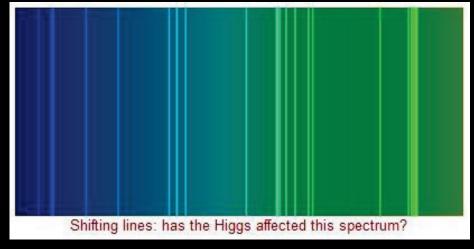
Probing the Atomic Higgs force -and more-



Cédric Delaunay CNRS/LAPTh Yotam Soreq MIT

CD, R. Ozeri, G. Perez, YS
hep-ph: 1601.05087 + in progress

CD, YS hep-ph:1602.04838

C. Frugiuele, E. Fuchs, G. Perez, M. Schlaffer hep-ph:1602.04822



Higgs tasting 20-05-2016 | Benasque

Outline

- 1. The Higgs Mechanism and the Flavor Puzzle
- 2. Higgs Force in Atoms
- 3. Probing Higgs Couplings with Isotope Shift
- 4. The Weak Force

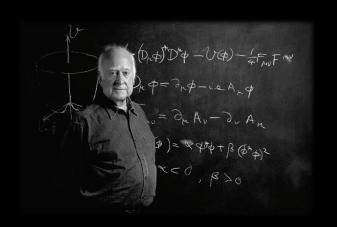
Yotam's talk

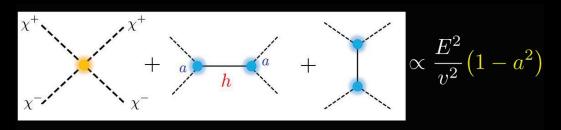
5. New Physics Forces

The Higgs Mechanism and the Flavor Puzzle

The Higgs Mechanism

• breaks EW symmetry: $SU(2)_L \times U(1)_Y \rightarrow U(1)_{QED}$





ATLAS+CMS: $|a-1| \lesssim \mathcal{O}(10\%)$ ATLAS-CONF-2015-044

provides charged fermion masses:

in the SM: $m_f = y_f imes v$

The flavor Puzzle

Charged fermion masses are highly hierarchical:

$$m_t \sim 10^5 m_e$$

• The origin of this hierarchy is unknown, despite a host of precision flavor measurements.

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• Charged fermion masses are highly hierarchical:

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- The origin of this hierarchy is unknown, despite a host of precision flavor measurements.
- Within the SM, it is *assumed* to originate from hierarchical Higgs-to-fermion couplings:

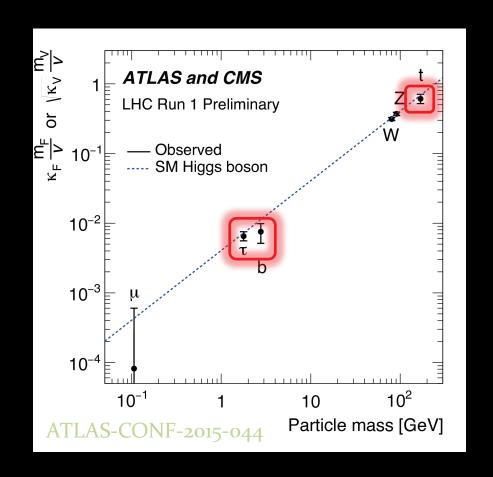
$$y_f^{
m SM} \propto m_f$$

How well can we test?

ATLAS+CMS Higgs-signal/SM:

$\mu^{ au au}$	$1.12^{+0.25}_{-0.23}$
μ^{bb}	$0.69^{+0.29}_{-0.27}$

 μ_{ttH} 2.3^{+0.7}_{-0.6}



→ the Higgs mechanism is likely to be the dominant source of 3rd generation masses

There is an opportunity to probe *c*-coupling directly, thanks to charm-tagging:

in VH production

Perez-Soreq-Stamou-Tobioka '15

in Hc production

Isidori-Goertz'15

Other probes exist:

• $h \to J/\psi \gamma$

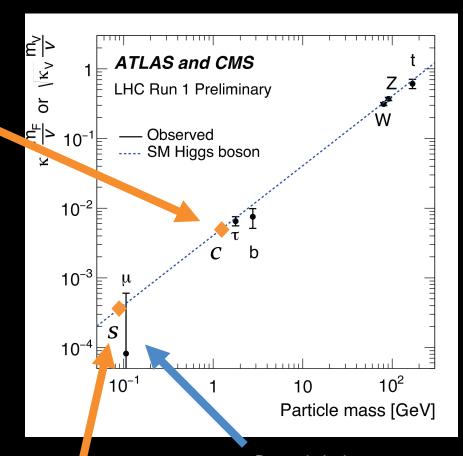
Perez-Soreq-Stamou-Tobioka '15

global fits

CD-Golling-Perez-Soreq '13

• $\Gamma_h \leq 1.7 \,\mathrm{GeV}$

Perez-Soreq-Stamou-Tobioka '15

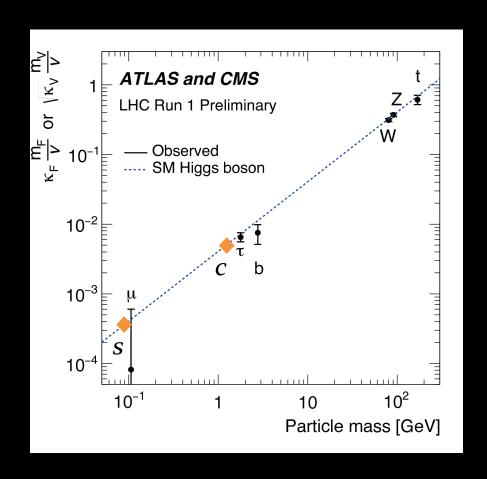


 $h \to \phi \gamma$?

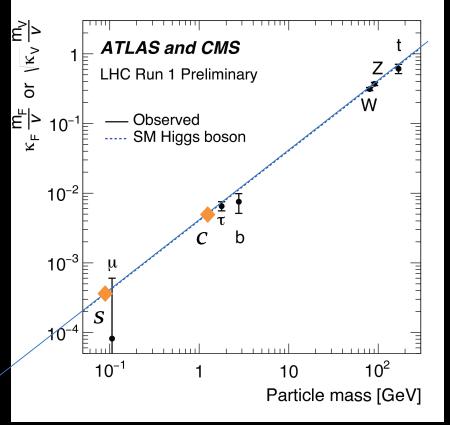
Kagan et al. '14

Sensitivity to muon-coupling, with high-enough luminosity
ATL-PHYS-PUB-2014-016

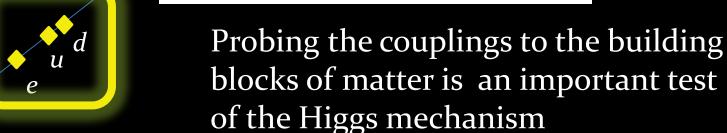
What about *e,u,d*?

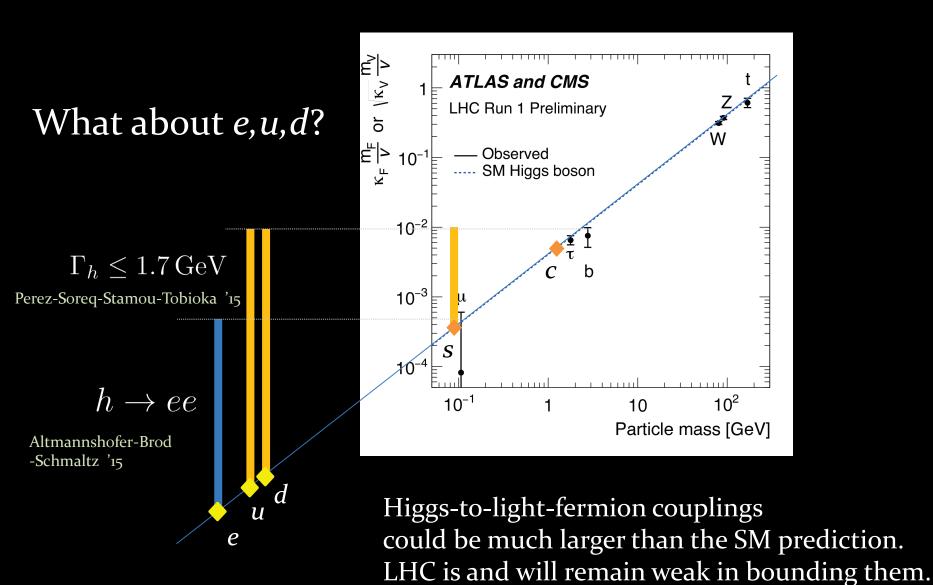


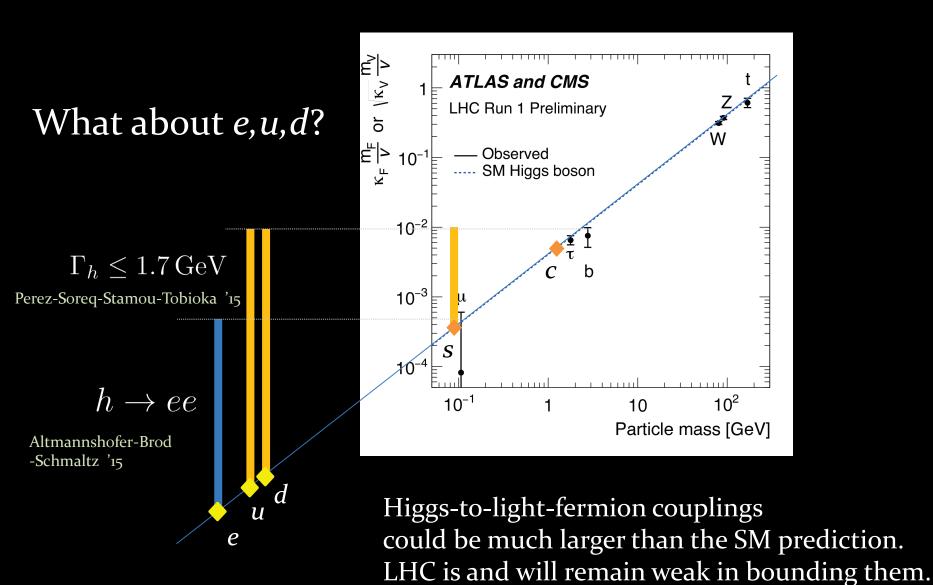
What about *e,u,d*?



[stable nuclei] [chemistry]







The atomic Higgs force

The Atomic Higgs Force

• The Higgs results in an attractive force between nuclei and their bound electrons (à la Yukawa):

$$V_{\text{Higgs}}(r) = -\frac{y_e y_A}{4\pi} \frac{e^{-m_h r}}{r} \approx -\frac{y_e y_A}{4\pi m_h^2} \frac{\delta(r)}{r^2}$$

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• $y_A=Zy_p+(A-Z)y_n$ with: Shifman-Vainshtein-Zakharov '78 + nuclear data, see *e.g.* micrOmegas

$$y_n \approx 7.7 y_u + 9.4 y_d + 0.75 y_s + 2.6 \times 10^{-4} c_g$$
 $y_p \approx 11 y_u + 6.5 y_d + 0.75 y_s + 2.6 \times 10^{-4} c_g$ in matching

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 Uncertainties $y_p \approx 11y_u + 6.5y_d + 0.75y_s + 2.6 \times 10^{-4}c_g$ in matching

• c_q constrained by LHC, weaker sensitivity to s-coupling

Higgs Force Strength

• Under current LHC constraints:

```
Higgs width (direct) y_{n,p} \lesssim 3 \; (0.2) \qquad \text{and} \qquad y_e \lesssim 1.3 \times 10^{-3} global fit (indirect)
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- Higgs force possibly stronger than SM by $\sim 10^6$!
- This shifts transition frequencies by: electron-density at the nucleus

$$\Delta \nu_{nS \to n'D,F}^{\text{Higgs}} \approx 1 \,\text{Hz} \times A \frac{y_e y_{n,p}}{0.004} \frac{|\psi(0)|^2}{4n^3 a_0^{-3}}$$

Bohr radius $(\alpha m_r)^{-1}$

Optical Atomic Clock Transitions

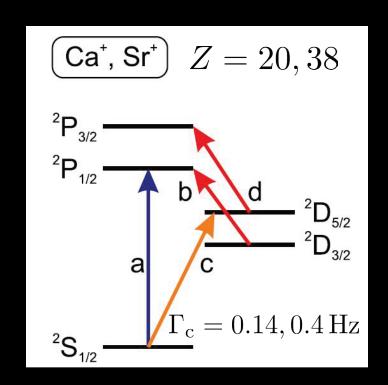
Optical Atomic Clocks

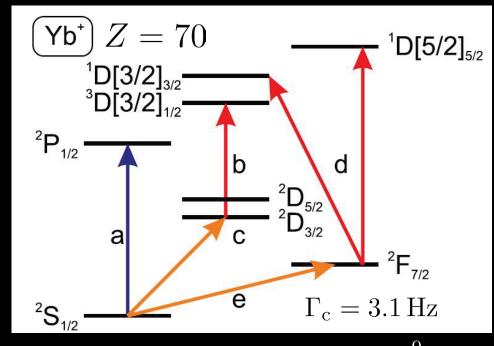
• State-of-the-art accuracy at the 10^{-18} level

Optical Atomic Clocks

- State-of-the-art accuracy at the 10^{-18} level
- Narrow transitions with S-wave are needed:

Ludlow-Boyd-Ye, Rev. Mod. Phys. 87 (2015)





$$\Gamma_e = 10^{-9} \, \mathrm{Hz}$$

Frequency Comparisons

• Experimental accuracy in $^{40}\mathrm{Ca}^+$, $^{88}\mathrm{Sr}^+$ is $\sim \mathrm{Hz}$

Dube et al., Phys. Rev. A87 (2013) Chwalla et al., PRL 102 (2009)

$$\nu_{E2}^{\text{Ca}^{+}} = 411\ 042\ 129\ 776\ 393.2(1.0)\text{Hz}$$

$$\nu_{E2}^{\text{Sr}^{+}} = 444\ 779\ 044\ 095\ 485.5(9)\text{Hz}$$
 $\sim 10^{15}\text{Hz}$

sensitivity to the Higgs force

$$y_e y_n \lesssim 4 \times 10^{-5} \sim LHC8/100$$

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 $y_{e}y_{n} \lesssim 4 \times 10^{-5} \sim \mathrm{LHC8/100}$

• Theory side is however much less promissing: electron-electron correlations, nuclear finite-size, relativistic corrections, QED...

are not accounted for at the 10^{-15} level...

Isotope Shifts and King plots

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• The Higgs force can't be switched on and off. Instead, let's try to cancel the « background ».

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• The Higgs force however scales like the nuclear mass A, so there is still a net shift between isotopes!

- There are yet non-trivial IS from changes in:
 - the reduced mass: $m_r = \frac{m_e m_A}{m_e + m_A} \simeq m_e (1 m_e/m_A)$
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$$\delta \nu_{AA'}^i = K_i \mu_{AA'} + F_i \delta \langle r^2 \rangle_{AA'} + H_i (A - A')$$

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 mass shift field shift Higgs shift

MS/FS effects are typically in the GHz range ≫ HS

The King Plot

W. H. King, J. Opt. Soc. Am. 53, 638 (1963)

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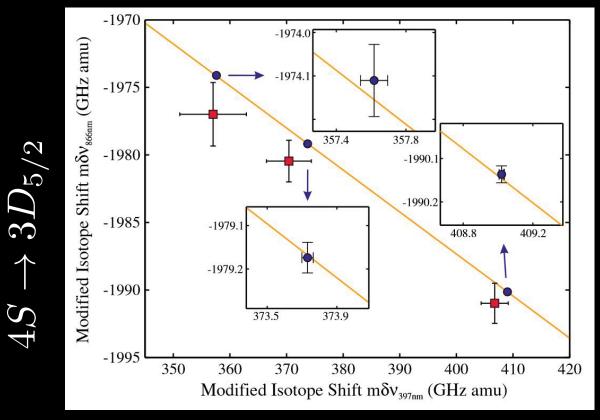
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• Plot $m\delta\nu_{AA'}^1$ vs. $m\delta\nu_{AA'}^2$ along the isotopic chain and as long as linearity is observed, H_{21} can be bounded (unless accidentally $m\delta\nu\propto A'$)

Proof of Concept in Ca⁺

Gebert et al. PRL 115 (2015)

$$A = 40, A' = 42, 44, 48$$



IS ~ 1 GHz error ~ 100 kHz



 $y_e y_n \lesssim 40$

 $4S o 4P_{1/2}$ (not-clock)

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Huntemann et al. PRL 113 (2014) Godun et al. PRL 113 (2014)

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This is ~10 times better than (comparable to)
 LHC8 direct (indirect) bounds, with good/better
 prospect for improvements!

probing new physics with isotope shift spectroscopy

PROBING GENERIC NEW PHYSICS

isotope shits including non QED or QCD

$$\delta \nu_{AA'}^i = K_i \mu_{AA'} + F_i \delta \langle r^2 \rangle_{AA'} + X_{AA'}^i$$

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- Higgs exchange (scalar operators)
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Ytterbium (Yb+) - as a test case

capture new physics by

$$\mathcal{L}_{\text{NP}} = \frac{1}{\Lambda^2} \left[\sum_{q} c_{eq}^S \mathcal{O}_{eq}^S + c_{eq}^V \mathcal{O}_{eq}^V \right] + \frac{c_{eg}}{\Lambda^3} \mathcal{O}_{eg}$$

$$\mathcal{O}_{eq}^{S} = (\bar{e}e)(\bar{q}q) \qquad \mathcal{O}_{eq}^{V} = (\bar{e}\gamma_{\mu}e)(\bar{q}\gamma^{\mu}q) \qquad \mathcal{O}_{eg} = \alpha_{s}(\bar{e}e)G_{\mu\nu}^{a}G^{\mu\nu\,a}$$

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$$X_{AA'}^{i}|_{\text{EFT}} = 4 \text{ Hz} \times y_{en} (A - A') \frac{|\psi(0)|^2}{4a_0^{-3}} \left(\frac{\text{TeV}}{\Lambda}\right)^2$$

 $y_{en} \approx 8.8 c_{eu}^S + 11 c_{ed}^S + 0.86 c_{es}^S - 2.4 \times 10^{-3} c_{eq}$

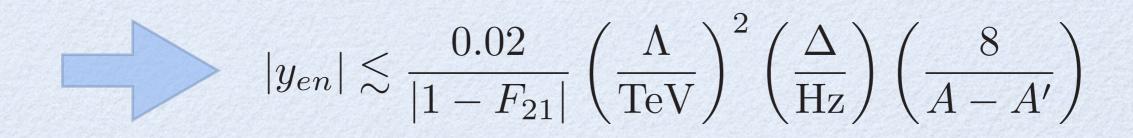
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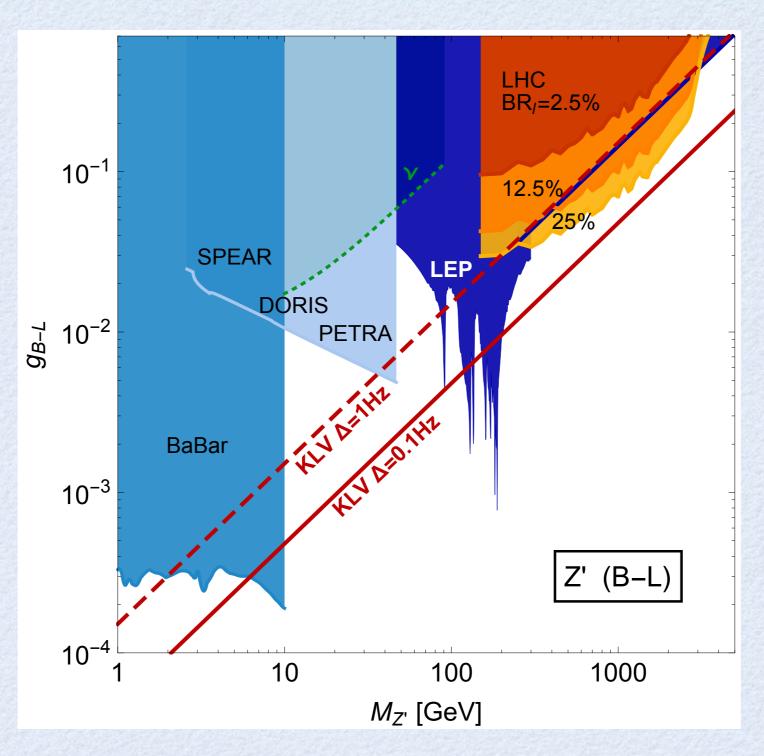
operator	Upper bound on $ c_i $	Lower bound on Λ_i [TeV]
\mathcal{O}_i	$(\Lambda = 1 { m TeV})$	(c=1)
\mathcal{O}_{eu}^{V}	2.3×10^{-2}	6.6
\mathcal{O}_{ed}^{V}	1.1×10^{-2}	9.3
\mathcal{O}_{eu}^{S}	2.6×10^{-3}	20
\mathcal{O}_{ed}^{S}	2.1×10^{-3}	22
\mathcal{O}_{es}^{S}	2.7×10^{-2}	6.1
\mathcal{O}_{ec}^{S}	0.20	2.3
\mathcal{O}_{eb}^{S}	0.87	1.1
\mathcal{O}_{et}^{S}	56	0.13
\mathcal{O}_{eg}	9.6	0.47

~ LHC8, ×2 LEP2

×10 LEP2

$$\mathcal{L}_{\text{NP}} = \frac{1}{\Lambda^2} \left[\sum_{q} c_{eq}^S \mathcal{O}_{eq}^S + c_{eq}^V \mathcal{O}_{eq}^V \right] + \frac{c_{eg}}{\Lambda^3} \mathcal{O}_{eg}$$

Z'BENCHMARK MODEL



PROBING THE Z COUPLINGS

the effect of Z^0 on isotope shift:

$$X_{AA'}^{i}|_{\text{weak}} = -1.3 \,\text{Hz} \times q_W (A - A') \frac{|\psi(0)|^2}{4a_0^{-3}}$$

neutron nuclear weak charge (SM=-1)

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neutron nuclear weak charge (SM=-1)

deviation from the SM can be constrained

$$|\delta q_W| \lesssim \frac{7.4 \times 10^{-2}}{|1 - F_{21}|} \left(\frac{\Delta}{\text{Hz}}\right) \left(\frac{8}{A - A'}\right)$$
 or $|\delta g_u + 2\delta g_d| \lesssim 1.8 \times 10^{-2}$

stronger than model independent bounds, but weaker than atomic parity violation

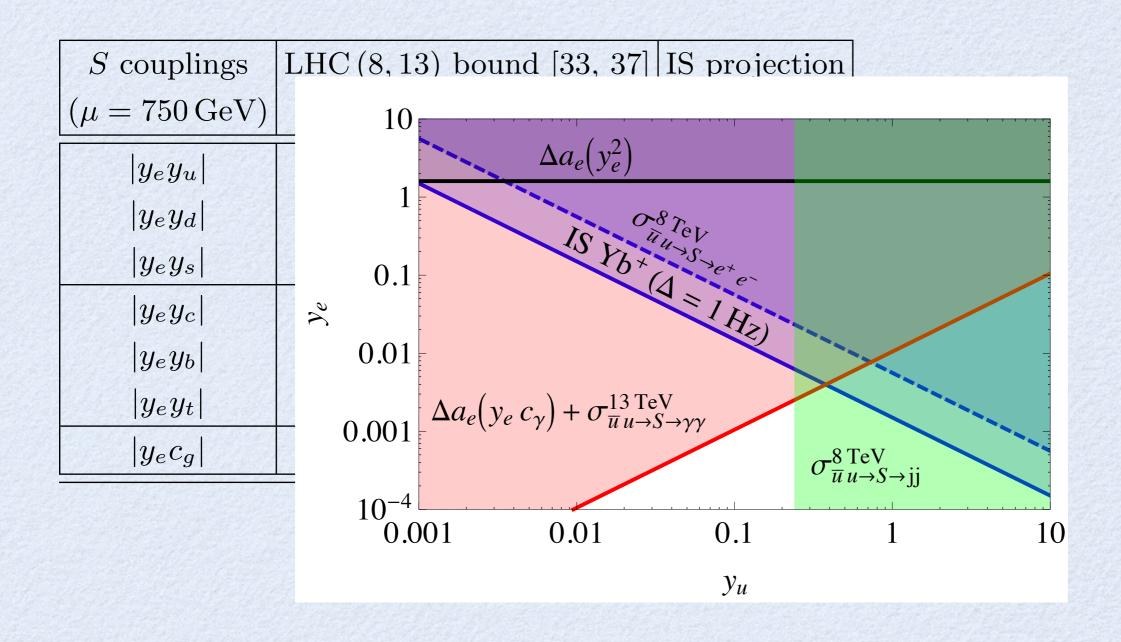
ON POSSBILE 750GEV RESONANCE

from LHC: coupled to hadrons

S couplings	LHC (8, 13) bound [33, 37]	IS projection
$(\mu = 750 \mathrm{GeV})$	$(\Gamma_S = 45 \mathrm{GeV})$	$(\Delta = 1 \mathrm{Hz})$
$ y_e y_u $	$(5.6, 6.0) \times 10^{-3}$	1.5×10^{-3}
$ y_e y_d $	$(7.3, 7.8) \times 10^{-3}$	1.2×10^{-3}
$ y_e y_s $	$(2.9, 2.5) \times 10^{-2}$	1.5×10^{-2}
$ y_ey_c $	$(3.6, 3.0) \times 10^{-2}$	9.6×10^{-2}
$ y_e y_b $	$(5.6, 4.5) \times 10^{-2}$	0.49
$ y_e y_t $	(0.19, 0.16)	32
$ y_e c_g $	(0.72, 0.60)	150

ON POSSBILE 750GEV RESONANCE

from LHC: coupled to hadrons



LIGHT NEW PHYSICS

the EFT breaks

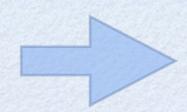


long range interaction

$$V_{\text{light}}(r) = (-1)^{s+1} \alpha_{\phi} N_e N_A \frac{e^{-m_{\phi}r}}{r}$$

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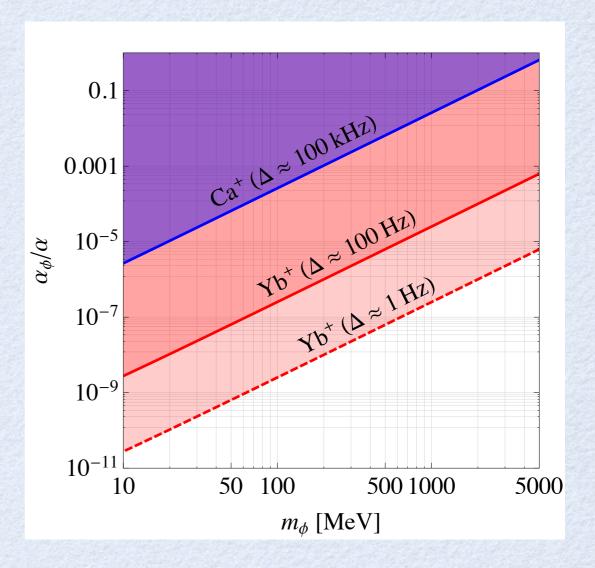
long range interaction

$$V_{\text{light}}(r) = (-1)^{s+1} \alpha_{\phi} N_e N_A \frac{e^{-m_{\phi}r}}{r}$$

$$\psi(r \lesssim a_0/Z) \simeq \psi(0)e^{-Zr/a_0}$$

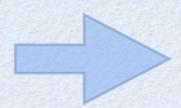
$$X_{AA'}^{i}|_{\text{light}} \simeq 5 \times 10^{7} \,\text{Hz} \times (-1)^{s} \alpha_{\phi} N_{e} (N_{A} - N_{A'})$$

$$\times \frac{|\psi(0)|^{2}}{4a_{0}^{-3}} \left(\frac{\text{GeV}}{m_{\phi} + 2Za_{0}^{-1}}\right)^{2}. \tag{18}$$



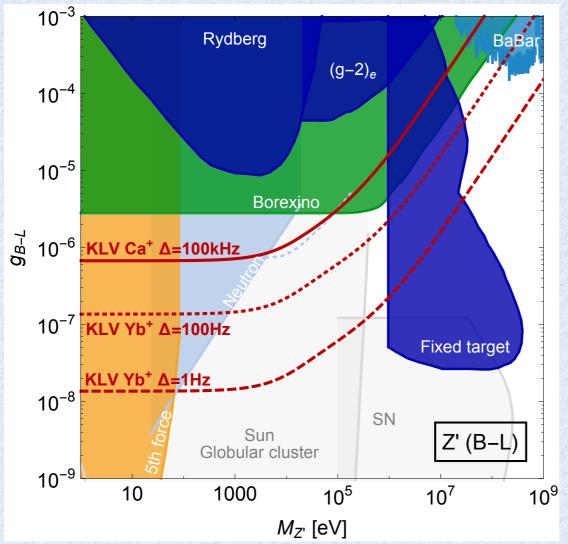
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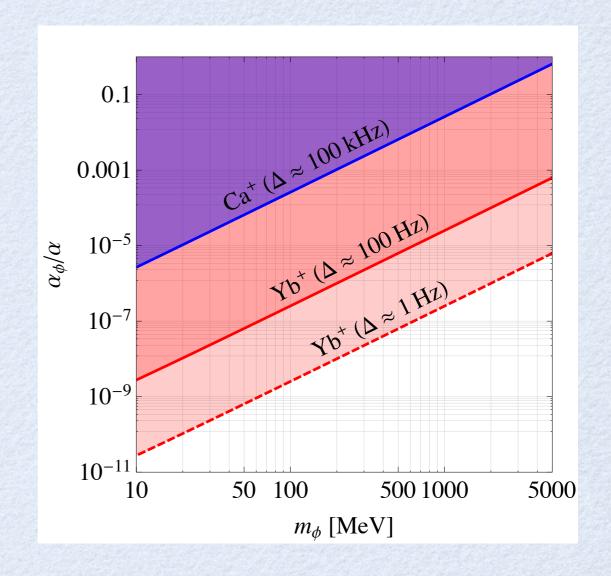


long range interaction

$$V_{\text{light}}(r) = (-1)^{s+1} \alpha_{\phi} N_e N_A \frac{e^{-m_{\phi}r}}{r}$$



C. Delanunay, C. Frugiele, E. Fuchs, C. Grojean, R. Harnik, G. Perez, R. Ozeri, Y. Soreq - Work in progress



SUMMARY

- the atomic Higgs force can be probed by the state-of-theart isotope shift measurements, and may shed light on the flavor puzzle
- isotope shift can also probe
 - the Z⁰ couplings
 - generic new physics, which is not aligned with QED
- not only Yb+, can consider also Ca/Ca+, Sr/Sr+, Dy

BACKUP SLIDES

isotope shift can be written as

$$\delta \nu_i^{AA'} \equiv \nu_i^A - \nu_i^{A'} = K_i \mu_{AA'} + F_i \delta \langle r^2 \rangle_{AA'}$$

depends on the transition-i:

 K_i - mass shift

 F_i - field shift

nucleus parameters:

$$\mu_{AA'} = 1/m_A - 1/m_{A'}$$
$$\delta \langle r^2 \rangle_{AA'} = \langle r^2 \rangle_A - \langle r^2 \rangle_{A'}$$

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need to control isotope shit to the level of nucleus parameters:

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$$\delta \langle r^2 \rangle_{AA'} = \langle r^2 \rangle_A - \langle r^2 \rangle_{A'}$$

$$\frac{\text{Higgs Shift}}{\text{total IS}} \sim \frac{\text{Hz}}{\text{GHz}} \sim 10^{-9}$$

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$$\frac{\text{Higgs Shift}}{\text{total IS}} \sim \frac{\text{Hz}}{\text{GHz}} \sim 10^{-9}$$

isotope shift are controlled by two small parameters

$$\varepsilon_{\mu} = m_e \mu_{AA'} \sim (A - A') \times 10^{-8}$$
$$\varepsilon_r = \delta \langle r^2 \rangle_{AA'} / a_0^2 \sim (A - A') \times 10^{-11}$$

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Field Shift NDA

LO:
$$|\psi(0)|^2 \delta \langle r^2 \rangle_{AA'} \sim \varepsilon_r$$

NLO/LO :
$$\mathcal{O}(\varepsilon_r^2, \varepsilon_\mu^2, \varepsilon_r \varepsilon_\mu)/\varepsilon_r \sim 10^{-7}$$

BUT NLO is linear up to overlap - extra suppression of ε_r

non linear effect in the King plot $(\epsilon_r)^2 \sim 10^{-14}$

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Mass Shift NDA

LO : $m_e \mu_{AA'} \sim \mathcal{O}(\varepsilon_{\mu})$

NLO: $\sim \alpha^2 m_e^2 (1/m_A^2 - 1/m_{A'}^2)$

 $NLO/LO \sim \alpha^2 \varepsilon_r \sim 10^{-10}$

Palmer 87

more details

Electron Density in Nuclei

• Coulomb potential: $V(r) = -\frac{Z_{\text{eff}}(r)\alpha}{r}$

Nuclear charge screened by inner electrons:

$$Z_{
m eff}(r) \sim \left\{ egin{array}{ll} Z & r < a_0/Z & {
m ion\, charge} \ r/a_0 & a_0/Z < r < a_0/(1+n_e) \ 1+n_e & r > a_0/(1+n_e) \end{array}
ight.$$

See *e.g.* Budker-Kimball-DeMille: Atomic Physics

• Using non-relativistic hydrogen-like wavefunction:

$$|\psi(0)|^2 \simeq \frac{4.2Z}{a_0^3} (1 + n_e)^2$$

Higher-Order Corrections

Need to control King's linearity at least down to:

$$\frac{Hz}{\text{total IS}} \sim \frac{Hz}{GHz} \sim 10^{-9}$$

- Higher-order corrections are not trivial to compute, many-body, relativistic simulations are needed [in progress]
- Yet, IS are controlled by two small parameters:

$$\varepsilon_{\mu} = m_e \mu_{AA'} \sim (A - A') 10^{-8}$$
$$\varepsilon_r = \delta \langle r^2 \rangle_{AA} / a_0^2 \sim (A - A') 10^{-11}$$

• So, we can entertain NDA...

Field Shift

Perturbation theory: See

Seltzer '69 Blundell et al. '87 nuclear charge distribution

$$\delta\nu_{AA'}^{\rm FS} = -e\int d^3r_e |\psi(r_e)|^2 \delta V(r_e) \;, \quad \delta V(r_e) = \frac{Ze}{4\pi} \int d^3r_N \frac{\delta\rho(r_N)}{|\vec{r_e} - \vec{r_N}|}$$
 electron density nuclear potential

- LO: $\propto |\psi(0)|^2 \overline{\delta \langle r^2 \rangle_{AA'}} \sim \mathcal{O}(\varepsilon_r)$
- NLO/LO: $\sim \mathcal{O}(\varepsilon_{\mu}^2, \varepsilon_r^2, \varepsilon_{\mu}\varepsilon_r)/\varepsilon_r \sim 10^{-7}$
- NLO is linear up to overlap with the nucleus $\sim \mathcal{O}(\varepsilon_r)$
- Hence, non-linearities are only of $\mathcal{O}(\varepsilon_{\mu}^2) \sim 10^{-14}$

Specific Mass Shift

- MS arises from:
 - « rescaling » Rydberg constant (normal MS)
 - electron-electron correlation, relativistic... (specific MS)
- at LO, both scale like $m_e \mu_{AA'} \sim \mathcal{O}(\varepsilon_{\mu})$
- NLO correction is parametrically: Palmer '87

$$\sim \alpha^2 m_e^2 (m_A^{-2} - m_{A'}^{-2})$$

• Hence, NLO/LO $\sim \mathcal{O}(\alpha^2 \varepsilon_r) \sim 10^{-10}$