

# Muon Colliders vs other technologies based Colliders

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# Disclaimer

## Comparison between High Energy Leptons & Protons Colliders

- Muon Colliders (MAP, LEMMA, MC in LHC tunnel, (in FCC tunnel?))
- E<sup>+</sup>/E<sup>-</sup> Circular colliders (FCC ee)
- E<sup>+</sup>/E<sup>-</sup> Linear colliders (ILC, CLIC, PWFA, LPA, DLA)
- Protons Colliders (LHC, FCC hh)

## Over a wide energy range

- From 125 GeV to Multi-TeV at the level of the elementary constituents

## Of major performances, especially:

- Physics potential: Luminosity
  - Including whole particle energy spectrum
  - limited to particles within 1% momentum spread
  - Total =  $\sum$  from all detectors
- Practical technicalities:
  - Cost & Power

## Through Figures of Merit (FoM) for fair and objective comparison

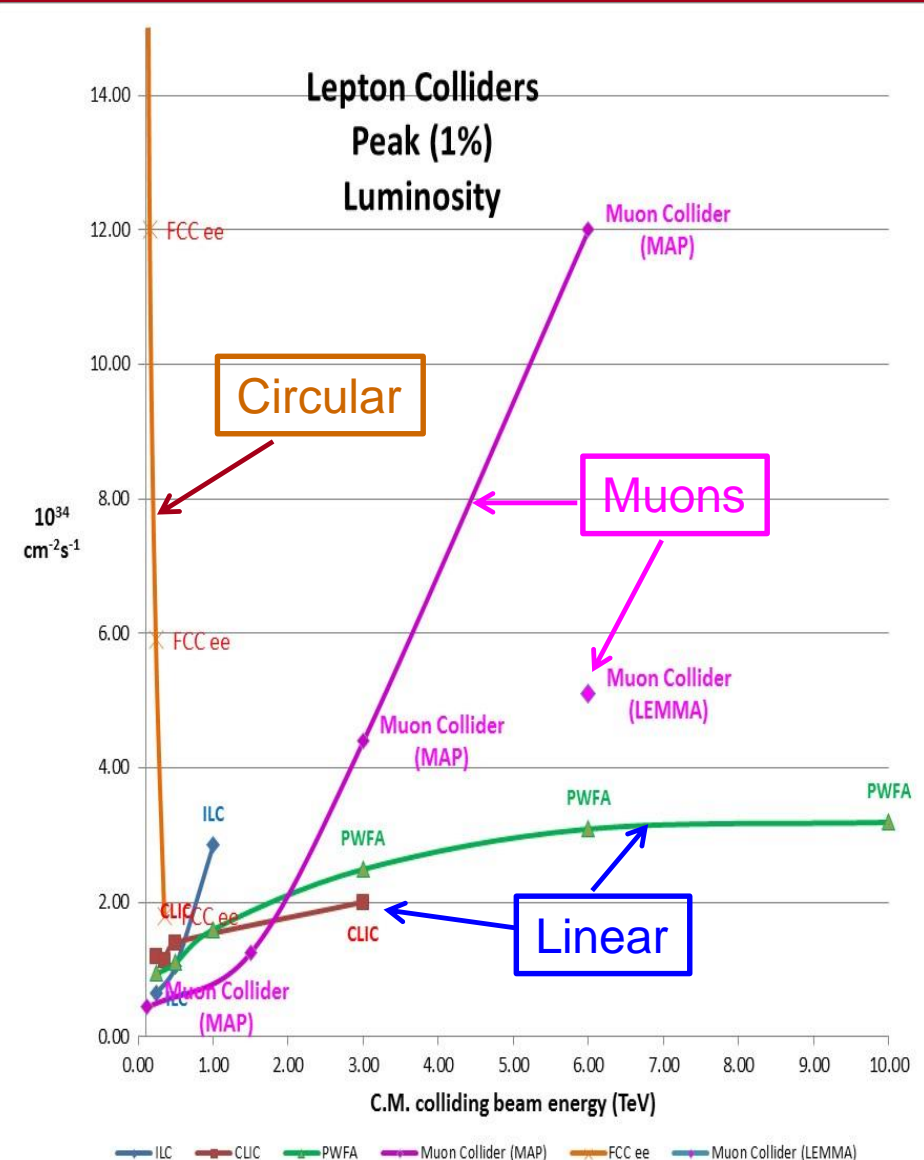
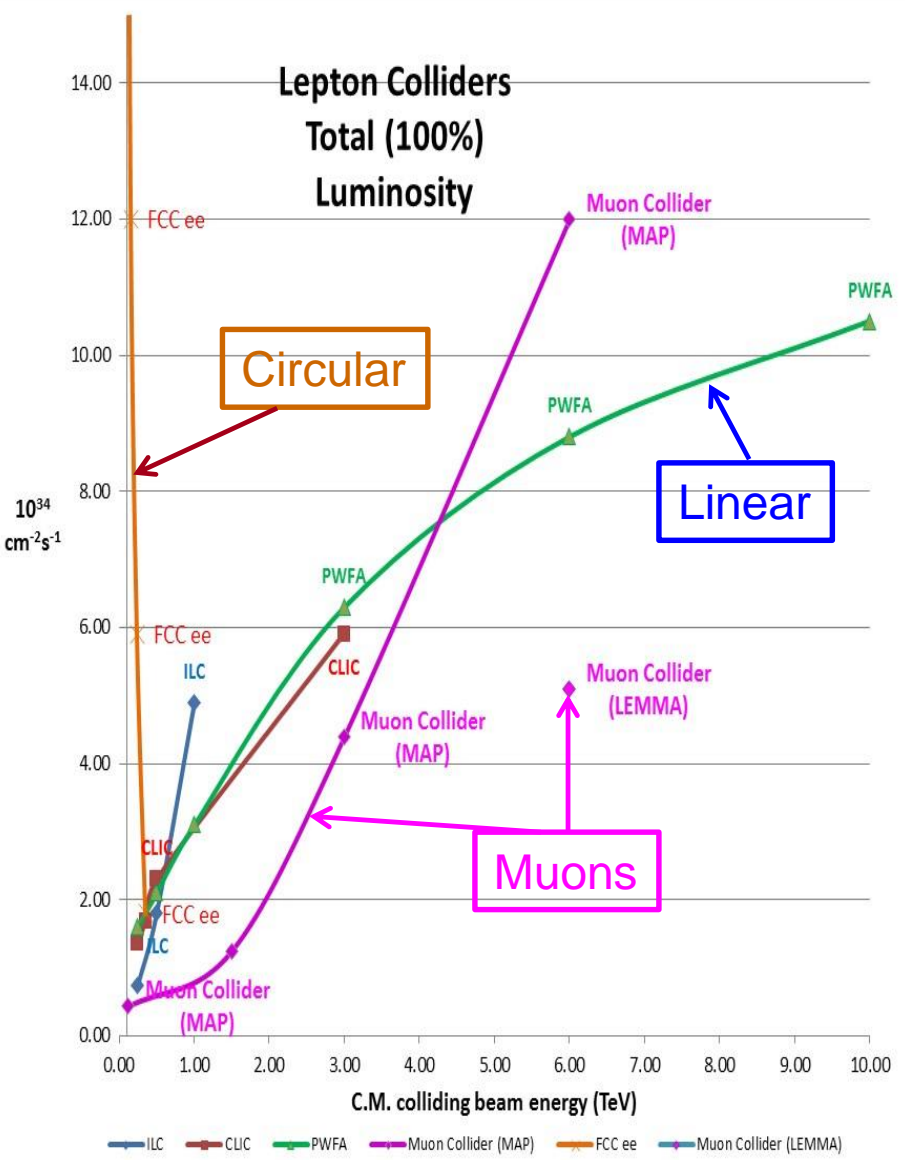
- Based on **official data** when available, collected in 2015, thus possibly out of date
- Some power estimations slightly corrected for common assumptions
- When no available data (Cost), estimation using a common model even if not accurate

**Welcome to point out necessary corrections or updates**

# Data (updated August 2015)

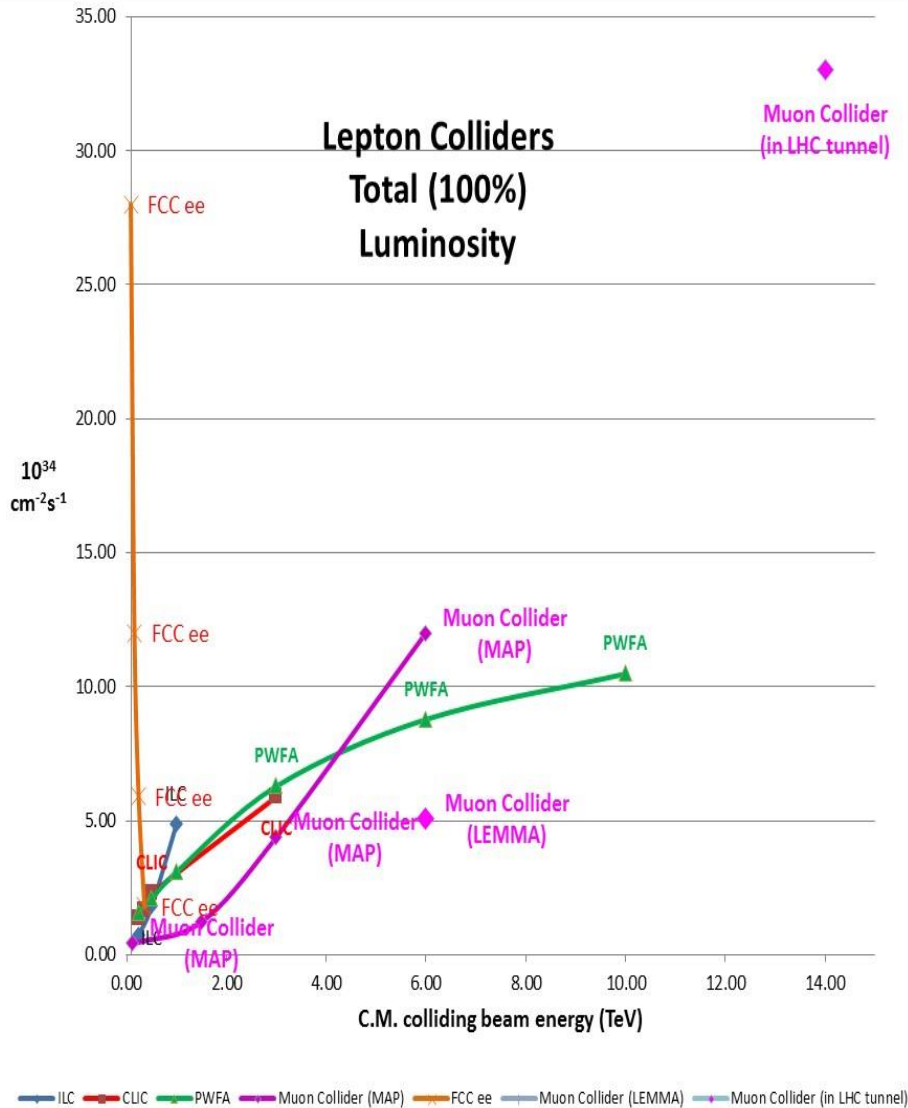
	Facility	Ecm TeV	HIGGS/5y	Ltot 10 <sup>^34</sup>	L0.01 10 <sup>^34</sup>	Nb IP #	Power MW	size km	Cost		
									Official	Shiltsev B\$	
Linear Colliders	ILC	0.25	115000	0.75	0.65	1	128	21.0	5.07	1.02E+01	
		0.50		1.80	1.05	1	162	31.0	7.80	1.31E+01	
		1.00		4.90	2.86	1	301	48.0	12.09	1.79E+01	
	CLIC	0.25	170000	1.37	1.19	1	235	13.2	6.13	1.04E+01	
		0.35		1.69	1.13	1	250	11.4		1.12E+01	
		0.50		2.30	1.40	1	272	13.2	7.81	1.27E+01	
		3.00		5.90	2.00	1	589	48.3		2.66E+01	
	PWFA beam driven	0.25	150000	1.60	0.94	1	133	2.3			8.25E+00
		0.50		2.10	1.10	1	150	3.0			1.06E+01
		1.00		3.10	1.60	1	186	4.5			1.41E+01
		3.00		6.30	2.50	1	301	8.0			2.26E+01
		6.00		8.80	3.10	1	398	13.0			3.08E+01
	Laser driven Plasma (LPA)	10.00		10.50	3.20	1	478	18.5			3.87E+01
		0.25	1.00	0.64	0.64	1	113	2.3			8.08E+00
		3.00	1.00	6.40	6.40	1	344	5.6			2.25E+01
	Dielectrics (DLA)	10.00		10.00				15.0			
0.25		185000	1.30	1.30	1	146	3.1			8.53E+00	
3.00			5.40	5.40	1	449	15.6			2.41E+01	
	Circular Colliders	FCC ee	0.09		28.00	28.00	4				
0.16				12.00	12.00	4					
0.24			0.00	1458000	5.90	5.90	4	320	81.0	10.00	1.42E+01
0.35			0.00		1.80	1.80	4	350	81.0	10.50	1.53E+01
Muon Collider	HIGGS Factory	0.13	Rubbia	220000	1.43	1.43	1	200	1.5	3.75	7.21E+00
		0.13	MAP	67500	0.44	0.44	1	200	1.5	3.75	7.14E+00
	MAP	1.50	MAP		1.25	1.25	2	216	2.5		1.62E+01
		3.00	MAP		4.40	4.40	2	230	4.0		2.16E+01
		6.00	MAP		12.00	12.00	2	270	6.0		2.93E+01
	LEMMA	6.00	LEMMA 6kme+acc		5.10	5.10	2.00	490.00	6.00		3.05E+01
		6.00	LEMMA27kme+acc		5.10	5.10	2.00	399.00	6.00		3.00E+01
	LHC tunnel	14.00	LHC 2 det	135000	33.00	33.00	2	333	26.7		1.07E+01
		14.00	LHC 4 det		33.00	33.00	4	377	26.7		1.07E+01
FCC upgrade	100.00	FCC μμ		10.00	10.00	4		100.00			
Proton Collider	LHC	2.00		2.00	2.00	2	200	26.7		2.02E+01	
	LHC-HL	2.00		5.00	5.00	2	200	26.7		2.02E+01	
	FCC-hh	14.29		10.00	10.00	2	400	100.0		4.81E+01	

# Lepton Colliders Luminosity

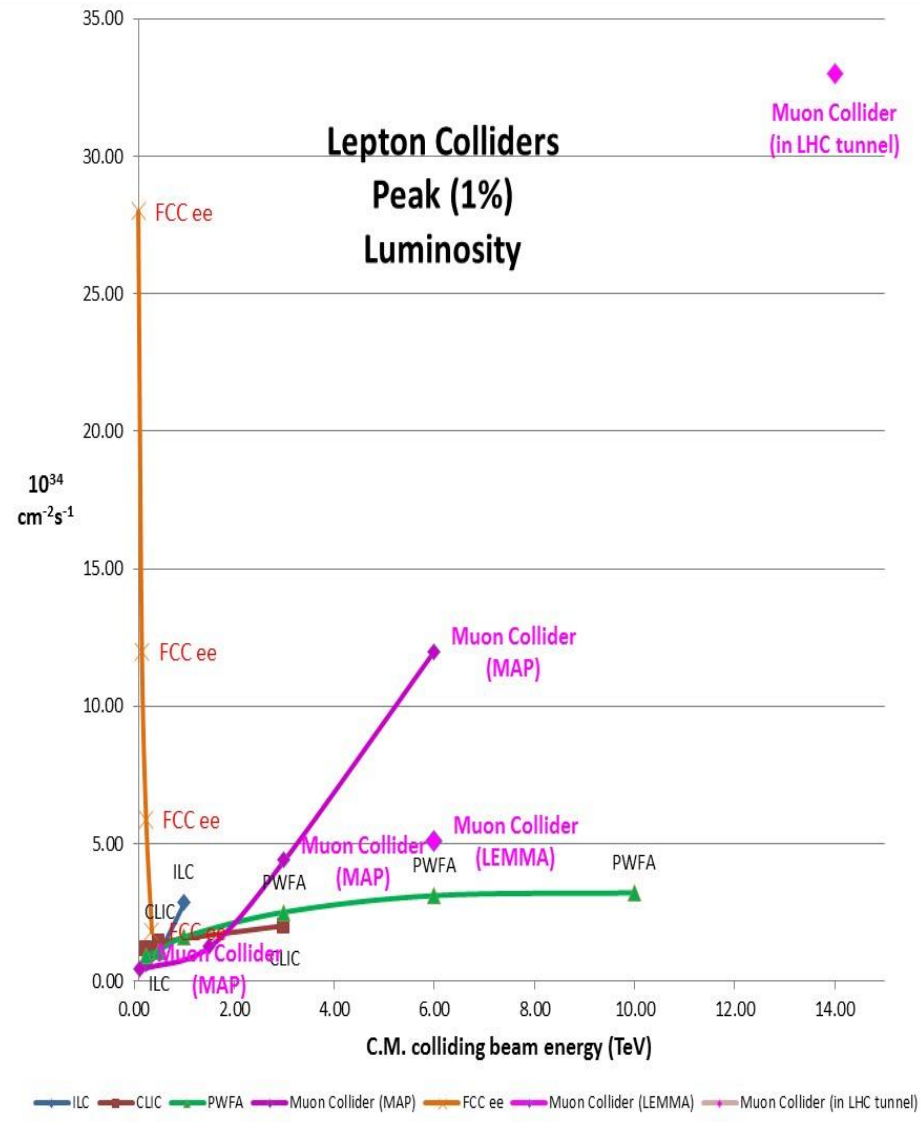


# Lepton Colliders Luminosity

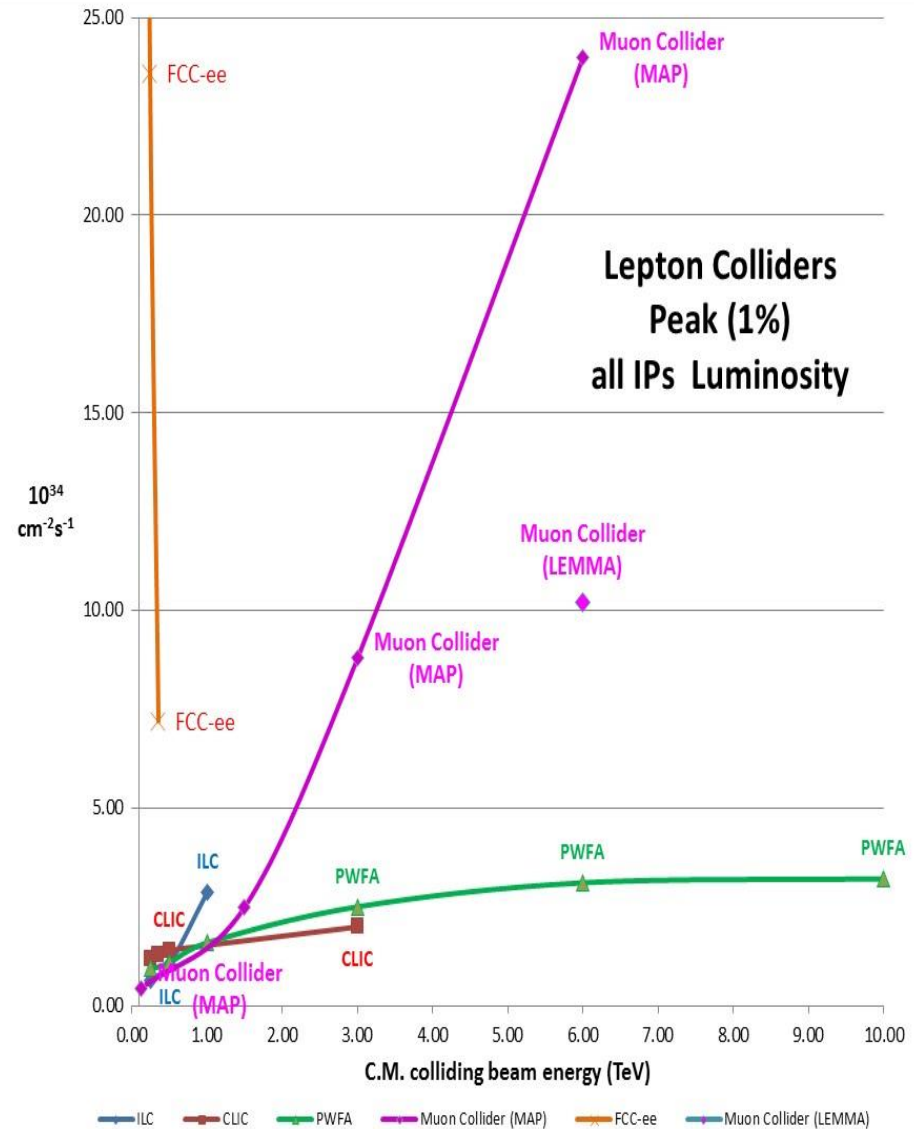
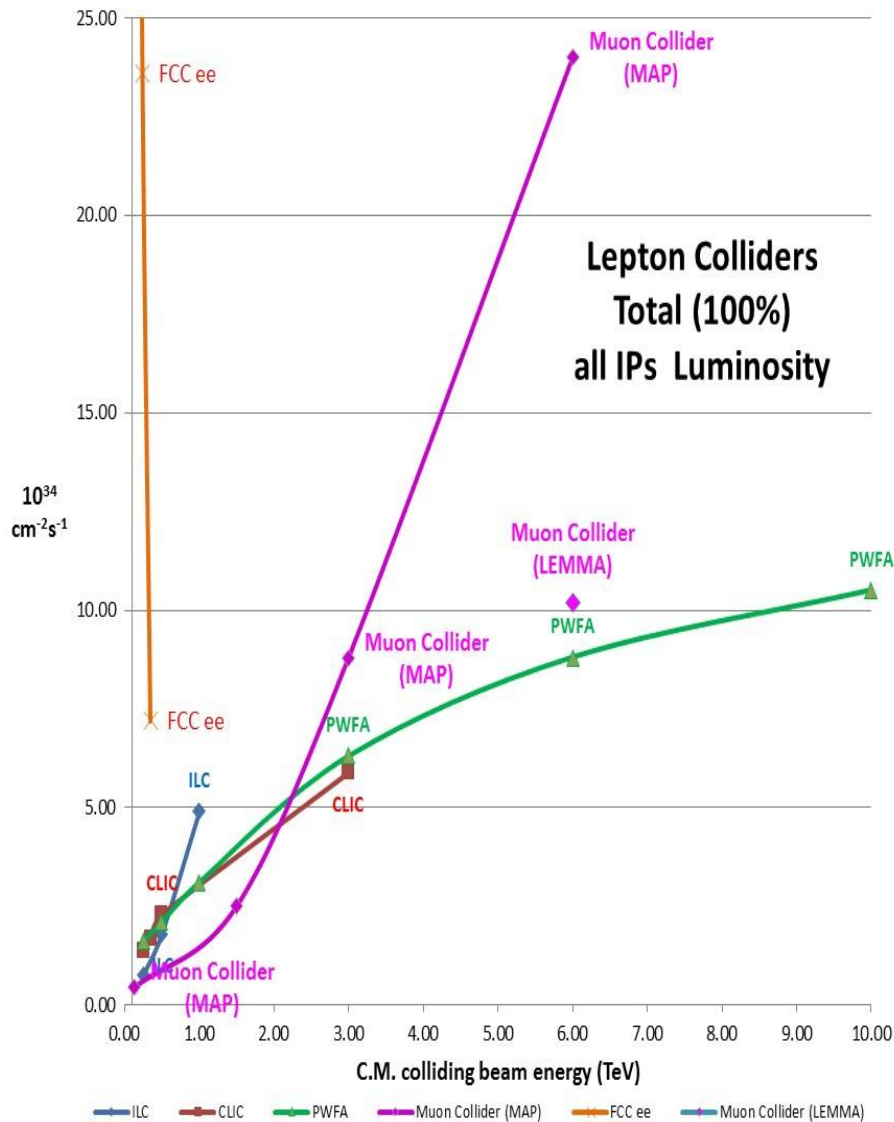
**Lepton Colliders  
Total (100%)  
Luminosity**



**Lepton Colliders  
Peak (1%)  
Luminosity**

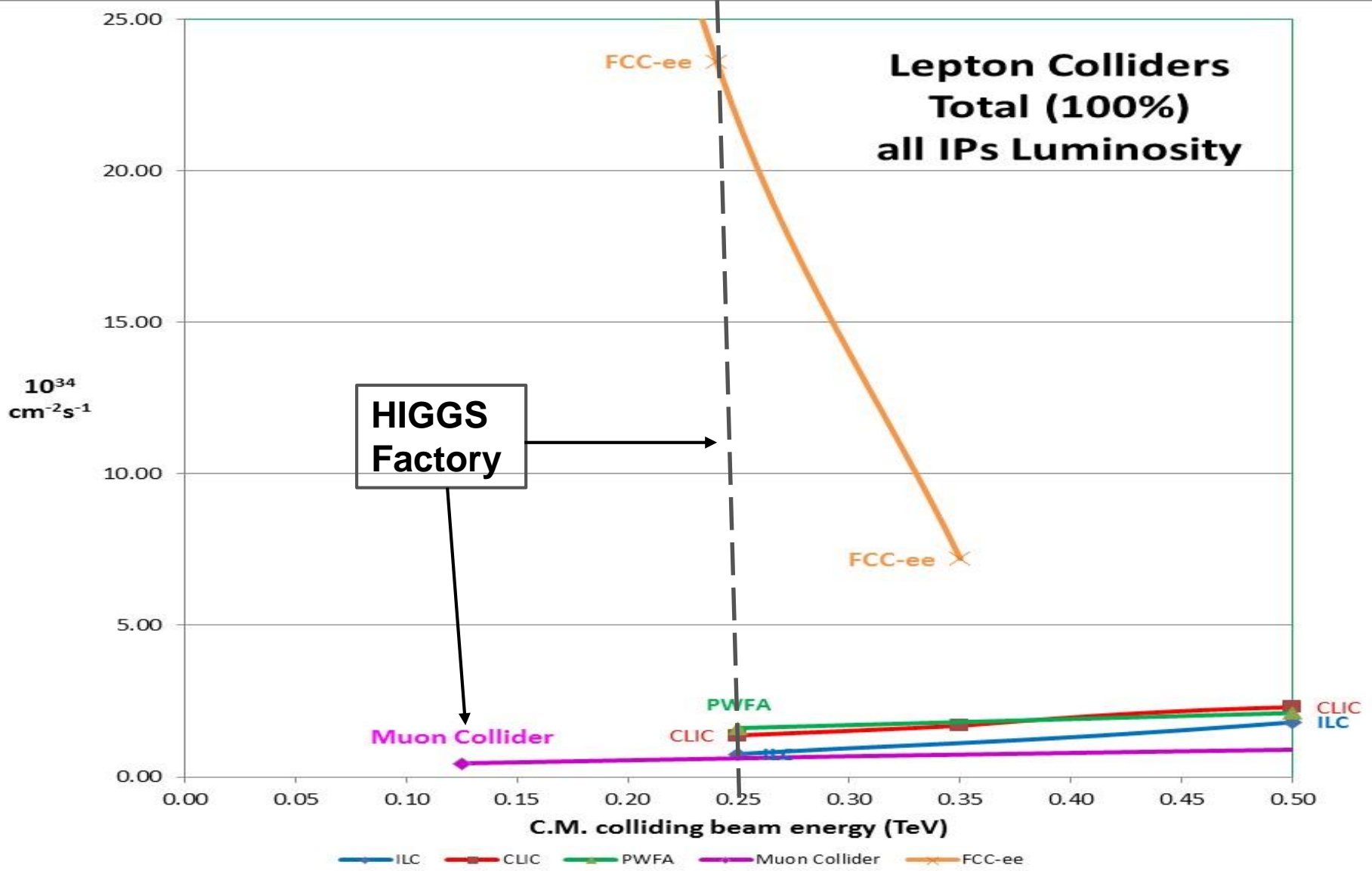


# Lepton Colliders $\Sigma$ IP Luminosity

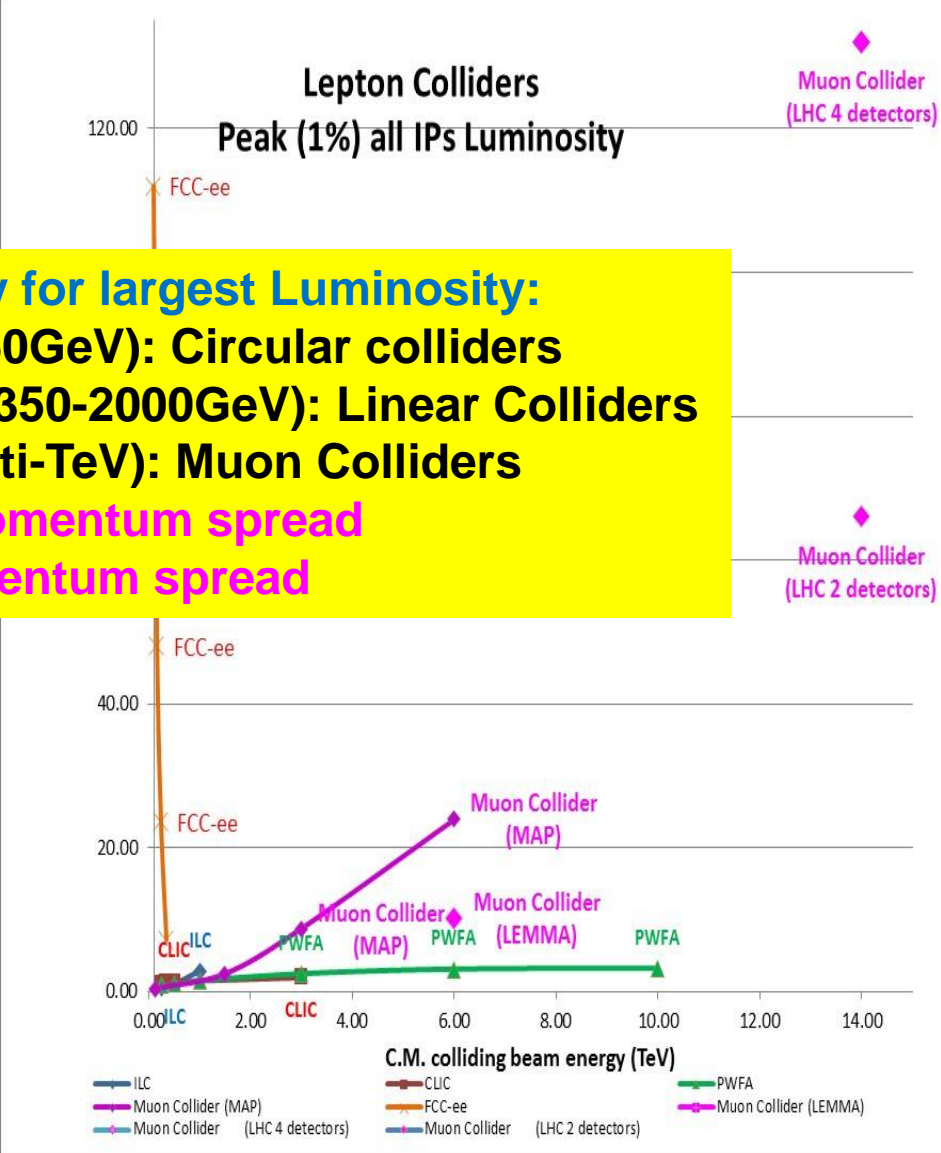
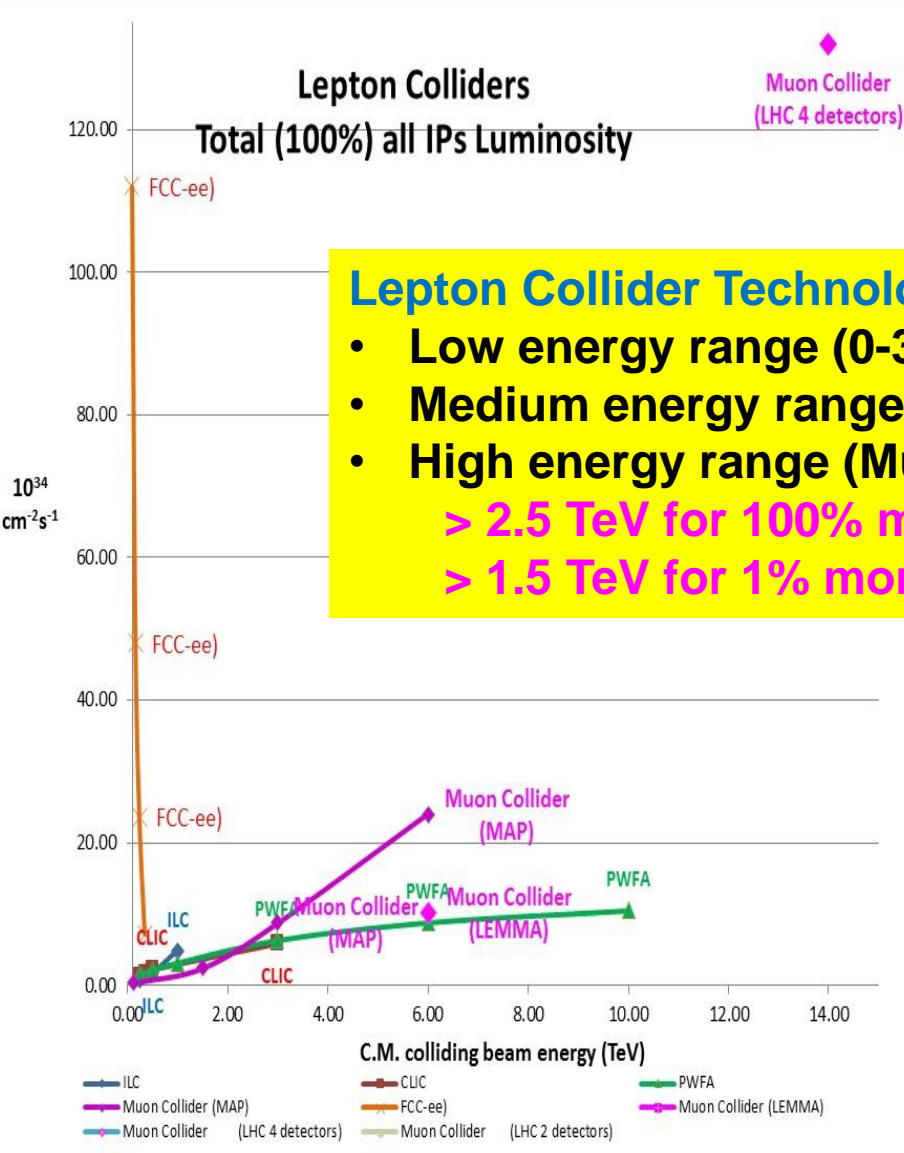


# Lepton Colliders

## $\Sigma$ IP Luminosity in HIGGS energy range



# Lepton Colliders All IP Luminosities

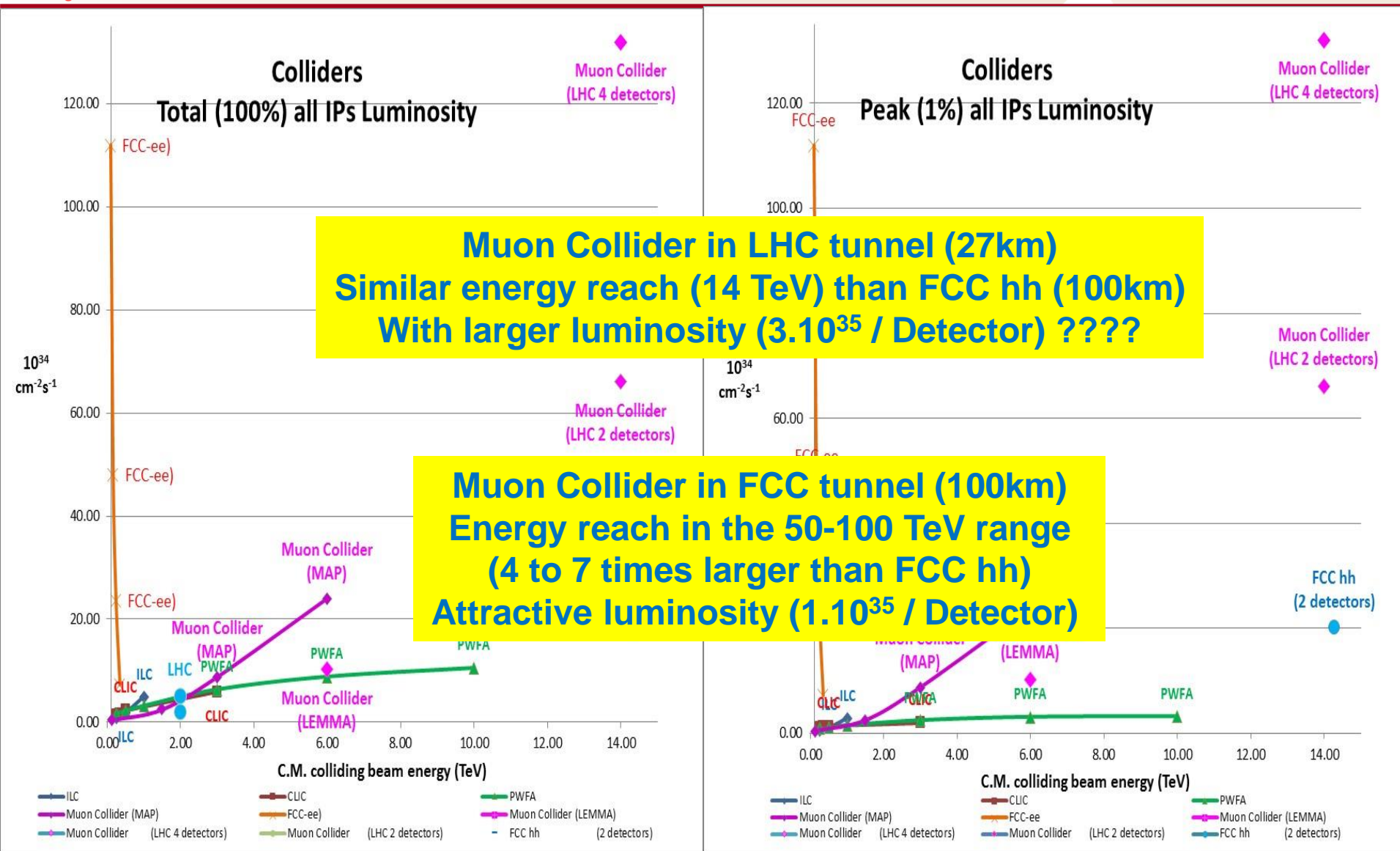


**Lepton Collider Technology for largest Luminosity:**

- Low energy range (0-350GeV): Circular colliders
- Medium energy range (350-2000GeV): Linear Colliders
- High energy range (Multi-TeV): Muon Colliders
  - > 2.5 TeV for 100% momentum spread
  - > 1.5 TeV for 1% momentum spread



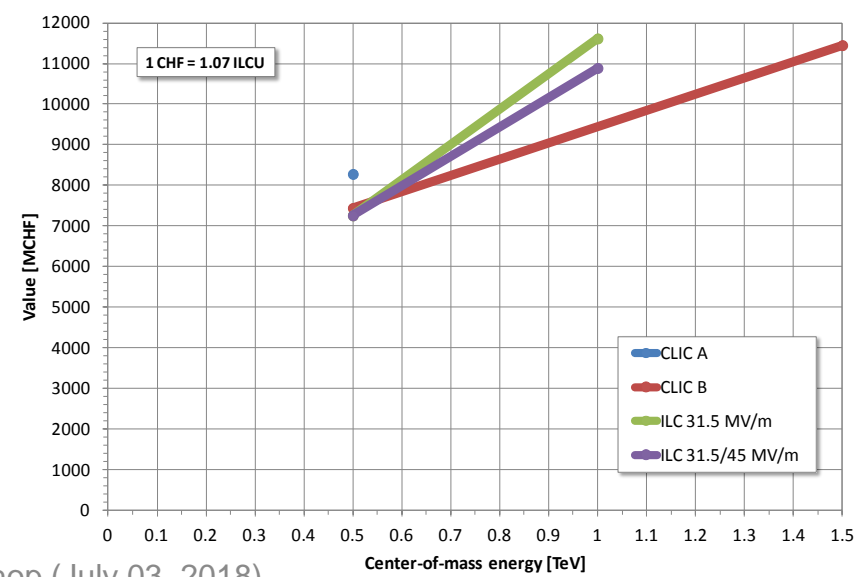
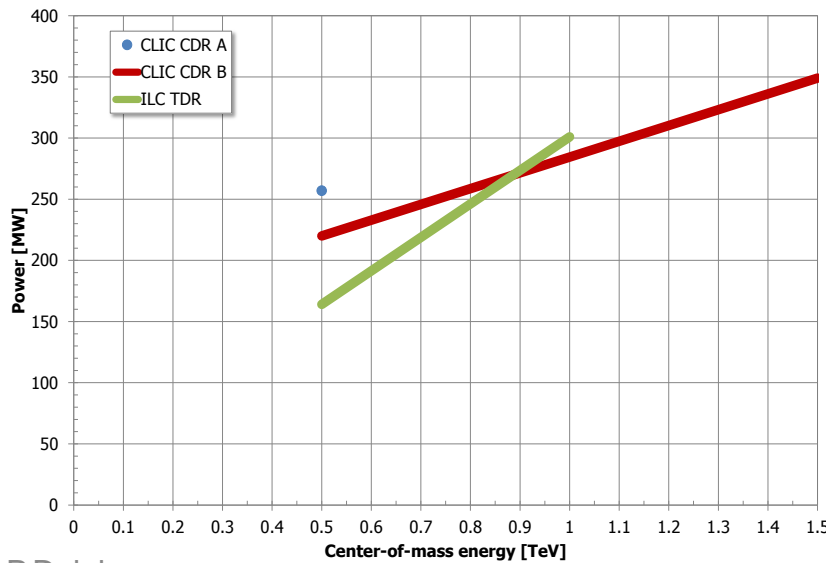
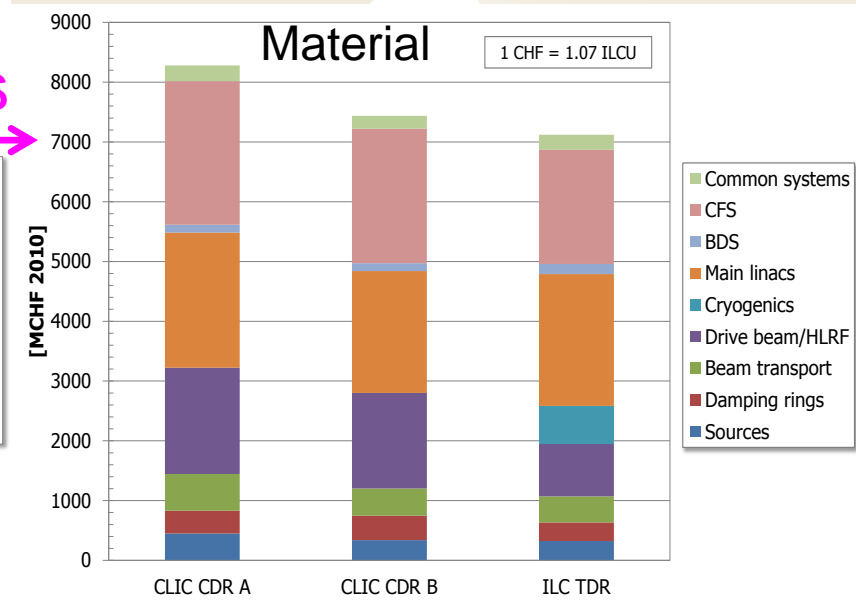
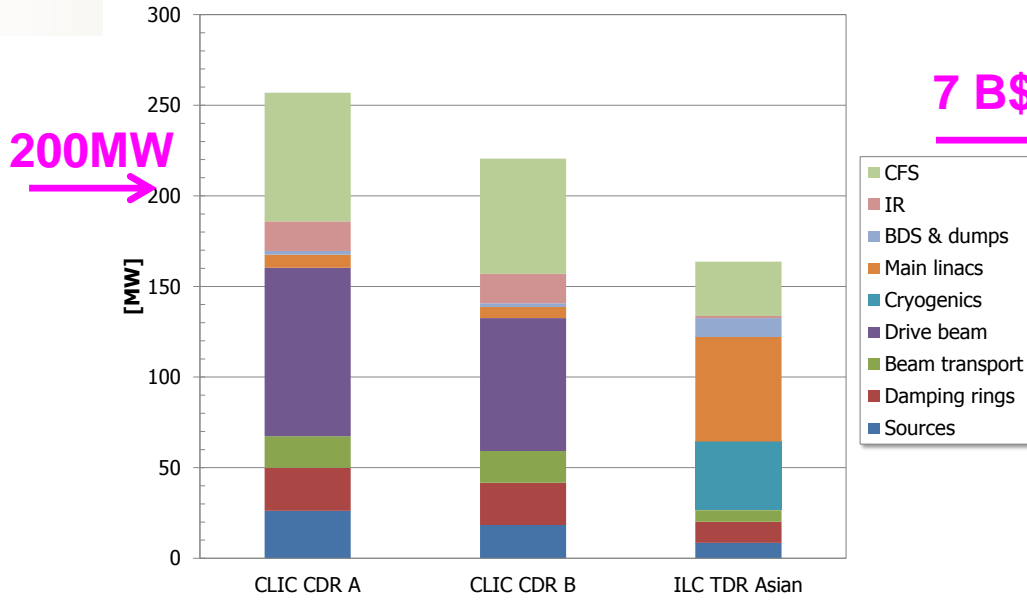
# Lepton & Hadron Colliders Luminosities (elementary constituent c.m.energy)



# Future Facilities limited by Practicalities

## Power

## Cost



# Wall-plug power consumption



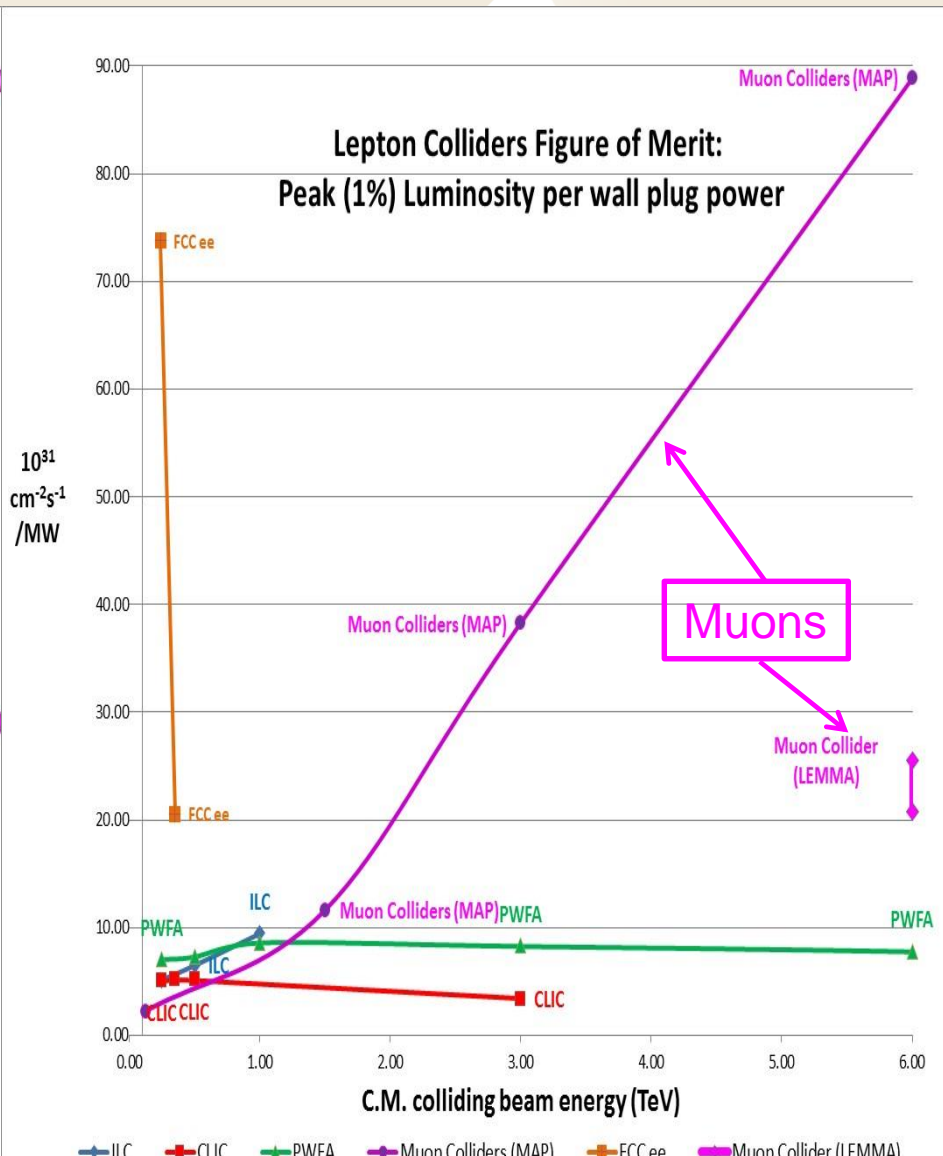
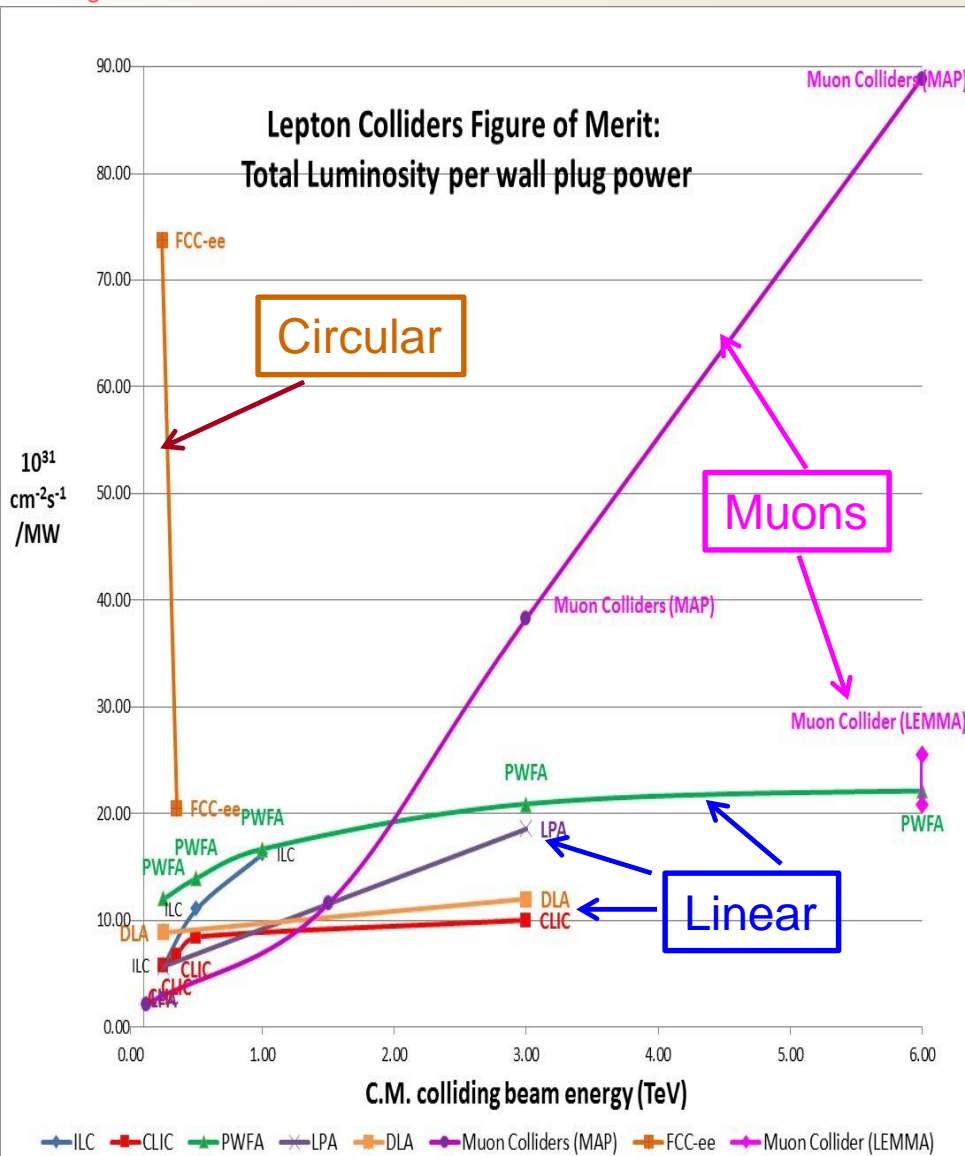
## Wall-plug power consumption function of energy and luminosity

- In linear collider:
- $P \propto L \cdot E + \text{offset (Injectors+conventional facilities)}$

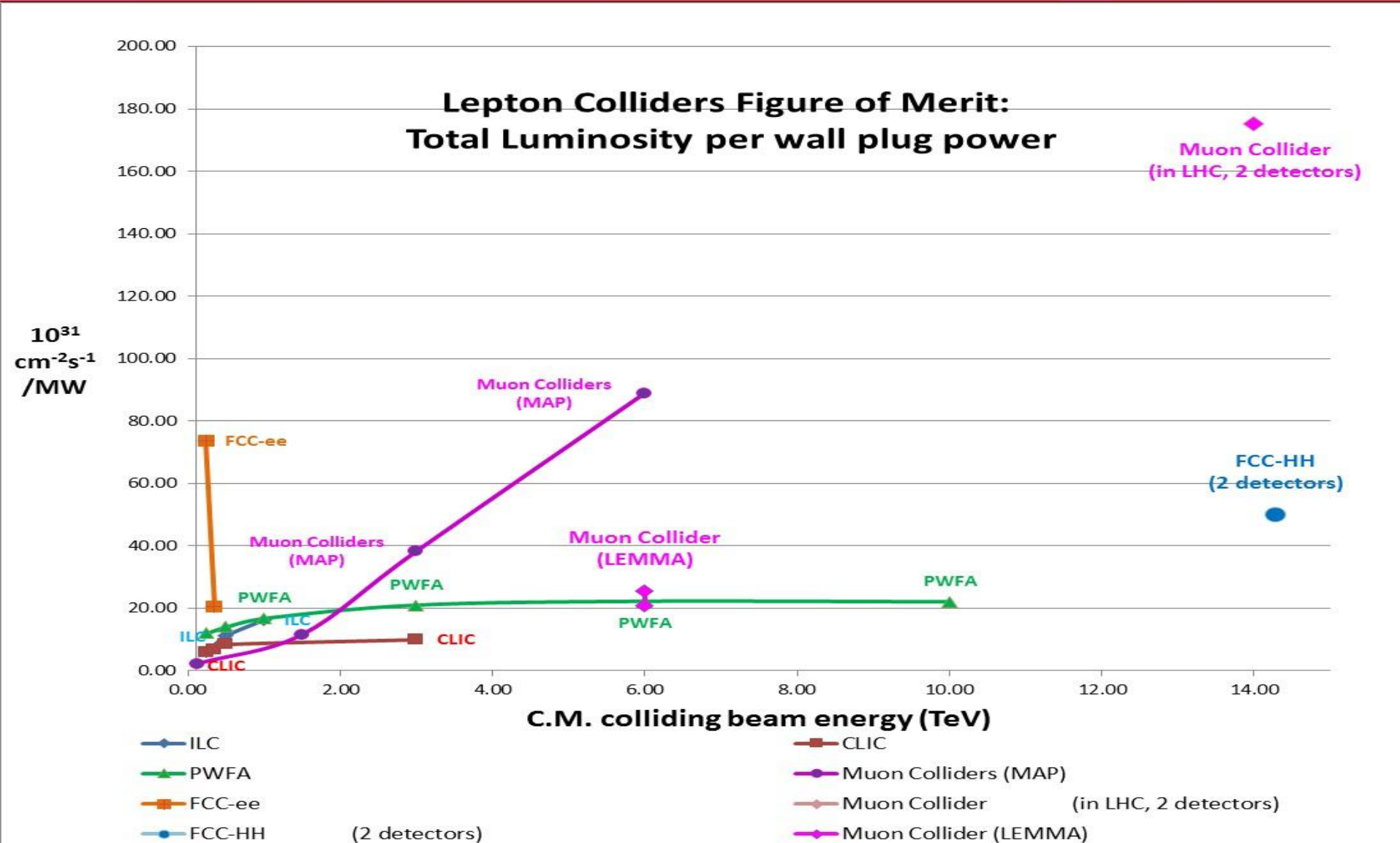
Fair comparison through a Figure of merit (FoM):

$$\text{FoM} = \text{Luminosity} / \text{Wall Plug consumption (L per MW)}$$

# Figure of merit: Luminosity per wall plug power



# Figure of merit: Luminosity per wall plug power



# Phenomenological Cost model (V.Shiltsev)

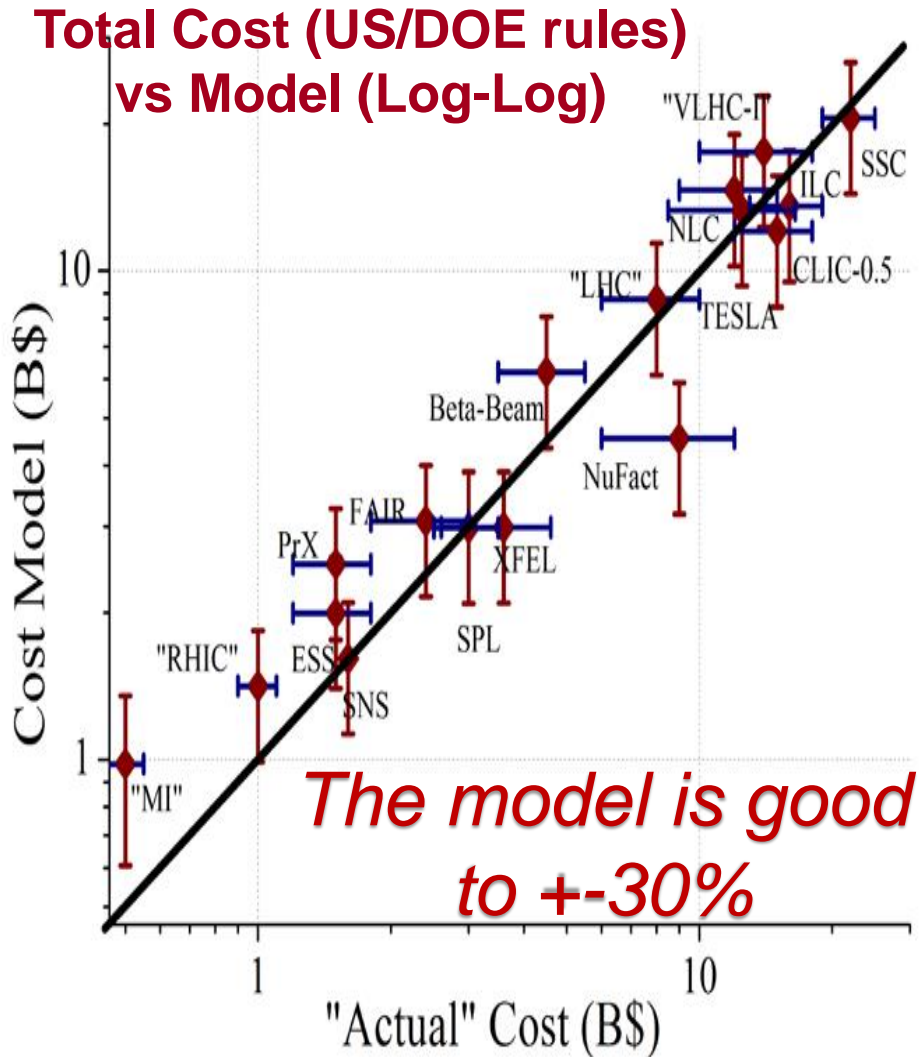
## Conventional Technology

$$\text{Cost} = \alpha L^{1/2} + \beta E^{1/2} + \gamma P^{1/2}$$

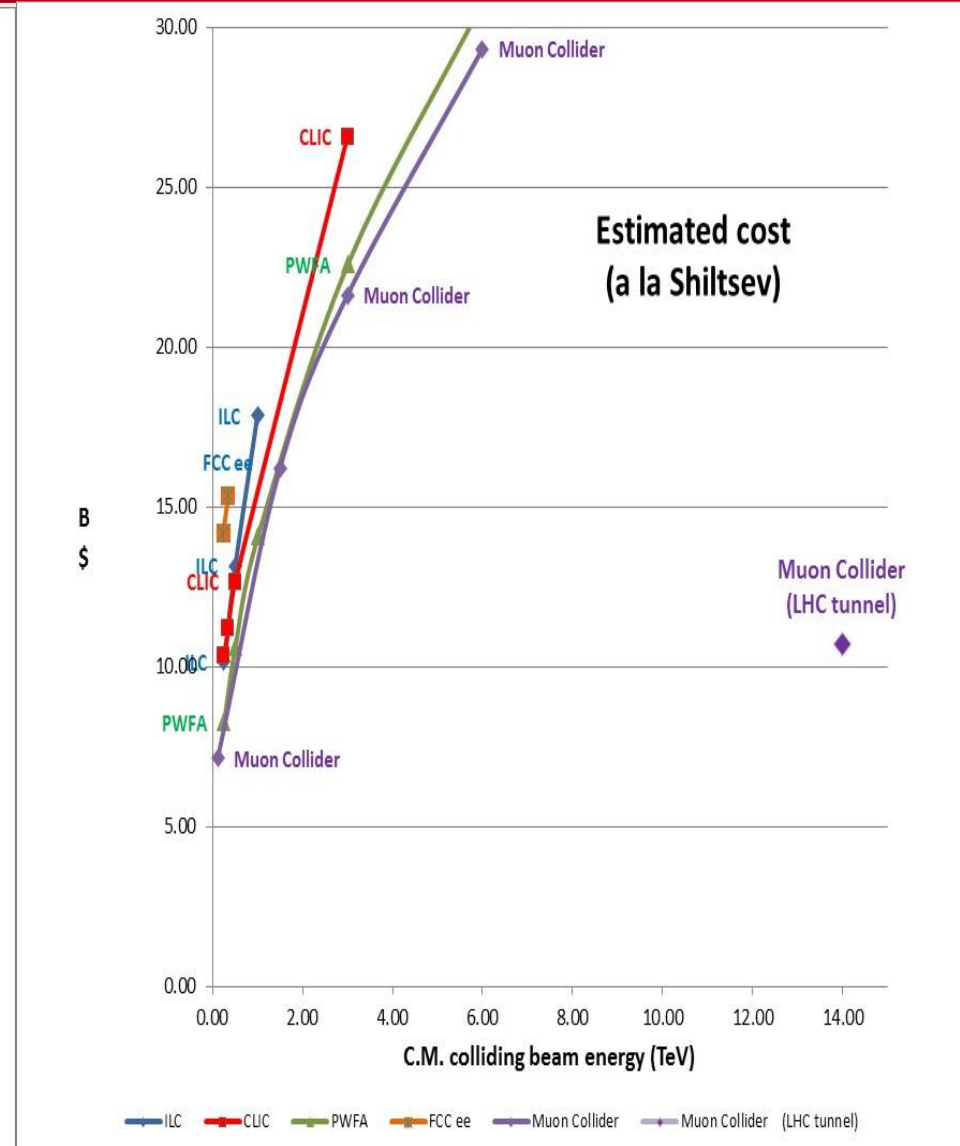
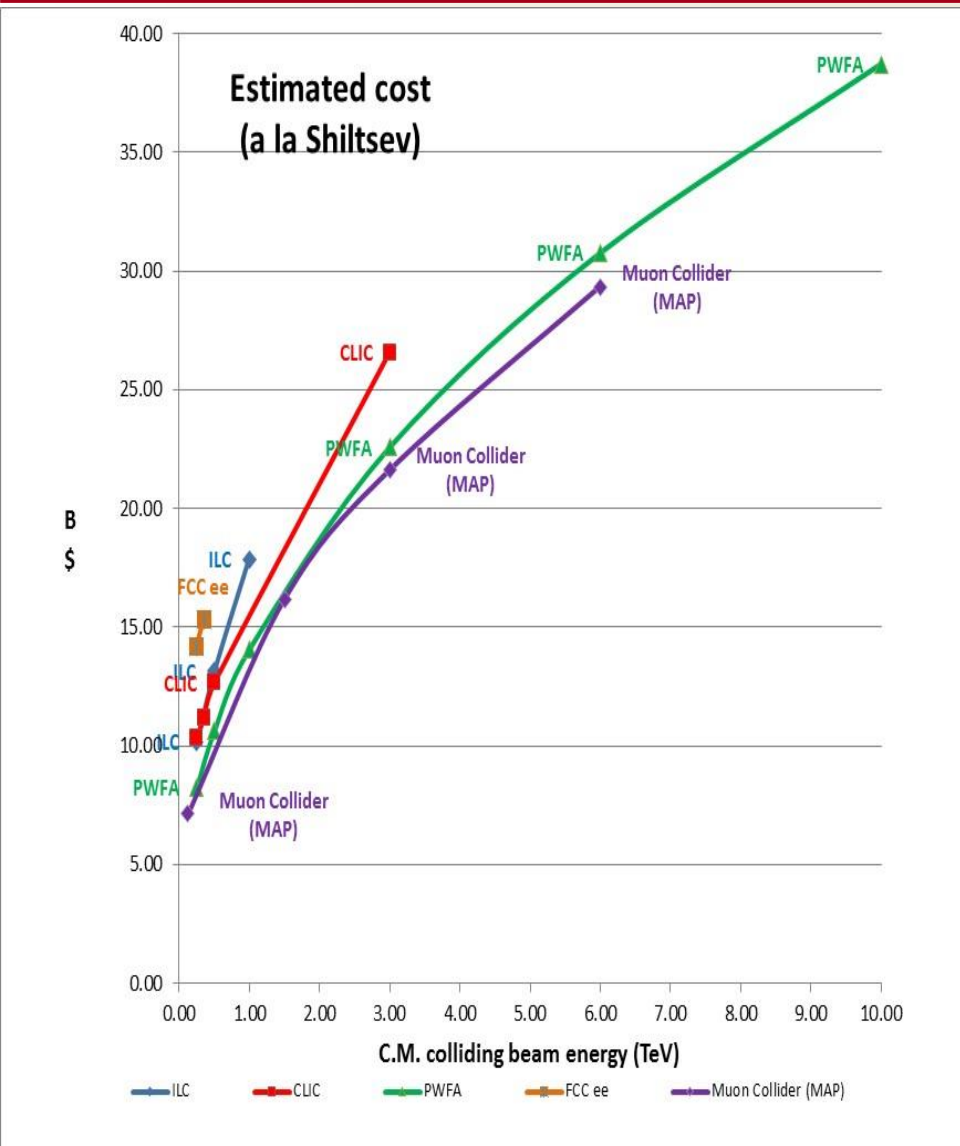
“Total Project Cost”  
 “Tunnel Length” – Civil Construction  
 “Energy” – Cost of Accelerator Components  
 “Site Power” Infrastructure

where  $\alpha, \beta, \gamma$  – technology dependent constants

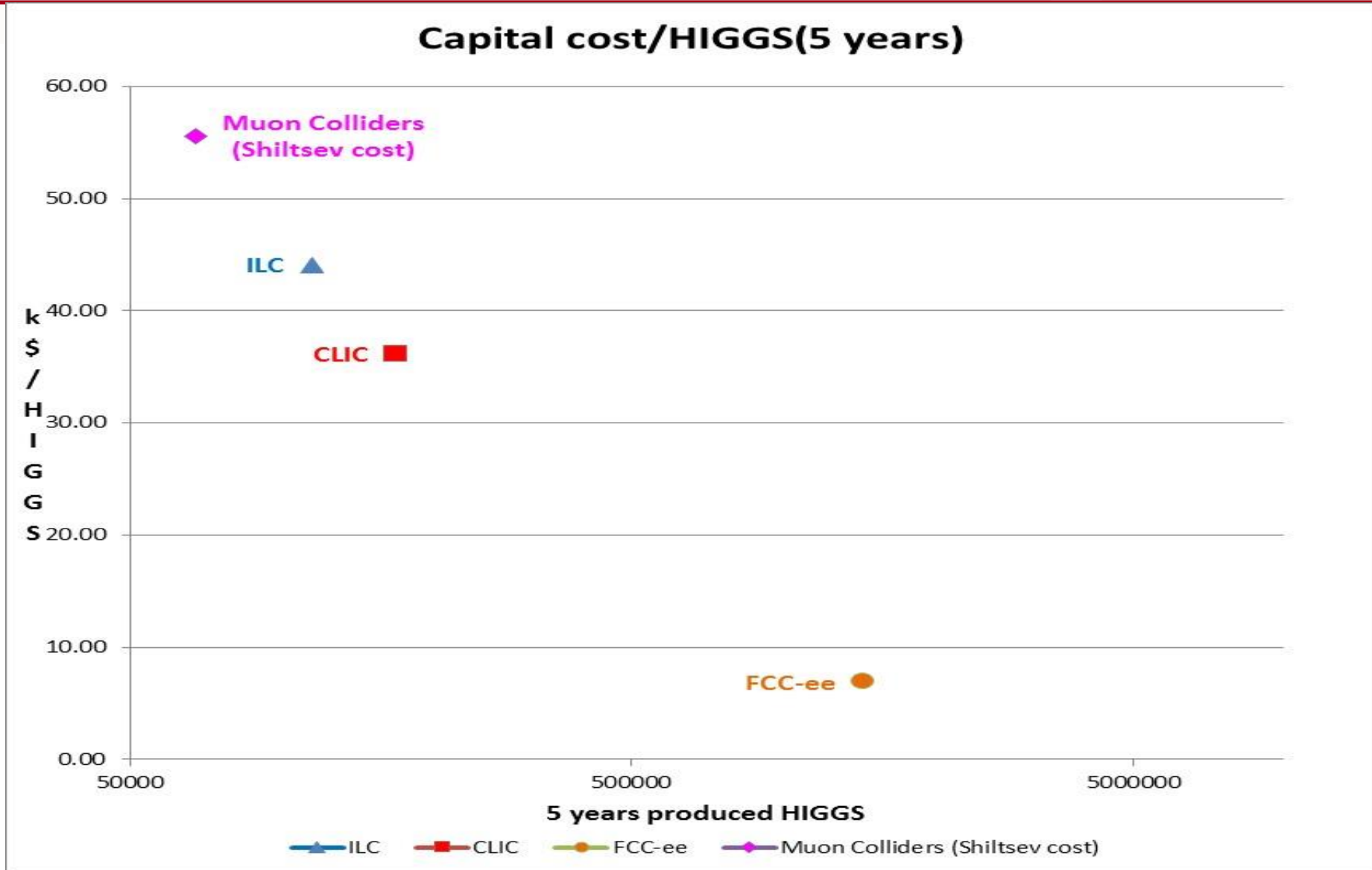
- $\alpha \approx 2\text{B}\$/\text{sqrt}(L/10 \text{ km})$
- $\beta \approx 10\text{B}\$/\text{sqrt}(E/\text{TeV})$  for RF
- $\beta \approx 2\text{B}\$/\text{sqrt}(E/\text{TeV})$  for SC magnets
- $\beta \approx 1\text{B}\$/\text{sqrt}(E/\text{TeV})$  for NC magnets
- $\gamma \approx 2\text{B}\$/\text{sqrt}(P/100 \text{ MW})$



# Estimated cost (a la Shiltsev)

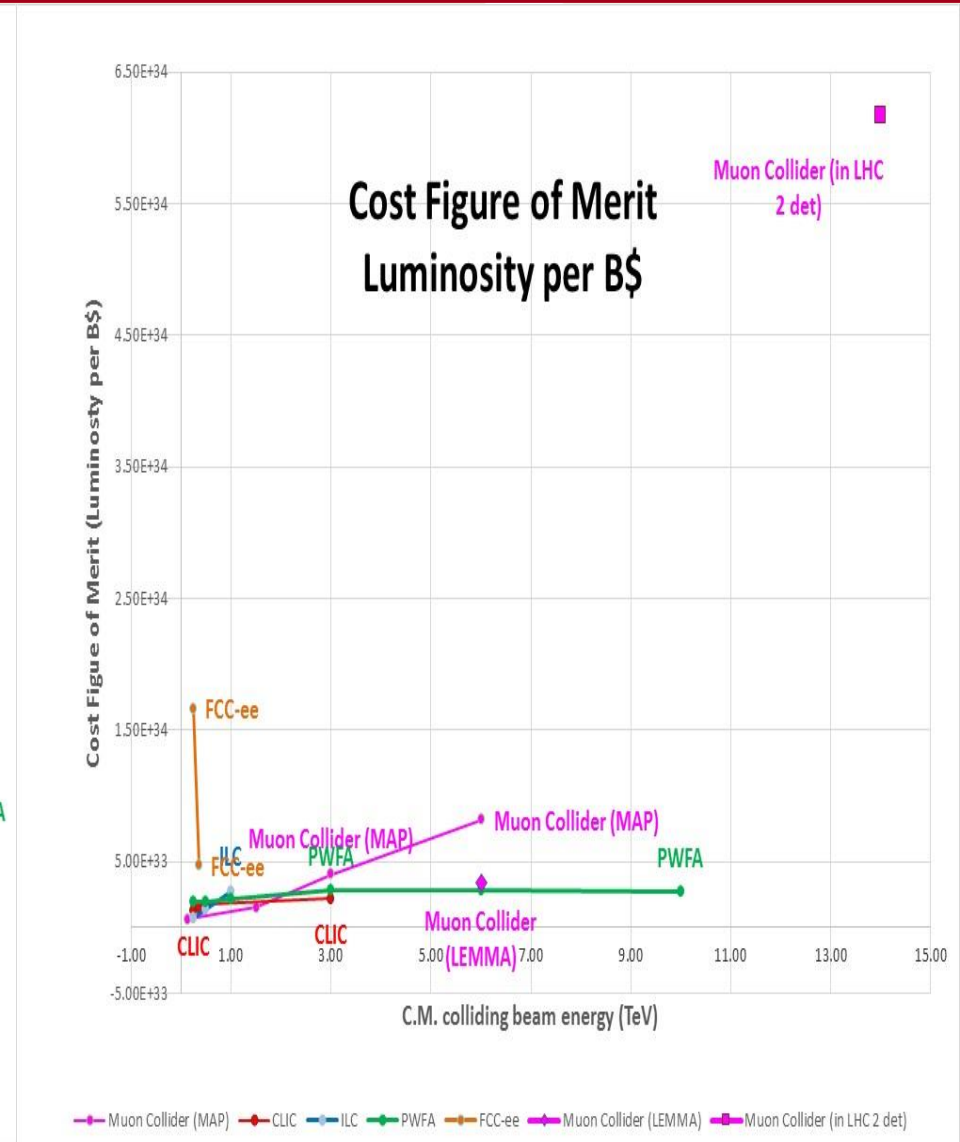
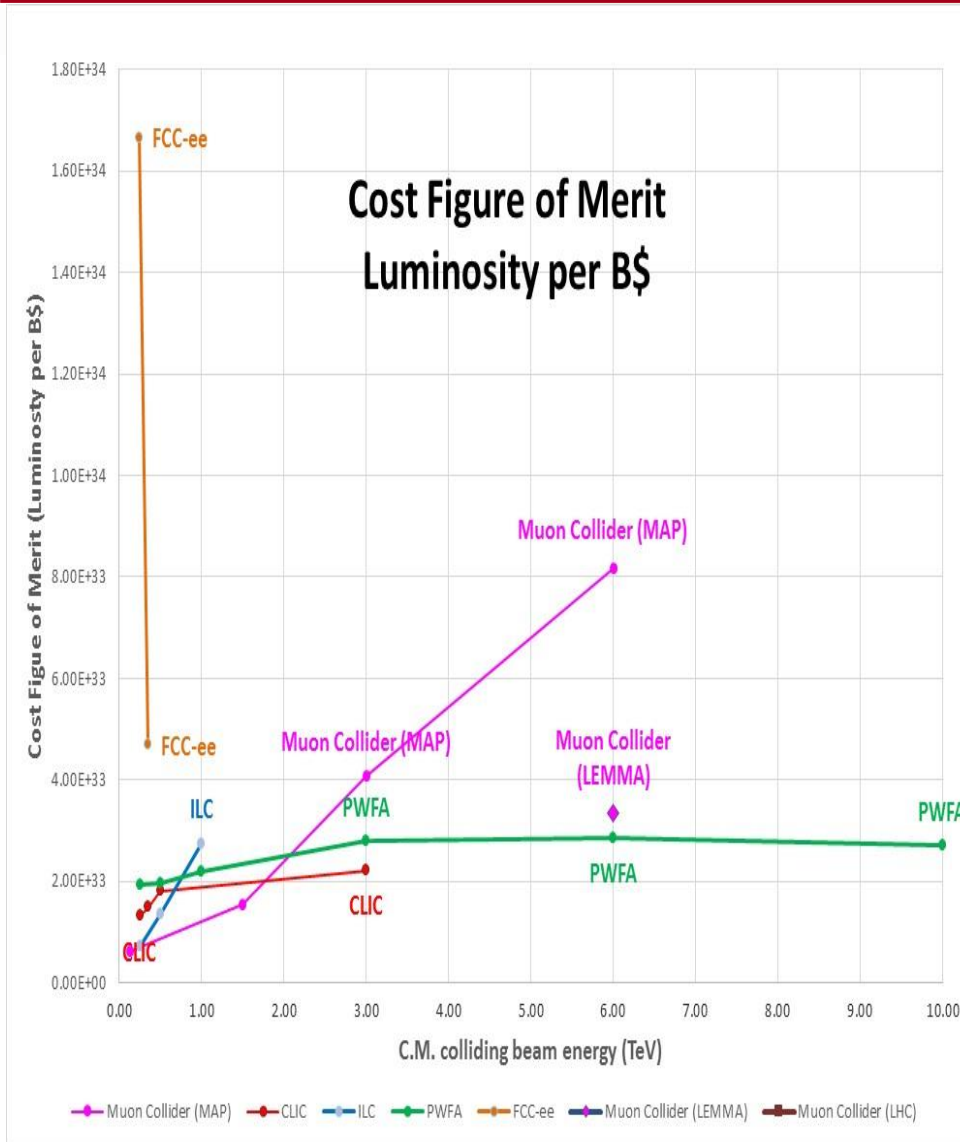


# HIGGS cost

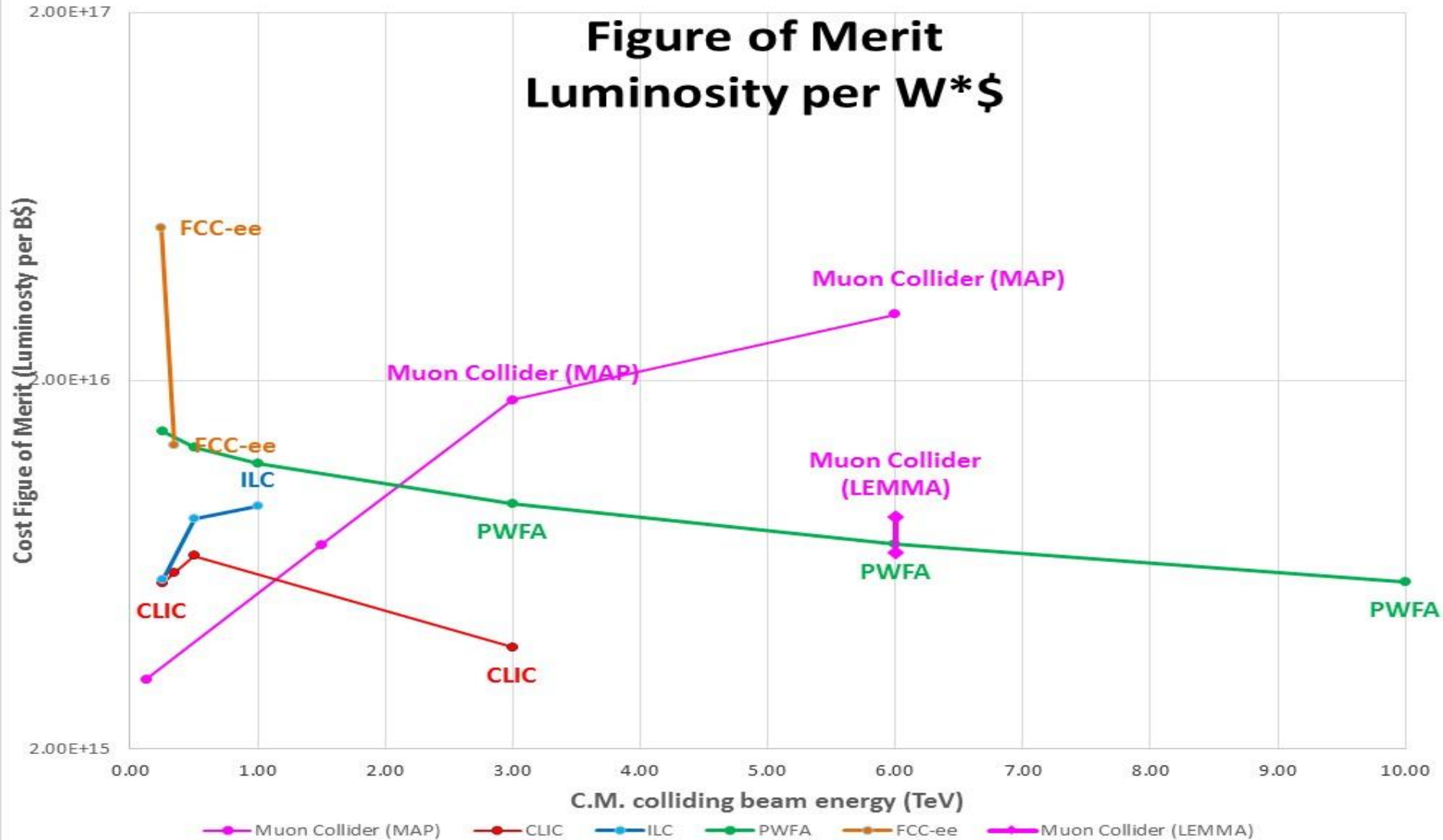




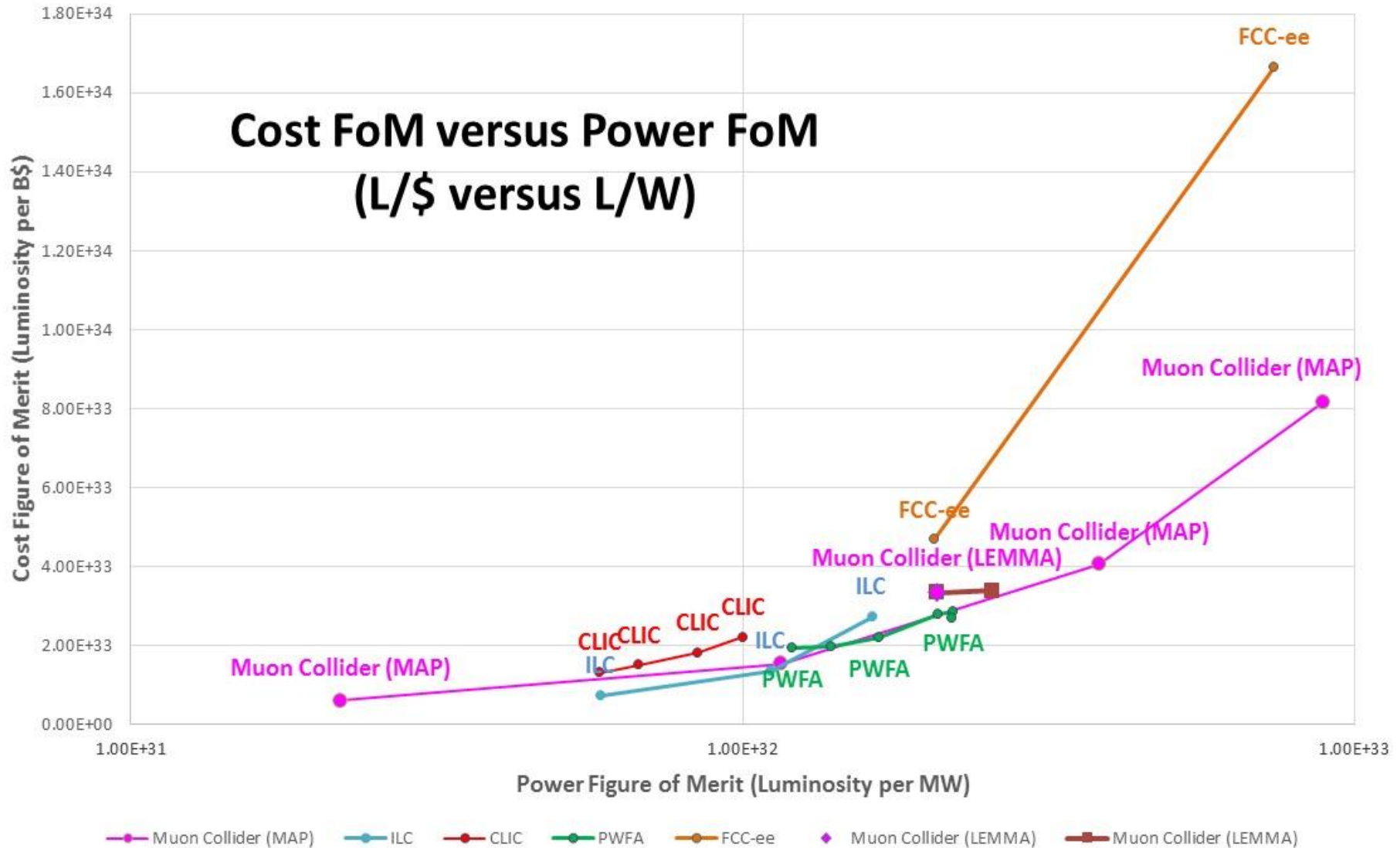
# Cost Figure of merit Luminosity per Billion\$



# Combined Figure of Merit

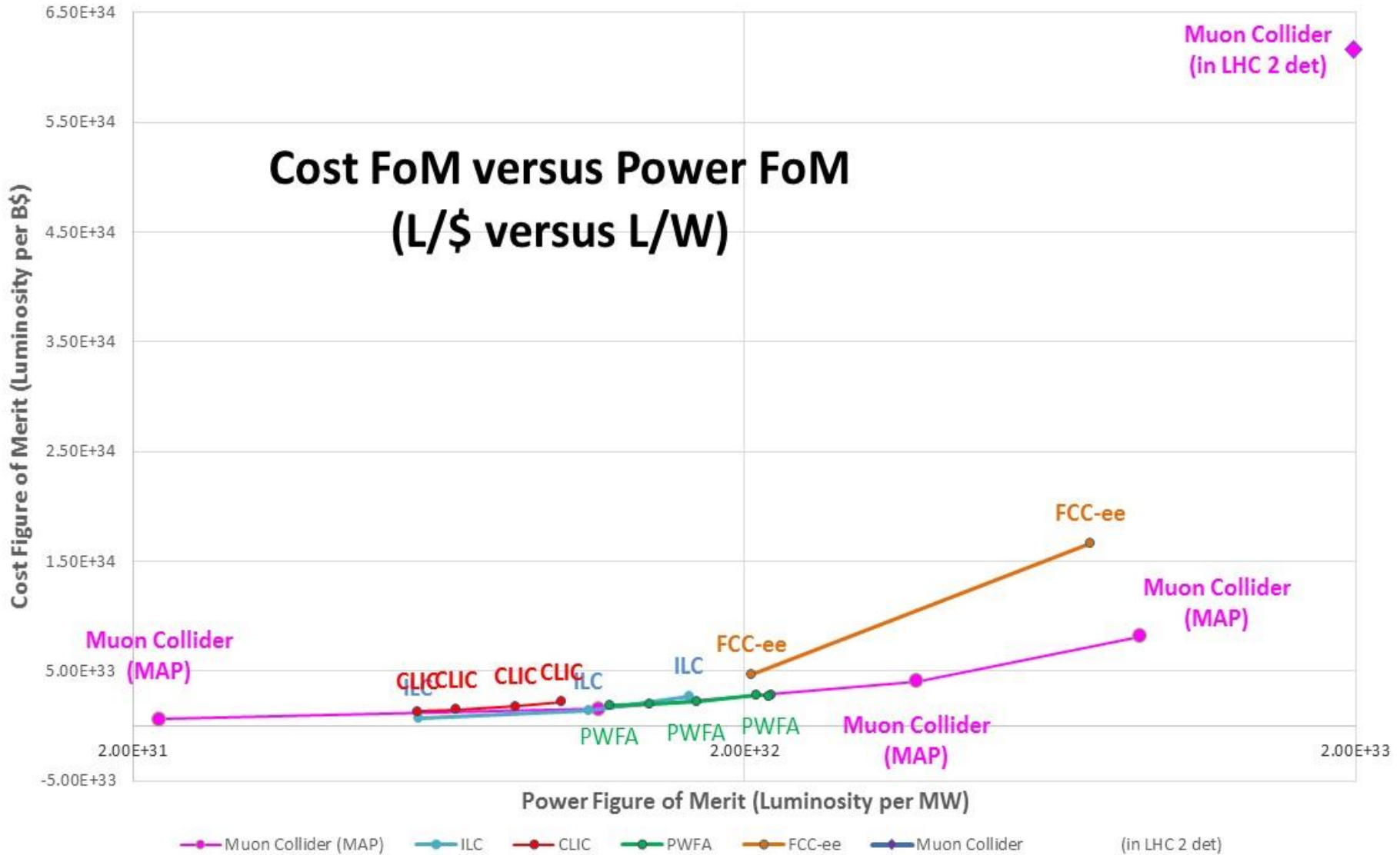
$$\text{FoM} = L / (\text{Power} \times \text{Cost})$$


# Cost Figure of Merit versus Power FoM



# Cost Figure of Merit versus Power FoM

**Cost FoM versus Power FoM  
 (L/\$ versus L/W)**



# Conclusion

**In the HIGGS-TOP energy level, e<sup>+</sup>/e<sup>-</sup> Circular Colliders best suited but large circumference ring and limited in energy upgrade**

**In the TeV range, linear colliders most suited technologies with similar performances and various energy reach**

**Muon Collider (MC) ideal technology to extend lepton colliders in the Multi-TeV range**

- Although challenging and performance limited, MC as HIGGS Factory attractive as a step towards higher colliding beam energies
- MAP scheme pretty mature, relies on critical  $10^6$  6D cooling
- LEMMA scheme appealing (no cooling, energy reach) if feasible (e<sup>+</sup> rate?)

**Impressive potential of Muon Collider in LHC tunnel (preliminary)**

- Taking advantage of existing CERN facilities (LHC tunnel and injectors) to reduce cost
- Excellent Luminosity, Power FoM and Cost FoM but at limit of neutrino radiation
- Energy reach similar to 100TeV FCC-hh at level of elementary constituents
- «Too nice to be true»??? Preliminary study to be confirmed.

**Plea to launch a feasibility study of a  
Muon Collider in the LHC (and FCC?) tunnel**