

Quad Misplacement studies for the pEDM rings

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$$\frac{d\vec{s}}{dt} = \frac{e}{m}\vec{s} \times \left[\left(\left(G + \frac{1}{\gamma} \right) \vec{B} - \frac{\gamma G}{\gamma + 1} \vec{\beta}(\vec{\beta} \cdot \vec{B}) - \left(G + \frac{1}{\gamma + 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right) + \frac{\eta}{2c} \left(\vec{E} - \frac{\gamma}{\gamma + 1} \vec{\beta}(\vec{\beta} \cdot \vec{E}) + c\vec{\beta} \times \vec{B} \right) \right]$$

- ▶ We aim to measure the spin precession rate around radial axis (in other words, vertical spin component : s_y)
- ▶ There are several terms to change s_y
- ▶ $(\eta/2c)E_r$ is the EDM effect
- ▶ $s_l(G + 1/2)B_r$, $s_l\beta_l E_y$, $s_r\beta_y E_r$, etc. are all systematic error sources
- ▶ This work is about the ones with E-field term

Quadrupole misplacement

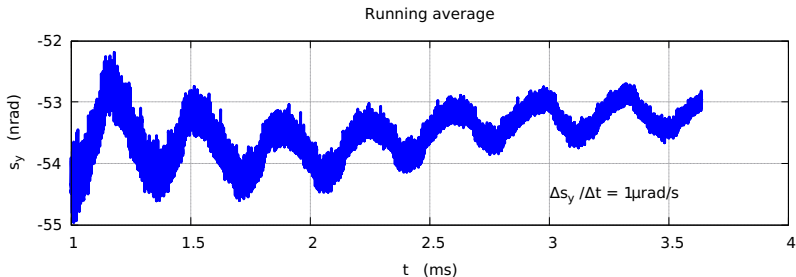


- ▶ A vertically misplaced quad ($100\mu\text{m}$) causes a vertical kick as well as a change in s_y because of $s_l\beta_l E_y$ and $s_r\beta_r E_y$.
- ▶ This effect was mentioned in several talks in the kick-off meeting (March 2017)
- ▶ In fact E_y has a direct effect only in case of geometrical phase, because it averages to zero.
- ▶ However, simulations with one vertically misplaced quad show accumulation of s_y . This is an indirect effect of E_y .

Simulations with pEDM prototype ring - 1



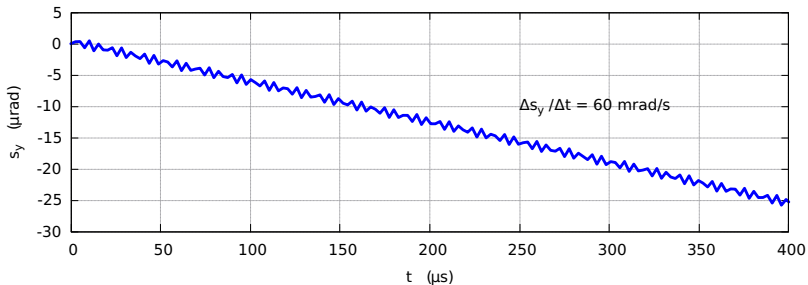
- ▶ Designed by Sig Martin
- ▶ FODO lattice with two long (≈ 25 m) straight sections
- ▶ One quad misplaced by $100 \mu\text{m}$ vertically.
- ▶ Initially spin is parallel to the momentum



Simulations with pEDM prototype ring - 2



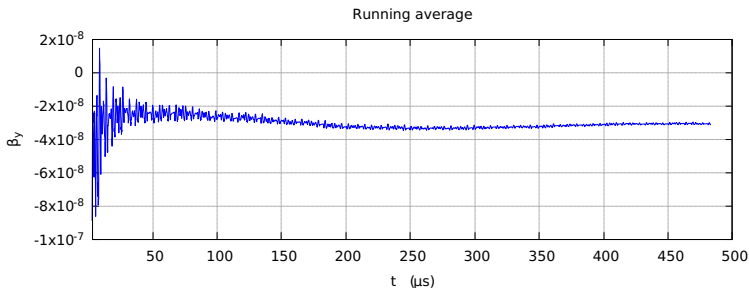
- ▶ s_y grows even faster if the spin has initial horizontal component



Simulations with pEDM prototype ring - 3



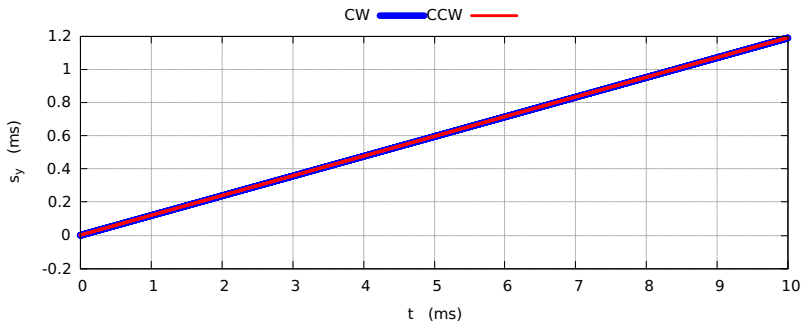
- ▶ It turns out that the effect comes from the deflectors: $s_r\beta_y E_r/c$



$$\frac{L_{def}}{L_{ring}} \frac{s_r\beta_y E_r}{c} \approx 0.57 \times \frac{0.5 \times 3.2 \times 10^{-8} \times 10^7}{3 \times 10^8} \approx 0.3nT$$

- ▶ 10^{-17} T \rightarrow 2 nrad/s
- ▶ 3×10^{-10} T \rightarrow 60 mrad/s
- ▶ Consistent with spin tracking result

CW-CCW cancellation



- ▶ CW-CCW particles cancel each other exactly.
- ▶ More can be done to decrease the growth of s_y .

Randomly misaligned quads

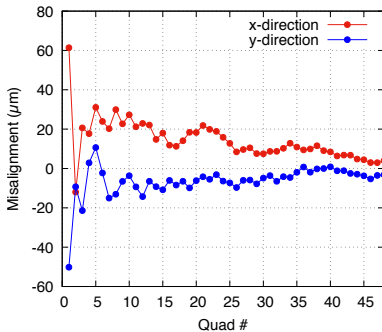
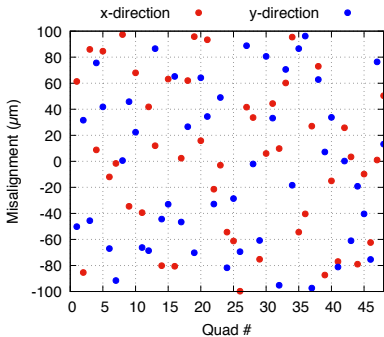


- ▶ Random misalignment introduces geometric phase effects
- ▶ We studied Lebedev's lattice. Similar with Sig's prototype lattice, but with 4-fold symmetry and larger number of elements
- ▶ Some of the results are presented in last year's kick-off meeting
- ▶ More details can be found at [arXiv:1709.01208](https://arxiv.org/abs/1709.01208)

Misalignment of the quads



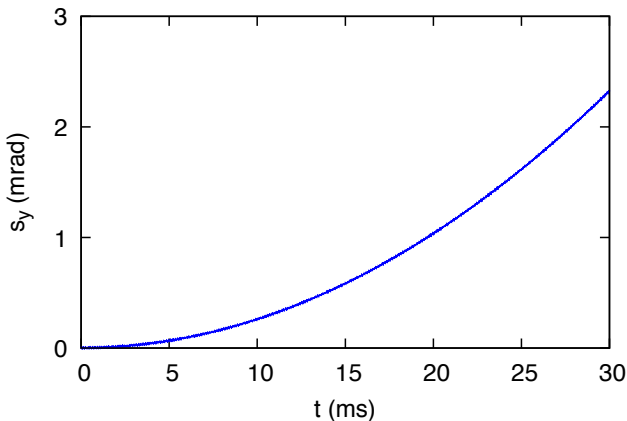
- ▶ All quads are misaligned within $\pm 100\mu\text{m}$
- ▶ The average along the ring is a few μm in both directions
- ▶ Unlike the previous case, this configuration leads to geometric phase effect



Growth of s_y

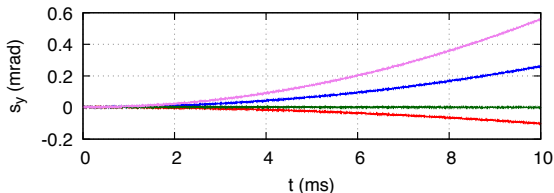
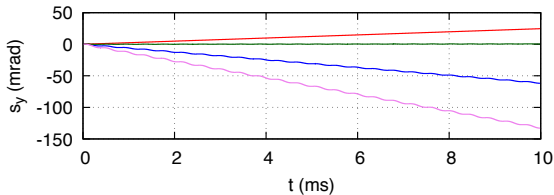


- ▶ s_y grows quadratically because of coupling with s_r , which grows linearly.
- ▶ We propose several methods to minimize the growth



Fixing the energy

- ▶ Misplaced quads shift the closed orbit, leading to off-magic momentum and growing s_r
- ▶ Simulations show that the RF cavity can be tuned to cross zero-growth
- ▶ Purple line represents the original RF configuration



Correction quadrupoles - 1

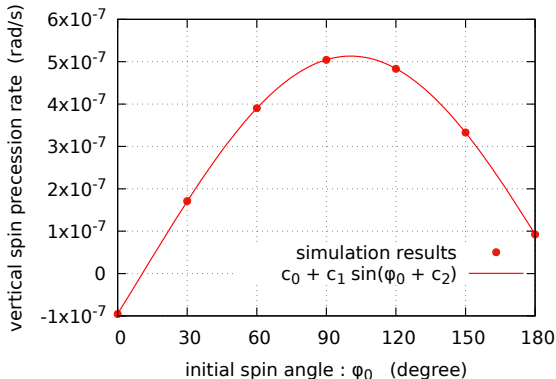


- ▶ The effect becomes more sensitive with large horizontal spin component (s_r)
- ▶ We added a correction quadrupole with weaker strength.
- ▶ Then simulated particles with large initial s_r . This amplifies the effect of the quad misalignment.
- ▶ Then we tuned the quadrupole strength to minimize the growth of s_y .
- ▶ This method can be improved by using correction quadrupoles / dipoles on both sides of every quad

Correction quadrupoles - 2

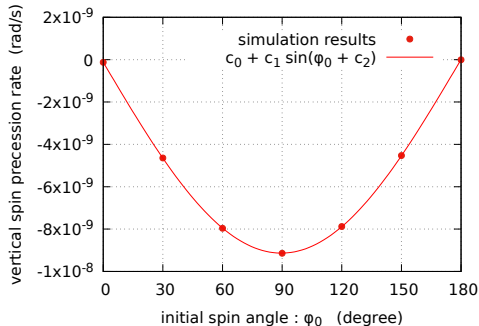


- ▶ The spin precession rate after tuning the correction quadrupole (shifting by around 2.2cm)
- ▶ Note the strong dependence on the initial angle: c_1
- ▶ There is also a large phase c_2 .



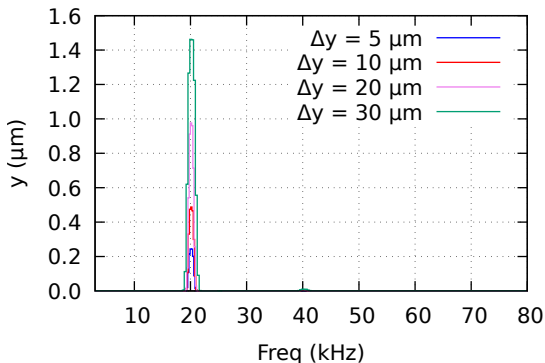
Quad strength

Quadrupole	Lattice-1	Lattice-2
k_1 (V/m ²)	-3.4×10^7	0
k_2 (V/m ²)	4.2×10^7	10^5
k_3 (V/m ²)	3.7×10^7	-2×10^5
k_4 (V/m ²)	-3.2×10^7	0



Beam-based alignment

- ▶ We simulated a ring with one quad modulated by 3%.
- ▶ The vertical motion shows a peak at that frequency.
- ▶ One can actuate the quadrupoles to minimize the peak.
- ▶ JEDI group recently made beam-based alignment at the order of $10\mu\text{m}$ without modulation



Lattice with alternating field index - 1

- ▶ Switching back to the quad-free weak focusing lattice may be another solution because of the weak vertical field.
- ▶ In previous studies we have shown that a lattice with weak focusing, alternating field index also fits the requirements of pEDM experiment.
- ▶ <https://npvm2.ceem.indiana.edu/elog1/scratch/177>

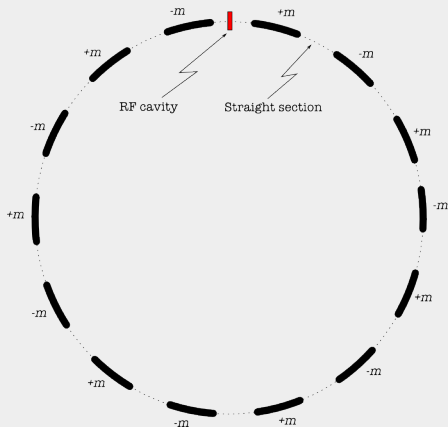
Spin coherence time simulations
for a ring with
alternating field index

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Ring Design

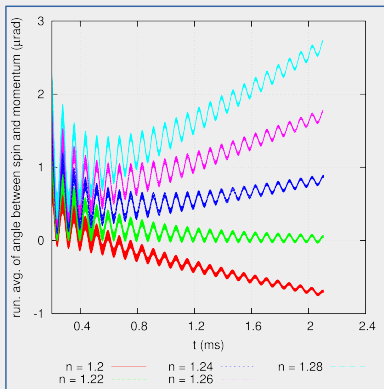
- The ring has 14 bending and straight sections
- Ring radius is 40m
- Each straight section is 1m
- One of the straight sections have RF cavity



Results – Spin Coherence Time

Field index $n = (1+m)$	Approx. SCT (s)
1.2	1333
1.22	20000
1.24	1333
1.26	645
1.28	408

- Initial $\Delta p/p = 2e-4$
- SCT values increased by more than an order of magnitude w.r.t. case of constant field index
- Average angle changes sign at a specific field index (around $n=1.22$), leading infinite SCT



- ▶ We have studied quad misplacement and it turns out that we have several tools to suppress the false EDM signals.
- ▶ Trim quadrupoles can decrease the false EDM signal by several orders of magnitude.
- ▶ Most efficient way of tuning the trim quadrupoles is to use them with horizontally polarized beams. Softer focusing also helps since the effect is proportional to vertical field.
- ▶ We can also consider the lattice with alternating index.