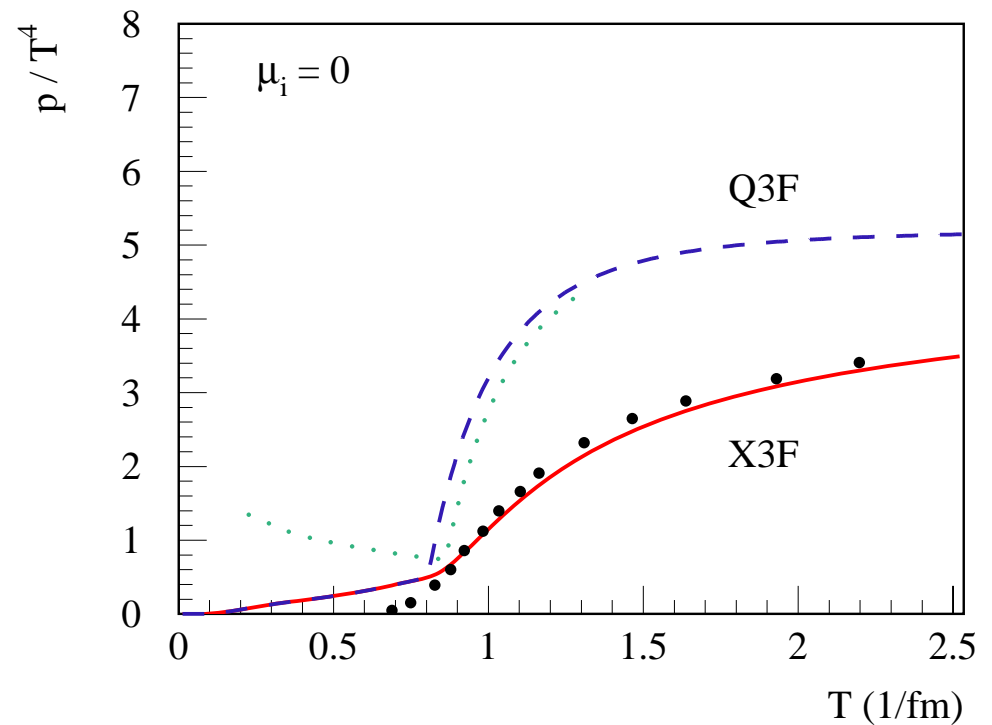
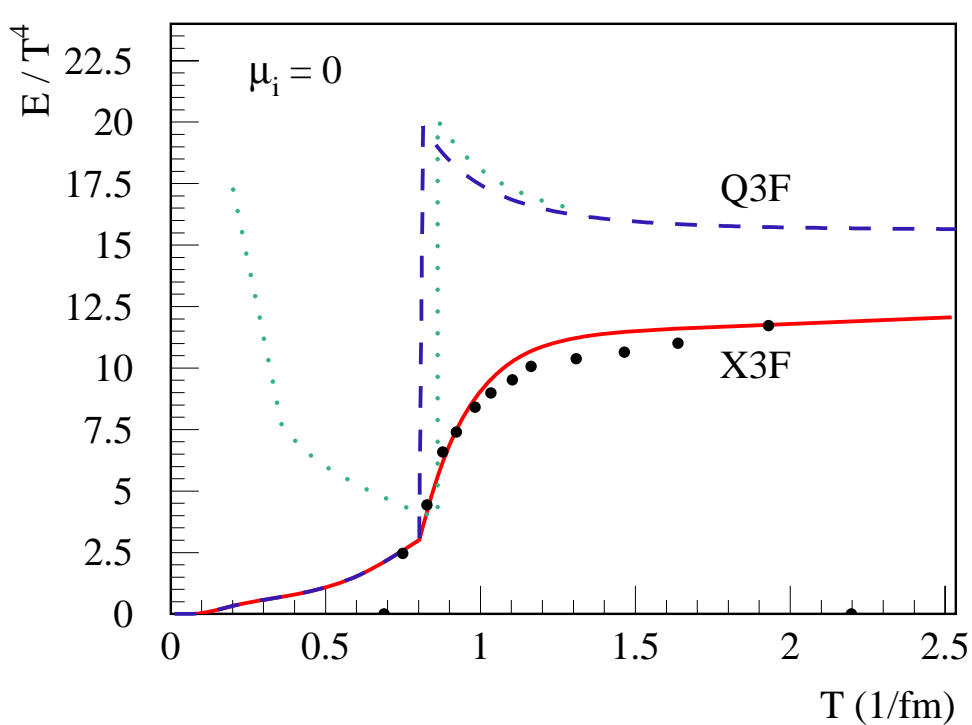
$p_k$  = parton four-momentum

## Hydro code - Yuri Karpenko, Kiev & Nantes (unpublished)

- ▷ C++ code, coupled directly to EPOS
- ▷ Code based on Godunov method: introducing finite cells and computing fluxes between cells using the (approximate) Riemann problem solution for each cell boundary.
- ▷ Use relativistic HLLE solver to solve Riemann problems
- ▷ To achieve more accuracy in time: predictor-corrector scheme is used for the second order of accuracy in time, i.e. the numerical error is  $O(dt^3)$ , instead of  $O(dt^2)$
- ▷ To achieve more accuracy in space : to achieve the second order scheme, the linear distributions of quantities (conservative variables) inside cells are used. The conservative quantities are  $(e + p * v^2)/(1 - v^2)$ ,  $(e + p) * v/(1 - v^2)$  .
- ▷ The code is written in hyperbolic coordinates

**EoS:** Massless quarks and gluons + bag, hadron resonance gas

- ▷ “Hirano” : PCE,  $\mu_B = \mu_S = \mu_Q = 0$
- ▷ “Q3F”: 1st order PT, excl volume correction,  $\mu_B, \mu_S, \mu_Q$  considered, parameters as in Spherio
- ▷ “X3F” crossover” :  $p = p_Q + \lambda(p_H - p_Q)$ ,  $\lambda = \exp(-\frac{T-T_c}{\delta})\theta(T-T_c) + \theta(T_c-T)$



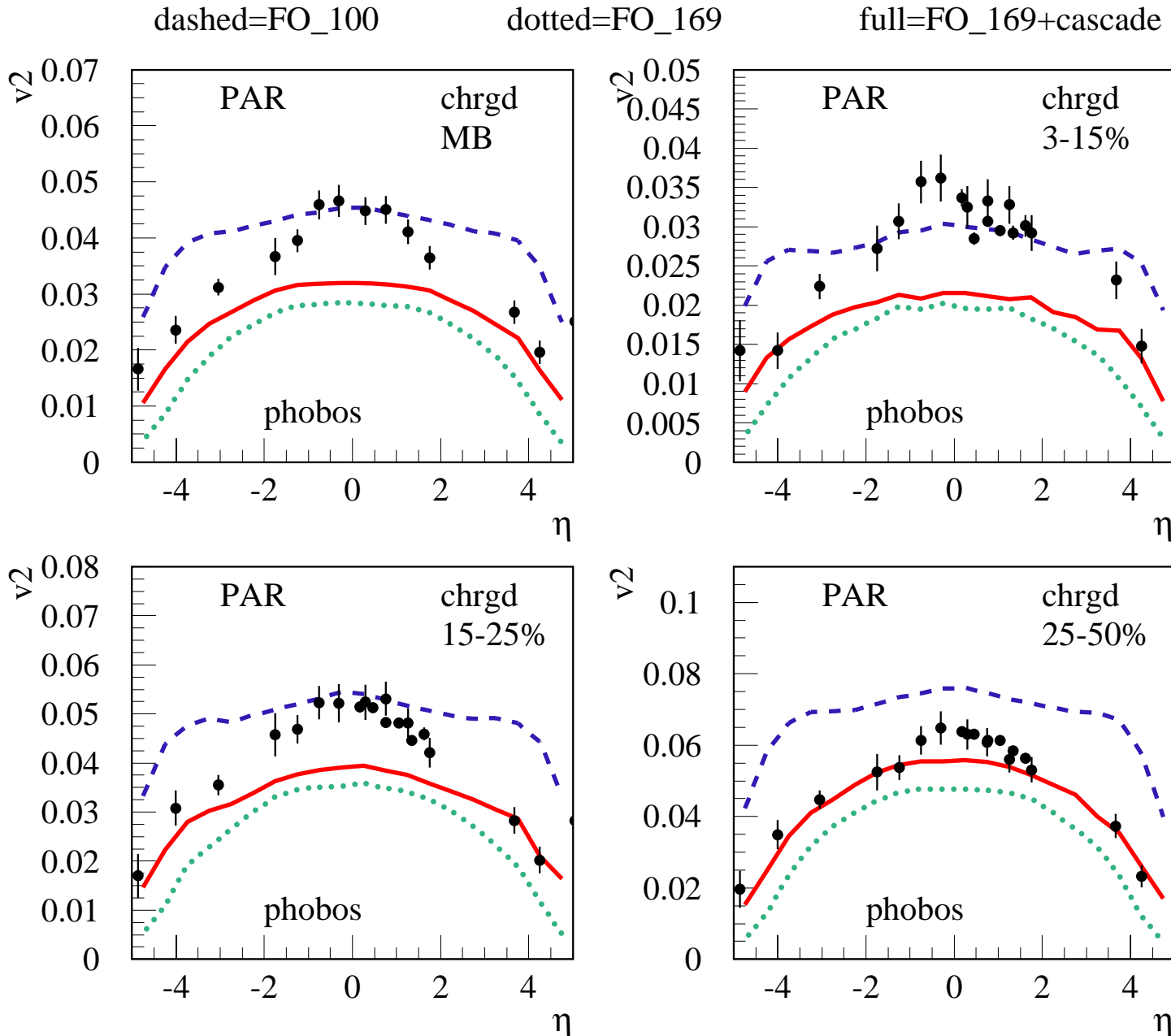


# Checking hydro procedures against AuAu@RHIC

Understand what observables are affected  
by the different elements:

- ▷ flux-tube initial condition
- ▷ core-corona procedure
- ▷ three flavor cross-over EoS
- ▷ EbE treatment
- ▷ hadronic FS cascade
- ▷ hadron table
- ▷ not considered: viscosity, initial flow

# Elliptical flow *(Hirano initial condition & PCE EoS)*



dashed:  
pure hydro, FO  
at 100 MeV

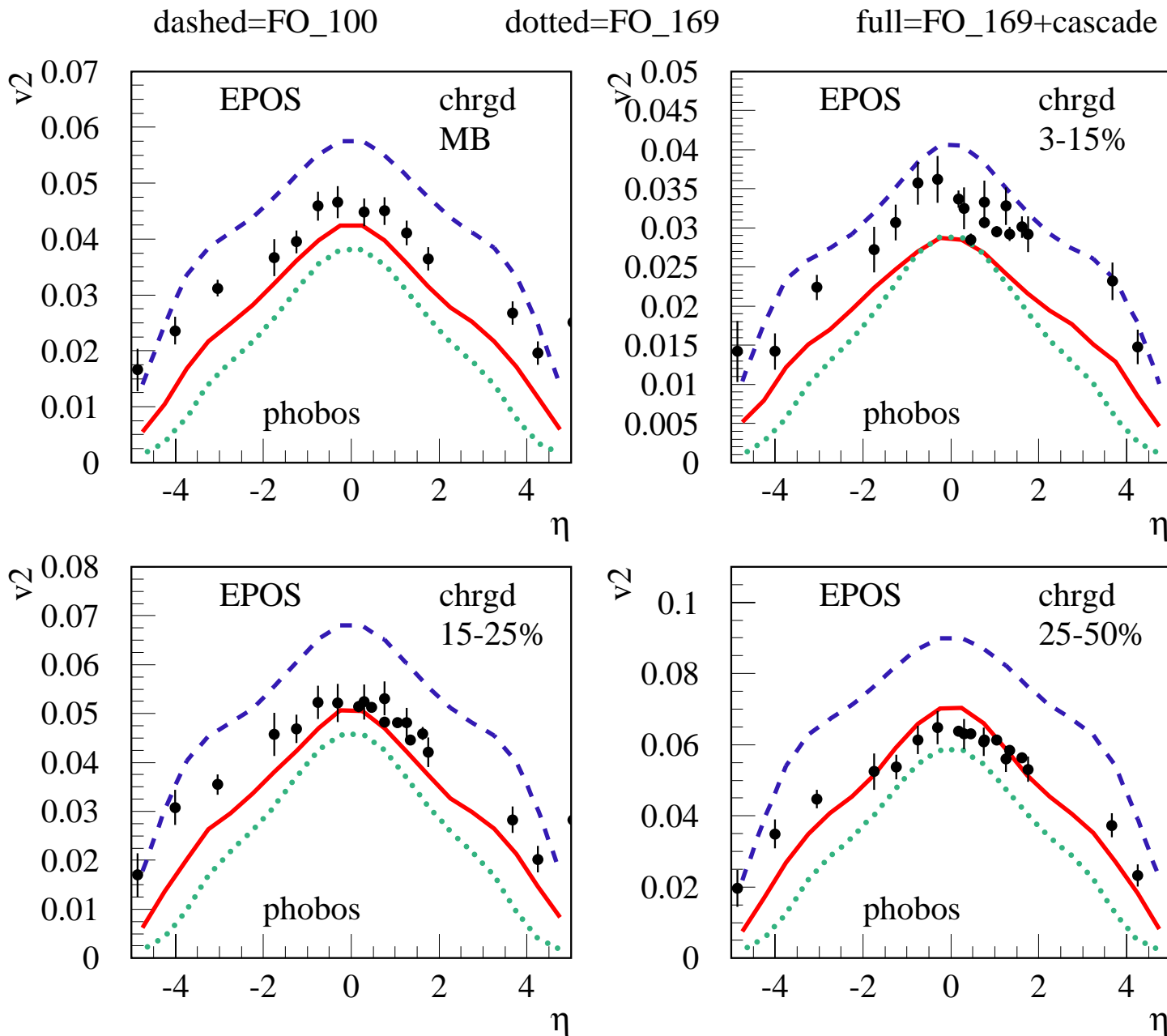
dotted:  
pure hydro, FO  
at 169 MeV.

full:  
hydro, FO at 169  
MeV, + hadronic  
cascade

(UrQMD in  
collaboration  
with S.Haussler,  
M.Bleicher, S.  
Porteboeuf)

$T_c = 170\text{MeV}$

# Elliptical flow *(EPOS initial condition, only core)*



dashed:  
pure hydro, FO  
at 100 MeV

dotted:  
pure hydro, FO  
at 169 MeV.

full:  
hydro, FO at 169  
MeV, + hadronic  
cascade

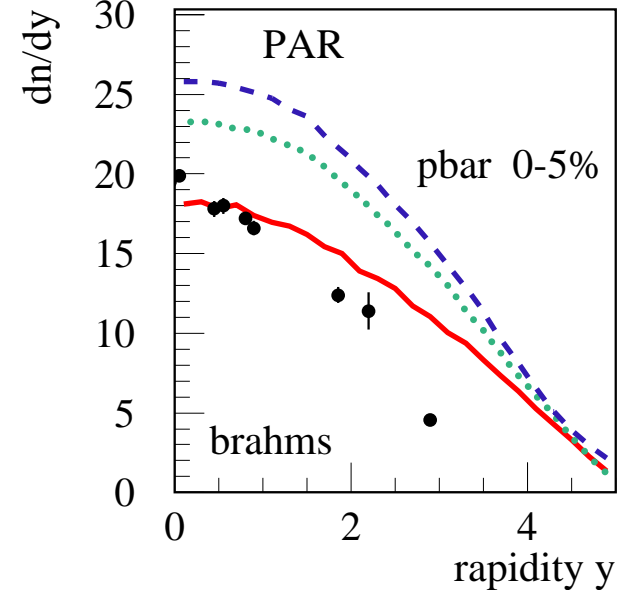
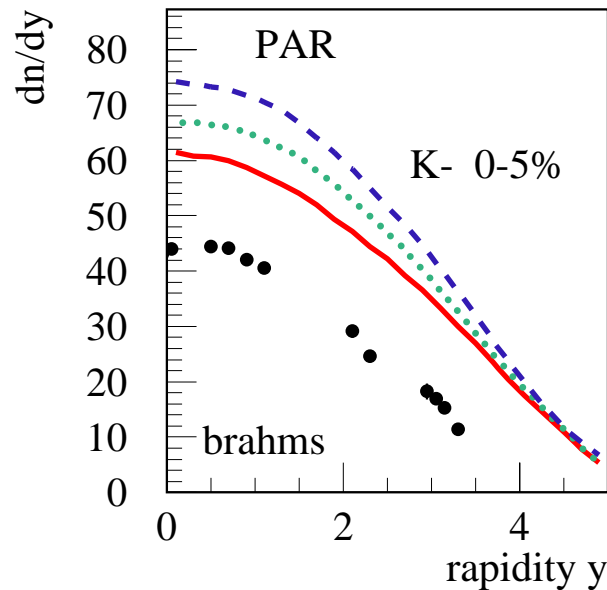
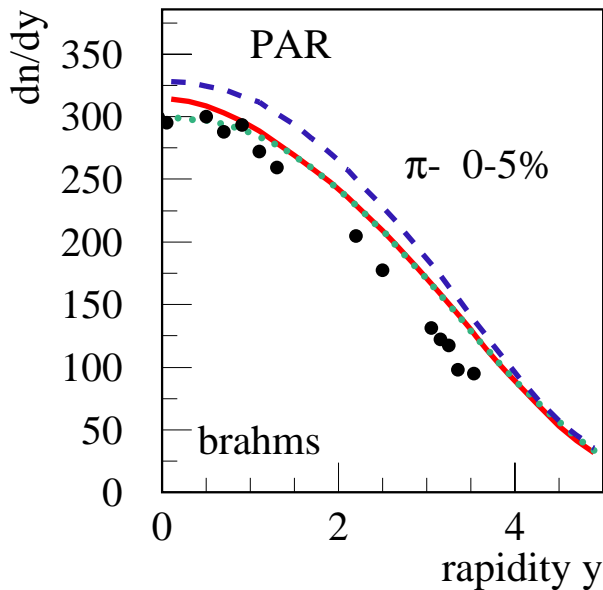
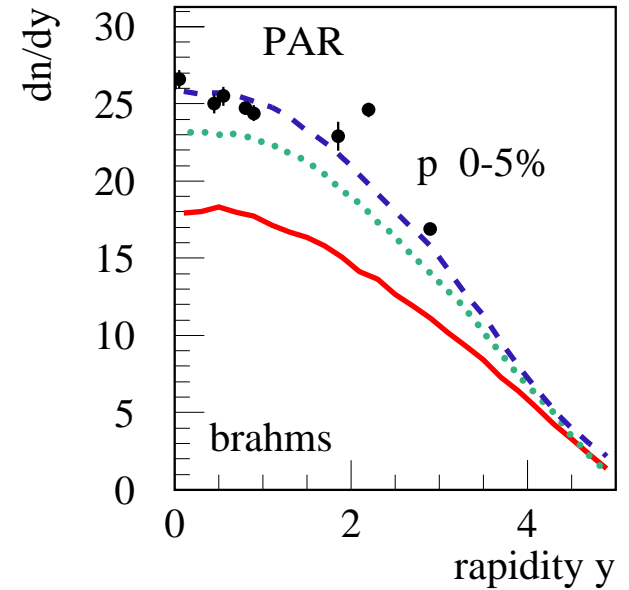
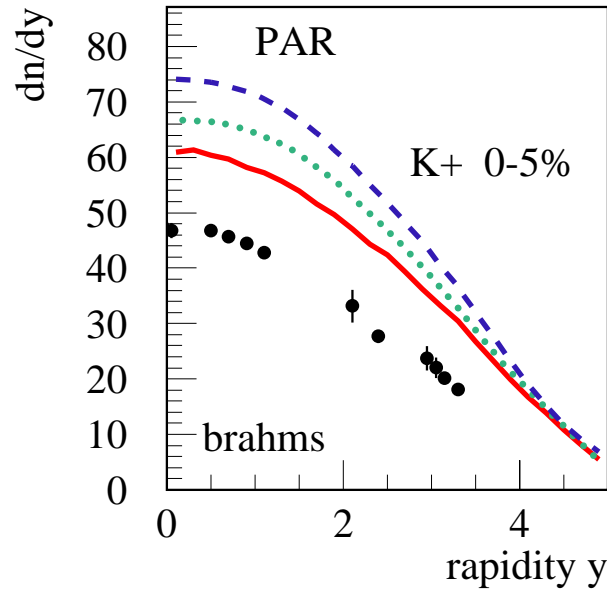
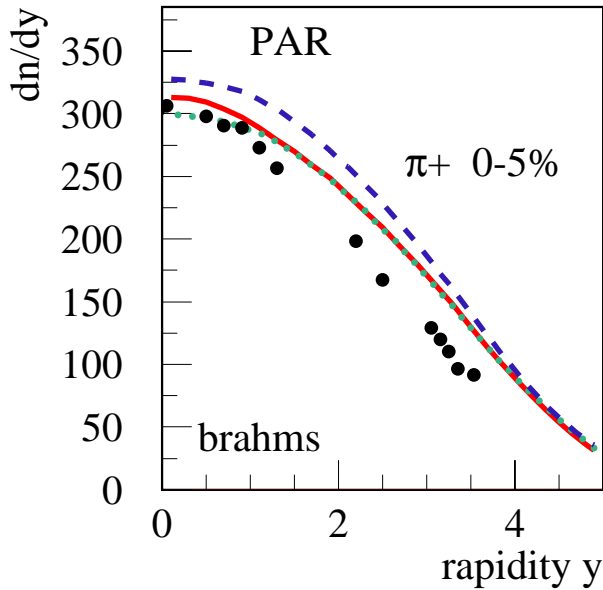
EPOS here means  
pure hydro, no  
corona

# Yields *(Hirano initial cond & PCE EoS) $\approx$ EPOS*

dashed=FO\_100

dotted=FO\_169

full=FO\_169+cascade

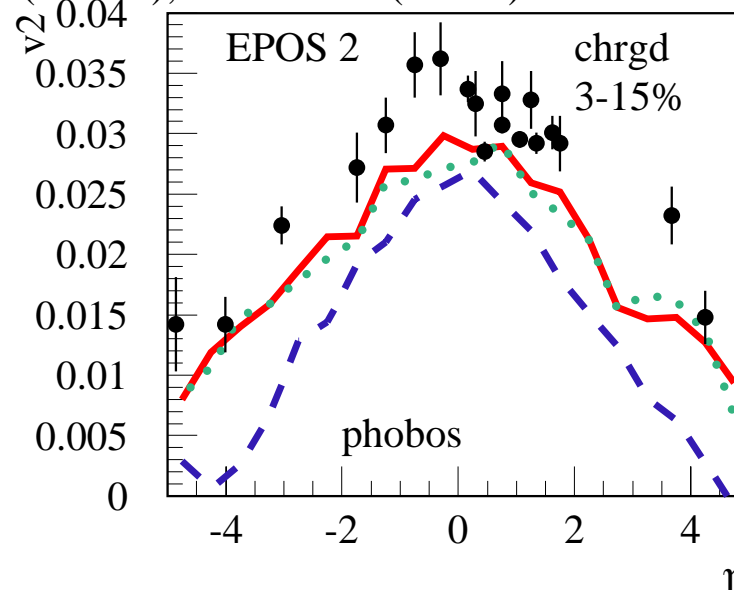
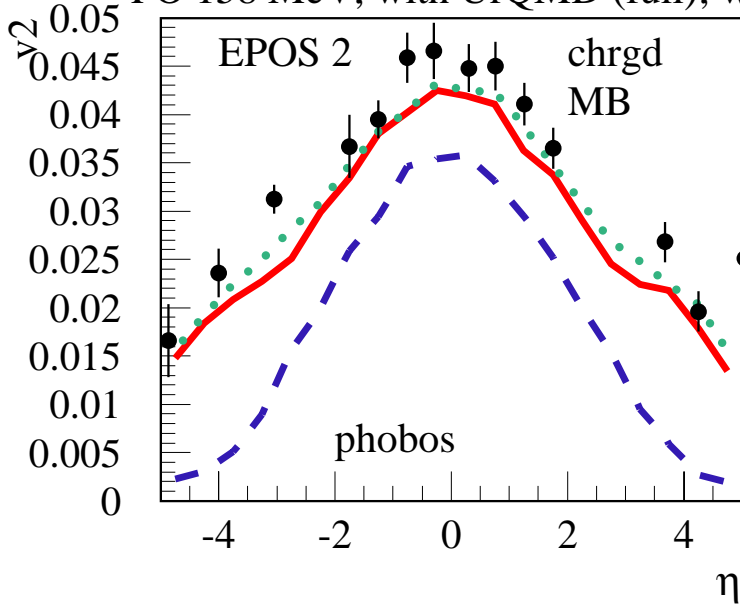


In the following:

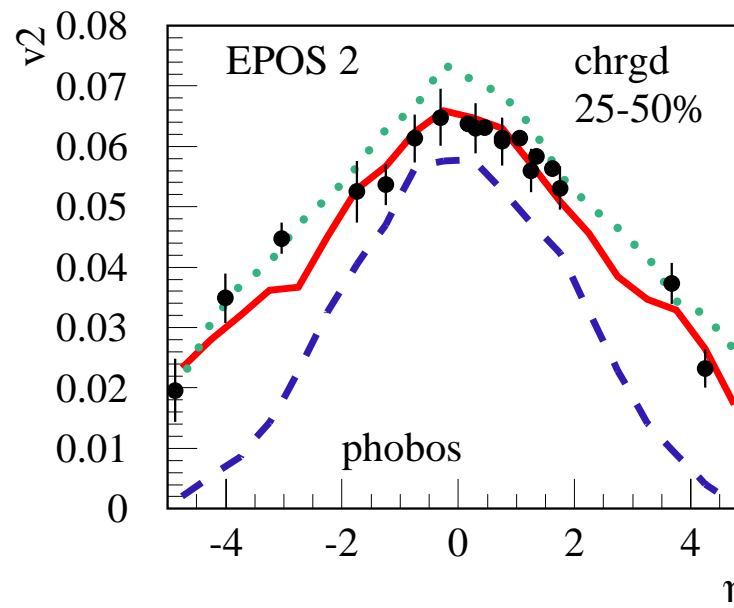
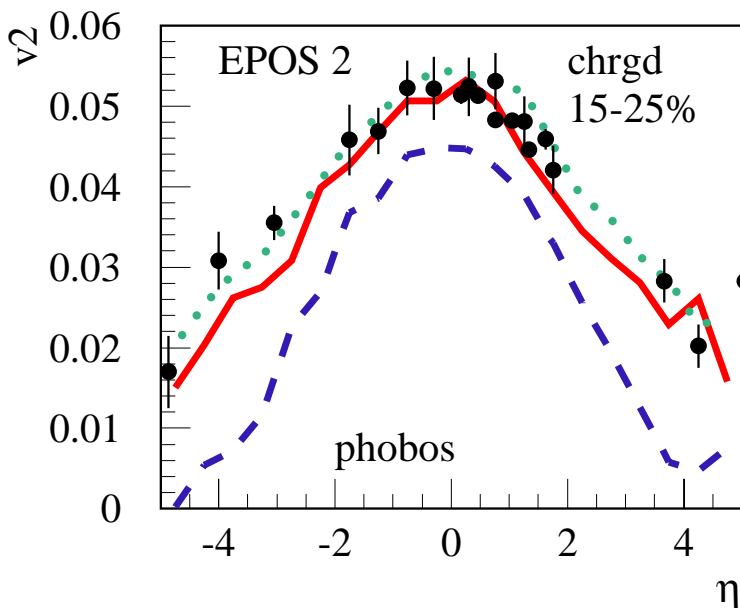
- ▷ flux-tube initial condition
- ▷ core-corona procedure
- ▷ three flavor cross-over EoS (X3F)
- ▷ EbE treatment
- ▷ hadronic FS cascade

# EPOS & 3DHydro, FO at 158MeV, EoS X3F, EbE

FO 158 MeV, with UrQMD (full); w/o (dashed); with elastic (dotted)



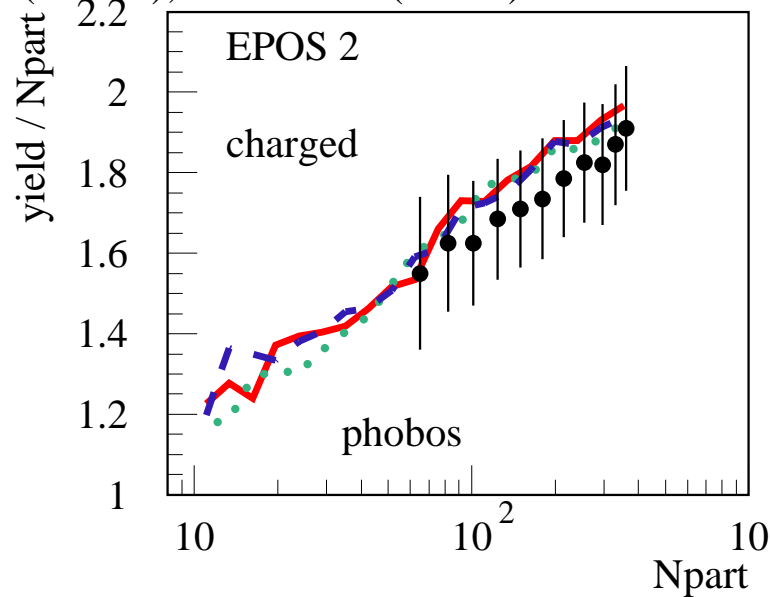
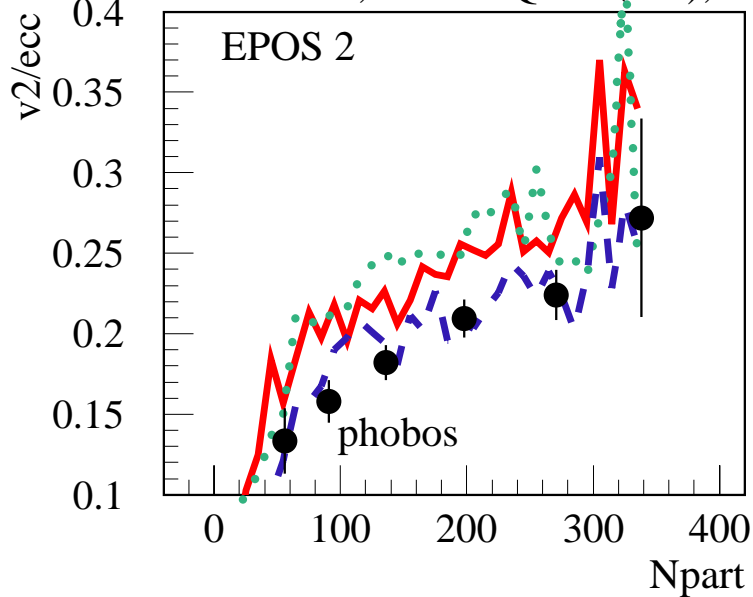
hadronic  
cascade,  
elastic,  
no  
cascade



important:  
flux-tube  
core-corona  
  
EoS Q3F  
 $\approx 20\%$  lower

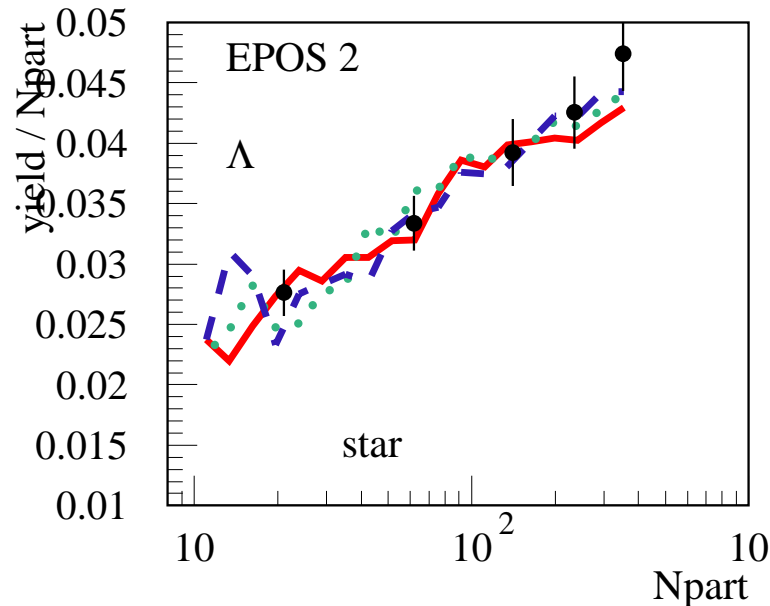
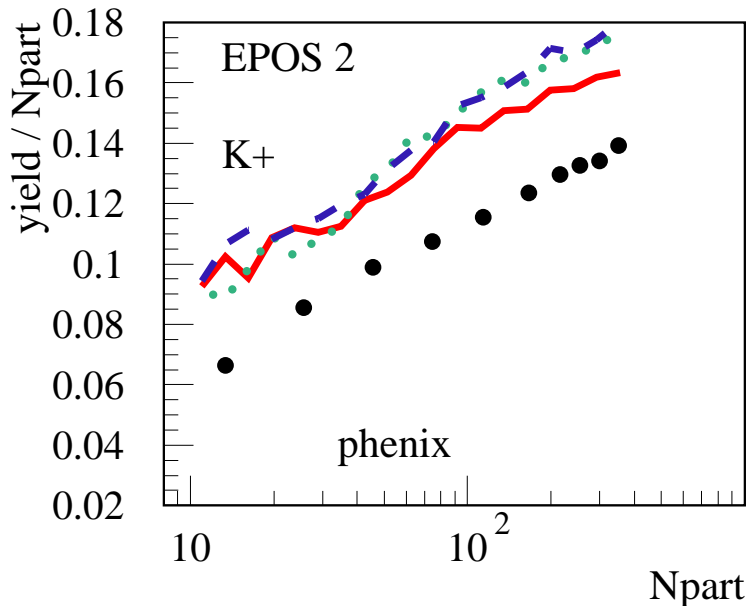
# $v_2/ecc$ , chrgd, K, $\Lambda$ -yields per part. (Npart)

FO 158 MeV, with UrQMD (full); w/o (dashed); with elastic (dotted)



**EoS X3F**

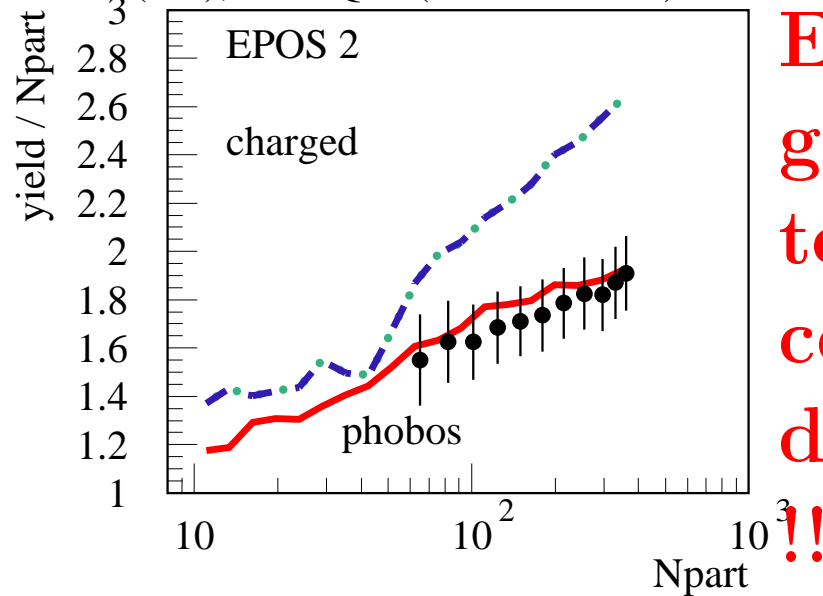
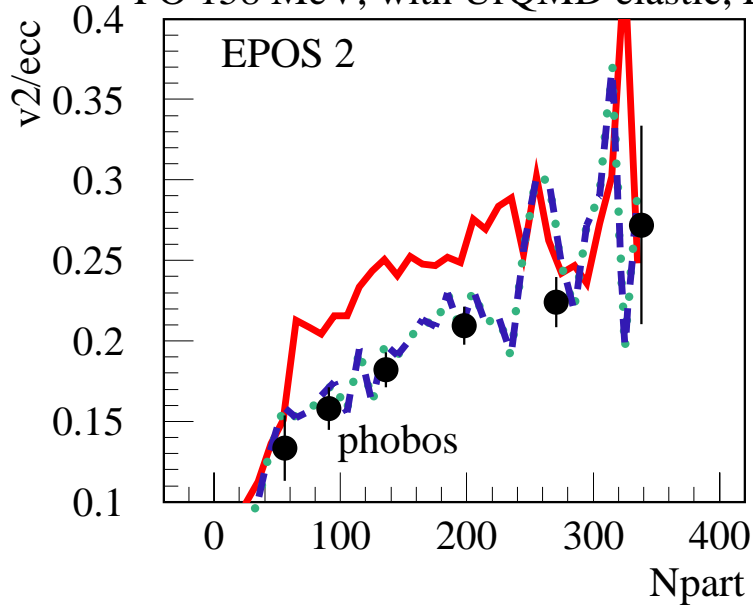
**core-corona effect**



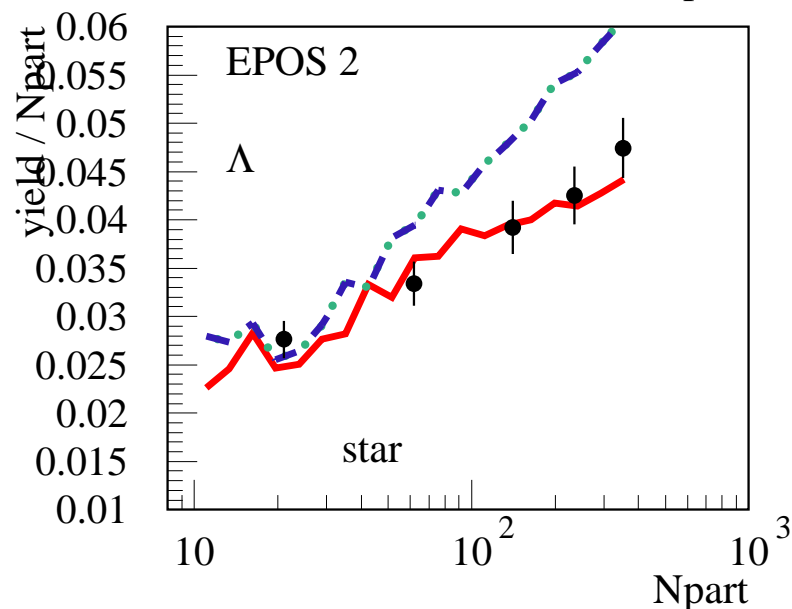
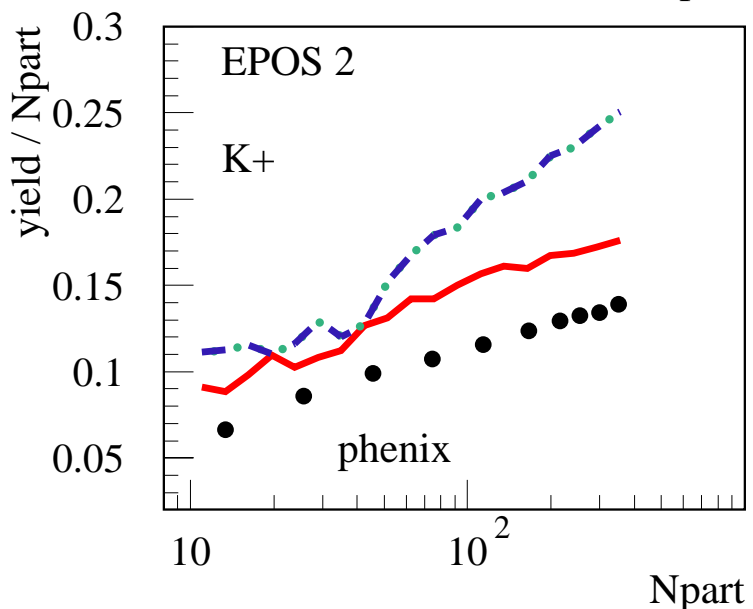
**kaon excess**

# comparing **EoS Q3F** and **X3F**

FO 158 MeV, with UrQMD elastic, EoS X3F (full); EoS Q3F (dashed-dotted)



**EoS Q3F**  
gives  
too steep  
centrality  
dependence

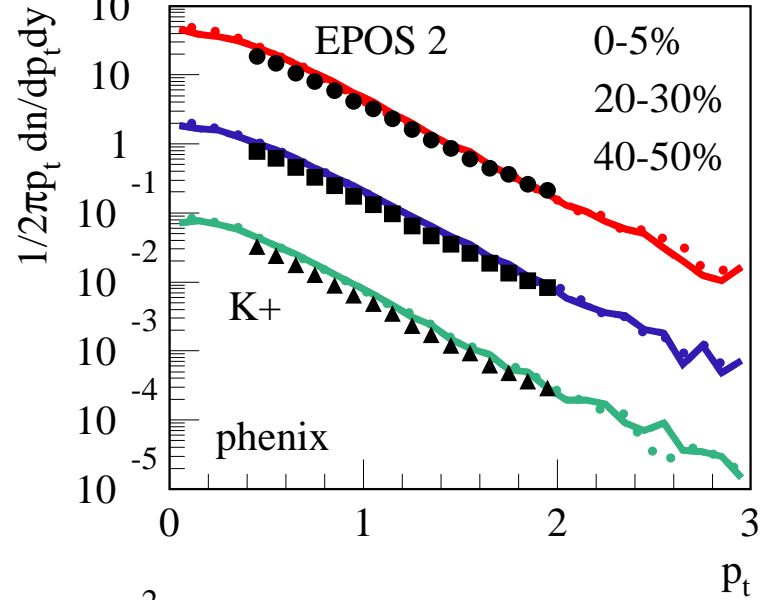
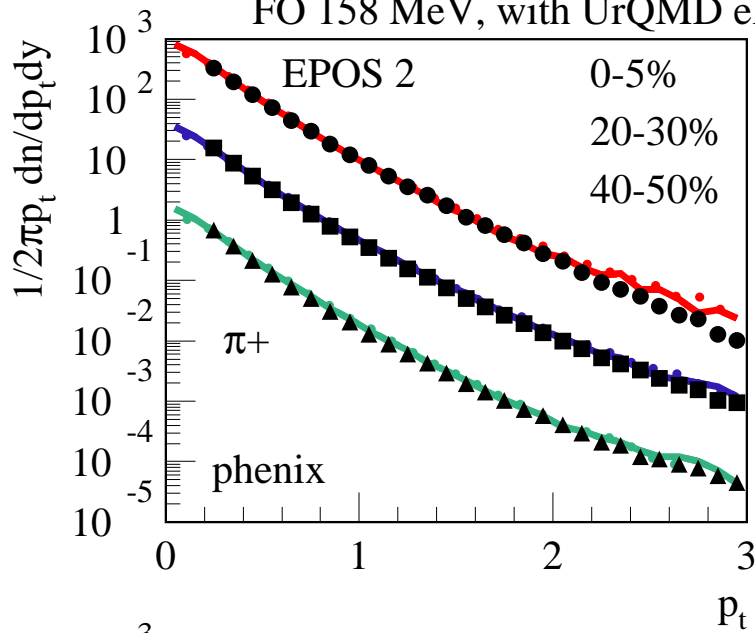


!!!

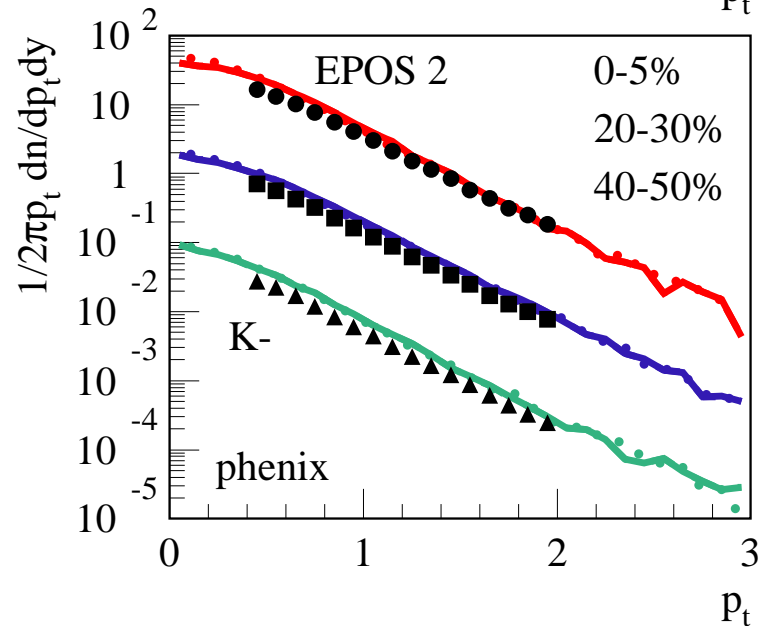
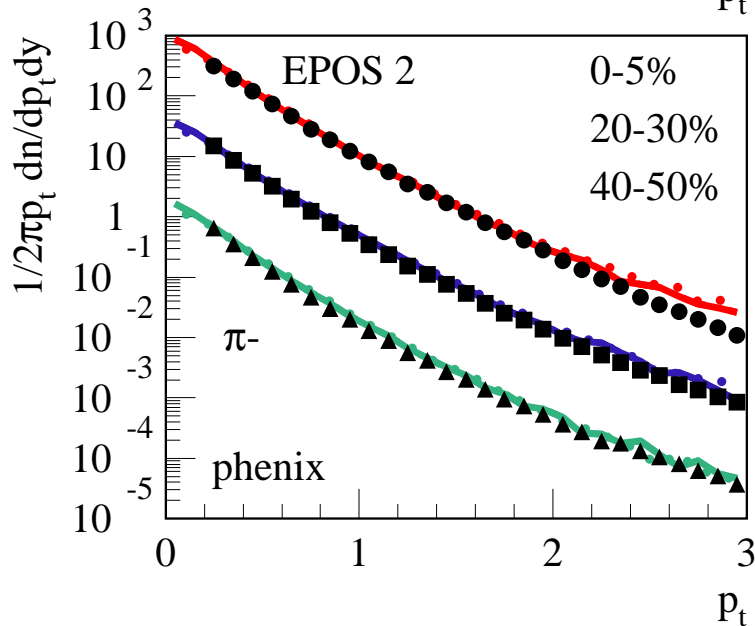


# pt spectra of pi and K

FO 158 MeV, with UrQMD elastic (full); w/o (dotted)



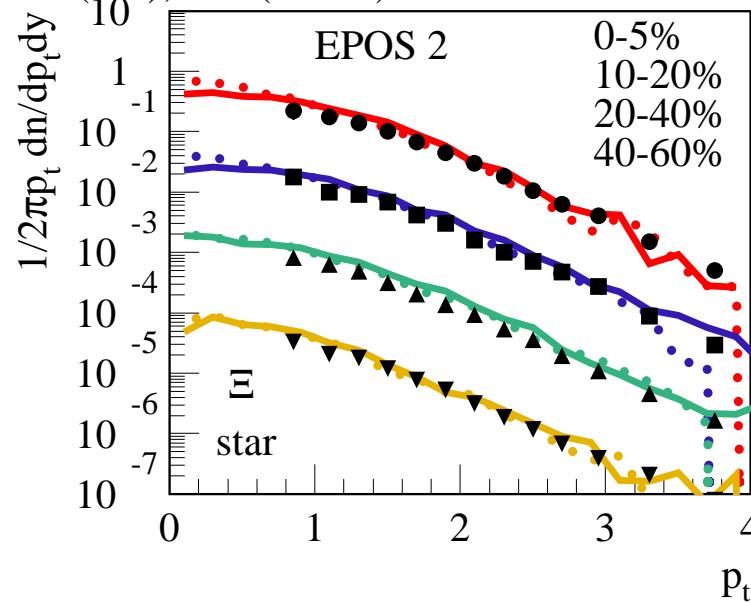
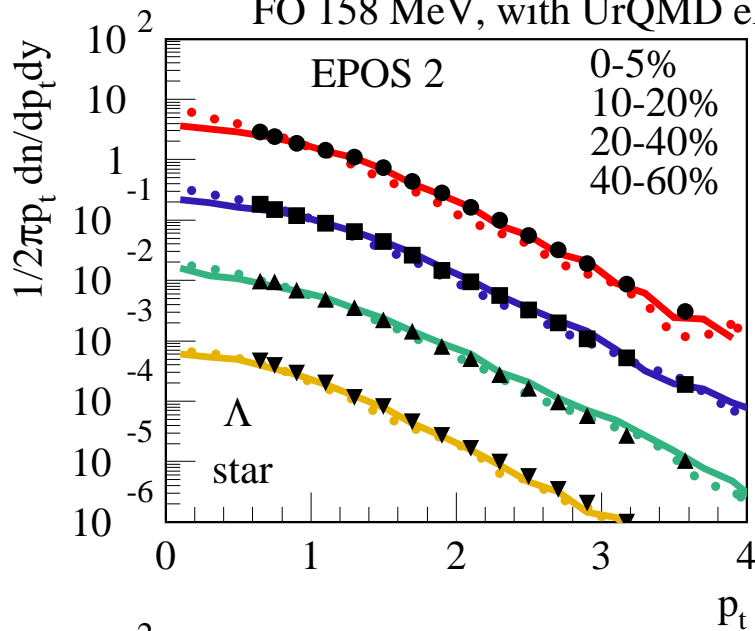
soft & hard  
(w/o e loss)



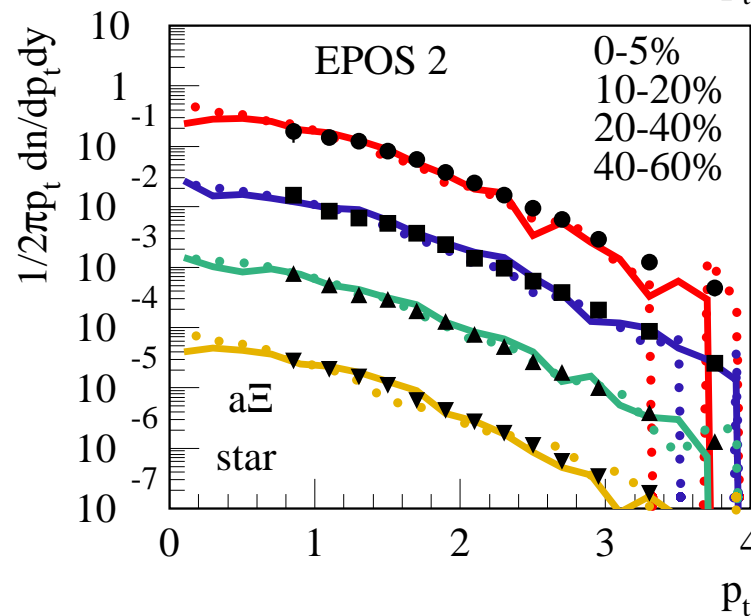
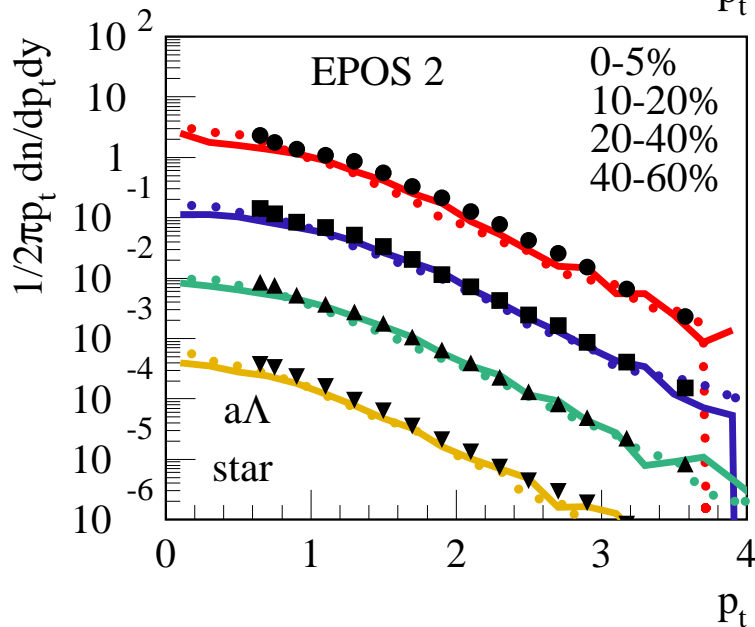
kaon excess

# pt spectra of $\Lambda$ and $\Xi$

FO 158 MeV, with UrQMD elastic (full); w/o (dotted)

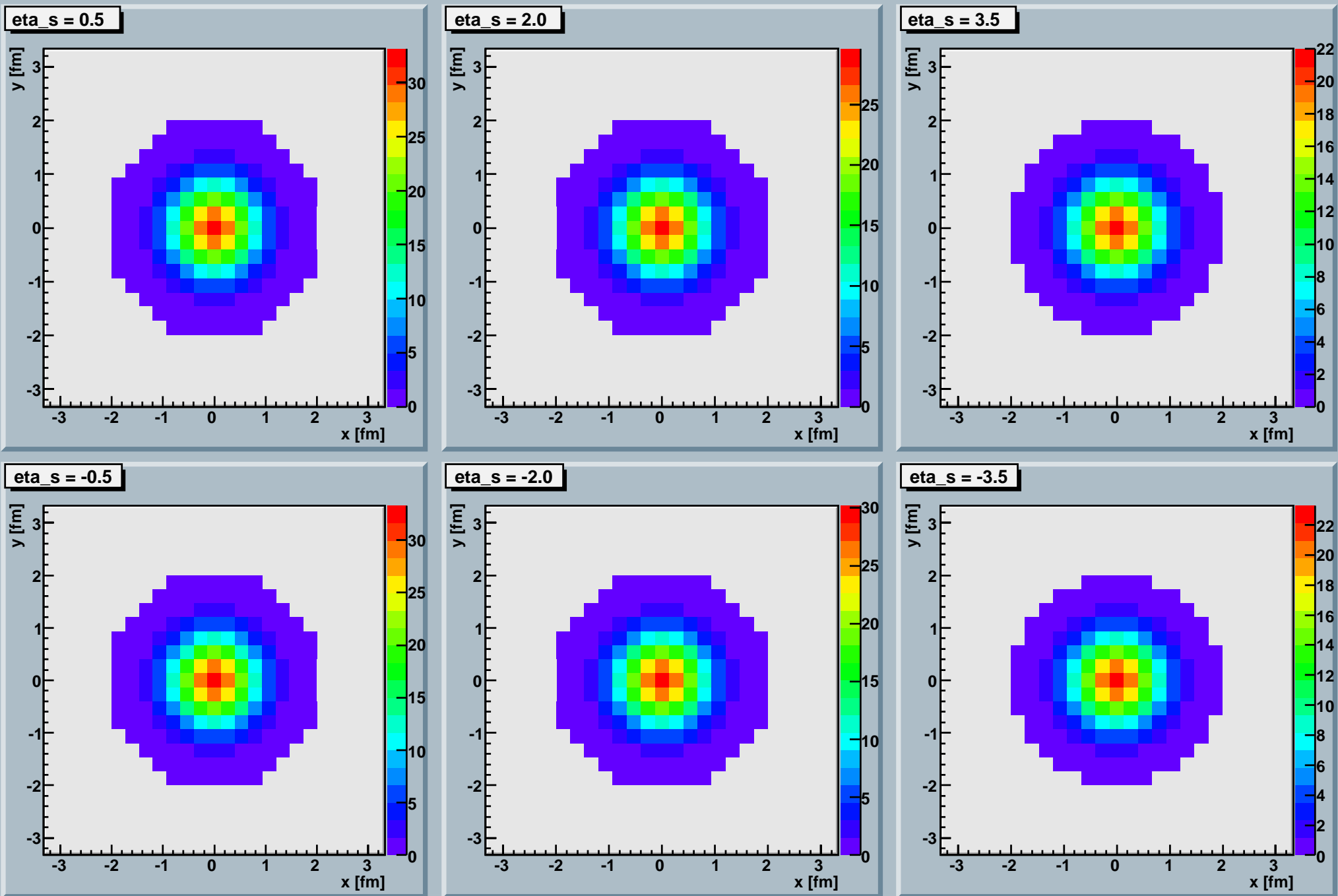


FO 158 MeV  
and elastic  
rescattering

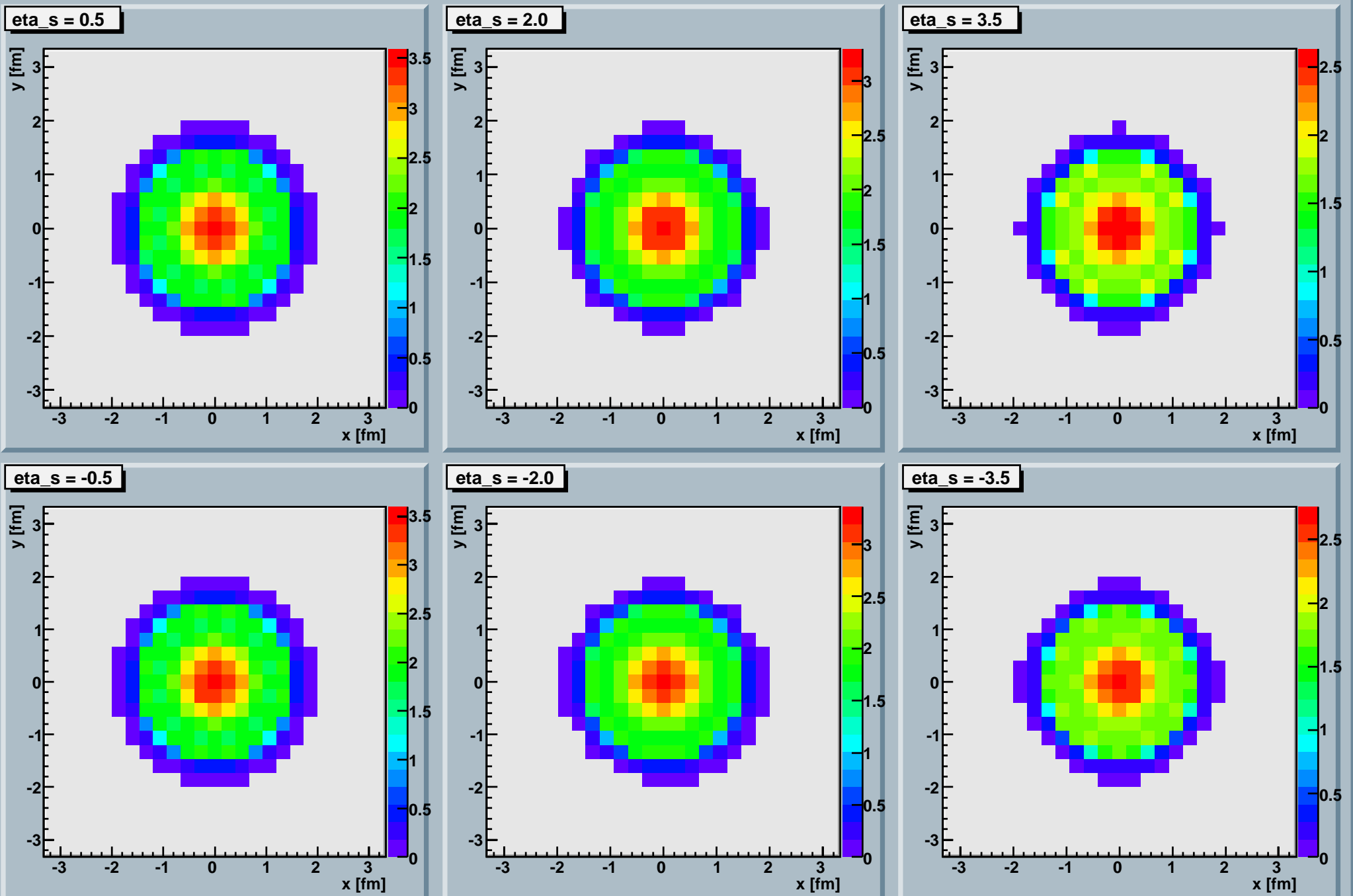


back to pp

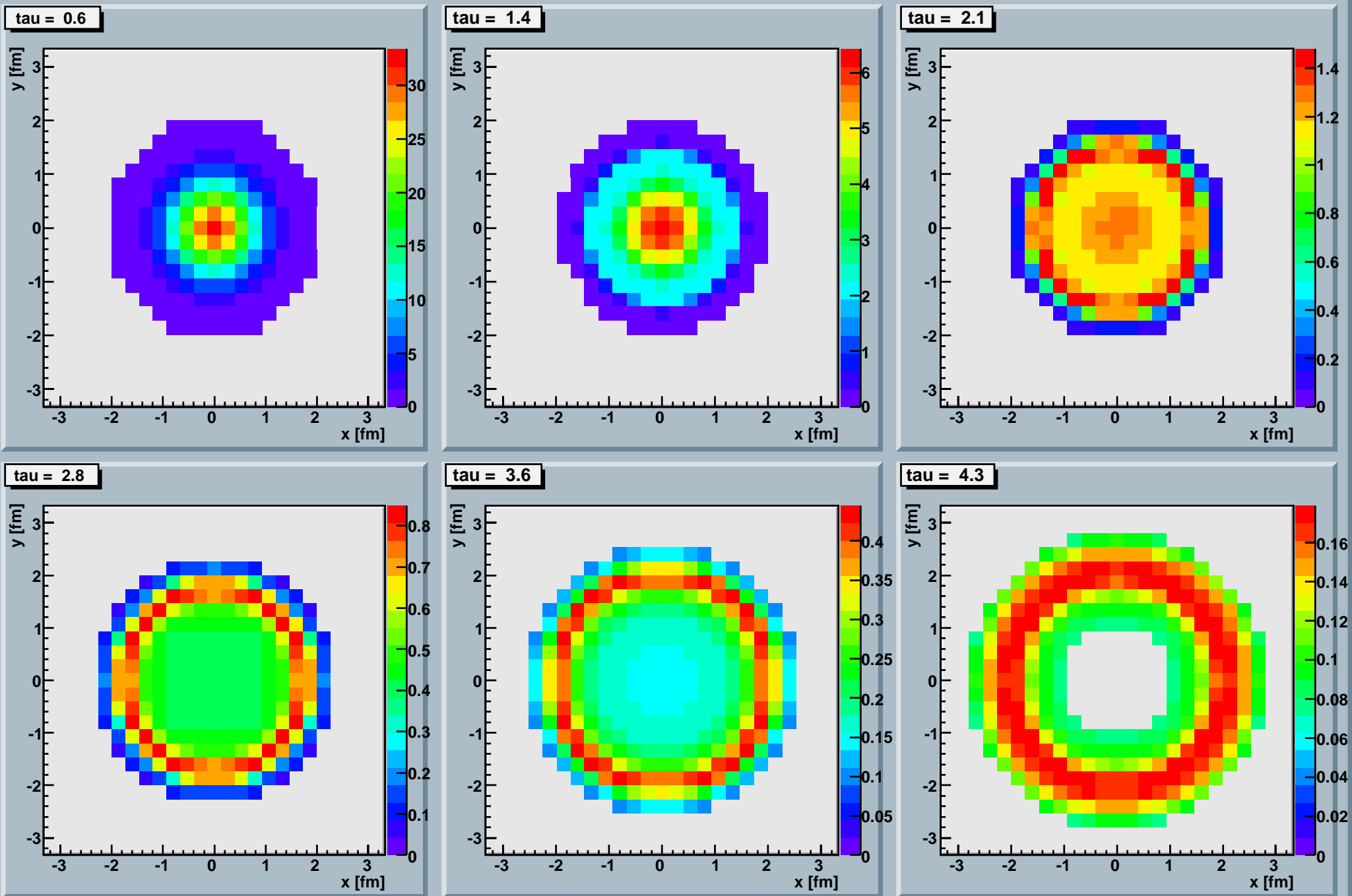
*energy density [GeV/fm<sup>3</sup>] ( $\tau = 0.6\text{fm}$ )  $b = 0\text{fm}$  15coll*



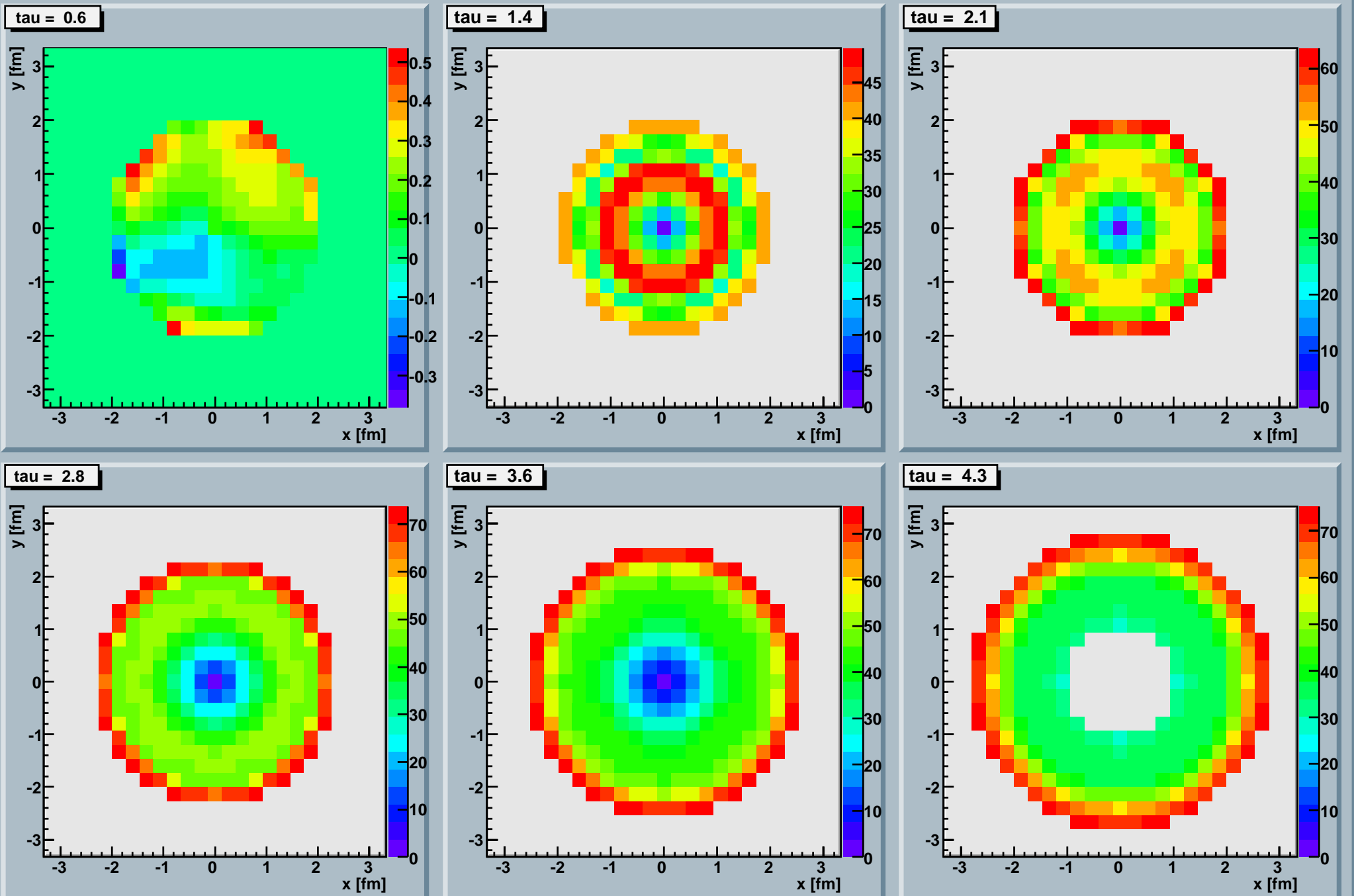
*energy density [GeV/fm<sup>3</sup>] ( $\tau = 1.6\text{fm}$ )  $b = 0\text{fm}$  15coll*



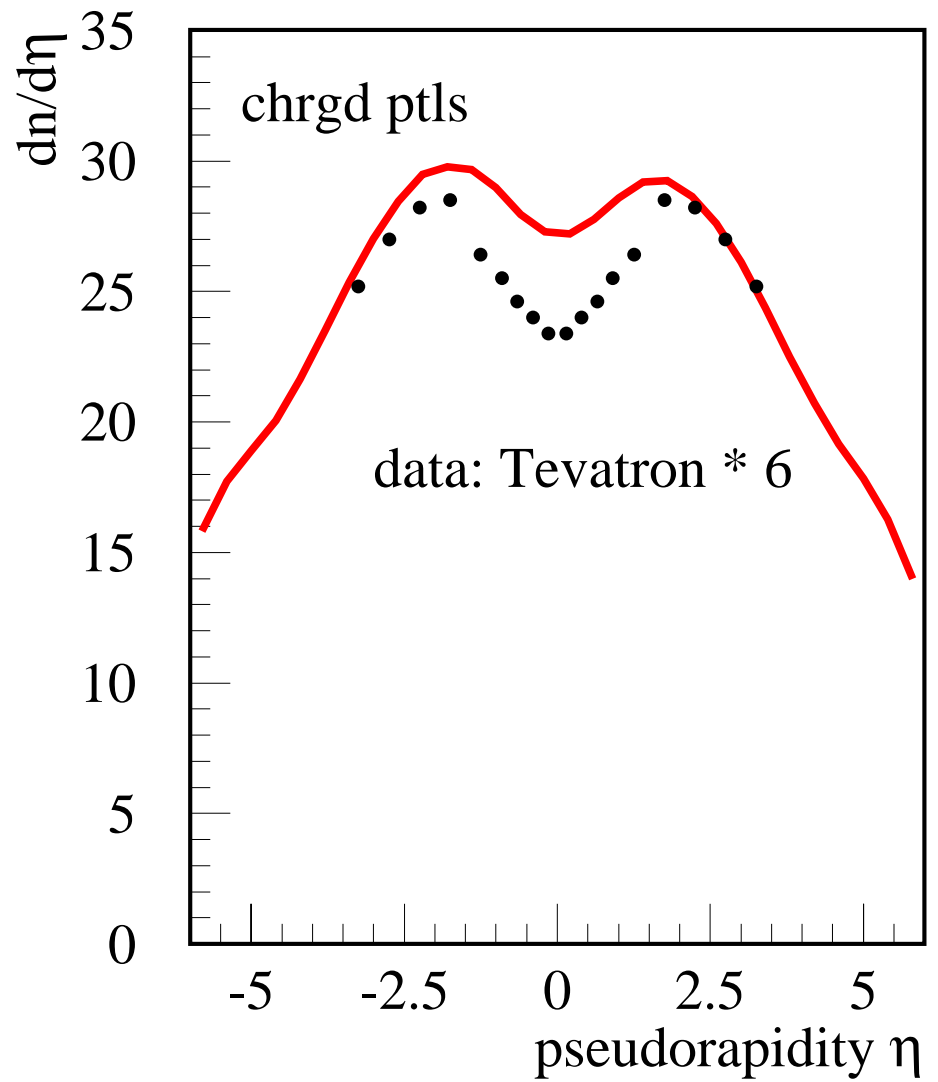
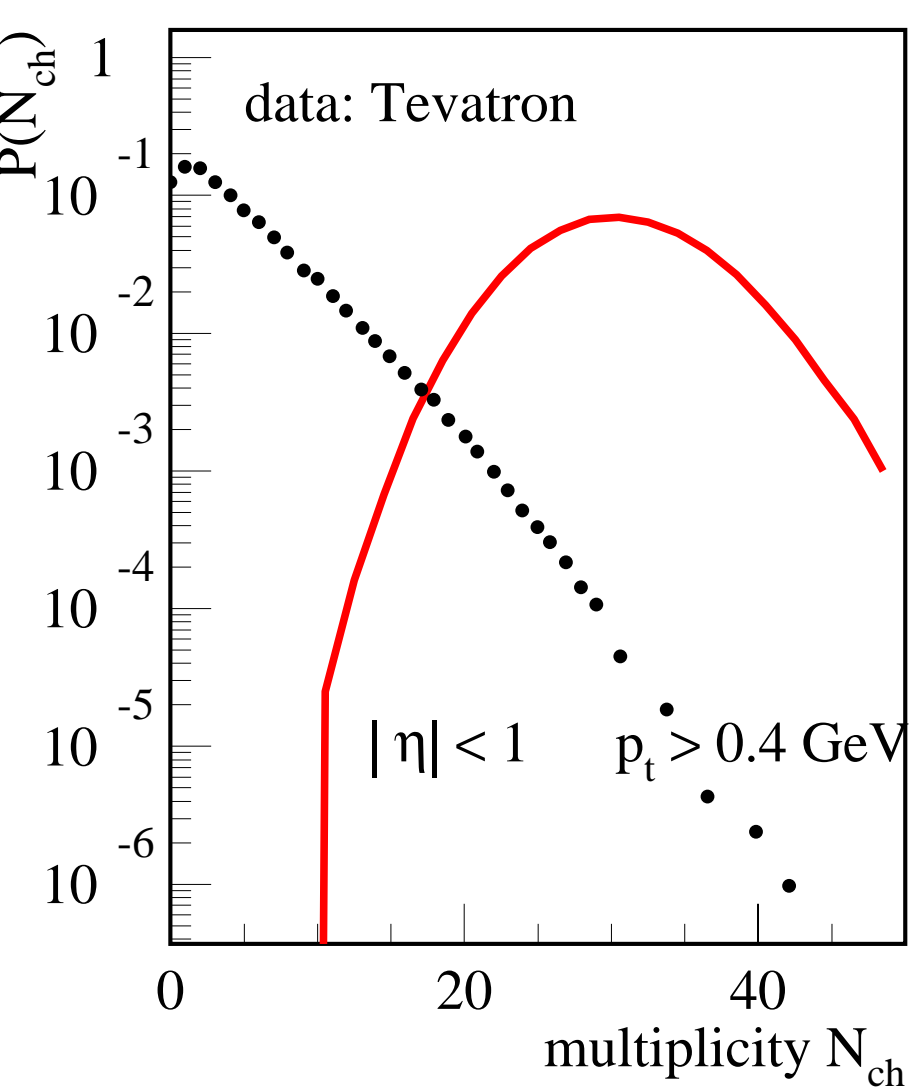
*energy density [GeV/fm<sup>3</sup>] (eta\_s=0) b=0fm 15coll*



*rad velocity [% of c] (eta\_s=0) b=0fm 15coll*

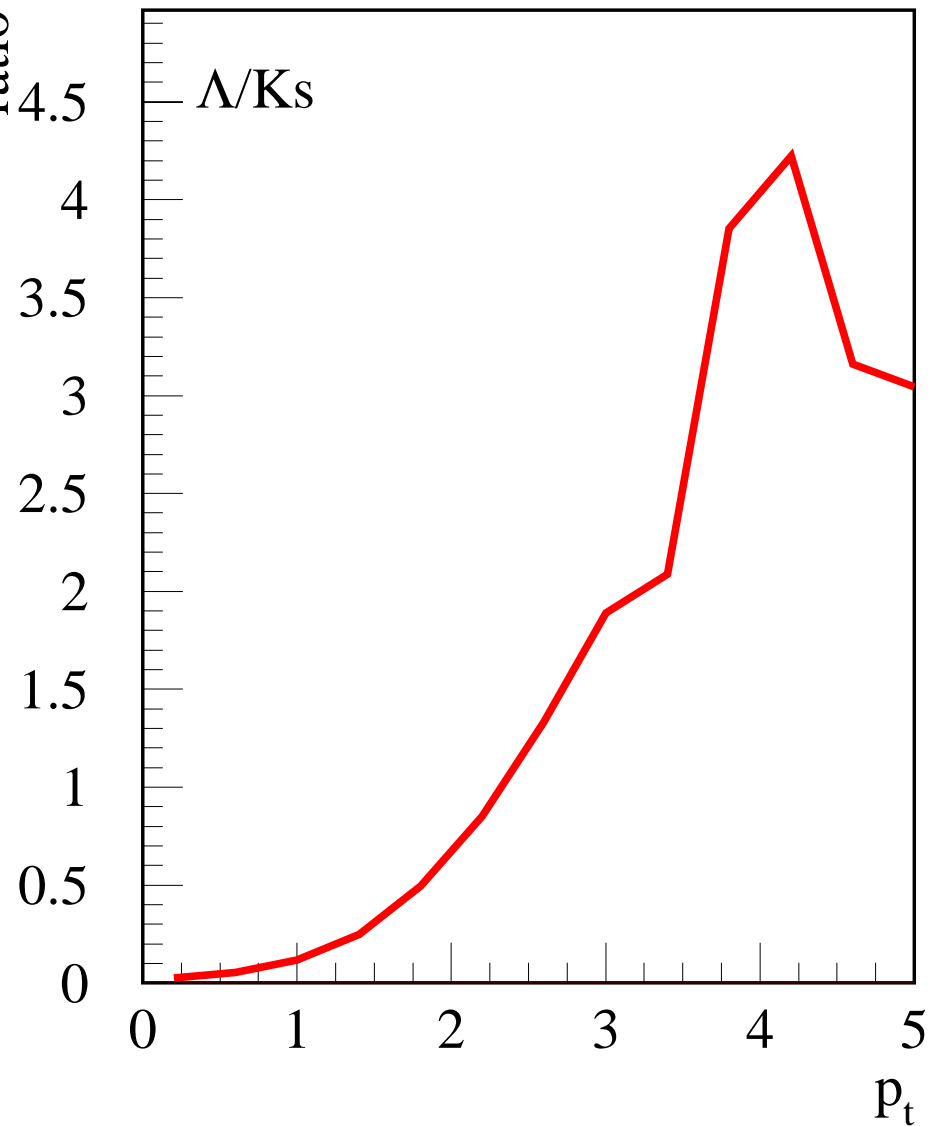
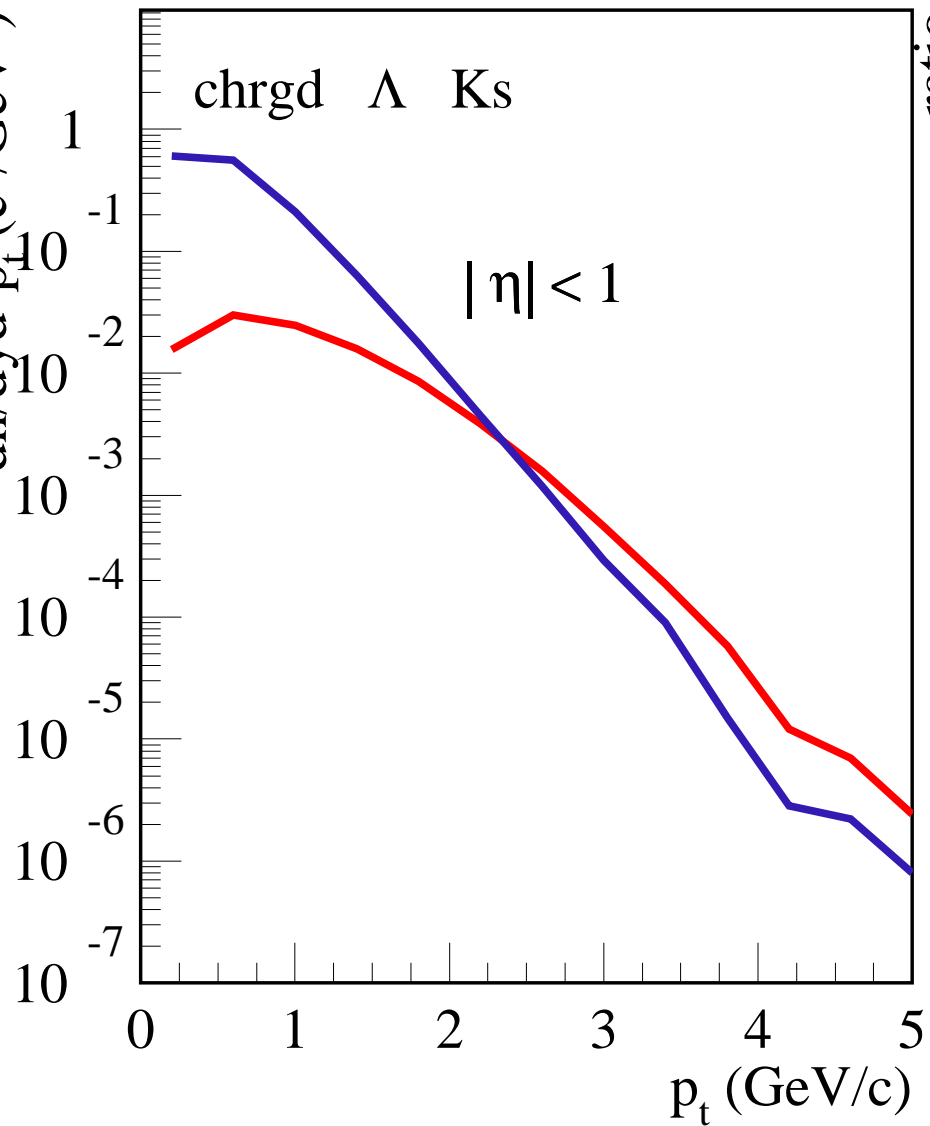


EPOS 2.01 p+p14TeV b=0, v=15 (only soft)

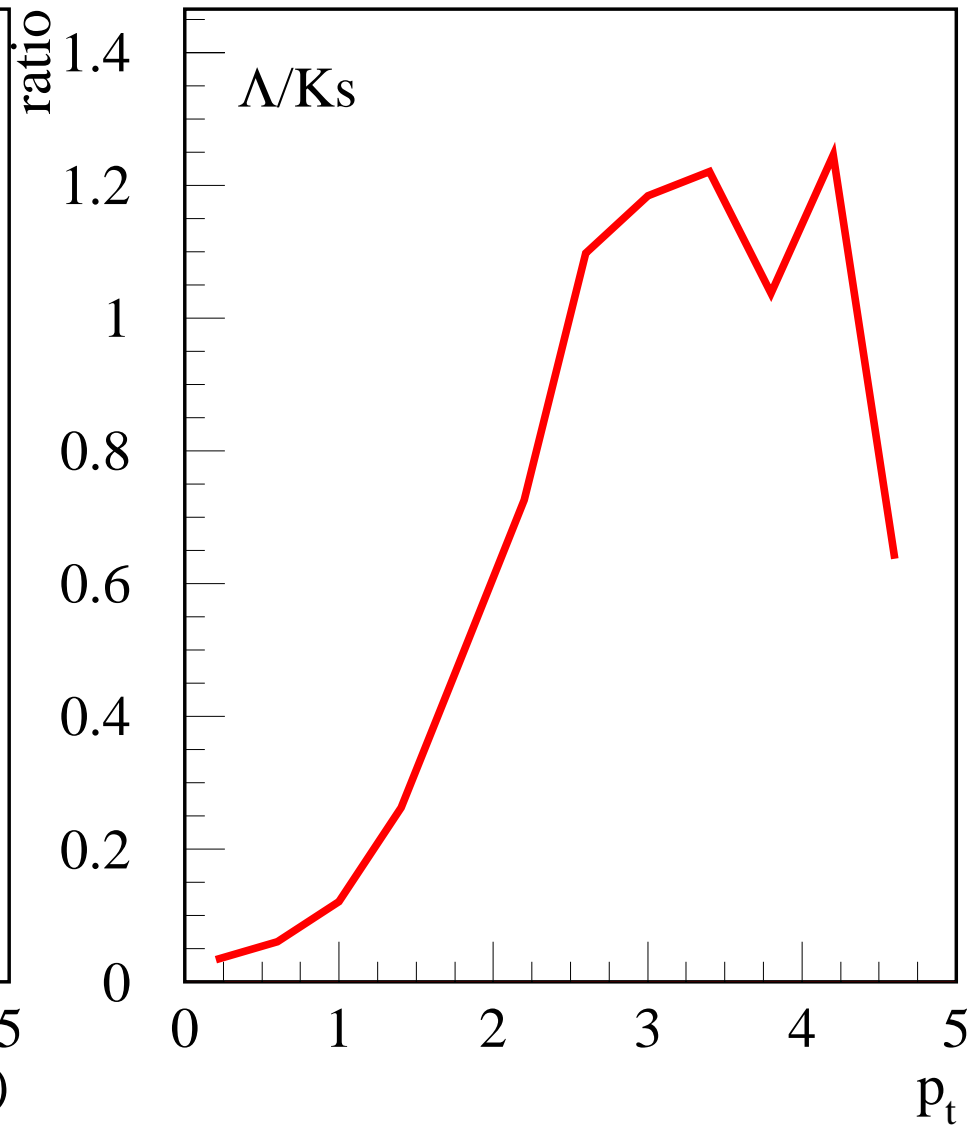
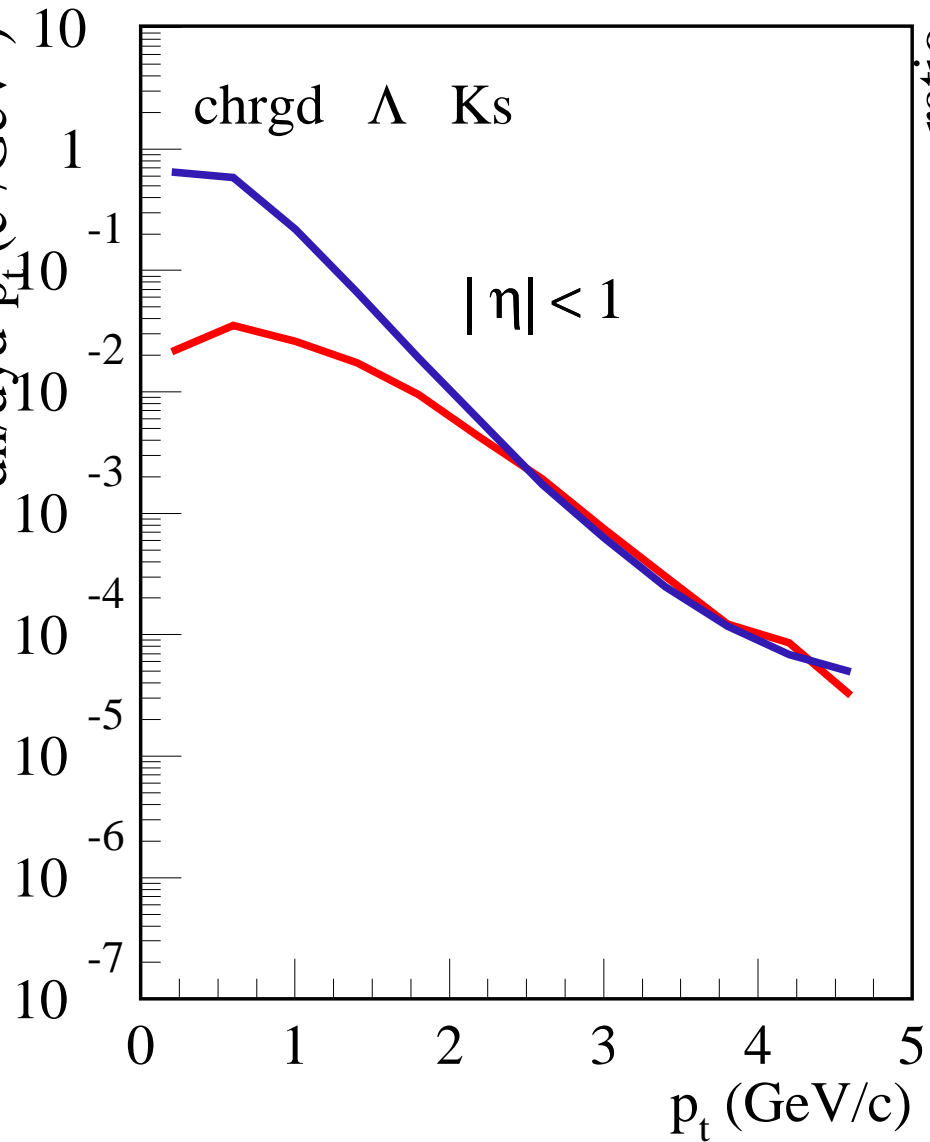




EPOS 2.01 p+p14TeV b=0, v=15 (only soft)

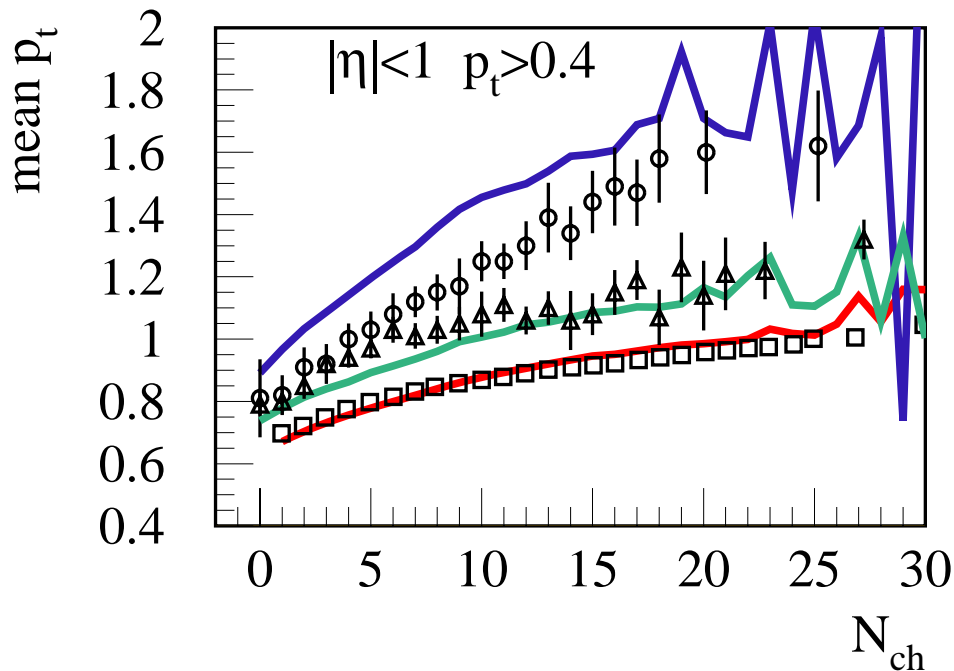
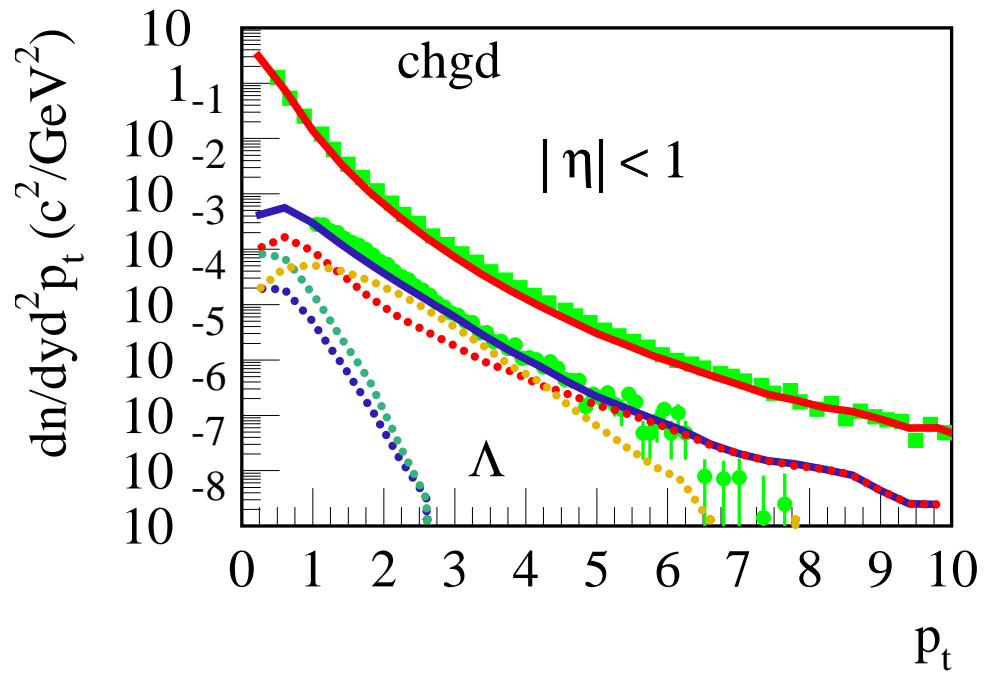


EPOS 2.01 p+p14TeV b=0, v=15 (soft+hard)



# Collective effects at Tevatron?

Charged particle and lambda pt spectra: different shapes (as in AA)



Tevatron 1.8 TeV  
EPOS 1

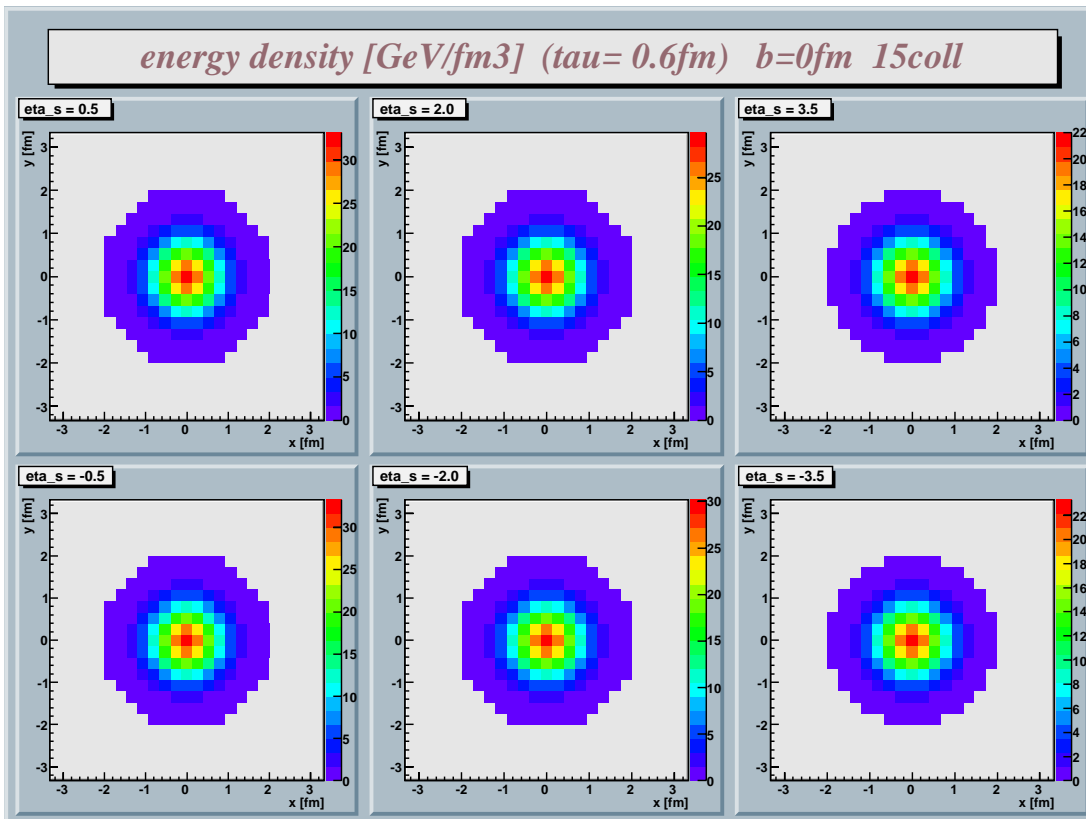
Increase of mean  $p_t$  vs multiplicity of charged ptls,  $K_s$ ,  $\Lambda$  (as in AA)

For pp & LHC, one should study the “centrality” dependence of observables:

- ▷ mean  $p_t$
- ▷ multi-strange baryon yields
- ▷ ratios of  $p_t$  spectra
- ▷ jet fragmentation functions
- ▷ heavy quark production

**Initial state effects (multiple scattering) and final state effects (flow, energy loss)**

**Also:** multiple scattering events should exhibit long range  $y$  correlations coming from the  $\eta_s$  correlation of the initial flux tubes



study particle yields, spectra, ... at forward rapidity as a function of the backward multiplicity

This should clearly exhibit the flux tube structure

## to summarize

- ▷ Core-corona procedure separates events into two classes: core and corona events
- ▷ Multiple scattering provides high energy density “core events”
- ▷ core events should expand collectively, decay statistically
- ▷ EPOS 2 features
  - flux-tube initial cond based on multiple scattering
  - core-corona procedure
  - three flavor cross-over EoS (X3F)
  - EbE treatment
  - hadronic FS cascade
  - full hadron set