

# $\gamma$ -jet fragmentation function & jet-induced medium excitation



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“Opportunities and challenges with jets at LHC and beyond”

Central China Normal University, Wuhan

10-12 June 2018

# Outlines

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## Introduction

2

## Model description

- ❑ Linear Boltzmann transport model(LBT)
- ❑ 3+1D hydrodynamic model(CLVisc)
- ❑ CoLBT-hydro model for jet transport and jet-induced medium excitation.

3

## Results

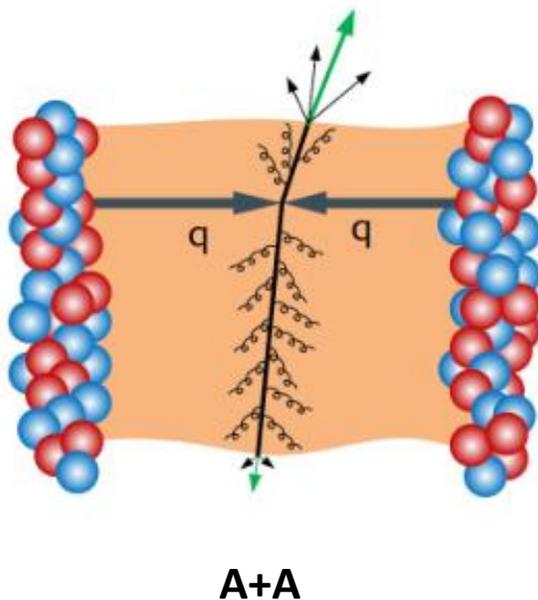
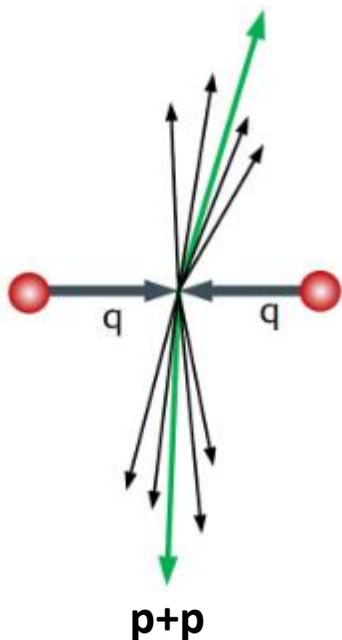
- ❑ Medium modification of  $\gamma$ -triggered fragmentation function at RHIC
- ❑  $\gamma$ -hadron azimuthal correlation at RHIC
- ❑ Medium modification of  $\gamma$ -triggered fragmentation function at LHC

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## Summary and outlook



## Jet tomography for the study of QGP



QGP medium effect:

- ✓ Interaction with medium constituents
- ✓ Induced gluon radiation

Leading partons energy loss

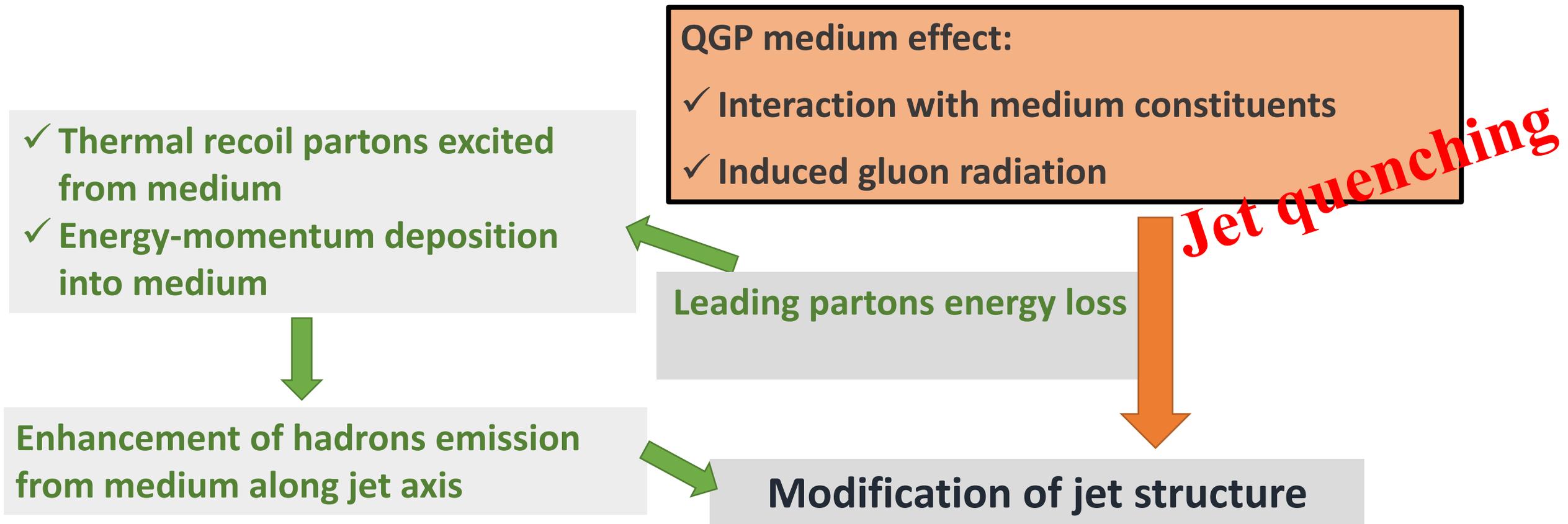
**Jet quenching**

Modification of jet structure

**Where does the lost energy go?**

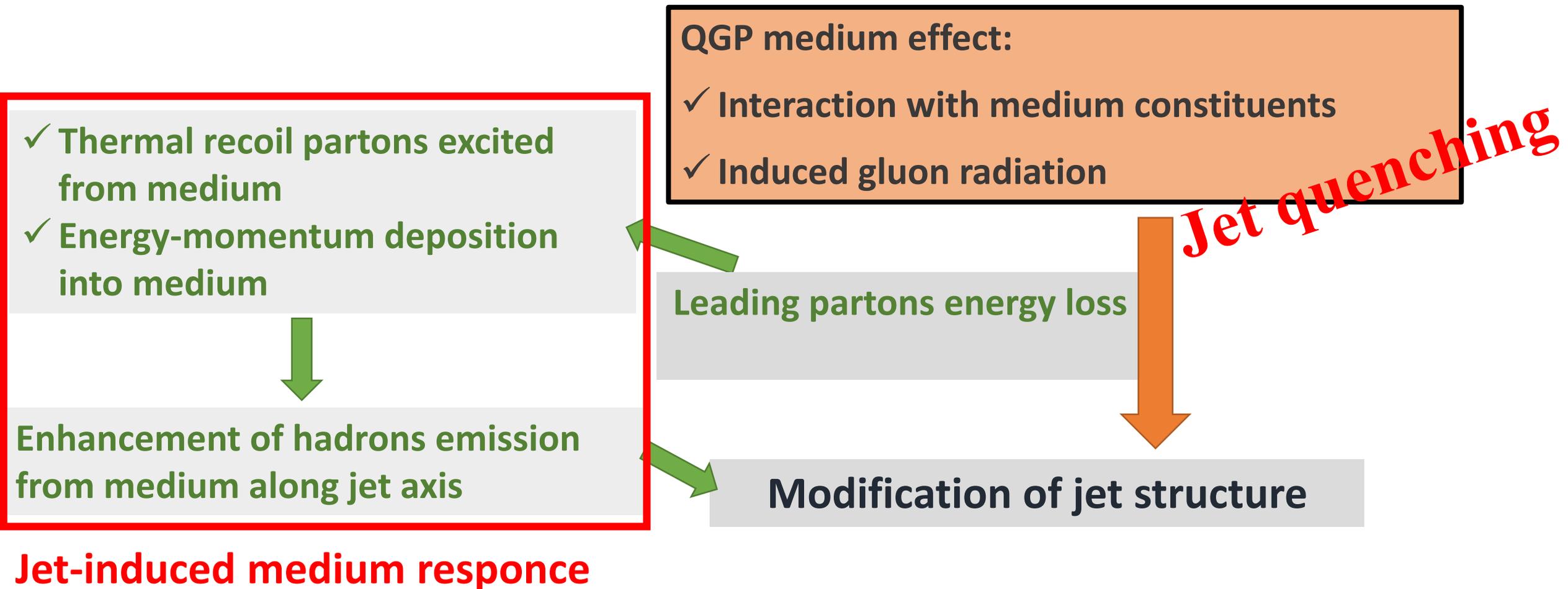


## Jet tomography for the study of QGP



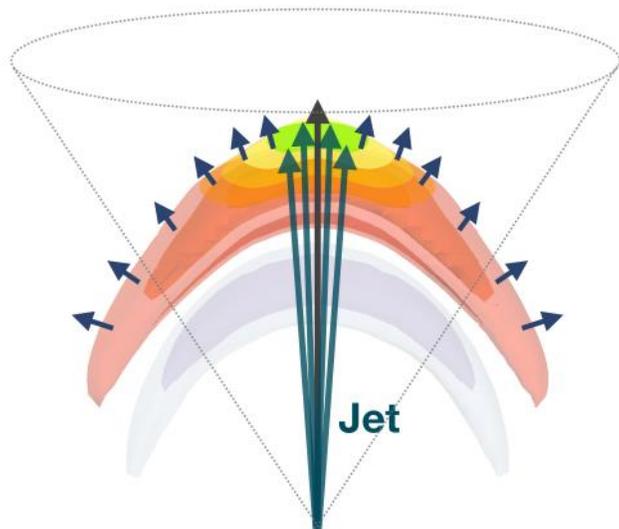


## Jet tomography for the study of QGP



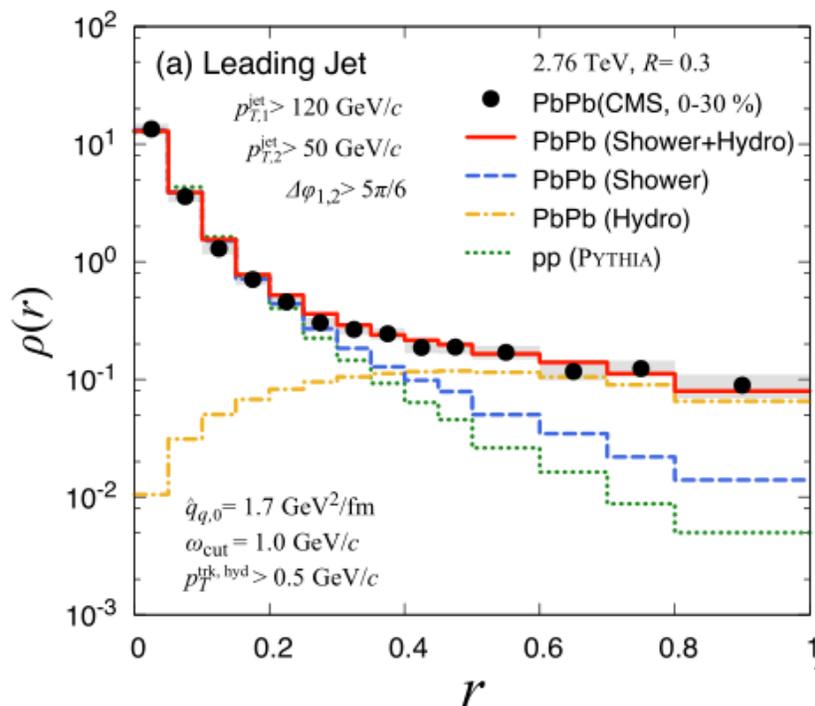


# Motivation



The modified jet can be determined by:

- ✓ Energy loss of the leading jet shower partons.
- ✓ The redistribution of the lost energy and momentum in the medium.



Medium response contributes to many jet-observables:

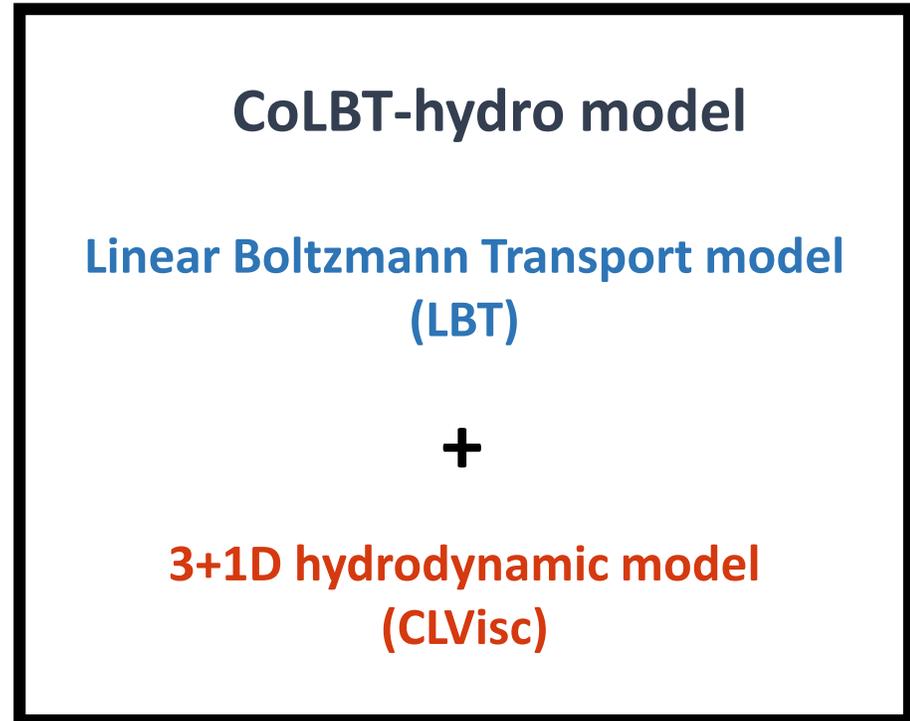
- ✓ Energy redistribution in reconstructed full jet(jet shape)
- ✓ Gamma-hadron and jet-hadron fragmentation function & gamma-hadron azimuthal distribution.

and so on.



Frameworks for the study of whole jet quenching pictures(including medium response):

- ✓ Full Boltzmann transport approach  
in the same Monte-Carlo transport(cross section)
- ✓ jet plus hydrodynamics approach
  - No recoil partons contribution
  - Neglect the effect of medium response on the subsequent evolution of hard jets
  - No concurrent





# Linear Boltzmann Jet Transport Model

## Linear Boltzmann Jet Transport Model(LBT)

Monte Carlo jet transport model based on pQCD calculation:

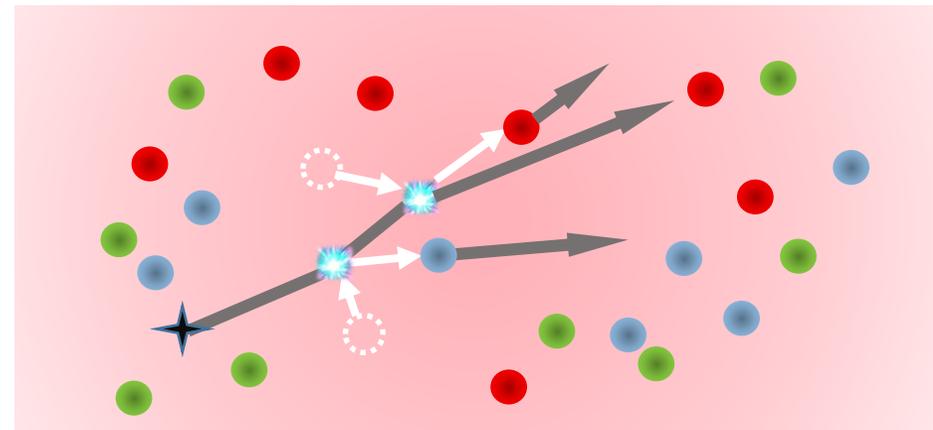
- Jet transport is simulated according to linear Boltzmann equation

$$p_a \cdot \partial f_a = \frac{\gamma_b}{2} \int \prod_{i=b,c,d} d[p_i] (f_c f_d - f_a f_b) |M_{ab \rightarrow cd}|^2 S_2(\hat{s}, \hat{t}, \hat{u}) (2\pi)^4 \delta^4(p_a + p_b - p_c - p_d),$$

- Consider both elastic and inelastic processes

$$\frac{dN_g^a}{dz dk_{\perp}^2 dt} = \frac{2\alpha_s C_A P_a(z)}{\pi} \frac{k_{\perp}^4}{(k_{\perp}^2 + z^2 m^2)^4} \cdot \frac{p \cdot u}{p_0} \hat{q}_a(x) \sin^2\left(\frac{t - t_i}{\tau_f}\right),$$

- Keep track of **jet shower parton** and **thermal recoil parton**
- Take into account of back reaction and denote initial thermal partons in each scattering as **“negative” partons**





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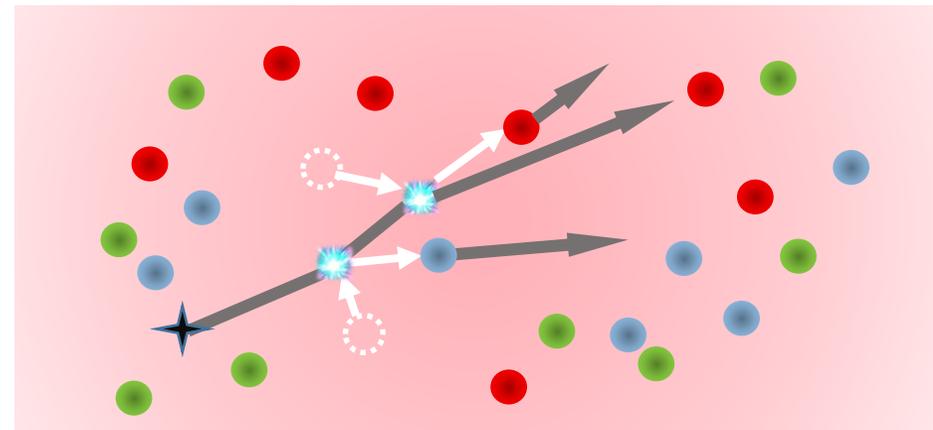
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**recoil parton**

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**“negative” partons**

### Jet-induced medium partons





## 3+1D hydrodynamic model(**CLVisc model**)

### ➤ Hydrodynamic evolution of bulk medium

to solve  $T^{\mu\nu}=0$  with a parameterized equation of state(Eos) s95p-pce by KT algorithm + the second Runge-Kutta method.

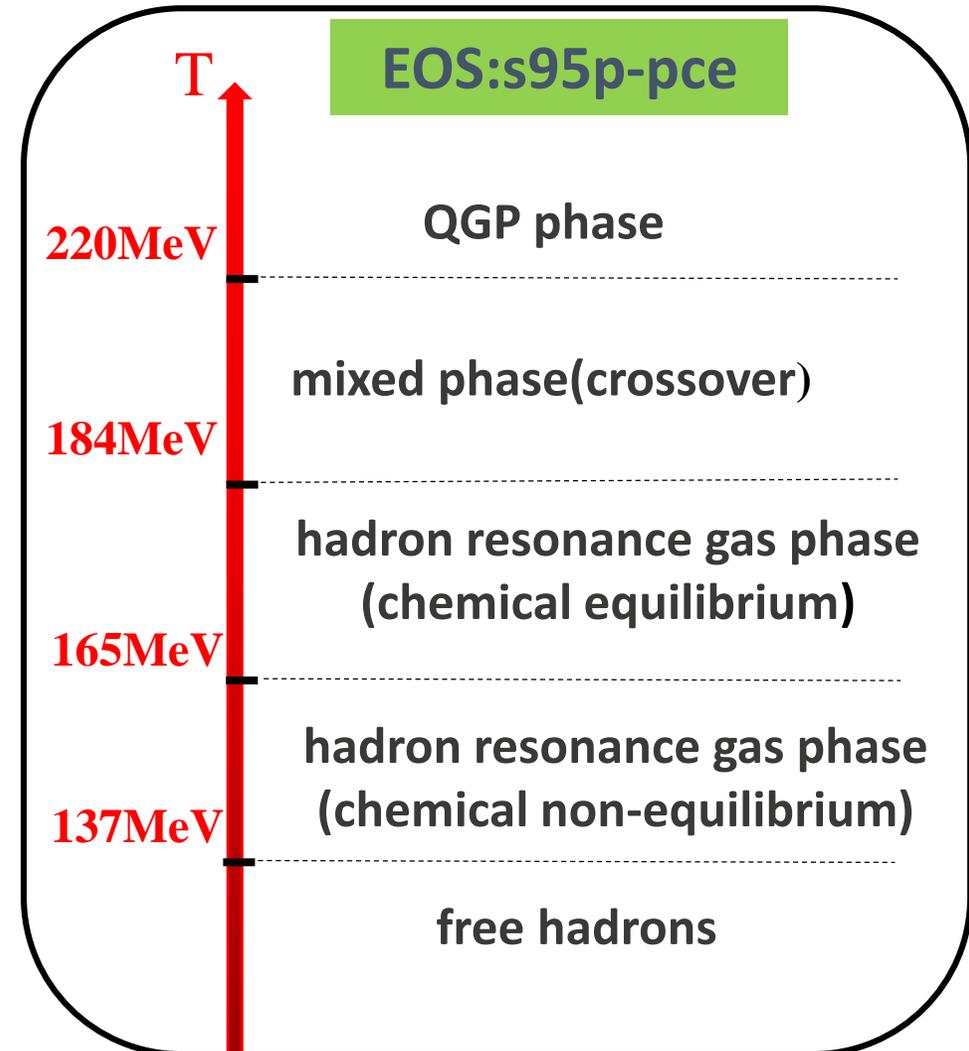
### ➤ Calculate hadron spectrum from freeze-out hypersurface.

Cooper-Frye formular:

$$\frac{dN_i}{dY p_T dp_T d\phi} = g_i \int_{\Sigma} p^\mu d\Sigma_\mu f(p \cdot u)$$

$$f(p \cdot u) = \frac{1}{(2\pi)^3} \frac{1}{\exp((p \cdot u - \mu_i)/T_f) \pm 1}$$

### ➤ Hadron resonance decay

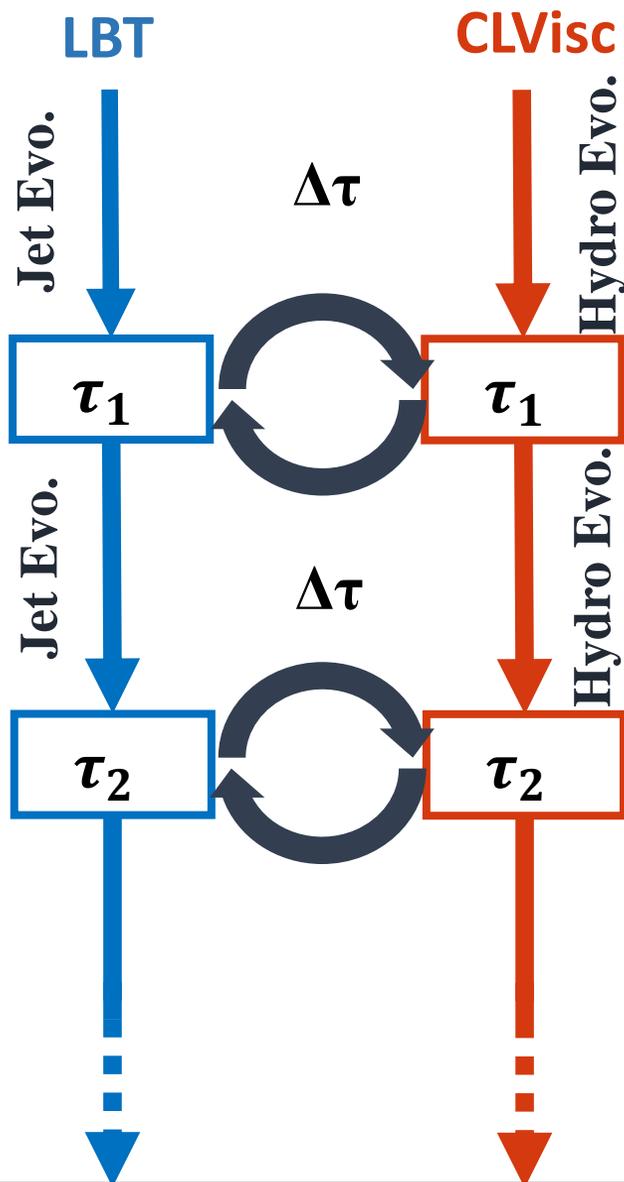




## CoLBT-hydro model

Linear Boltzmann Transport model (LBT) + 3+1D hydrodynamic model (CLVisc)

- ✓ formulated in Milne coordinates  $(\tau, x_{\perp}, \eta_s)$
- ✓ simulated in sync with each other



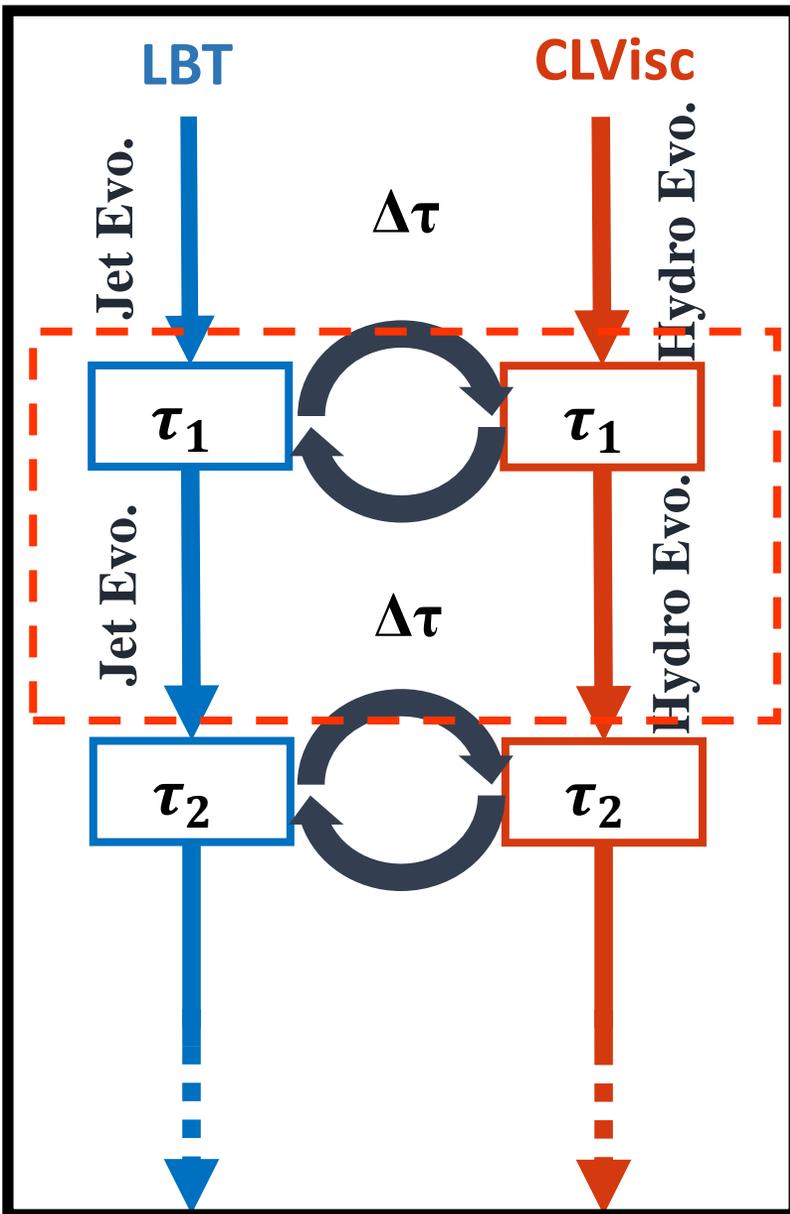
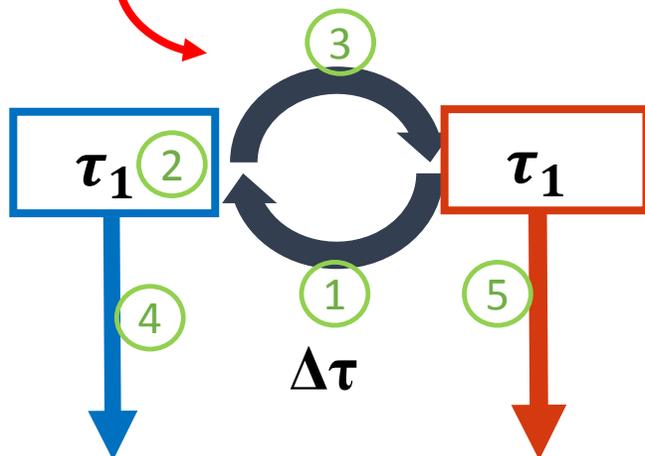


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- ✓ simulated in sync with each other

- ① provide medium info  $(T, u)$  to jet partons
- ② carry out jet shower partons' transport according to medium info.
- ③ soft  $(p \cdot u < p_{cut}^0)$  and 'negative'  $(p \cdot u < 0)$  partons deposited into medium as source term
- ④ hard  $(p \cdot u \geq p_{cut}^0)$  partons propagate in LBT frame
- ⑤ update the medium info through solving  $\partial_{\mu} T^{\mu\nu} = j^{\nu}$





# Hydrodynamic equations with source term

**Assumption: Instantaneous local thermalization of deposited energy and momentum**

**Hydrodynamic equation with source term**

$$\partial_\mu T_{QGP}^{\mu\nu}(x) = j_{jet}^\nu(x)$$

**Energy-momentum  
tensor of QGP fluid**

**Energy and momentum  
deposited from jet**

**source term:**

$$j_{jet}^\nu(x) = \sum_i \frac{\theta(p_{cut}^0 - p_i \cdot u) p_i^\nu}{\Delta\tau} \delta^3(\vec{x} - \vec{x}_i)$$



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soft partons  
(  $p \cdot u < p_{cut}^0$  )

negative partons  
(  $p \cdot u < 0$  )



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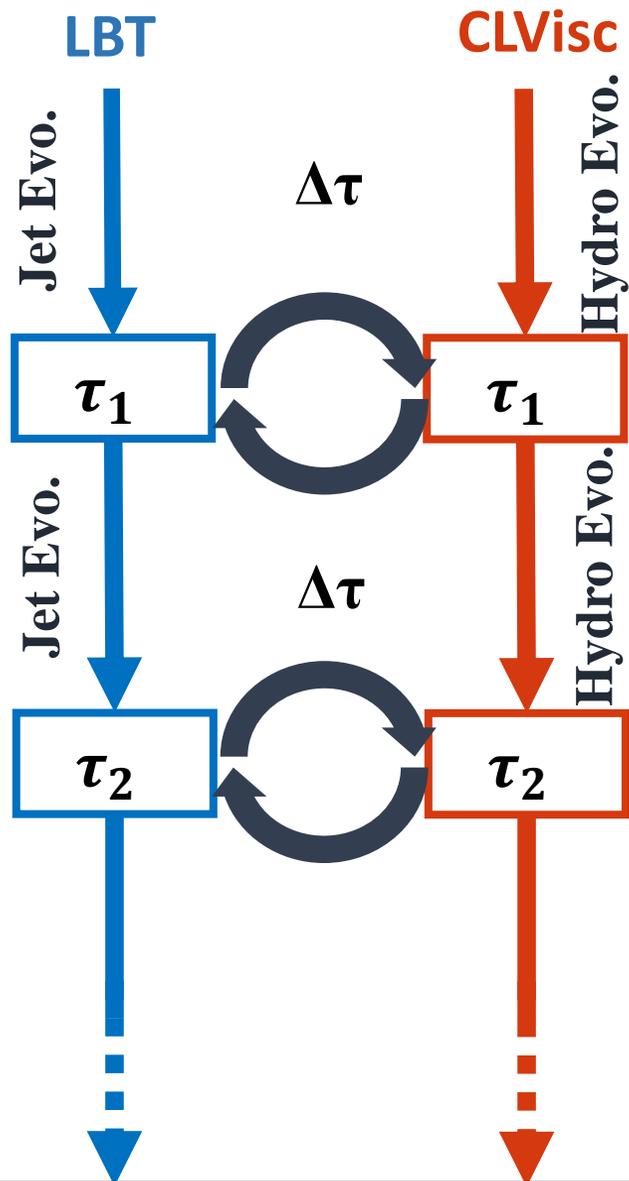
negative partons  
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Gaussian approximation:

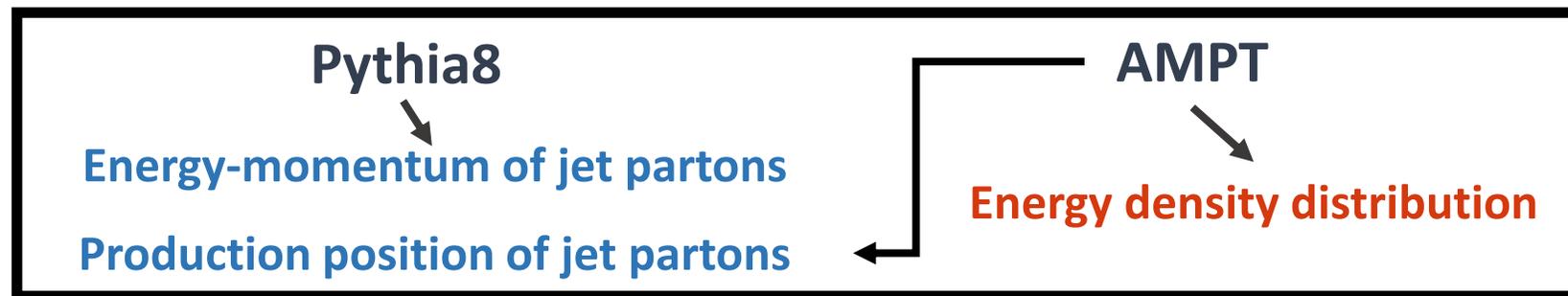
$$\frac{\delta^3(\vec{x} - \vec{x}_i)}{\Delta\tau} \rightarrow \frac{1}{\tau\Delta\tau(2\pi)^{3/2}\sigma_\tau^2\sigma_{\eta_s}} \exp\left[-\frac{(\vec{x}_\perp - \vec{x}_{\perp i})^2}{2\sigma_\tau^2} - \frac{(\eta_s - \eta_{si})^2}{2\sigma_{\eta_s}^2}\right]$$



# Initial condition



Initial condition



## AMPT:

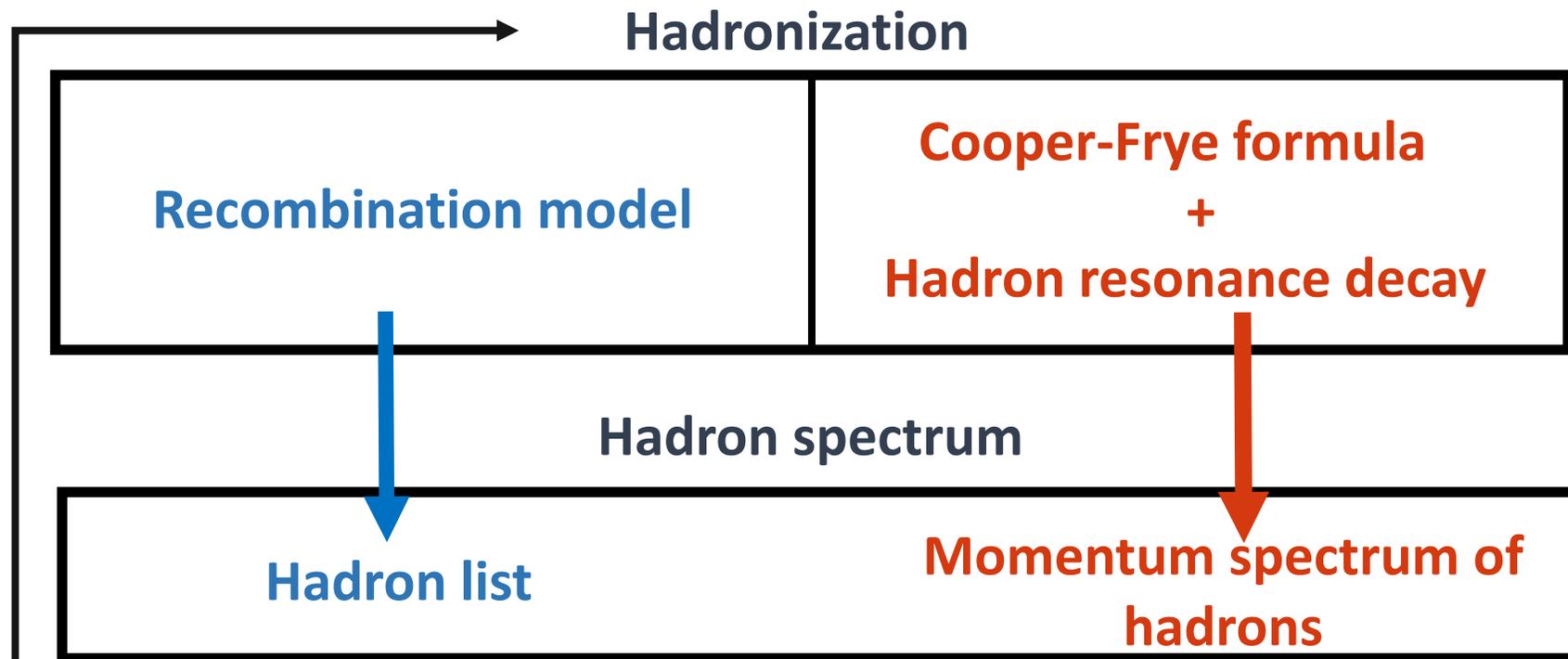
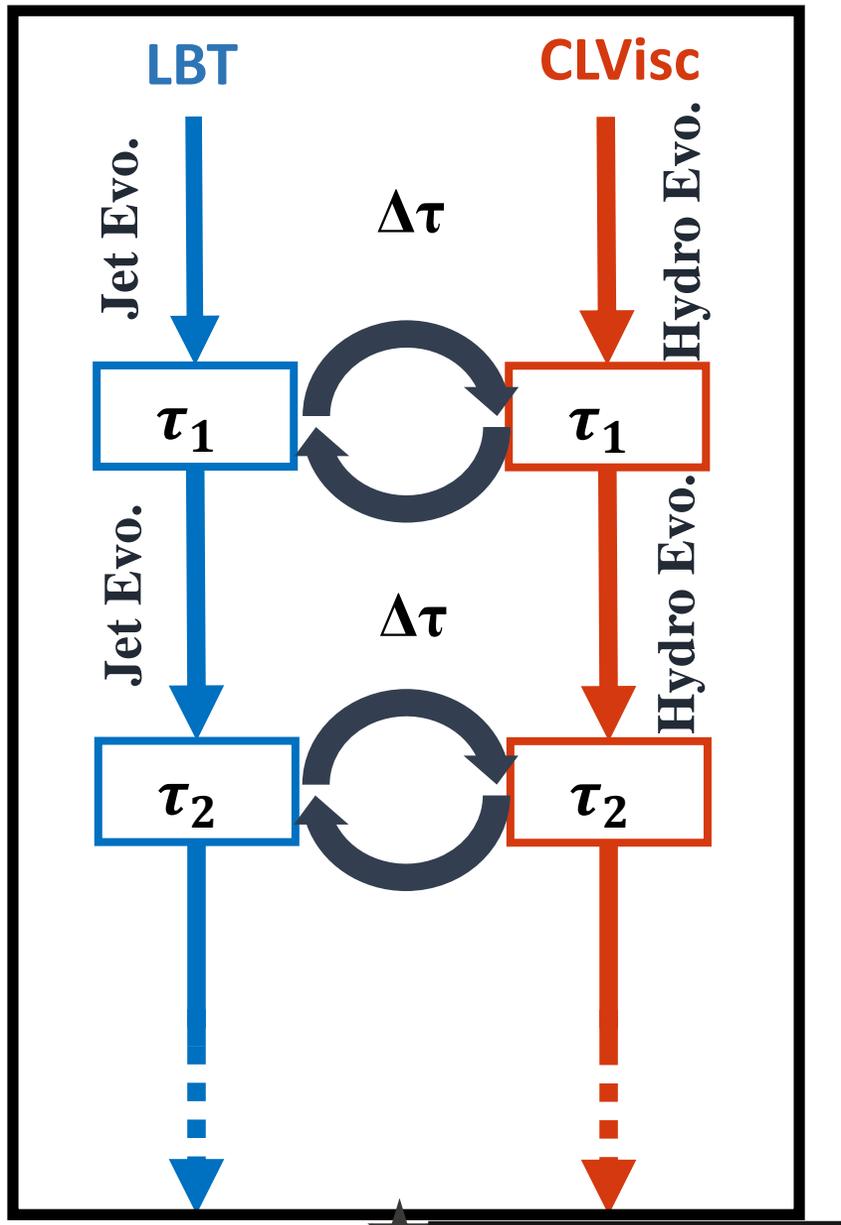
- ✓ Energy density distribution includes transverse and longitudinal fluctuation.
- ✓ Production positions of jet partons: sampled from spatial distribution of binary hard processes.

## Pythia8:

- ✓ Energy-momentum of jet partons different in each event.



# Hadronization



✓ Recombination model from Texas A-M group



## We need to increase calculation efficiency of the CoLBT-hydro model:

- ✓ the final observables needs abundant event statistics
- ✓ one event calculation in single core of CPU takes long time (6-7 hours/event)

	single core(CPU)
Hydrodynamics evolution of medium	30-40 min
Hadron spectrum calculation in FO hypersurface	Almost 2 h
Hadron resonance decay	3-4 h



# GPU parallel computation

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- ✓ the final observables needs abundant event statistics
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GPU parallel computation + GPU cluster

CoLBT-hydro for event-by-event simulations

	single core(CPU)	GPU
Hydrodynamics evolution of medium	30-40 min	20-30 sec
Hadron spectrum calculation in FO hypersurface	Almost 2 h	1-2 min
Hadron resonance decay	3-4 h	2-3 min

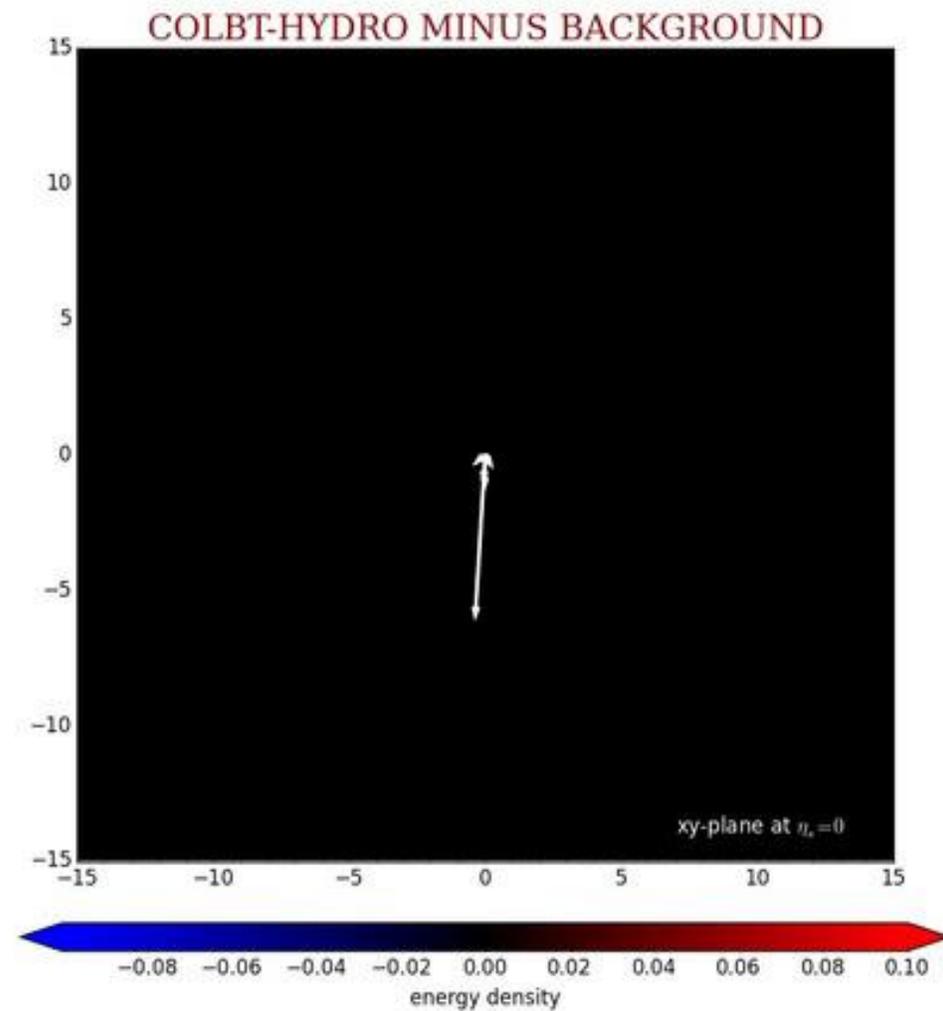
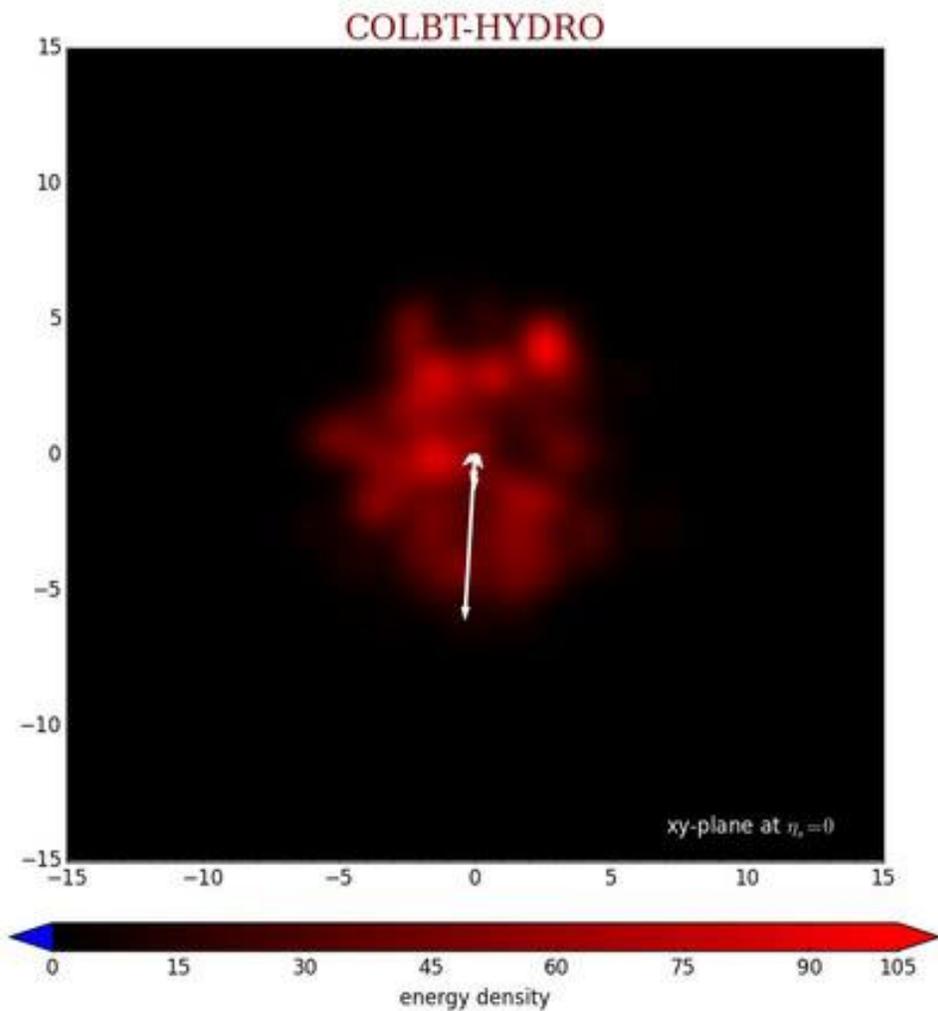


More than 100 times faster



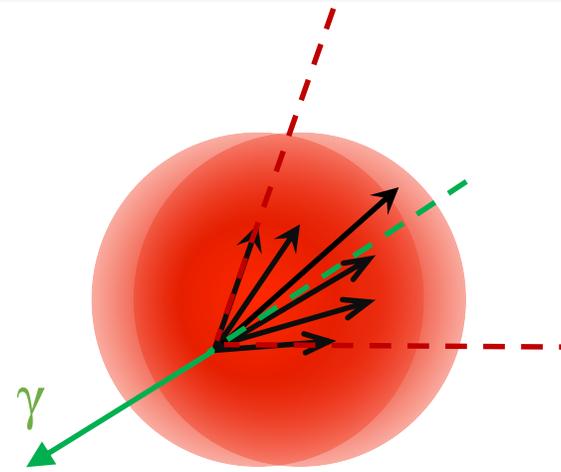
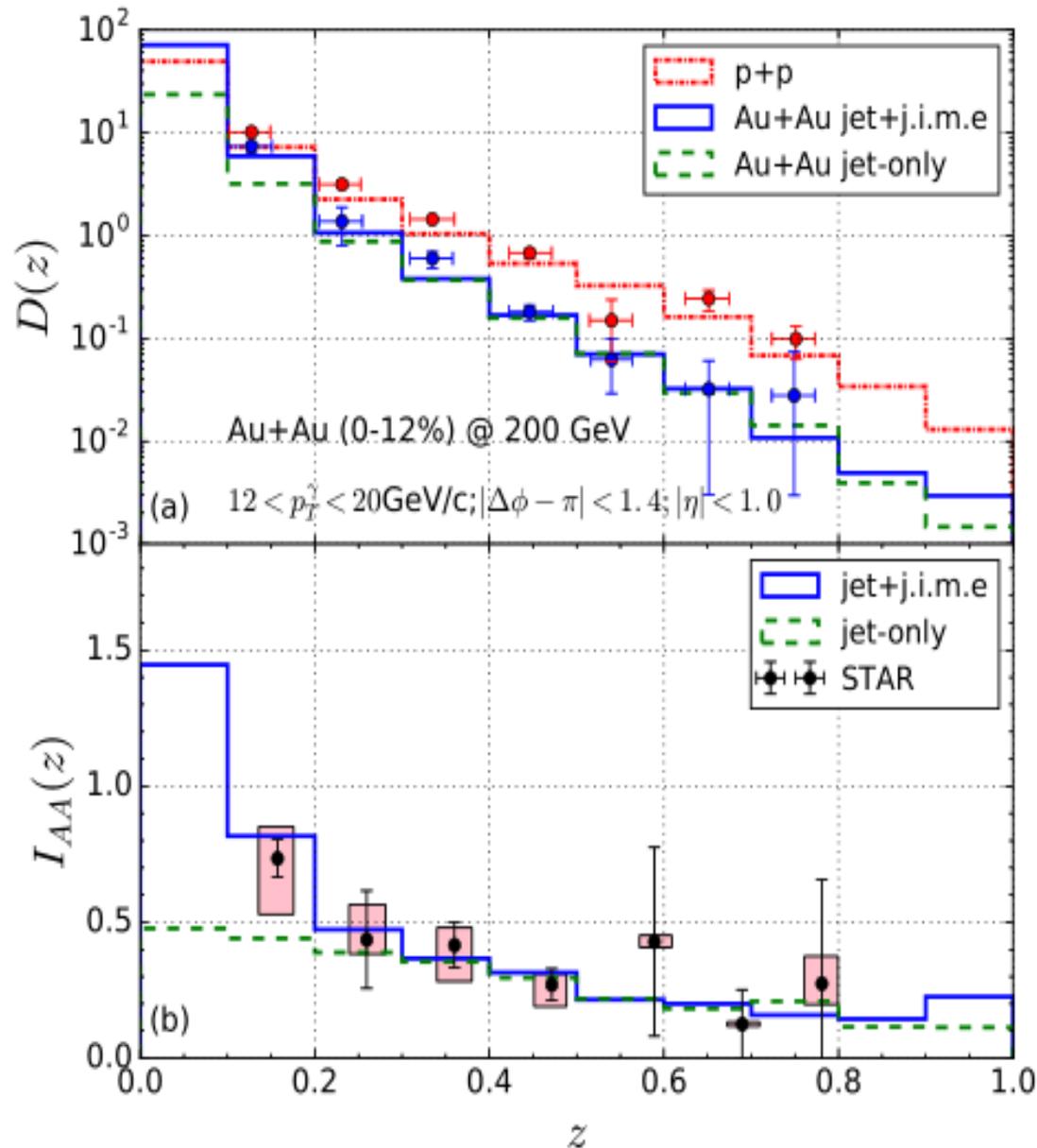
# Jet transport and jet-induced medium excitation

Jet propagation in hot medium at  $\tau = 0.4 \text{ fm}$





# Medium modification of $\gamma$ -triggered fragmentation function



$$z = \frac{p_T^h}{p_T^\gamma}$$

$$D(z) = \frac{1}{N_{event}} \frac{dN}{dz}$$

$$I_{AA}(z) = \frac{D_{AA}(z)}{D_{pp}(z)}$$

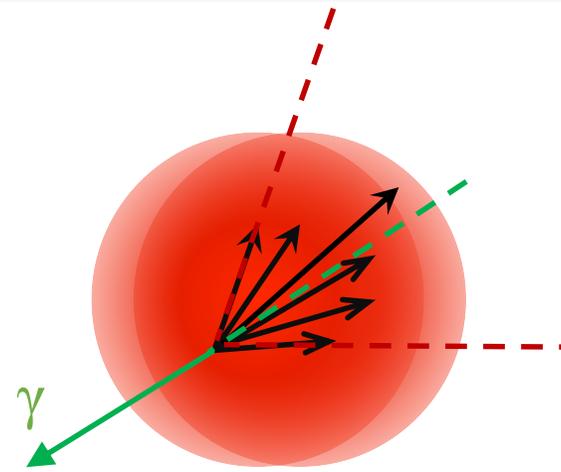
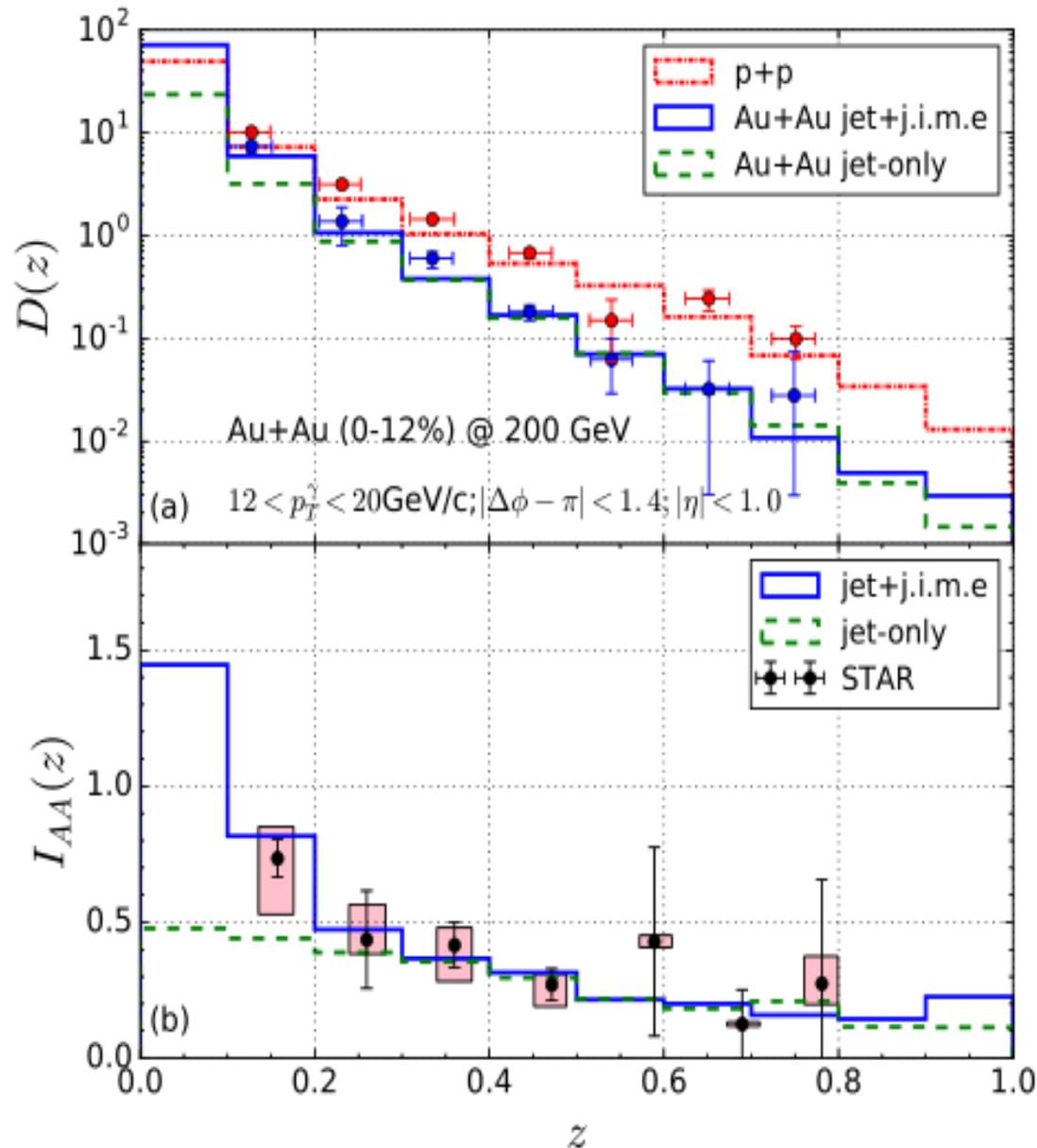
In our calculation:

- ✓ p+p results :  
     jet partons from Pythia8 + recombination model
- ✓ Au+Au results :

$$D(z) = \left. \frac{dN_h}{dydz} \right|_{LBT} + \left. \frac{dN_h}{dydz} \right|_{hydro}^{w/jet} - \left. \frac{dN_h}{dydz} \right|_{hydro}^{no/jet}$$



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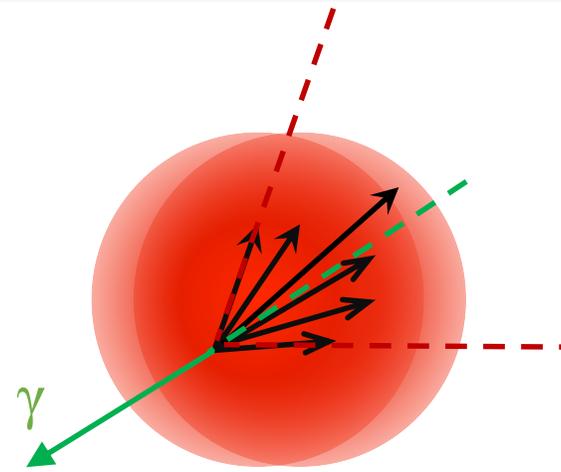
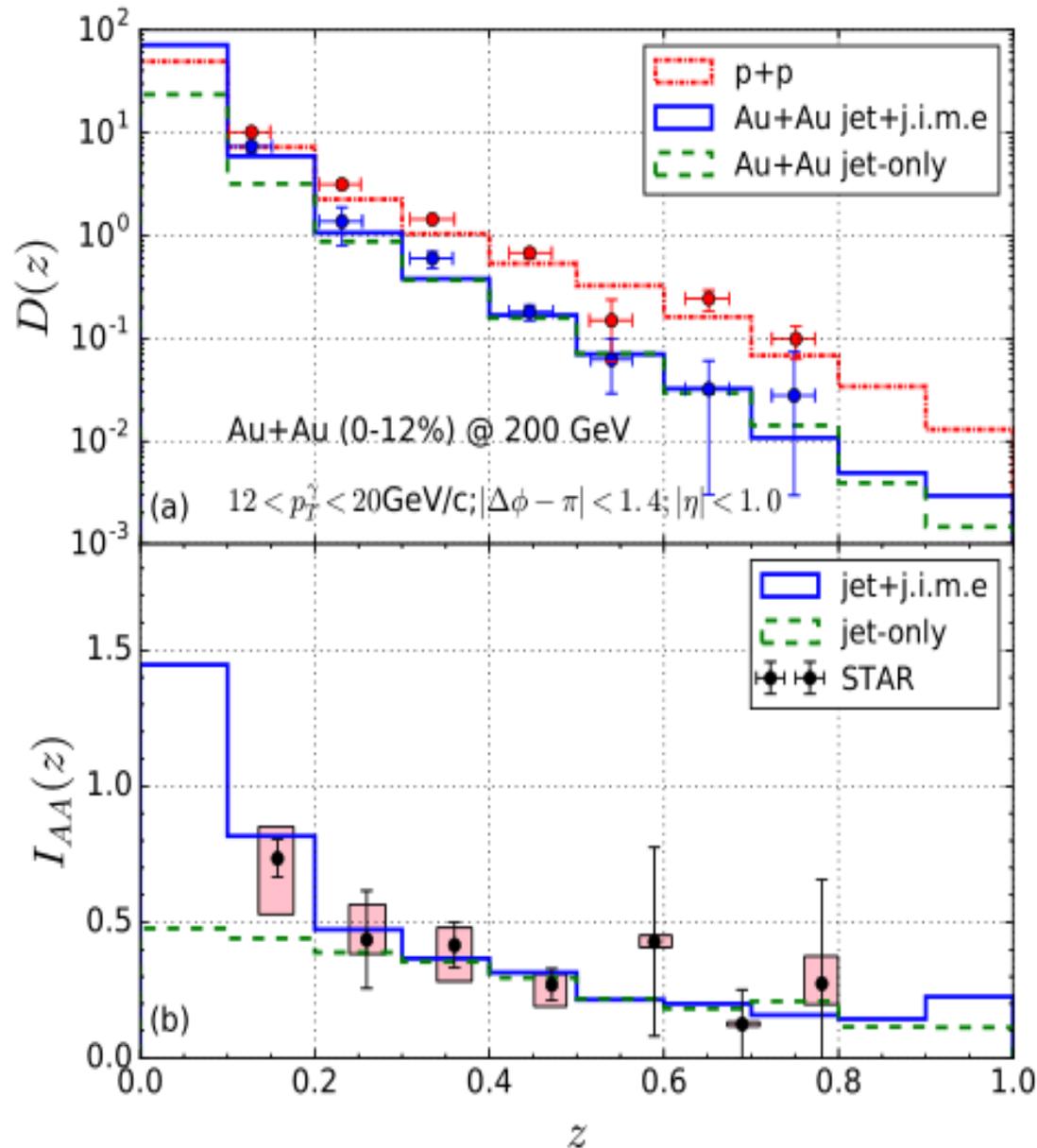
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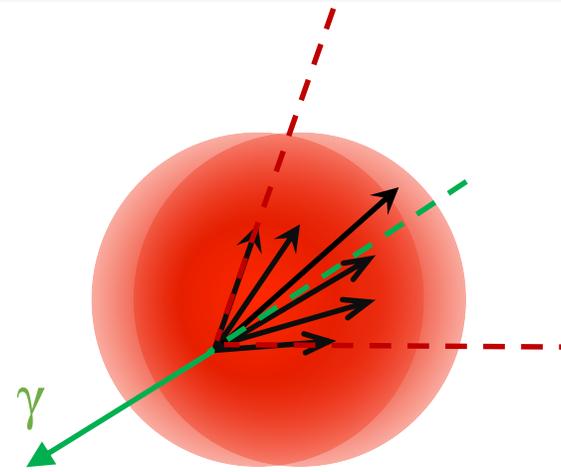
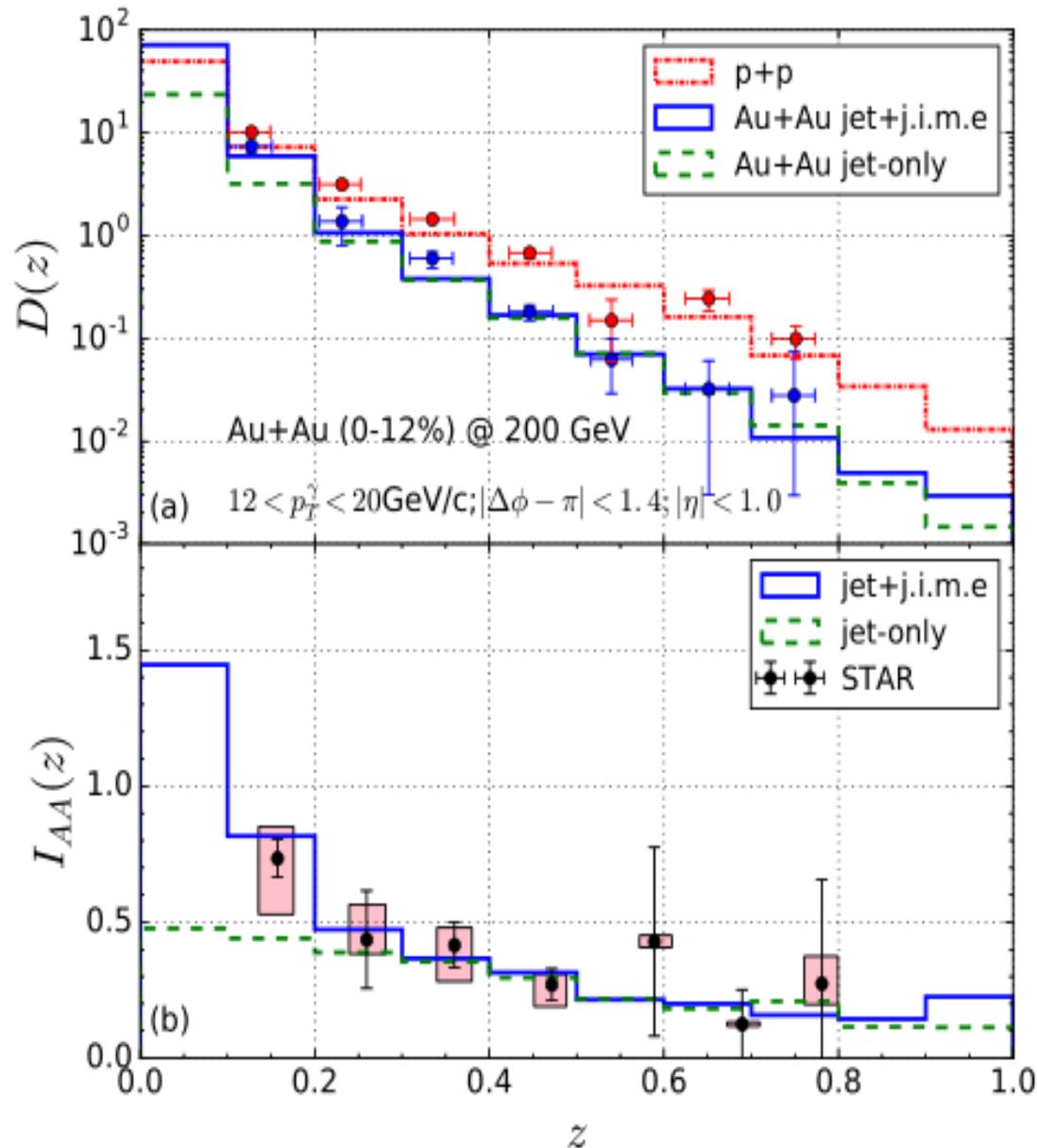
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Medium response by energy-momentum deposition



# Medium modification of $\gamma$ -triggered fragmentation function



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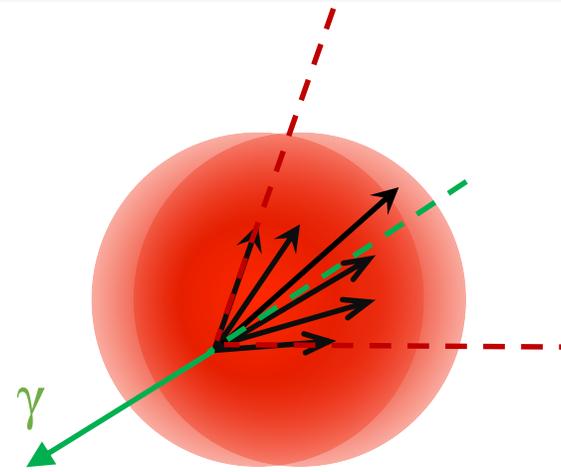
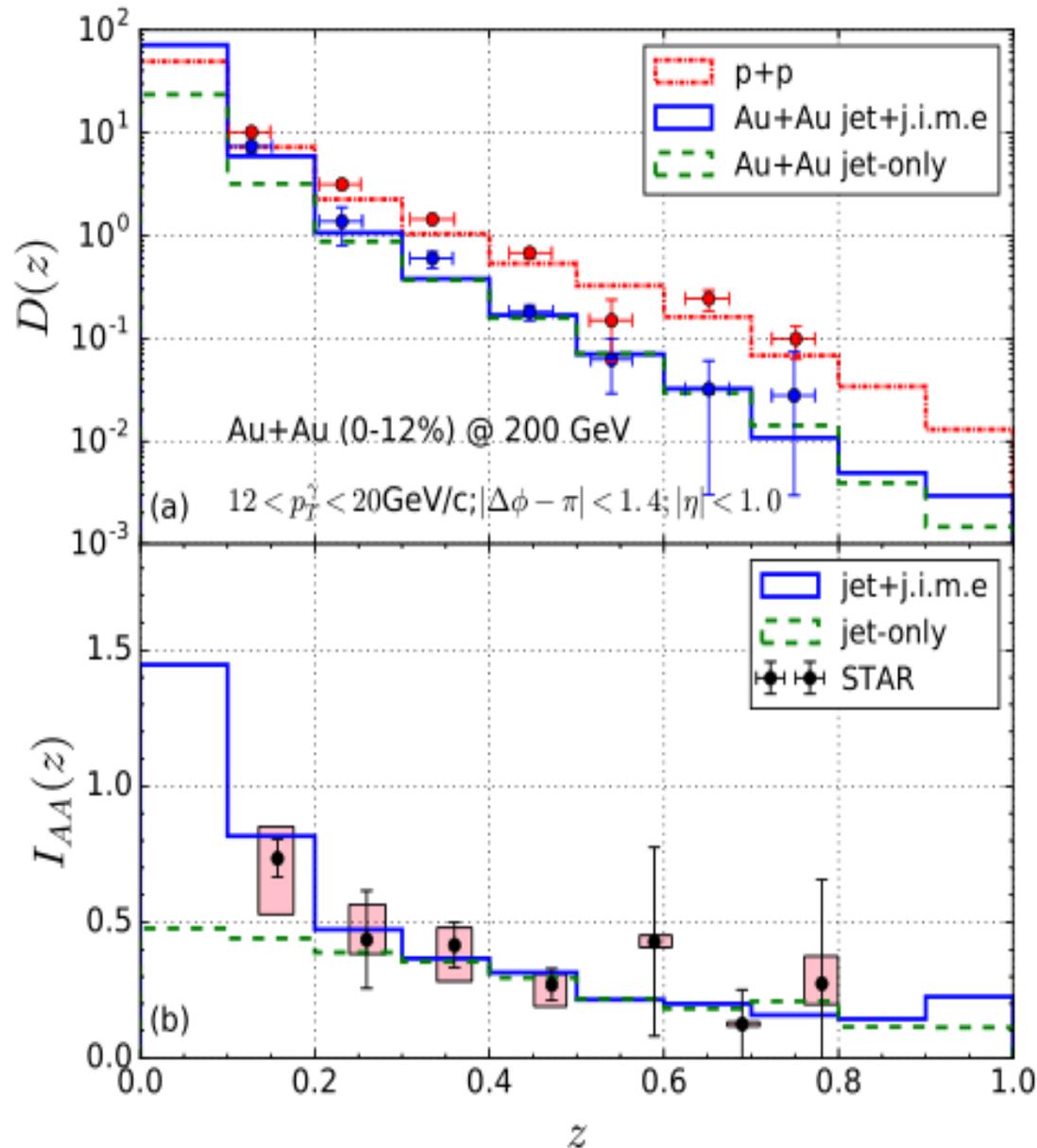
Remnant recoil parton contribution

Medium response by energy-momentum deposition

background



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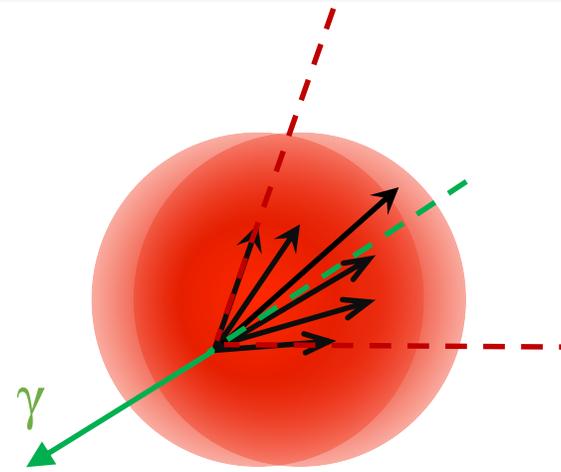
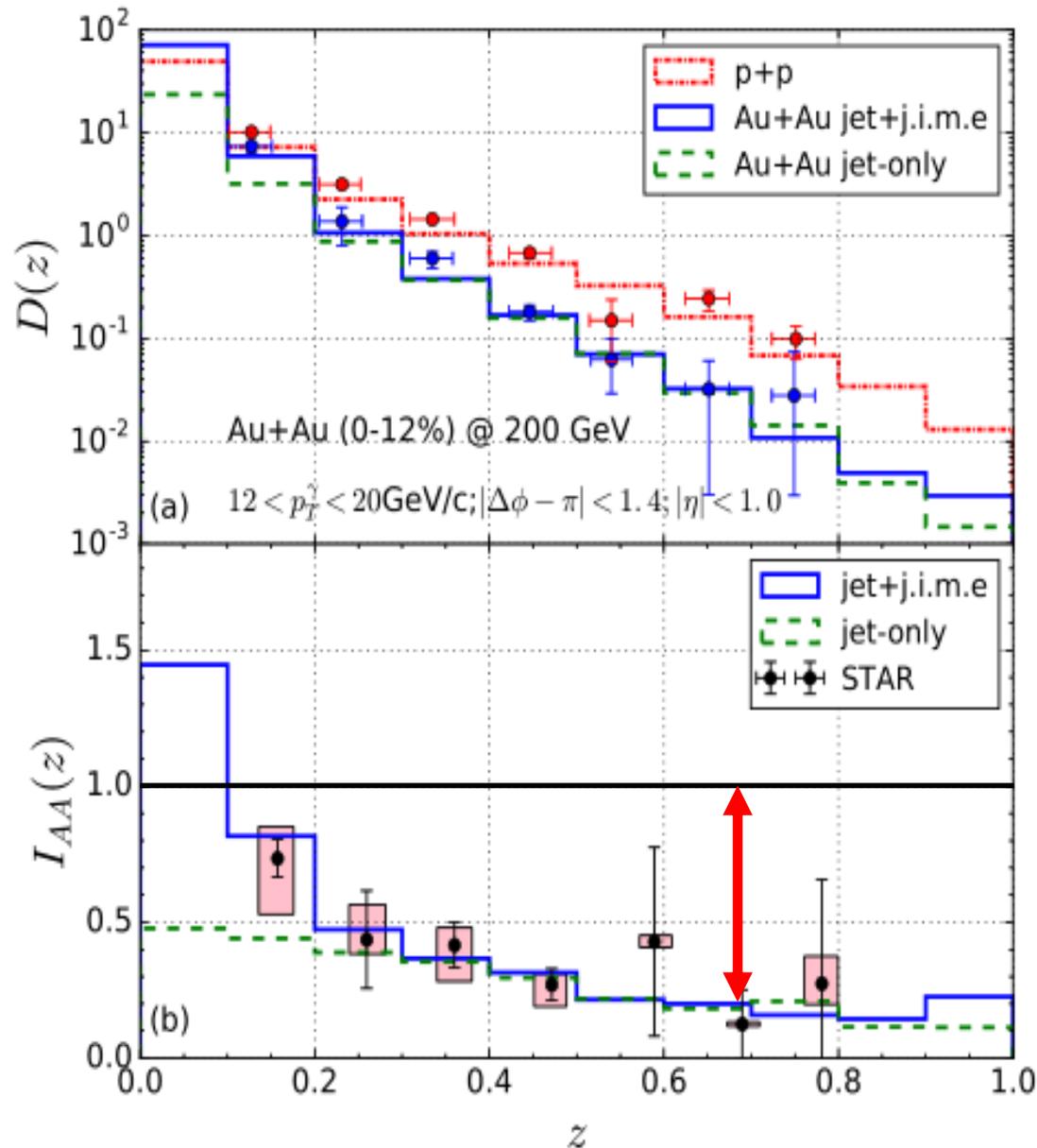
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Remnant recoil parton contribution      Medium response by energy-momentum deposition

jet-induced medium excitation(j.i.m.e)



# Medium modification of $\gamma$ -triggered fragmentation function



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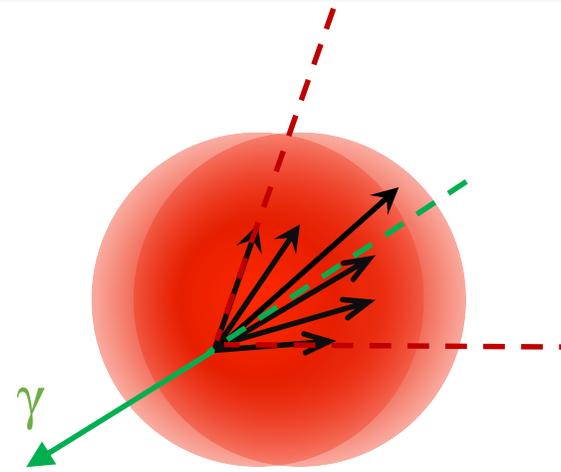
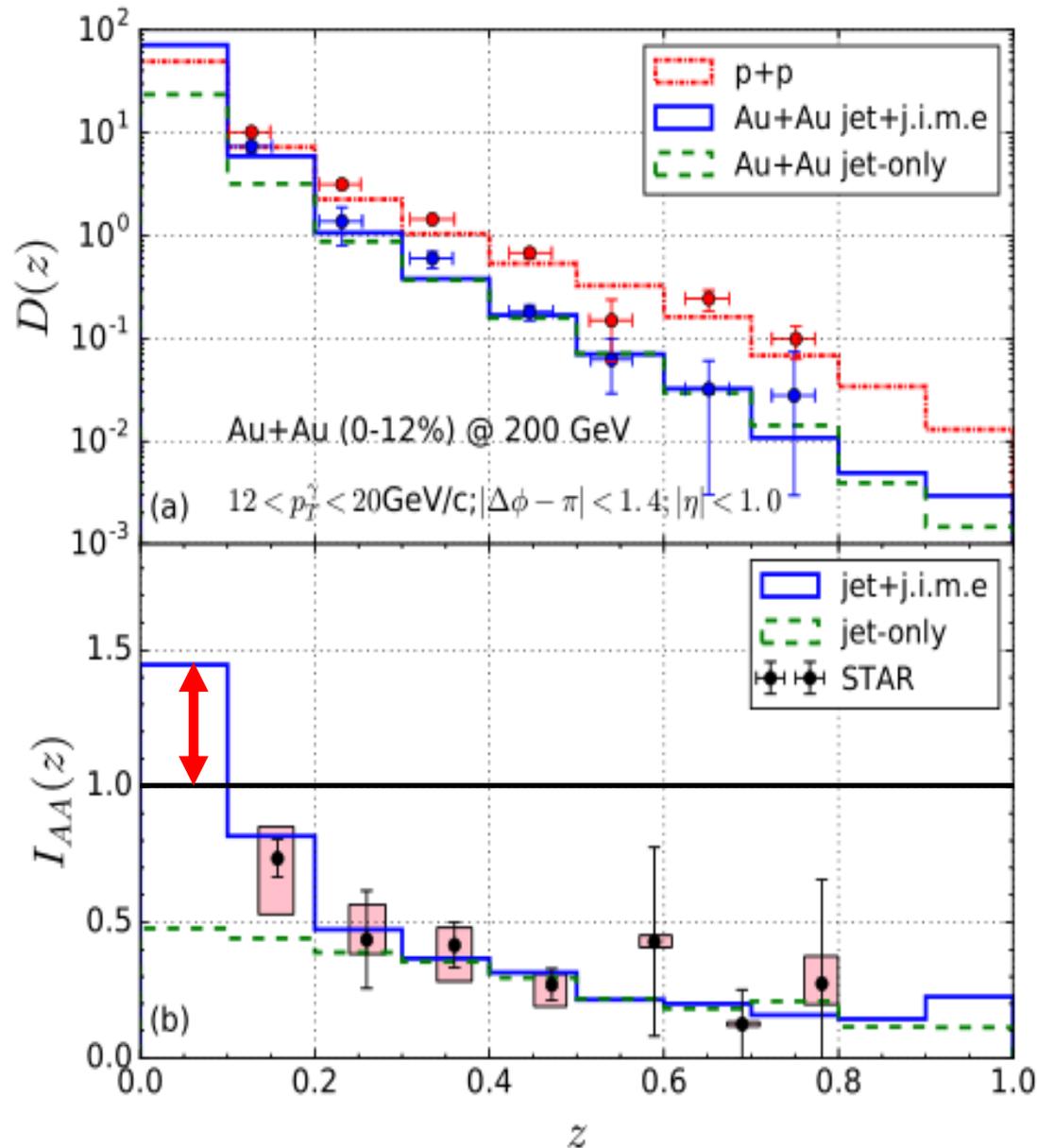
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$$I_{AA}(z) = \frac{D_{AA}(z)}{D_{pp}(z)}$$

- ✓ The suppression of leading hadron yield at the intermediate and high  $z$
- ← energy loss of jet partons due to interaction with hot medium



# Medium modification of $\gamma$ -triggered fragmentation function



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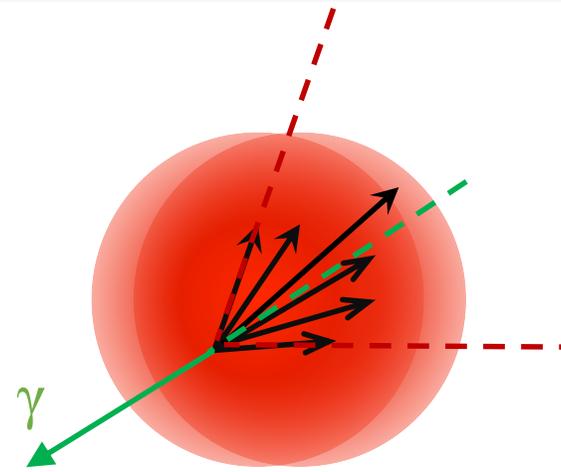
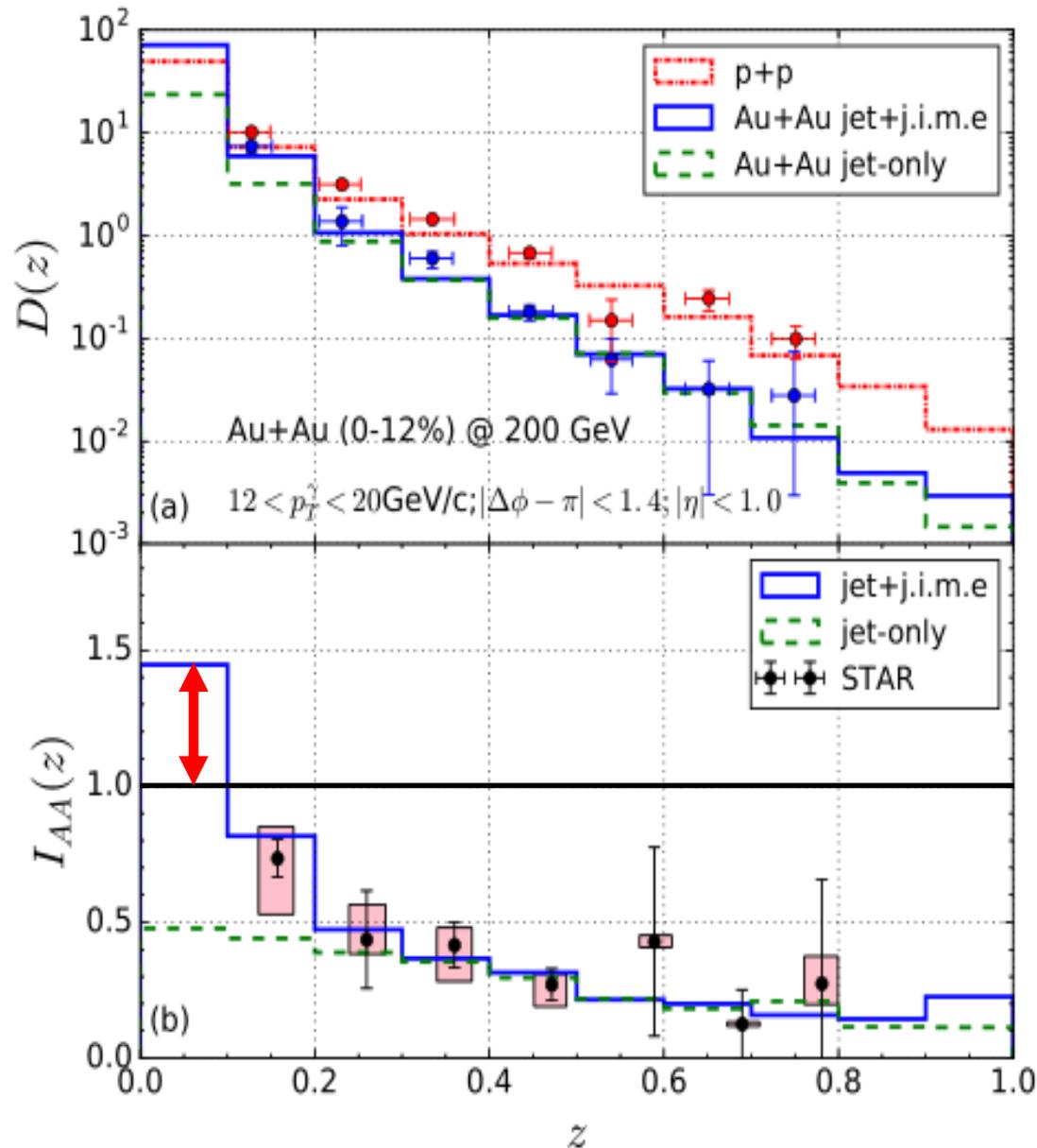
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  - ← energy loss of jet partons due to interaction with hot medium.
- ✓ The enhancement of soft hadrons yield at small  $z$ 
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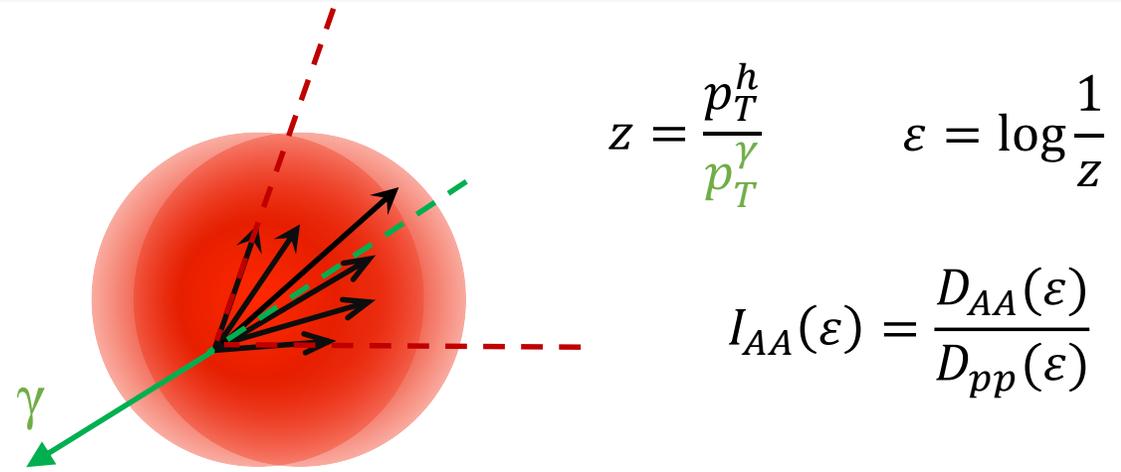
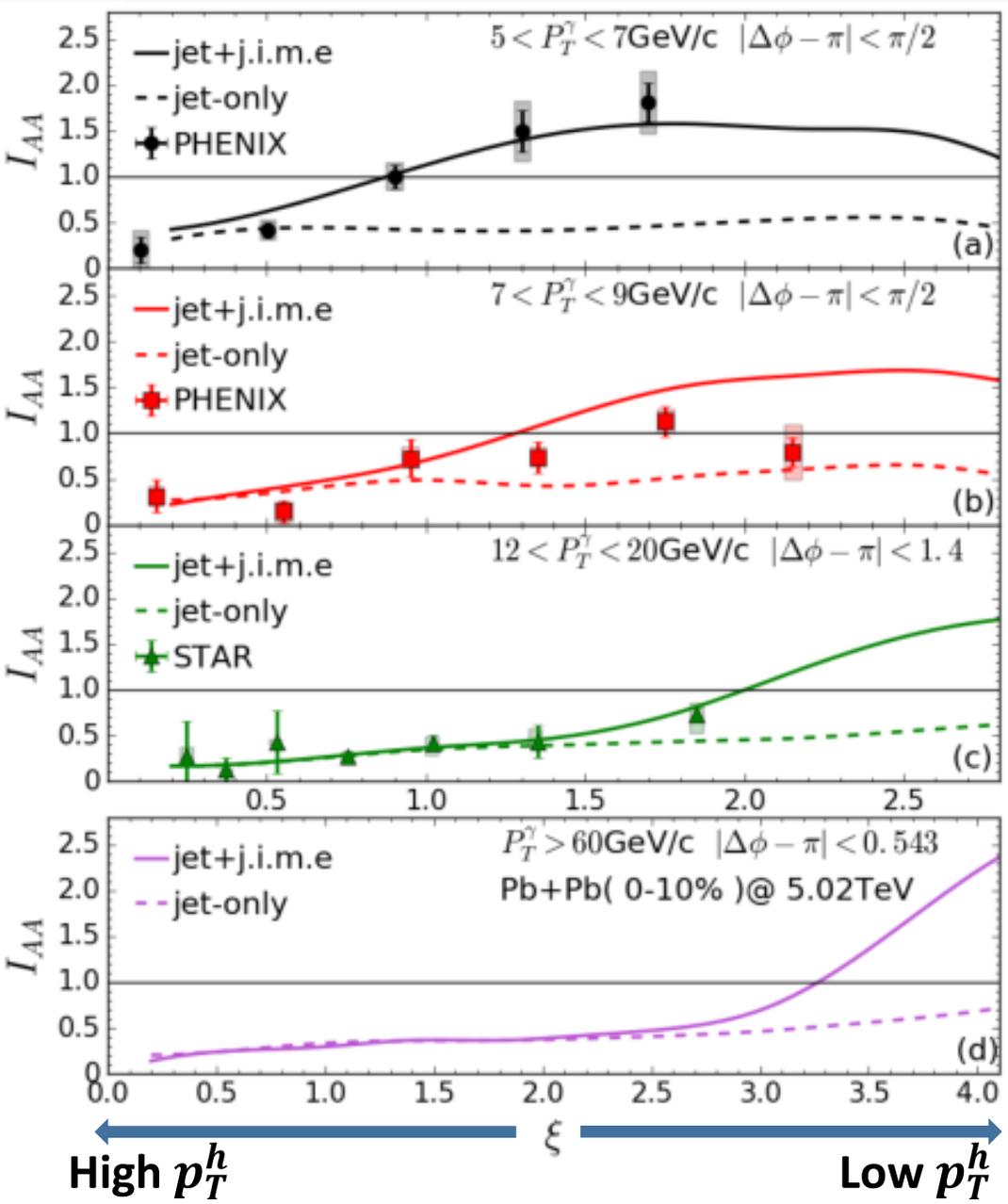
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  - ← jet-induced medium excitation.

$$\alpha_s = 0.3 \quad \text{and} \quad p_{cut}^0 = 2 \text{ GeV}/c$$



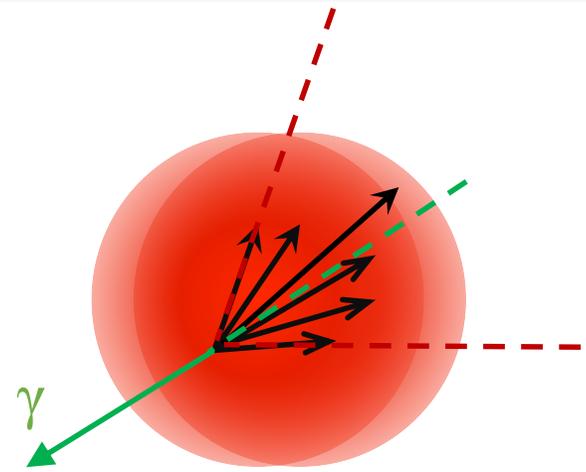
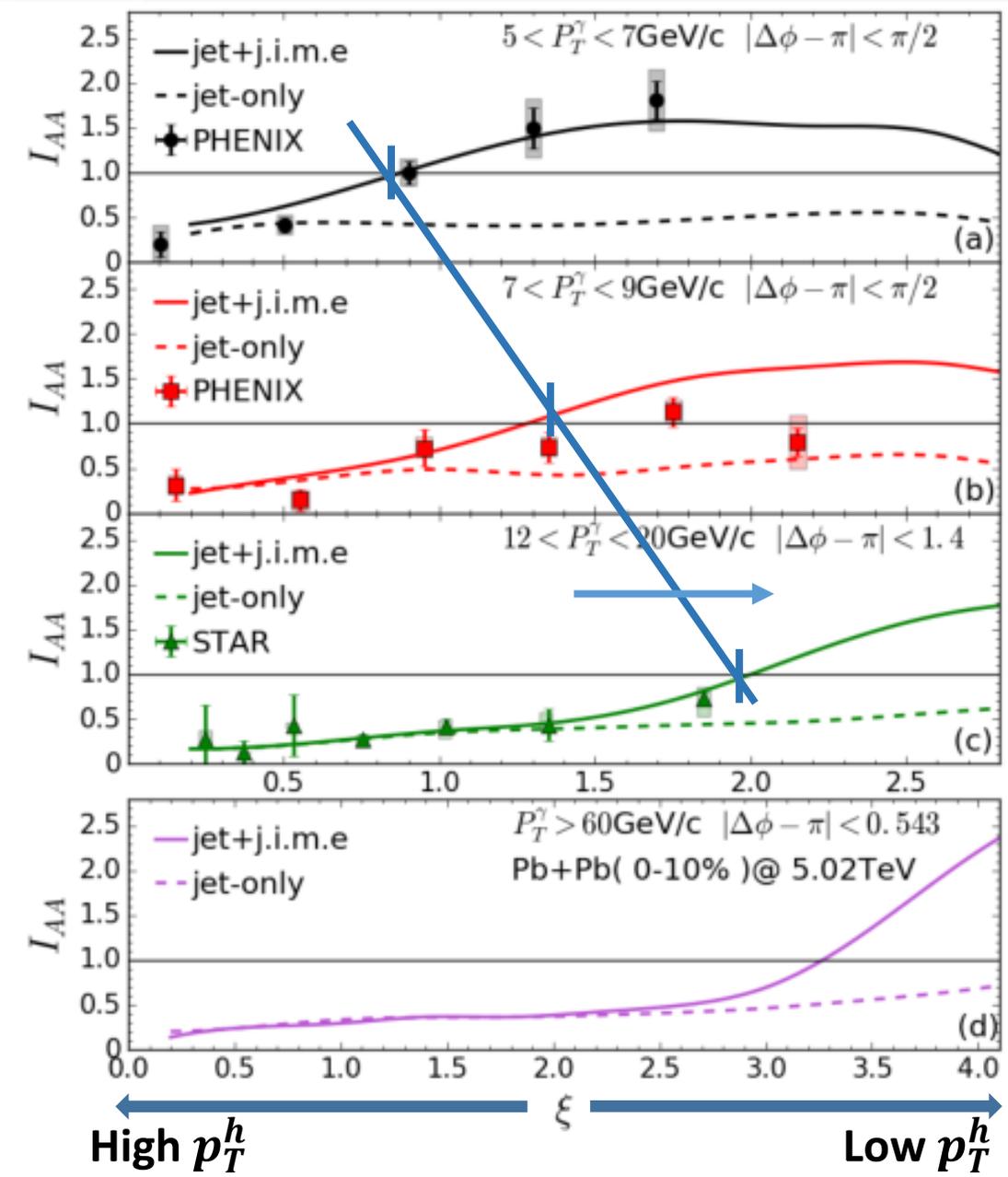
# Medium modification of $\gamma$ -triggered fragmentation function



- ✓ The suppression of leading hadron at small  $\varepsilon$
- ✓ The enhancement of soft hadrons at large  $\varepsilon$



# Medium modification of $\gamma$ -triggered fragmentation function



$$z = \frac{p_T^h}{p_T^\gamma} \quad \varepsilon = \log \frac{1}{z}$$

$$I_{AA}(\varepsilon) = \frac{D_{AA}(\varepsilon)}{D_{pp}(\varepsilon)}$$

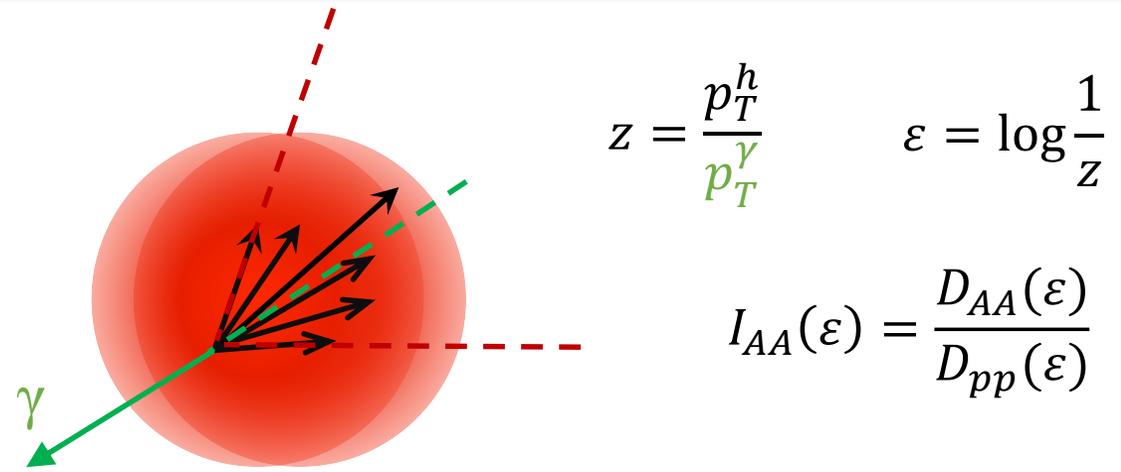
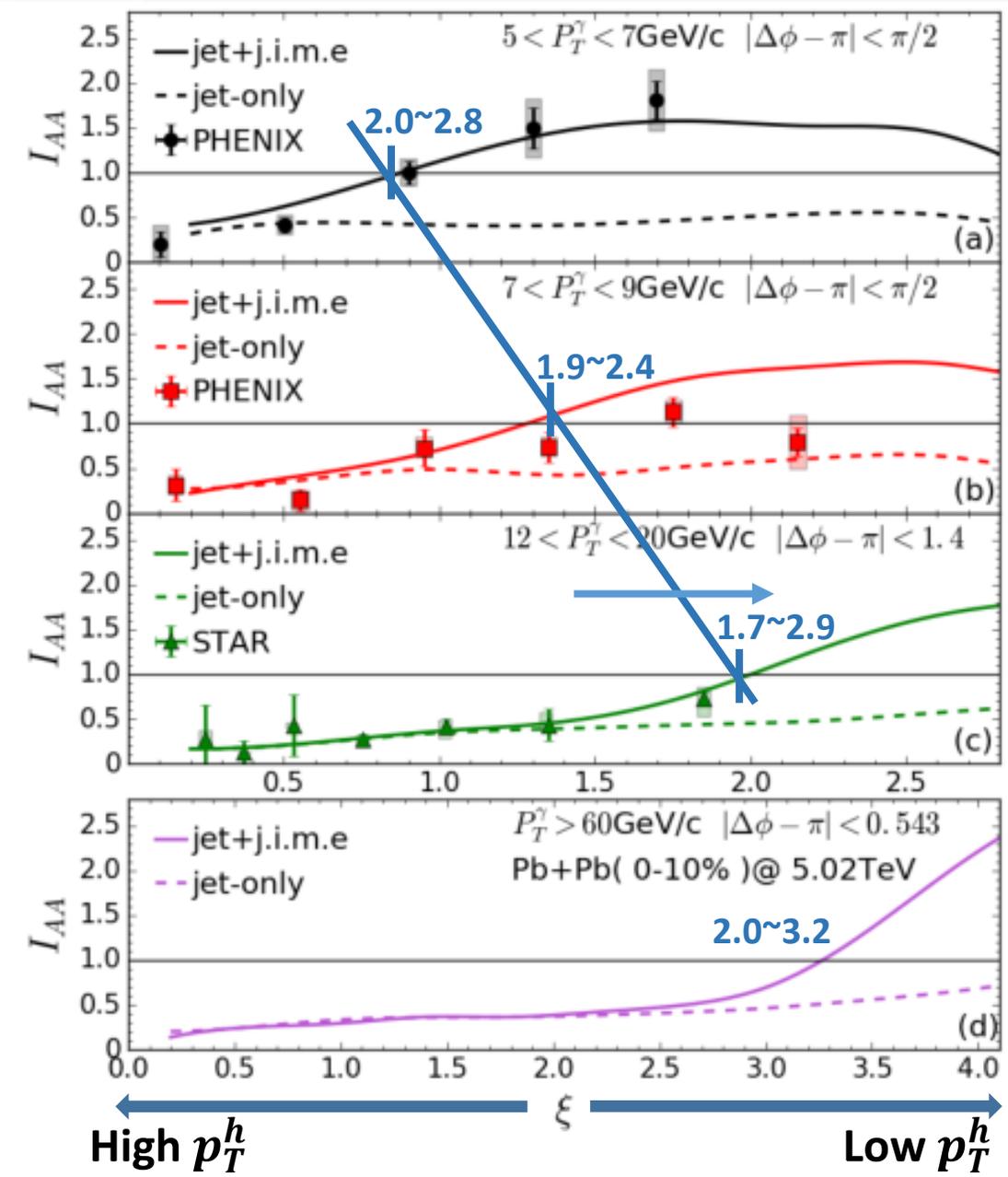
- ✓ The suppression of leading hadron at small  $\varepsilon$
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When  $p_T^\gamma$  range increases:

- ✓ Transition point ( $I_{AA} = 1$ ) from relative enhancement to suppression shift to large  $\varepsilon$ .



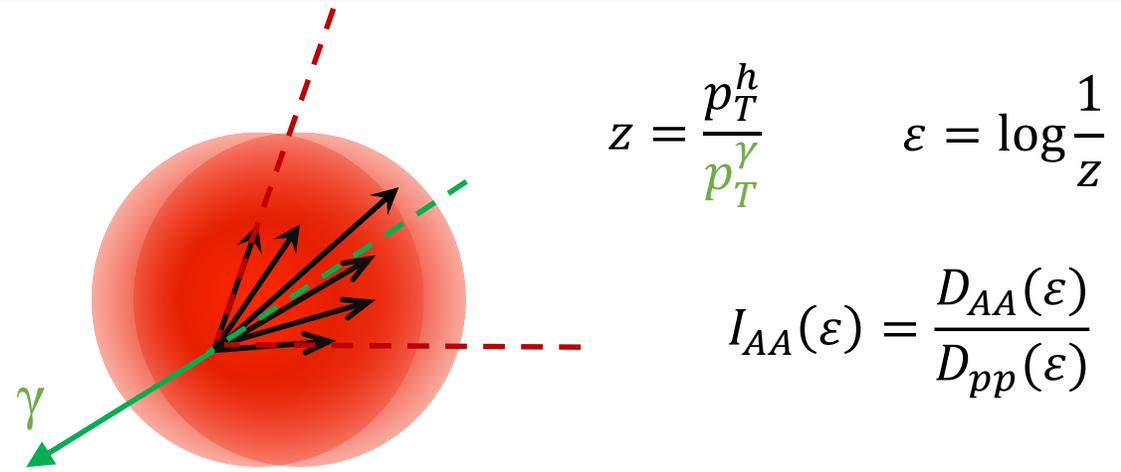
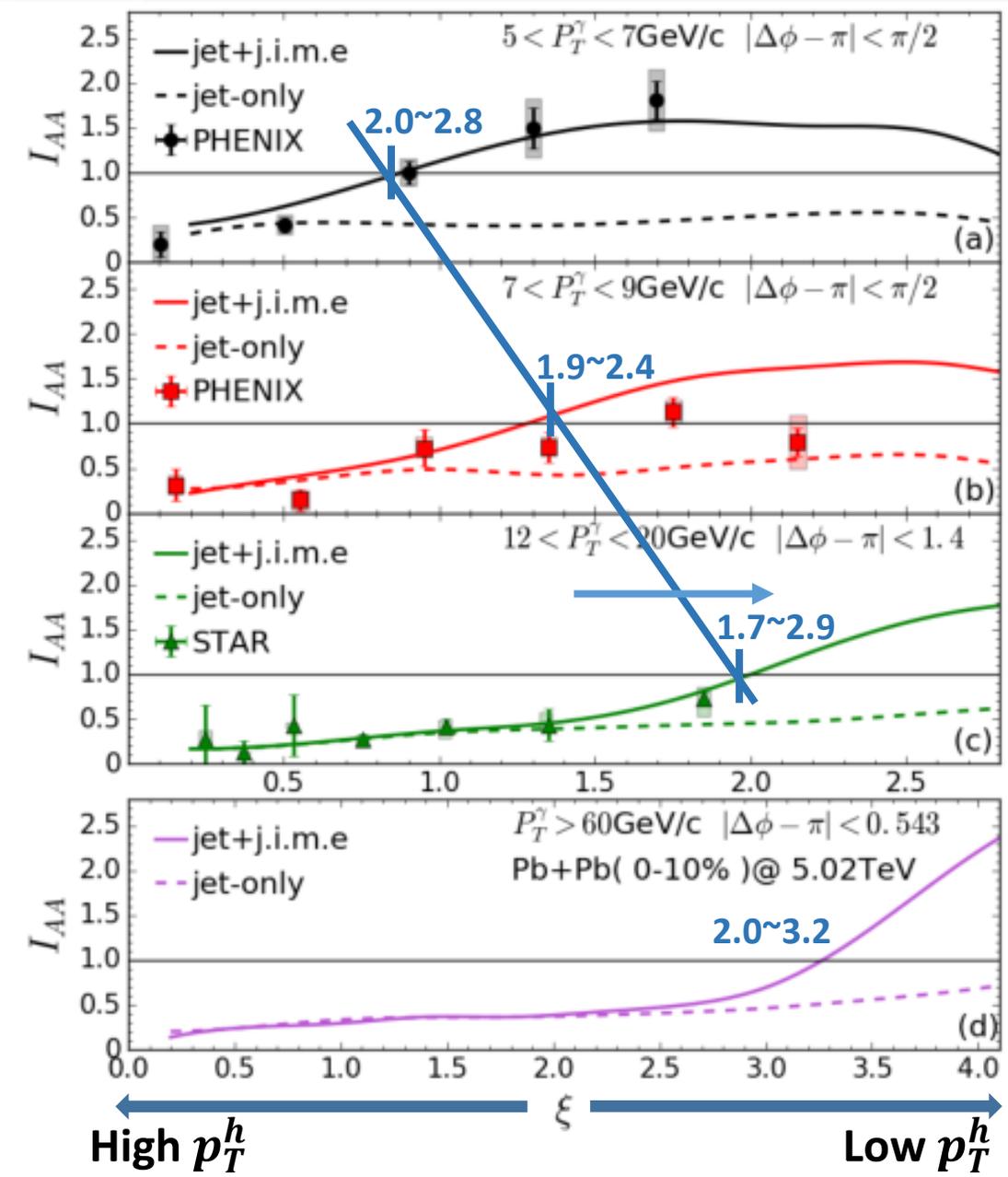
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- ✓ The suppression of leading hadron at small  $\varepsilon$
  - ✓ The enhancement of soft hadrons at large  $\varepsilon$
- When  $p_T^\gamma$  range increases:
- ✓ Transition point ( $I_{AA} = 1$ ) from relative enhancement to suppression shift to large  $\varepsilon$ .
  - ✓ Transition point corresponds to the fixed  $p_T^h$  range ( $p_T^h \sim 2 \text{ GeV/c}$  at RHIC,  $p_T^h \sim 3 \text{ GeV/c}$  at LHC)



# Medium modification of $\gamma$ -triggered fragmentation function



- ✓ The suppression of leading hadron at small  $\varepsilon$
- ✓ The enhancement of soft hadrons at large  $\varepsilon$

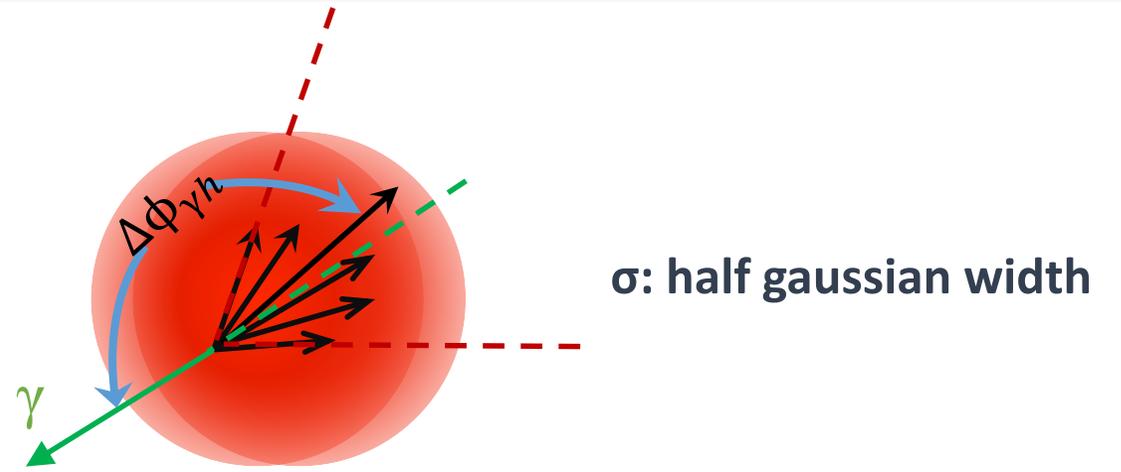
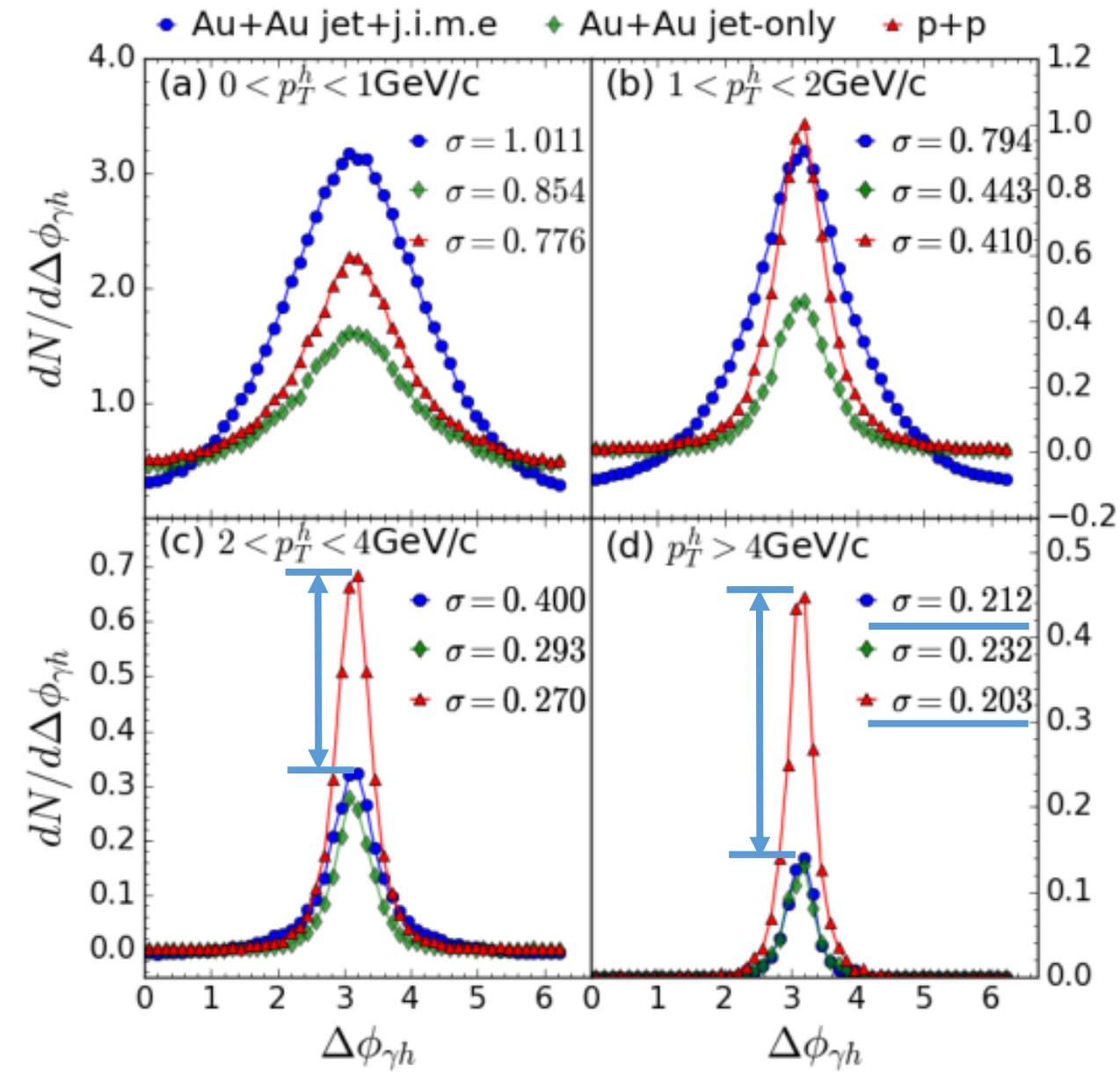
When  $p_T^\gamma$  range increases:

- ✓ Transition point ( $I_{AA} = 1$ ) from relative enhancement to suppression shift to large  $\varepsilon$ .
- ✓ Transition point corresponds to the fixed  $p_T^h$  range ( $p_T^h \sim 2 \text{ GeV/c}$  at RHIC,  $p_T^h \sim 3 \text{ GeV/c}$  at LHC)

soft hadrons from j.i.m.e. carry an average thermal energy that is independent of the jet energy



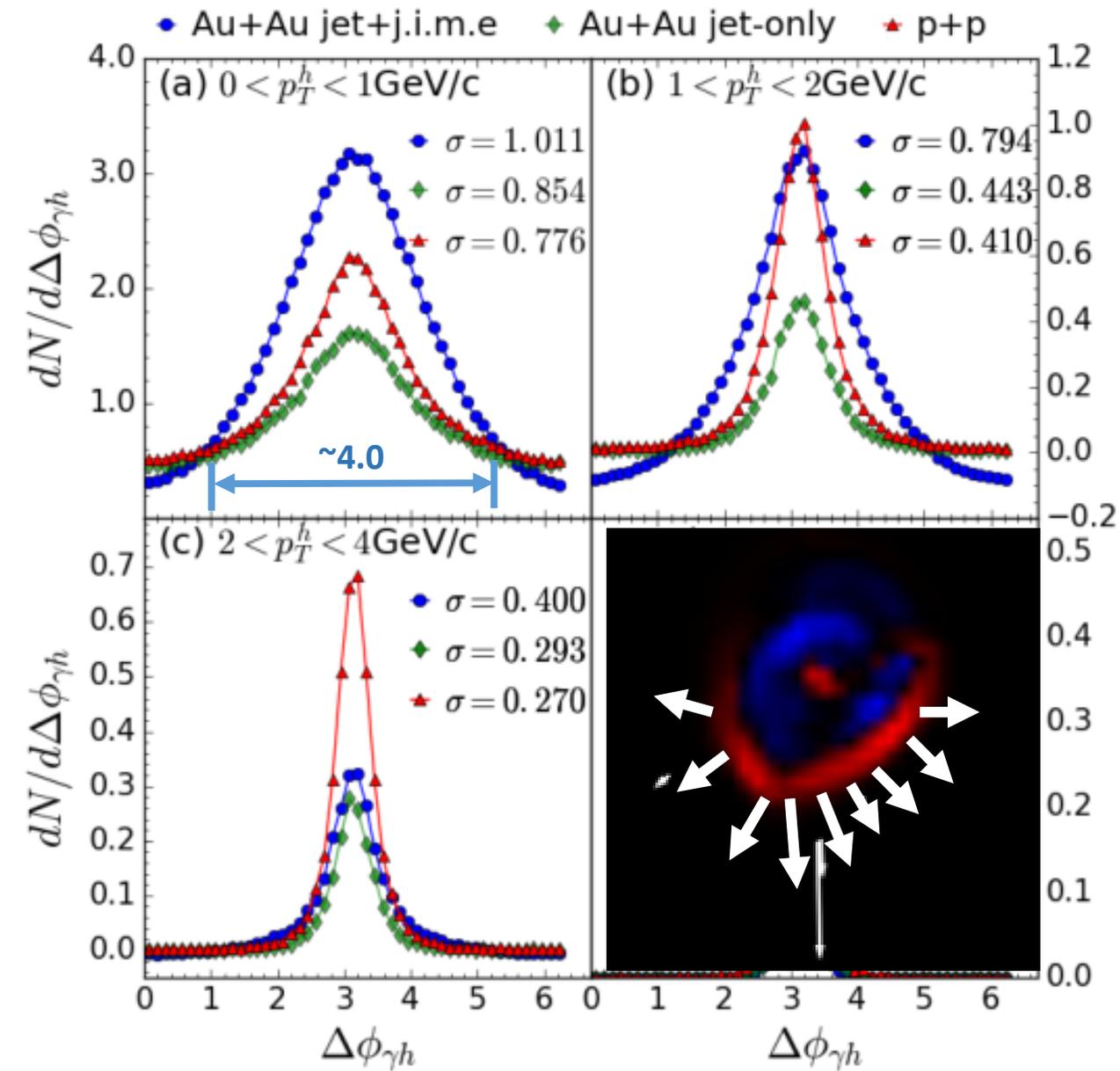
# $\gamma$ -hadron azimuthal correlation in RHIC



✓ Large  $p_T$  hadron yield are suppressed in Au+Au and the width of their angular distribution remain approximately unchanged from p+p



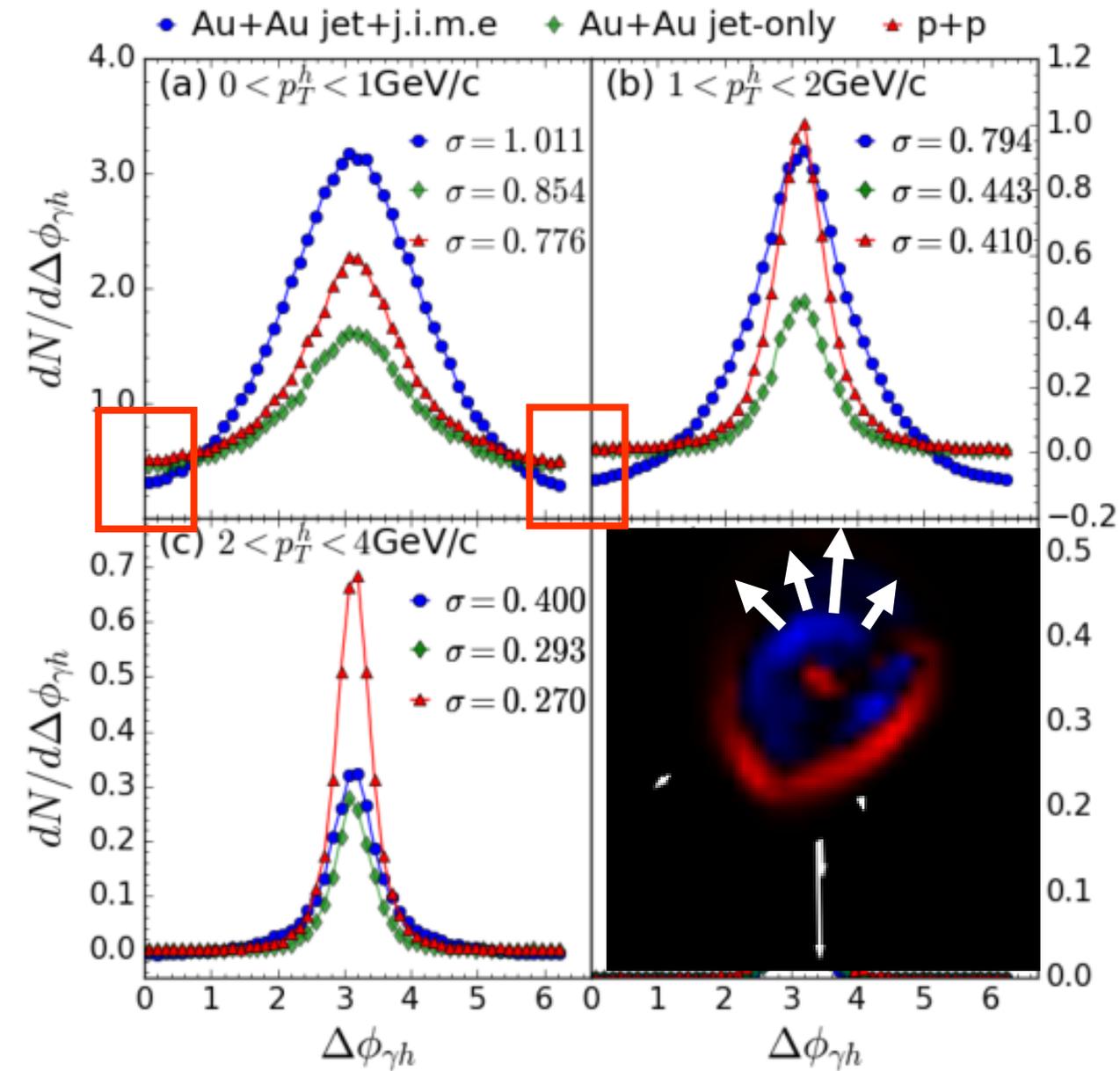
# $\gamma$ -hadron azimuthal correlation in RHIC



- ✓ Large  $p_T$  hadron yield are suppressed in Au+Au and the width of their angular distribution remain approximately unchanged from p+p
  - ✓ The angular distributions for the enhanced soft hadrons in Au+Au are significantly broadened.
- soft hadrons from j.i.m.e propagate at large angle relative to the jet direction



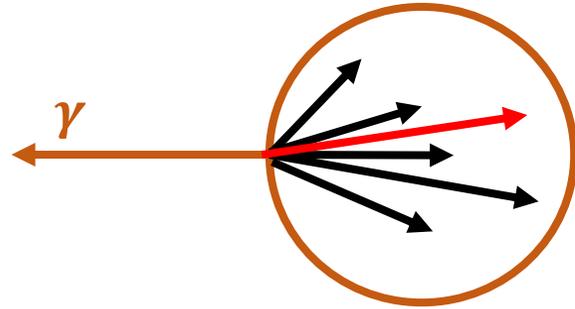
# $\gamma$ -hadron azimuthal correlation in RHIC



- ✓ Large  $p_T$  hadron yield are suppressed in Au+Au and the width of their angular distribution remain approximately unchanged from p+p
- ✓ The angular distributions for the enhanced soft hadrons in Au+Au are significantly broadened.
- soft hadrons from j.i.m.e propagate at large angle relative to the jet direction
- ✓ soft hadrons yield in Au+Au collision along gamma direction become smaller than one in pp collision. the effect of diffusion wake caused by → the deposition of energy-momentum into the medium



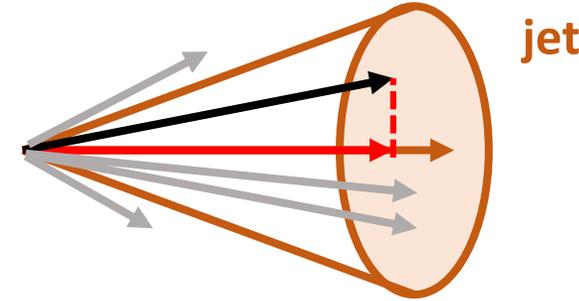
# Fragmentation function at RHIC and LHC



$$z = \frac{p_T^h}{P_T^\gamma}$$

STAR(PHENIX)

- ✓ Photon-hadrons FF, no reconstructed jets
- ✓ Take hadrons away from the triggering object(photon)
- ✓ Look at the fraction of hadron  $p_T$  in photon  $p_T$



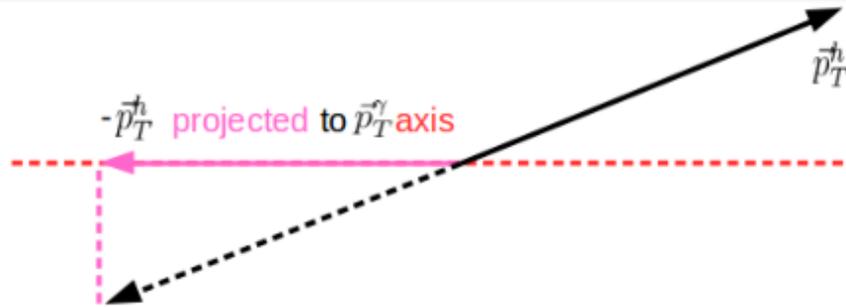
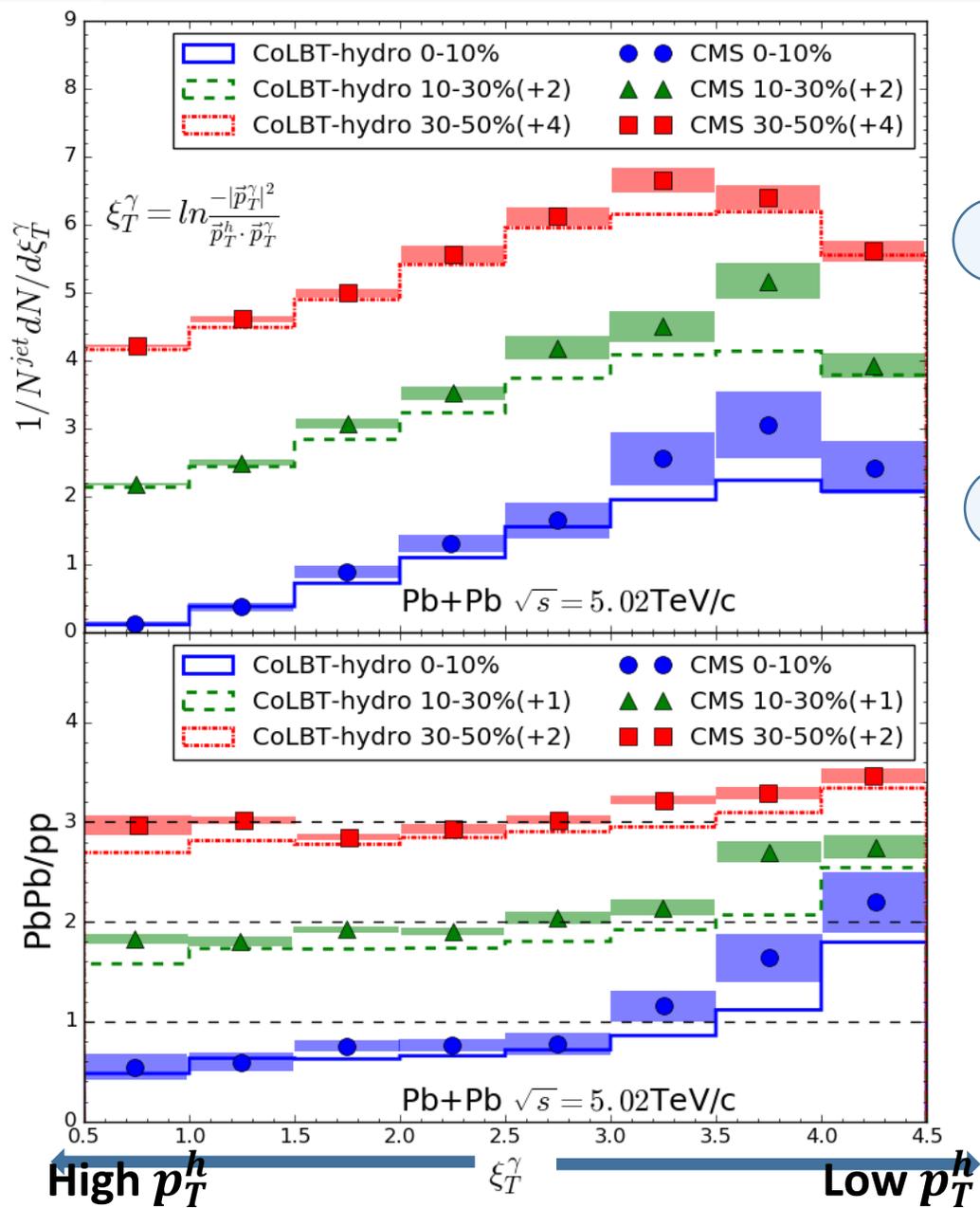
$$z = \frac{p_{||}^h}{p^{jet}}$$

CMS

- ✓ jet+hadrons FF, reconstructed jets
- ✓ Take hadrons in side the jet cone
- ✓ Project  $p_T^h(p^h)$  onto jet axis and look at the fraction in  $p_T^{jet}(p^{jet})$



# Fragmentation function at LHC

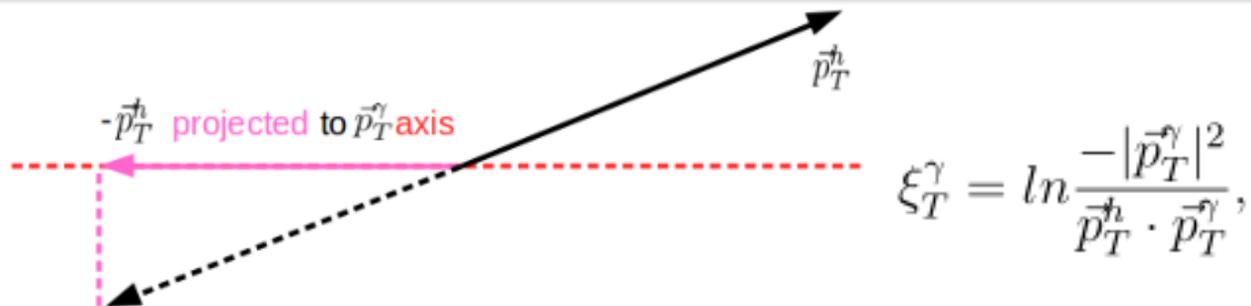
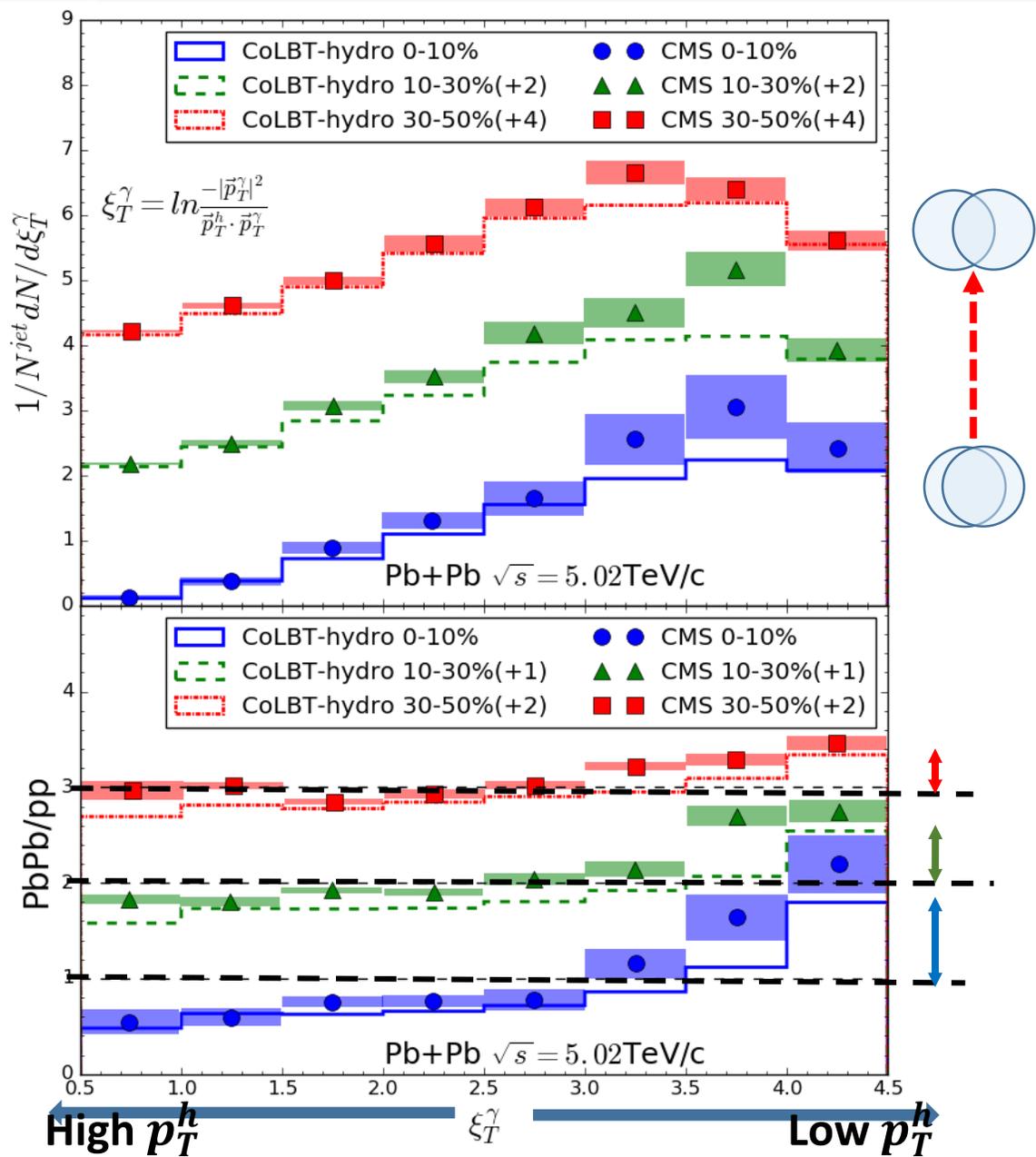


$$\xi_T^\gamma = \ln \frac{-|\vec{p}_T^\gamma|^2}{\vec{p}_T^h \cdot \vec{p}_T^\gamma}$$

✓ Based on photon energy, proxy for the parton energy before jet quenching.



# Fragmentation function at LHC



✓ Based on photon energy, proxy for the parton energy before jet quenching.

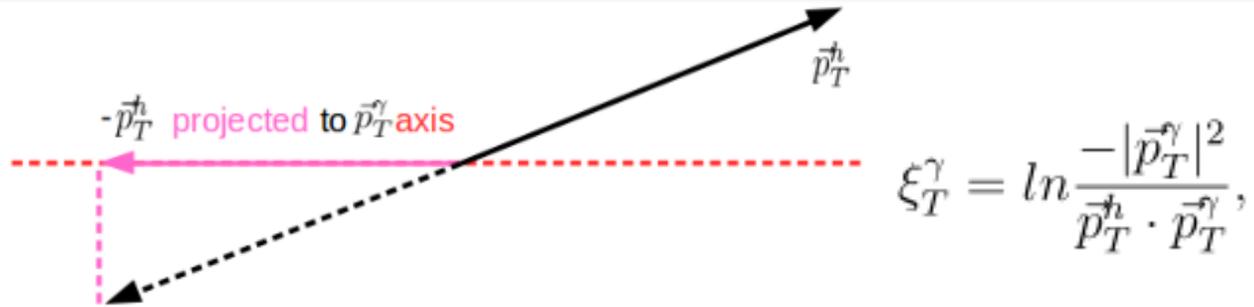
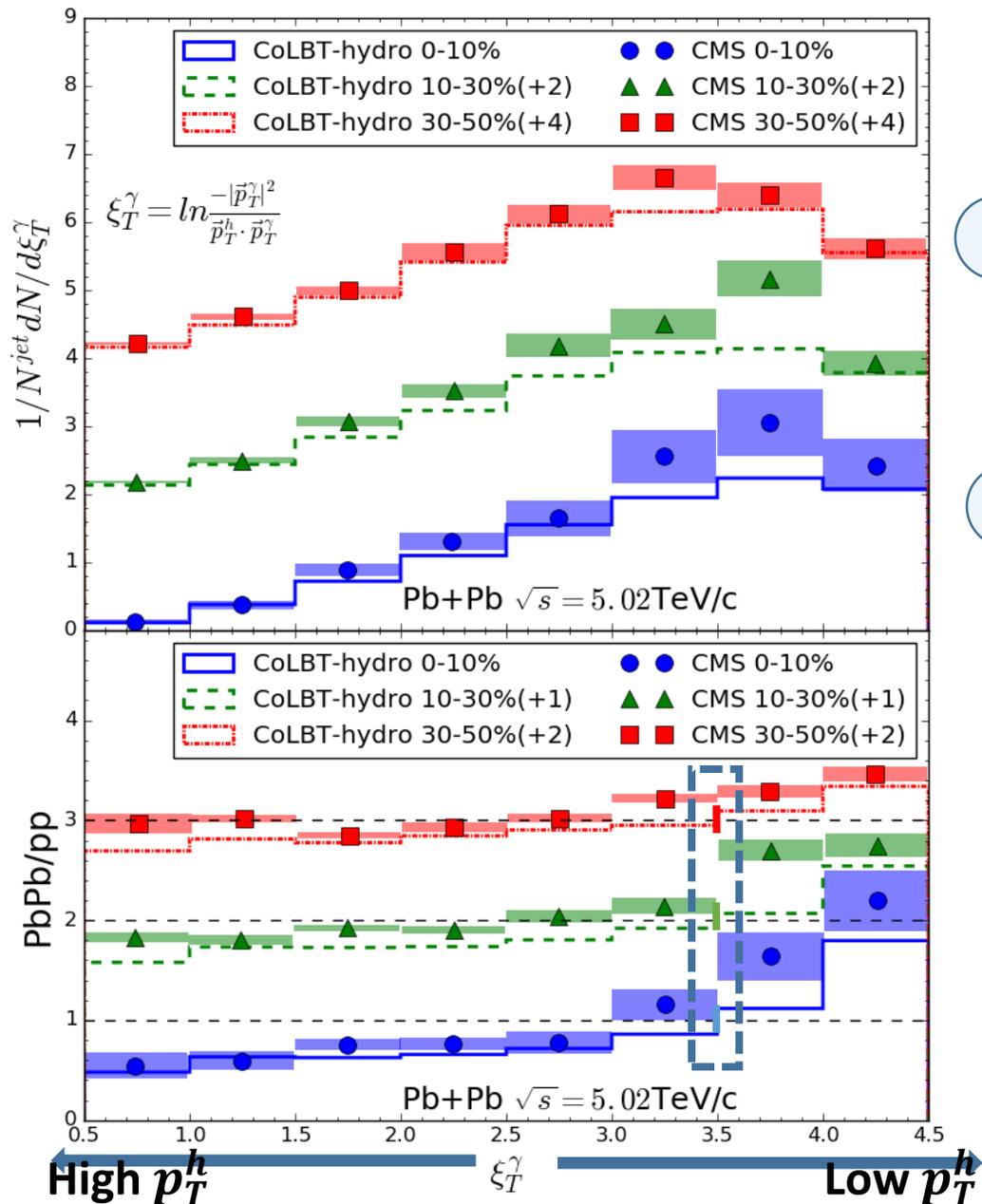
Centrality dependence:

- ✓ Enhancement of low  $p_T^h$  hadrons
- ✓ Suppression of high  $p_T^h$  hadrons

→ path length and temperature different



# Fragmentation function at LHC



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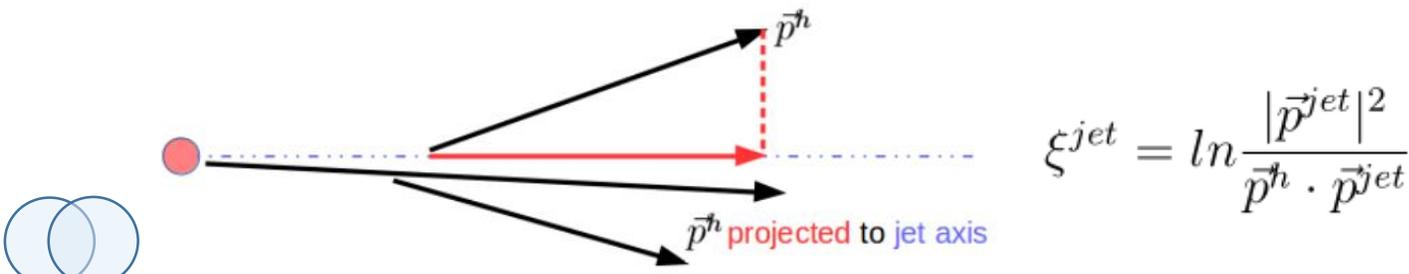
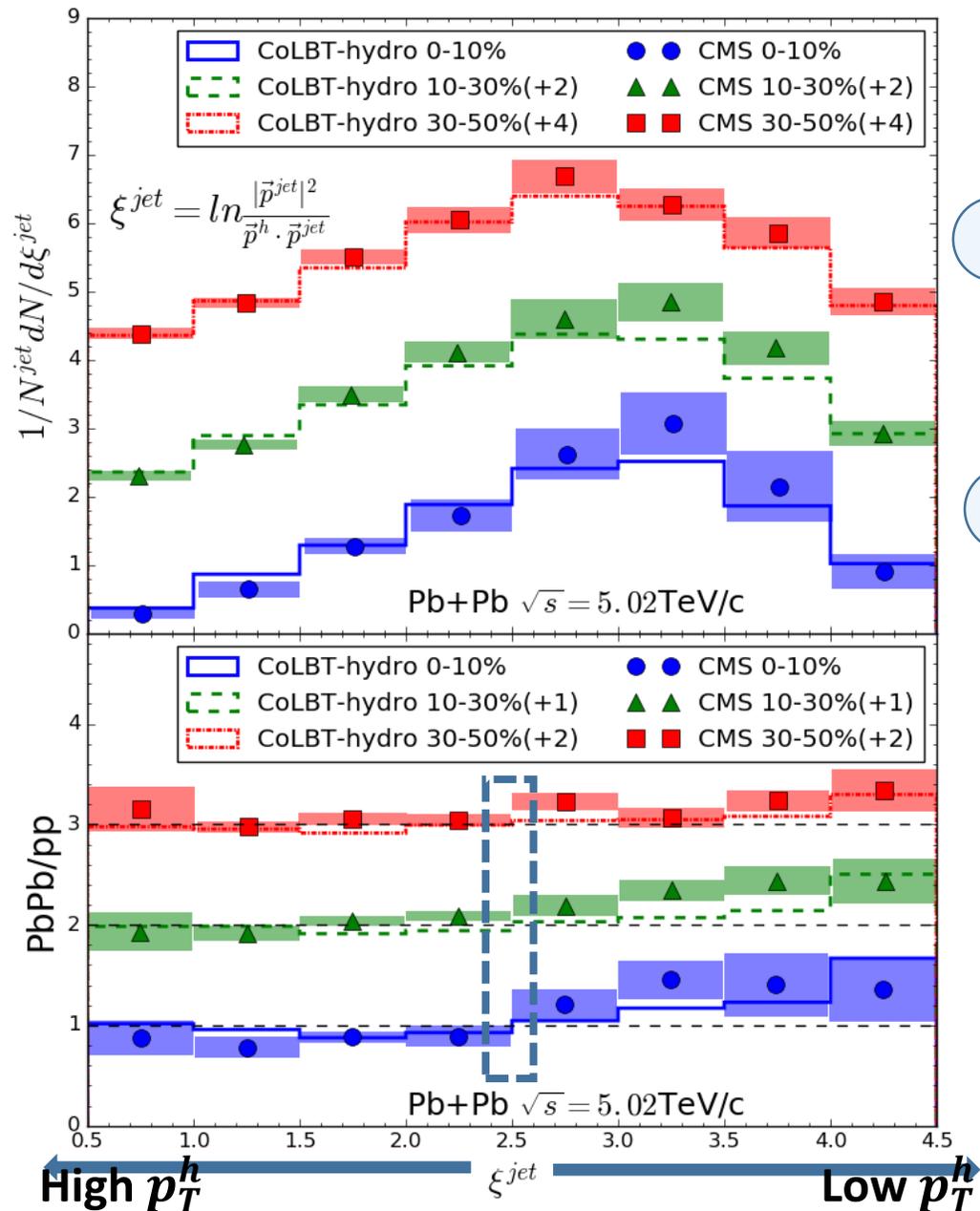
No (slightly) centrality dependence:

- ✓ Transition point ( $I_{AA} = 1$ ) from relative enhancement to suppression.

$$\varepsilon_T^\gamma \approx 3.5 \rightarrow p_T^h \approx 2 \sim 3 \text{ GeV}$$



# Fragmentation function at LHC



✓ Based on reconstructed jet energy

Centrality dependence:

- ✓ Enhancement of low  $p_T^h$  hadrons
  - ✓ Suppression of high  $p_T^h$  hadrons
- path length and temperature different

No (slightly) centrality dependence:

- ✓ Transition point ( $I_{AA} = 1$ ) from relative enhancement to suppression.

$$\xi^{jet} \approx 2.5 \rightarrow p_T^h \approx 2 \sim 3 \text{ GeV}$$

A graphic consisting of a large white circle with the word "Summary" in blue text inside it. The circle is surrounded by several smaller blue circles of varying sizes, some overlapping the bottom edge of the white circle.

## Summary

- ✓ We develop CoLBT-Hydro model for simultaneous event-by-event simulations of jet propagation and hydrodynamic evolution of the bulk medium including jet-induced medium excitation.
- ✓ CoLBT-hydro describes well both the suppression of leading hadrons due to parton energy loss and enhancement of soft hadrons due to jet-induced medium excitation
- ✓ The onset of soft hadron enhancement at a constant  $p_T^h$  with broadened angular distribution and depletion of soft hadrons in the  $\gamma$  direction



## The model needs to be improved in

- ✓ Ideal hydrodynamic
- ✓ Neglect hadronization between jet shower partons and thermal partons
- ✓ Neglect the interaction between hadrons
- ✓ Only use AMPT as initial condition for medium hydrodynamic evolution
- ✓ Light quark on shell

.....

## The model can be used to calculate

- ✓ Nuclear modification factor  $R_{AA}$
  - ✓ dihadron correlation
  - ✓ jet shape
  - ✓ dijet correlation
- and many other observables