



Diffraction and Low-x 2018

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Reggio Calabria, Italy

Odderon and LHC data

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Contents

- * New “open” of max-Odderon
- * Elastic hadron scattering – new data LHC
- * Phenomenological analysis of the new data
- * ρ and σ_{tot}
- * Comparing the data with High Energy Generalized Structure model (HEGSh)
- * Overlapping function at $\sqrt{s} = 13 \text{ TeV}$;
- * Total cross sections
- * Results and Summary

Did TOTEM experiment discover the Odderon?

 Evgenij Martynov^{a,*}, Basarab Nicolescu^b

(13)

 At $s \rightarrow \infty$ we have

$$\Delta\sigma(s) \equiv \sigma_{tot}^{\bar{p}p}(s) - \sigma_{tot}^{pp}(s) \rightarrow 2O_1\pi \ln(s/m^2) \quad (16)$$

$$\Delta\rho(s) \equiv \rho^{\bar{p}p}(s) - \rho^{pp}(s) \rightarrow -2\frac{O_1}{H_1} \quad (17)$$

Table 1

The values of parameters of FMO model.

Parameter	Value	Error
H_1 (mb)	0.24964	+0.02452 -0.03058
H_2 (mb)	-0.31854	+0.86147 -0.63729
H_3 (mb)	30.012	+4.304 -6.363
O_1 (mb)	-0.05098	+0.01050 -0.00989

E.Leaders, P. Gauron, B. Nicolescu, Nucl.Phys.B (1988)

$$\rho(s, t) = \text{Re}F_h(s, t) / \text{Im}F_h(s, t);$$

$$\Delta\rho = -2(-0.05098 / 0.24964) = 0.408; \text{ hence } \rho_{p\bar{p}} = 0.5;$$

We would like to stress that there is no general argument against the FMO approach.

Volume 232, number 2

PHYSICS LETTERS B

30 November 1989

FORWARD SCATTERING AT COLLIDER ENERGIES AND EIKONAL UNITARIZATION OF THE ODDERON [☆]

 J. FINKELSTEIN ¹

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H.M. FRIED, K. KANG and C-I TAN

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(8) behaves as $s^{-\sigma}$, and so $\Delta\sigma_T(s) \rightarrow O(s^{-\sigma} \log s)$.

(ii) *Bare odderon coincides with bare pomeron trajectory.* In this case, $\delta=0$, $r \rightarrow \alpha'_- / \alpha'_+ = 1$, and the first integral in (8) goes to a real constant. Since $\text{Re} B_- \sim \log s$, $\text{Im} B_- = -2\pi\alpha'_-$, we find that $\text{Re} F_- \sim s \log s$ and $\text{Im} F_- \sim s$, as claimed earlier by an analyticity argument.

We have shown that if $\delta=0$ and $r=1$, then the odderon trajectory coincides with the pomeron trajectory.

CERN $\bar{p}p \rightarrow \bar{p}p$ $\sqrt{s} = 540 \text{ GeV}$

Problems

$$\rho = 0.24 \pm 0.04 \quad (\text{UA4 Coll. M. Bozzo et al.})$$

$$\rho = 0.135 \pm 0.015 \quad (\text{UA4/2 Coll., C. Augier et al.})$$

Comment

$$1992 \quad \rho = \cancel{0.24} \rightarrow 0.19 \pm 0.03 \quad (\text{O.V. Selyugin, Yad.Fiz. 55, 841})$$

$$1995 \quad \rho = \cancel{0.135} \rightarrow 0.17 \pm 0.02 \quad (\text{O.V. Selyugin, Phys.Lett.B 198, 583})$$

$$2009 \quad \rho = 0.172 \pm 0.009$$

(A.Kendi, E.Ferreira, T.Kodama, arXiv : 0905.1955(hep - ph))

ODDERON s and t dependence

Max Odderon - $\text{Re}(O_-) \propto \ln(s/s_0)^2$; $\text{Im}(O_-) \propto \ln(s/s_0)$;

A. Donnachie, P.V. Landshoff

$$\frac{-\lambda \hat{t}}{\hat{t} + \tau} \quad \text{at } -\hat{t} < t_1;$$

$$g(t) = C \frac{t_0^3}{t^4} \quad \text{at } |t| > t_0; \quad C = 0.04; \quad t_0 = 4.23 \text{ GeV}^2;$$

$$g(t) = C \frac{1}{t_0} e^{2(1-t^2/t_0^2)} \quad \text{at } |t| < t_0;$$

E. Martynov, arXiv: 1305.3093
(E.Leader, P. Gauron, B. Nicolescu,
Phys.Lett.B (1990)

$$O(s, t) = z \, t [O_1(s, t) + O_2(s, t) + O_3(s, t)]$$

O.V.S. HEGS model

$$O(s, t) = \frac{h_t \, t}{1 + r_o^2 t} e^{Bt/4 \, \text{Ln}(s/s_0)} ;$$

Simple phenomenological analysis of 13 TeV data

$$F_1^{em}(t) = \alpha f_1^2(t) \frac{s - 2m^2}{t}; \quad F_3^{em}(t) = F_1^{em};$$

and for spin-flip amplitudes:

$$F_2^{em}(t) = \alpha \frac{f_2^2(t)}{4m^2} s; \quad F_4^{em}(t) = -F_2^{em}(t),$$

$$F_5^{em}(t) = \alpha \frac{s}{2m\sqrt{|t|}} f_1(t) f_2(t),$$

where the form factors are:

$$f_1(t) = \frac{4m_p^2 - (1+k)t}{4m_p^2 - t} G_d(t);$$

$$f_2(t) = \frac{4m_p^2 k}{4m_p^2 - t} G_d(t);$$

$$\frac{dN}{dt} = \mathcal{L} \left[\frac{4\pi\alpha^2}{|t|^2} G^4(t) - \frac{2\alpha (\rho(s,t) + \phi_{CN}(s,t)) \sigma_{tot} G^2(t) e^{-\frac{B(s,t)|t|}{2}}}{|t|} + \frac{\sigma_{tot}^2 (1 + \rho(s,t)^2) e^{-B(s,t)|t|}}{16\pi} \right] \quad (1)$$

Non-exponential behavior (origins)

1. Non-linear Regge trajectory

- a) Contributions of the meson cloud (J.Pumplin, G.L. Kane; O.V.S.)
- b) Pion loops (Anselm, Gribov, Khoze, Martin; Jenkovski et al.)

2. Different slopes of the other contributions (real part, odderon, spin-flip amplitude)

3. Unitarization

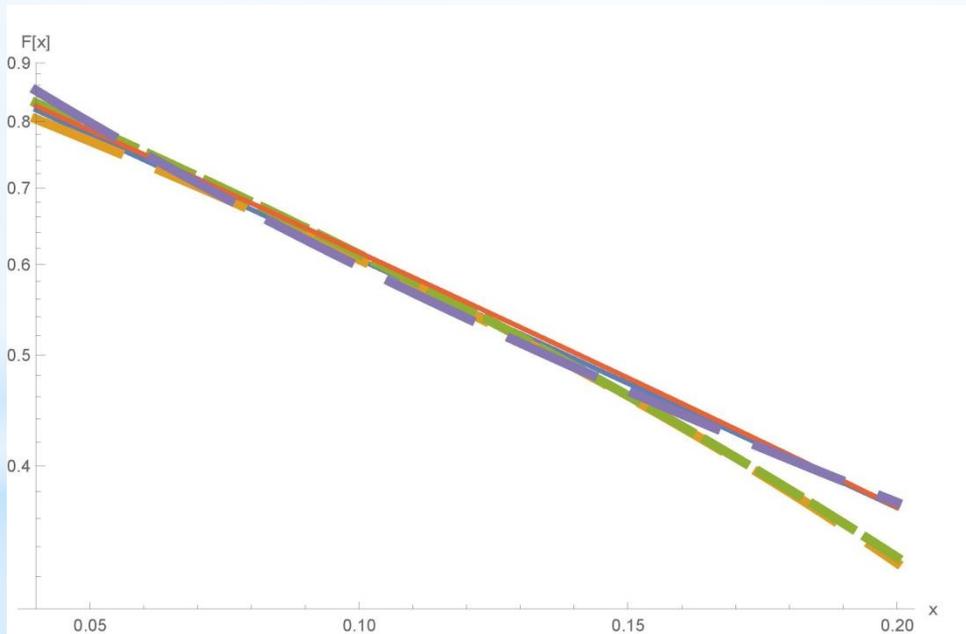
$$\Gamma(b) = e^{-b^2/R^2}; \quad \rightarrow F_1(t) \approx e^{5t};$$

$$\Gamma(b) = \delta(R_0); \quad \rightarrow F_1(t) \approx J_0(R\sqrt{|t|});$$

$$\Gamma(b) = e^{-(b-R_0)^2/R_0^2}; \quad \rightarrow F_1(t) \approx e^{2.8t} J_0(2.8\sqrt{|t|});$$

$$\Gamma(b) = C(0-R_0); \quad \rightarrow F_1(t) \approx J_1(R_0\sqrt{|t|}) / R_0\sqrt{|t|};$$

$$\Gamma(b) = e^{-\mu(\sqrt{4R_0^2-t})}; \quad \rightarrow F_1(t) \approx e^{-5R_0(\sqrt{\mu^2-t}-\mu)};$$



Phenomenologic analysis (exponentials)

$$F^h(s, t) = (i + \rho) \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2}$$

$$F^h(s, t) = (i + \rho) \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2 - Ct^2}$$

$$F^h(s, t) = (i + \rho) \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2 + D(\sqrt{4\mu^2 - t} - 2\mu)}$$

$$F^h(s, t) = [i + \rho(t)] \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2 + D(\sqrt{4\mu^2 - t} - 2\mu) + Ct^2} \quad f(t)_{em.}^2;$$

$$F^h(s, t) = h \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2 + i\varphi(t)}$$

TOTEM analysis 13 TeV

$$0.0085 \leq |t| \leq 0.07 \text{ GeV}^2; \quad N = 80.$$

Table 5: Summary of results for various fit config

N_b	$ t _{\max} = 0.07 \text{ GeV}^2$	
	χ^2/ndf	ρ
1	0.7	0.09 ± 0.01
2	0.6	0.10 ± 0.01
3	0.6	0.09 ± 0.01

1. Normalization on $\sigma_{el} = 31.0 \pm 1.7 \text{ mb} (5.5\%).$

$$\sigma_{tot} = 110.6 \pm 3.4 \text{ mb} (3.1%).$$

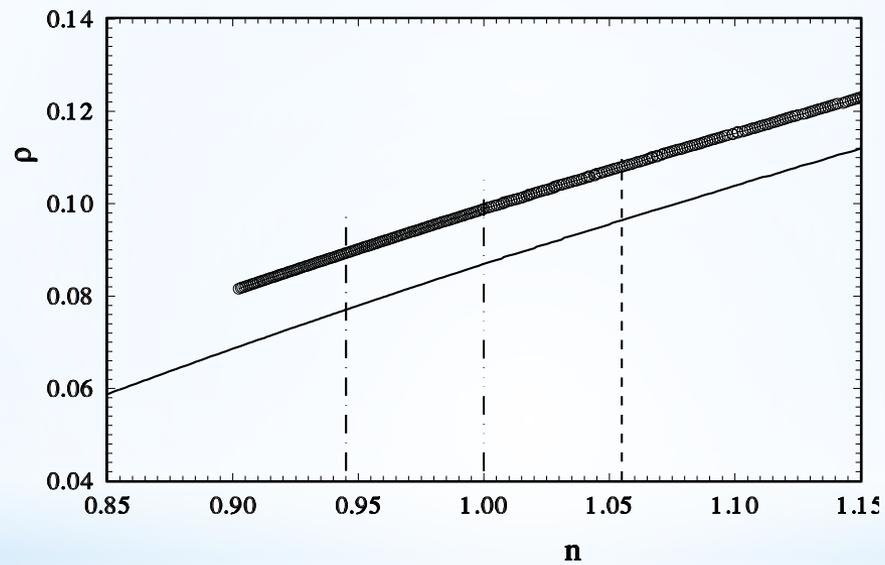
2. “unprecedented precision” $\rho = 0.1 \pm 0.01 \text{ mb} (10%).$

$$\text{UA4/2 – (in text) } \rho = 0.135 \pm 0.007 \text{ mb} (5.).$$

3. *CNI term from* $A_N(1 - i\alpha G(t));$

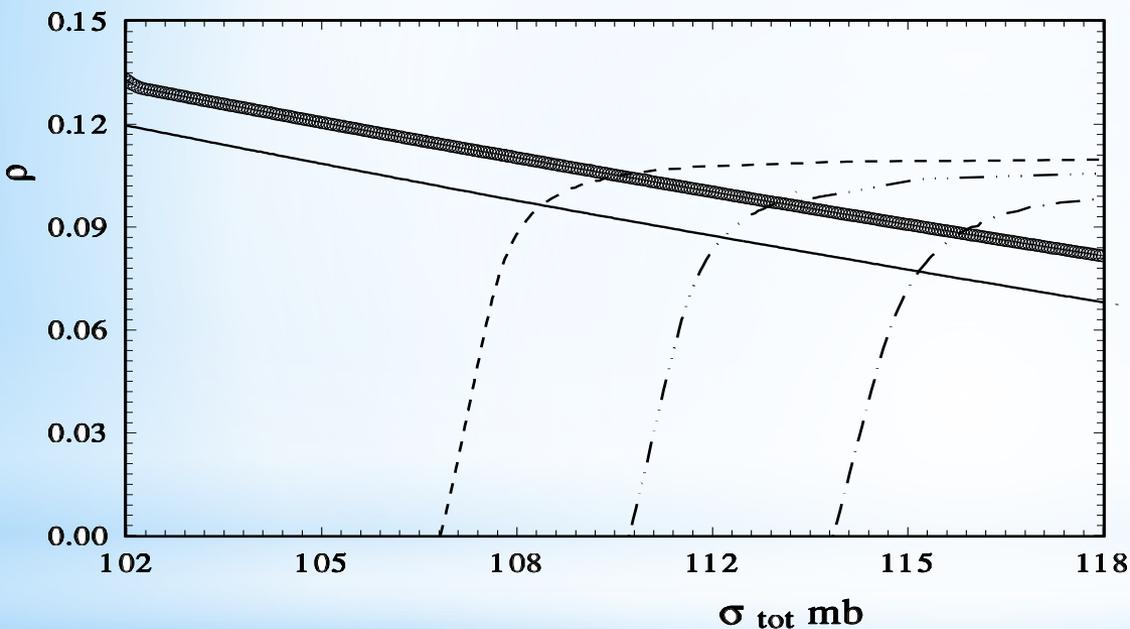
TOTEM 13 TeV

$0.00085 \leq |t| \leq 0.07 \text{ GeV}^2; \quad N = 80.$



Simple exponential (Born term)

$$F_B^h(s, t) = h [i - \rho_0(1 + at)] f_1(t)^2 \sigma_{tot} e^{\alpha' t}$$

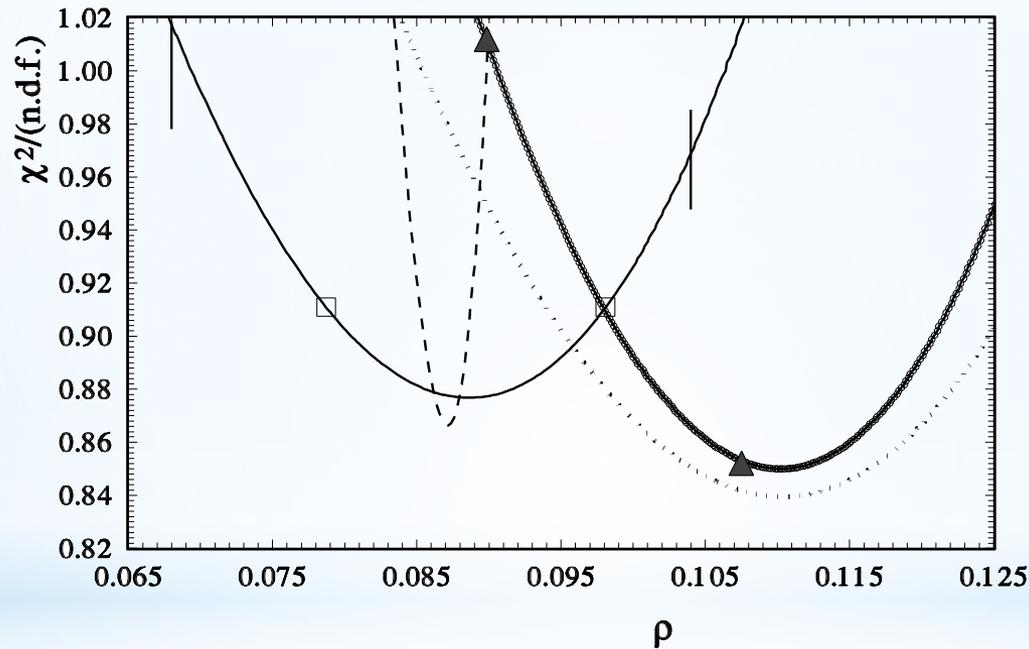


With form-factor
Without form-factor n-free

n(fix) = 1.055; 1.0; 0.945

Eikonal representation

$$F_B^h(s, t) = h \hat{s}^\Delta f_1(t)^2 \sigma_{tot} e^{\alpha' t \text{Ln}(\hat{s})}$$



$$\rho_{Born}(\sqrt{s} = 13 \text{TeV}, t = 0) = 0.089 \pm 0.013;$$

$$\rho_{Unitar.}(\sqrt{s} = 13 \text{TeV}, t = 0) = 0.11 \pm 0.016;$$

TOTEM 13 TeV

(extraction $\text{Re}F(s,t)$ from experimental data)

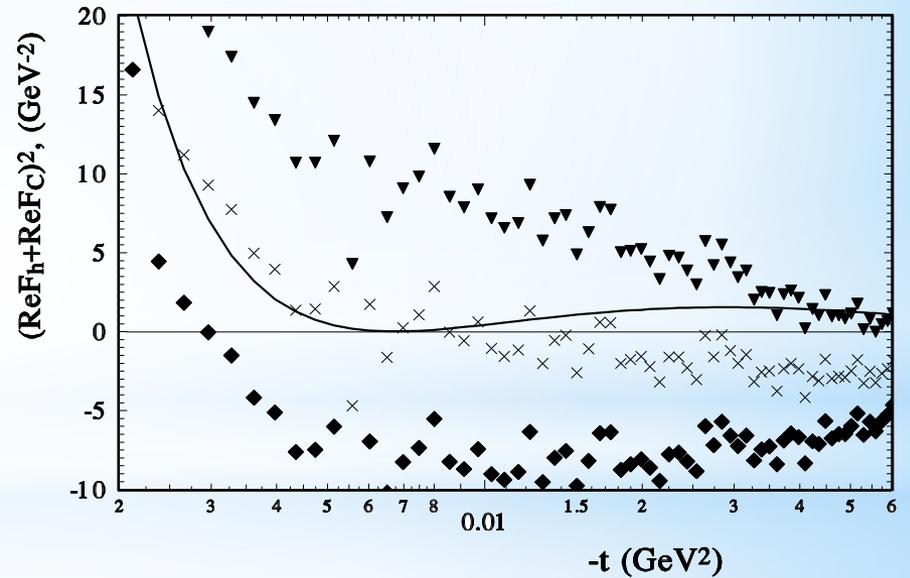
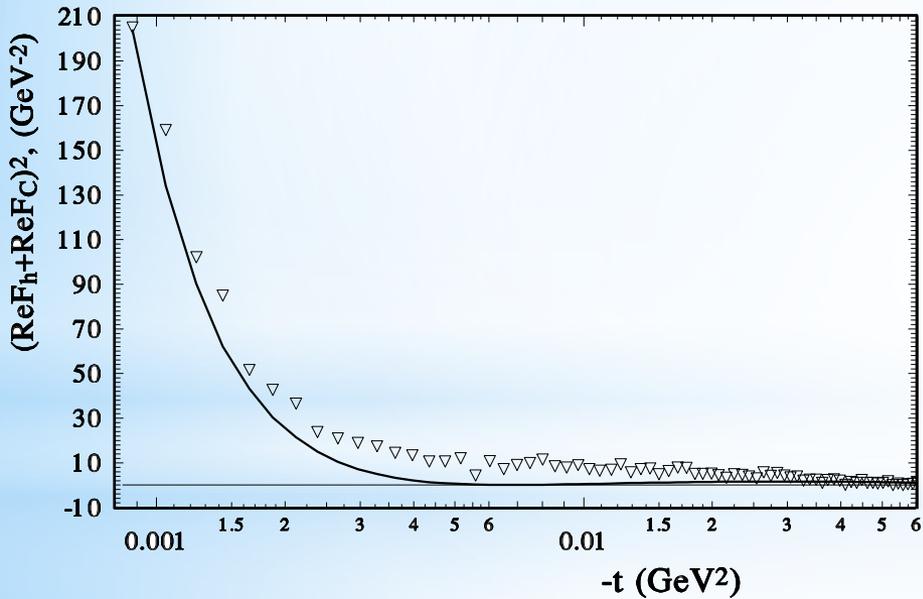
O.S. "VI Intern. Conf. On Diffraction...", Blois, France,(1995);
O.S., P. Gauron, B. Nicolescu, Phys.Lett. B629 (2005) 83-92;

$$\Delta_R^{th}(t) = [\text{Re } F^h(t) + \text{Re } F^C(t)]^2 ; \quad \sigma_{tot} \text{ mb}, B(t), \rho(t=0), n;$$

$$\Delta_R^{Exp}(t) = \left[\frac{d\sigma}{dt} \Big|_{\text{exp.}} - k\pi (\text{Im } F^h(t) + \text{Im } F^C(t)) \right]^2 / (k\pi)$$

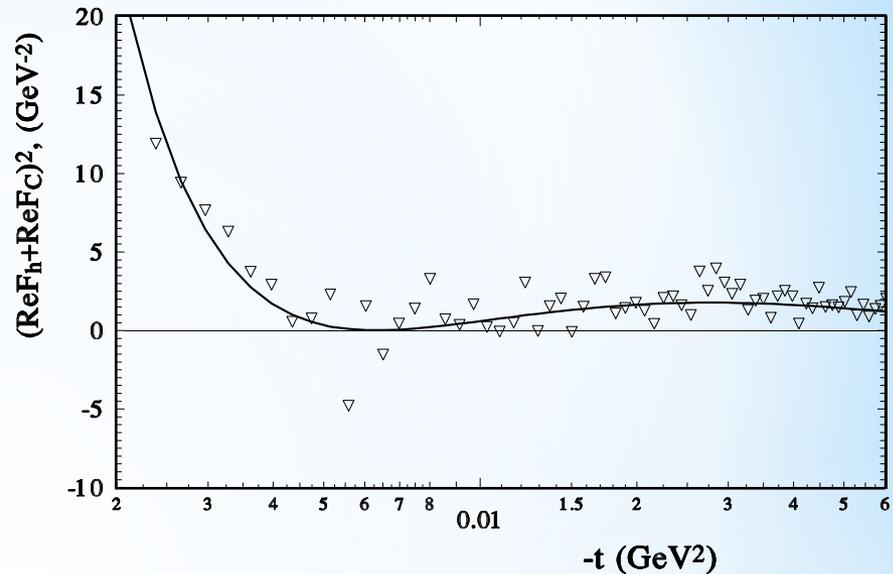
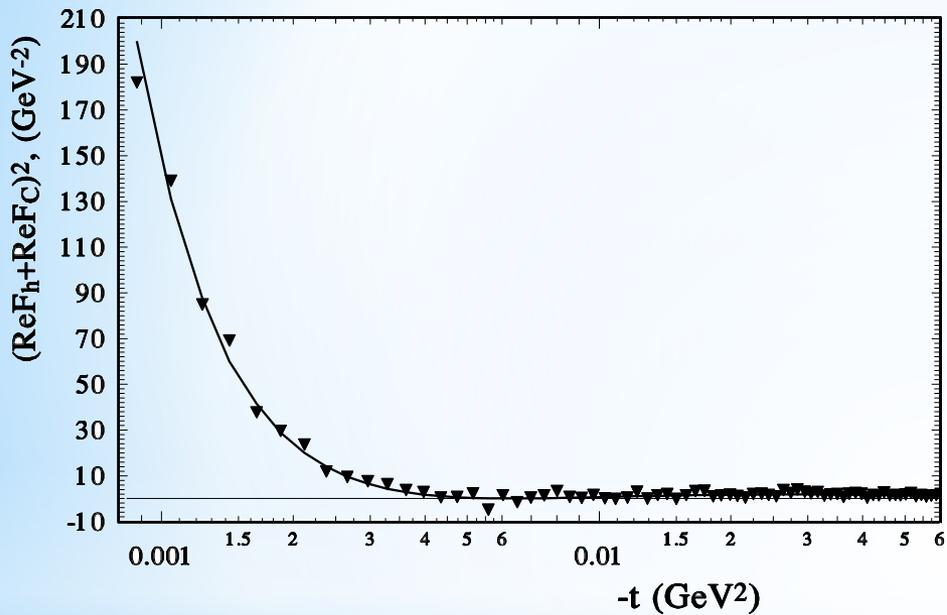
$$F_h(s,t) = h (1 + \rho) \sigma_{tot} e^{Bt/2};$$

$$\sigma_{tot} = 110.6 \text{ mb}, \quad B = 20.36 \text{ GeV}^{-2}, \quad \rho(t=0) = 0.1, \quad n = 1.;$$



$$F_B^h(s, t) = h (i + \rho) \sigma_{tot} e^{\alpha' t} f_1(t)^2;$$

$$\sigma_{tot} = 108 \text{ mb}, \quad \rho(t=0) = 0.108, \quad n = 1.06;$$



$$t_0 = -0.0063 \text{ GeV}^2; \quad F_C(t_0) = -2.25; \quad \text{Re}F_h = 2.25; \quad \rho(t_0) = 0.105;$$

Odderon and HEGS model

High Energy General Structure (HEGS) model O.V.S. - Eur. Phys. J. C (2012) 72:2073

Extending of model (HEGS1) – O.V. S. Phys.Rev. D 91, (2015) 113003

$$\hat{s} = s / s_0 e^{-i\pi/2}; \quad s_0 = 4m_p^2.$$

$$n=980 \rightarrow 3416; \quad 9 \leq \sqrt{s} \leq 8000 \text{ GeV}; \quad 0.00037 < |t| < 15 \text{ GeV}^2;$$

$$F_1^B(s, t) = h_1 G_{em}(t) (\hat{s})^{\Delta_1} e^{\alpha_1 t \ln(\hat{s})}; \quad F_2^B(s, t) = h_2 G_A(t)^2 (\hat{s})^{\Delta_1} e^{\alpha_1/4 t \ln(\hat{s})}$$

$$F^B(\hat{s}, t) = F_1^B(\hat{s}, t) (1 + R_1 / \sqrt{\hat{s}}) + F_2^B(\hat{s}, t) (1 + R_2 / \sqrt{\hat{s}}) + F_{odd}^B(s, t);$$

$$F_{Odd}^B(s, t) = h_{Odd} G_A(t)^2 (\hat{s})^{\Delta_1} \frac{t}{1 - r_o^2 t} e^{\alpha_1/4 t \ln(\hat{s})};$$

$$B(t) = (\alpha_1 + k_0 q e^{k_0 t \ln \hat{s}}) \ln \hat{s}.$$

5+4 – fitting parameters

General Parton Distributions -GPDs

Electromagnetic
form factors
(charge
distribution)

Gravitation
form factors
(matter distribution)

$$F_1^D(t) = \frac{4M_p^2 - t \mu_p}{4M_p^2 - t} G_D(t);$$

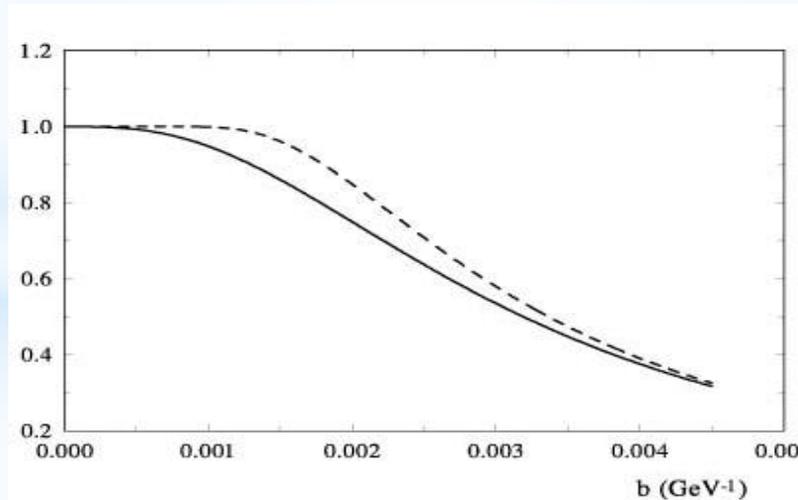
$$G_D(t) = \frac{\Lambda^4}{(\Lambda^2 - t)^2};$$

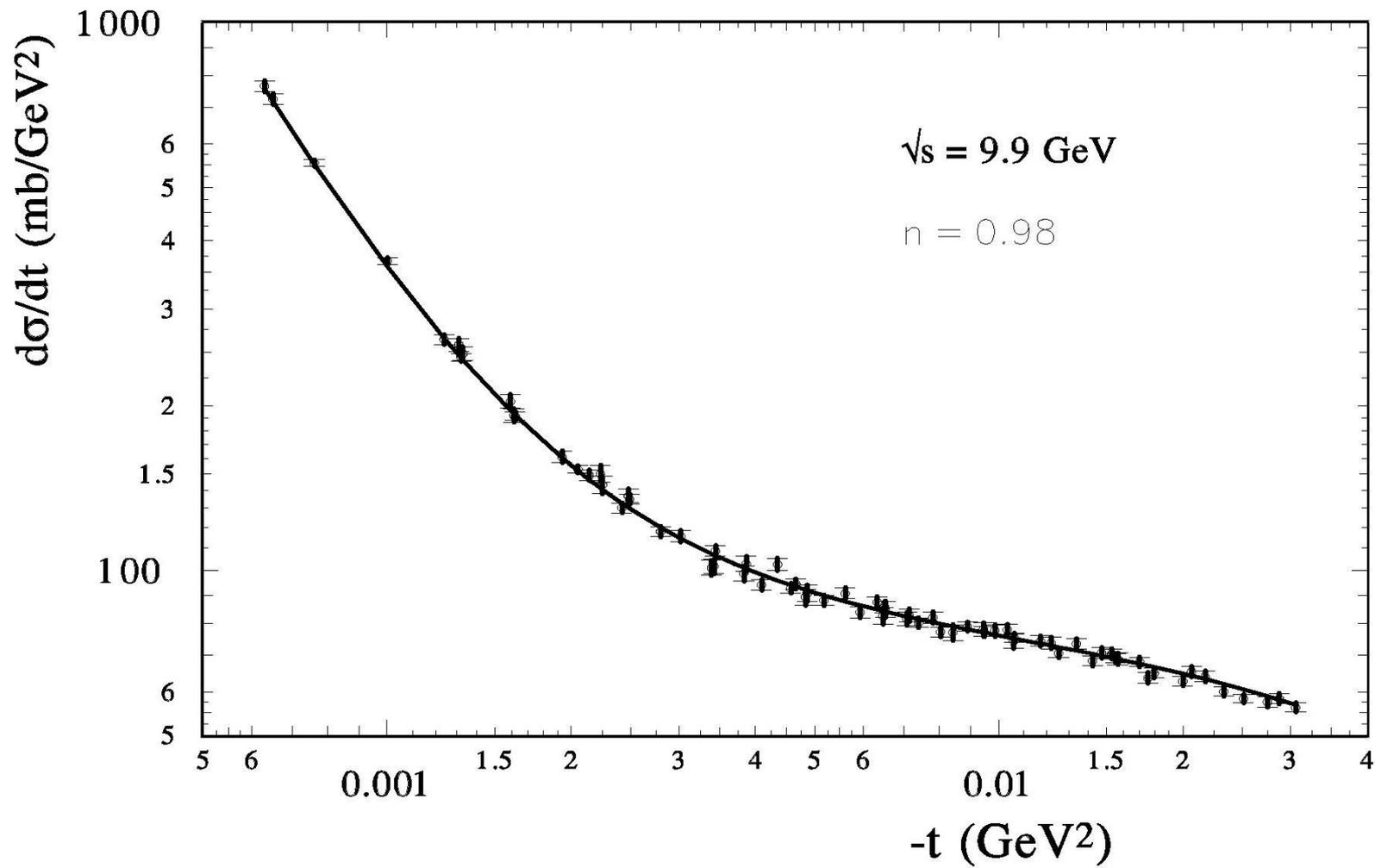
$$G_A(t) = \frac{\Lambda_A^4}{(\Lambda_A^2 - t)^2};$$

UNITARIZATION → eikonal representation

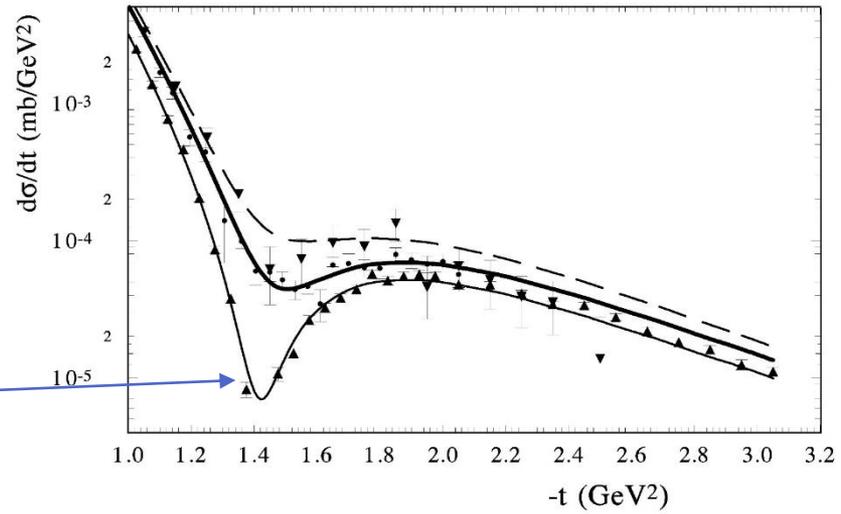
$$\chi(s,b) = 2\pi \int_0^\infty q J_0(bq) F_B^h(s,q) dq \qquad \chi(s,b) = -\frac{1}{2k} \int_{-\infty}^\infty dz V[\sqrt{z^2 + b^2}]$$

$$F^h(s,t) = \frac{1}{2\pi} \int_0^\infty b J_0(bq) [1 - e^{-\chi(s,b)}] db$$

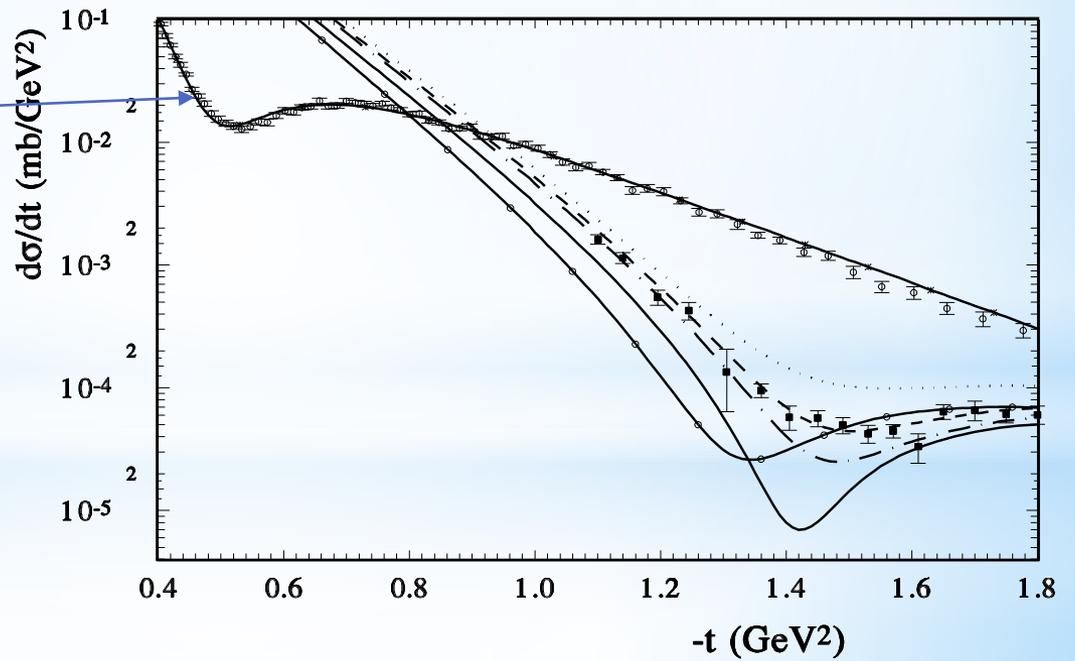


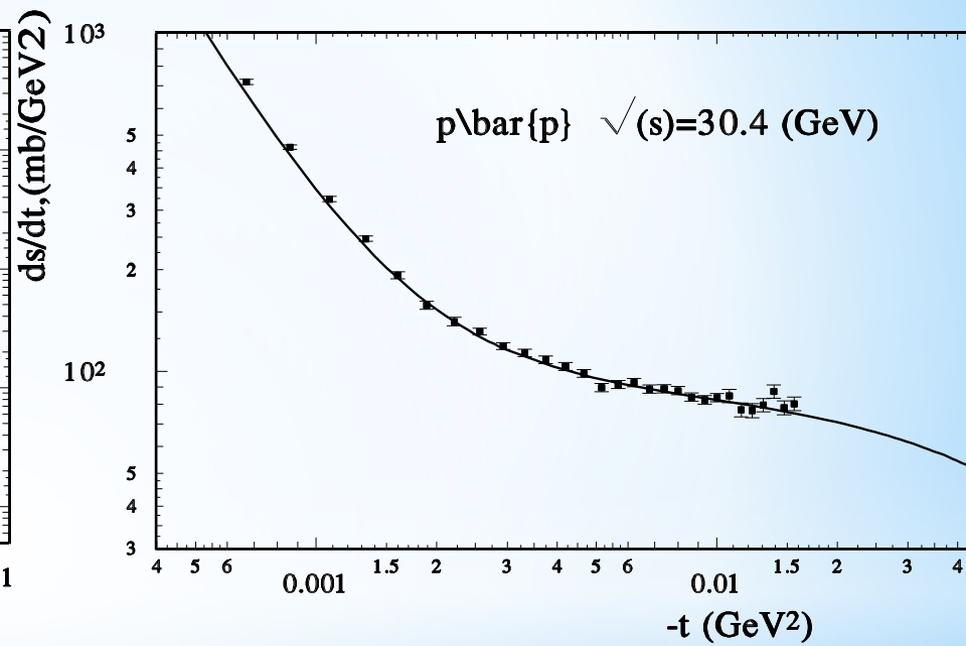
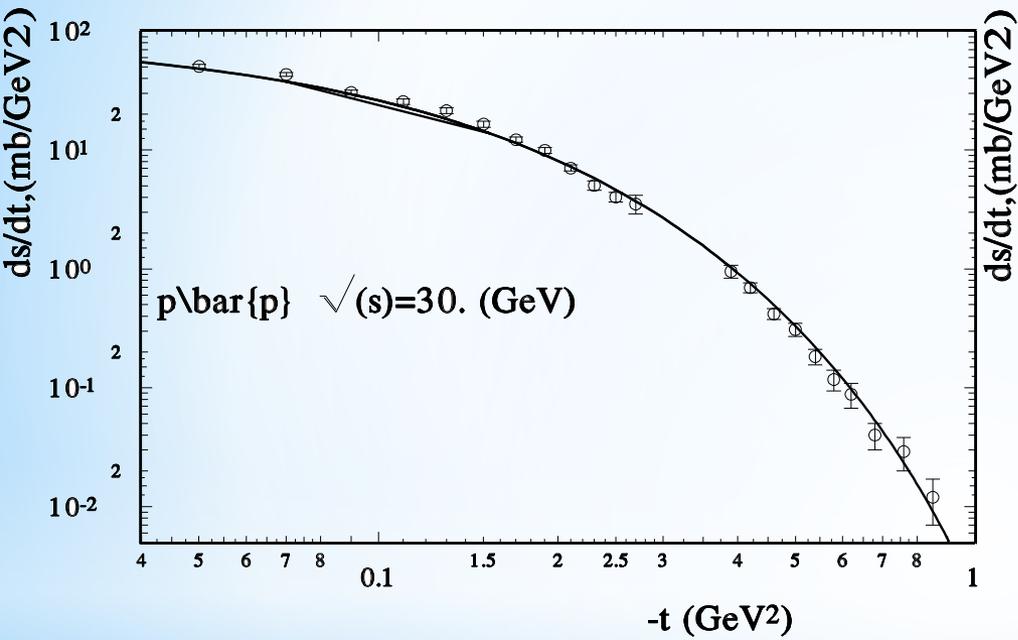


$\sqrt{s} = 30 \text{ GeV};$



$\sqrt{s} = 7 \text{ TeV};$

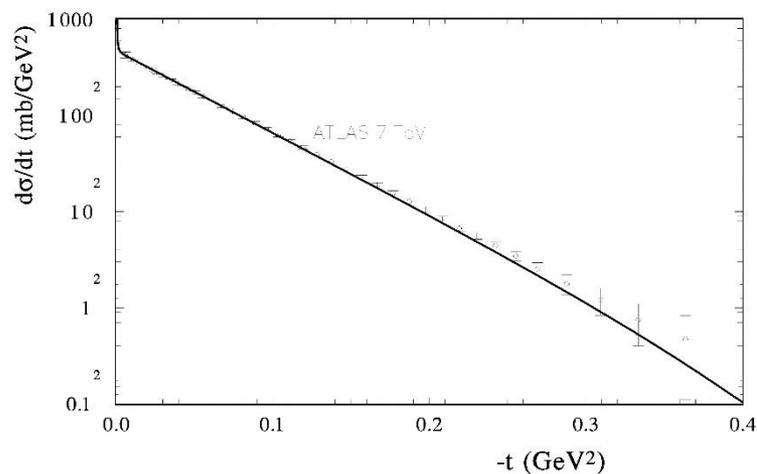
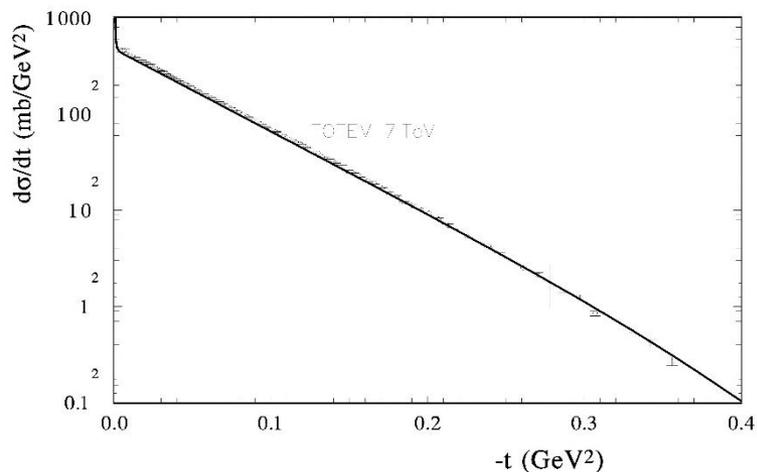




7 TeV (TOTEM) - t [0.00515 – 0.371] 7 TeV (ATLAS) - t [0.0062 – 0.3636]

$n = 0.94$

$n = 1.0$

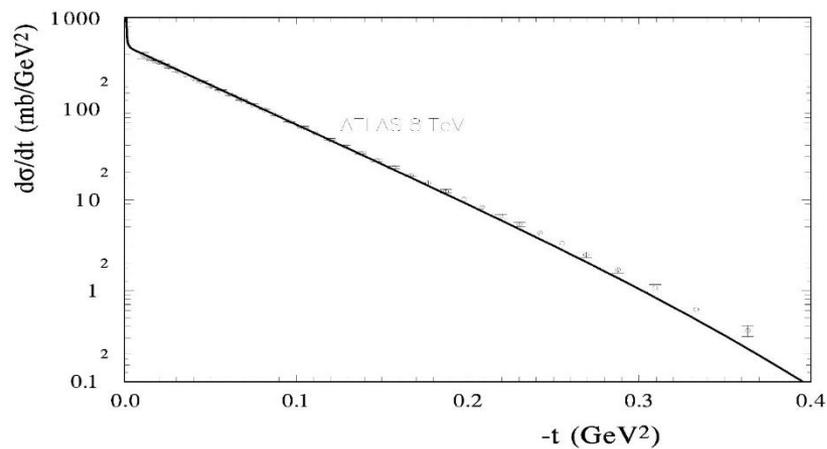
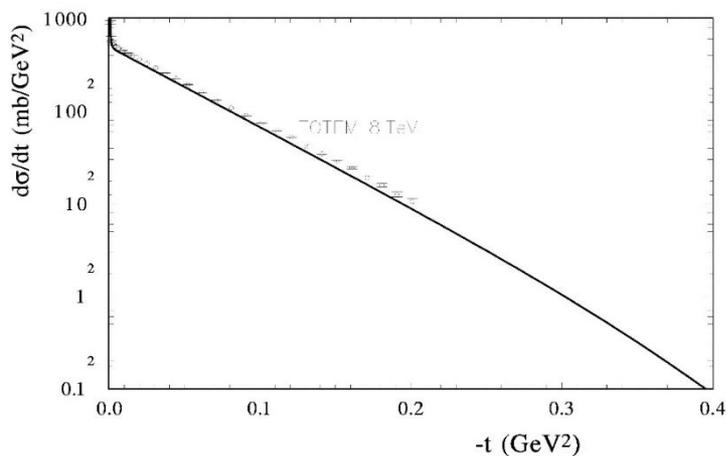


8 TeV (TOTEM) - t [0.000741 – 0.201]

8 TeV (ATLAS) - t [0.01050 – 0.3635]

$n = 0.9$

$n = 1.0$



HEGS-h model and Odderon

$$n \rightarrow 870; \quad 100 \leq \sqrt{s} \leq 13000 \text{ GeV}; \quad 0.0008 < |t| < 3 \text{ GeV}^2;$$

$$F_{Odd}^B(s, t) = G_A(t)^2 (\hat{s})^{\Delta_1} (h_{Odd}^c + h_{Odd}^t \frac{t}{1 - r_0^2 t}) e^{B(t)/4t \ln(\hat{s})};$$

$$B(t) = \alpha_1 [1 + q e^{\alpha_0 t \ln \hat{s}} / (1 + \alpha_0 \ln \hat{s})].$$

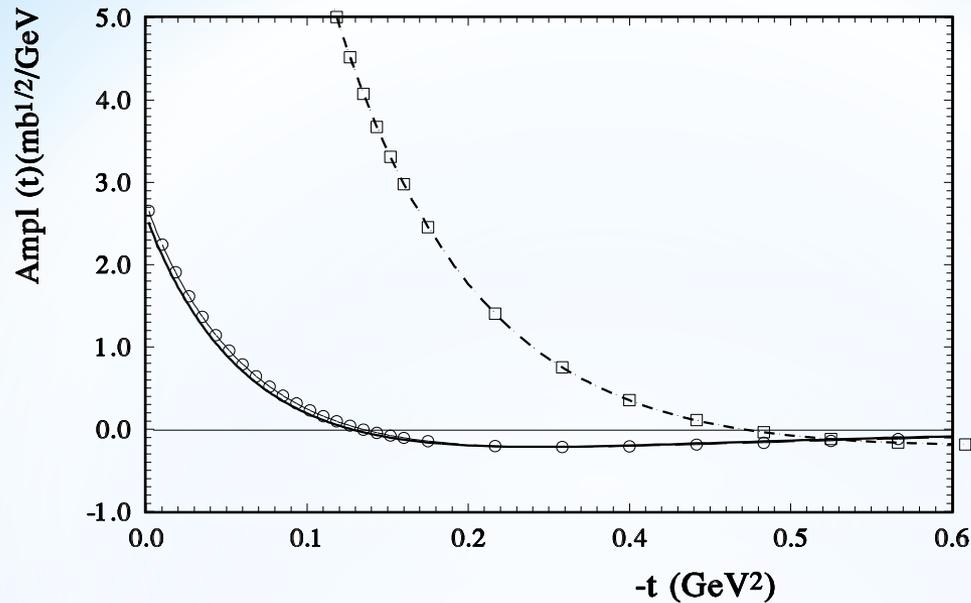
Without Oddron – 2 fitting parameters – pomerons constants: $h_1; h_2;$

$$\sum \chi^2 = 1207;$$

With Oddron – 5 fitting parameters (+ 3) :

$$+ h_{Odd}^c; h_{Odd}^t; r_0^2;$$

$$(5) \rightarrow \sum \chi^2 = 1132;$$



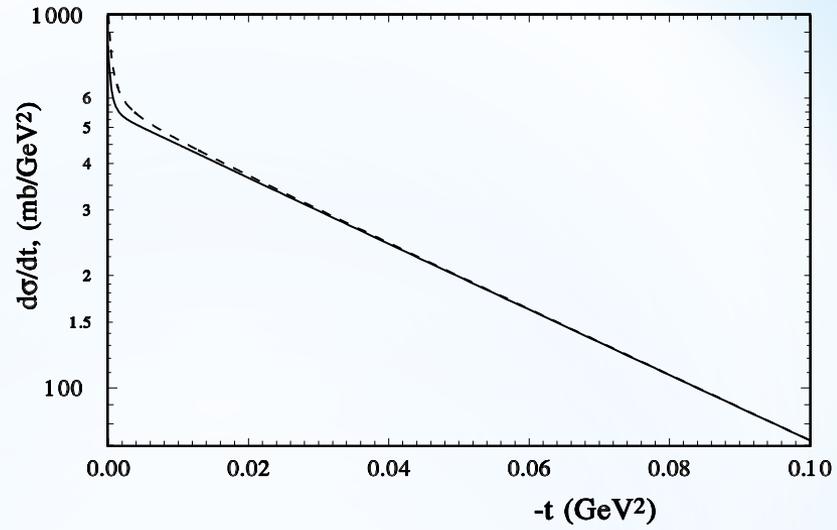
$$R = \frac{h_{Odd}^c}{h_{Odd}^t} = 0.2;$$

The amplitude of pp at $\sqrt{s} = 13\text{TeV}$

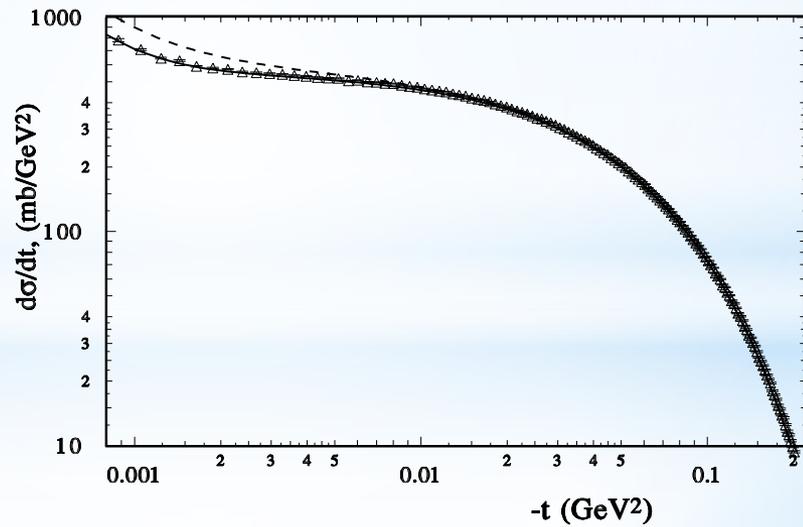
with h_{Odd}^t dashed line – $\text{Im } F(t)$; hard line $\text{Re } F(t)$;

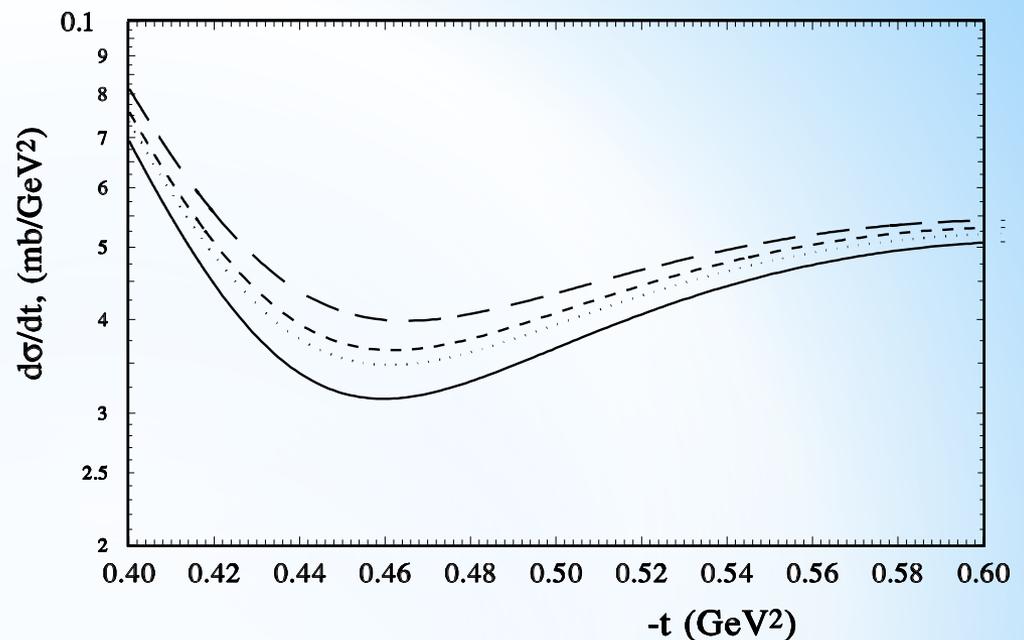
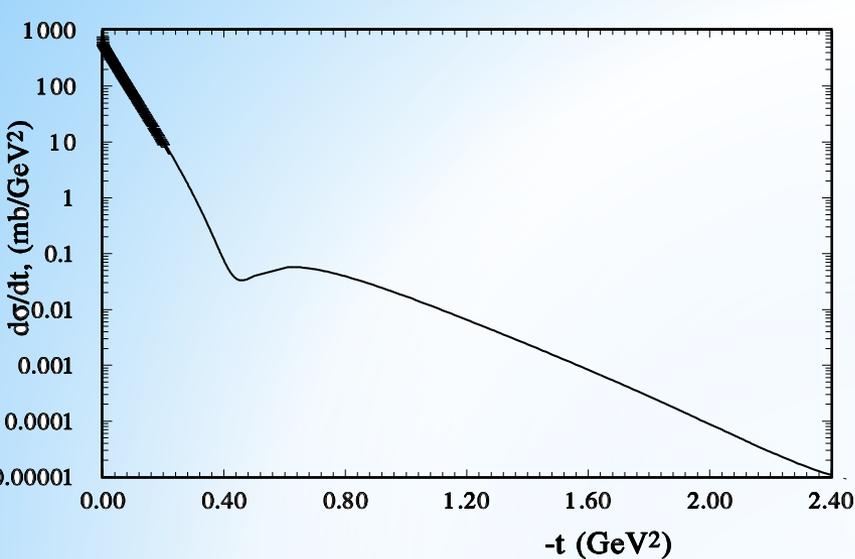
with h_{Odd}^c and h_{Odd}^t (\square – $\text{Im } F(t)$; O – $\text{Re } F(t)$);

dashed line – $p\bar{p}$



Δ – TOTEM data ($\sqrt{s} = 13\text{TeV}$)





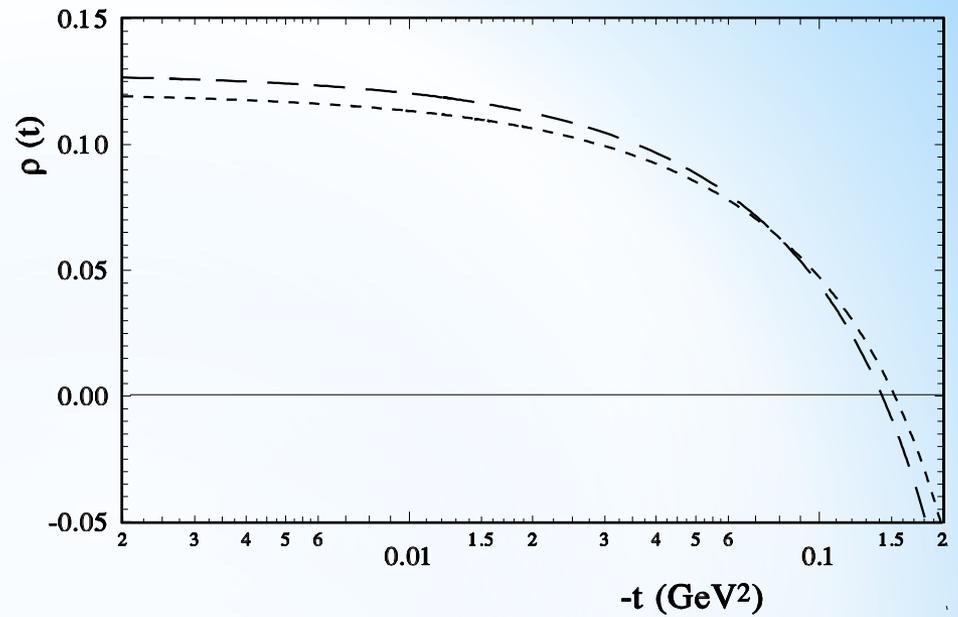
hard line pp ; *long dashed* $p\bar{p}$ (*HEGSh*);
dotted – pp ; *short – dashed* – $p\bar{p}$ (*without Odderon*);

$HEGSh \rightarrow -t_{\min} = 0.46 GeV^2; -t_{\max} = 0.62 GeV^2; R = 1.78;$

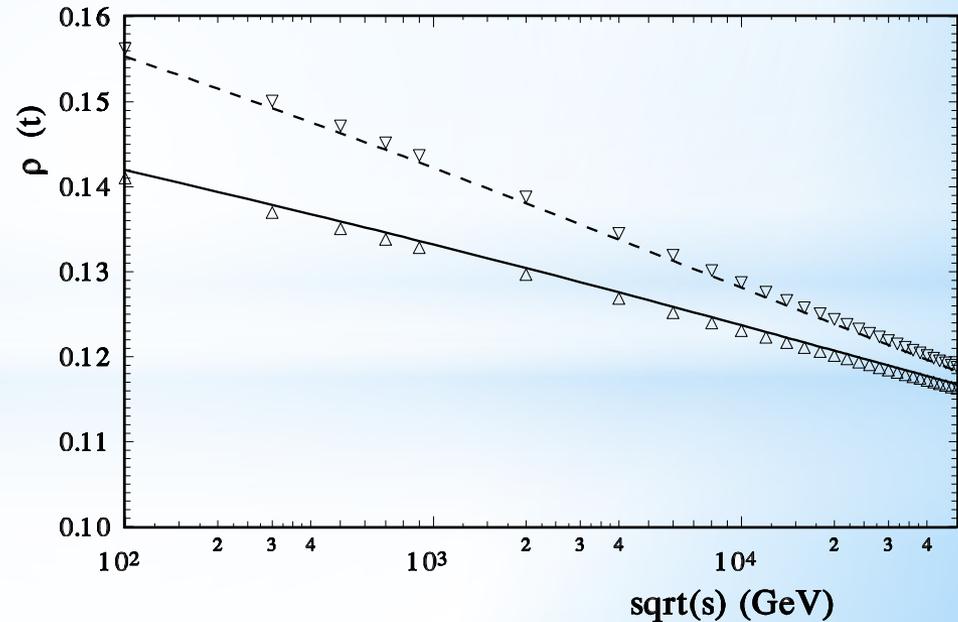
$TOTEM \rightarrow -t_{\min} = 0.47 GeV^2; -t_{\max} = 0.638 GeV^2; R = 1.78;$

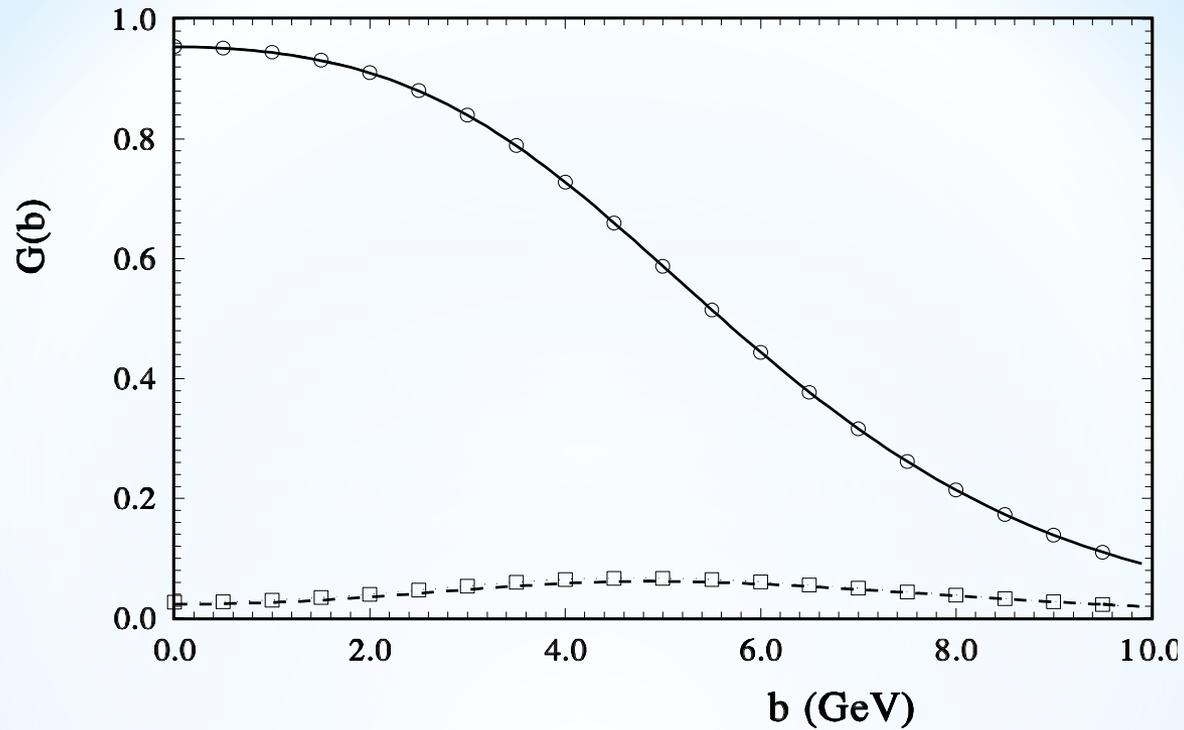
Nemez, talk on workshop , May 28 (2018)

$\rho(t)$ at $\sqrt{s} = 13\text{TeV}$;
 long dashed line – pp ;
 short dashed line – $p\bar{p}$;



$\rho(s, t = 0)$;
 hard line – pp ;
 dashed line – $p\bar{p}$;
 Δ and ∇ with h_{Odd}^C .



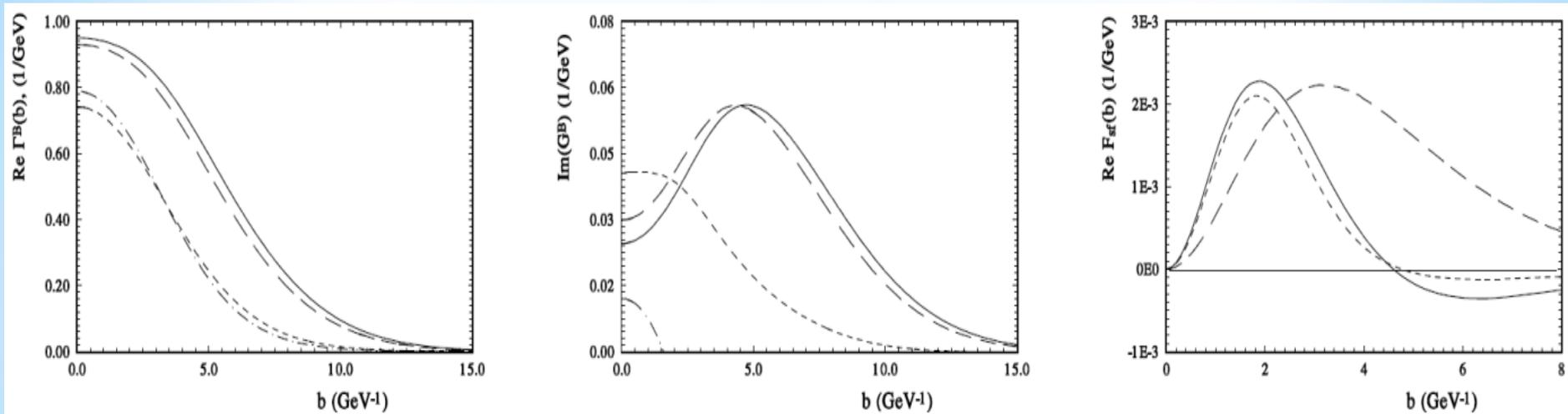


The $G(b)$ of pp at $\sqrt{s} = 13\text{TeV}$

with h_{Odd}^t dashed line – $\text{Im}G(b)$; hard line $\text{Re}G(t)$;

with h_{Odd}^C and h_{Odd}^t (\square – $\text{Im}G(t)$; O – $\text{Re}G(t)$);

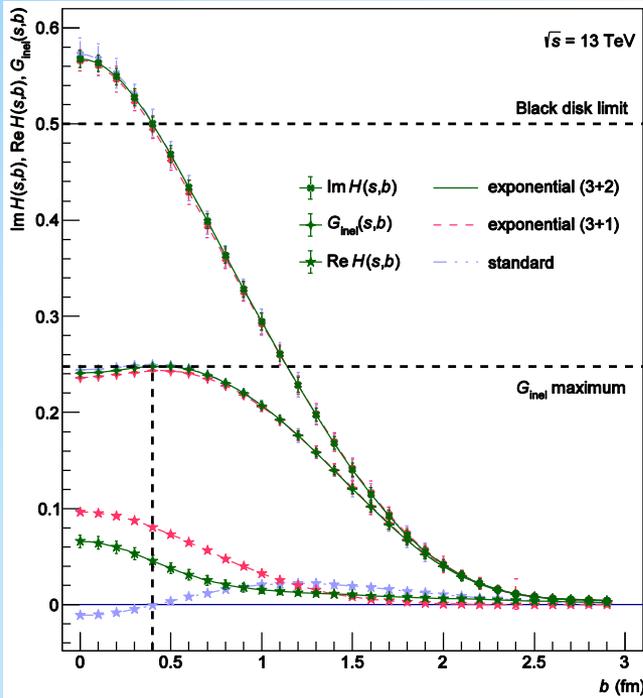
Extending of model (HEGS1) – O.V. S. Phys.Rev. D 91, (2015) 113003



The profile function $\Gamma(s, b)$: the real part ([left](#)) and imaginary part ([middle](#)) at energies $s=9.8$ GeV (dashed line), $s=52.8$ GeV (dash-dotted line), $s=7$ TeV (long dashed line), $s=14$ TeV ([solid](#) line).

the spin-flip amplitude in the b - representation (right) ([solid](#) line - eq.(12), dashed line - eq.(13) long dashed line - with q factor and normal exponential form

A.Alkin, E.Martynov, O.Kovalenko, S.Troshin



$$\text{Im } H(s, b = 0) = 0.572 \pm 0.001;$$

$$\sigma_{tot} = 112.05 \pm 0.05; \quad \rho(t = 0) = 0.099 \pm 0.001;$$

TOTEM

$$\sigma_{tot} = 110.6 \pm 3.4 \text{ mb}; \quad \rho(t = 0) = 0.1 \pm 0.01;$$

$$F^h(s, t) = \frac{1}{2\pi} \int_0^\infty b J_0(bq) G(s, b) db$$

$-t_1 \geq 0.0156 \text{ GeV}^2$ – *Coulomb free*;

$$I_i = \sqrt{\frac{16\pi s^2}{k_{mb}} \left. \frac{d\sigma}{dt} \right|_{t=t_i} - (\text{Re } A(t))^2}. \quad (12)$$

hence

$$I_i = |\text{Im } A(t)|;$$

* Summary

1. $\rho_{eik.}(\sqrt{s} = 13 TeV, t = 0) = 0.11 \pm 0.015;$

2. HEGSh model:

$$\rho_{HEGS}(\sqrt{s} = 13 TeV, t = 0) = 0.13 \pm 0.015;$$

$$\sigma_{tot}(\sqrt{s} = 13 TeV) = 106 \pm 2.5 mb;$$

3. B(t) – non-linear behavior (form factor, eikonalization);

4. The max-Odderon contribution at $t=0$ is very small;

5. The form of the diffraction minimum at 13 TeV shows the Odderon contribution;
most important Odderon contribution at low energies and non-small t .

6. Eikonalization leads to $\text{Re}(\text{Odd}_{\max})$ growth as $\text{Log}(s/s_0)$;

7. The standard eikonal approximation works perfectly

from $\sqrt{s}=9$ GeV up to 13 TeV.

THANKS FOR YOUR ATTENTION

analysis 13 TeV

$$F^h(s, t) = (i + \rho) \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2}$$

σ_{tot}, mb	B(=0)	$\rho(t=0)$	n	$\Sigma \chi^2$
107.2 fx	18.23	-0.146	1. fx	377
110.6fx	20.17	0.024	1 fx	617
114.0 fx	21.7	0.103	1 fx	2253
111.8	20.78	0.086	1 fx	70.65
114.1	20.26	0.08	0.96	69.85

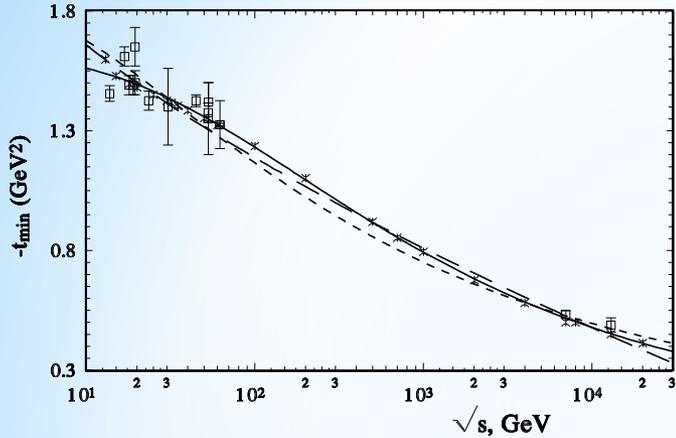
$$F^h(s, t) = (i + \rho) \frac{\sigma_{tot}}{4\pi \cdot 0.38938} e^{Bt/2} f_{em}(t)^2;$$

σ_{tot}, mb	B(=0)	$\rho(t=0)$	n	$\Sigma \chi^2$
107.2 fx	9.82	-0.15	1 fx	436
110.6 fx	11.27	0.015	1 fx	954
114.0	12.9	0.114	1 fx	1827
112.1	12.02	0.098	1 fx	70.2
108.8	12.06	0.108	1.07	68.25

N	$\sum_{i=1}^N \chi_i^2$	ρ	B	C	n	σ_{tot}, mb
47	77.84	0.14fixed	20.0	0. — <i>fix</i>	1.05	96.8 ± 0.1
47	71.65	0.1 <i>fix</i>	20.	0. <i>fix</i>	1.05	97.1 ± 0.1
47	66.3	0.05 <i>fix</i>	20.	0. <i>fix</i>	1.05	97.2 ± 0.1
47	62.8	0. <i>fix</i>	19.4	0. <i>fix</i>	1.05	97.1 ± 0.1
47	63.1	0.14fixed	17.2	2.1 ± 0.5	1.05	97.56 ± 0.2
47	61.9	0.1 <i>fix</i>	17.7	1.87 ± 0.5	1.05	97.7 ± 0.2
47	61.0	0.05 <i>fix</i>	18.2	1.24 ± 0.5	1.05	97.7 ± 0.2
47	60.6	0. <i>fix</i>	18.8	0.8 ± 0.5	1.05	97.4 ± 0.2
47	60.8	-0.05 <i>fix</i>	19.3	0.4 ± 0.5	1.05	96.9 ± 0.3
47	61.1	-0.064 ± 0.05	19.8	0. <i>fix</i>	1.05	96.57 ± 0.58
47	60.6	-0.011 ± 0.09	18.9	0.7 ± 0.9	1.05	97.3 ± 0.9

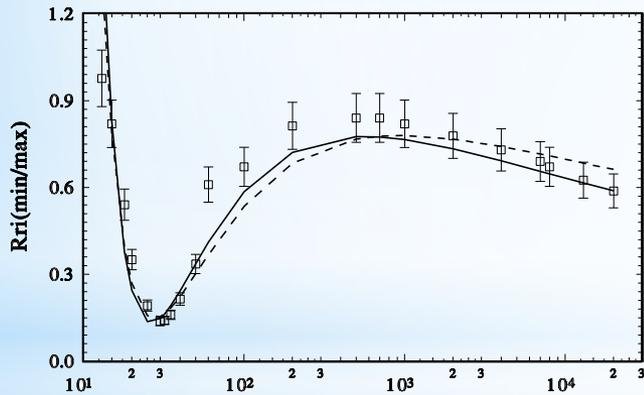
Table 10: The basic parameters of the model are determined by fitting experimental data.

“Now our calculations show the inconsistency of the size of $\rho=0.14$ with the parameters of the scattering amplitude obtained by the TOTEM Collaboration.”

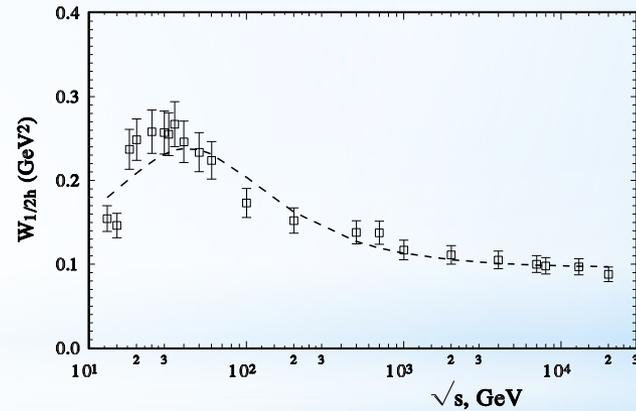


$$t_{\min} = a_1 / [(1 + a_2 \ln(s / s_0))^2];$$

$$a_1 = 1.85 \pm 0.08; a_2 = 0.009 \pm 0.001; s_0 = 4m_p.$$



$$R_{\frac{\max}{\min}} = \frac{b_1}{\ln(s / s_0)^2} [b_3 + (b_2 - \frac{1}{\ln(s / s_0)})^2];$$



$$W_{1/2h} = c_1 + c_2 / (c_4 / \sqrt{s} + (\sqrt{s})^\epsilon);$$

tm2

Whh

BSW₁ - C. Bourrely, J. Soffer, T.T. Wu - ()

BSW₂ - C. Bourrely, J. Soffer, T.T. Wu - ()

HEGS₀ – O.V.S. -

HEGS₁ – O.V.S. -

	BSW ₁	BSW ₂	HEGS ₀	HEGS ₁
N _{exp}	369	955	980	3416
N _{par}	7+Regge	11+Regge	3+2	5+4
\sqrt{s} , <u>GeV</u>	24 ÷ 630	13.4 ÷ 1800	52 ÷ 1800	9 ÷ 8000
Δt , <u>GeV²</u>	0.1 ÷ 2.6	0.1 ÷ 5	$8.7 \cdot 10^{-4} \div 10$	$3.7 \cdot 10^{-4} \div 15$
(Σx^2)/N	4.45	1.95	1.8	1.28

$F_{Odd}^B(s,t)$ with h^c_{odd} and h^t_{odd}

$F_{Odd}^B(s,t)$ with h^t_{odd}

