Gravitational waves from cosmic domain walls

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Based on

KS, Universe 3 (2017) 40 [arXiv:1703.02576] also

T. Hiramatsu, M. Kawasaki, KS, T. Sekiguchi, JCAP 10 (2013) 001 [arXiv:1207.3166]

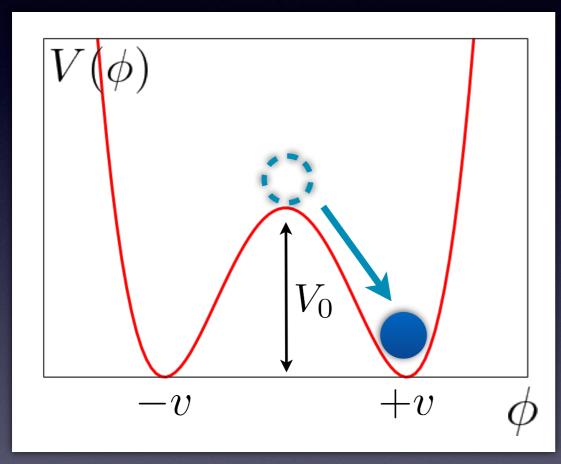
T. Hiramatsu, M. Kawasaki, KS, JCAP 02 (2014) 031 [arXiv:1309.5001]

K. Kadota, M. Kawasaki, KS, JCAP 10 (2015) 041 [arXiv: 1503.06998]

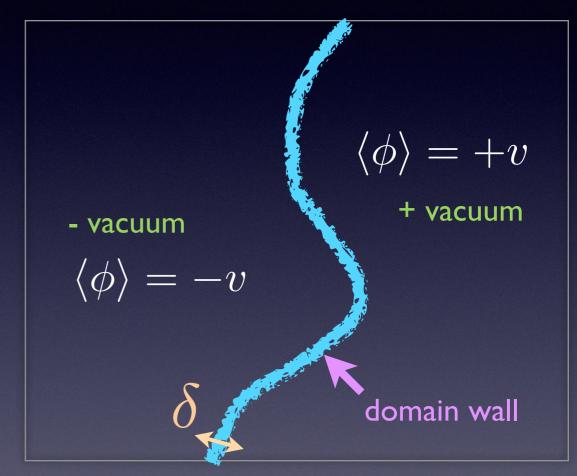
Domain wall

Example: $\mathbb{Z}_2 \to \mathbb{I}$

$$V(\phi) = \frac{\lambda}{4} (\phi^2 - v^2)^2$$



field space



real space

Width of wall: $\delta \sim m_{\phi}^{-1} \sim (\sqrt{\lambda}v)^{-1}$

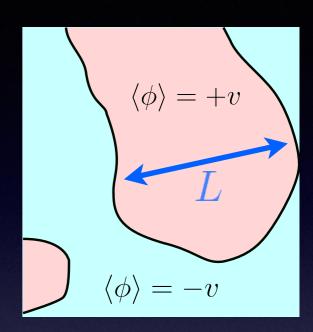
Surface energy density (tension): $\sigma \sim \delta \cdot V_0 \sim \lambda^{1/2} v^3$

Cosmological evolution

- Scaling solution Press, Ryden and Spergel (1989)
 - One wall per one Hubble radius

$$L \sim H^{-1} \sim t$$

L: distance between two neighboring walls



Energy density

$$\rho_{\rm wall} \sim \sigma L^2/L^3 \sim \sigma/t$$

decays slower than $ho_{
m matter} \propto a^{-3}$ and $ho_{
m radiation} \propto a^{-4}$

a(t) : scale factor of the universe

Come to overclose the universe (domain wall problem)

Zel'dovich, Kobzarev and Okun (1975)

Possible scenarios to avoid the problem:
 Inflation after the spontaneous symmetry breaking or unstable domain walls

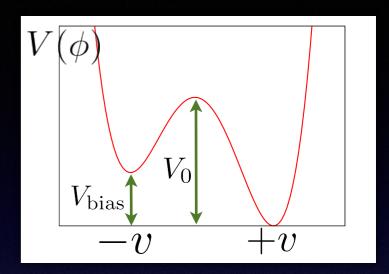
Collapse of domain walls

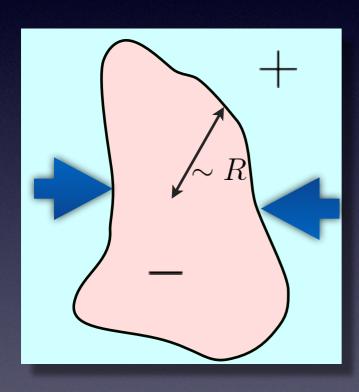
Approximate discrete symmetry (energy bias)

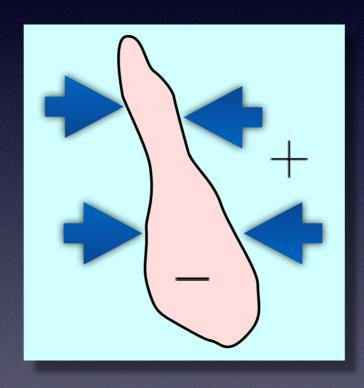
Vilenkin (1981); Gelmini, Gleiser and Kolb (1989); Larsson, Sarkar and White (1997)

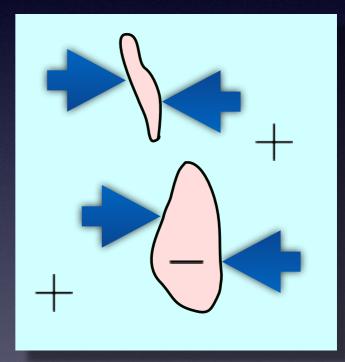
$$V_{\text{bias}} = V(-v) - V(+v) > 0$$
 $V_{\text{bias}} \ll V_0$

Acts as a volume pressure $~p_V \sim V_{
m bias}$









Annihilation occurs when p_V becomes comparable to the tension of the walls $p_T \sim \sigma/R$.



R: curvature radius

Time scale $t_{
m ann} \sim \sigma/V_{
m bias}$ corresponding to the temperature of the universe

$$T_{\rm ann} \sim 10 \,{\rm MeV} \, \left(\frac{\sigma}{{
m TeV}^3}\right)^{-1/2} \left(\frac{V_{\rm bias}}{{
m MeV}^4}\right)^{1/2}$$

Gravitational waves from domain walls

Vilenkin (1981); Preskill, Trivedi, Wilczek and Wise (1991); Gleiser and Roberts (1998)

- Gravitational waves are expected to be produced from domain walls until they are annihilated at $T \simeq T_{\rm ann}$.
- Magnitude of gravitational waves
 - Quadrupole formula

$$P \sim G \ddot{Q}_{ij} \ddot{Q}_{ij} \sim M_{
m wall}^2/t^2$$
 :Power [energy / time]

$$Q_{ij} \sim M_{\rm wall} t^2$$

$$M_{\rm wall} \sim \sigma \mathcal{A} t^2$$

Energy density

During the scaling regime

$$L \sim t$$

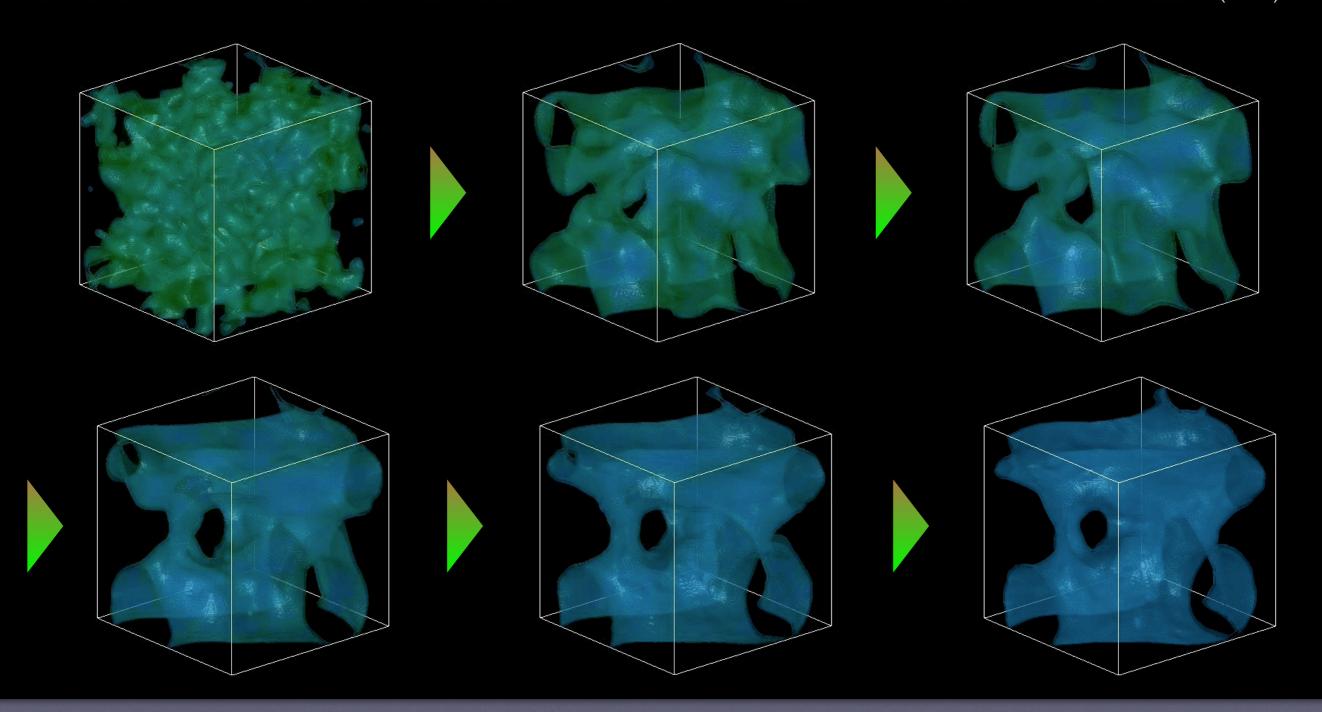
$$\rho_{\text{wall}} \sim \sigma/t$$

$$\mathcal{A} \equiv \frac{\rho_{\text{wall}}}{\sigma} t \simeq \text{const. of } \mathcal{O}(1)$$

$$\rho_{\rm gw} \sim \frac{Pt}{L^3} \sim G\mathcal{A}^2 \sigma^2$$

Numerical study

Hiramatsu, Kawasaki and KS (2010) Kawasaki and KS (2011) Hiramatsu, Kawasaki and KS (2014)

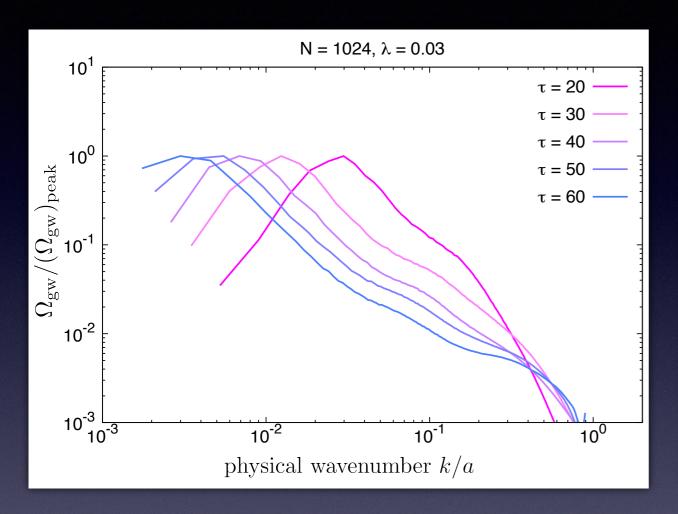


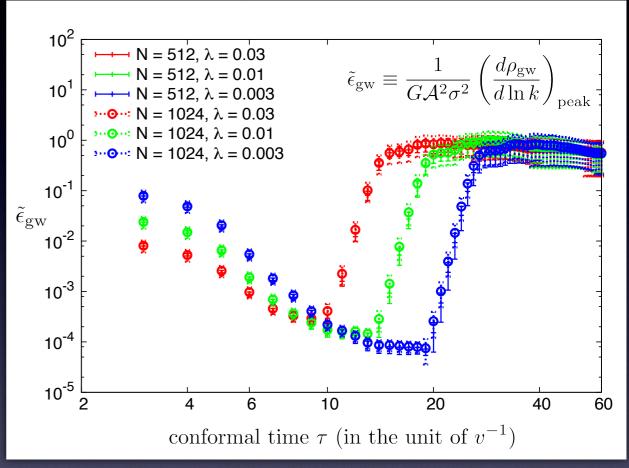
Solve the classical field equation on the lattice:

$$\ddot{\phi} + 3H\dot{\phi} - a(t)^{-2}\nabla^2\phi = -\frac{\partial V}{\partial \phi}, \qquad V(\phi) = \frac{\lambda}{4}(\phi^2 - v^2)^2$$

Numerical study

Hiramatsu, Kawasaki and KS (2014)





- Spectrum of GWs has a peak at $k/a \sim H$ and declines as $\sim k^{-1}$ at higher k.
- Confirmed the behavior $\rho_{\rm gw} \sim G A^2 \sigma^2 \sim {\rm constant}$ during the scaling regime.

Peak amplitude and frequency at the present time

- Assume that the production of gravitational waves is terminated at $T=T_{\mathrm{ann}}$.
- Peak amplitude:

Since
$$ho_{\rm gw}(t_{
m ann}) \sim G \mathcal{A}^2 \sigma^2$$
,

$$\Omega_{\rm gw} h^2(t_0)_{\rm peak} \equiv \frac{1}{\rho_{\rm crit}(t_0)/h^2} \left(\frac{d\rho_{\rm gw}(t_0)}{d\ln k}\right)_{\rm peak}
\sim 3 \times 10^{-18} \left(\frac{g_{*s}(T_{\rm ann})}{10}\right)^{-4/3} \left(\frac{\sigma}{1 \,{\rm TeV}^3}\right)^2 \left(\frac{T_{\rm ann}}{10 \,{\rm MeV}}\right)^{-4}$$

Peak frequency:

$$f_{\text{peak}} \sim \left(\frac{a(t_{\text{ann}})}{a(t_0)}\right) H(t_{\text{ann}})$$

$$\sim 10^{-9} \,\text{Hz} \left(\frac{g_{*\rho}(T_{\text{ann}})}{10}\right)^{1/2} \left(\frac{g_{*s}(T_{\text{ann}})}{10}\right)^{-1/3} \left(\frac{T_{\text{ann}}}{10 \,\text{MeV}}\right)$$

 $g_{*\rho}(T), \ g_{*s}(T)$: effective d.o.f. for the energy density and entropy density

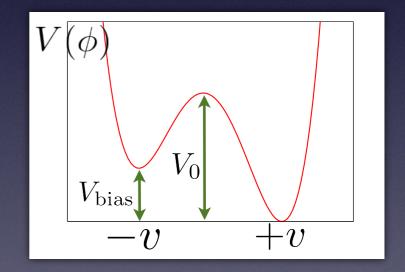
Model dependence

$$\Omega_{\rm gw} h_{\rm peak}^2 \sim 3 \times 10^{-18} \left(\frac{\sigma}{1 \,{\rm TeV}^3}\right)^2 \left(\frac{T_{\rm ann}}{10 \,{\rm MeV}}\right)^{-4}, \quad f_{\rm peak} \sim 10^{-9} \,{\rm Hz} \left(\frac{T_{\rm ann}}{10 \,{\rm MeV}}\right)$$

- The peak amplitude and frequency are determined by two parameters:
 - ullet Tension (or surface mass density) of domain walls σ
 - ullet Temperature at their annihilation $T_{
 m ann}$

$$T_{\rm ann} \sim 10 {
m MeV} \left(\frac{\sigma}{1 {
m TeV}^3} \right)^{-1/2} \left(\frac{V_{\rm bias}}{1 {
m MeV}^4} \right)^{1/2}$$

• The values of σ and $V_{\rm bias}$ (and hence $T_{\rm ann}$) depend on underlying particle physics models.



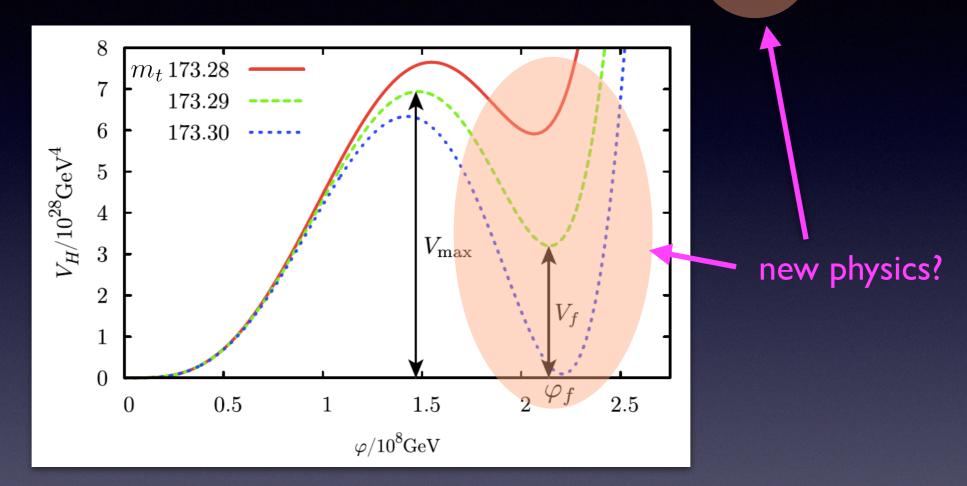


Prediction for the gravitational wave signatures differs according to the details of the models.

Standard Model Higgs field

Kitajima and Takahashi (2015)

• Higgs potential at high energy scales: $V_H = \frac{1}{4}\lambda(\varphi)\varphi^4 + \frac{\varphi^6}{\Lambda^2}$



- Quantum fluctuations during inflation lead to the formation of Higgs domain walls.
- Up to parameter values, a significant amount of gravitational waves can be produced.

Axion models

- QCD axion models can lead to N > I degenerate minima in the low energy effective potential.
 (N: integer determined by QCD anomaly)
- Formation of domain walls at the epoch of QCD phase transition. Sikivie (1982)

$$\sigma \approx 8m_a f_a^2$$

$$\approx 5 \times 10^9 \,\mathrm{GeV}^3 \, \left(\frac{f_a}{10^{12} \,\mathrm{GeV}}\right)$$

 f_a : axion decay constant

• Resulting GW spectrum has a peak at $\sim 10^{-11}\,{\rm Hz}$, but its amplitude is quite small.

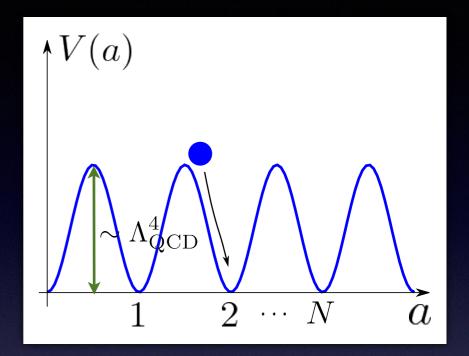
(otherwise cold axions are overproduced)

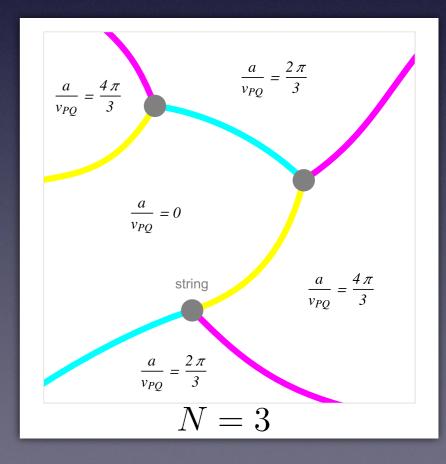
$$\Omega_{\rm gw} h_{\rm peak}^2 \lesssim 10^{-20}$$

Hiramatsu, Kawasaki, KS and Sekiguchi (2013)

• A large GW amplitude is predicted in models with axion-like particles (ALPs) or aligned axion models.

Daido, Kitajima and Takahashi (2015) Higaki, Jeong, Kitajima, Sekiguchi and Takahashi (2016)





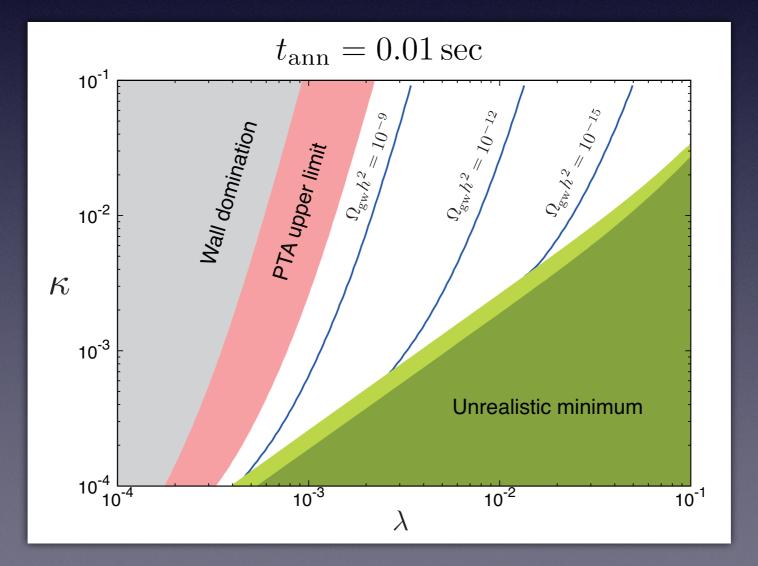
Next-to-minimal supersymmetric Standard Model (NMSSM)

Additional singlet supermultiplet with an approximate discrete Z_3 symmetry.

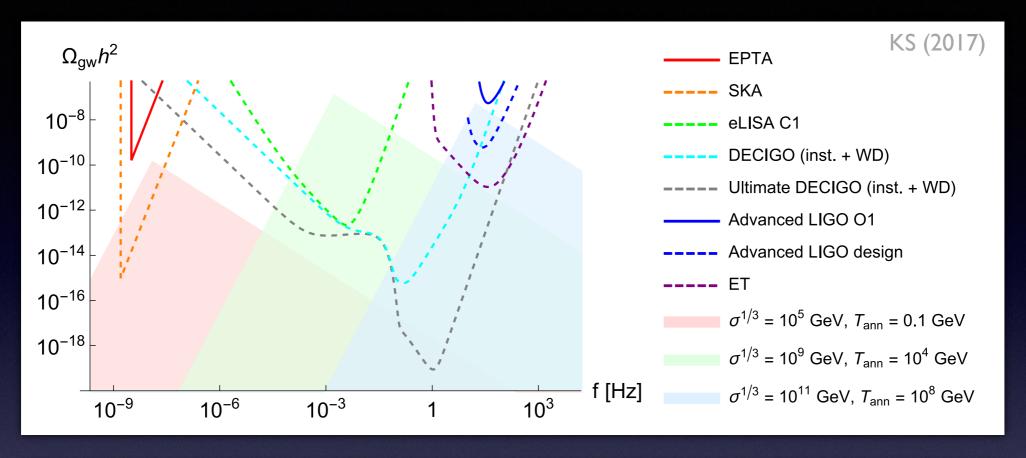
$$W_{\rm NMSSM} \supset \lambda S H_u H_d + \kappa S^3$$
 $\qquad \qquad \qquad \mu_{\rm eff} = \lambda \langle S \rangle$

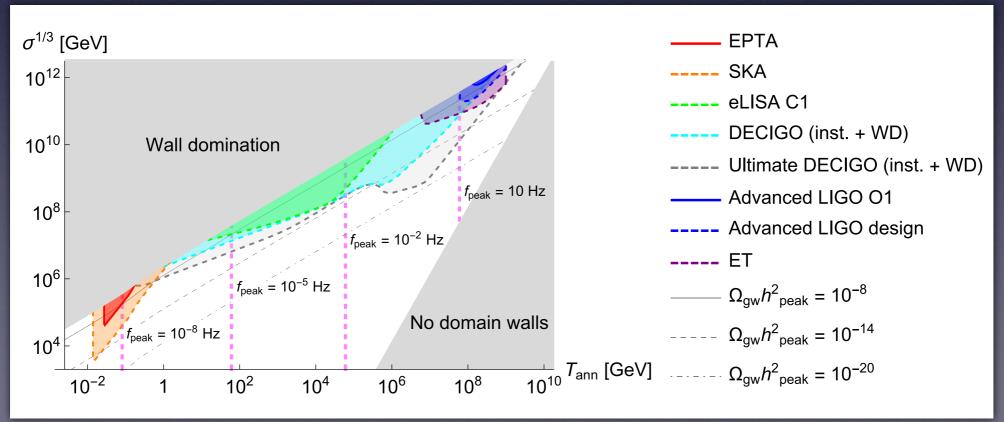
$$Z_3:\Phi o e^{2\pi i/3}\Phi$$
 Φ : every chiral supermultiplets of the NMSSM

If the annihilation of domain walls happens slightly before BBN, a significant amount of GWs can be produced. Kadota, Kawasaki and KS (2015)



Implications for present and future observations





Summary

- Formation of domain walls:
 Prediction of particle theory with spontaneously broken discrete symmetry.
- Domain walls must be unstable and annihilated in order to avoid cosmological problem.
 They can leave an imprint on gravitational waves.
- Various well-motivated particle physics models.
- Signatures can potentially be observed in forthcoming gravitational wave experiments.