

Influence of proton bunch and plasma parameters on the AWAKE experiment

Mariana Moreira

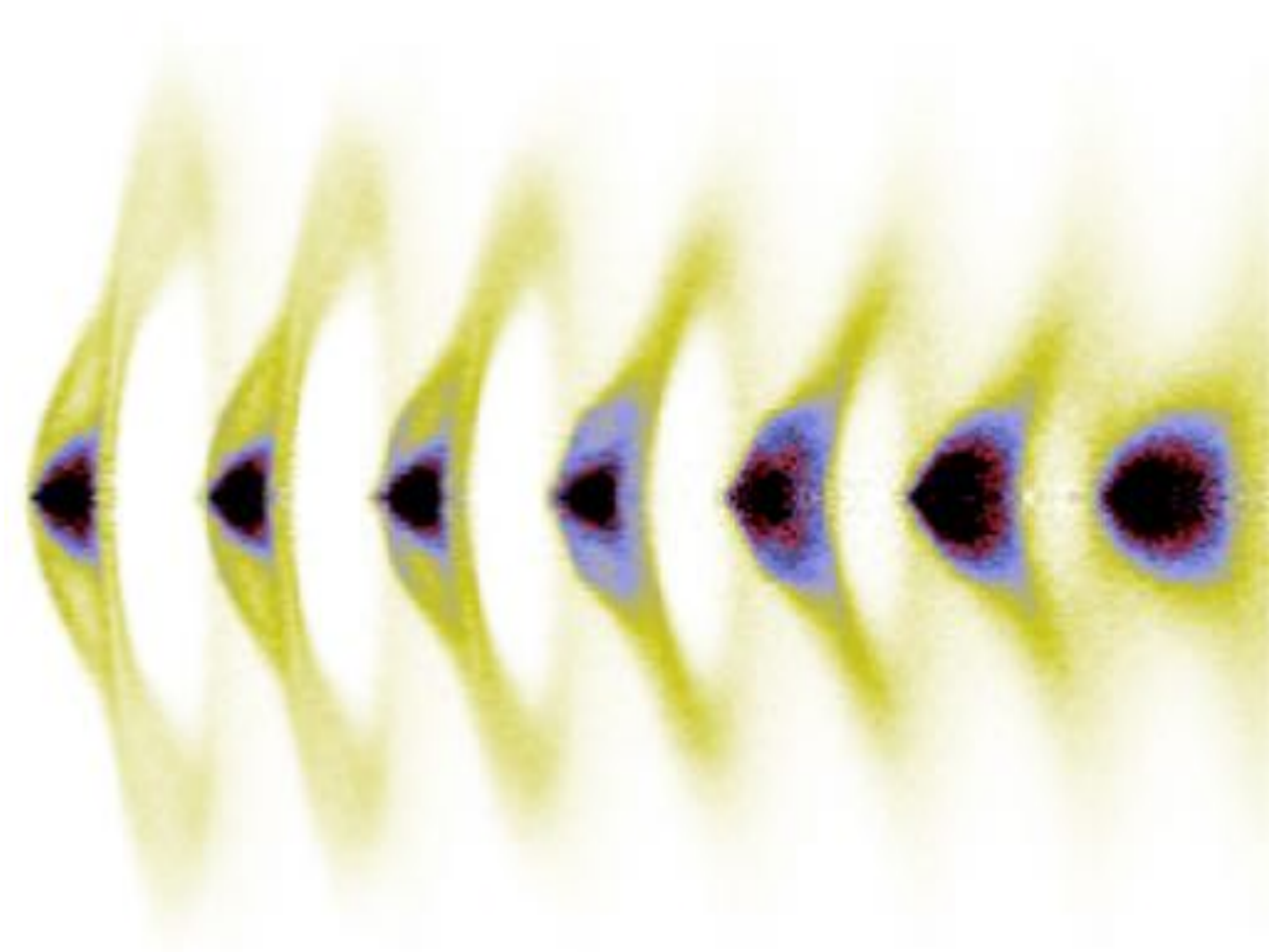
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The PIC method

Question 1:

Robustness in the AWAKE experiment

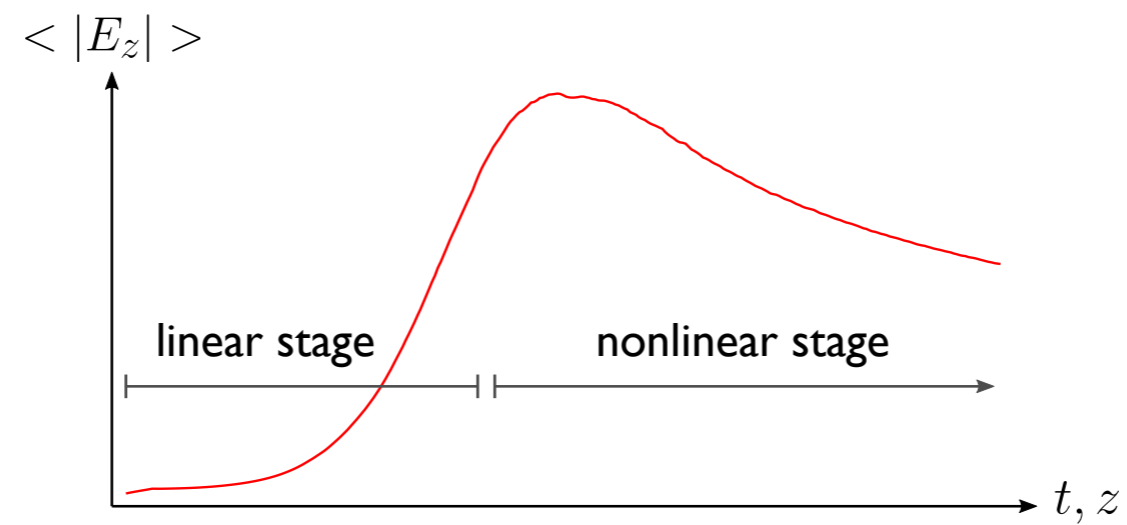
Question 2:

Beyond the linear theory of the SMI

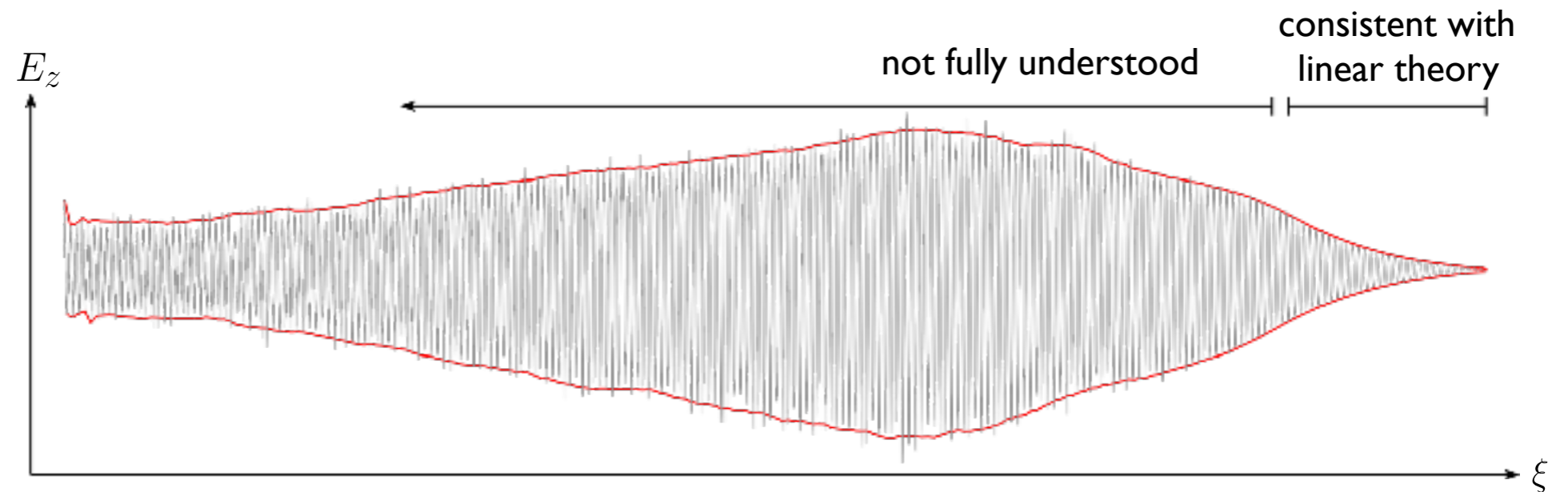
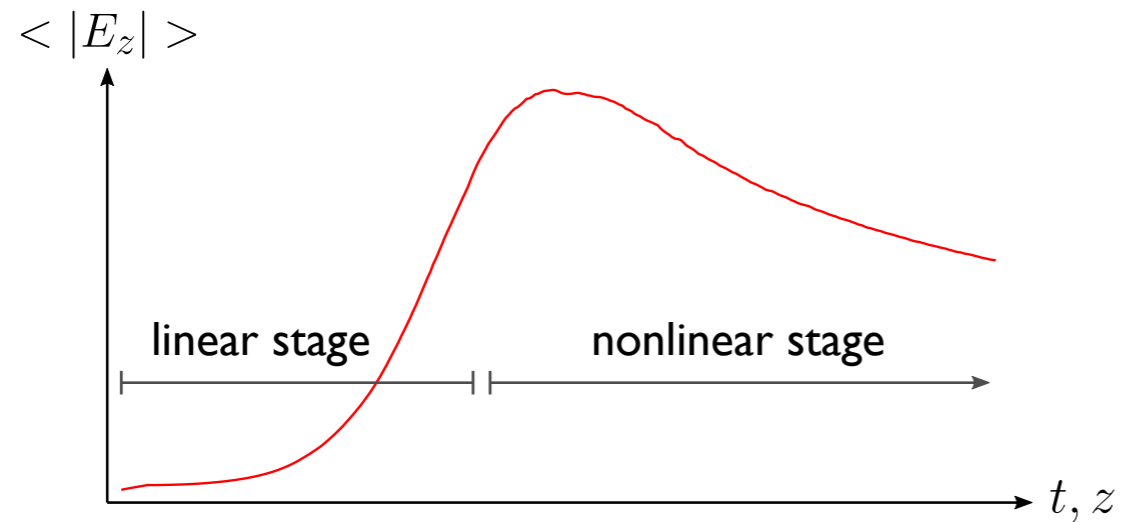
Question 3:

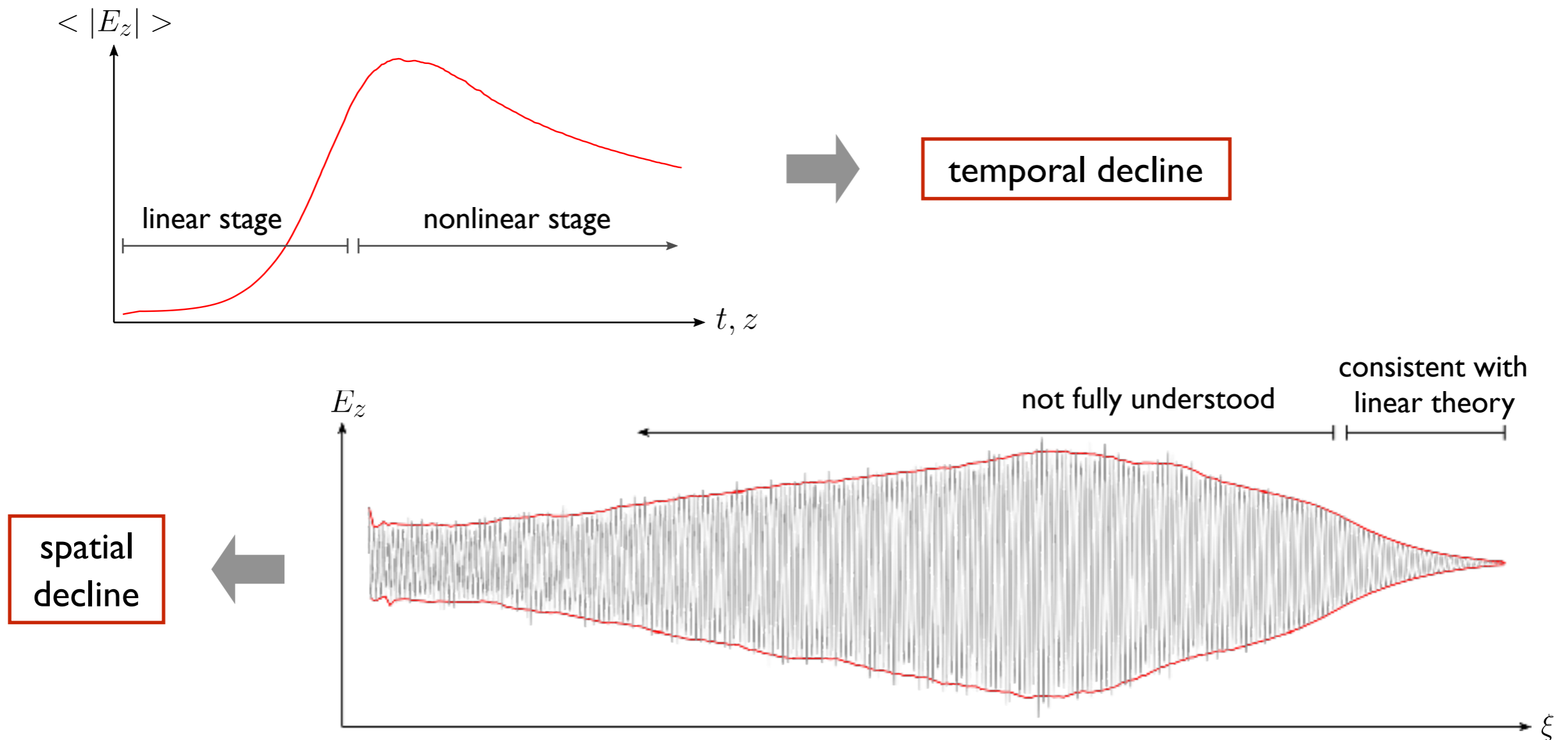
Antiprotons as wakefield drivers

Conclusion



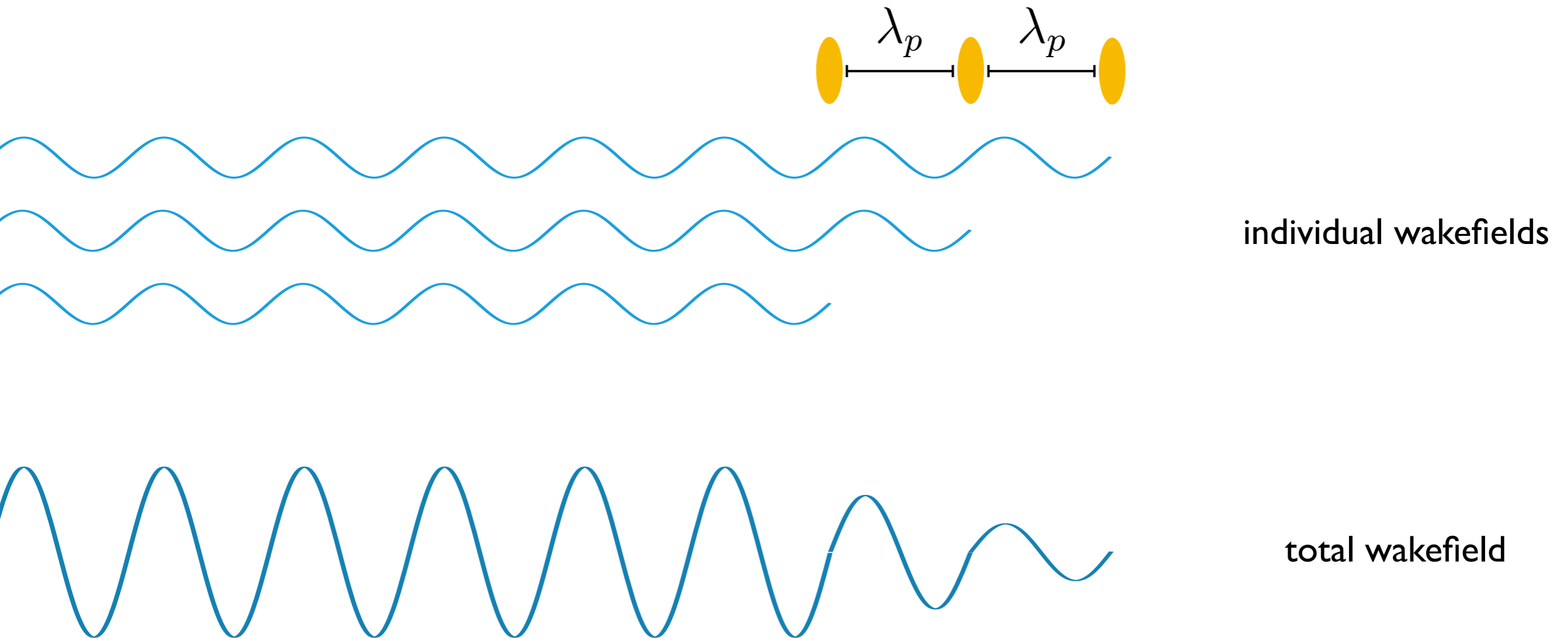
Beyond the linear stage of the SMI



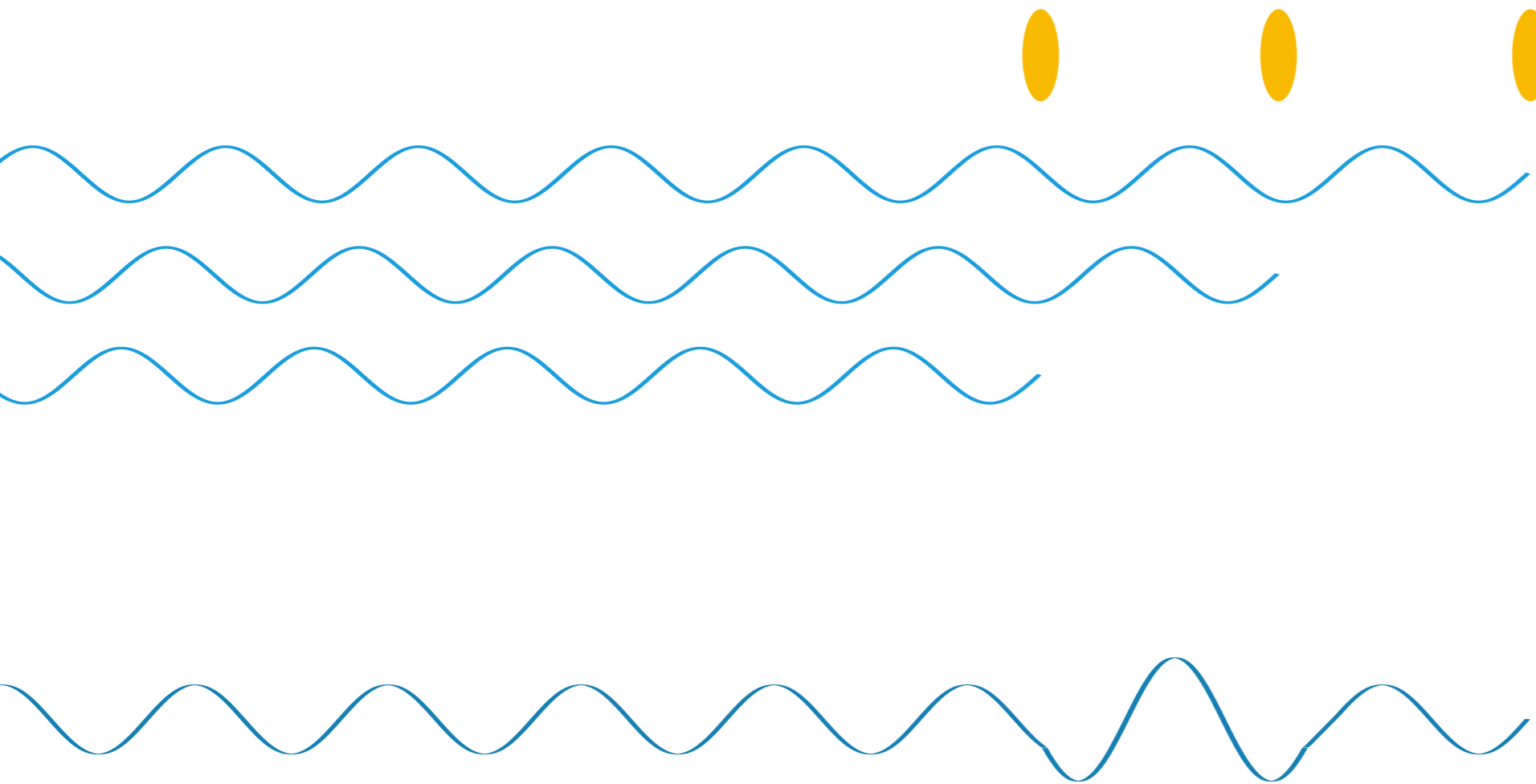


Second question

Why does the wakefield amplitude decrease along the beam and along time (after saturation of the SMI)?



Hypothesis: incoherent interference of wakes



individual wakefields

total wakefield

Linear wakefield theory

Axial electric field excited in plasma by an axisymmetric particle beam in cylindrical coordinates:

$$E_z(\xi, r) = 4\pi e k_p^2 \int_{-\infty}^{\xi} d\xi' \int_0^{\infty} dr' r' \cos [k_p(\xi - \xi')] I_0(k_p r_{<}) K_0(k_p r_{>}) n_b(\xi', r')$$

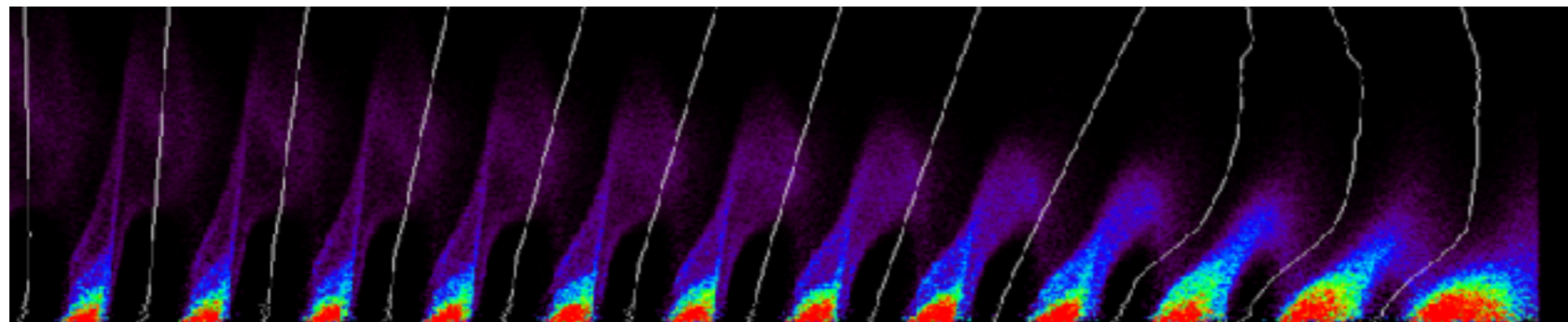
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Single beamlet linear wakefield solver

- **input:** charge density data from PIC simulation for the driver beam $\rho(\xi, r)$
- identify and isolate beamlets



} partially parallel

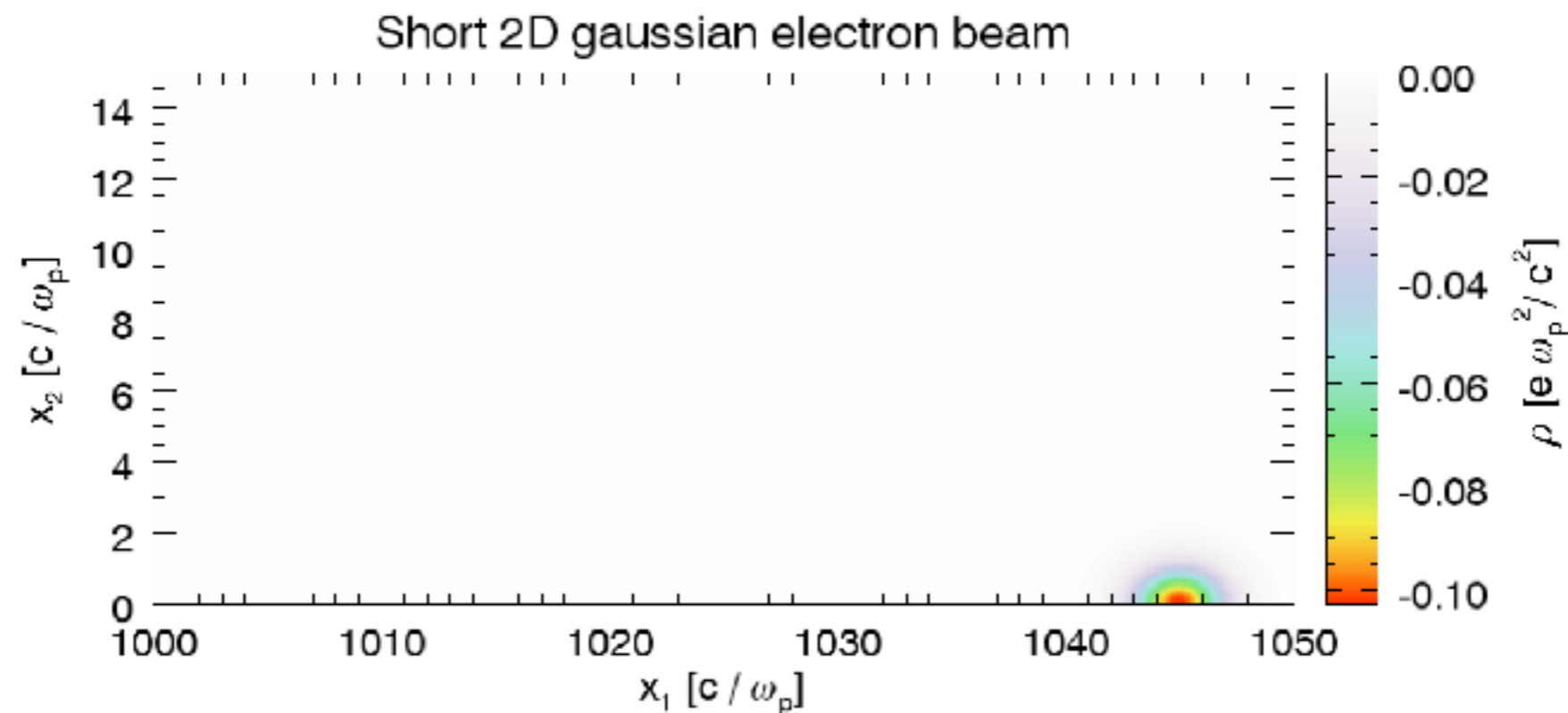
} parallel

- solve equation for each beamlet and add all the contributions
- **output:** axial electric field distribution over simulation window $E_z(\xi, r)$

Subtasks involved

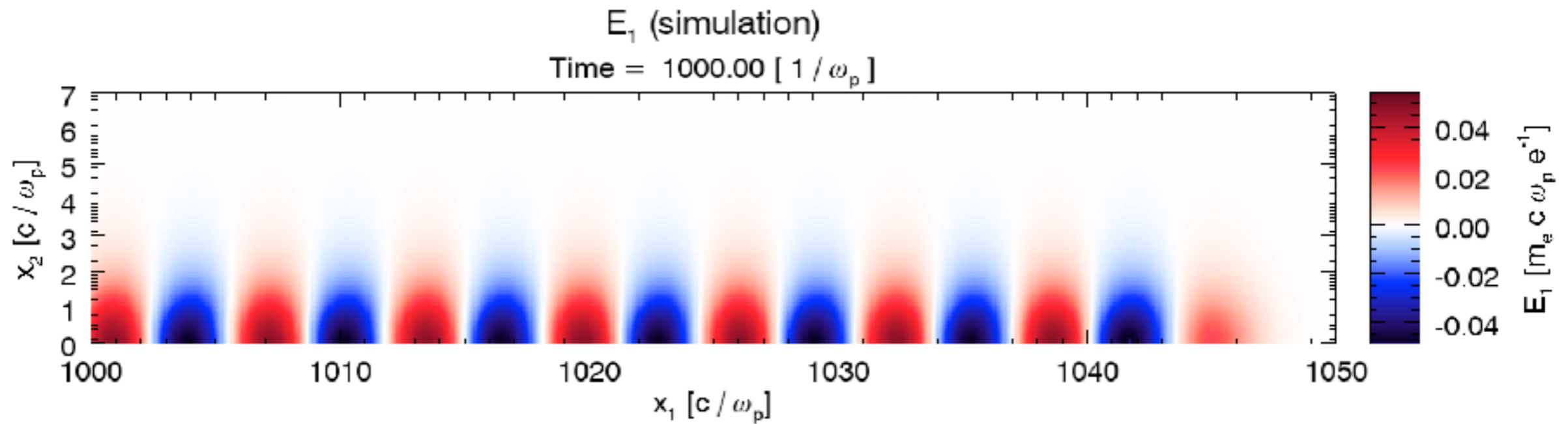
- devising and/or perfecting the algorithms for each step
- implementing in C with parallelization (MPI)
- scalability tests on Accelerates
- benchmark (and finding the last bugs)

Benchmark

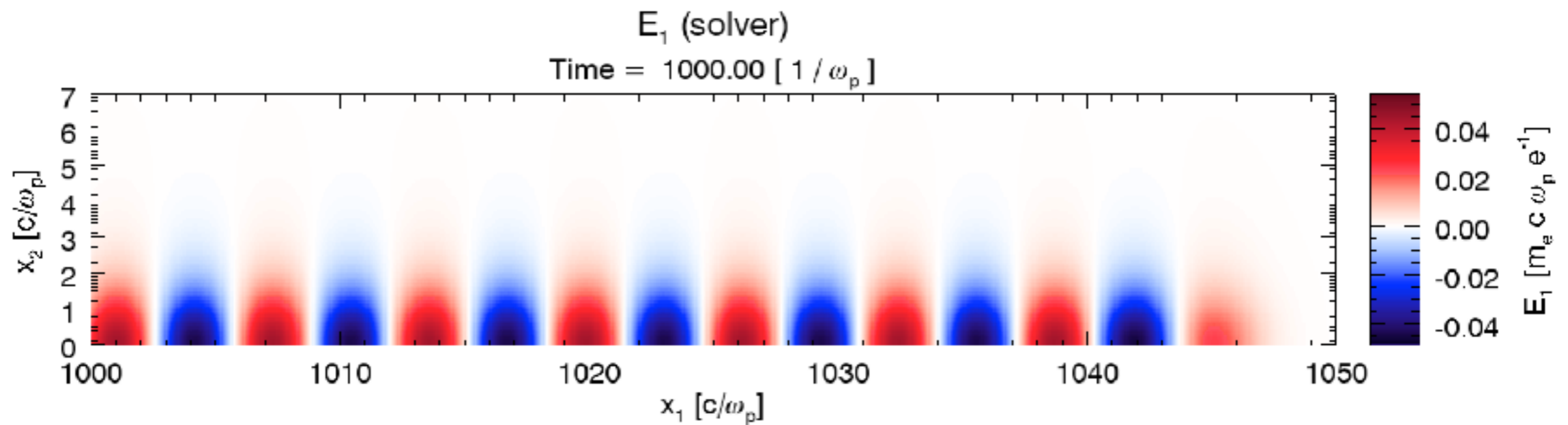


Excellent agreement

Simulation results

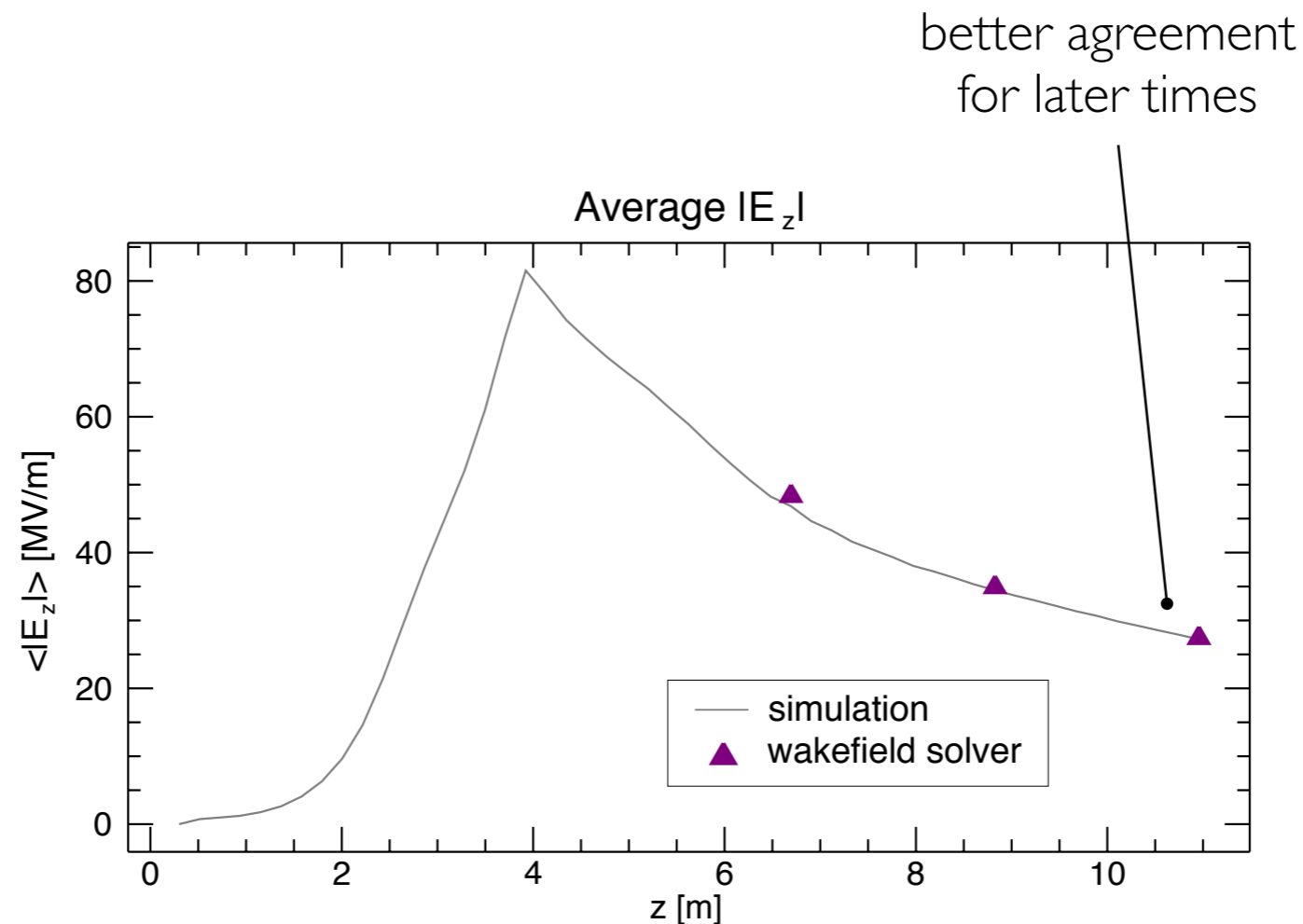


Wakefield solver



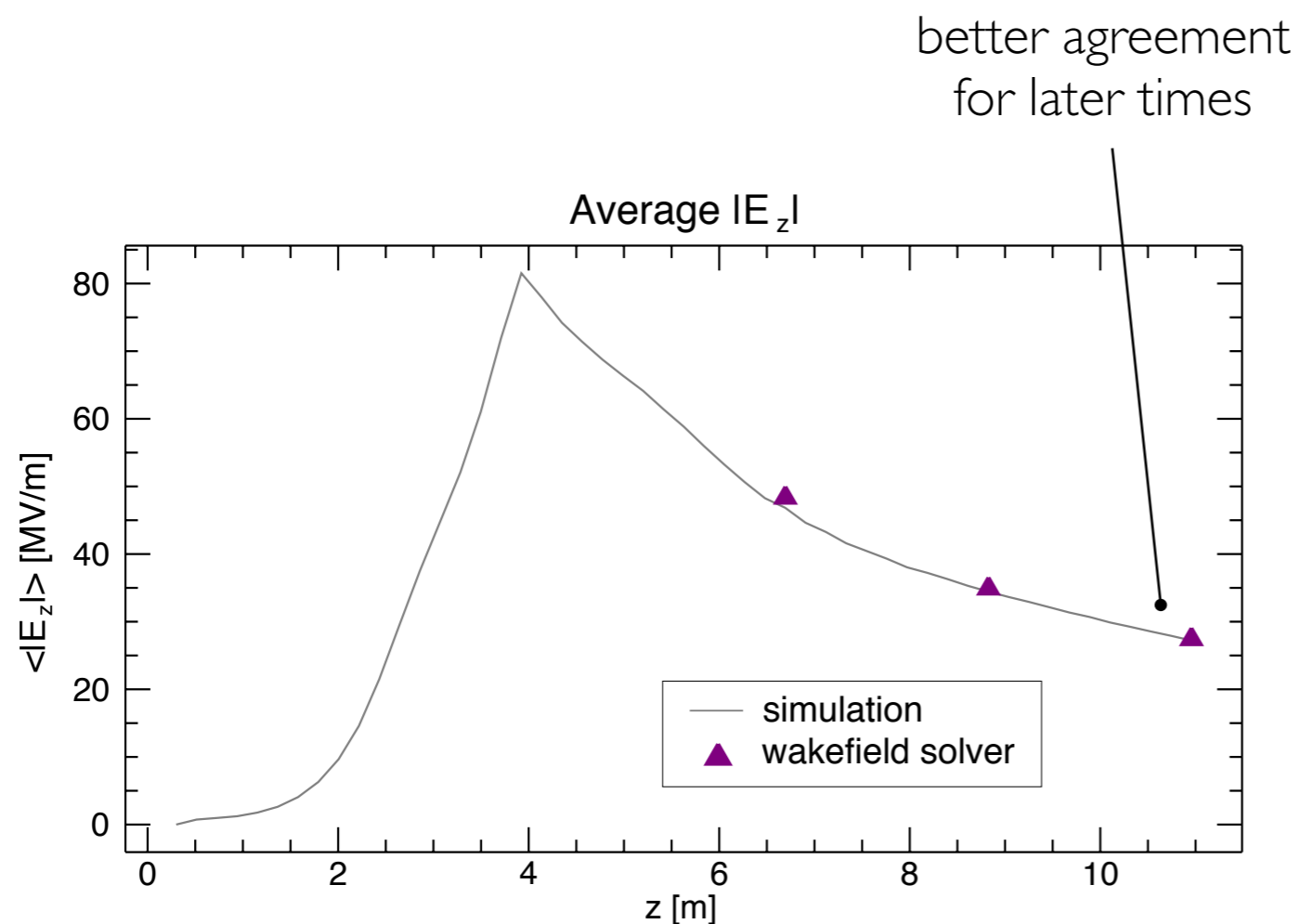
General wakefield

- comparison of the total E_z field at three simulation times
- good agreement both in terms of field amplitude and configuration



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Separate contributions

- wakefield is solved up to a specified beamlet number
- **two outputs:**
 - field due to last beamlet
 - field due to all previous beamlets
- comparison for two simulation times and three beamlet numbers

beamlet nr.	position along simulation window
8	96%
90	60%
170	25%

Incoherence causes the decline along the beam

But the decline along z must have a different dominant cause

beamlet nr. 8
rel. amplitude: 20%

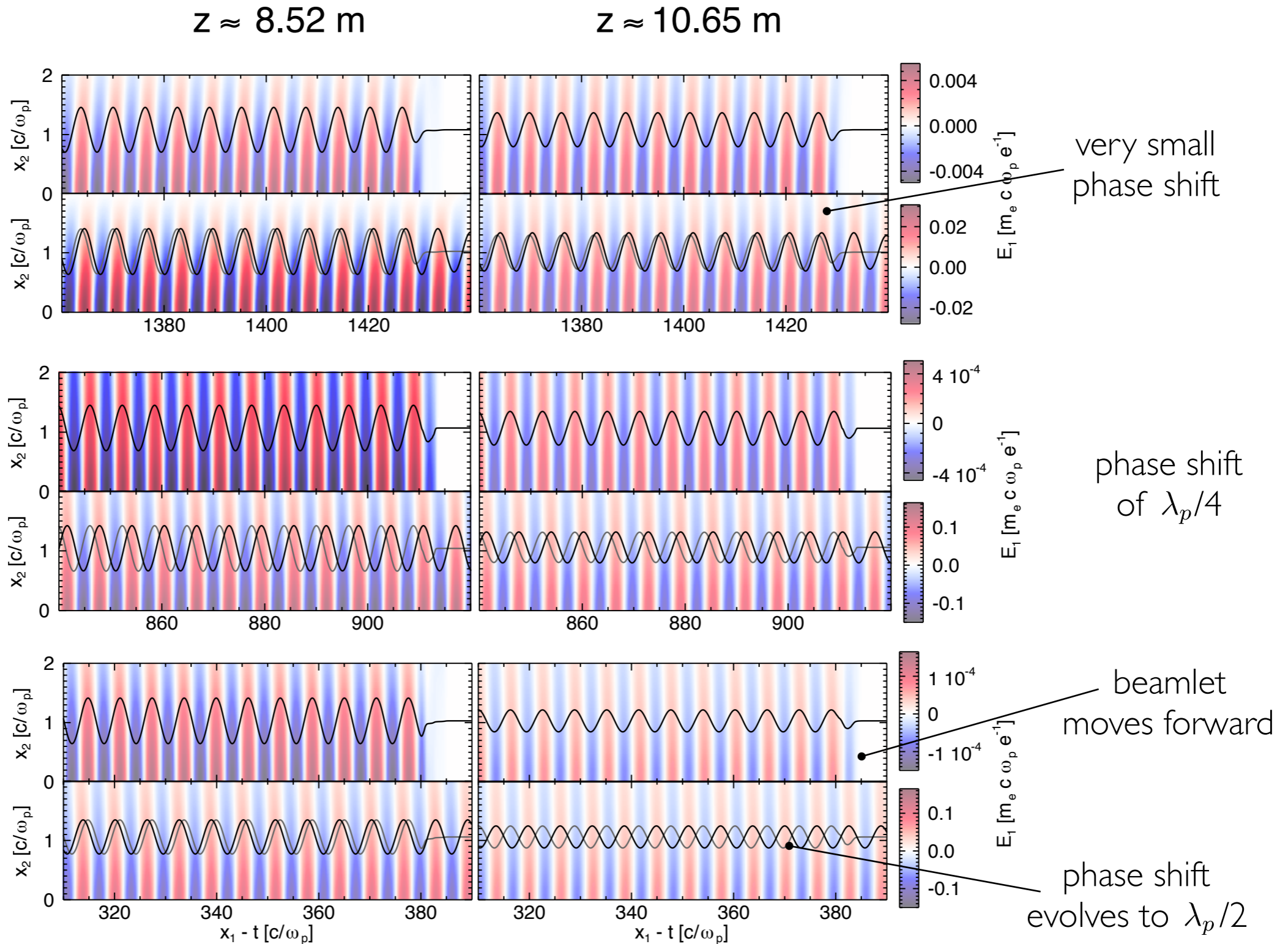
beamlets nr. 1–7

beamlet nr. 90
rel. amplitude: 0.3%

beamlets nr. 1–89

beamlet nr. 170
rel. amplitude: 0.1%

beamlets nr. 1–169



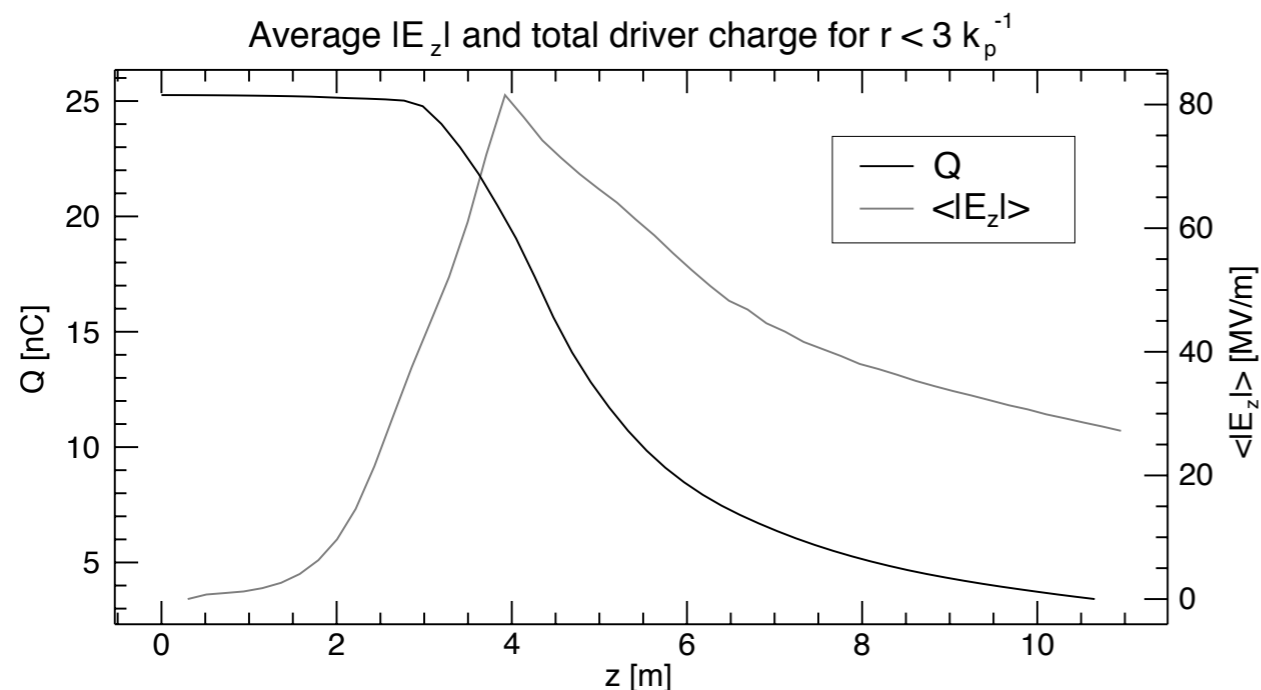
Decline along beam (ξ)

- for a fixed time the individual wakes interfere incoherently with one another
- the total amplitude therefore falls in space
- no hidden nonlinear effects (overlap between wakefield solver and PIC simulation)

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Decline along propagation distance (z)



- identical trends for the wakefield-driving charge and average field after saturation
- loss of driver charge is the overwhelming cause for temporal decline

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Asymmetry between opposite charges

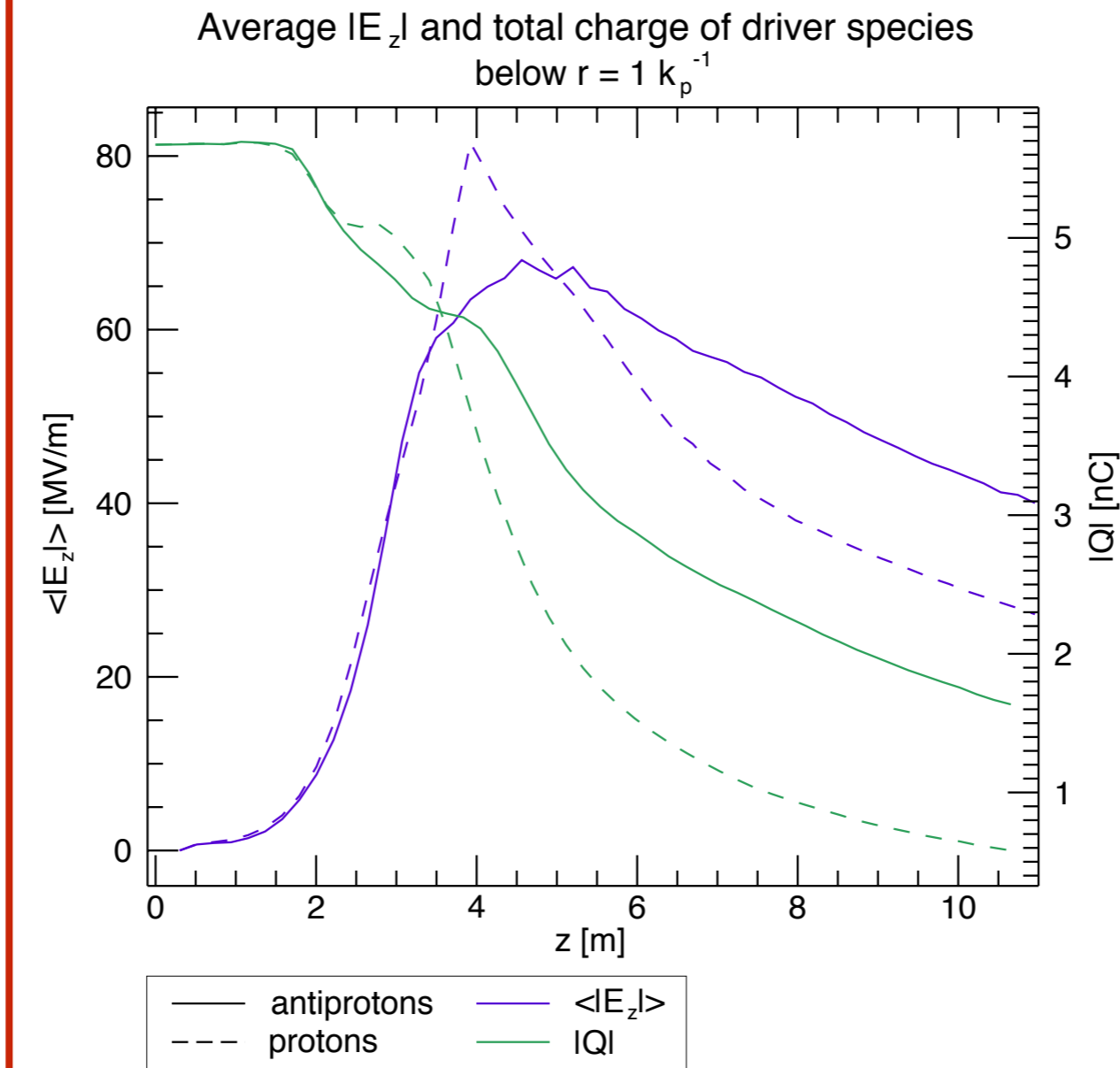
- most PWFA experiments have used electrons as drivers
- positrons seem to be less efficient as drivers*
- linear wakefield theory is perfectly symmetrical for opposite charges

Third question

How would the hypothetical substitution of the driver protons by antiprotons change the AWAKE experiment?

* S. Lee et al. Phys. Rev. E 64 045501 (2001)

More driver charge available

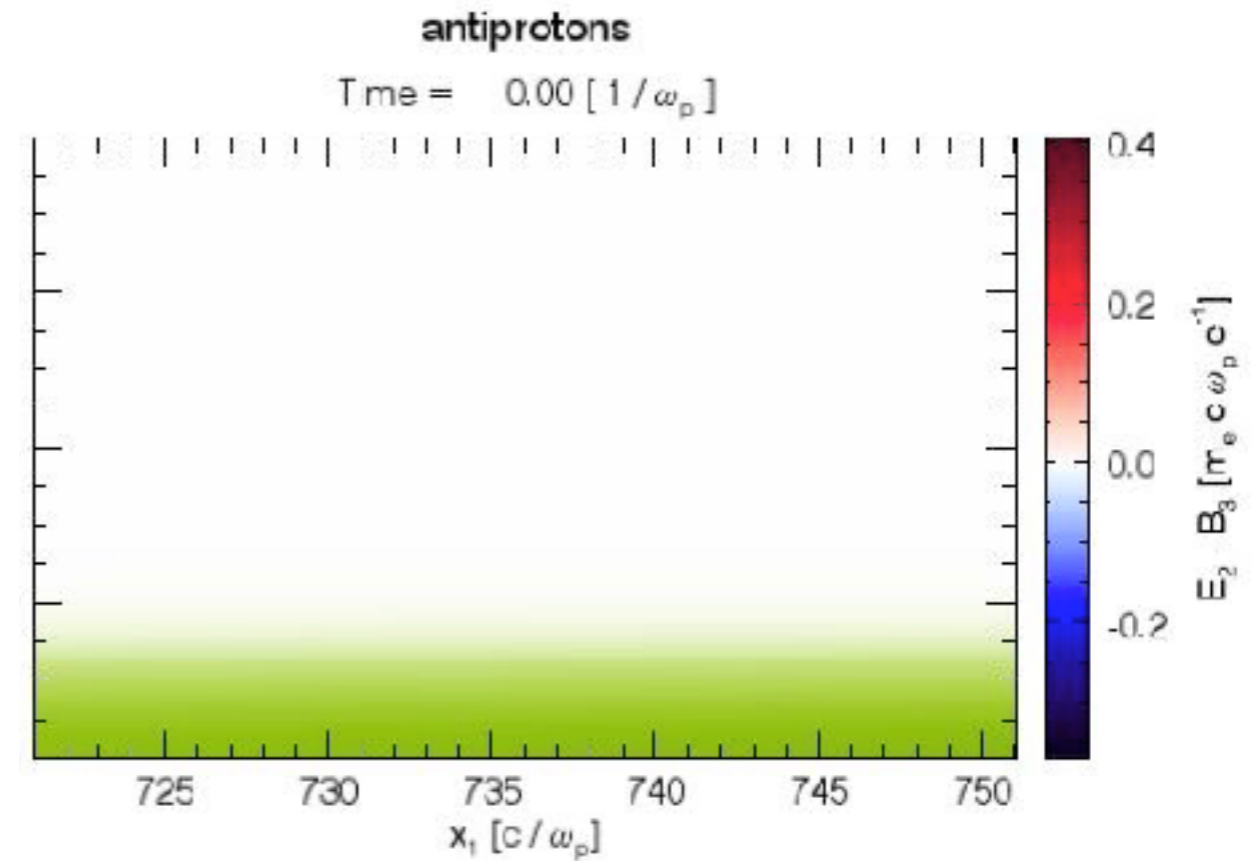
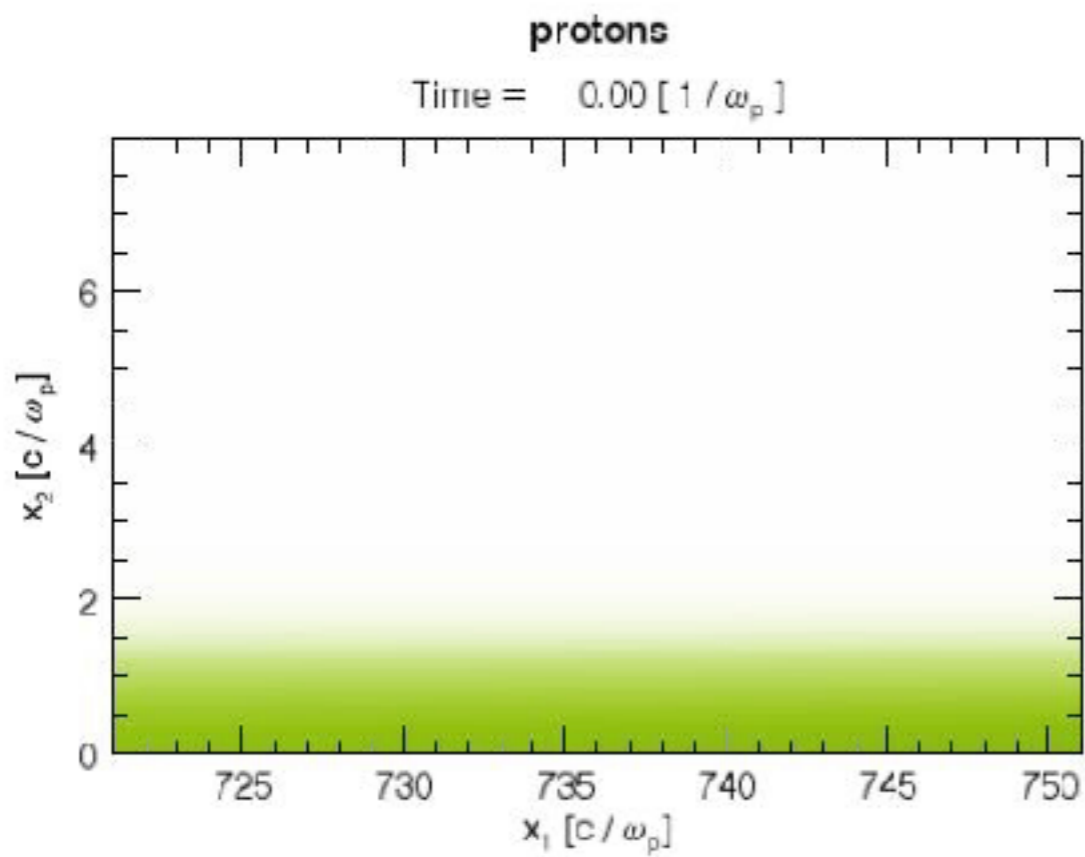


2.8x more driver charge at 10.33 m

1.5x higher average $|E_z|$ at 10.33 m

Field configuration recaptures off-axis charge

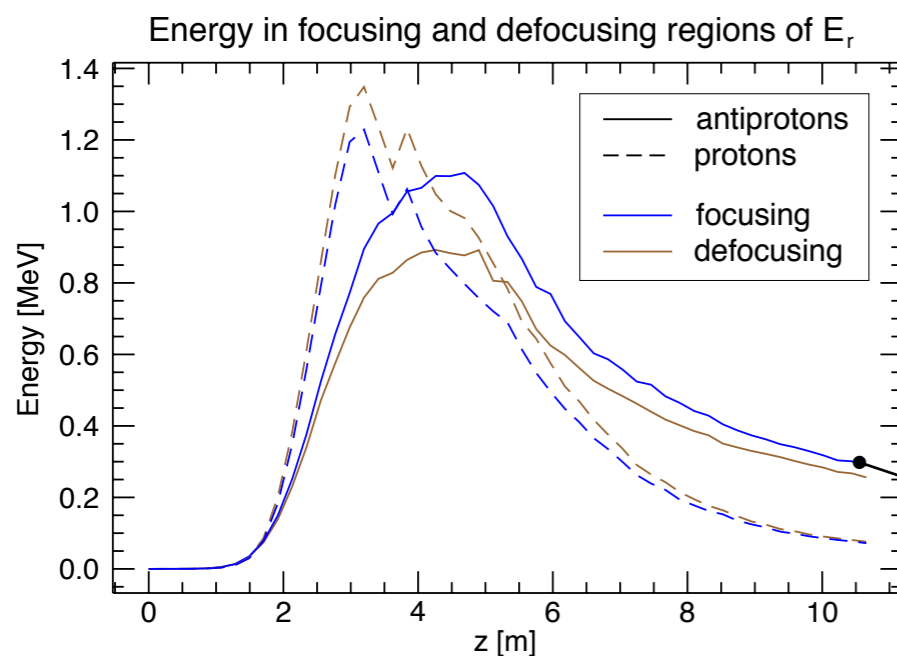
Why is so much antiproton charge retained?



Energy contained in E_r offers important clues

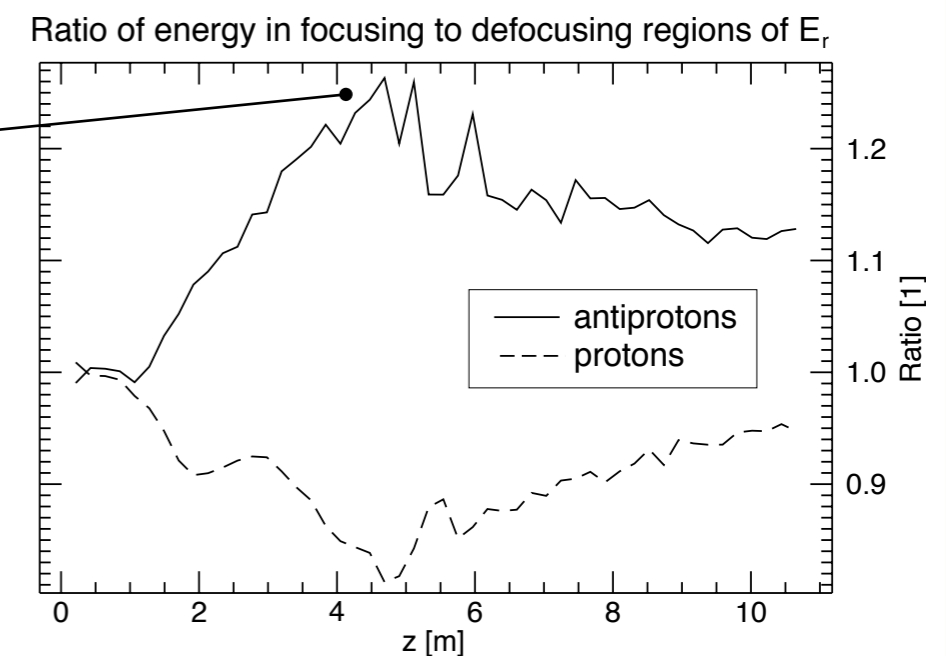
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Antiprotons have more energy available for focusing



larger energy imbalance for antiprotons

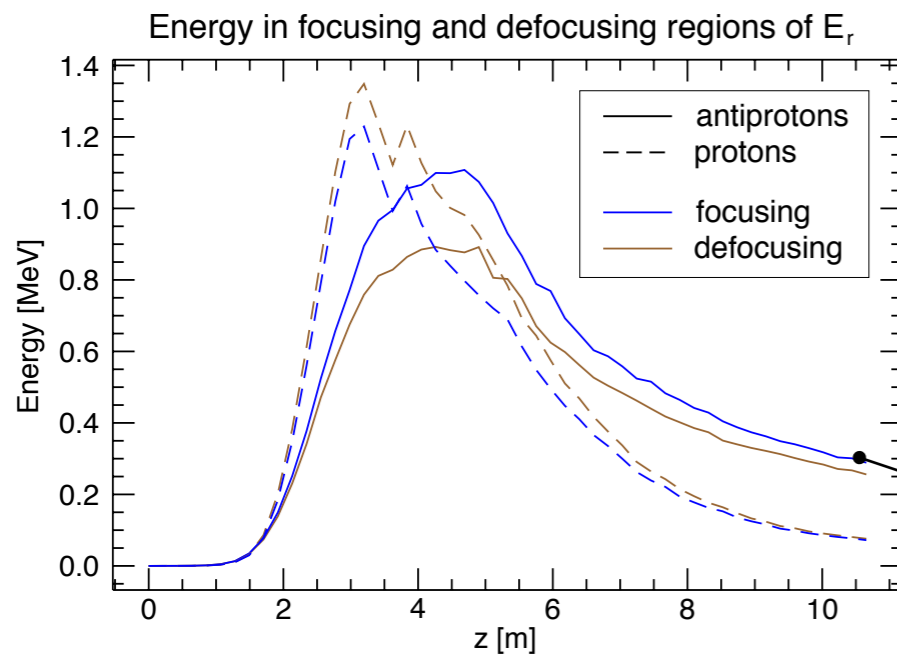
3.8x more energy in focusing fields



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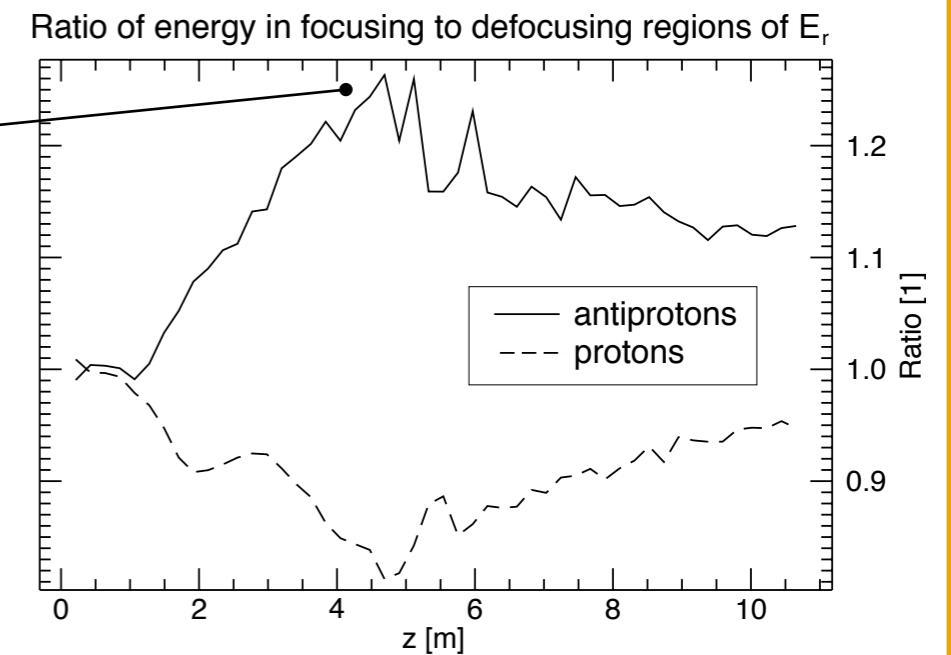
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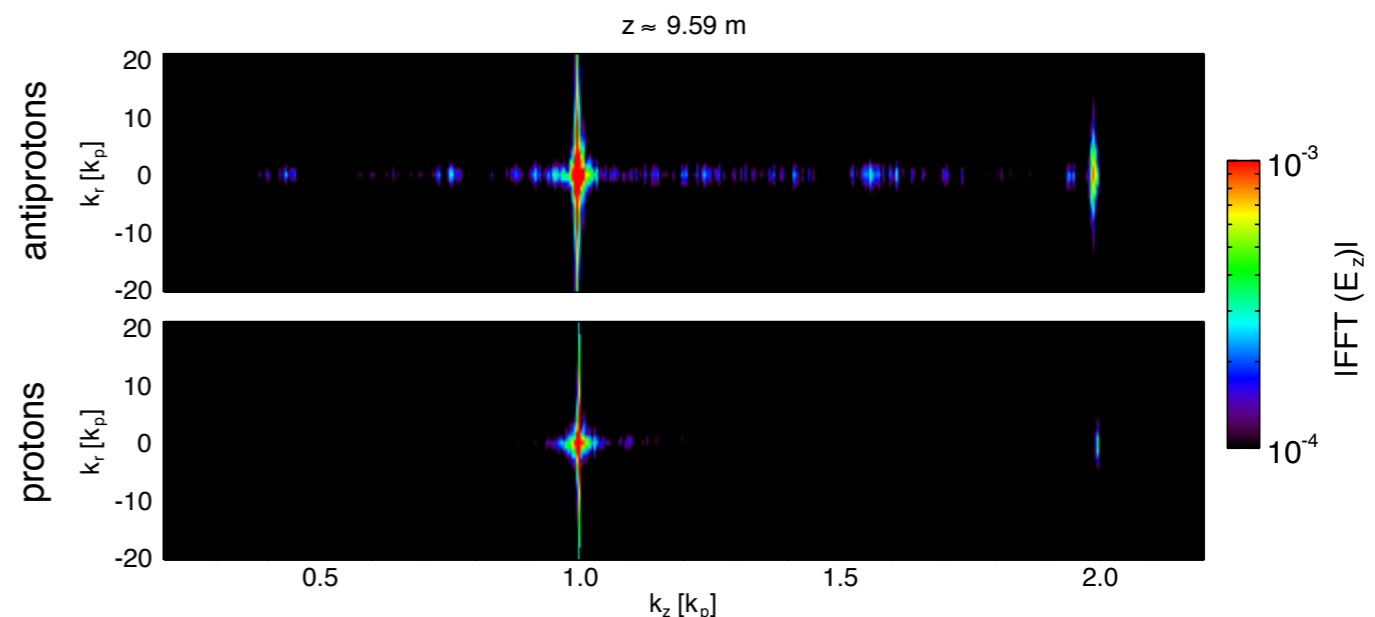


The antiproton-driven wakefield is more nonlinear

- 2D Fourier transform of E_z

- purely linear wake:

$$k_z = n k_p, n \in \mathbb{Z}$$



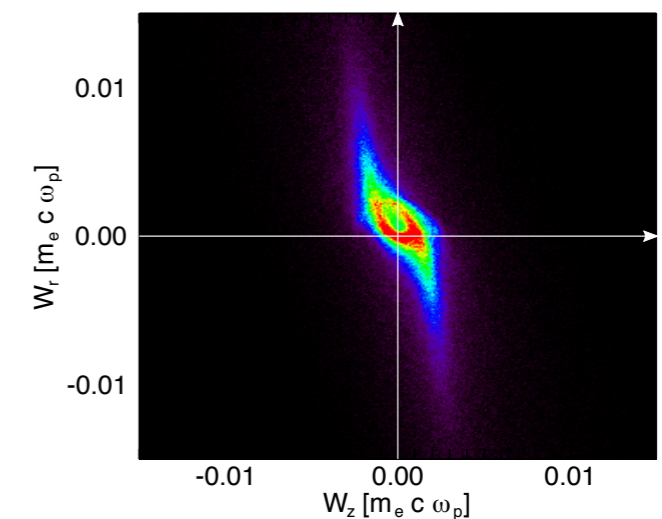
Why is the amplitude of the antiproton wakefield lower than expected?

Charge density in longitudinal and transverse force plane

- normalized, unsigned forces:

$$W_z = E_z \quad W_r = E_r - B_\varphi$$

- each increment of charge is deposited in W_r/W_z plane according to the fields acting on it



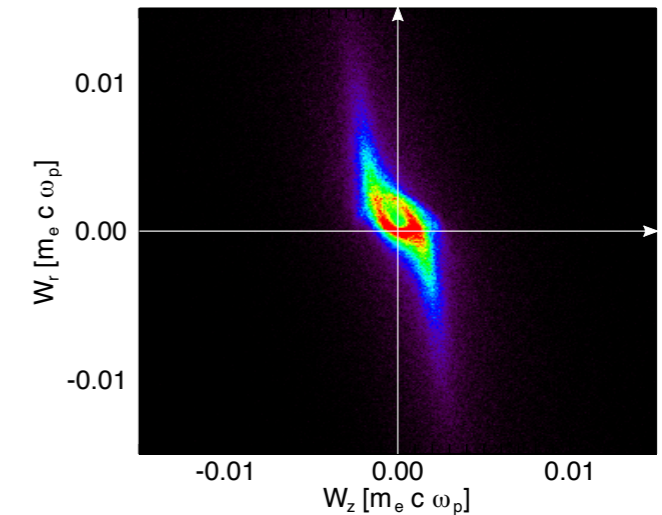
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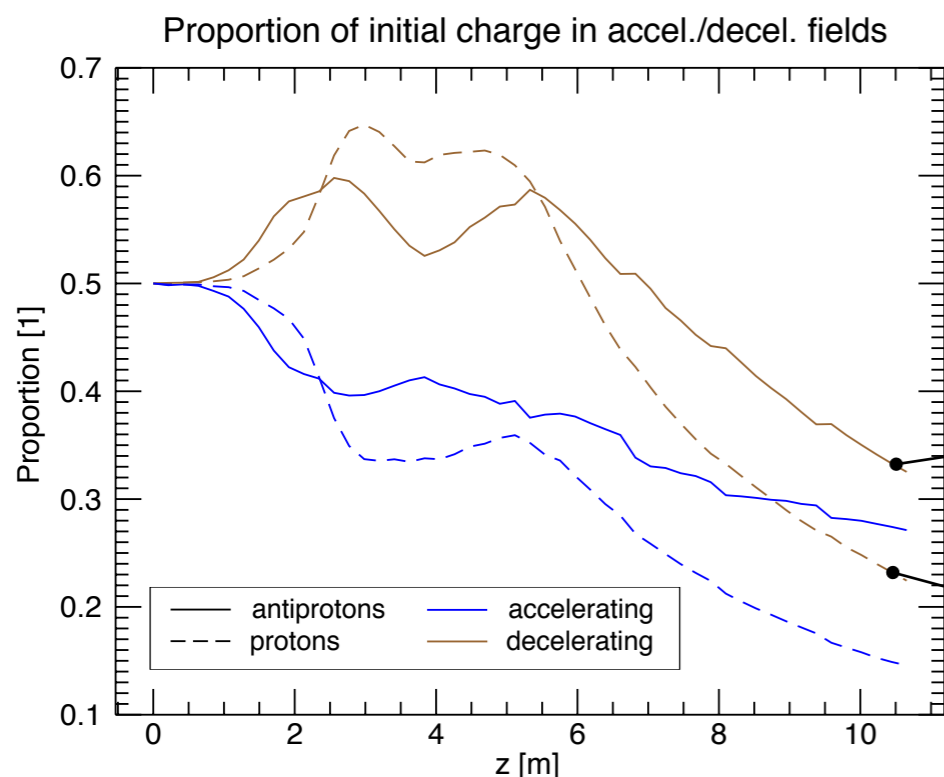
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A lower portion of the remaining antiprotons gives up energy



- integrate charge density on W_r/W_z plane for $W_z > 0$ and $W_z < 0$

55% of antiprotons left

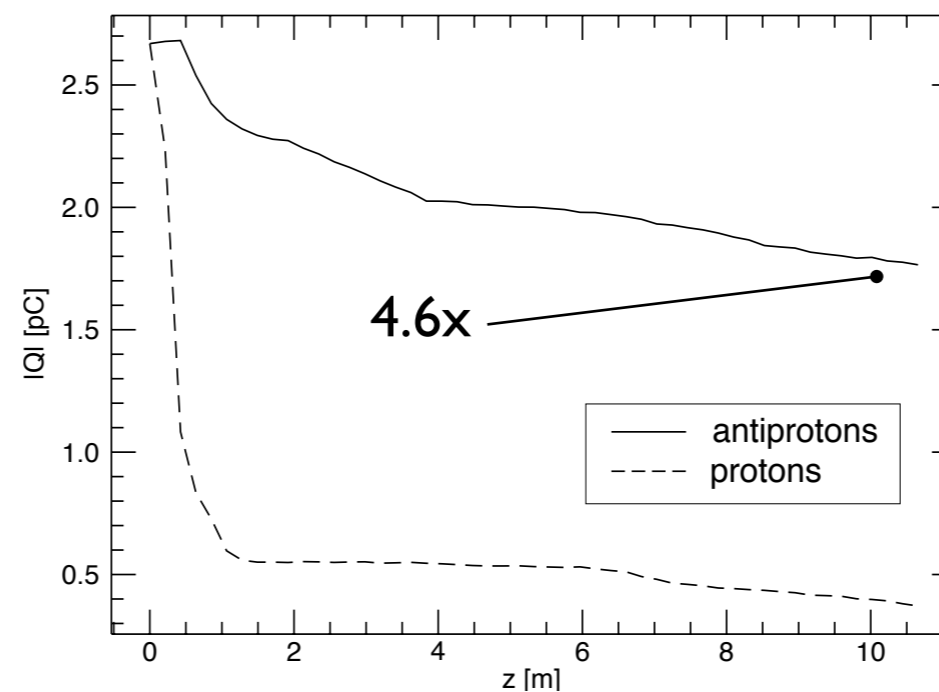
61% of protons left

} difference is not large enough to explain the underwhelming amplitude of E_z

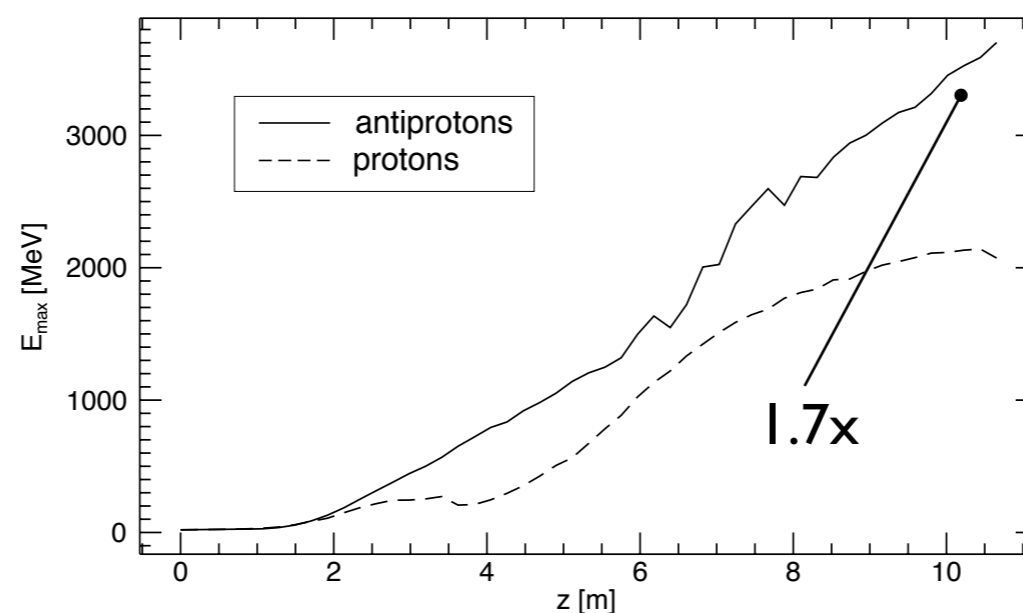
Benefits are also reflected on witness electrons

A witness electron bunch is introduced in the simulation

Witness charge



Max. electron energy



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Deterministic injection of electrons is possible for AWAKE

The outputs from the experiment are robust against shot-to-shot fluctuations

The temporal decline of the wakefield amplitude is due to charge loss

The spatial decline is due to incoherent interference between individual wake contributions

A parallel program was developed to study the nonlinear phase of the SMI

Antiprotons are more efficient as wakefield drivers

The wakefield driven by antiprotons is more nonlinear than the one driven by protons

More antiproton charge is preserved due to stronger fields