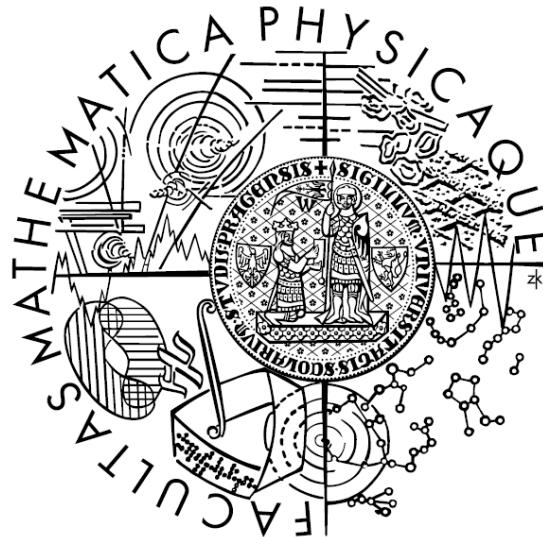


Faculty of Mathematics and Physics

**Multivariate analysis of decays of the Higgs boson
into pairs of tau leptons using the ATLAS detector
at the LHC**



Tomáš Kello

Supervisor of the master thesis: Mgr. Daniel Scheirich, Ph.D.

Institute of Particle and Nuclear Physics

Výjezdní seminář, Malá Skála, 2018

Content

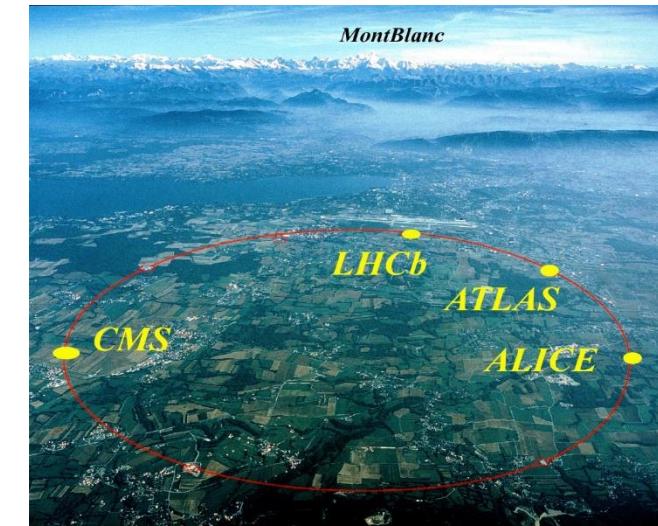
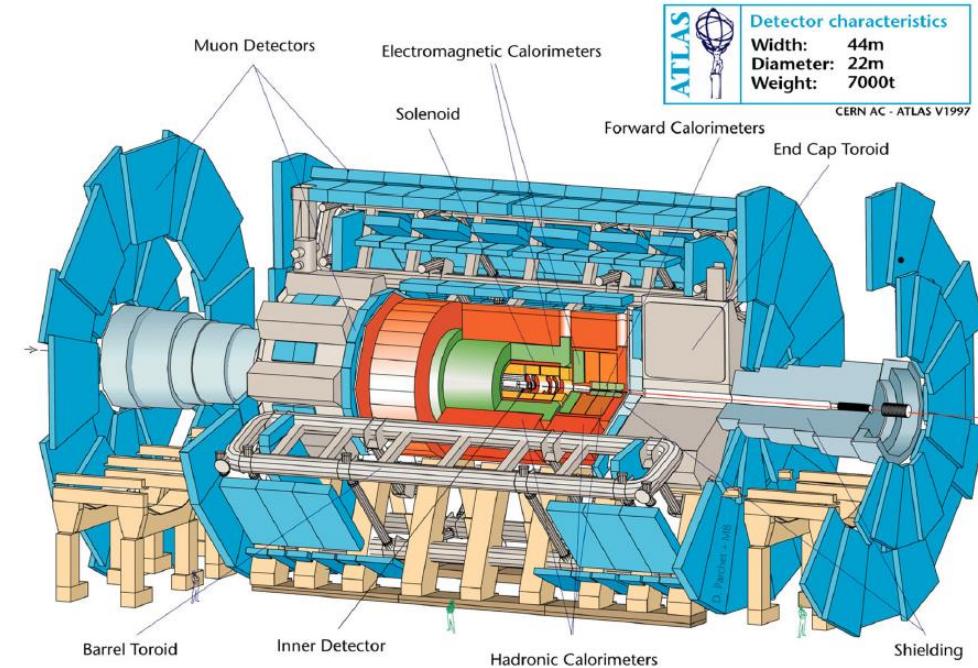
- 1) ATLAS detector subsystems
- 2) Higgs boson mechanism
- 3) Data & MC – preselection and categorisation
- 4) MVA – Boosted Decision Trees
- 5) BDT Training
- 6) Final BDT score cut

Content

- 1) ATLAS detector subsystems
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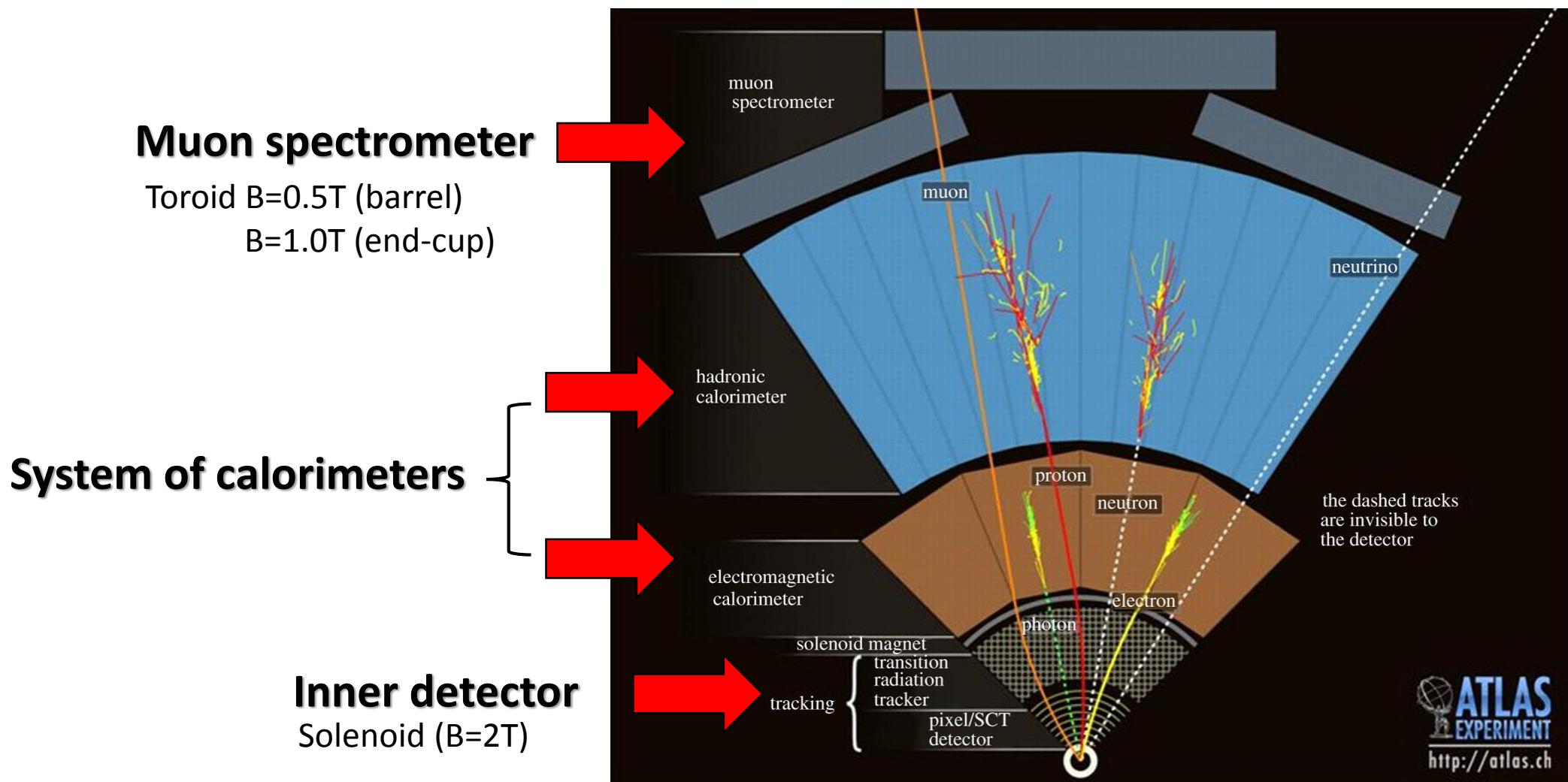
The ATLAS experiment at the LHC

- **Inner detector** (pixel detector, semiconductor tracker, transition radiation tracker, solenoid, $|\eta| < 2.5$)
- **Electromagnetic calorimeter** (absorber: lead layer, active medium: liquid argon, $|\eta| < 3.2$, FCal $3.1 < |\eta| < 4.9$)
- **Hadron calorimeter** (absorber: steel layer, active medium: liquid argon, $|\eta| < 4.9$),
- **Muon spectrometer** (monitored drift tube chambers, cathode strip chambers, thin gap chambers, toroid, $|\eta| < 2.7$),
- **Trigger** (75kHz -> 1kHz reduction, L1 (hardware), L2 + event filter (software))



The ATLAS experiment at the LHC

MET
←



Content

- 1) ~~ATLAS detector subsystems~~
- 2) Higgs boson mechanism
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Standard model. Elementary particles

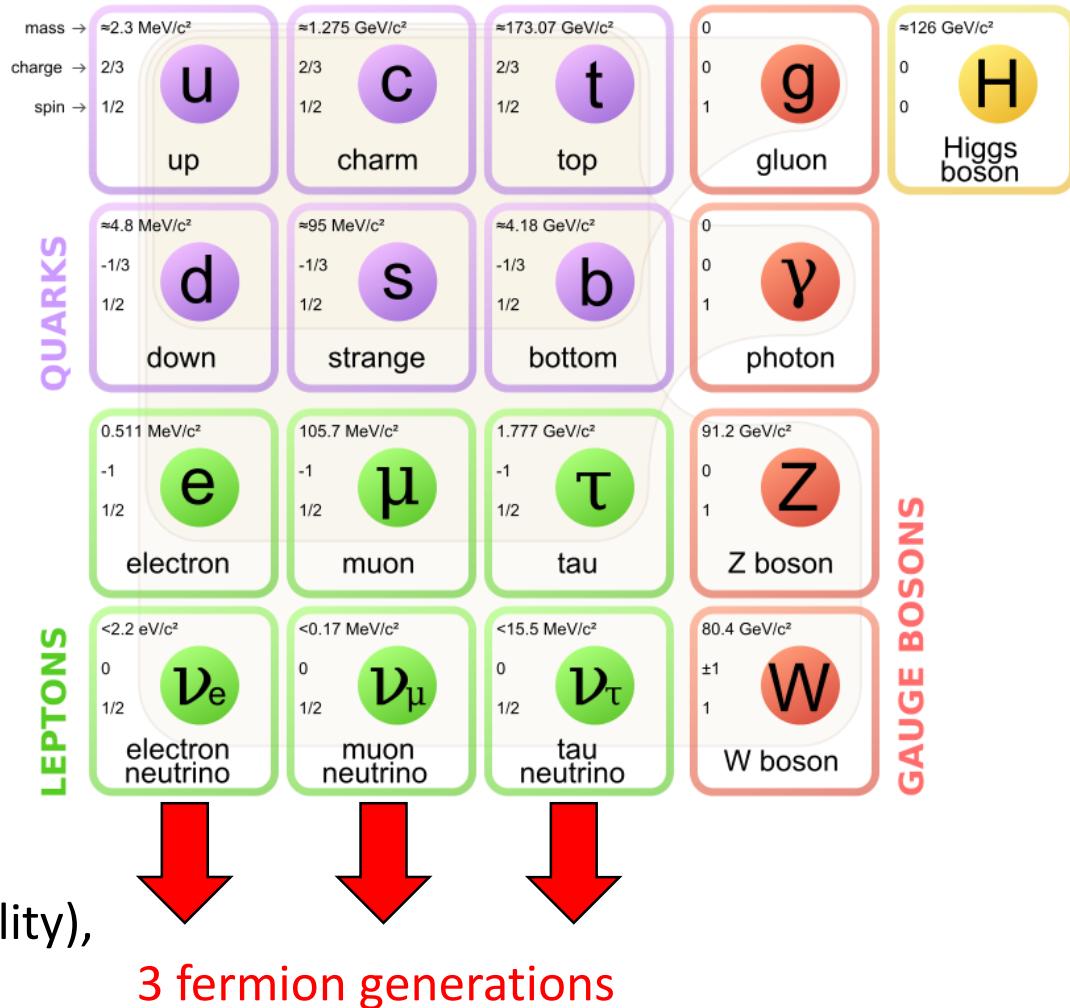
- **Fermions** (half-integer spin)

- quarks (u, d, c, s, t, b),
- leptons ($e, \nu_e, \mu, \nu_\mu, \tau, \nu_\tau$),

- **Bosons** (integer spin)

- gluon g (strong interaction),
- photon γ (electromagnetic interaction),
- W^\pm, Z^0 bosons (weak interaction),

- **Higgs boson H^0** (scalar particle (renormalizability),
neutral charge, spin 0)



Higgs mechanism

- **The minimal Higgs-Goldstone sector of EW theory**
 - 3 massive vector bosons + 1 physical scalar boson \Rightarrow 4 real scalar fields
 - $SU(2) \times U(1)$ gauge theory (1 complex weak isospin $SU(2)$ doublet; transformation properties under weak hypercharge $U(1)$)

$$\Phi = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix} = \begin{pmatrix} \varphi_1 + i\varphi_2 \\ \varphi_3 + i\varphi_4 \end{pmatrix}$$

- **The Goldstone model**

- $SU(2) \times U(1)$ symmetry requirement

$$\begin{aligned} \mathcal{L}_{\text{Goldstone}} &= (\partial_\mu \Phi^\dagger)(\partial^\mu \Phi) - V(\Phi) \\ V(\Phi) &= -\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2 \end{aligned}$$

μ ... mass dimension

λ ... dimensionless coupling constant

- space-time constant $\Phi \Leftrightarrow$ minimum of energy density for

$$\Phi_0^\dagger \Phi_0 = \frac{\nu^2}{2}$$

$$\nu = \frac{\mu}{\sqrt{\lambda}}$$

ν ... „vacuum value“

Higgs mechanism

- A deviation from the „vacuum value“

$$\Phi(x) = \exp\left(\frac{i}{v}\pi^a(x)\tau^a\right) \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v + H(x)) \end{pmatrix}$$

„angular“ shifted „radial“
variable variable

$H(x)$... massive Higgs field
 $\pi^a(x)$... Goldstone boson representatives
 τ^a ... Pauli matrices

- mass term appears with a correct sign, Goldstone bosons become massless

$$\mathcal{L} = \text{kin. terms} + \text{interactions} - \lambda v^2 H^2 \quad \Leftrightarrow \quad m_H^2 = 2\lambda v^2 \quad m_\pi = 0$$

- $SU(2) \times U(1)$ local symmetry requirement $\Rightarrow U$ -gauge

$$\Phi_U(x) = \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v + H(x)) \end{pmatrix}$$

Higgs mechanism

- The U -gauge Higgs Lagrangian

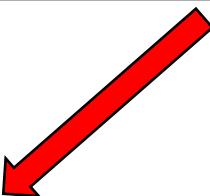
A_μ^a ... Yang-Mills fields corresponding to $SU(2)$
 B_μ ... Yang-Mills fields corresponding to $U(1)$
 Y ... weak hypercharge
 g, g' ... coupling constants

$$\mathcal{L}_{Higgs}^{(U)} = \Phi_U^\dagger \left(\bar{\partial}_\mu + ig A_\mu^a \frac{\tau^a}{2} + ig' Y B_\mu \right) \left(\bar{\partial}_\mu - ig A^{b\mu} \frac{\tau^b}{2} - ig' Y B^\mu \right) \Phi_U - \lambda \left(\Phi_U^\dagger \Phi_U - \frac{v^2}{2} \right)^2 + \text{kin. + selfinter.}$$

...

$$\mathcal{L}_{Higgs}^{(U)} = \frac{1}{2} \partial_\mu H \partial^\mu H - \lambda v^2 H^2 - \lambda v H^3 - \frac{1}{4} \lambda H^4 + \frac{1}{8} (\nu + H)^2 (g^2 A_\mu^a A^{a\mu} - 4Ygg' A_\mu^3 B^\mu + 4Y^2 g'^2 B_\mu B^\mu)$$

$$Z_\mu = \frac{1}{\sqrt{g^2 + g'^2}} (g A_\mu^3 - g' B_\mu) \quad Y = \frac{1}{2}$$



$$\mathcal{L}_{mass}^{(IVB)} = \frac{1}{4} g^2 v^2 W_\mu^- W^{+\mu} + \frac{1}{8} (g^2 + g'^2) v^2 Z_\mu Z^\mu$$

$$m_W = \frac{1}{2} g v$$

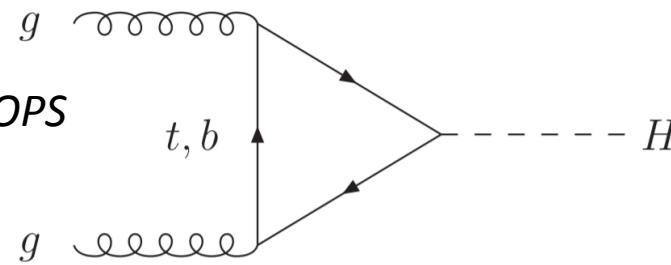
$$m_Z = \frac{1}{2} v \sqrt{(g^2 + g'^2)}$$

Higgs production

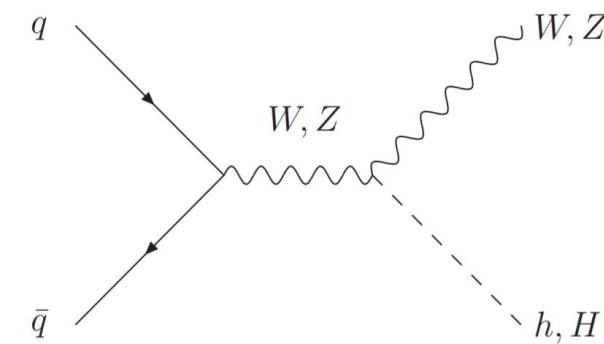
PDG 2016, [9]: $m_{H_0} \doteq (125.09 \pm 0.24)\text{GeV}$

ggF (gluon-gluon fusion)

PowhegNNLOPS



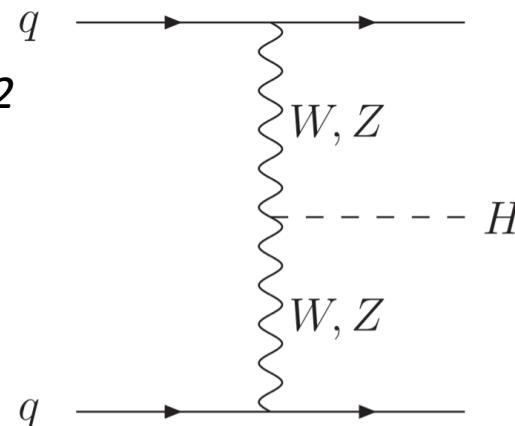
Higgs Strahlung VH



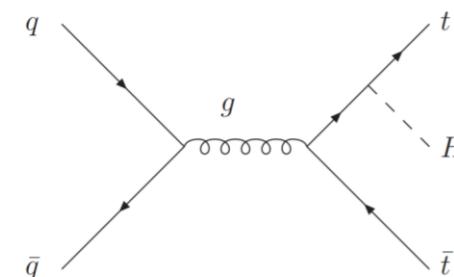
Powheg Box2
(NLO)

VBF (vector-boson fusion)

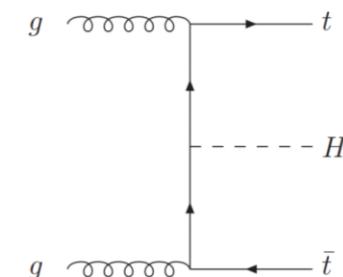
Powheg Box2
(NLO)



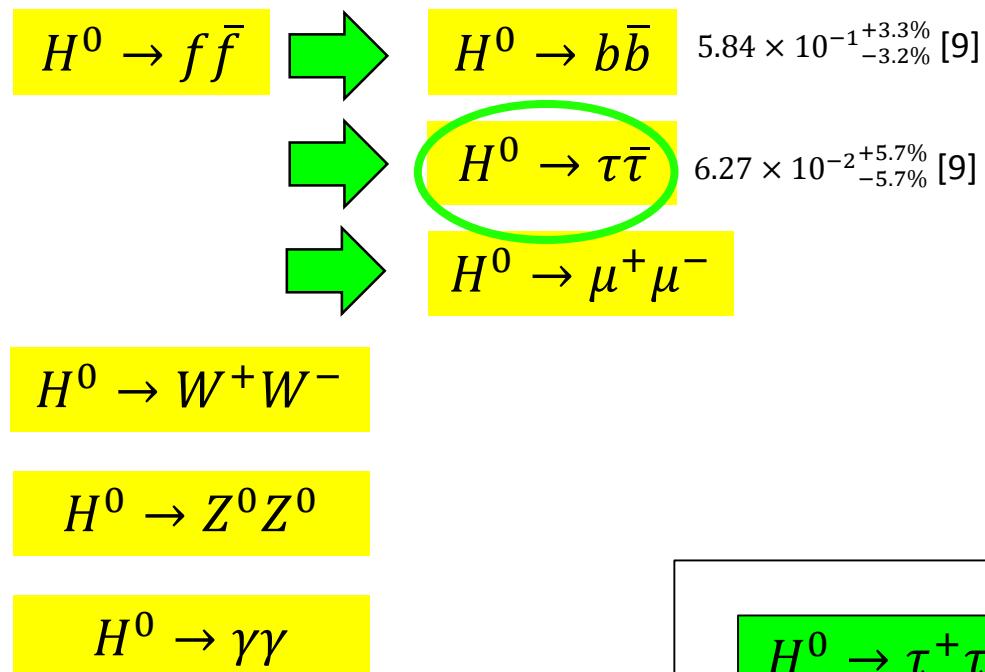
$t\bar{t}H$ production



MG5_aMC@NLO
v2.2.2

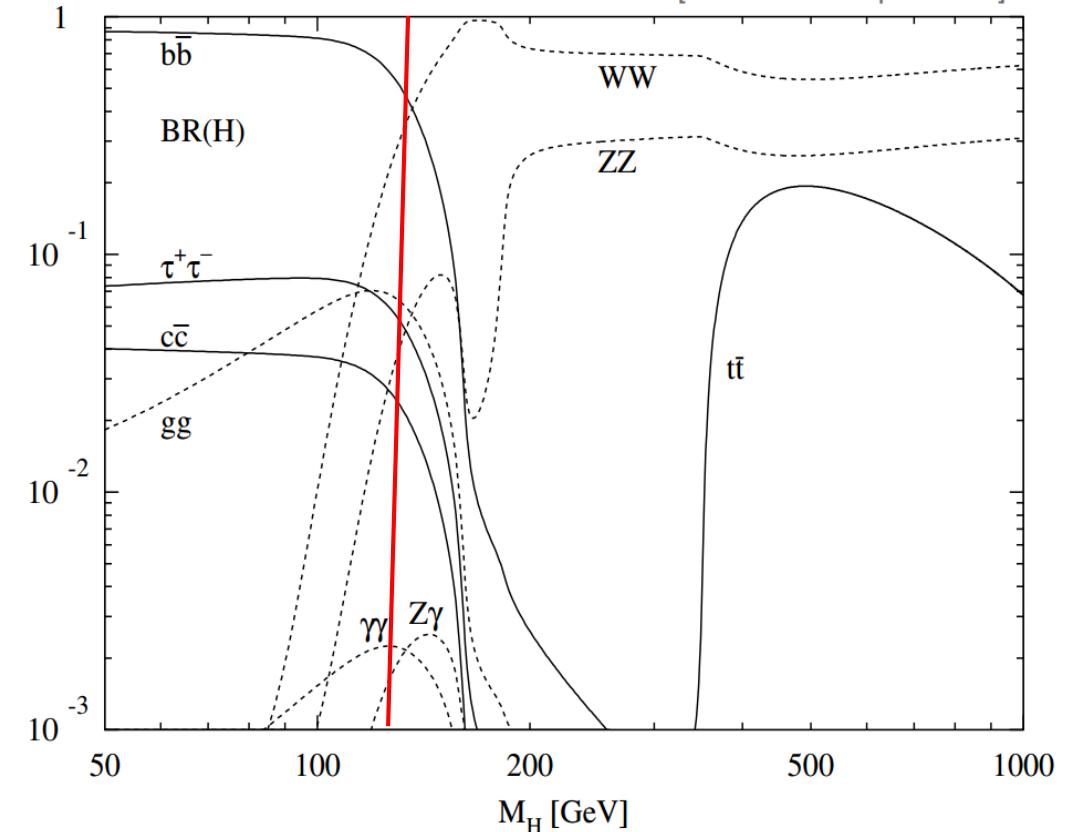


Higgs decay modes



...

$H^0 \rightarrow \tau^+\tau^- \rightarrow l^+\bar{\nu}l^-\bar{\nu}\nu$
 $\sqrt{s} = 13 \text{ TeV}$
integrated luminosity = 36.2 fb^{-1}
Run 2 (2015 & 2016)



$$\begin{aligned} DF &= e\mu \\ SF &= ee/\mu\mu \end{aligned}$$

Content

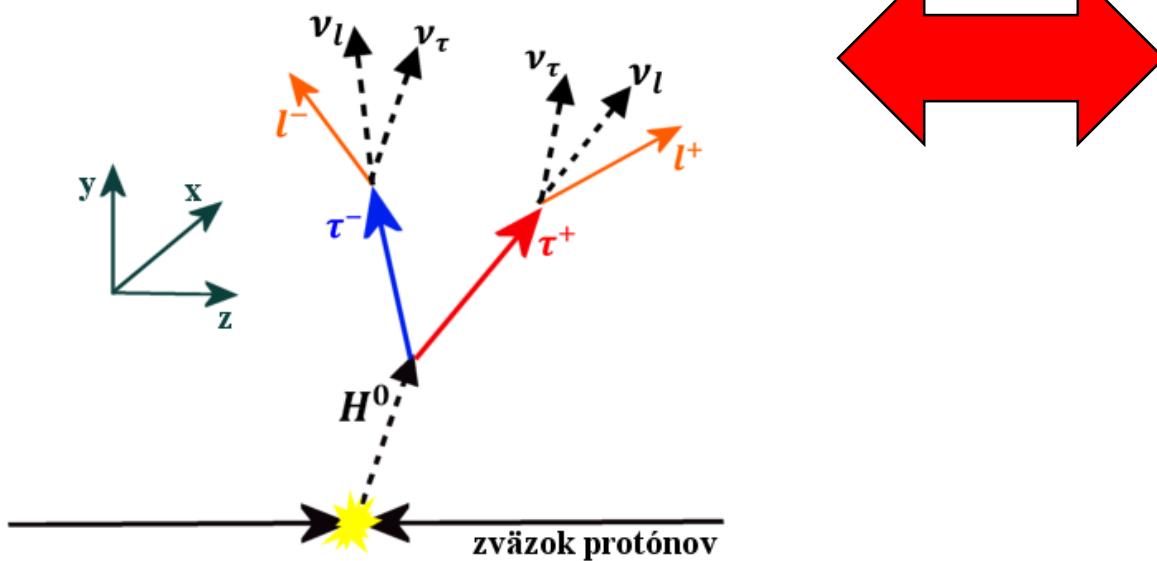
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Data&MC

Signal

$$H^0 \rightarrow \tau^+ \tau^- \rightarrow l^+ \bar{\nu} \nu l^- \bar{\nu} \nu$$

- ggF
- VBF
- VH
- tt>H



Background

- $pp \rightarrow Z^0 \rightarrow \tau^+ \tau^-$,
- $pp \rightarrow Z^0 \rightarrow e^+ e^-$,
- $pp \rightarrow Z^0 \rightarrow \mu^+ \mu^-$,
- $pp \rightarrow t\bar{t}$,
- „single top“,
- $pp \rightarrow W^\pm \rightarrow l^\pm \nu_l$,
- „diboson decays“

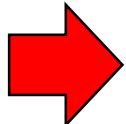
Sherpa 2.2.1

- jet associated W/Z production
- VBF Z production
- diboson

Powheg-Box v2 & Powheg-Box v1 NLO

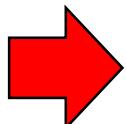
- $t\bar{t}$ & single top

Data&MC



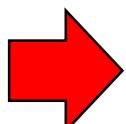
Object reconstruction requirements

- primary vertices
- electrons, muons
- jets
- missing transversal energy E_T^{miss}



Trigger selection

- Single electron/Single muon p_T threshold
- Di-electron/Di-muon/electron-muon p_T threshold



Preselection requirements

- number of leptons
- opposite charge
- lepton (medium) gradient isolation criteria
- ...

$\tau_{lep}\tau_{lep}$ preselection criteria

$m_{\tau\tau}^{coll} < m_Z - 25 \text{ GeV}$	
SF	DF
$30 < m_{ll} < 75 \text{ GeV}$	$30 < m_{ll} < 100 \text{ GeV}$
$E_T^{miss} > 55 \text{ GeV}$	$E_T^{miss} > 20 \text{ GeV}$

$$p_T^{jet1} > 40 \text{ GeV}$$

$$N_{b-jets} = 0$$

VBF

$$p_T^{jet2} > 30 \text{ GeV}$$

Boosted

not VBF

$$|\eta_{jj}| > 3$$

$$p_T^{\tau\tau} > 100 \text{ GeV}$$

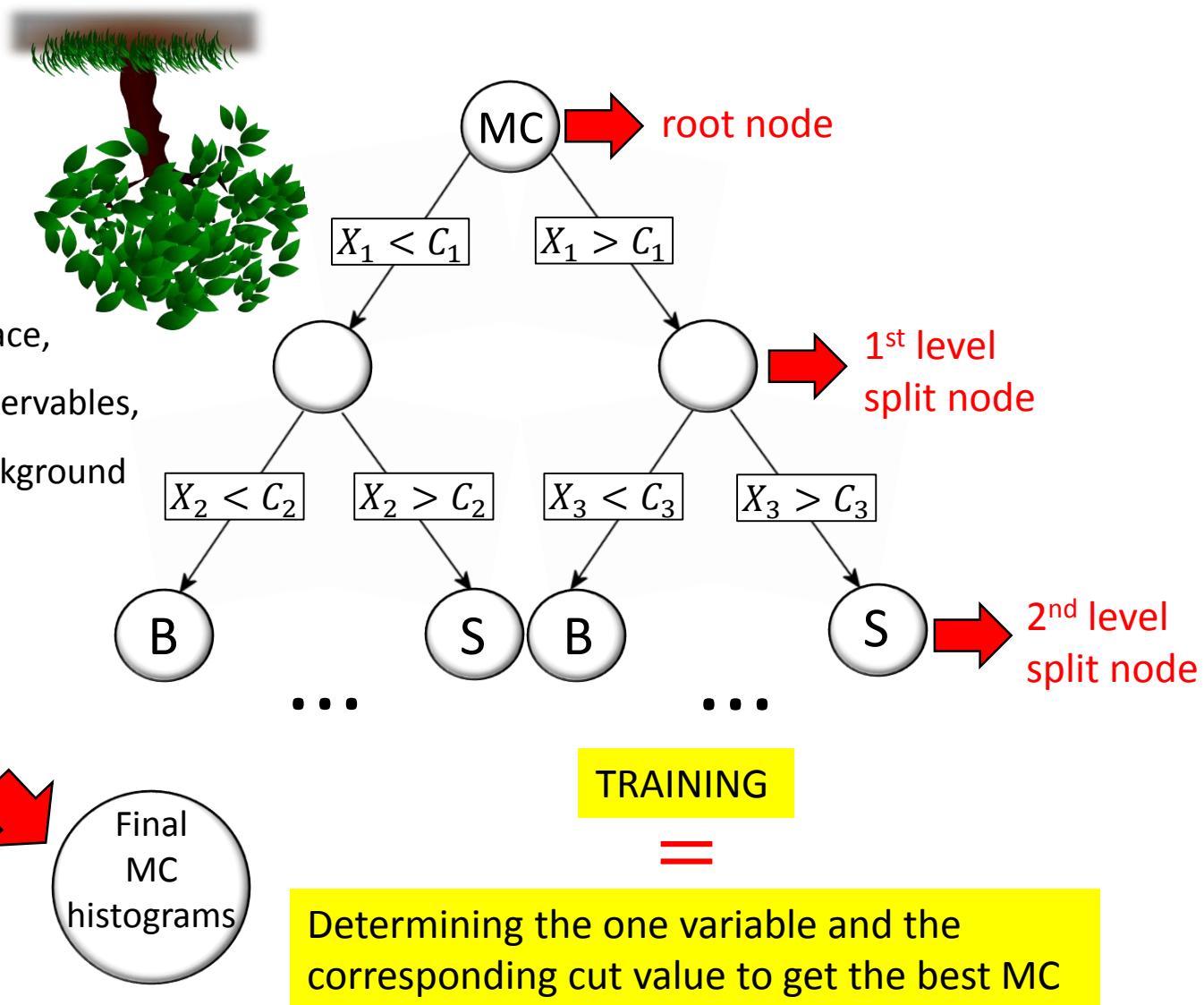
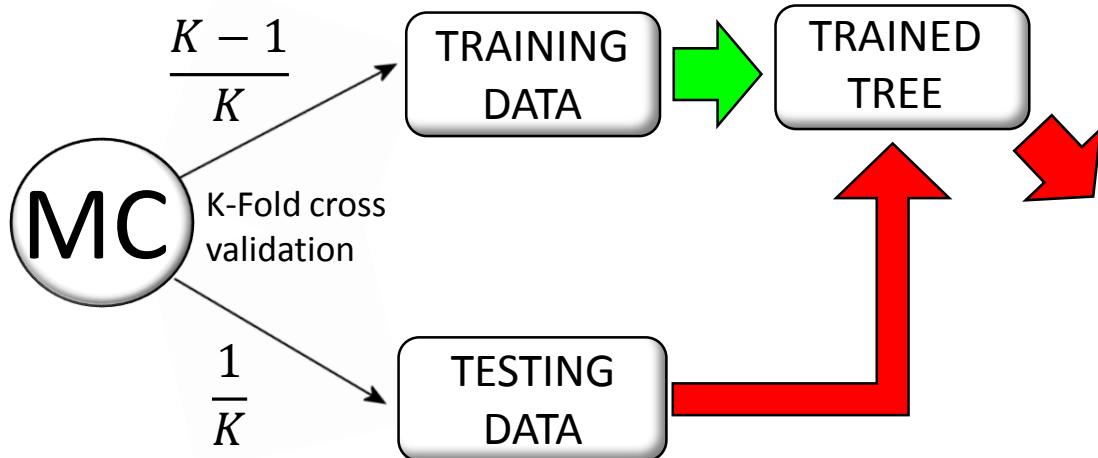
$$m_{jj} > 400 \text{ GeV}$$

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Decision Tree

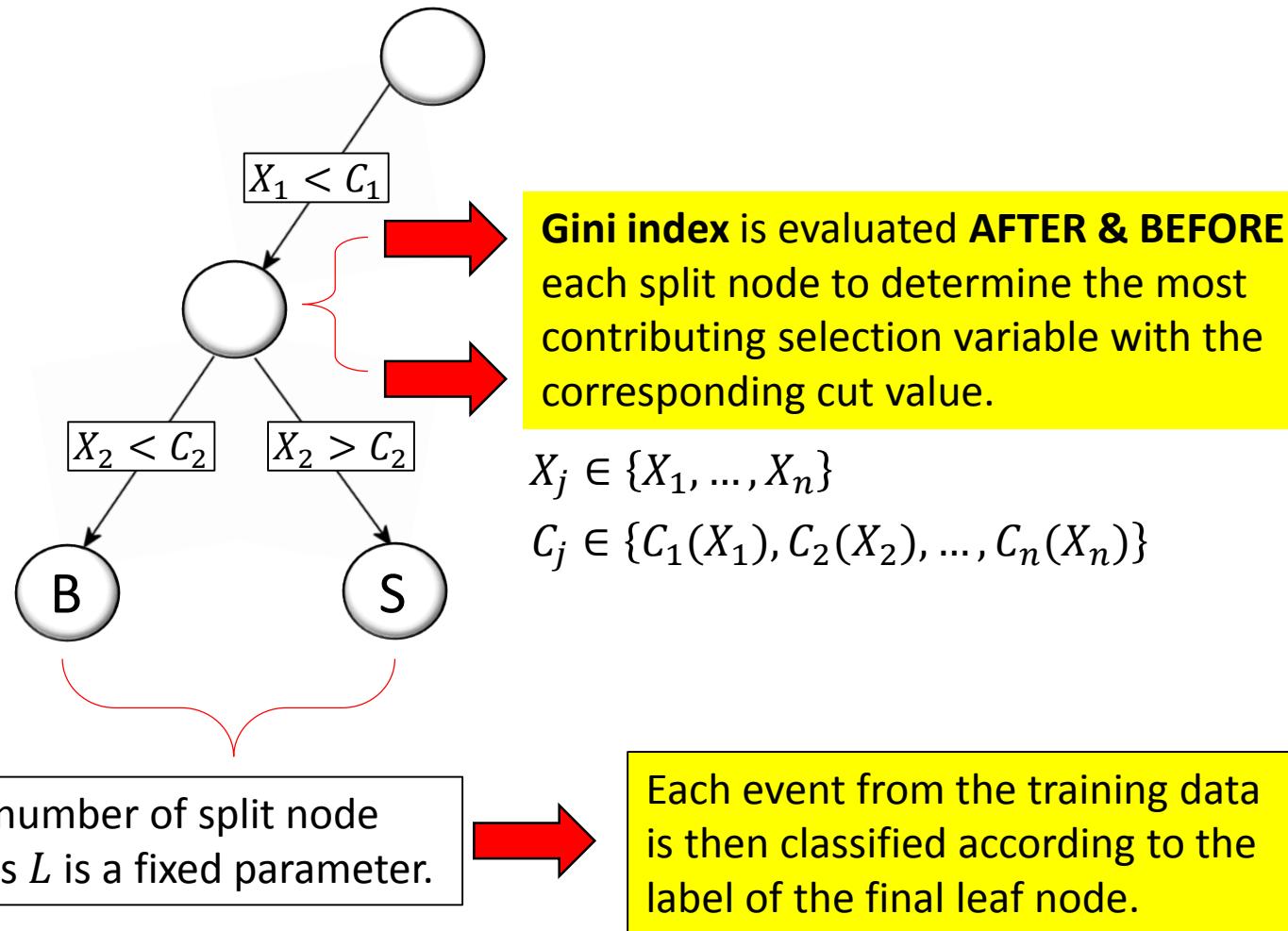
- multivariate classification algorithm,
- operates within a multi-dimensional observable space,
- more sophisticated non sequential approach to observables,
- Task: **to maximize a figure of merit** of signal vs. background selection.



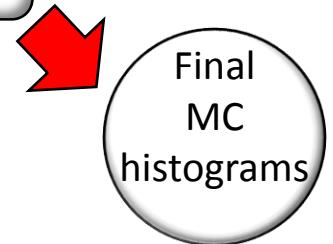
$$X_j \in \{X_1, \dots, X_n\}$$

$$C_j \in \{C_1(X_1), C_2(X_2), \dots, C_n(X_n)\}$$

Training algorithm



TRAINED
TREES



$$\text{Gini index} = p(1 - p)$$

$$\text{purity} \dots p = \frac{N_S}{N}$$

the difference of Gini indices is being maximized $(G_L - G_{L-1})_{max}$

Boosted Decision Tree

(Gradient Boost)

- **sequential method** – learning from the mistakes of previous classifiers
- **tree ensemble model construction**

$$F(x; P) = \sum_{m=1}^M \beta_m f(x; a_m) \quad P \in \{\beta_m; a_m\}_0^M$$

$f(x; a_m)$... weak classifiers x ... testing sample
 P ... parameters y ... training sample

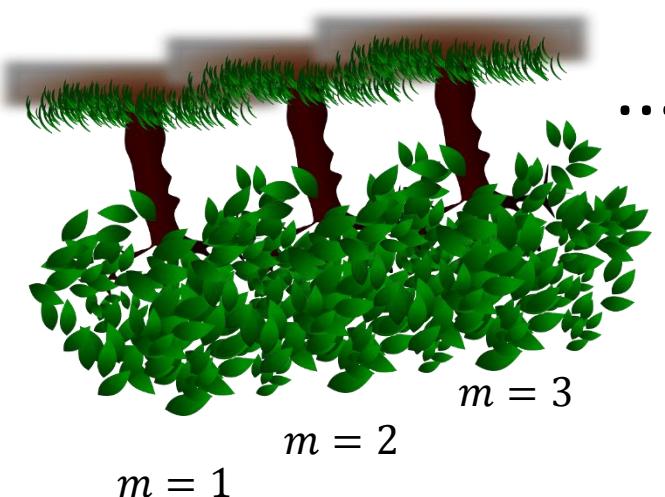
- **loss function minimization**

basic $L(F(x), y) = (F(x) - y)^2$

gradient $L(F(x), y) = \ln(1 + e^{-2F(x)y})$

- executed by loss function **gradient calculation**

$$F(x) \approx F(x) + k \frac{\delta L(F(x), y)}{\delta F(x)}$$



M number of trees in the forest

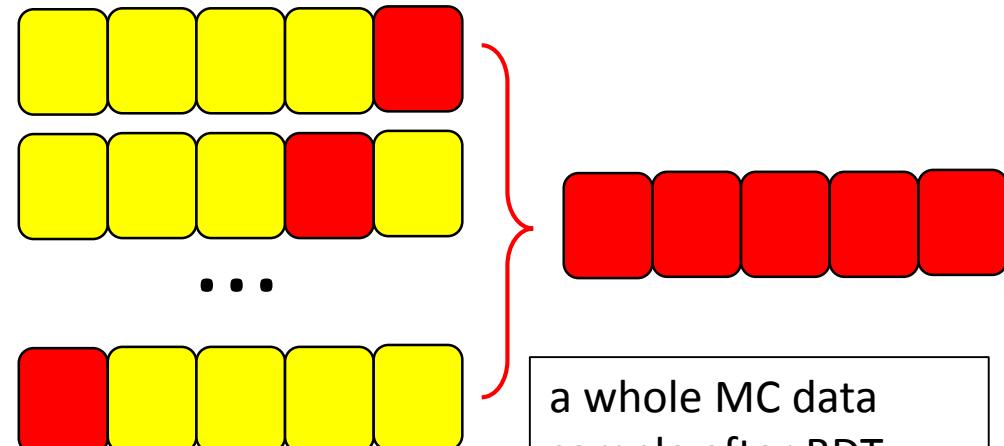
K-Fold cross validation (K=5)



Training data



Testing data

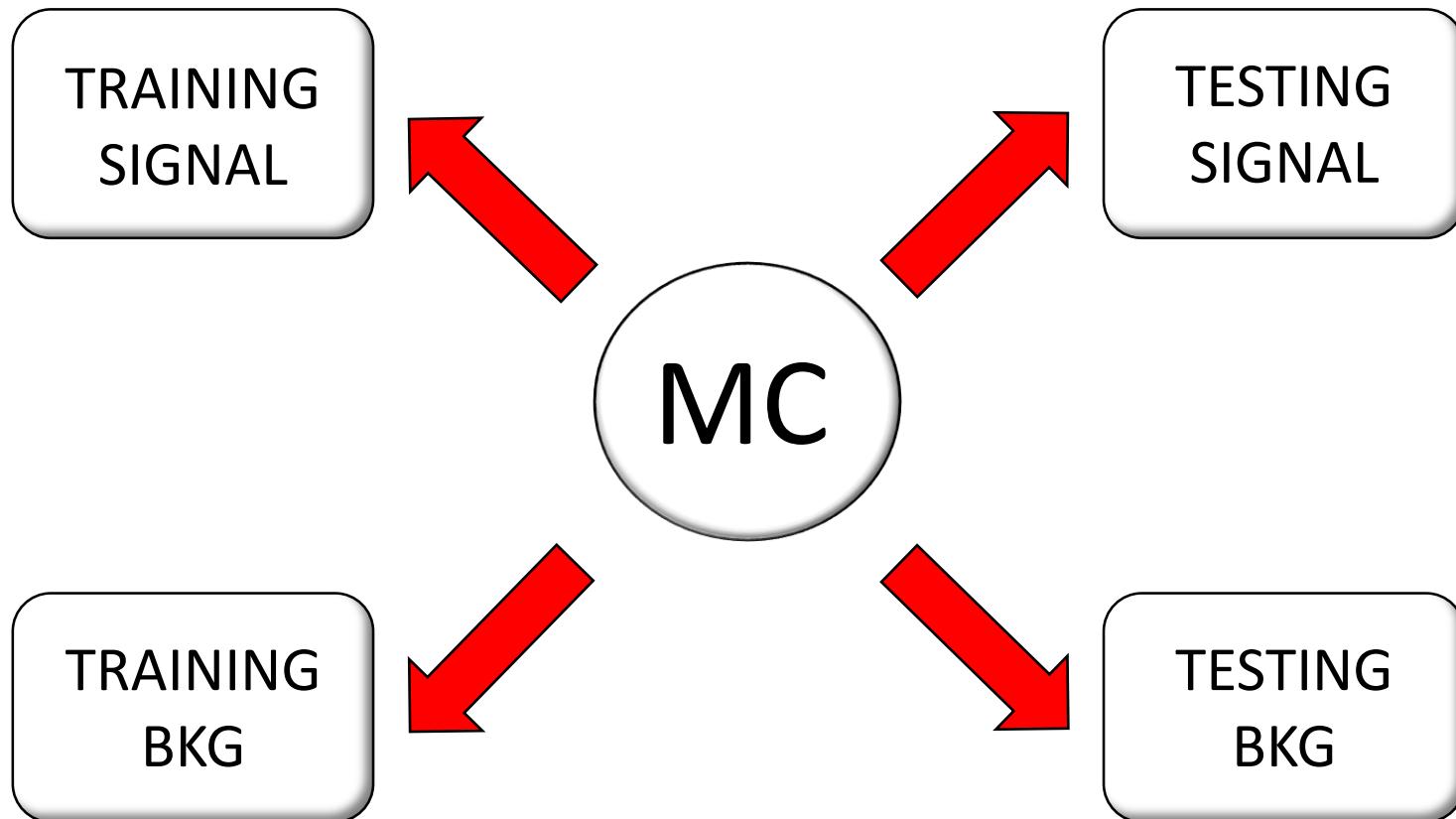


a whole MC data sample after BDT selection

Content

- 1) ~~ATLAS detector subsystems~~
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- 4) ~~MVA – Boosted Decision Trees~~
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- 6) Final BDT score cut

BDT training – splitting data randomly

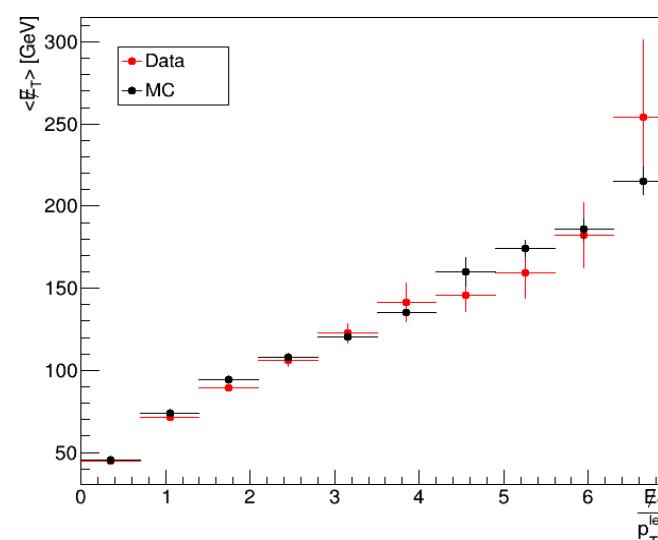
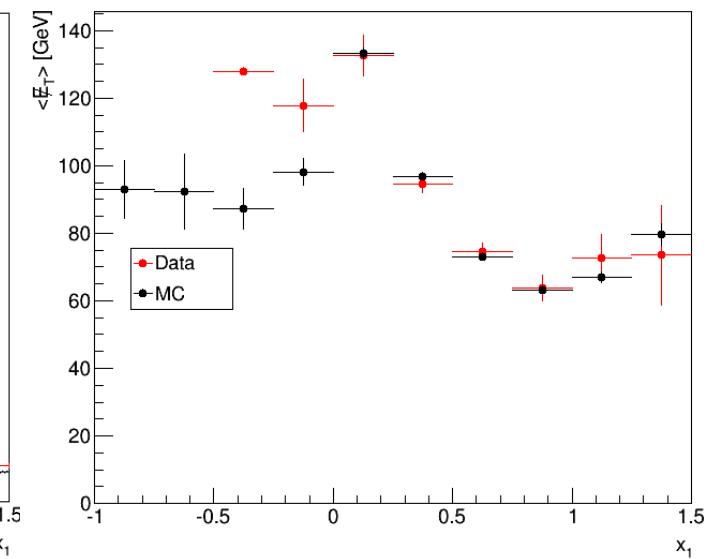
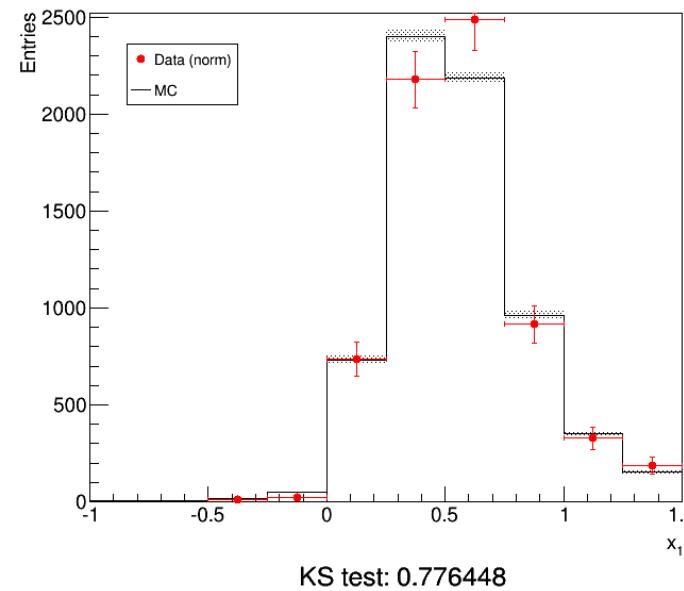
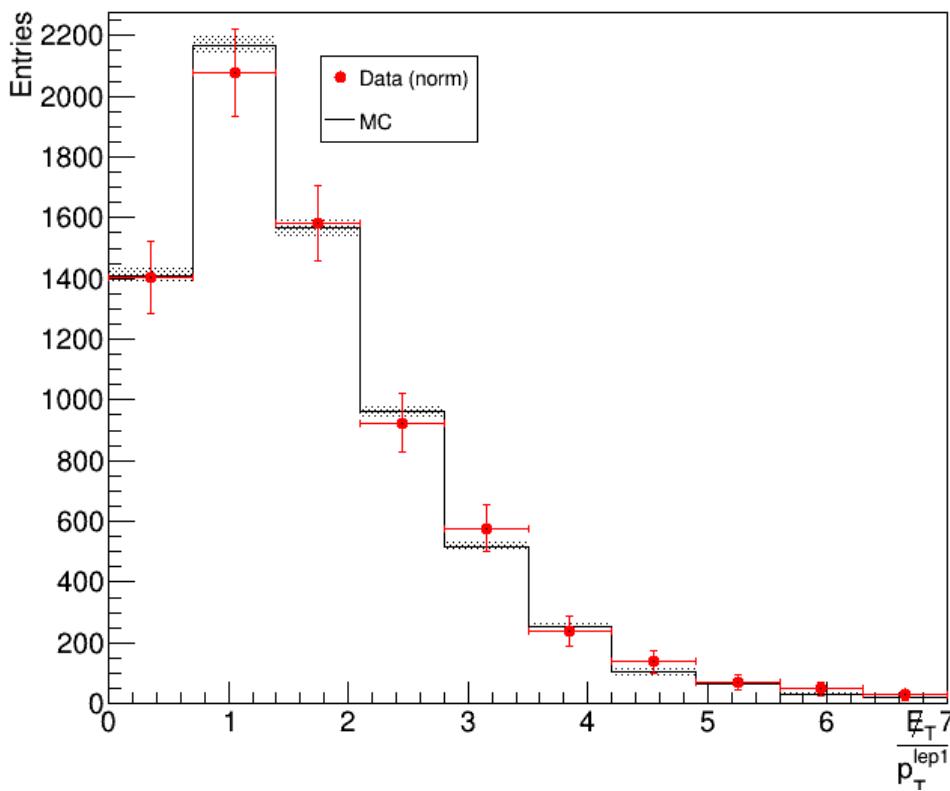
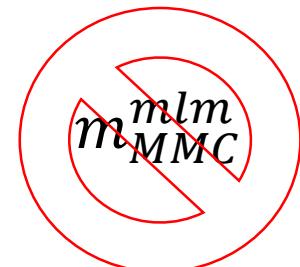


BDT training – DQ and variables selection

KS test: 0.000000

Starter Pack Selection

- Boosted SF – 34 variables
- Boosted DF – 34 variables
- VBF SF – 40 variables
- VBF DF – 40 variables

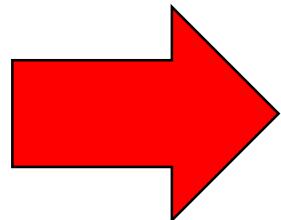


NONE was excluded

BDT training – DQ and variables selection

Starter Pack Selection

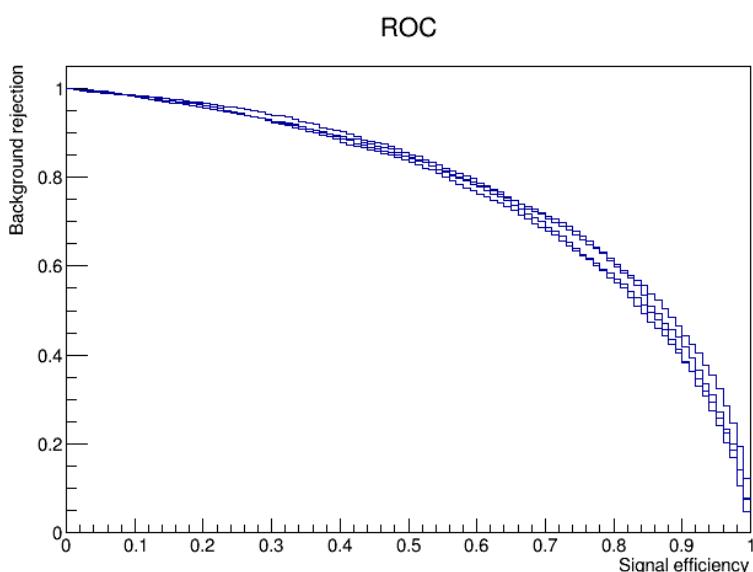
- Boosted SF – 34 variables
- Boosted DF – 34 variables
- VBF SF – 40 variables
- VBF DF – 40 variables



Final List of Variables

VBF

Boosted



SF

- E_T^{miss}
- m_{ll}, m_{jj}
- $p_T^{\text{jet1}}, p_T^{\text{jet2}}$
- p_T^{tot}
- $m_{ll,\text{jet1}}$
- $m_{l1,l2,j1}, m_{l1,l2,j2}$
- x_1, x_2
- $\min \Delta\eta(l_1, l_2, \text{jets})$
- $\min \Delta R(l_2, \text{jets})$
- ΔR_{ll}
- $N(\text{jets} > 30\text{GeV})$
- $E_T^{\text{miss}}/p_T^{\text{lep2}}$

DF

- E_T^{miss}
- m_{ll}, m_{jj}
- $m_T^{\text{lep1}}, m_T^{\text{lep2}}$
- $p_T^{\text{jet1}}, p_T^{\text{jet2}}$
- p_T^{tot}
- $m_{l1,l2,j2}$
- $\min \Delta\eta(l_1, l_2, \text{jets})$
- ΔR_{ll}
- $N(\text{jets} > 30\text{GeV})$
- $E_T^{\text{miss}}/p_T^{\text{lep1}}$
- $E_T^{\text{miss}}/p_T^{\text{lep2}}$

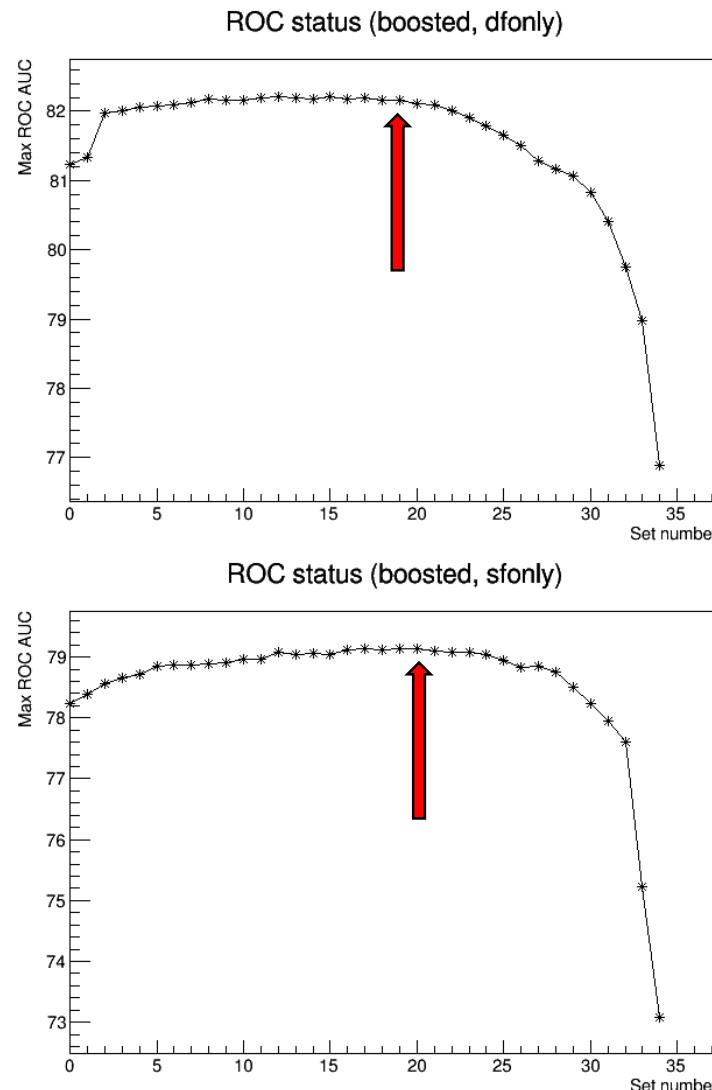
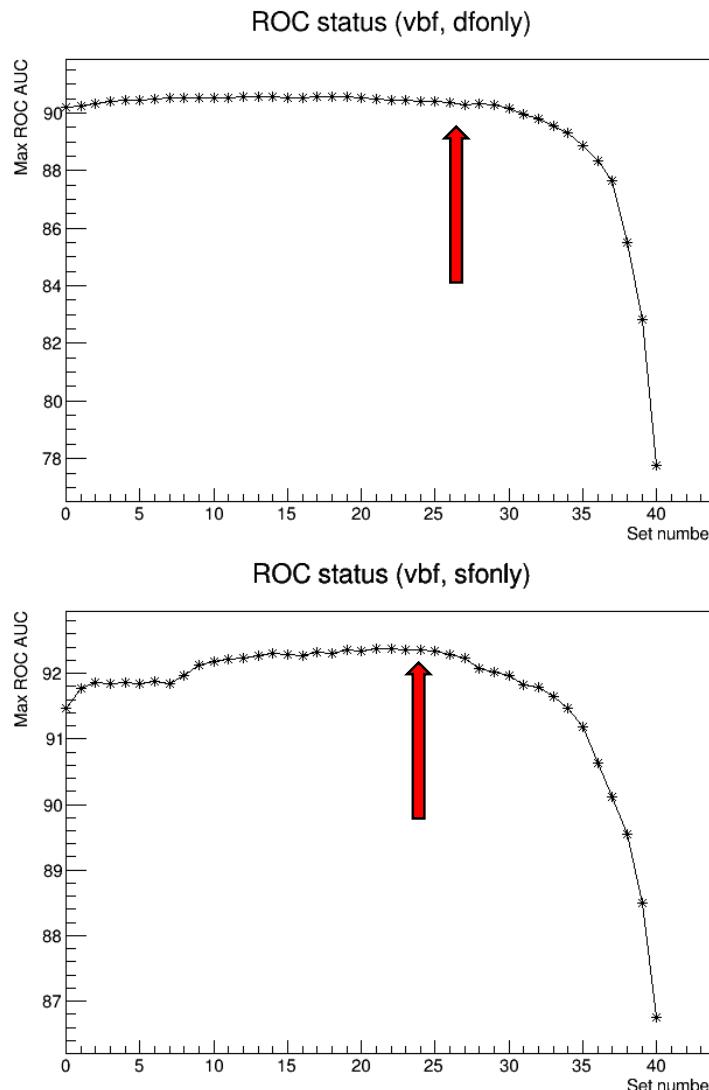
SF

- m_{ll}, m_{jj}
- p_T^{jet2}
- p_T^{tot}
- $m_{ll,\text{jet1}}$
- $m_{T,\text{lep1}}$
- x_1, x_2
- η_{ll}
- Sphericity*

DF

- m_{ll}
- $p_T^{\text{jet1}}, p_T^{\text{jet2}}$
- p_T^{tot}
- $m_{ll,\text{jet1}}, m_{l1,l2,j1}$
- $m_{T,\text{lep1}}$
- x_1, x_2
- p_T^{Higgs}
- Sphericity*
- ΔR_{ll}
- $E_T^{\text{miss}}/p_T^{\text{lep1}}$
- $E_T^{\text{miss}}/p_T^{\text{lep2}}$

BDT training – DQ and variables selection



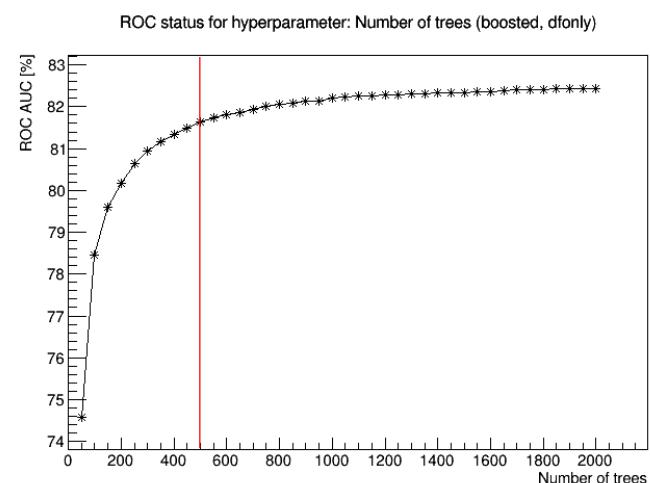
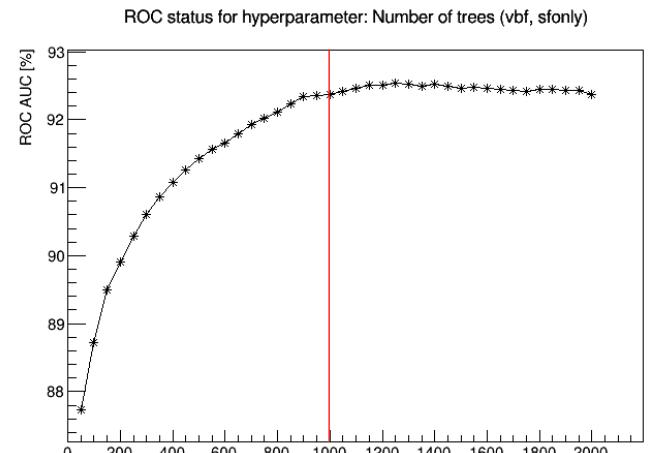


BDT training – Hyperparameters optimization

	BOOSTED		VBF	
	SF	DF	SF	DF
number of trees	400	550	1000	250
tree depth	3	5	3	3
minimum node size	6%	7%	3.5%	6%
shrinkage	0.3	0.2	0.3	0.3

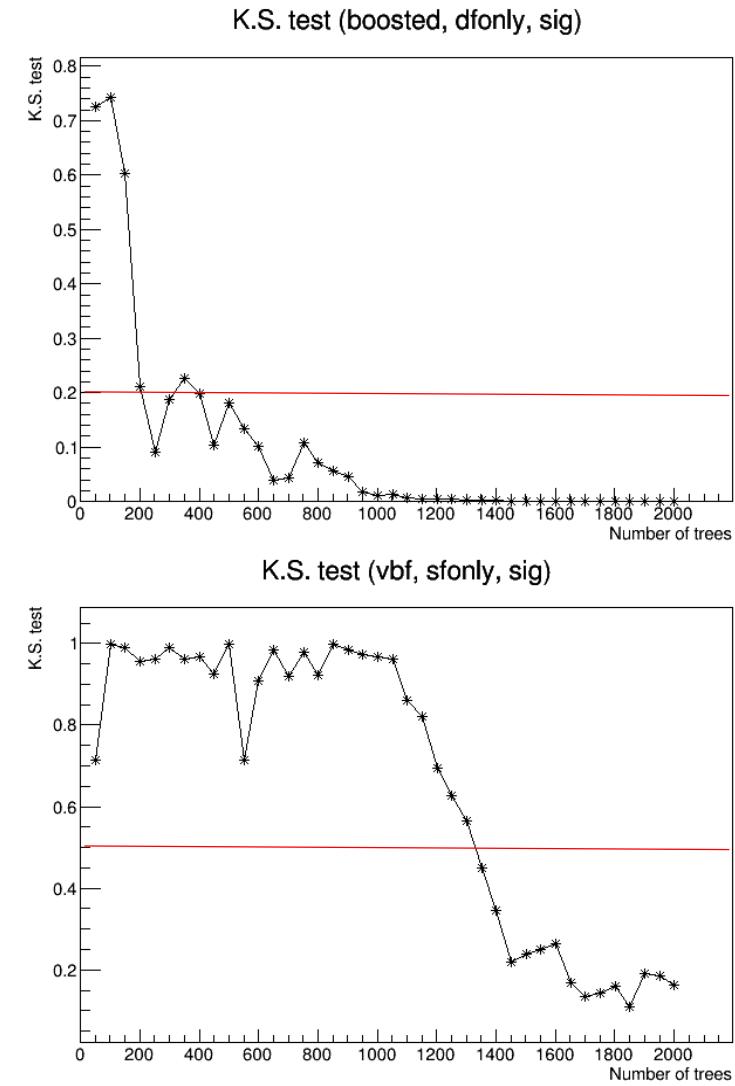
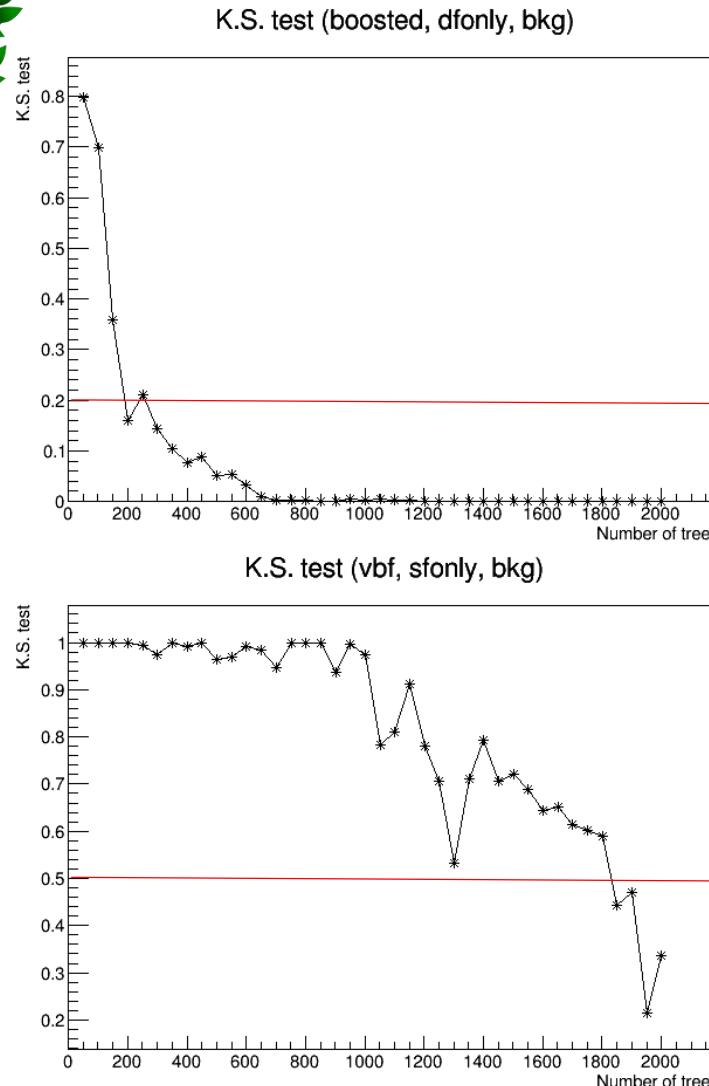
Other parameters

number of selection cuts per node $N_C = 20$
negative weights treatment: we have **PRAYed**
pre-training transformation: **Gauss**





BDT training – Hyperparameters optimization



Content

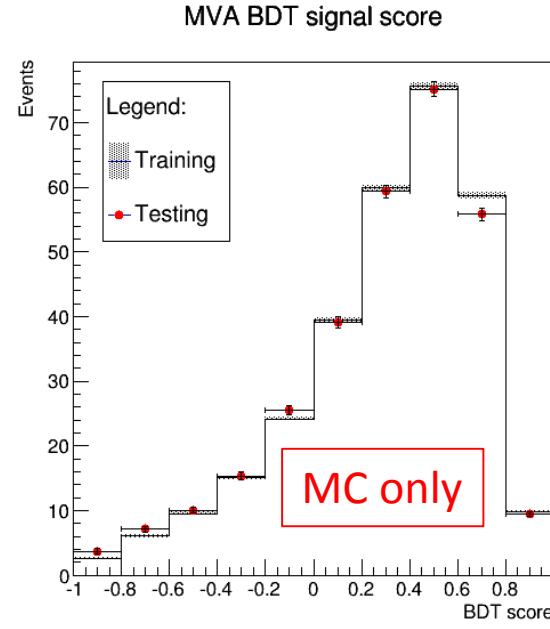
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BDT score

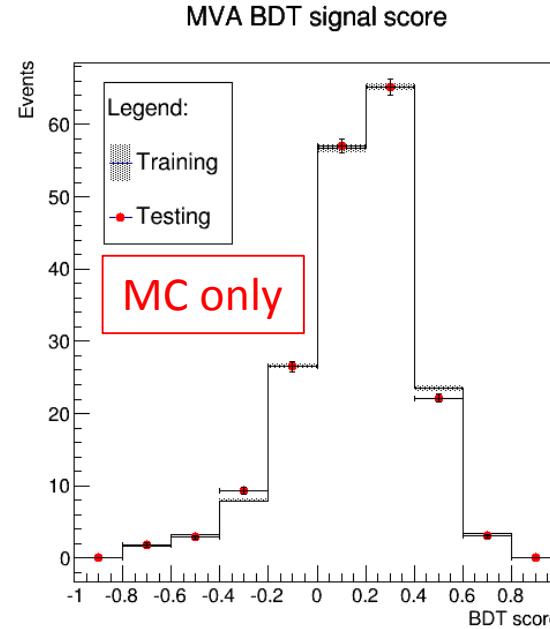
Workflow

- trigger selection and preselection
- MC modelling profiles
- variables reduction
- BDT hyperparameter optimization
- overtraining test
- **BDT score calculation (event by event – testing data)**
- **the best BDT score cut – the best SIG vs. BKG separation**

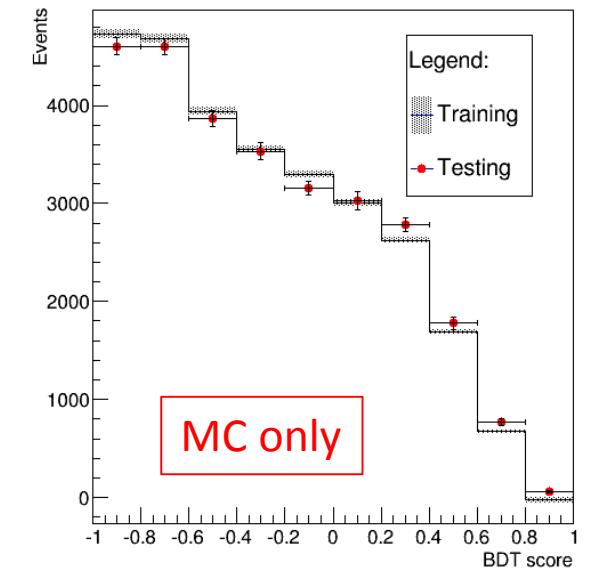
Boosted
DF



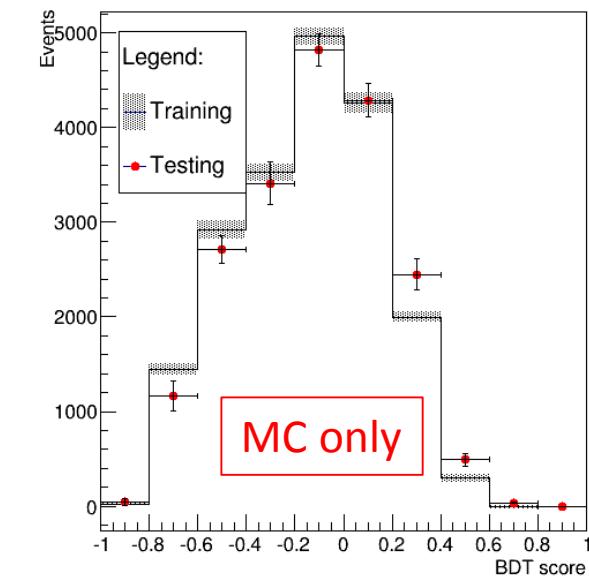
Boosted
SF



MVA BDT background score



MVA BDT background score



BDT score

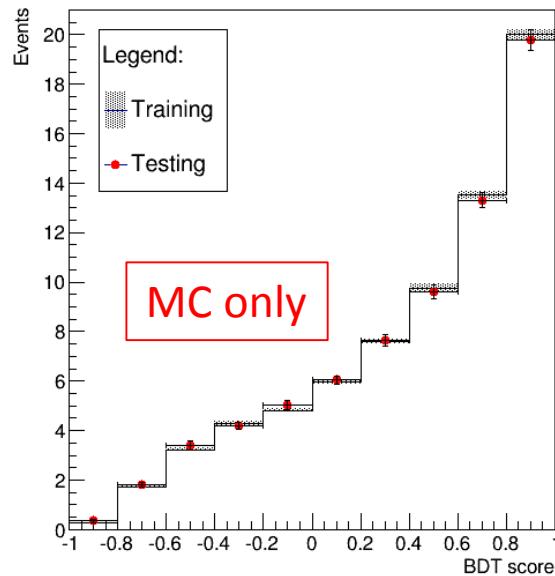
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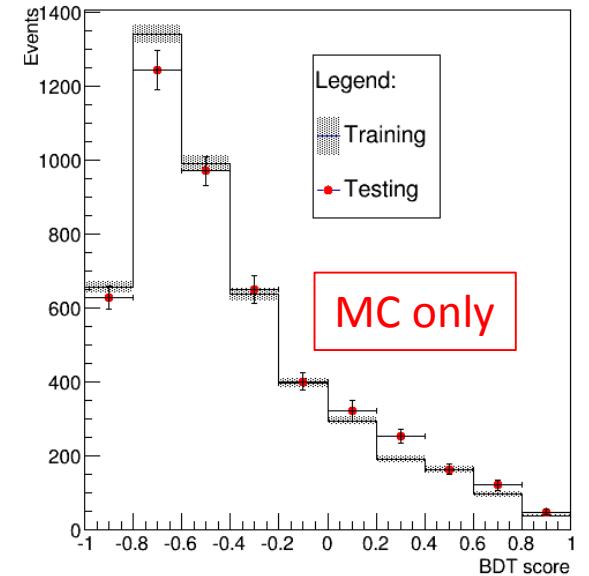
VBF
DF

VBF
SF

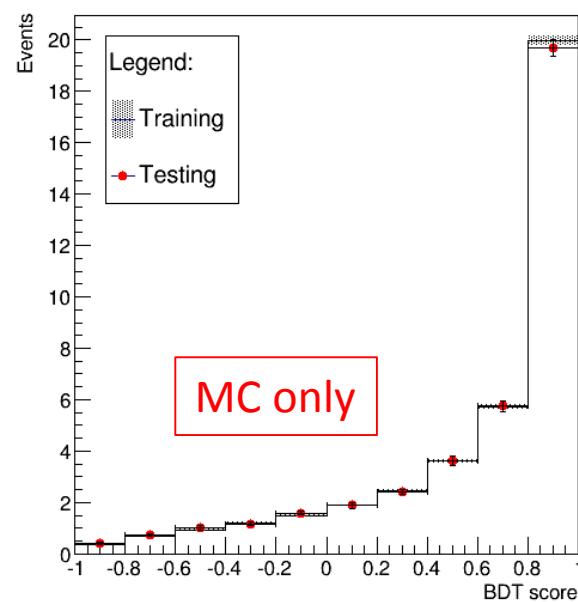
MVA BDT signal score



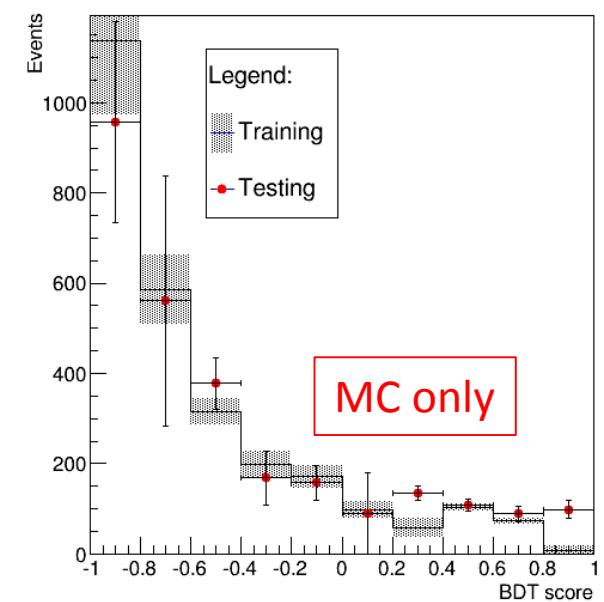
MVA BDT background score



MVA BDT signal score



MVA BDT background score

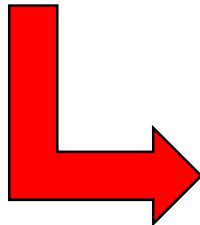


BDT score

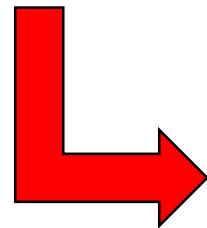
+1

-1

Definition: Likelihood estimation of event being signal or background



the better BDT cut – the better SIG/BKG selection



determined by calculation of
Expected significance Z

Profile Likelihood Ratio

Express how likely it is, that expected signal has
outreached background noises only by chance

Significance estimation

Systematic errors

- Theoretical systematics
 - signal cross section uncertainties (higher order corrections)
 - ggH + 1 or 2 exclusive jets (QCD corrections)
 - background acceptances (higher order corrections)
 - PDFs uncertainties
 - parton shower distribution
- Experimental systematics
 - triggering efficiencies
 - object identification and reconstruction uncertainties
 - energy scale
 - luminosity uncertainties
- Background modelling
 - $Z \rightarrow \tau\tau$ control region
 - shape of the $m_{\tau\tau}^{MMC}$ distribution
 - Shape and normalization of the fake-lepton background

BDT score

Final BDT selection and Significance (expected)

	BDT score >	$Z_{expected}$
Boosted SF	-0.1	0.18
Boosted DF	-1.0	0.42
VBF SF	0.6	0.44
VBF DF	0.8	0.88

$$Z_{combined}^{expected} = 1.16$$

Summary

Final BDT selection and Significance (expected)

	BDT score >	$Z_{expected}$
Boosted SF	-0.1	0.18
Boosted DF	-1.0	0.42
VBF SF	0.6	0.44
VBF DF	0.8	0.88

MVA BDT $\tau_{lep}\tau_{lep}$ $Z_{expected}^{combined} = 1.16$

Cut based $\tau_{lep}\tau_{lep}$ $Z_{expected}^{combined} = 1.18$

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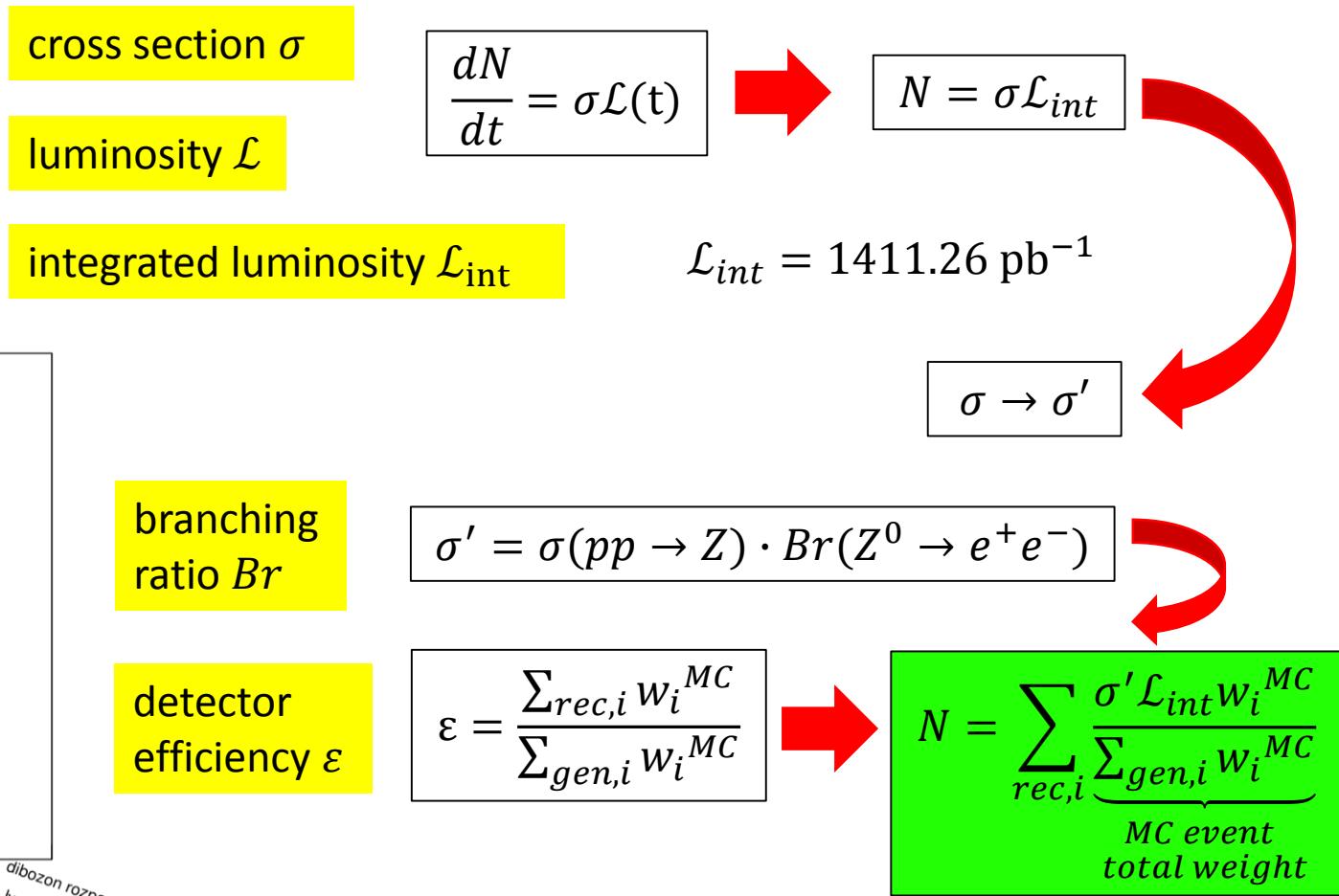
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Appendices

Monte Carlo simulation

- signal + background,
- various processes \leftrightarrow various weights,
- perturbative method



Appendices – Preselection (2016)

Trigger selection

- $p_T^e > 15 \text{ GeV}$,
- $p_T^\mu > 10 \text{ GeV}$,
- $|\eta| < 2.47$,

Quality of lepton reconstruction

- purity \leftrightarrow reconstruction efficiency

Lepton isolation

- „free isolation“ $\varepsilon = \frac{N_{iso,lep}}{N_{lep}} = 99\%$,

Invariant mass

- $m_{ll} < 100 \text{ GeV } (l_1 \neq l_2)$,
- $m_{ll} < 80 \text{ GeV } (l_1 = l_2)$,

Charge conservation, dilepton decays

pseudorapidity η

$$\eta = -\ln \left(\tan \frac{\theta}{2} \right)$$

θ polar angle

invariant mass

$$m_{ll}^2 = (E_1 + E_2)^2 - (\vec{p}_1 + \vec{p}_2)^2$$

E_i, \vec{p}_i lepton energy and momentum

Appendices – Preselection (2016)

Collinear approximation

$$H^0 \rightarrow \tau^+ \tau^- \rightarrow l^+ \bar{\nu} l^- \bar{\nu}$$

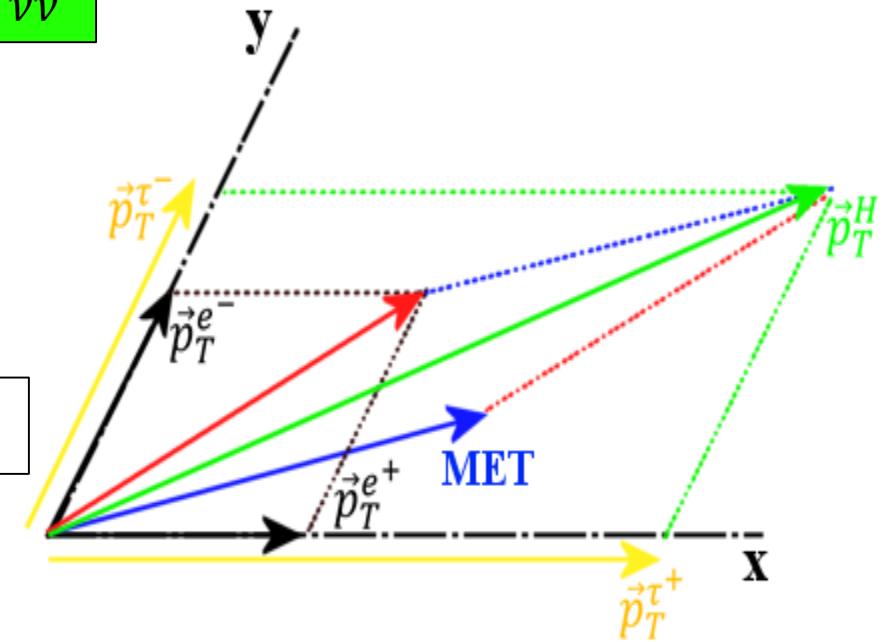
- neutrino flight direction \approx lepton direction ($m_H \gg m_\tau$),
- ν, l, τ mass neglected,
- azimuthal angle between leptons $\cos \phi > -1$,



$$m_{coll}^2 = (\vec{p}_{l,1} + \vec{p}_{\nu,1} + \vec{p}_{l,2} + \vec{p}_{\nu,2})^2 - (\vec{p}_{l,1} + \vec{p}_{\nu,1} + \vec{p}_{l,2} + \vec{p}_{\nu,2})^2$$

- leads to excluding of non physical event reconstruction

$$x_1 = \frac{p_T^{l_1}}{p_T^{\tau_1}} \quad x_2 = \frac{p_T^{l_2}}{p_T^{\tau_2}} \quad x_{1,2} \in (0,1)$$



H^0 mass reconstruction with respect to the collinear approx.

MET ... missing energy transversal