

Primordial Black Holes from Axions?

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work in collaboration with
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1 Motivation.

Outline

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- 2 Axionic string-wall networks.

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- 3 PBHs from the QCD Axion and from Axion-Like Particles (ALPs).
- 4 Summary and conclusions.

Motivation

- Nature of DM remains mysterious. [see tomorrow's talks](#).
- Some well-motivated *particle physics* candidates (many others on the market)
 - 1 **WIMPs**: motivated by the WIMP miracle and by SUSY solution to hierarchy problem. Currently under experimental pressure (no WIMP + no low scale SUSY).
 - 2 **Axions**: motivated by strong CP problem (QCD) and ubiquitous in String Theory. Only very small region of parameter space currently probed (ADMX), more to come!.
- Recent LIGO observations of $O(10)M_{\odot}$ BHs revive interest in traditionally astrophysical candidate: **Primordial Black Holes (PBHs)** [see morning talks](#).
- Even if $\rho_{PBH}/\rho_{CDM} \ll 1$, PBHs can be seeds of cosmic structures [[Carr, Silk '18](#)]

- Conventional connection with particle physics: PBHs generated from **gravitational** collapse of inflationary overdensities.
- Gravitationally collapsing horizon-size overdensity would generate a PBH of mass

$$M_H \approx \frac{4}{3}\pi \frac{\rho}{H^3} = \frac{4}{3}\pi \frac{M_p^2}{H} \simeq \left(\frac{100 \text{ MeV}}{T} \right)^2 M_\odot,$$

- ⇒ PBHs of given mass require large overdensities re-entering at some $T \rightarrow$ need to **complicate** inflationary picture.
- **Broad motivation of this talk:** Can PBHs be generated by dynamics which occurs directly at T_{QCD} , **not tied to inflation?**
- Coincidence: T_{QCD} also sets the axion DM abundance from the misalignment mechanism.

- **Basic idea of this talk:** generate PBHs from the collapse of axionic domain walls [see also Deng et al.'16, Vachaspati '17].
 - **Collapse driven by tension** of the domain wall, **not** gravitational!
 - Independent from physics of inflation.
- **Alternative** particle physics approach to PBHsDM.
- **Remark:** will mainly use parameters of the QCD axion, but same mechanism can occur for general Axion-Like-Particles (ALPs).

Part 1

Axionic String-Wall Networks

Phases and Defects of the (QCD) Axion

- **Focus:** PQ symmetry broken **after** inflation.

1 At $T_{PQ} = \eta$, a complex scalar field Φ with potential

$$V(\Phi) = \frac{\lambda}{4} \left(|\Phi|^2 - \eta^2 \right)^2,$$

acquires a VEV $\Phi \simeq \eta e^{ia/\eta}$ which spontaneously breaks $U(1)_{PQ}$.

→ **Strings** form at T_{PQ} , around which $\Delta a = 2\pi\eta$.

- Scaling regime $\rho_{string} \simeq \mu_{string} H^2 \sim a(t)^{-4}$, where μ_{string} is the string tension.
- Strings radiate axions from T_{PQ} down to T_{QCD} .

Phases and Defects of the (QCD) Axion

→ Non-perturbative (QCD instantons) effects induce a potential for a

$$V(a, T) = \frac{m^2(T)\eta^2}{N_{DW}^2} \left[1 - \cos \left(\frac{a}{\eta} N_{DW} \right) \right],$$

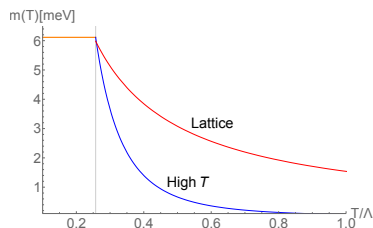
with periodicity $F = \eta/N_{DW}$.

→ $N_{DW} \equiv$ number of physically inequivalent vacua in the domain $[-\eta, \eta]$.

→ $N_{DW} \equiv$ color anomaly, e.g.

- KSVZ: $N_{DW} = 1$ in simplest case, $N_{DW} > 1$ with more generations of heavy fermions.
- DSFZ: $N_{DW} = 6$ in simplest case [other values possible \[see e.g. Monday's talk by Ziegler\]](#).

Temperature Dependence of the Axion Mass



$$T \lesssim 10^2 \text{MeV} \quad m^2(T) = c_T \frac{\Lambda_{QCD}^4}{F^2} \left(\frac{T}{\Lambda_{QCD}} \right)^{-n}$$

$$T \gtrsim 10^2 \text{MeV} \quad m^2(T) = c_0 \frac{\Lambda_{QCD}^4}{F^2}$$

Theoretical uncertainties on parameters

- High T DIGA-based calculation: $n \approx 7$, $c_T \approx 10^{-7}$, $c_0 \approx 10^{-3}$ [Wantz, Shellard '10] .
- Preliminary lattice calculations hint at $n \approx 2$, $c_T \approx 10^{-4}$ [see Grilli di Cortona et al. '15 and refs therein].

Phases and Defects of the (QCD) Axion

2 The axion is frozen because of Hubble friction until $3H(T_1) \simeq m(T_1)$.

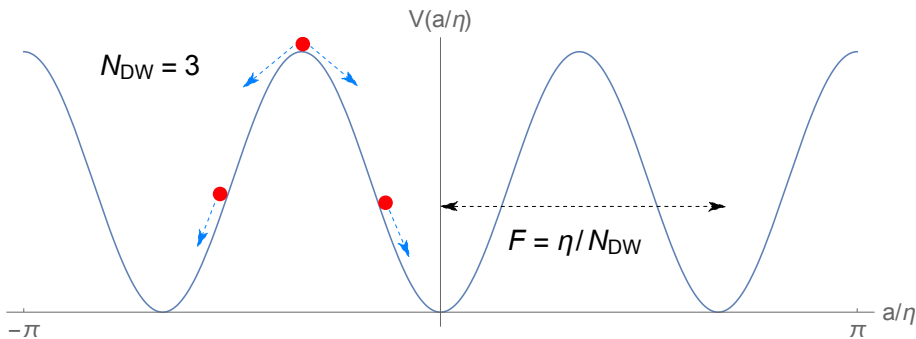
- At $T_1 \approx 1 - 6$ GeV the axion oscillates and behaves as CDM \rightarrow *Misalignment mechanism*.

\Rightarrow Oscillation occur around any of the N_{DW} vacua \Rightarrow Domain walls form!

- Each string gets attached to N_{DW} domain walls \Rightarrow String-Wall Network is formed

$N_{DW} = 1$: Strings cut holes in DWs \Rightarrow Network disappears rapidly after T_1 .

$N_{DW} > 1$: DWs are pulling each string from different directions \Rightarrow Network is stable.

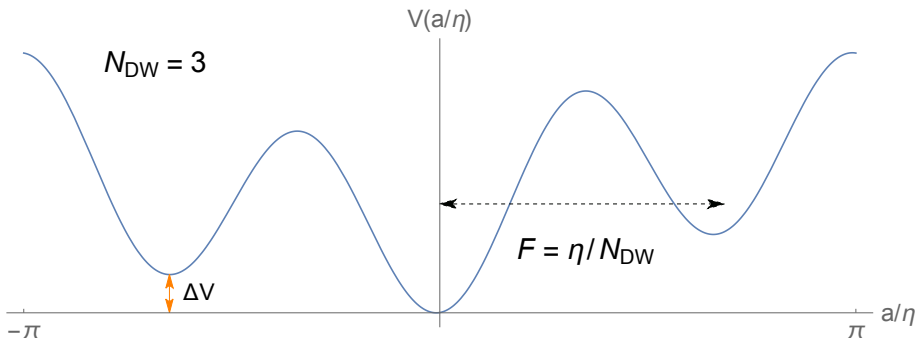


- Stable network enters scaling regime: $\rho_{DW} \sim \sigma H \sim a^{-2}$

⇒ Network overcloses the Universe!

- Here $\sigma \simeq 8mF^2$ is the DW tension.

→ Need to lift degeneracy of the vacua and induce network annihilation



- Can be achieved by adding

$$V_B = \Lambda_B^4 \left[1 - \cos \left(\frac{a}{\eta} + \delta \right) \right]$$

- Network annihilates at $T_2 \sim \sqrt{\frac{M_p \sigma}{\Lambda_B^4}}$.

Strings + Particles

$T_{\text{PQ}} \sim F$

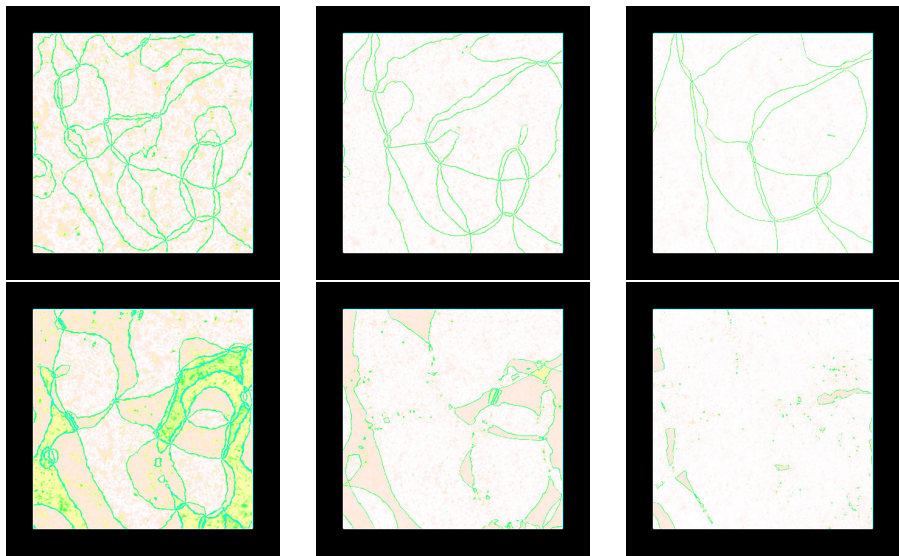
$T_{\text{QCD}} \sim \text{GeV}$

String-Wall Network + Particles

$T_2 \sim \text{few MeV} - \text{GeV}$

Particles

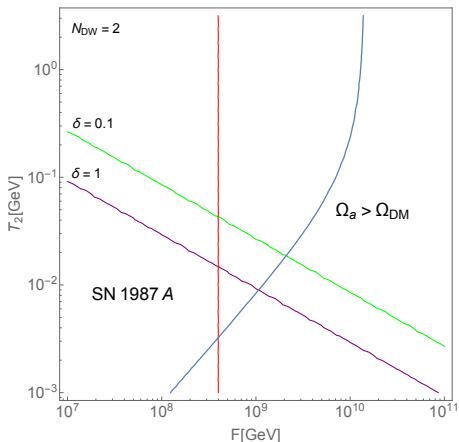
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Figures taken from [Kawasaki et al. '14]

1st row: $\Delta V = 0$, 2nd row: $\Delta V \approx 10^{-3} V_{QCD}$

Axion Dark Matter with $N_{DW} > 1$



Numerical parameters taken from [Kawasaki et al. '14](#) (pure scaling).
Uncertainties can enlarge untuned region of parameter space.

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Question for Part 2

Can (a fraction of) $\Omega_{a,DW}$ be made of PBHs?

Part 2

Primordial Black Holes from String-Wall Networks

Mechanism

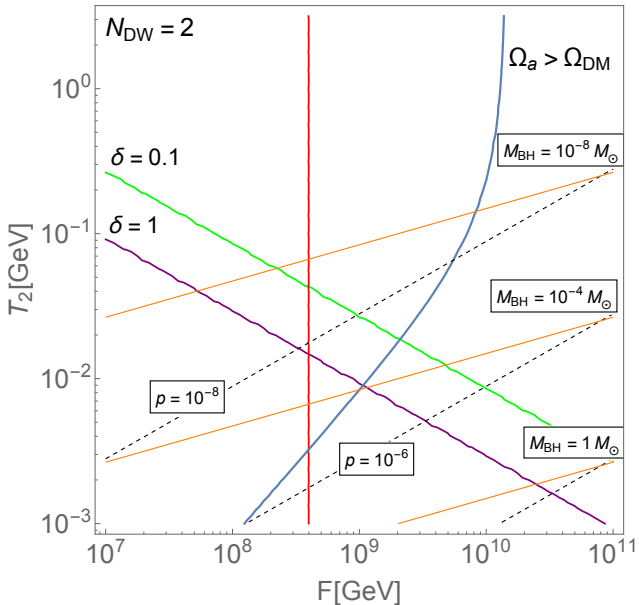
- Consider a closed domain wall entering the horizon at T_* with radius $R_0 \sim H^{-1}(T_*)$.
- It starts collapsing immediately under the action of its own tension.
- First consider spherical DW without loss of energy \rightarrow BH would form if DW allowed to shrink to R_s .
- Mass of the BH

$$M_{BH} \simeq 4\pi\sigma H^{-2}(T) \simeq 10^{-4} M_{\odot} \left(\frac{F}{10^9 \text{ GeV}} \right) \left(\frac{10 \text{ MeV}}{T} \right)^4$$

- Figure of merit

$$p = \frac{R_s}{H^{-1}(T)} = \frac{\sigma H(T_2)}{M_p^2 H(T_2)^2} = \frac{3\rho_{DW}}{\rho_{tot}}$$

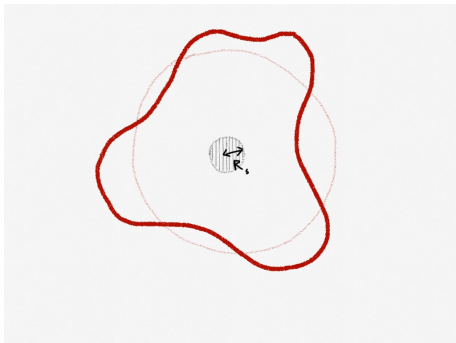
\rightarrow Larger p and M_{BH} if DWs collapse at the end of long NA epoch!



→ Figure of merit is small for the QCD axion!

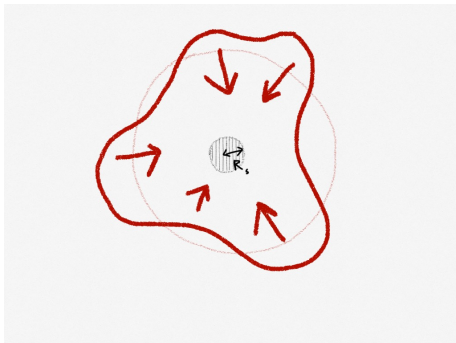
- Realistic setup: no reason for DWs to be spherical [see however \[Deng et al.'16, Garriga's talk\]](#) for nucleation of spherical DWs.
 - Expect asphericities of size $\sim H^{-1}(T)$. First assume that they remain constant during collapse ([see \[Widrow '89\]](#) for thin wall analysis).
- The smaller ρ , the smaller the probability of producing PBHs!

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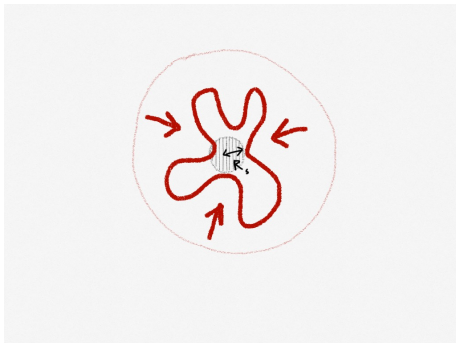
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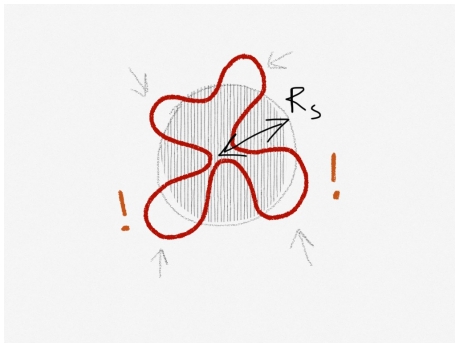
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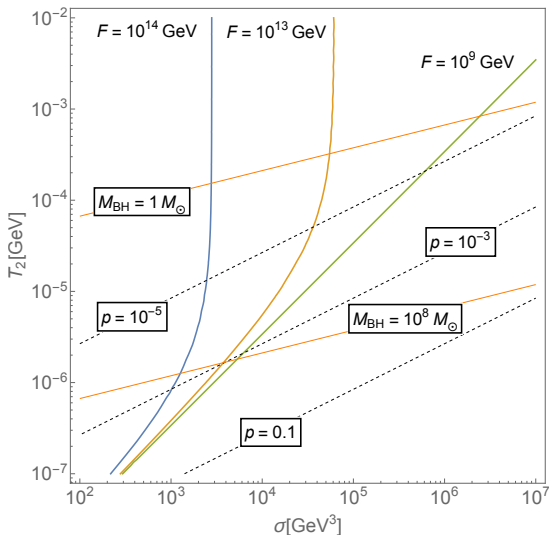
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But

- 1 Are asphericities reduced during the collapse?
- 2 What about generic ALP?
- 3 Also, what about avoiding SN bounds? [see e.g. Monday's talk by Ziegler](#)

Option 2: the ALP case (assuming same T dependence as QCD, $N_{DW} = 2$)



- R_s/H^{-1} larger by 4 orders of magnitude!
- Much heavier PBHs (up to upper bound)!

Option 1: Look at Physics of DW Collapse

- Thin Wall (Nambu-Goto) analysis shows that low l asphericities remain approximately constant during collapse [Widrow '89]

→ However, axionic DWs are in fact radiating axion quanta as they shrink

$$\mathcal{L}_{DW} = -\sigma \int_{DW} \sqrt{g} + e \int_{DW} A_3$$

Can think of as some friction on the DW motion.

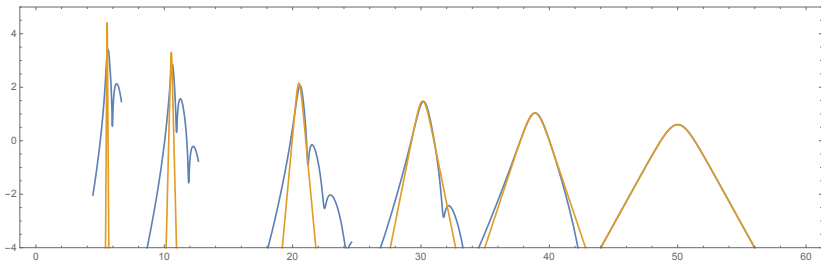
- **Idea:** can this smoothen the shape of the DW?
- Similar in a sense to interaction of DW with thermal plasma, where exponential suppression of asphericities is observed [see Garriga et al '92 for strings].

→ Currently trying to understand analytically (Thin Wall+Friction) and numerically (Thick Wall) reduction of asphericities!

- 1 DW starts radiating at $R_* \sim (R_0 m)^{2/3} m^{-1}$ [Widrow '89].
- 2 DW collapses until $R_{min} \sim (R_0 m)^{-2/3} m^{-1}$, then bounces [Vachaspati'17].

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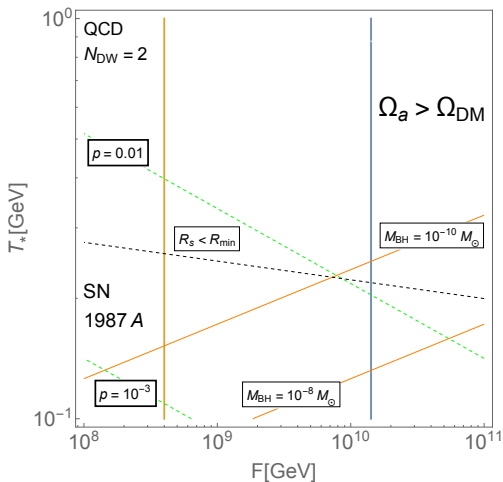
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→ Best Case Scenario: asphericities are very suppressed by axion radiation from R_* to R_S .

• Figure of merit then given by $p = R_*/H^{-1} \simeq (R_0 m)^{-1/3} m^{-1} \sim T^{2/3}$.

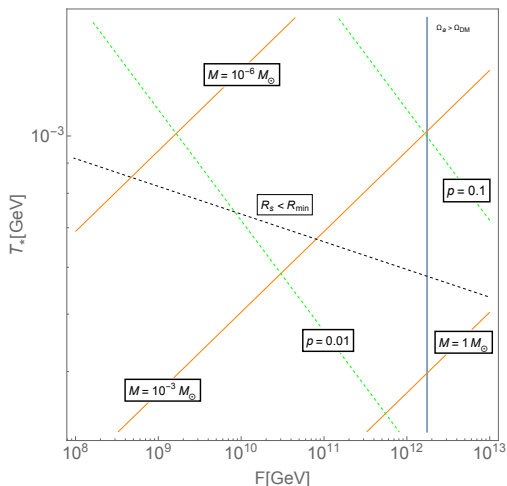
⇒ p larger for DWs which collapse **earlier** in the NA epoch!

→ However, cannot be too early, otherwise $R_S < R_{min}$ and BH cannot form.



- Here $T_\star = T$ at which given DW in the network starts to collapse.
- Figure of merit improves by 5 orders of magnitude!
- Region above dashed black line is disfavored → $N_{DW} = 1$ problematic for PBHs.

The ALP case with friction, $N_{DW} = 2$



Very interesting values of ρ and M_{BH} !

Summary and Outlook

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- 7 Final PBH **fraction**? Associated cosmo signatures (**GWs**, ...)?

Thanks for your attention!

