

Сильно-интенсивные переменные в модели со слиянием струн на поперечной решетке

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25 лет ALICE - научная сессия

- ◇ Definition of the strongly intensive observable $\Sigma(n_F, n_B)$
- ◇ $\Sigma(n_F, n_B)$ in the model with independent identical strings
- ◇ $\Sigma(n_F, n_B)$ for windows separated in azimuth and rapidity
- ◇ The model with string fusion on transverse lattice (grid)
- ◇ $\Sigma(n_F, n_B)$ in the model with string fusion on transverse grid
- ◇ Conclusions

Strongly intensive observable $\Sigma(n_F, n_B)$

We define the strongly intensive observable $\Sigma(n_F, n_B)$ between multiplicities in forward (n_F) and backward (n_B) windows in accordance with [*M.I.Gorenstein, M.Gazdzicki, Phys.Rev.C84(2011)014904*] as

$$\Sigma(n_F, n_B) \equiv \frac{1}{\langle n_F \rangle + \langle n_B \rangle} [\langle n_F \rangle \omega_{n_B} + \langle n_B \rangle \omega_{n_F} - 2 \text{cov}(n_F n_B)] , \quad (1)$$

where

$$\text{cov}(n_F, n_B) \equiv \langle n_F n_B \rangle - \langle n_F \rangle \langle n_B \rangle , \quad (2)$$

and ω_{n_F} and ω_{n_B} are the corresponding scaled variances of the multiplicities:

$$\omega_n \equiv \frac{D_n}{\langle n \rangle} = \frac{\langle n^2 \rangle - \langle n \rangle^2}{\langle n \rangle} . \quad (3)$$

$\Sigma(n_F, n_B)$ for symmetric reaction and symmetric windows

For symmetric reaction and symmetric observation windows $\delta\eta_F = \delta\eta_B = \delta\eta$:

$$\langle n_F \rangle = \langle n_B \rangle \equiv \langle n \rangle, \quad \omega_{n_F} = \omega_{n_B} \equiv \omega_n \quad (4)$$

and

$$\begin{aligned} \Sigma(n_F, n_B) &= \omega_n - \text{cov}(n_F, n_B) / \langle n \rangle = \frac{\langle n^2 \rangle - \langle n_F n_B \rangle}{\langle n \rangle} = \\ &= \frac{D_n - \text{cov}(n_F, n_B)}{\langle n \rangle} = \frac{\text{cov}(n_F, n_F) - \text{cov}(n_F, n_B)}{\langle n \rangle}. \end{aligned} \quad (5)$$

The model with independent identical strings as emitters

[M.A. Braun, C. Pajares, V.V. Vechernin, *Phys. Lett. B* **493**, 54 (2000)]

1) The number of strings, N , fluctuates event by event around some mean value, $\langle N \rangle$, with some scaled variance, $\omega_N = D_N / \langle N \rangle$.

Intensive observable does not depend on $\langle N \rangle$.

Strongly intensive observable does not depend on $\langle N \rangle$ and ω_N .

2) The fragmentation of each string contributes event-by-event to the forward and backward observation rapidity windows, $\delta\eta_F$, and $\delta\eta_B$, the μ_F and μ_B charged particles correspondingly, which fluctuate around some mean values, $\langle \mu_F \rangle$ and $\langle \mu_B \rangle$, with some scaled variances, $\omega_{\mu_F} = D_{\mu_F} / \langle \mu_F \rangle$ and $\omega_{\mu_B} = D_{\mu_B} / \langle \mu_B \rangle$.

The observation rapidity windows are separated by some rapidity interval: $\eta_{sep} = \Delta\eta$ - the distance between the centers of the $\delta\eta_F$ and $\delta\eta_B$.

Clear that in this model (and the same for n_B):

$$\langle n_F \rangle = \langle \mu_F \rangle \langle N \rangle = \langle N \rangle \mu_0, \quad \omega_{n_F} = \omega_{\mu_F} + \langle \mu_F \rangle \omega_N,$$

Two-particle correlation function of a string

Along with the observed standard two-particle correlation function:

$$C_2(\eta_1, \eta_2) \equiv \frac{\rho_2(\eta_1, \eta_2)}{\rho(\eta_1)\rho(\eta_2)} - 1, \quad (6)$$

where

$$\rho(\eta) = \frac{dN_{ch}}{d\eta}, \quad \rho_2(\eta_1, \eta_2) = \frac{d^2 N_{ch}}{d\eta_1 d\eta_2} \quad (7)$$

one can introduce the string two-particle correlation function, $\Lambda(\eta_1, \eta_2)$, characterizing correlation between particles, produced from the same string:

$$\Lambda(\eta_1, \eta_2) \equiv \frac{\lambda_2(\eta_1, \eta_2)}{\lambda(\eta_1)\lambda(\eta_2)} - 1. \quad (8)$$

The $\Lambda(\eta_1, \eta_2)$ characterizes the string decay properties.

Connection between the two-particle correlation functions

In this model we have the following connection:

$$C_2(\eta_1, \eta_2) = \frac{\omega_N + \Lambda(\eta_1, \eta_2)}{\langle N \rangle}$$

[V. Vechernin, *Nucl. Phys. A939(2015)21*]. (Note that one often loses the constant part $\omega_N/\langle N \rangle$ of C_2 , using di-hadron correlation approach.)

At midrapidities, implying uniform rapidity distribution:

$$\lambda(\eta) = \mu_0 = \frac{\langle \mu_F \rangle}{\delta y_F} = \frac{\langle \mu_B \rangle}{\delta y_B}, \quad \rho(\eta) = \frac{dN_{ch}}{d\eta} = \rho_0 = \frac{\langle n_F \rangle}{\delta y_F} = \frac{\langle n_B \rangle}{\delta y_B} = \langle N \rangle \mu_0$$

and the correlation functions depends only on a difference of rapidities:

$$\eta_{sep} = \eta_1 - \eta_2 = \Delta\eta$$

We suppose that the string correlation function

$$\Lambda(\Delta\eta) \rightarrow 0, \text{ when } \Delta\eta \gg \eta_{corr},$$

where the η_{corr} is the correlation length.

$\Sigma(n_F, n_B)$ for small observation windows

For small observation windows, of a width $\delta\eta \ll \eta_{\text{corr}}$, we find [V.Vechernin, Nucl.Phys.A939(2015)21]:

$$\omega_n = D_n / \langle n \rangle = 1 + \mu_0 \delta\eta [\Lambda(0) + \omega_N] , \quad (9)$$

$$\text{cov}(n_F, n_B) / \langle n \rangle = \mu_0 \delta\eta [\Lambda(\Delta\eta) + \omega_N] , \quad (10)$$

$$\Sigma(n_F, n_B) = \omega_n - \text{cov}(n_F, n_B) / \langle n \rangle = 1 + \mu_0 \delta\eta [\Lambda(0) - \Lambda(\Delta\eta)] , \quad (11)$$

where $\Delta\eta = \eta_F - \eta_B = \eta_{\text{sep}}$ is a distance between the centers of the forward and backward observation windows. For a single string we have

$$\omega_\mu = D_\mu / \langle \mu \rangle = 1 + \mu_0 \delta\eta \Lambda(0) , \quad (12)$$

$$\text{cov}(\mu_F, \mu_B) / \langle \mu \rangle = \mu_0 \delta\eta \Lambda(\Delta\eta) , \quad (13)$$

$$\Sigma(\mu_F, \mu_B) = \omega_\mu - \text{cov}(\mu_F, \mu_B) / \langle \mu \rangle = 1 + \mu_0 \delta\eta [\Lambda(0) - \Lambda(\Delta\eta)] , \quad (14)$$

So in $\Sigma(n_F, n_B)$ we have the cancelation of the contributions from the fluctuation of the number of strings, ω_N , and it becomes **strongly intensive**:

$$\Sigma(n_F, n_B) = \Sigma(\mu_F, \mu_B)$$

Strongly intensive observable $\Sigma(n_F, n_B)$

In general case the strongly intensive variable for a single string is defined similarly to $\Sigma(n_F, n_B)$ by

$$\Sigma(\mu_F, \mu_B) \equiv \frac{1}{\langle \mu_F \rangle + \langle \mu_B \rangle} [\langle \mu_F \rangle \omega_{\mu_B} + \langle \mu_B \rangle \omega_{\mu_F} - 2 \text{cov}(\mu_F, \mu_B)] . \quad (15)$$

It depends only on properties of a single string.

So in the model with independent identical strings for symmetric reaction and small symmetric observation windows we found for $\Sigma(n_F, n_B)$:

$$\Sigma(\eta_{sep}) = 1 + \mu_0 \delta\eta [\Lambda(0) - \Lambda(\eta_{sep})]$$

We see that really **the $\Sigma(\eta_{sep})$ is strongly intensive quantity.**

It does not depend on $\langle N \rangle$ and ω_N .

Properties of the Σ in independent identical string model

$$\Sigma(\eta_{sep}) = 1 + \mu_0 \delta\eta [\Lambda(0) - \Lambda(\eta_{sep})]$$

The $\Sigma(0) = 1$ and increases with the gap between windows, η_{sep} , because the $\Lambda(\eta_{sep})$ decrease with η_{sep} , as the correlations in string go off with increase of η_{sep} .

The rate of the $\Sigma(\eta_{sep})$ growth with η_{sep} is proportional to the width of the observation window $\delta\eta$ and μ_0 - the multiplicity produced from one string.

The model predicts saturation of the $\Sigma(\eta_{sep})$ on the level

$$\Sigma(\eta_{sep}) = 1 + \mu_0 \delta\eta \Lambda(0) = \omega_\mu$$

at large η_{sep} , as $\Lambda(\eta_{sep}) \rightarrow 0$ at the $\eta_{sep} \gg \eta_{corr}$, where the η_{corr} is a string correlation length.

The pair correlation function of a single string

The parametrization for the pair correlation function $\Lambda(\eta, \phi)$ of a single string (reflecting the Schwinger mechanism of a string decay, was suggested in [V.Vechernin, Nucl.Phys.A939(2015)21]:

$$\Lambda(\eta, \phi) = \Lambda_1 e^{-\frac{|\eta|}{\eta_1}} e^{-\frac{\varphi^2}{\varphi_1^2}} + \Lambda_2 \left(e^{-\frac{|\eta-\eta_0|}{\eta_2}} + e^{-\frac{|\eta+\eta_0|}{\eta_2}} \right) e^{-\frac{(|\varphi|-\pi)^2}{\varphi_2^2}} . \quad (16)$$

This formula has the nearside peak, characterizing by parameters Λ_1 , η_1 and φ_1 , and the awayside ridge-like structure, characterizing by parameters Λ_2 , η_2 , η_0 and φ_2 (two wide overlapping hills shifted by $\pm\eta_0$ in rapidity, η_0 - the mean length of a string decay segment). We imply that in formula (16)

$$|\varphi| \leq \pi . \quad (17)$$

If $|\varphi| > \pi$, then we use the replacement $\varphi \rightarrow \varphi + 2\pi k$, so that (17) was fulfilled. With such completions the $\Lambda(\eta, \phi)$ meets the following properties

$$\Lambda(-\eta, \phi) = \Lambda(\eta, \phi) , \quad \Lambda(\eta; -\phi) = \Lambda(\eta, \phi) , \quad \Lambda(\eta, \phi + 2\pi k) = \Lambda(\eta, \phi) \quad (18)$$

Fitting the model parameters by FBC in small windows

$\Lambda(\eta_{sep}, \phi_{sep})$ was fitted by the ALICE b_{corr} pp data with FB windows of small acceptance, $\delta\eta = 0.2, \delta\phi = \pi/4$, separated in azimuth and rapidity [ALICE collab., JHEP 05(2015)097]. It gives for the parameters:

\sqrt{s} , TeV		0.9	2.76	7.0
LRC	$\mu_0\omega_N$	0.7	1.4	2.1
SRC	$\mu_0\Lambda_1$	1.5	1.9	2.3
	η_1	0.75	0.75	0.75
	ϕ_1	1.2	1.15	1.1
	$\mu_0\Lambda_2$	0.4	0.4	0.4
	η_2	2.0	2.0	2.0
	ϕ_2	1.7	1.7	1.7
	η_0	0.9	0.9	0.9

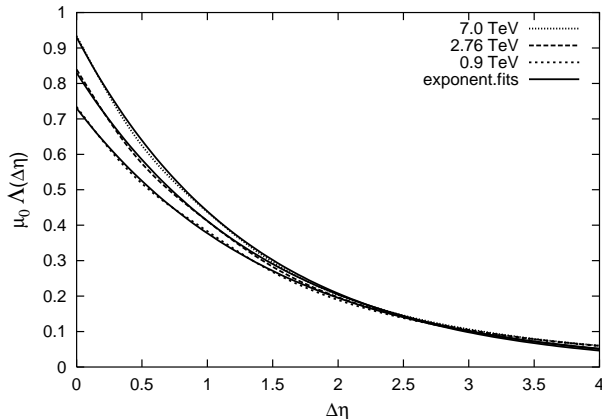
$\omega_N = \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}$ is the e-by-e scaled variance of the number of strings, μ_0 is the average rapidity density of the charged particles from one string, $i=1$ corresponds to the nearside and $i=2$ to the away-side contributions, η_0 is the mean length of a string decay segment.

[V.Vechernin, Nucl.Phys.A939(2015)21]

The string correlation function $\Lambda(\Delta\eta)$

Then we find $\Lambda(\Delta\eta)$ integrating over azimuth:

$$\Lambda(\eta_{sep}) = \frac{1}{\pi} \int_0^\pi \Lambda(\eta_{sep}, \phi_{sep}) d\phi_{sep} .$$



The string correlation function $\Lambda(\Delta\eta)$

The obtained dependencies in this figure for three initial energies are well approximated by the exponent:

$$\Lambda(\Delta\eta) = \Lambda_0 e^{-\frac{|\Delta\eta|}{\eta_{corr}}}, \quad (19)$$

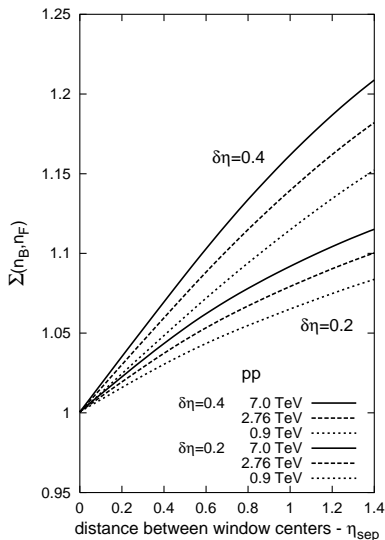
with the parameters presented in the table:

\sqrt{s} , TeV	0.9	2.76	7.0
$\mu_0 \Lambda_0$	0.73	0.83	0.93
η_{corr}	1.52	1.43	1.33

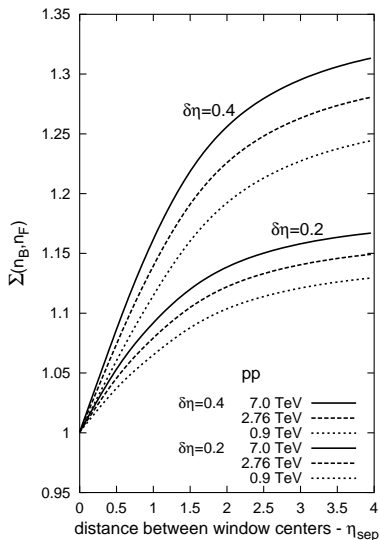
We see that the correlation length, η_{corr} , decreases with the increase of collision energy.

This can be interpreted as a signal of an increase with energy of the admixture of strings of a new type - the fused strings in pp collisions (see below).

Σ for 2π azimuth windows



in ALICE TPC acceptance



in wider pseudorapidity range

$\Sigma(n_F, n_B)$ in windows separated in azimuth and rapidity

For small windows:

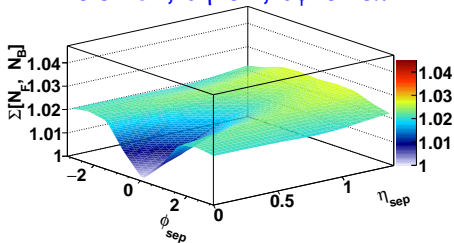
$$\Sigma(\eta_{sep}, \phi_{sep}) = 1 + \frac{\delta\eta\delta\phi}{2\pi} \mu_0 [\Lambda(0, 0) - \Lambda(\eta_{sep}, \phi_{sep})]$$

$$\Sigma(n_F, n_B) = \frac{D_n - \text{cov}(n_F, n_B)}{\langle n \rangle} = \frac{\text{cov}(n_F, n_F) - \text{cov}(n_F, n_B)}{\langle n \rangle} .$$

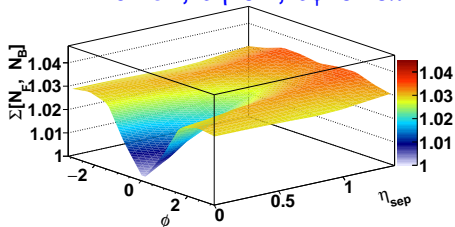
This explains the general nature of the compensation for neighbor windows.

Σ for $\delta\eta$ $\delta\phi$ windows separated in azimuth and rapidity - 1

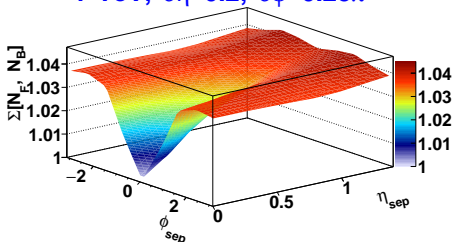
0.9 TeV, $\delta\eta=0.2$, $\delta\phi=0.25\pi$



2.76 TeV, $\delta\eta=0.2$, $\delta\phi=0.25\pi$



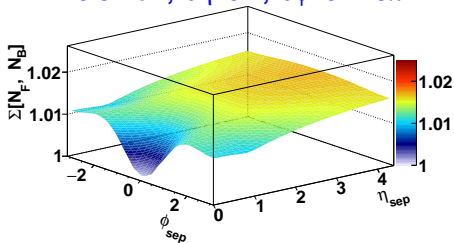
7 TeV, $\delta\eta=0.2$, $\delta\phi=0.25\pi$



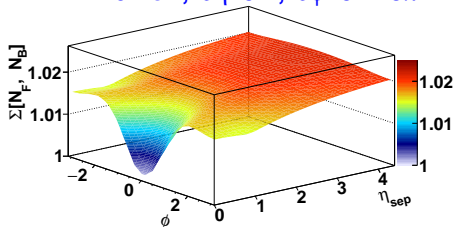
in ALICE TPC acceptance (ALICE experimental pp data analysis is in progress)

Σ for $\delta\eta$ $\delta\phi$ windows separated in azimuth and rapidity - 2

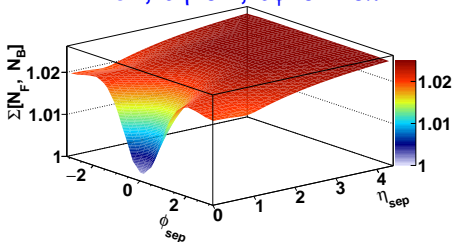
0.9 TeV, $\delta\eta=0.2$, $\delta\phi=0.125\pi$



2.76 TeV, $\delta\eta=0.2$, $\delta\phi=0.125\pi$



7 TeV, $\delta\eta=0.2$, $\delta\phi=0.125\pi$



with $\pi/8$ azimuth windows and for wider pseudorapidity range

String fusion effects

$pp \rightarrow pA \rightarrow AA$ - the increase of the string density in transverse plane leads to the string fusion

*M.A. Braun, C. Pajares, Phys.Lett. B287, 154 (1992);
Nucl. Phys. B390, 542 (1993).*

⇒ Reduction of multiplicity, increase of transverse momenta.

*N.S. Amelin, N. Armesto, M.A. Braun, E.G. Ferreira, C. Pajares,
Phys.Rev.Lett. 73, 2813 (1994).*

⇒ The influence on the Long-Range FB Correlations (LRC).

Various versions of string fusion

local fusion (overlaps)

M.A. Braun, C. Pajares Eur.Phys.J. **C16**, 349, (2000)

$$\langle n \rangle_k = \mu_0 \sqrt{k} S_k / \sigma_0, \quad \langle p_t^2 \rangle_k = p_0^2 \sqrt{k}, \quad k = 1, 2, 3, \dots \quad (20)$$

global fusion (clusters)

M.A. Braun, F. del Moral, C. Pajares, Phys.Rev. **C65**, 024907, (2002)

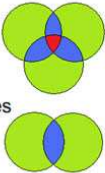
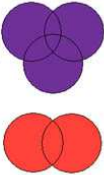
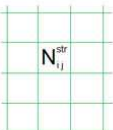
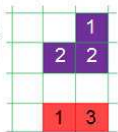
$$\langle p_t^2 \rangle_{cl} = p_0^2 \sqrt{k_{cl}}, \quad \langle n \rangle_{cl} = \mu_0 \sqrt{k_{cl}} S_{cl} / \sigma_0, \quad k_{cl} = k \sigma_0 / S_{cl} \quad (21)$$

the version of SFM with the finite lattice (grid) in transverse plane

V.Vechernin, Kolevatov R.S., hep-ph/0304295; hep-ph/0305136

Braun M.A., Kolevatov R.S., Pajares C., V.Vechernin, Eur.Phys.J. **C32**
(2004) 535

Various versions of string fusion

	"overlaps" (local fusion)	"clusters" (global fusion)
SFM	<p>○</p> <p>$C = \{S_1, S_2, \dots\}$</p> <p>S_k – area covered k-times</p>  <p>S_1 S_2 S_3</p>	<p>●</p> <p>$C = \{S_1^{cl}, S_2^{cl}, \dots\}$</p> <p>$N_1^{str} = 3$ S_1^{cl}</p> <p>$N_2^{str} = 2$ S_2^{cl}</p> <p>$k_i^{cl} = \frac{N_i^{str} \cdot \sigma_0}{S_i^{cl}}$</p> 
cellular analog of SFM	<p>□</p> <p>$C = \{N_{ij}^{str}\}$</p>  <p>$k_{ij} = N_{ij}^{str}$ – "occupation" numbers</p>	<p>■</p> <p>$C = \{S_1^{cl}, S_2^{cl}, \dots\}$</p> <p>$N_1^{str} = 5$ S_1^{cl}</p> <p>$N_2^{str} = 4$ S_2^{cl}</p> <p>$k_1^{cl} = 5/3$ $k_2^{cl} = 2$</p> <p>$S_1^{cl} = 3\sigma_0$ $S_2^{cl} = 2\sigma_0$</p> 

Domains in transverse area

The approach with string fusion on a transverse lattice (grid) was exploited later for a description of various phenomena (correlations, anisotropic azimuthal flows, the ridge) in high energy hadronic collisions in

ALICE collaboration et al., J. Phys. G **32** 1295 (2006), [Sect. 6.5.15]
V.Vechernin, Kolevatov R.S. Phys.of Atom.Nucl. **70** (2007) 1797; 1858

M.A. Braun, C. Pajares, Eur. Phys. J. C **71**, 1558 (2011)

M.A. Braun, C. Pajares, V.Vechernin, Nucl. Phys. A **906**, 14 (2013)

V.N. Kovalenko, Phys. Atom. Nucl. **76**, 1189 (2013)

M.A. Braun, C. Pajares, V.Vechernin, Eur. Phys. J. A **51**, 44 (2015)

V.V. Vechernin, Theor. Math. Phys. 184 (2015) 1271

V.V. Vechernin, Theor. Math. Phys. 190 (2017) 251

It leads to the splitting of the transverse area into domains with different, fluctuating values of color field within them.

What is similar to the models with the color field density variation in transverse plane based on the BFKL evolution

E. Levin, A.H. Rezaeian, Phys.Rev. D **84**, 034031 (2011)

or on the CGC approach *A.Kovner., M. Lublinsky*, Phys.Rev. D **83**, 034017 (2011)

Description of the configurations

$$C_N = \{N_1, \dots, N_M\} , \quad (22)$$

$$C = \{C_N, C_n^F, C_n^B, C_p^F, C_p^B\} , \quad (23)$$

$$C_n^F = \{n_1^F, \dots, n_M^F\} , \quad C_n^B = \{n_1^B, \dots, n_M^B\} , \quad (24)$$

$$C_p^F = \{p_1^{1F}, \dots, p_1^{n_1^F F}; \dots; p_M^{1F}, \dots, p_M^{n_M^F F}\} . \quad (25)$$

Then

$$n_F = \sum_{i=1}^M n_i^F , \quad p_F \equiv \frac{1}{n_F} \sum_{i=1}^M \sum_{j=1}^{n_i^F} p_i^{jF} \quad (26)$$

and the same for the p_B and n_B .

$\Sigma(n_F, n_B)$ in the model with string fusion on transverse grid

In this model we found that

$$\begin{aligned}\Sigma(n_F, n_B) &= \frac{\sum_{i=1}^M \sum_{N_i=1}^{\infty} P_i(N_i) \langle n_i^F \rangle_{N_i} \Sigma_{N_i}(n_i^F, n_i^B)}{\sum_{i=1}^M \sum_{N_i=1}^{\infty} P_i(N_i) \langle n_i^F \rangle_{N_i}} = \quad (27) \\ &= \frac{1}{\langle n_F \rangle} \sum_{i=1}^M \sum_{N_i=1}^{\infty} P_i(N_i) \langle n_i^F \rangle_{N_i} \Sigma_{N_i}(n_i^F, n_i^B),\end{aligned}$$

where we have introduced the $\Sigma_{N_i}(n_i^F, n_i^B)$ for i -th cell with N_i strings by analogy with (1) :

$$\Sigma_{N_i}(n_i^F, n_i^B) \equiv \frac{d_{N_i}(n_i^F) - \text{cov}_{N_i}(n_i^F, n_i^B)}{\langle n_i^F \rangle_{N_i}}, \quad (28)$$

$\Sigma(n_F, n_B)$ in the model with string fusion on transverse grid

If else all M cells are equivalent, $P_i(N_i) = P(N_i)$, then

$$\begin{aligned}\Sigma(n_F, n_B) &= \frac{\sum_{N_1=1}^{\infty} P(N_1) \langle n_1^F \rangle_{N_1} \Sigma_{N_1}(n_1^F, n_1^B)}{\sum_{N_1=1}^{\infty} P(N_1) \langle n_1^F \rangle_{N_1}} = \\ &= \frac{1}{\langle n_1^F \rangle} \sum_{N_1=1}^{\infty} P(N_1) \langle n_1^F \rangle_{N_1} \Sigma_{N_1}(n_1^F, n_1^B).\end{aligned}\quad (29)$$

It can be presented also as

$$\Sigma(n_F, n_B) = \sum_{k=1}^{\infty} \alpha_k \Sigma_k(\mu_F, \mu_B), \quad \alpha_k = \frac{\langle n \rangle_k}{\langle n \rangle}, \quad (30)$$

where k is a number of strings fused in a given sell and $\langle n \rangle_k$ is a mean number of particles produced from all sells with k fused strings.

The same result was obtained in the model with two types of string in [E.V.Andronov, *Theor.Math.Phys.*185(2015)1383] for the long-range part of $\Sigma(n_F, n_B)$, when at $\Delta\eta \gg \eta_{corr}$ we have $\Sigma_k(\mu_F, \mu_B) = \omega_\mu^{(k)}$ with $k=1,2$.

AA vs pp interactions - 1

The same value of $\Sigma(n_F, n_B)$ in AA collisions, as in pp, if we suppose the formation of the same strings in AA and pp collisions. Because the $\Sigma(n_F, n_B)$ does not depend on the mean value, $\langle N \rangle$, and the event-by-event fluctuations, ω_N , in the number of strings. It depends only on string properties.

If we suppose the formation of **new strings in AA collisions** (and may be in central pp collisions at high energy) with some new characteristics, compared to pp collisions, due to e.g. **string fusion** processes, then for a source with k fused strings

$$\Sigma_k(\eta_{sep}) = 1 + \mu_0^{(k)} \delta\eta [\Lambda_k(0) - \Lambda_k(\eta_{sep})]$$

For these fused strings we expect, basing on the string decay picture [V.Vechernin, Baldin ISHEPP XIX v.1(2008)276; arXiv:0812.0604]:

- 1) **larger multiplicity from one string**, $\mu_0^{(k)} > \mu_0$,
- 2) **smaller correlation length**, $\eta_{corr}^{(k)} < \eta_{corr}$.

AA vs pp interactions - 2

This corresponds to the analysis of the **net-charge fluctuations** in the framework of the string model for pp and AA collisions
[A. Titov, V. Vechernin, PoS(Baldin ISHEPP XXI)047(2012)].

$$\Sigma_k(\eta_{sep}) = 1 + \mu_0^{(k)} \delta\eta [\Lambda_k(0) - \Lambda_k(\eta_{sep})]$$

Both factors lead to the steeper increase of $\Sigma_k(\eta_{sep})$ with η_{sep} in the case of AA collisions, compared to pp.

In reality - a mixture of fused and single strings, see formula (30).
Unfortunately in this case through the weighting factors $\alpha_k = \langle n \rangle_k / \langle n \rangle$ the observable $\Sigma(n_F, n_B)$ becomes dependent on collision conditions and, strictly speaking, can not be considered any more as strongly intensive.

Conclusions

- The string model enables to understand the main features of the behavior of the strongly intensive observable $\Sigma(n_F, n_B)$. In particular the dependencies of this variable on the width of observation windows and the rapidity gap between them were found and its connection with the string two-particle correlation function was established.
- In the case with independent identical strings the model calculation confirms the strongly intensive character of this observable: it is independent of both the mean number of string and its fluctuation.
- In the case when the string fusion processes are taken into account and a formation of strings of a few different types takes place, it is shown that this observable is equal to a weighted average of its values for different string types. Unfortunately in this case through the weighting factors the observable $\Sigma(n_F, n_B)$ depends on collision conditions.