

ConformalTracking

geometry agnostic tracking library

ACAT 2019

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On behalf of the **CLICdp** collaboration

Saas-Fee, 11 March 2019

CLIC – Compact Linear Collider

- ▶ High-luminosity linear e^+e^- collider
- ▶ The only mature multi-TeV option for future lepton colliders

Current scenario:

Stage 1: 1 ab^{-1} @ $t\bar{t}/380\text{ GeV}$

Precision SM Higgs and top physics

Stage 2: 2.5 ab^{-1} @ 1.5 TeV :

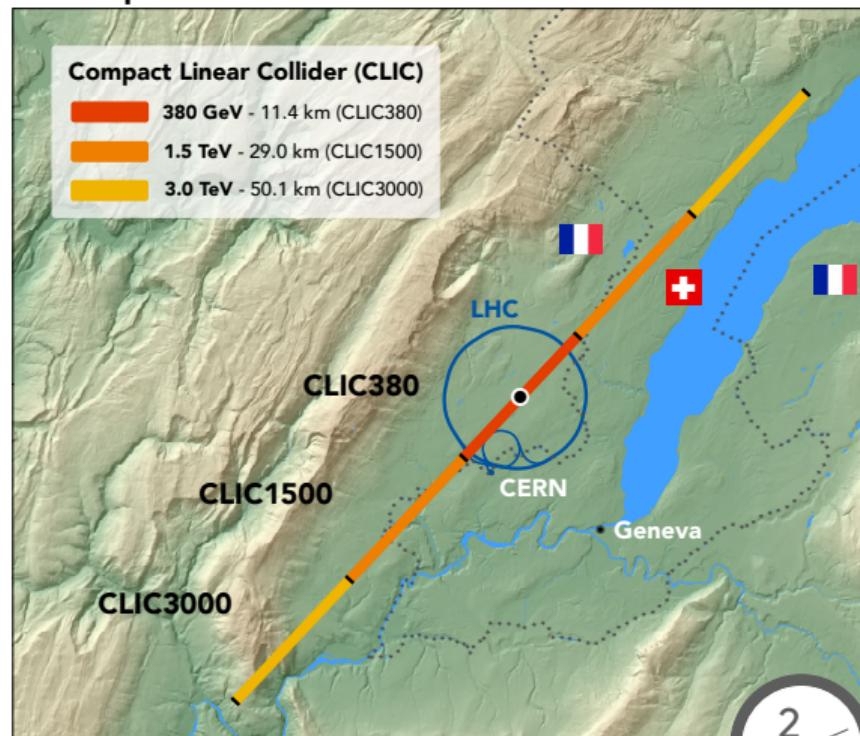
BSM, top and rare Higgs processes

Stage 3: 5 ab^{-1} @ 3 TeV :

BSM, top and rare Higgs processes

Each stage corresponds to 7-8 years

<https://clic.cern>



CLIC physics and tracking performance requirements

► Momentum resolution

Higgs recoil, $H \rightarrow \mu\mu$ or ℓ from BSM

$$\frac{\sigma(p_T)}{p_T^2} \sim 2 \times 10^{-5} \text{ GeV}^{-1}$$

► Jet energy resolution

$W/Z/H$ di-jet separation

$$\frac{\sigma(E)}{E} \sim 3.5 - 5\%$$

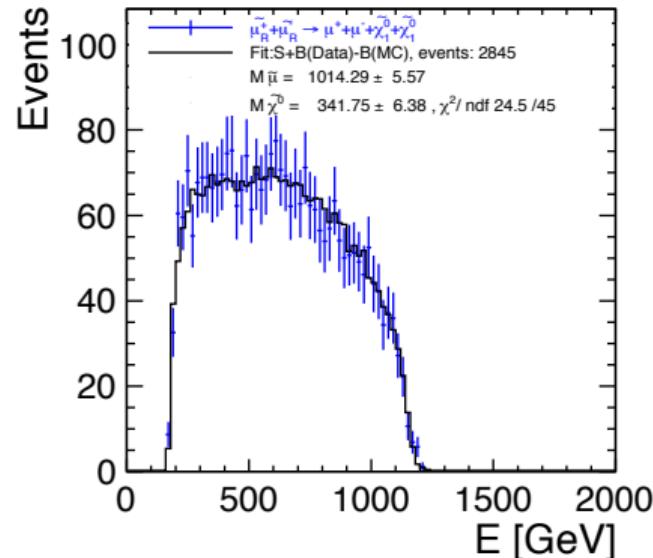
for $E = 1000 - 50$ GeV

► Impact parameter resolution

b/c tagging, Higgs couplings

$$\sigma_{r\phi} = \sqrt{a^2 + b^2 \cdot \text{GeV}^2 / (p^2 \sin^3 \theta)}$$

with $a = 5 \mu\text{m}$ and $b = 15 \mu\text{m}$



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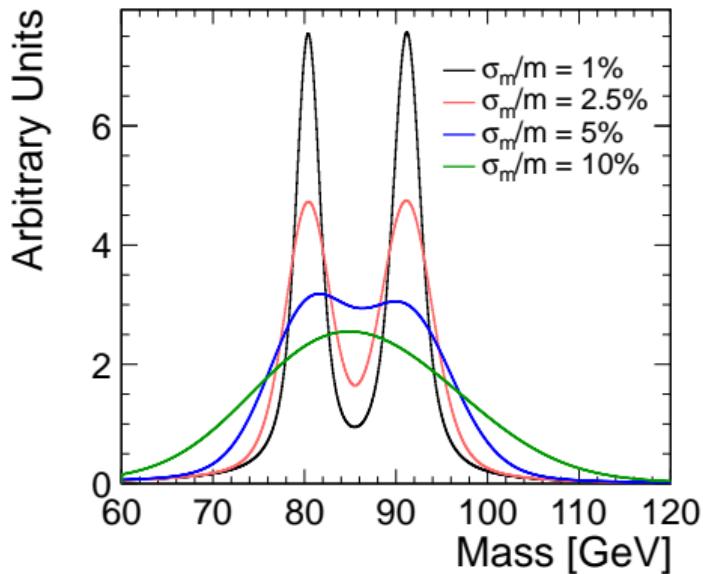
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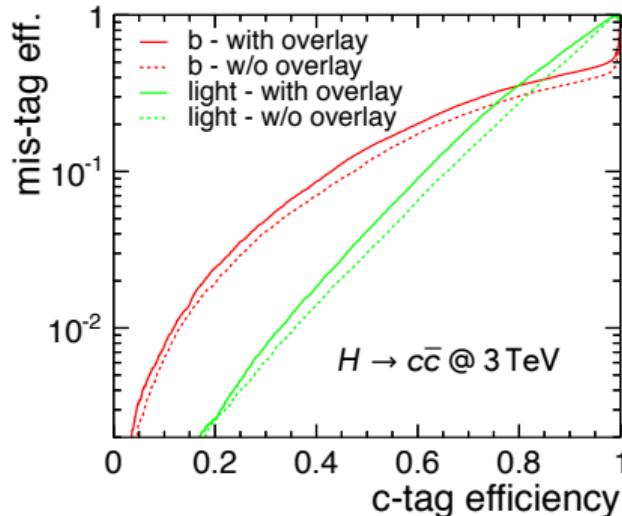
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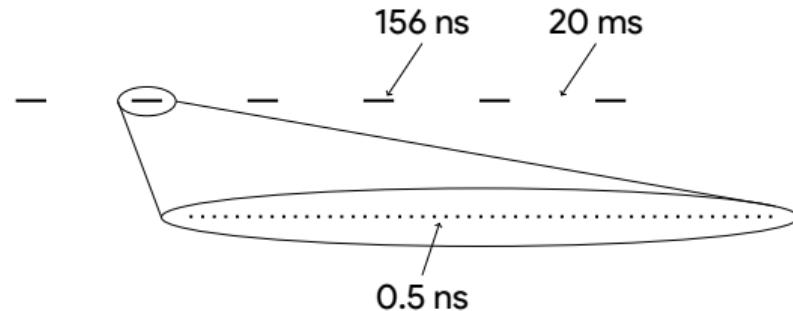
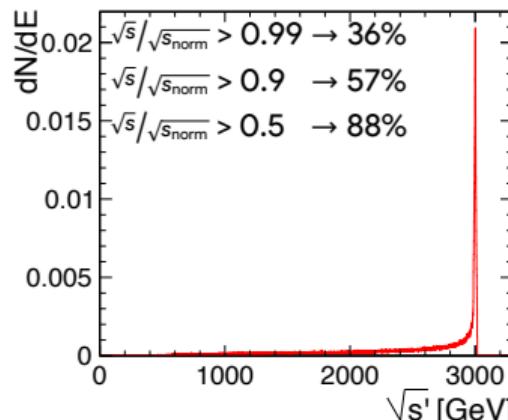
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CLIC beam structure and beam-induced backgrounds

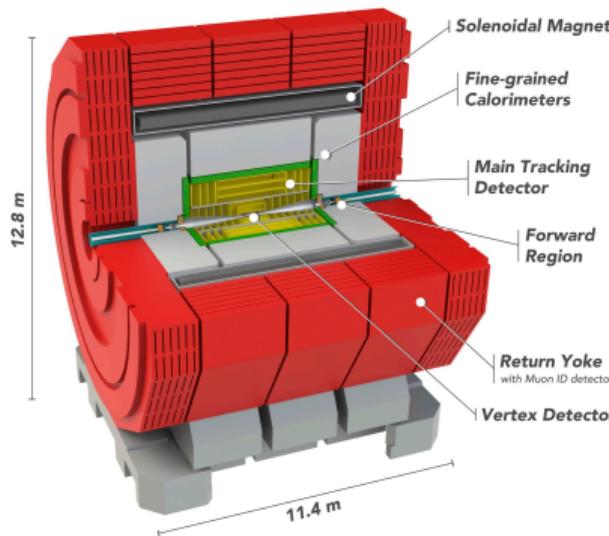
- ▶ Time stamp hits from the detectors
(central det \Leftrightarrow physics event)
- ▶ Tracking timing requirements
 - ▶ 10 ns integration time
 - ▶ $10/\sqrt{12}$ ns hit resolution
- ▶ Background overlay (10 (20) beam crossings before (after) physics event)



CLIC: trains at 50 Hz, 1 train = 312 bunches

- ▶ entire bunch train available for offline reconstruction
- ▶ not all bunches crossings contain a “hard” interaction

CLIC Detector Concept

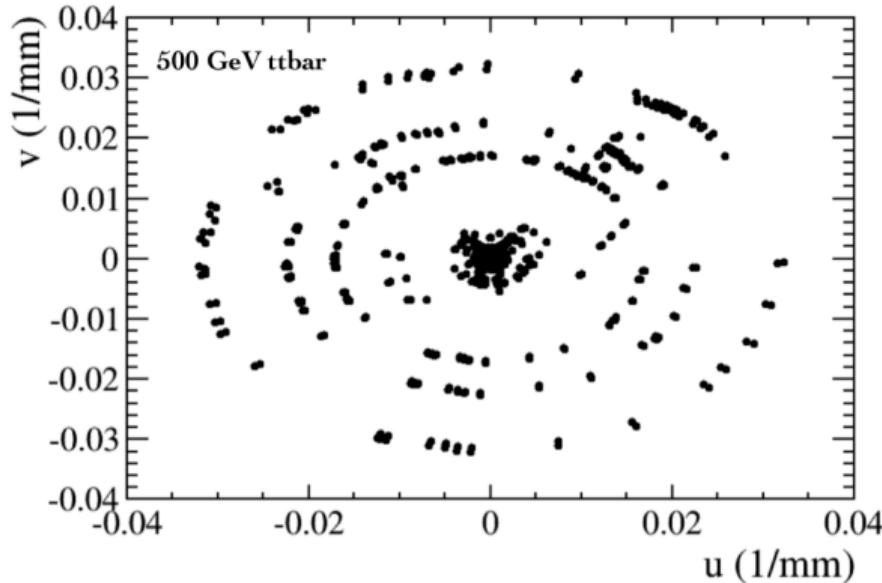


- ▶ B Field of 4 T
- ▶ Vertex: 3 double layers
 - ▶ Single-hit accuracy 3 μm
 - ▶ 0.2% X_0 per detection layer
 - ▶ Power pulsing \rightarrow 50 mW cm $^{-2}$
- ▶ Si tracker: $r_{max} = 1.5$ m
 - ▶ single point resolution = 7 $\mu\text{m} \times 90 \mu\text{m}$
 - ▶ detector: $\sim 1\%X_0$ per layer
 - ▶ support & cables: $\sim 2.5\%X_0$
- ▶ Precise timing for background rejection
 - ▶ 10 ns stamping for tracks
 - ▶ 1 ns accuracy for calo. cluster

Low-mass \rightarrow small multiple scattering \rightarrow ideal for conformal tracking

Tracks in Conformal Space

- Conformal map applies a geometry transform that maps **circles** in the x,y plane passing through the origin point into **straight lines** in the u,v plane



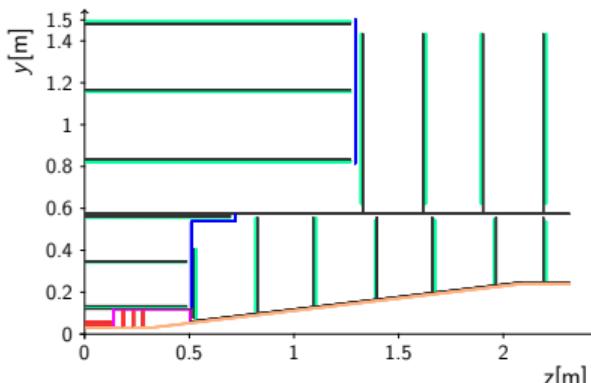
$$u = \frac{x}{x^2 + y^2}$$
$$v = \frac{y}{x^2 + y^2}$$

- Vertex hits outside
- Tracker hits closer to (0,0)

- Pattern recognition in conformal space via **cellular automaton**, used to perform straight line search

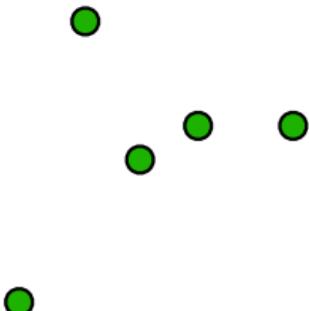
Pattern recognition – full chain

Build tracks	Vertex barrel	Standard cuts
Extend tracks	Vertex endcap	Standard cuts
Build tracks	Vertex b + e	Standard cuts
Build tracks	Vertex b + e	Looser cuts (angle x 5)
Build tracks	Vertex b + e	Looser cuts (angle x 10)
Build tracks	Vertex b + e	Looser cuts (angle x 10; χ^2 x 20)
Extend tracks	Tracker collection	Looser cuts (angle x 10; χ^2 x 20)
Build tracks	All collections	Displaced cuts

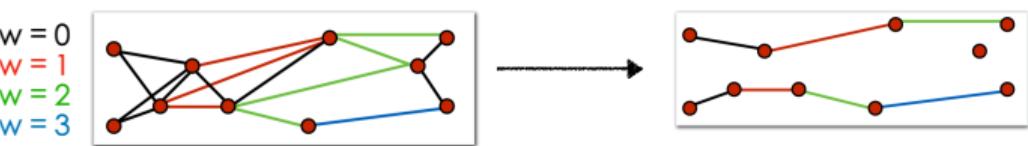


- ▶ Chain is fully configurable (boost::spirit)
- ▶ Pattern recognition geometry-agnostic
- ▶ Based only on the hit position in global space
- ▶ Without constraint on the hit position in subdetectors

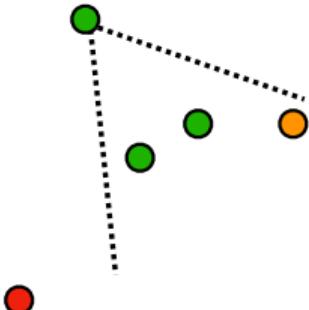
Build tracks in vertex barrel



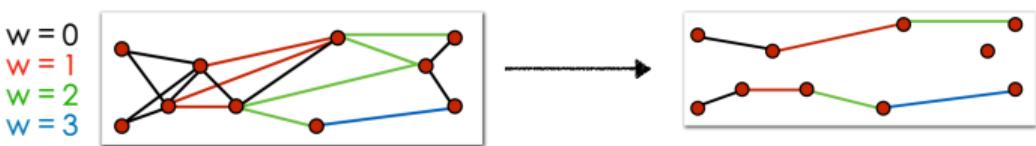
- ▶ Pattern search starts in vertex barrel
- ▶ Hit used as seed to look for neighbors with 2D tree
 - ▶ hits not outside the search cone
 - ▶ hits not too far from the seed hit
- ▶ Seed cells created and extended to virtual hits
- ▶ Cellular tracks are vectors of cells
 - ▶ each cell has a weight
 - ▶ each subsequent link increments the weight by 1
 - ▶ create valid tracks starting from higher weight
 - ▶ if more paths available, branch the track



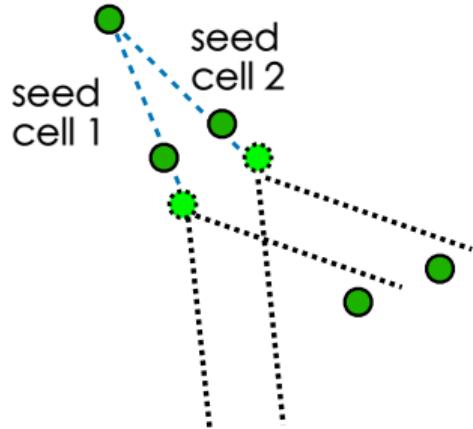
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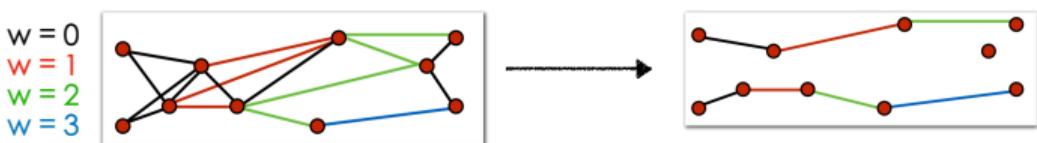
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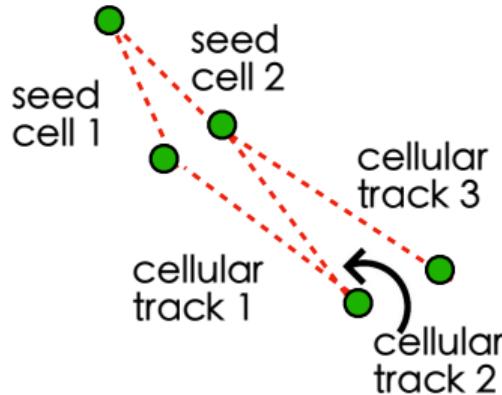
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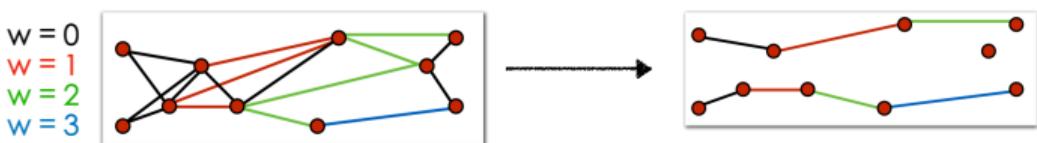
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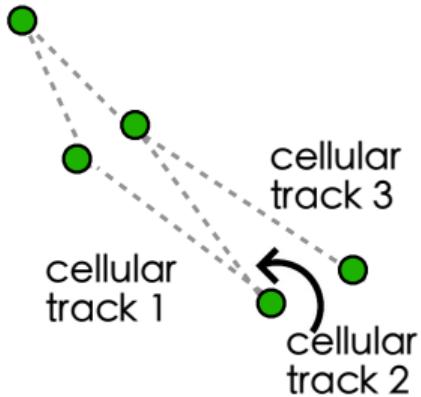
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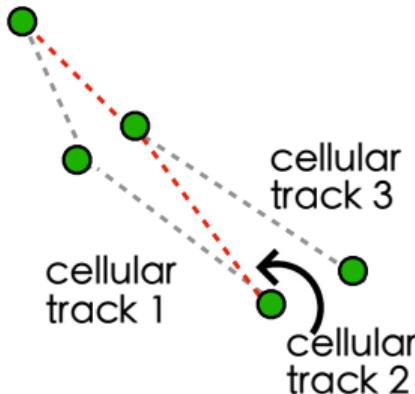


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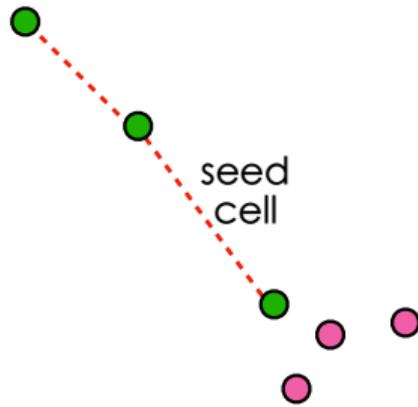
- ▶ For all cellular tracks starting from seed hit:
 - ▶ linear regression (u,v) $\rightarrow \chi^2/\text{ndf}$
 - ▶ linear regression (s,z) $\rightarrow \chi^2/\text{ndf}$
 - s : arc segment along the helix
 - ▶ remove hits progressively to refit and compare χ^2
- ▶ Best track is one with lowest χ^2
 - ▶ similar χ^2 are kept
 - ▶ clones (overlapping hits ≥ 2) are skimmed
 - ▶ longest usually preferred if χ^2 not too large
- ▶ Hits are marked as used and the search continues with the unused ones in the collection

Build tracks in vertex barrel



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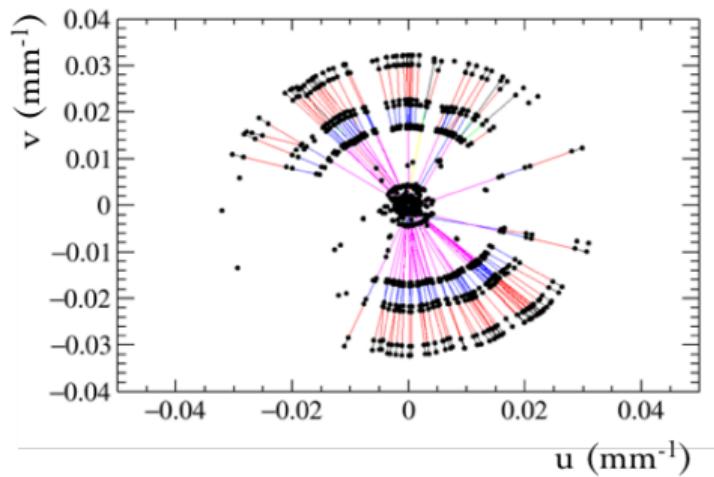
Extend tracks in vertex endcap



- ▶ Extended tracks from vertex barrel into the endcaps, starting from seed cell between the last two hits of the track
- ▶ Pick candidates to which to extend based on nearest neighbor search
- ▶ Each hit candidate is progressively added to the track. Based on a re-fit the hit is accepted / rejected based on its χ^2

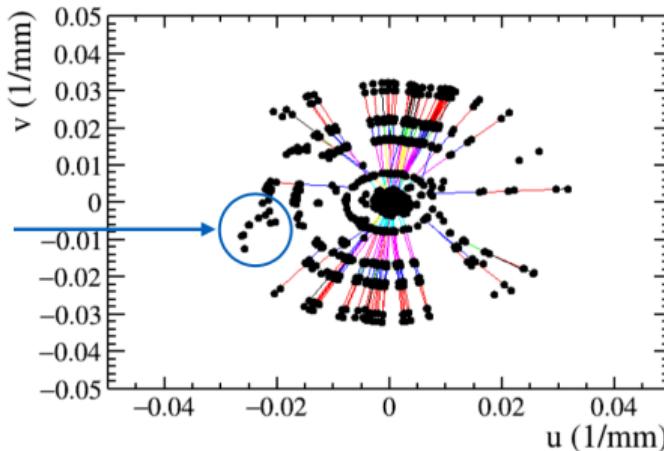
Build tracks with leftover vertex hits and extend in tracker

- ▶ After all possible extensions done, try to build new tracks from leftover hits
 - ▶ standard cuts
 - ▶ looser angle cuts
 - ▶ looser χ^2 cuts
- ▶ Extend all tracks made in the vertex (barrel, endcap, combined) to all the tracker hit collections



Displaced tracks in conformal space

- ▶ Conformal mapping turns circles through the origin into straight lines
 - ▶ Quadratic term to include displaced tracks, but eventually χ^2 breaks down

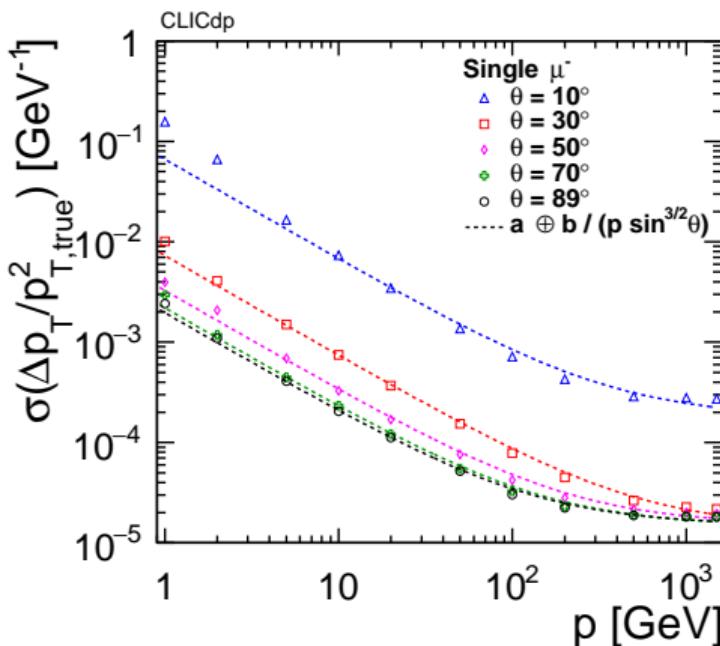
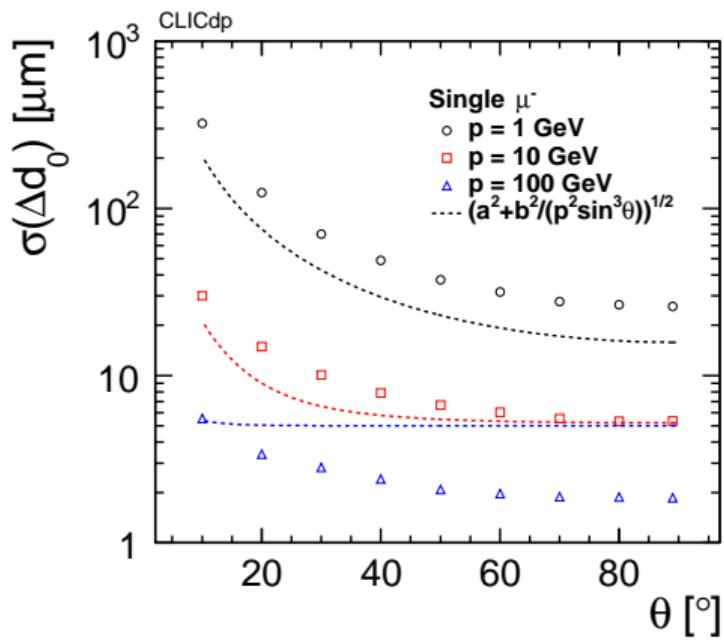


- ▶ Major strategy change
 - ▶ broader search angle than for prompt tracks
 - ▶ minimum 5 hits for tracks
 - ▶ start searching from tracker towards vertex
- ▶ Most time consuming segment of search

Fitting the tracks

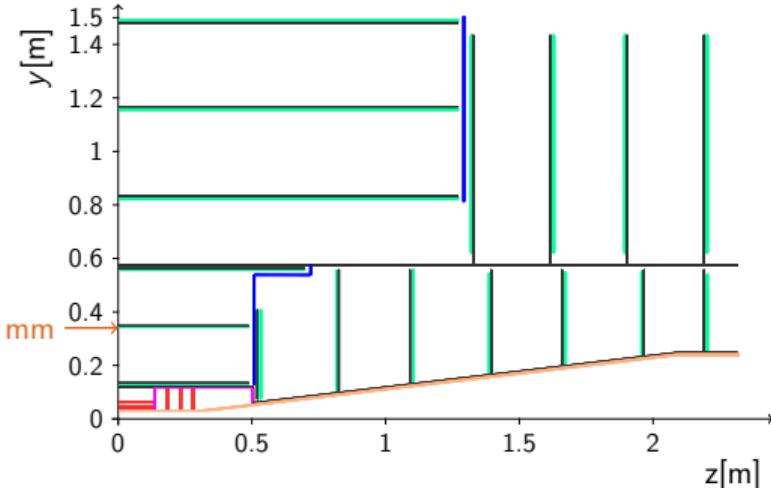
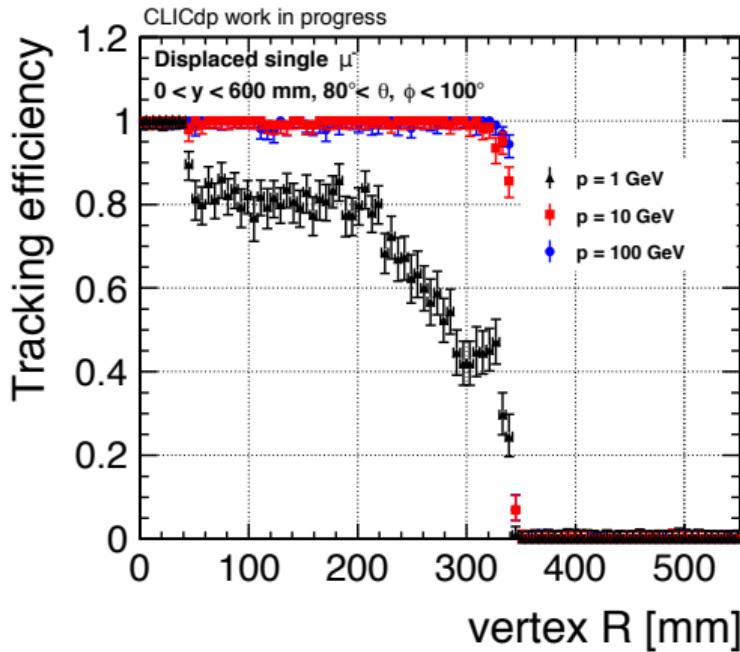
- ▶ Work done in Marlin (LC Framework) and LCIO EDM
- ▶ Based DD4hep/DDRec surface extension
- ▶ Kalman Filter track fit performed with KalTest
 - ▶ independent from the pattern recognition
 - ▶ DDKalTest: interface to DD4hep surfaces
- ▶ Helix prefix with 3 hits gives track state
 - ▶ first, middle, last
- ▶ Initialise fit with prefit parameters
- ▶ Kalman filter
 - ▶ hits added one by one
 - ▶ acceptance/rejected based on a χ^2 cut

Performance d_0 and p_T resolution for single μ



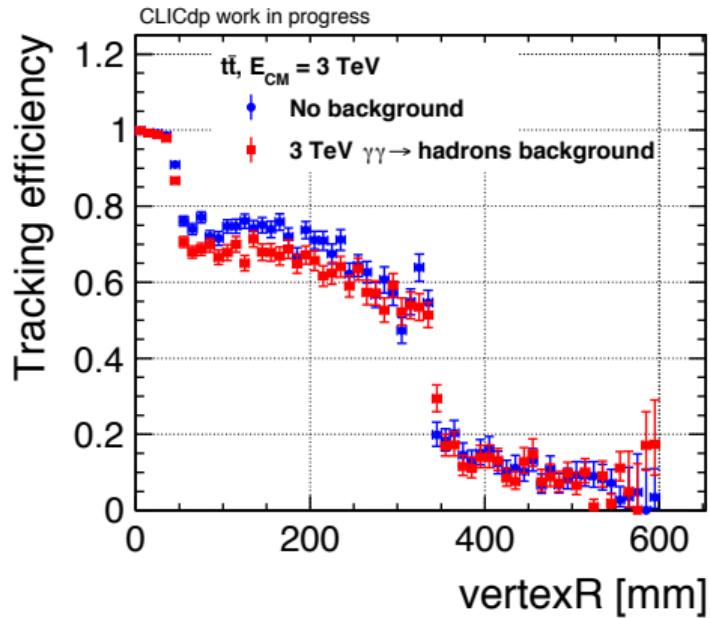
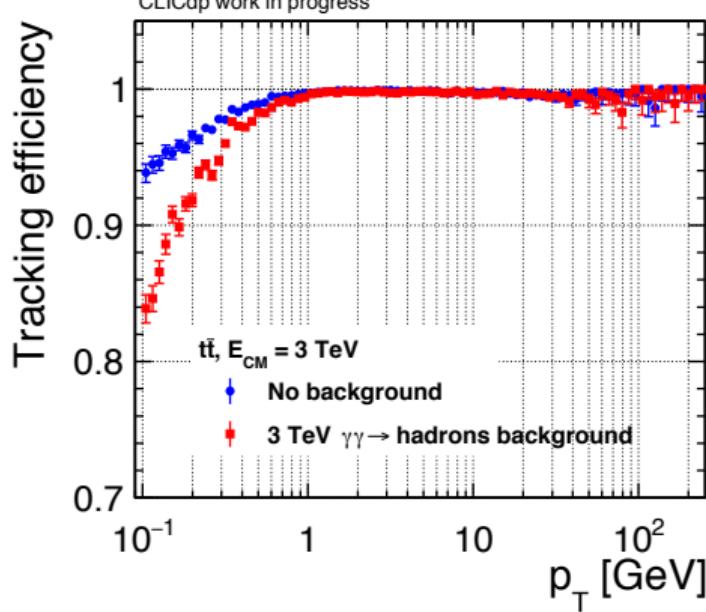
- In good agreement with target values of required performance

Efficiency for displaced single μ



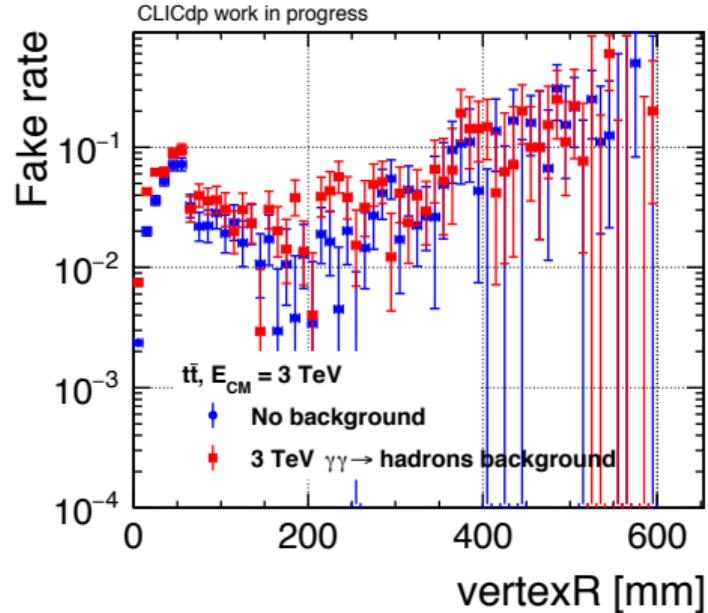
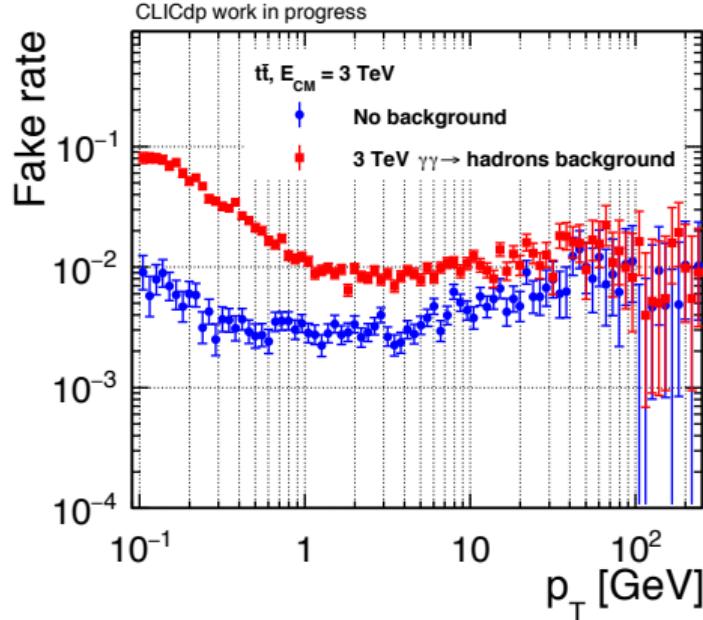
- Track generated uniformly along y axis with given opening angle

Efficiency for $t\bar{t}$ -bar @ 3 TeV



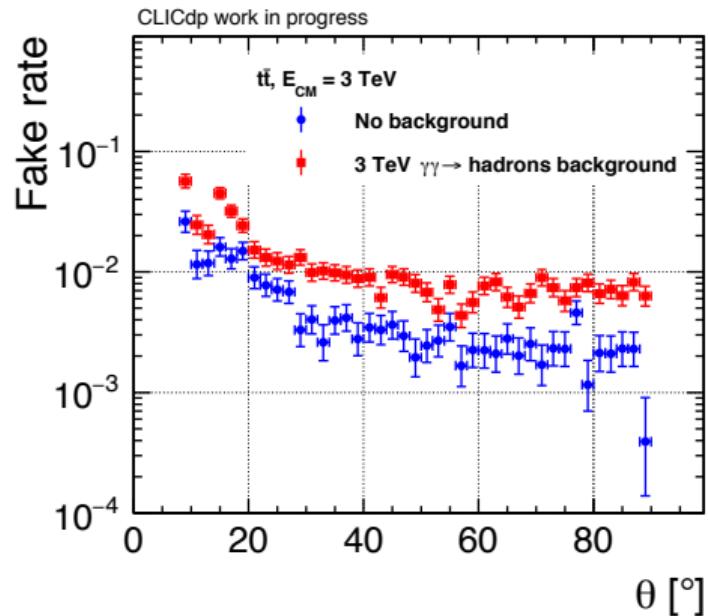
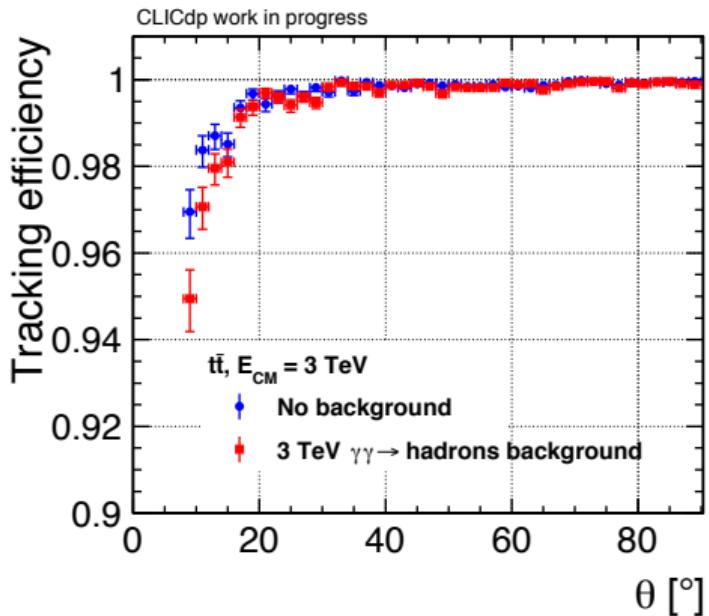
- Efficiency = pure reconstructed particles / reconstructable
 - pure = purity > 75% (hits belong to associated MC particles / total hits)
 - reconstructable = stable, $p_T > 0.1 \text{ GeV}$, unique hits ≥ 4

Fake rate for $t\bar{t}$ -bar @ 3 TeV



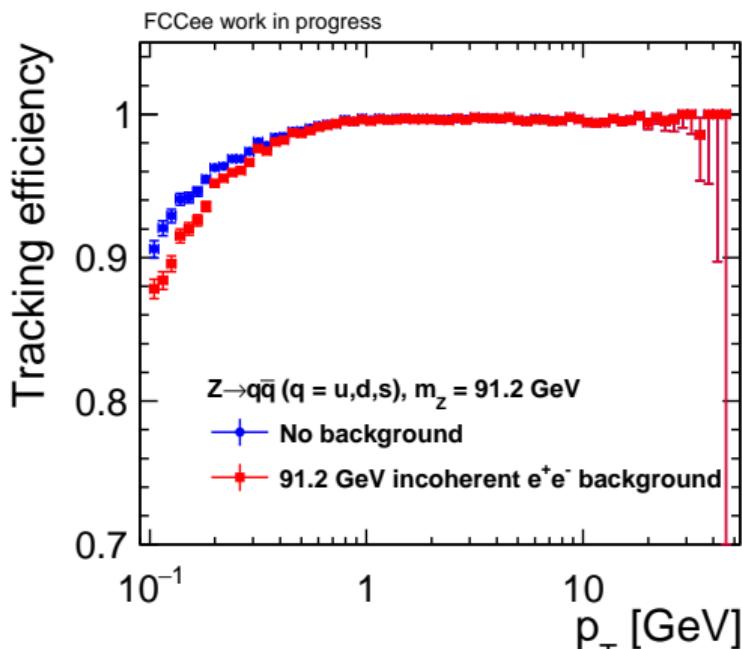
- ▶ Fake rate = impure reconstructed particles / reconstructed
 - ▶ fake = purity < 75% (hits belong to associated MC particles / total hits)

Efficiency and fake rate for $t\bar{t}$ -bar @ 3 TeV



- More performance plots <https://cds.cern.ch/record/2649437>

Works also with different geometry - FCCee



- Z bosons at rest decaying into light quarks
- background from e^+e^- pairs

- Works also with different detectors
e.g. FCCee CLD
- using [DD4hep Detector description](#)
- Smaller magnetic field $4T \rightarrow 2T$
- Larger tracker $1.5m \rightarrow 2.15m$
- smaller beam-pipe $29mm \rightarrow 15mm$
- adapting pattern recognition parameters

Summary

- ▶ ConformalTracking provides robust solution for pattern recognition
- ▶ Works in single particle as well as complex events
- ▶ Can cope successfully with beam induced backgrounds
- ▶ Perform well with displaced tracks
- ▶ Successfully handle different detector geometries
- ▶ github.com/iLCSoft/ConformalTracking/

BACKUP

CLIC and the European Strategy

- ▶ Formal European Strategy submissions
 - ▶ CLIC: Accelerator and Detector (arXiv:1812.07987)
 - ▶ CLIC: Physics Potential (arXiv:1812.07986)
- ▶ Yellow Reports
 - ▶ CLIC 2018 Summary Report (CERN-2018-005-M)
 - ▶ CLIC Project Implementation Plan (CERN-2018-010-M)
 - ▶ The CLIC potential for new physics (CERN-2018-009-M)
- ▶ Journal publications
 - ▶ Top-quark physics at the CLIC linear collider (arXiv:1807.02441)
 - ▶ Higgs physics at the CLIC electron-positron linear collider (arXiv:1608.07538)
- ▶ <https://clic.cern/european-strategy>

CLIC and the European Strategy

