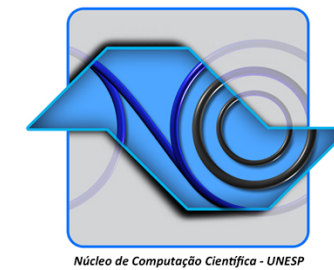


AIDA<sup>2020</sup>



# Towards full electromagnetic physics vectorisation in the GeantV transport framework

.....

Marilena Bandieramonte

([marilena.bandieramonte@cern.ch](mailto:marilena.bandieramonte@cern.ch))

on behalf of the GeantV development team

**27-31 August 2018,  
23rd Geant4 Collaboration  
Meeting, Lund**



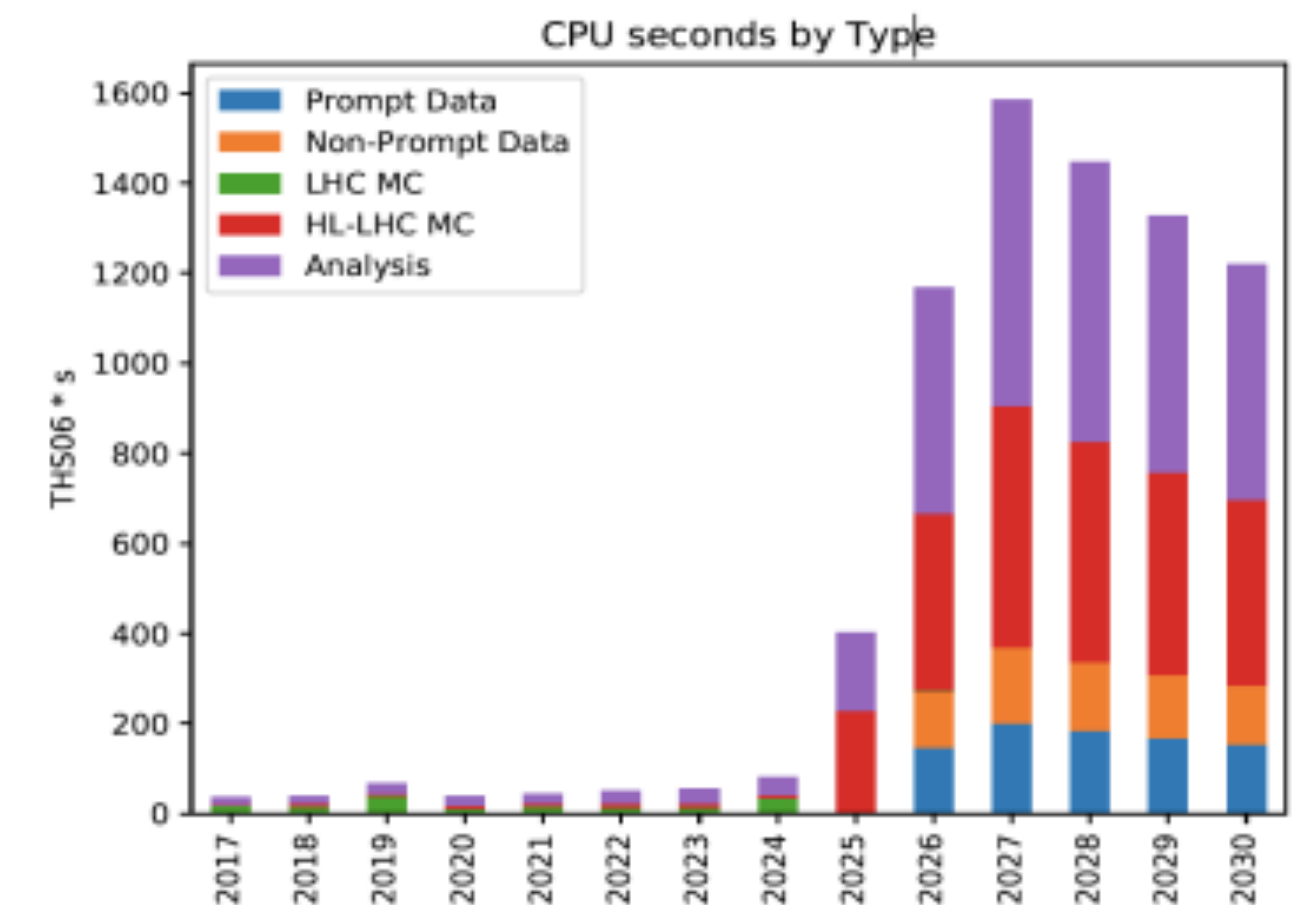
# MOTIVATION

.....



# MOTIVATION

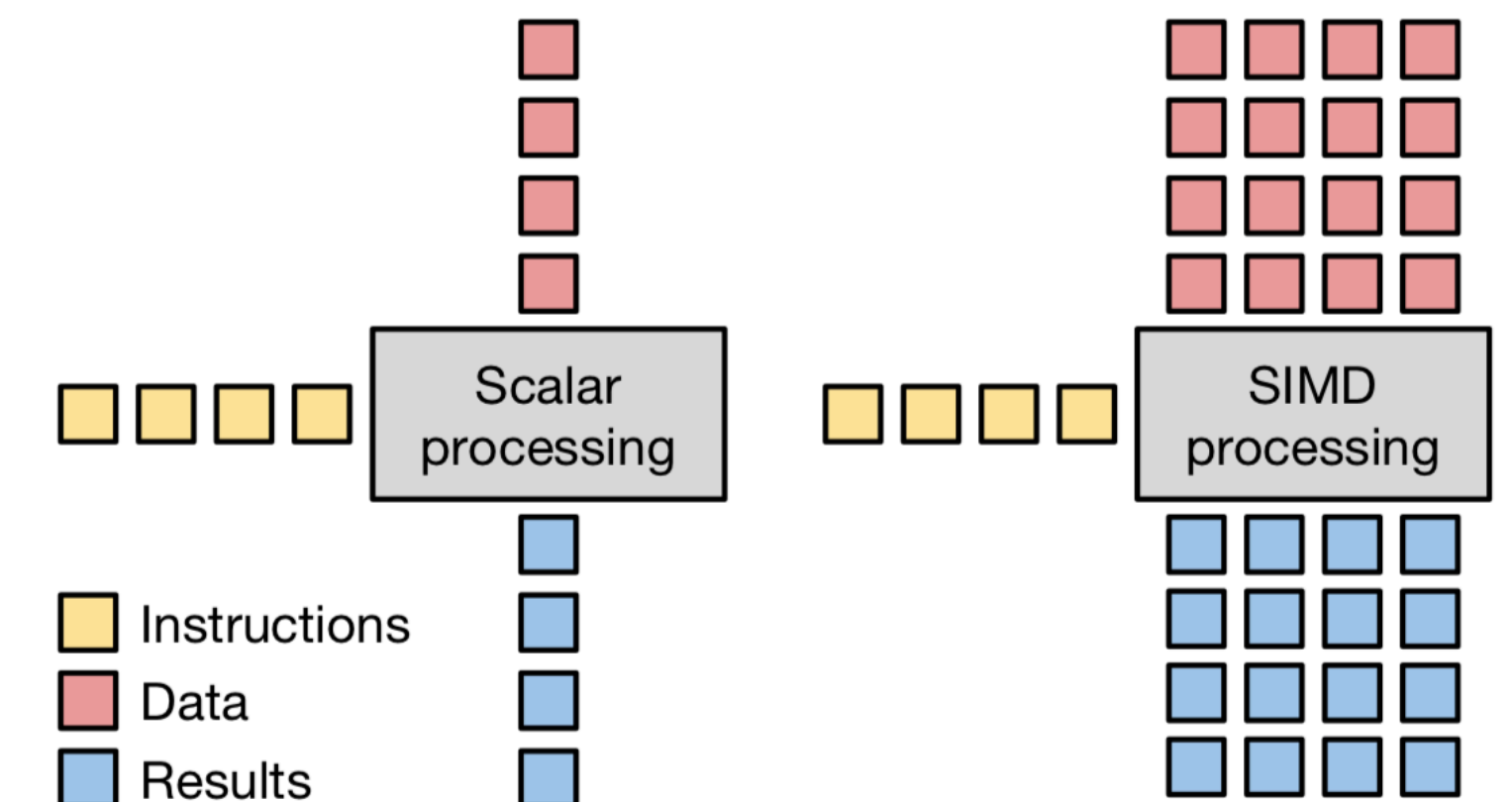
- Event simulation is one of the **most time consuming** parts of the workflow in the HEP sw ecosystem
  - For high-luminosity LHC phase (HL-LHC), the upgraded experiments expect to collect **150 times more data** than in Run 1
- The **GeantV R&D project** was launched in 2013, aiming at exploring emerging computer technologies in order to significantly increase run-time performance of detector simulation



**CMS and Atlas estimated CPU needs for HL-LHC (source: CWP)**

# MOTIVATION

- Event simulation is one of the **most time consuming** parts of the workflow in the HEP sw ecosystem
  - For high-luminosity LHC phase (HL-LHC), the upgraded experiments expect to collect **150 times more data** than in Run 1
- The **GeantV R&D project** was launched in 2013, aiming at exploring emerging computer technologies in order to significantly increase run-time performance of detector simulation
- The project studies performance gains when changing the classic particle transport approach, propagating **multiple tracks from multiple events in parallel**
  - improving code and data locality in the process
  - enabling SIMD/SIMT execution models:  
Vectorization+Multithreading
- **Vectorization of physics library** is important as key part of the algorithmic chain





# WHEN WE CAN PROFIT FROM VECTORIZATION

- Functions with many **math computations**, not bounded by **memory access**
  - Such as +, \*, /, sqrt, sin, cos, exp, log (ordered according to approximate computation complexity)
  - Load 4 doubles into SIMD register is one instruction but it is not faster than loading values one by one
- Functions with **minimal branching**
  - Branching **\*\*may\*\*** require to evaluate both branches for vectorized code

## Scalar code

```
if (cond > rndArray[0]) {  
    eps = Math::Exp(-a11 * rndArray[1]);  
    eps2 = eps * eps;  
} else {  
    eps2 = eps02 + (1. - eps02) * rndArray[1];  
    eps = Math::Sqrt(eps2);  
}
```

## Vector code

```
MaskD_v cond1 = cond > rnd1;  
if (!MaskEmpty(cond1)) {  
    vecCore::MaskedAssign(eps, cond1, Math::Exp(-a11 * rnd2));  
    vecCore::MaskedAssign(eps2, cond1, eps * eps);  
}  
if (!MaskEmpty(!cond1)) {  
    vecCore::MaskedAssign(eps2, !cond1, eps02 + (1.0 - eps02) * rnd2);  
    vecCore::MaskedAssign(eps, !cond1, Math::Sqrt(eps2));  
}
```

# GEANTV EM PHYSICS LIBRARY

Current State

particle	processes	model(s)	
		GeantV	Geant4
$e^-$	ionisation	Møller [100eV-100TeV]	Møller [100eV-100TeV]
	bremsstrahlung	Seltzer-Berger [1keV-1GeV]	Seltzer-Berger [1keV-1GeV]
		Tsai (Bethe-Heitler) w. LPM. [1GeV-100TeV]	Tsai (Bethe-Heitler) w. LPM. [1GeV-100TeV]
	Coulomb sc.	GS MSC model [100eV-100TeV]	Urban MSC model [100 eV-100MeV] Mixed model [100 MeV-100TeV]
$e^+$	ionisation	Bhabha [100eV-100TeV]	Bhabha [100eV-100TeV]
	bremsstrahlung	Seltzer-Berger [1keV-1GeV]	Seltzer-Berger [1keV-1GeV]
		Tsai (Bethe-Heitler) w. LPM. [1GeV-100TeV]	Tsai (Bethe-Heitler) w. LPM. [1GeV-100TeV]
	Coulomb sc.	GS MSC model [100eV-100TeV]	Urban MSC model [100 eV-100MeV] Mixed model [100 MeV-100TeV]
	annihilation	Heitler ( $2\gamma$ ) [0-100TeV]	Heitler ( $2\gamma$ ) [0-100TeV]
$\gamma$	photoelectric	Sauter-Gavrila + EPICS2014 [1eV-100TeV]	Sauter-Gavrila + EPICS2014 [1eV-100TeV]
	incoherent sc.	Klein-Nishina <sup>+</sup> [100eV-100TeV]	Klein-Nishina <sup>+</sup> [100eV-100TeV]
	$e^-e^+$ pair production	Bethe-Heitler <sup>+</sup> [100eV-80GeV]	Bethe-Heitler <sup>+</sup> [100eV-80GeV]
		Bethe-Heitler <sup>+</sup> w. LPM [80GeV-100TeV]	Bethe-Heitler <sup>+</sup> w. LPM [80GeV-100TeV]
	coherent sc.	-	Livermore
+	energy loss fluct.	-	Urban

- Every model is **tested and verified against the corresponding Geant4** model (cross section per atom, cross section per volume, and kinematic of primary and secondary particles)
- **EM showers** in GeantV can be **fully simulated** in real applications (i.e. FullCMS, TestEM3, TestEM5, FullLHCb) and the results are verified against the corresponding Geant4 simulation

# ELECTROMAGNETIC PHYSICS – FINAL STATE GENERATION

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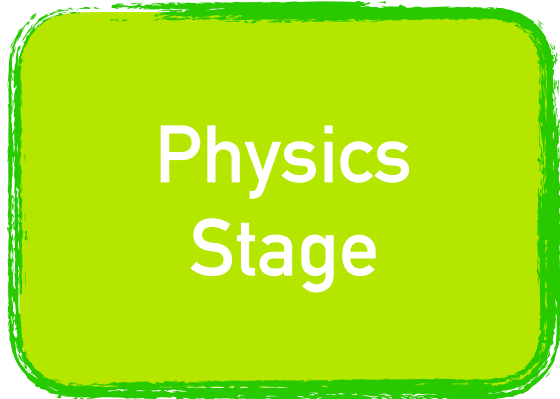
- When the particle undergoes a physics process, the **final state generation stage** occurs:



# ELECTROMAGNETIC PHYSICS – FINAL STATE GENERATION

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Physics  
Stage

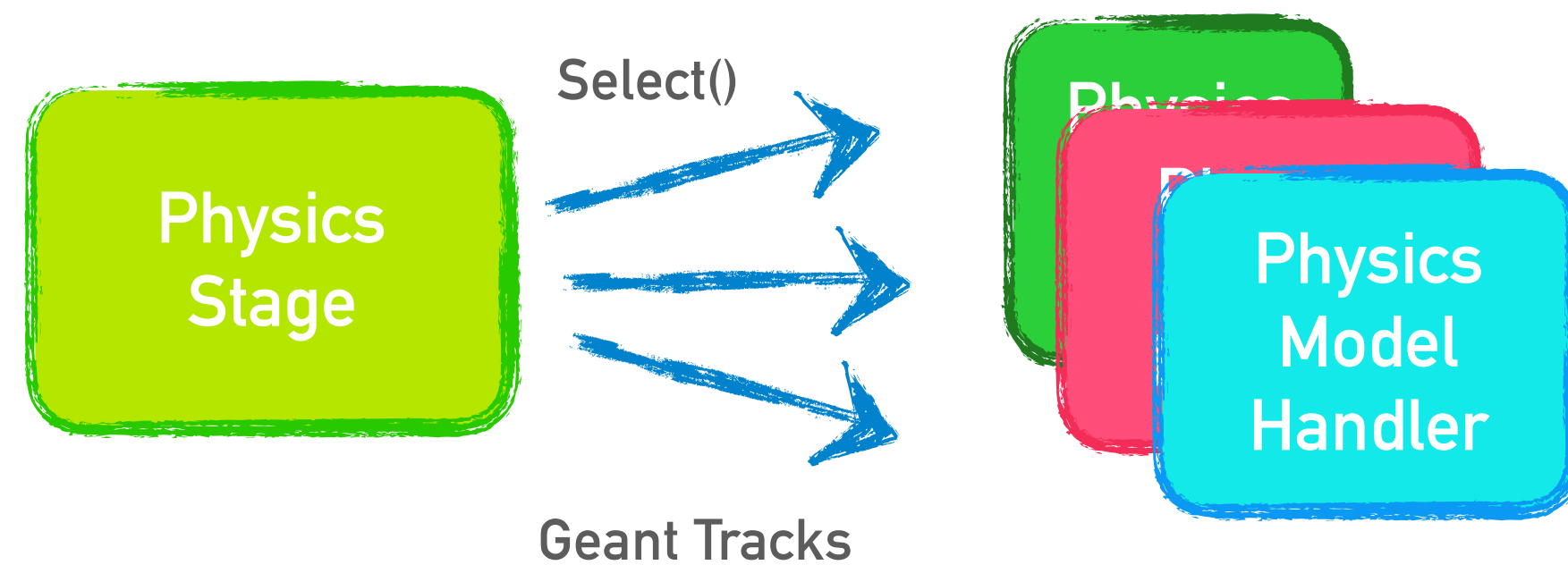




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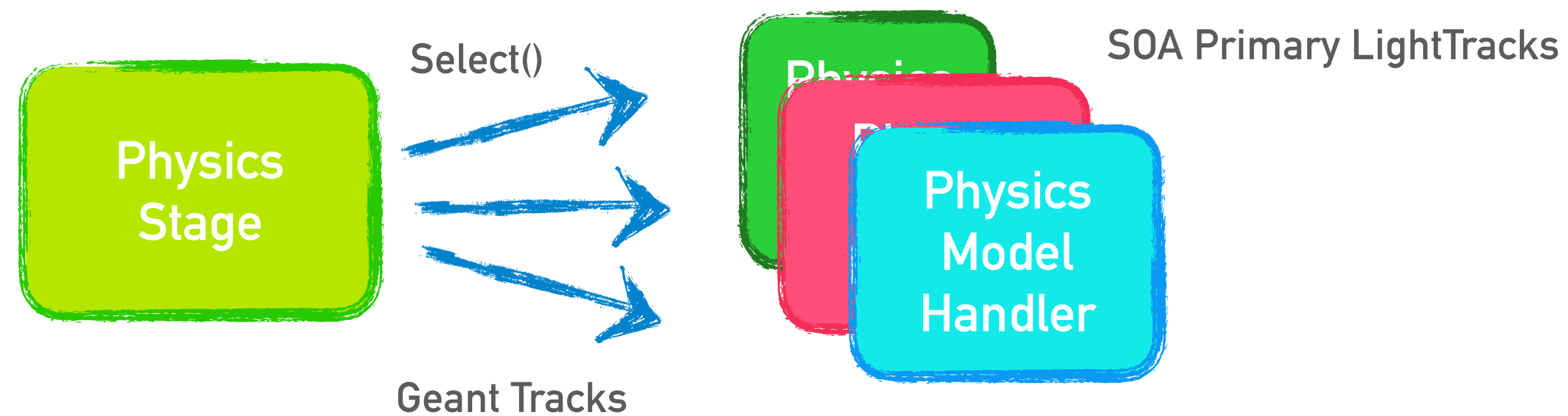
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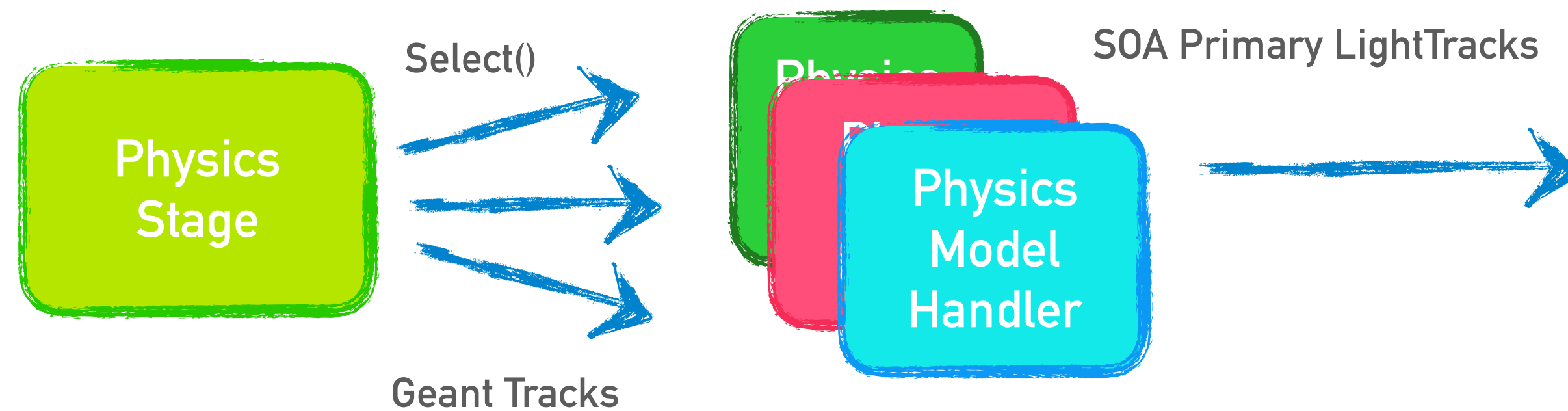
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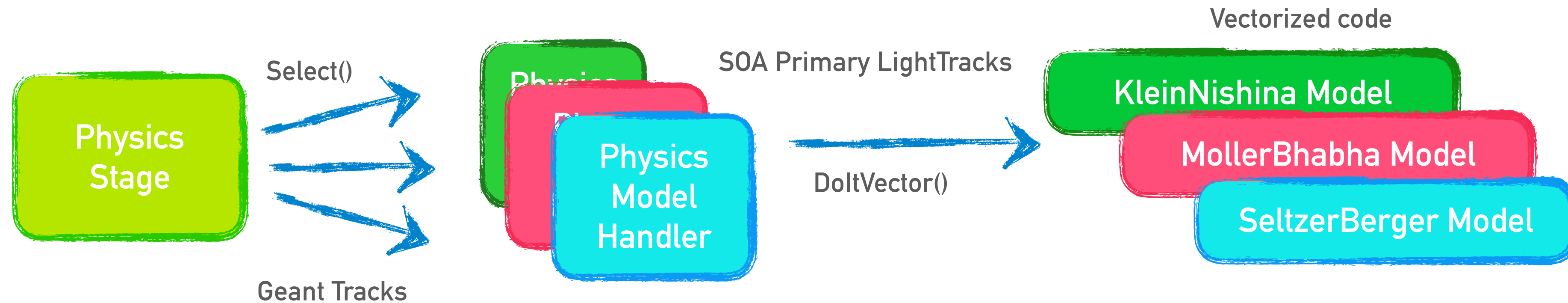
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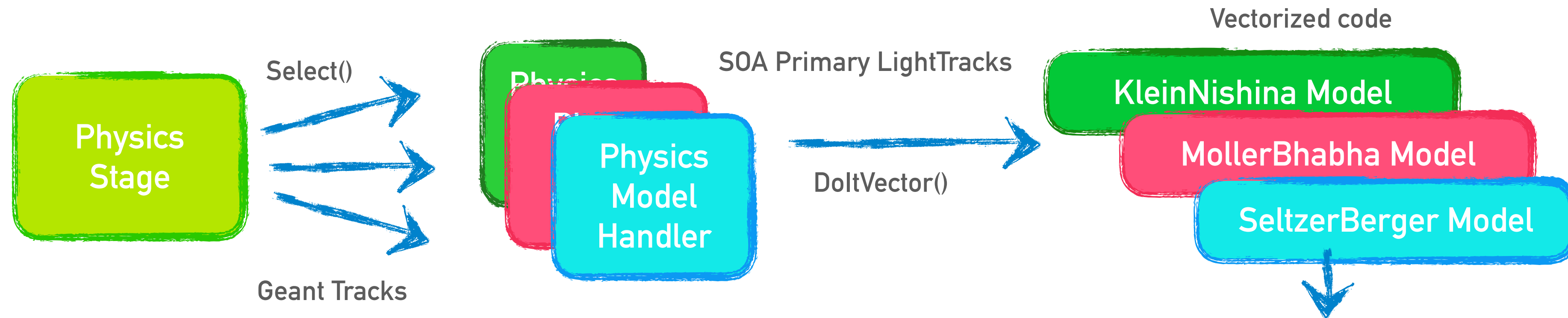
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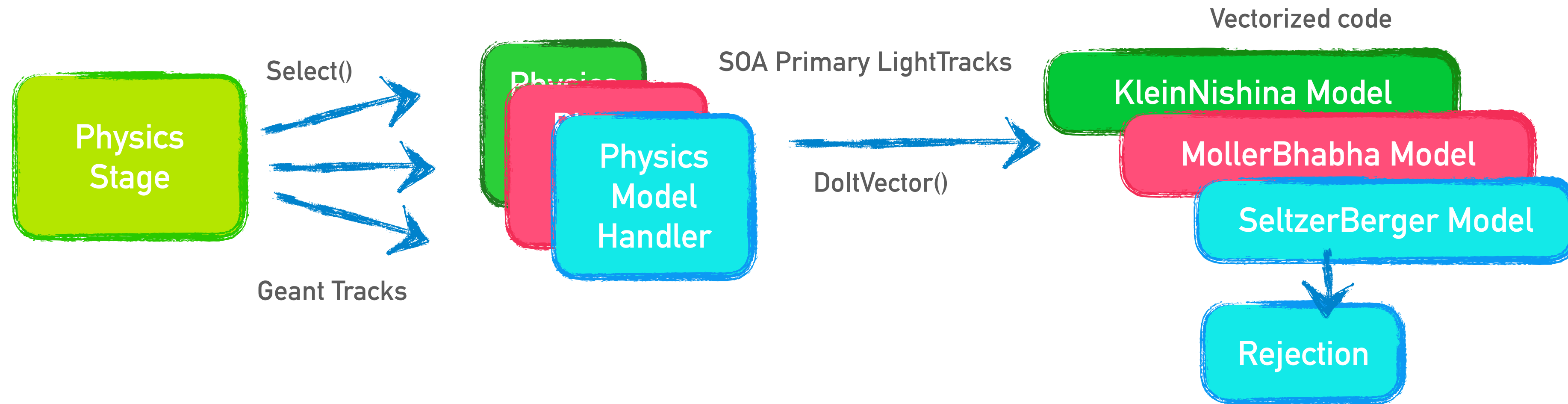
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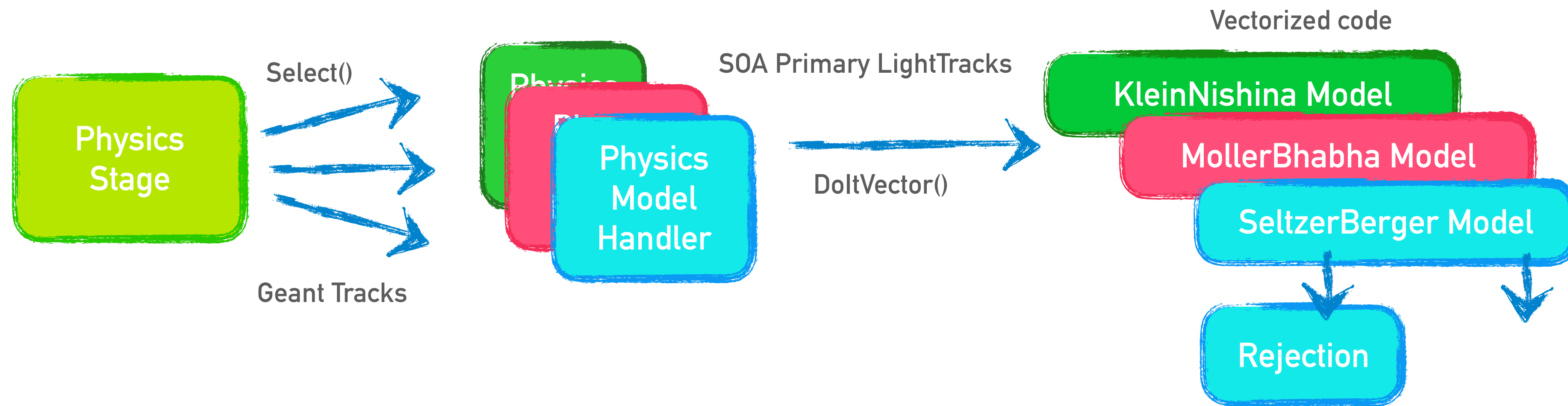
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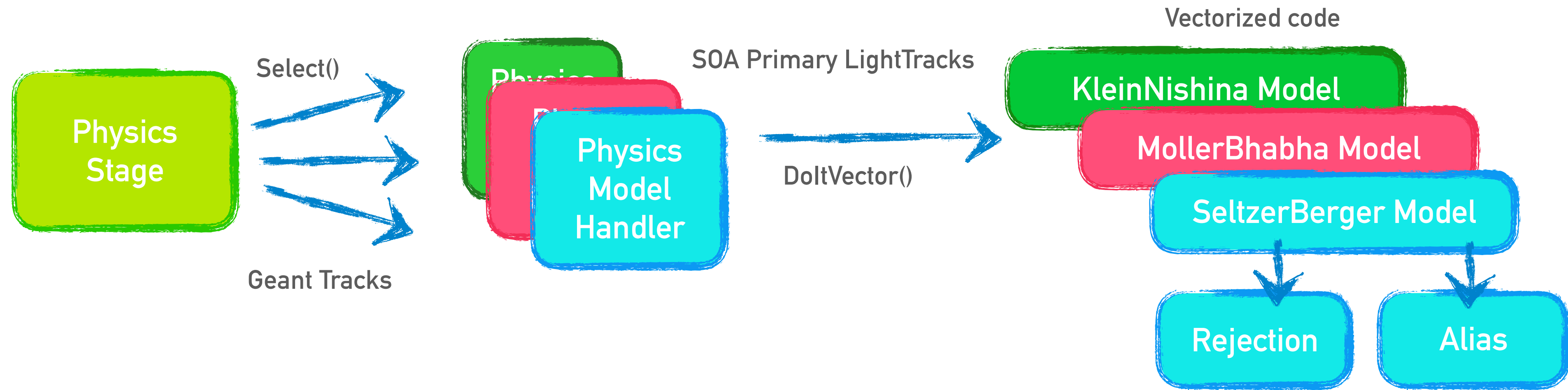
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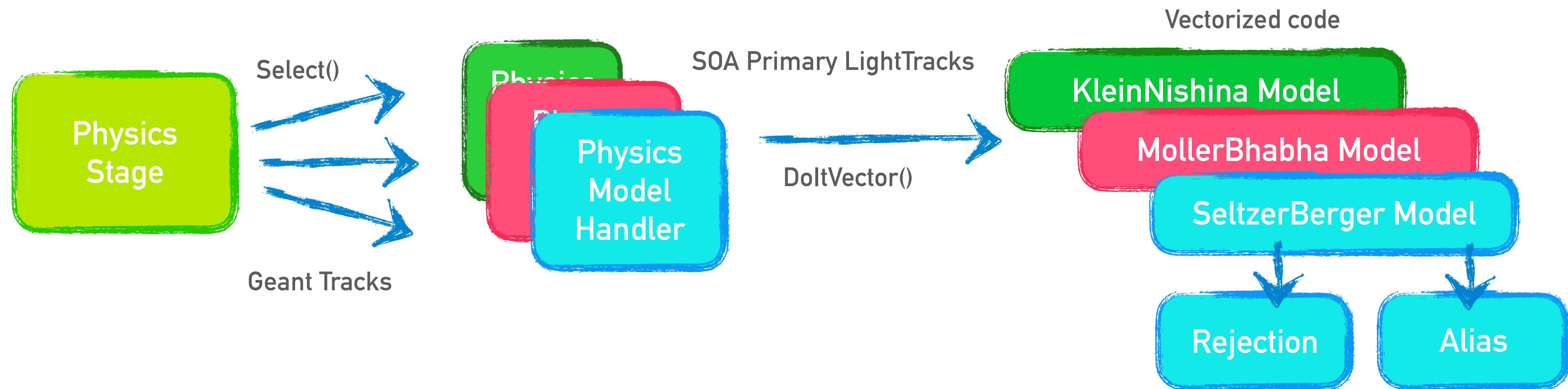
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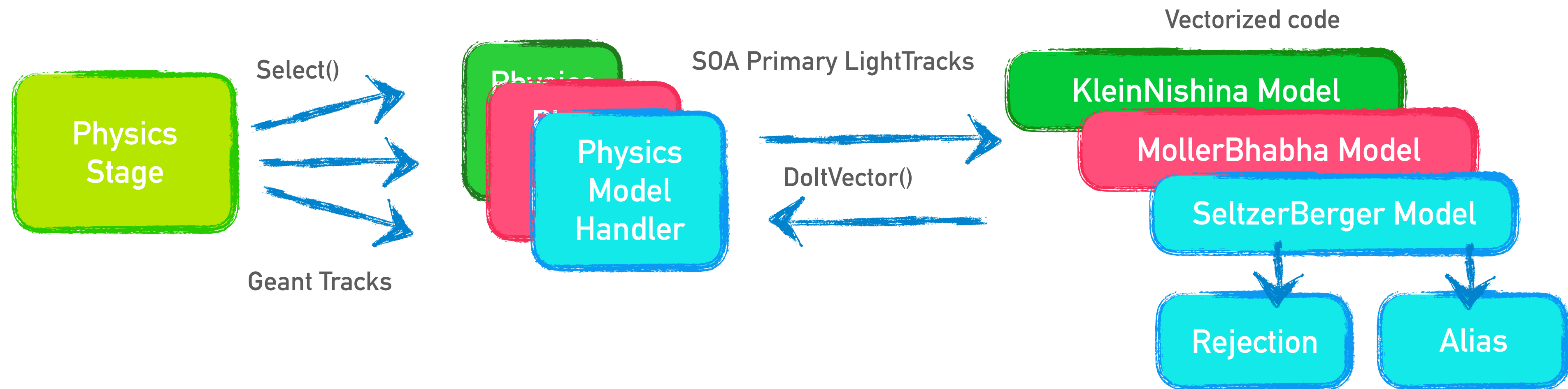


- Differential cross sections are used to update the **kinematic properties** of the primary particle and to **produce secondary particles** (if necessary)
- Sampling with **Rejection**:
  - **pros**: fast if rejection rate is low, **cons**: unpredictable number of trials
- Sampling with **Alias** tables + approximation
  - **pros**: constant ex. time, **cons**: introduce extra-computations, memory footprint



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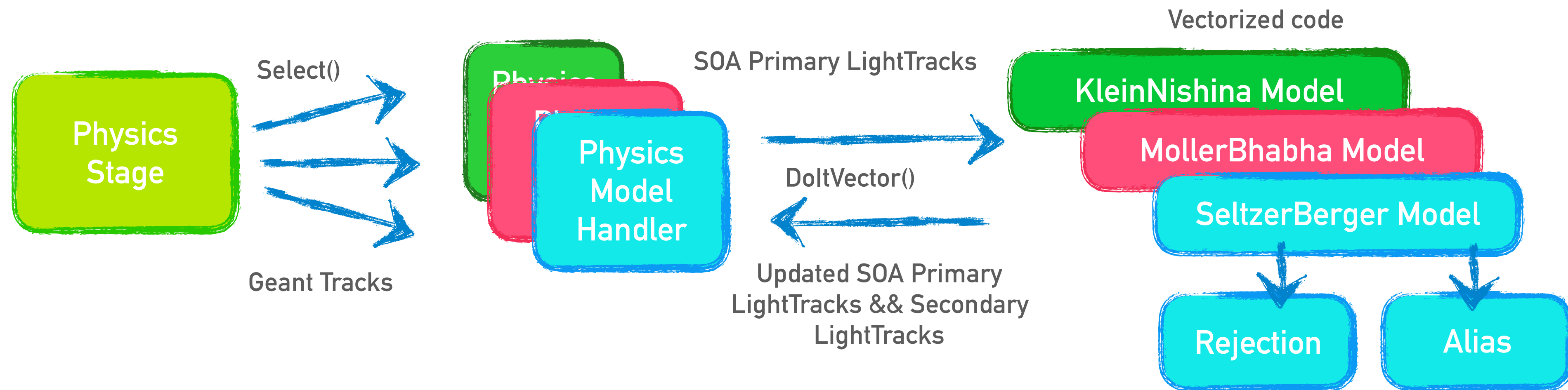
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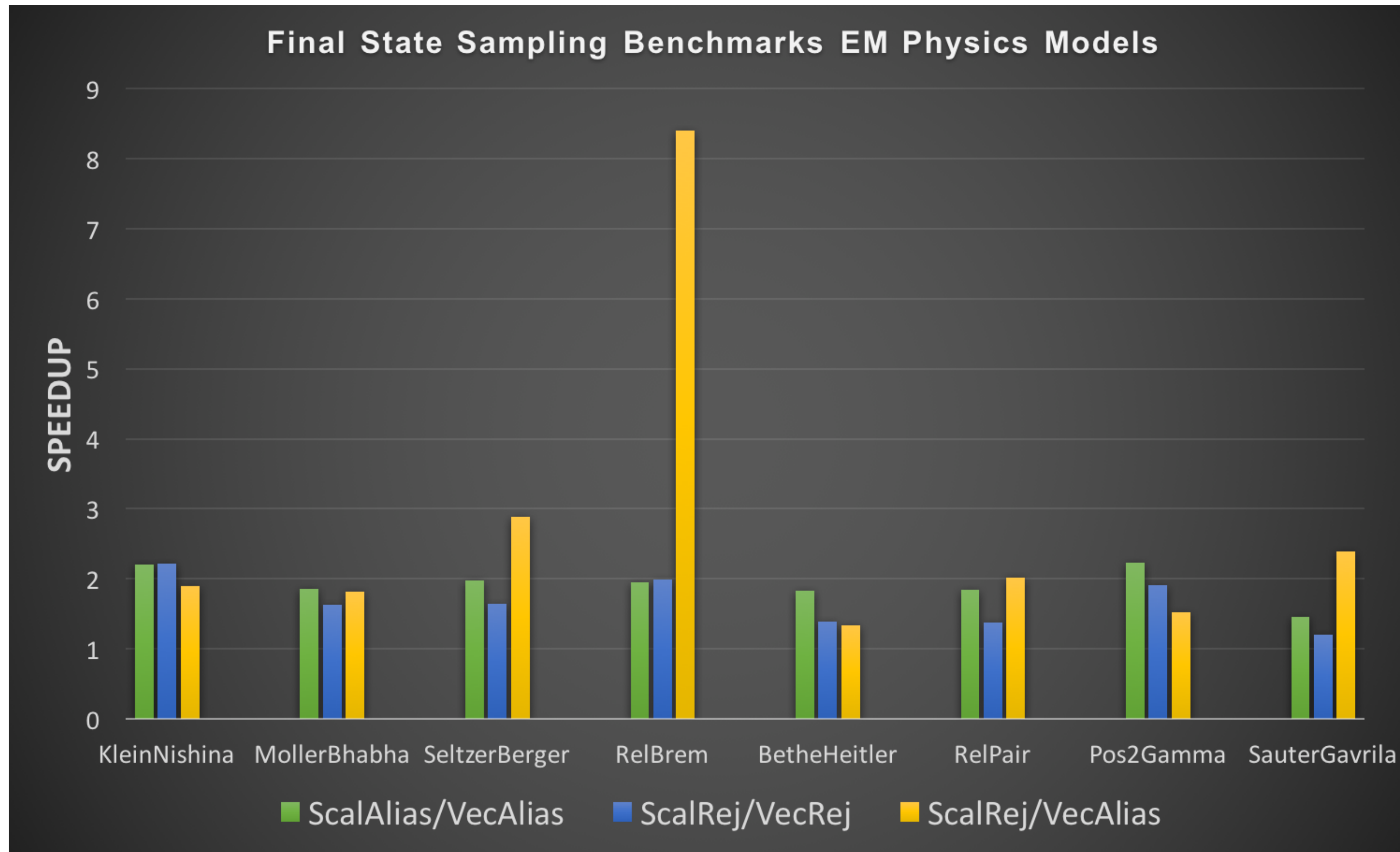
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# MODEL LEVEL TEST BENCHMARKS

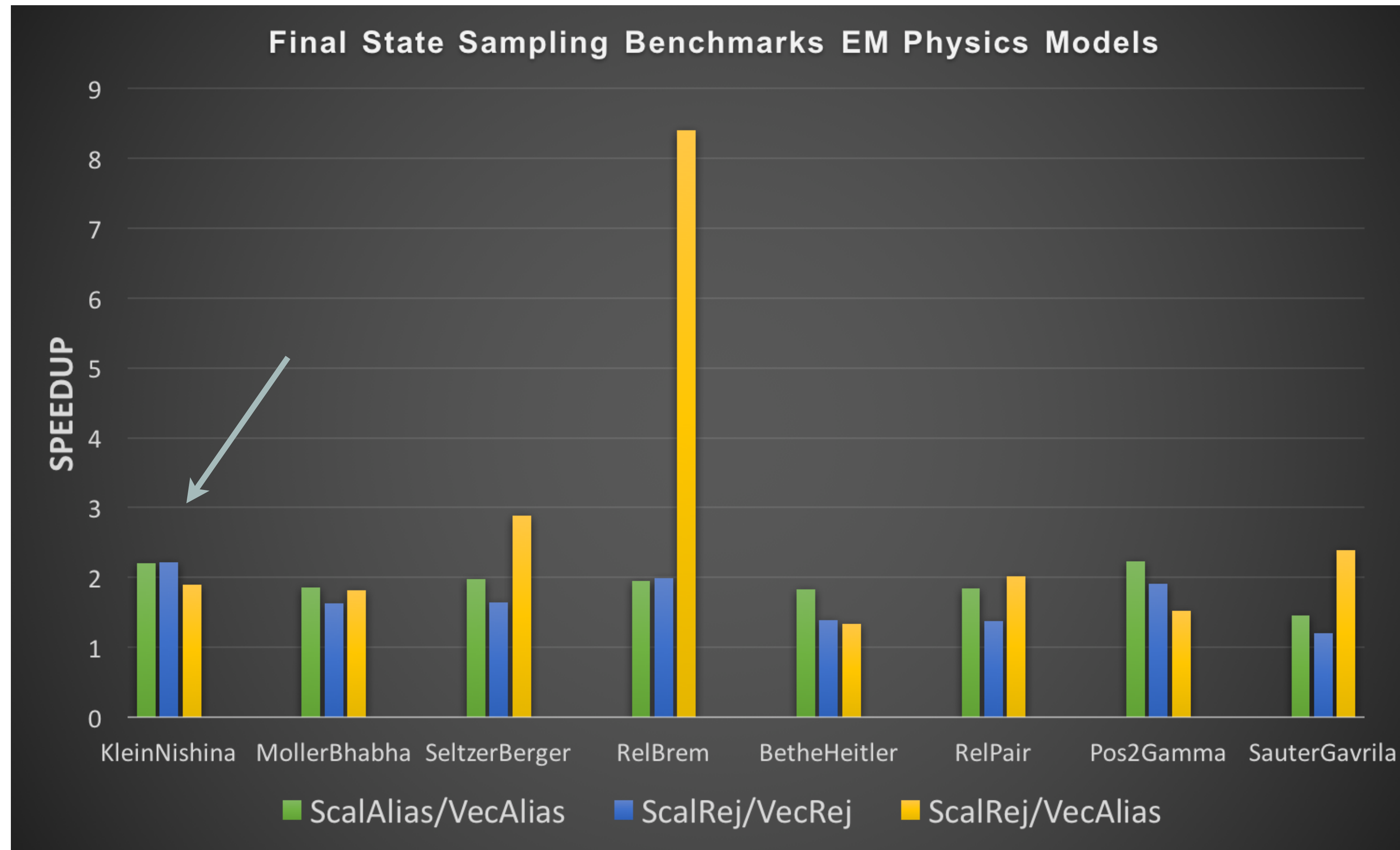
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See talk from A. Gheata for benchmarks on the full simulation chain

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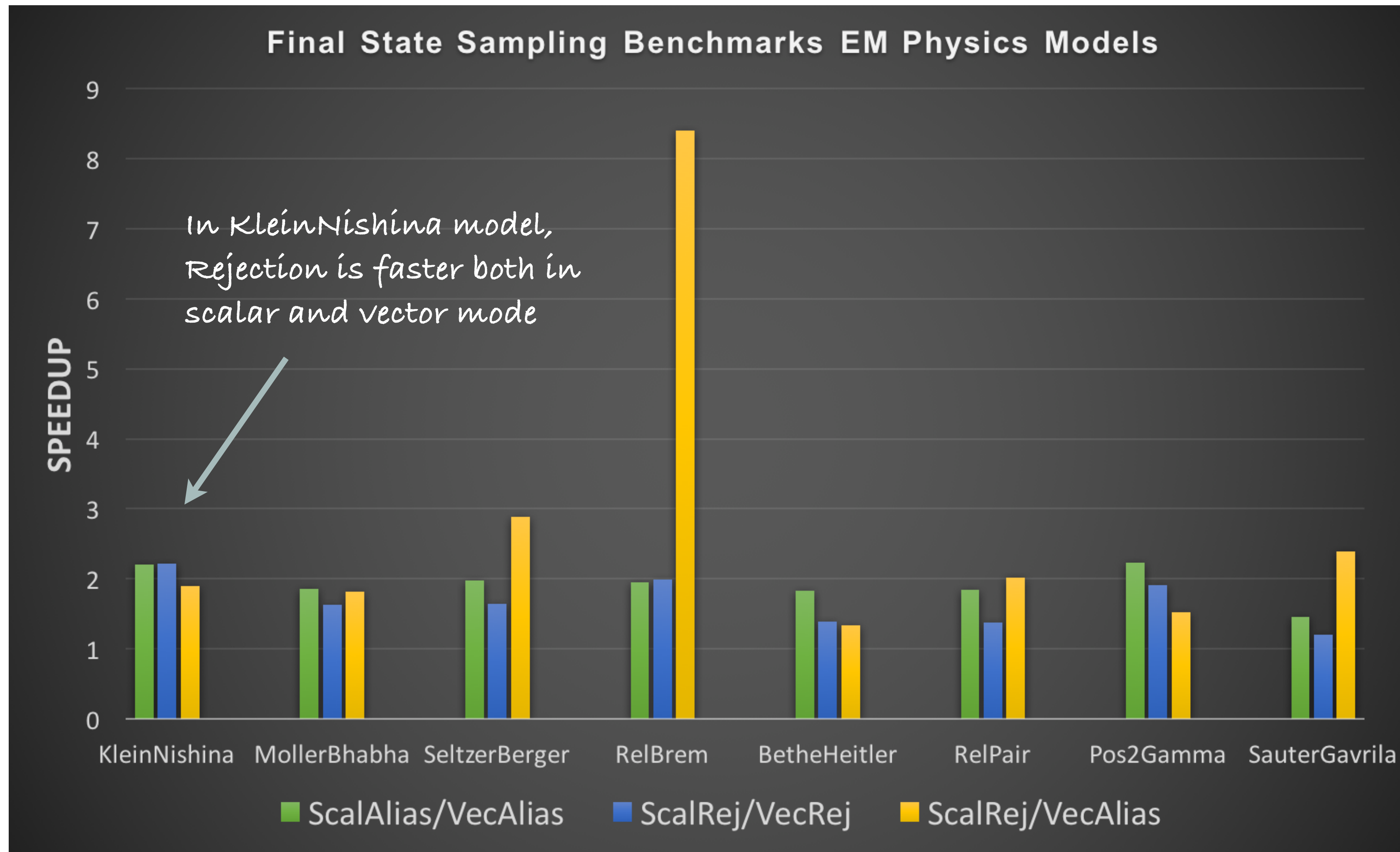
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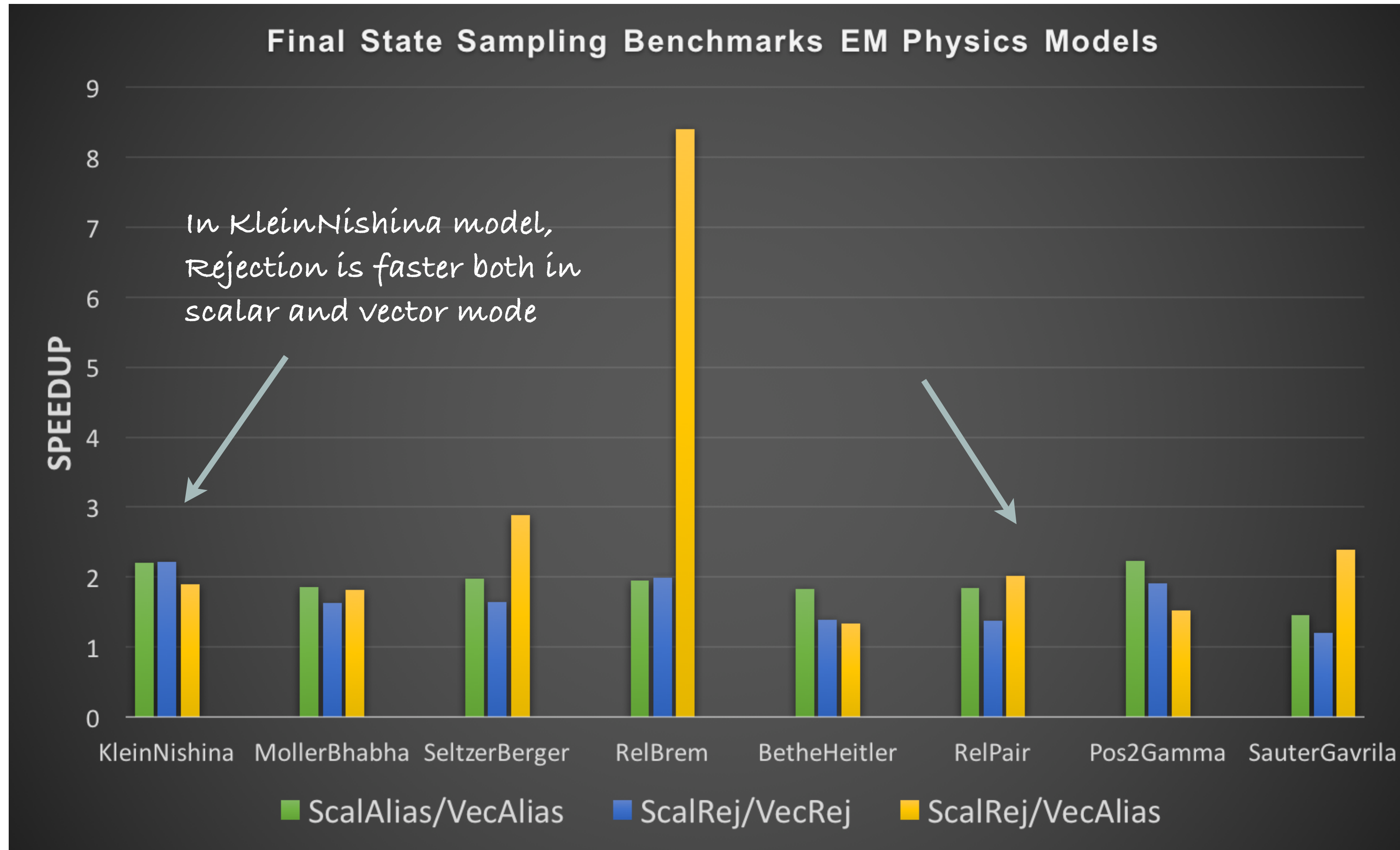


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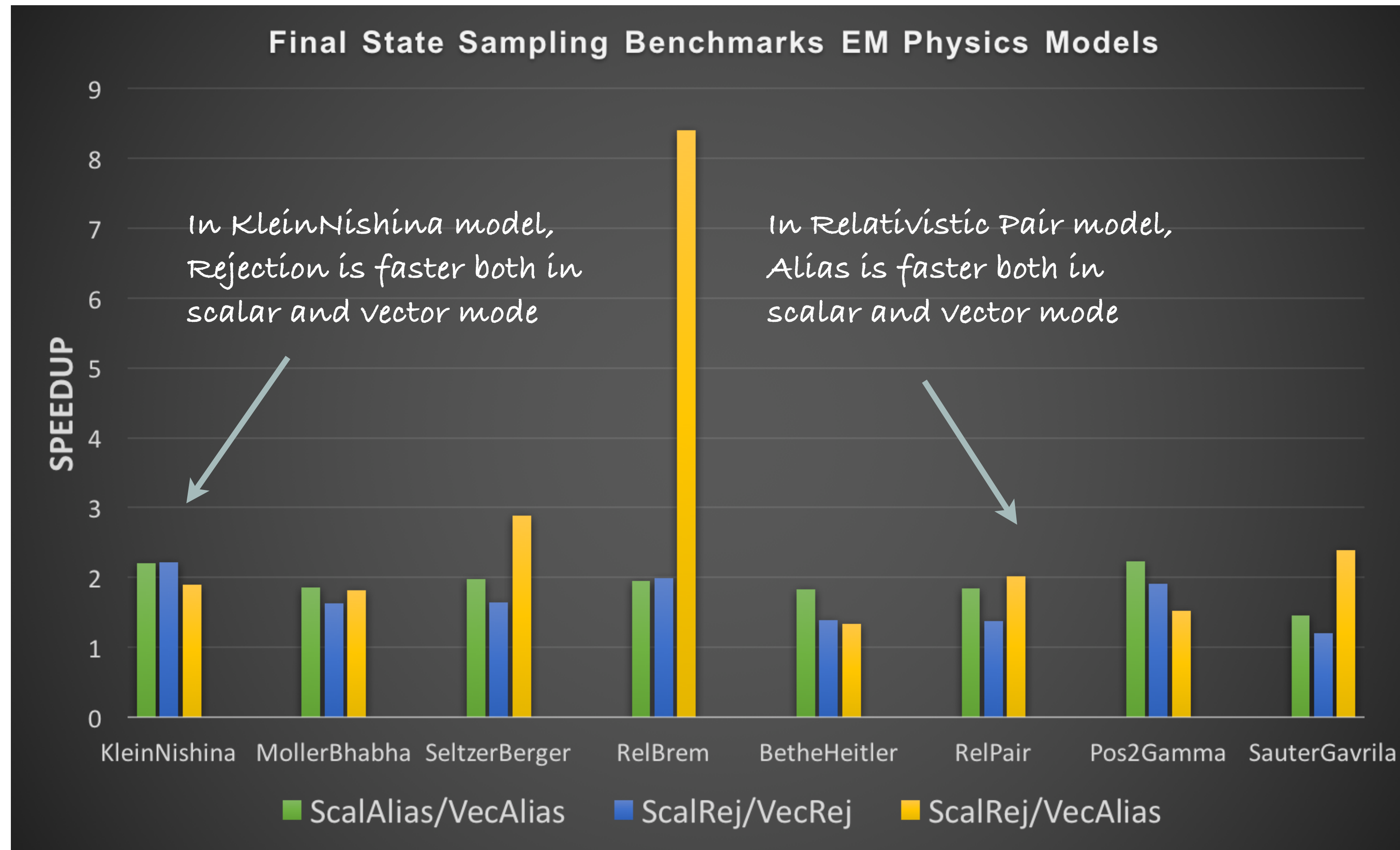
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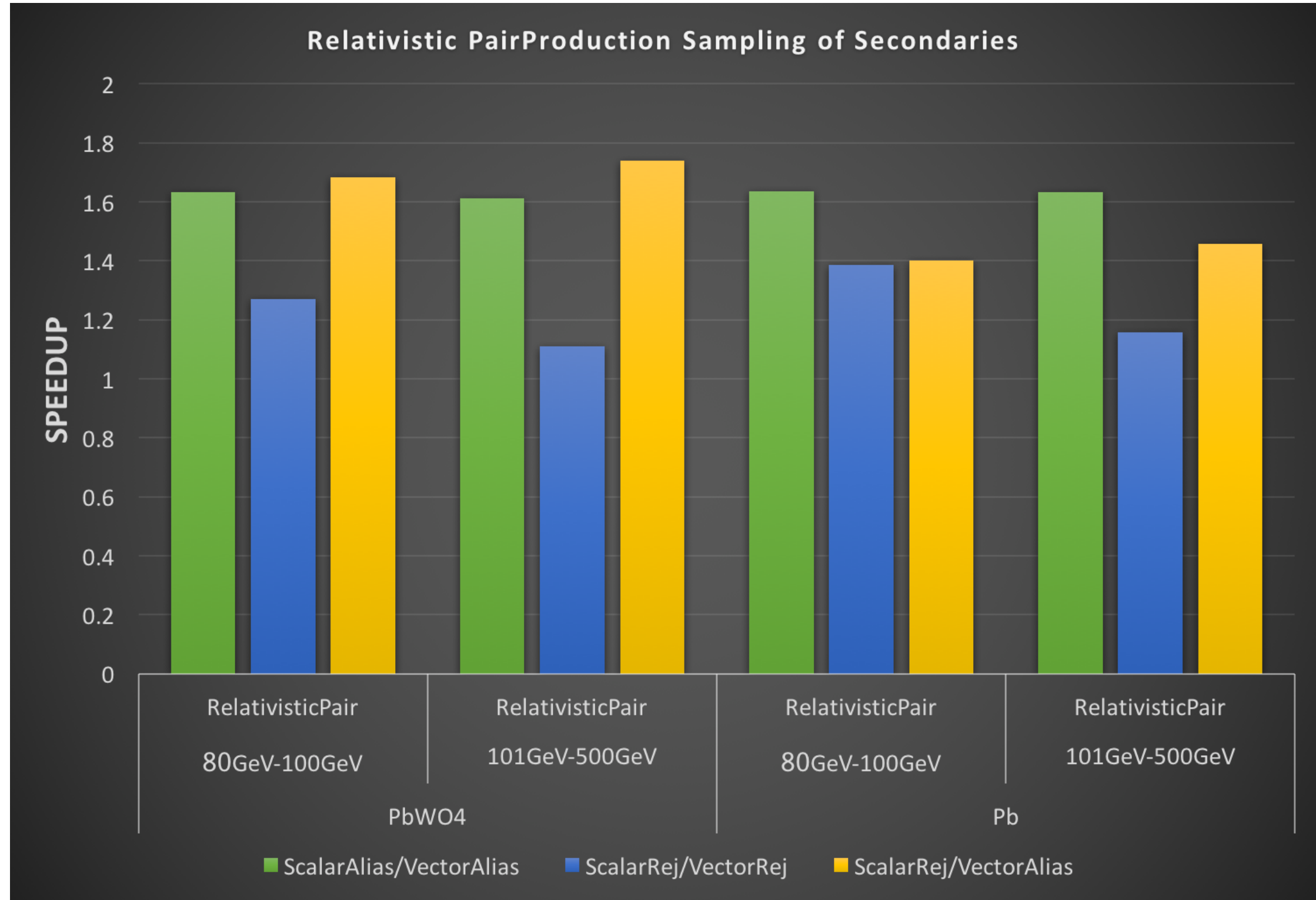
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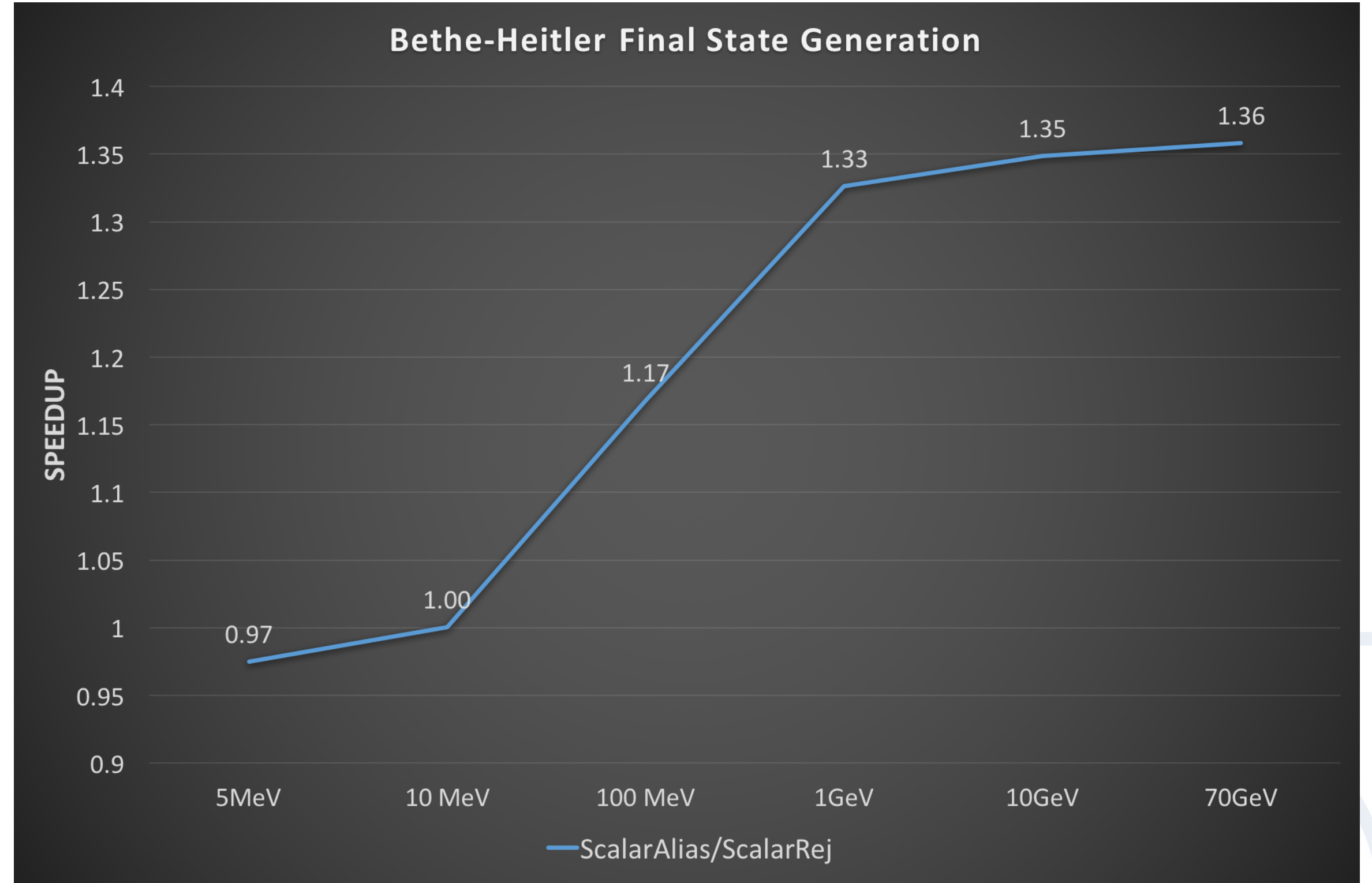
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# TUNING THE SIMULATION THROUGH MODELS

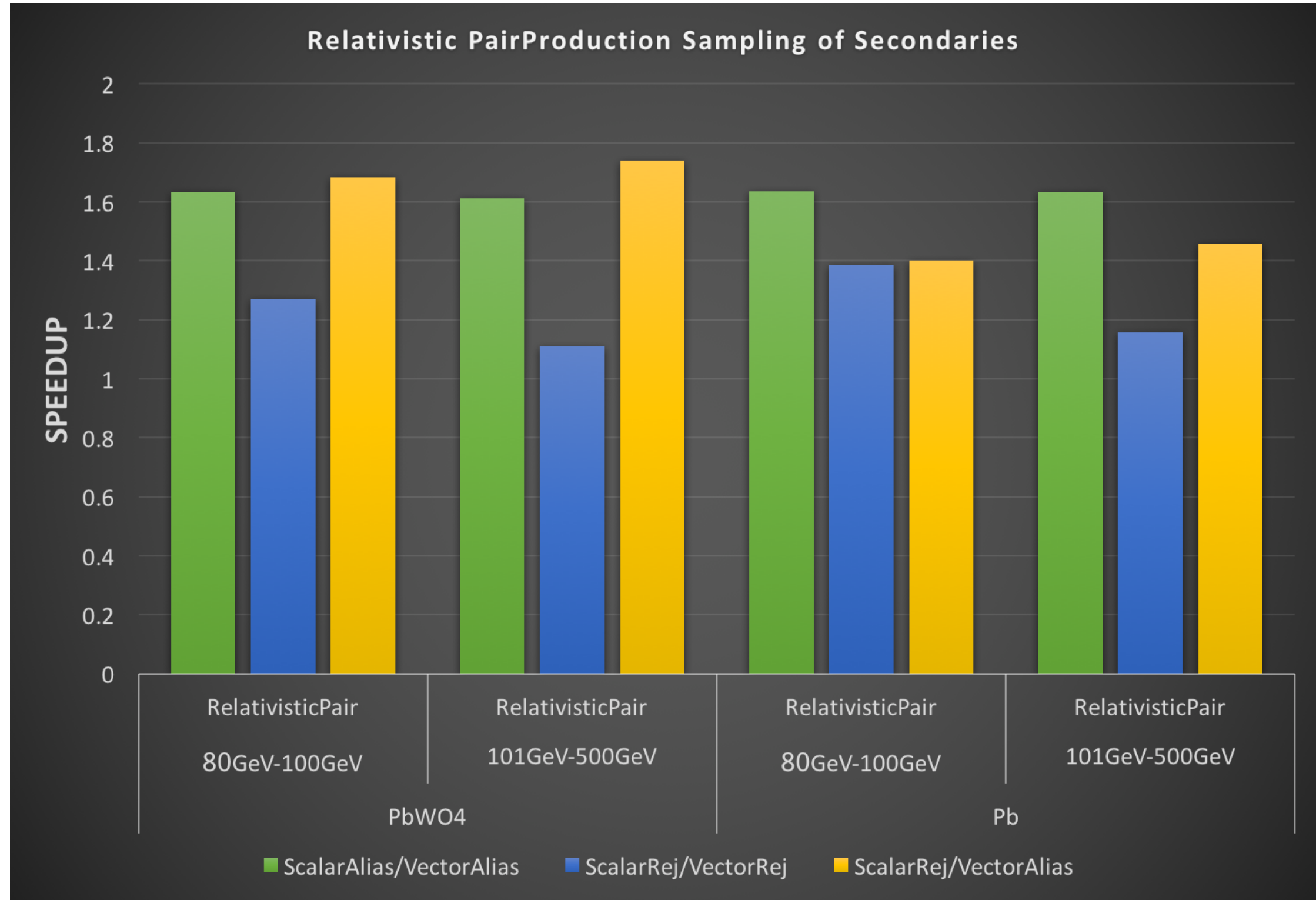


Specs: Haswell core i7 - AVX - Vc backend  
Detector: Pb/PbWO4  
Model for Energy Range [80GeV-100TeV]  
Vectorized, #baskets: 256

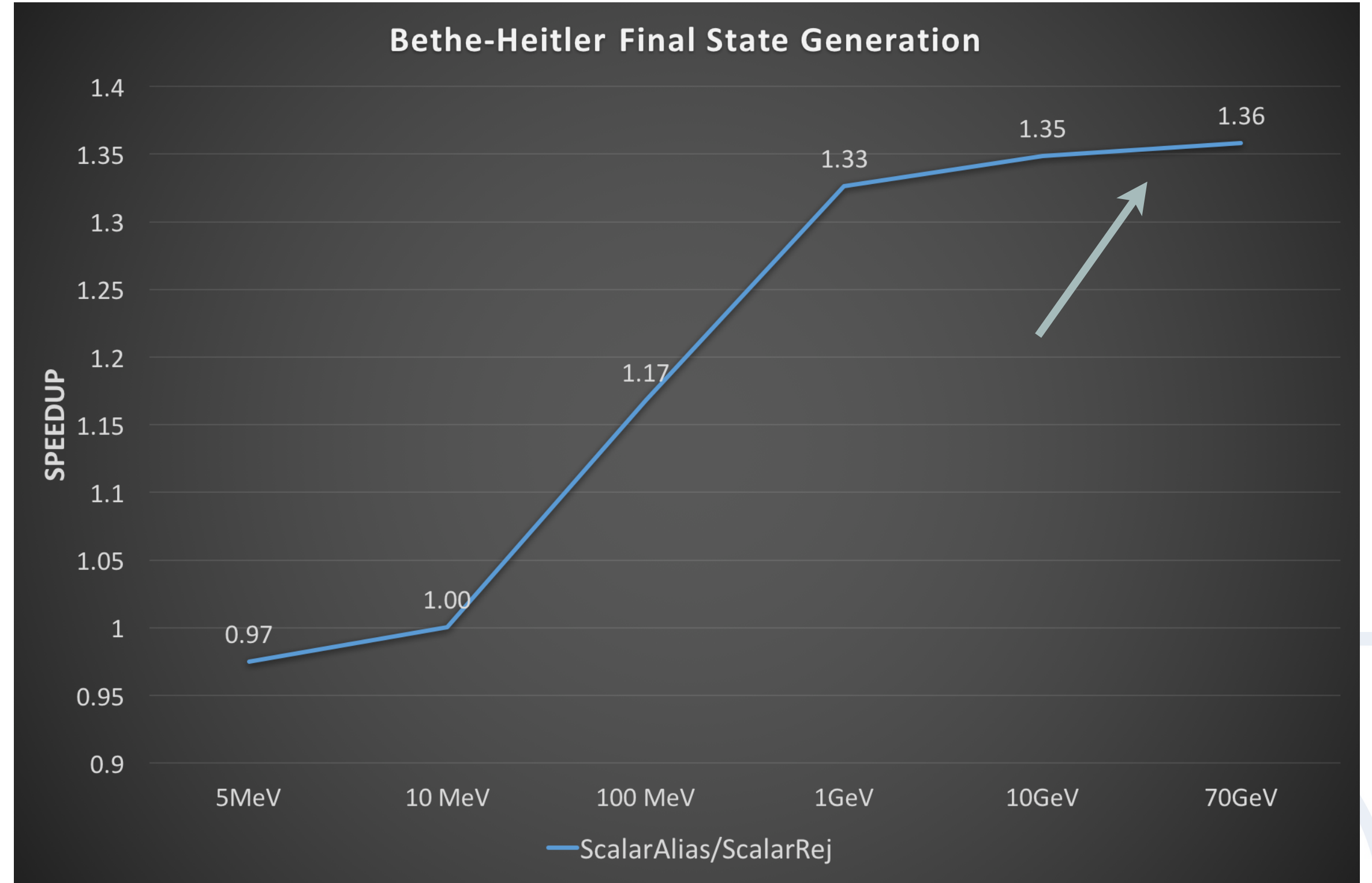


Specs: Haswell core i7 - AVX - Vc backend  
Detector: Pb  
Model for Energy Range [100eV-80GeV]  
Scalar execution

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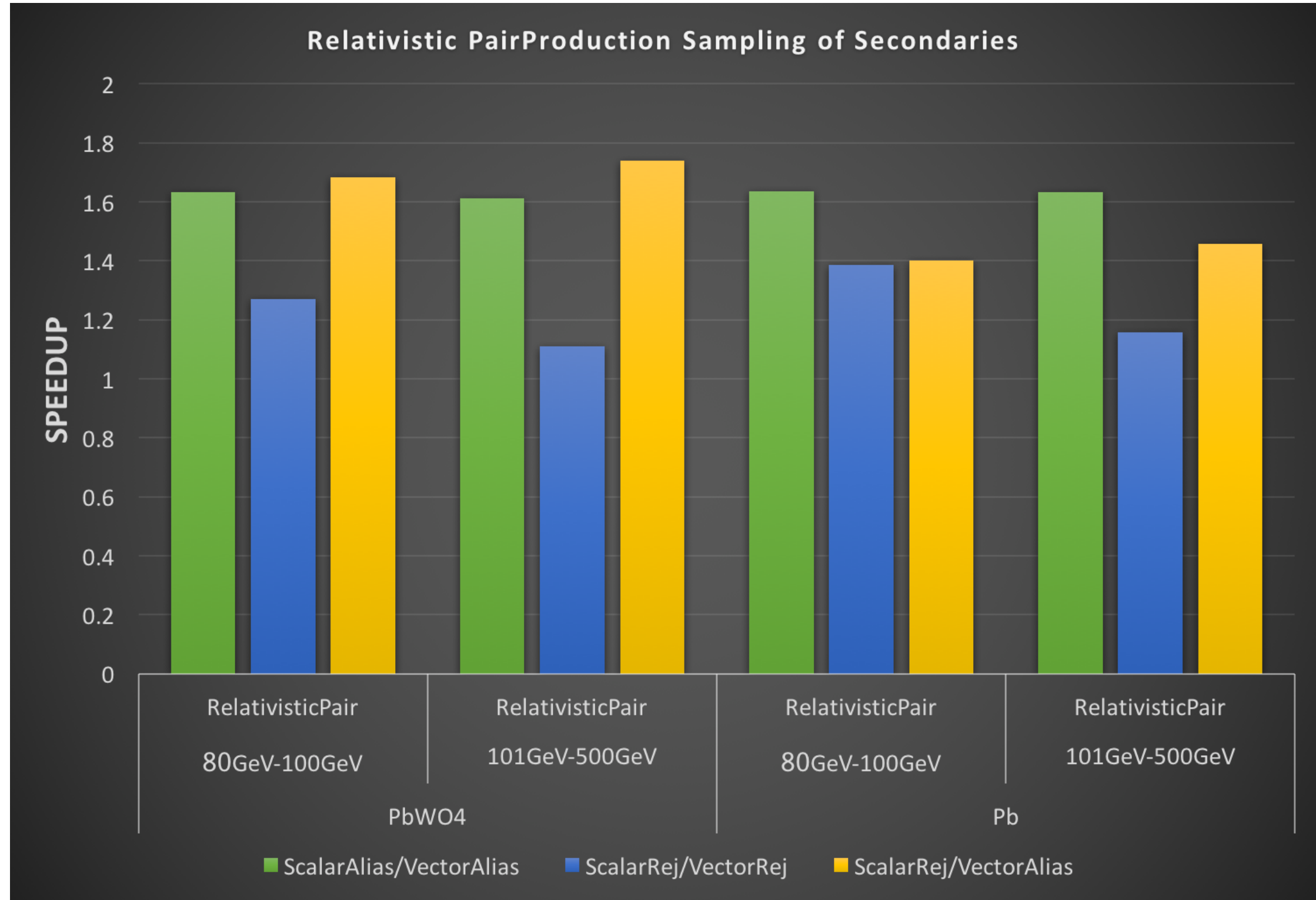
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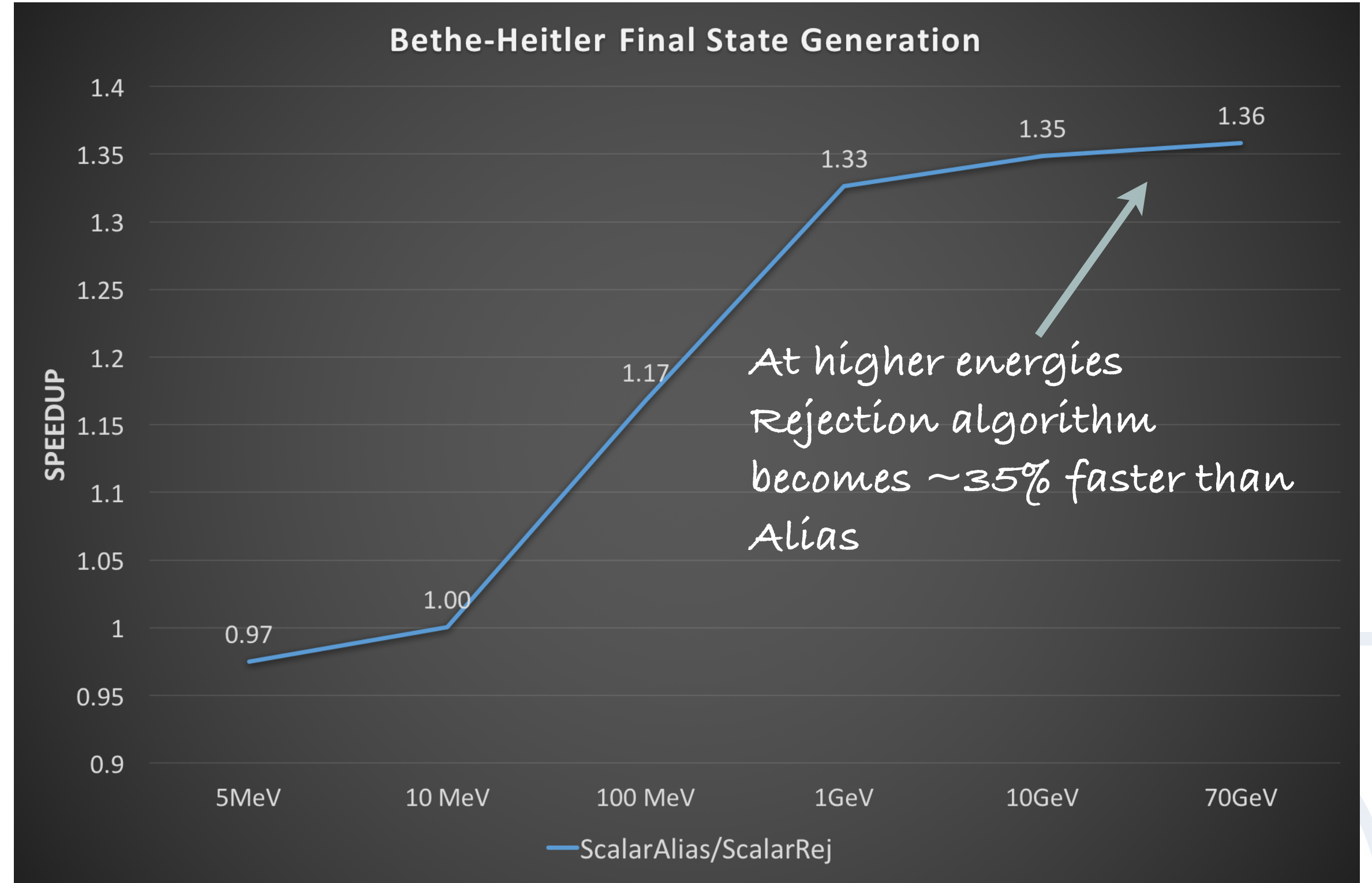
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- EM showers can be **fully simulated** in GeantV
  - All the EM models are now **vectorized**
- **SpeedUp : there is no generic solution**
  - Final-state EM Model level: between **1.5-3** on Haswell, **2-4** on Skylake with AVX2
  - See [talk](#) from A. Gheata for the impact on realistic EM showers in calorimeters and fullCMS applications



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## WORK IN PROGRESS



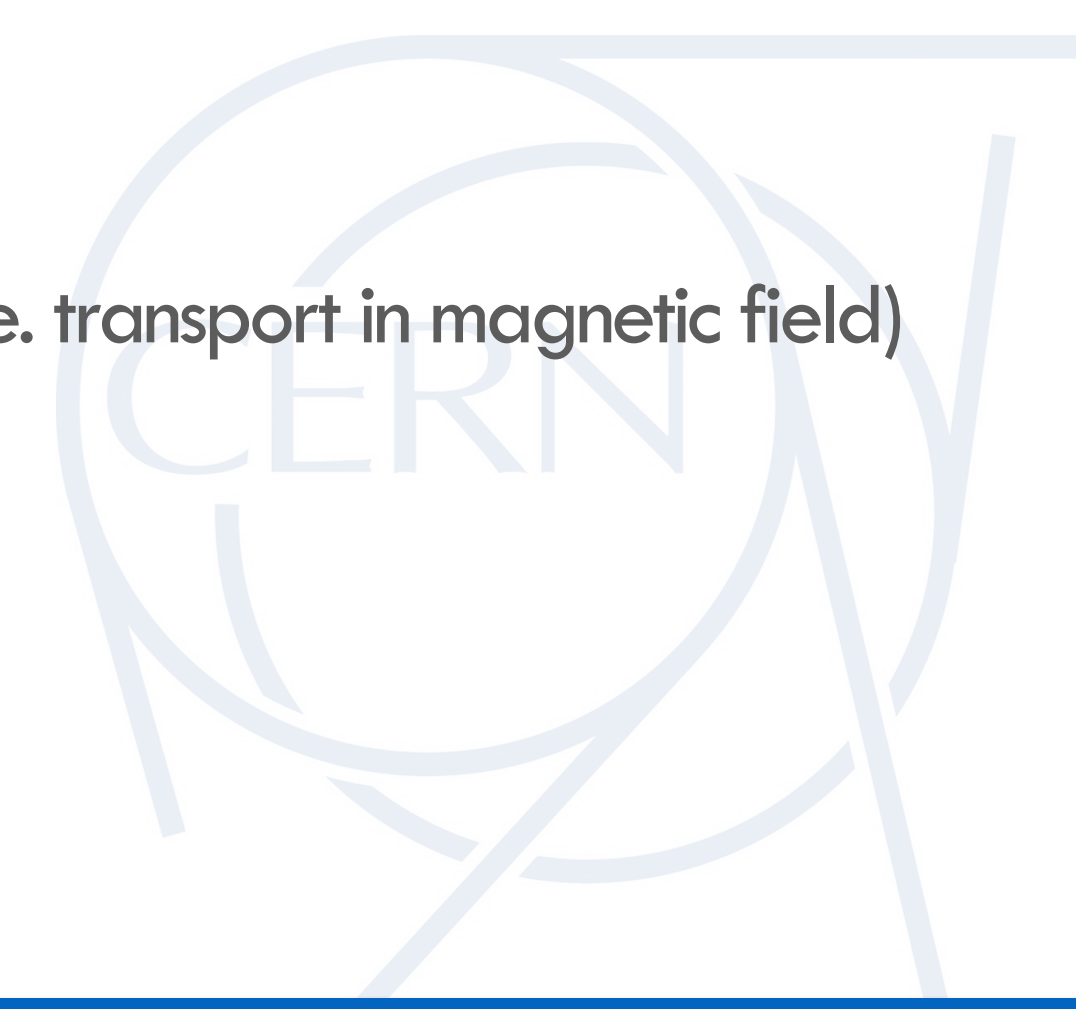
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## WORK IN PROGRESS

- Work on **other parts** of the physics framework
- **VecMath library** and **Vectorized pRNG** (handling reproducibility issues)
- Study the possibility to substitute **double precision** computations with **single** one, in some parts of the physics library (i.e. transport in magnetic field)
- Add **AVX512** support (UME::SIMD)



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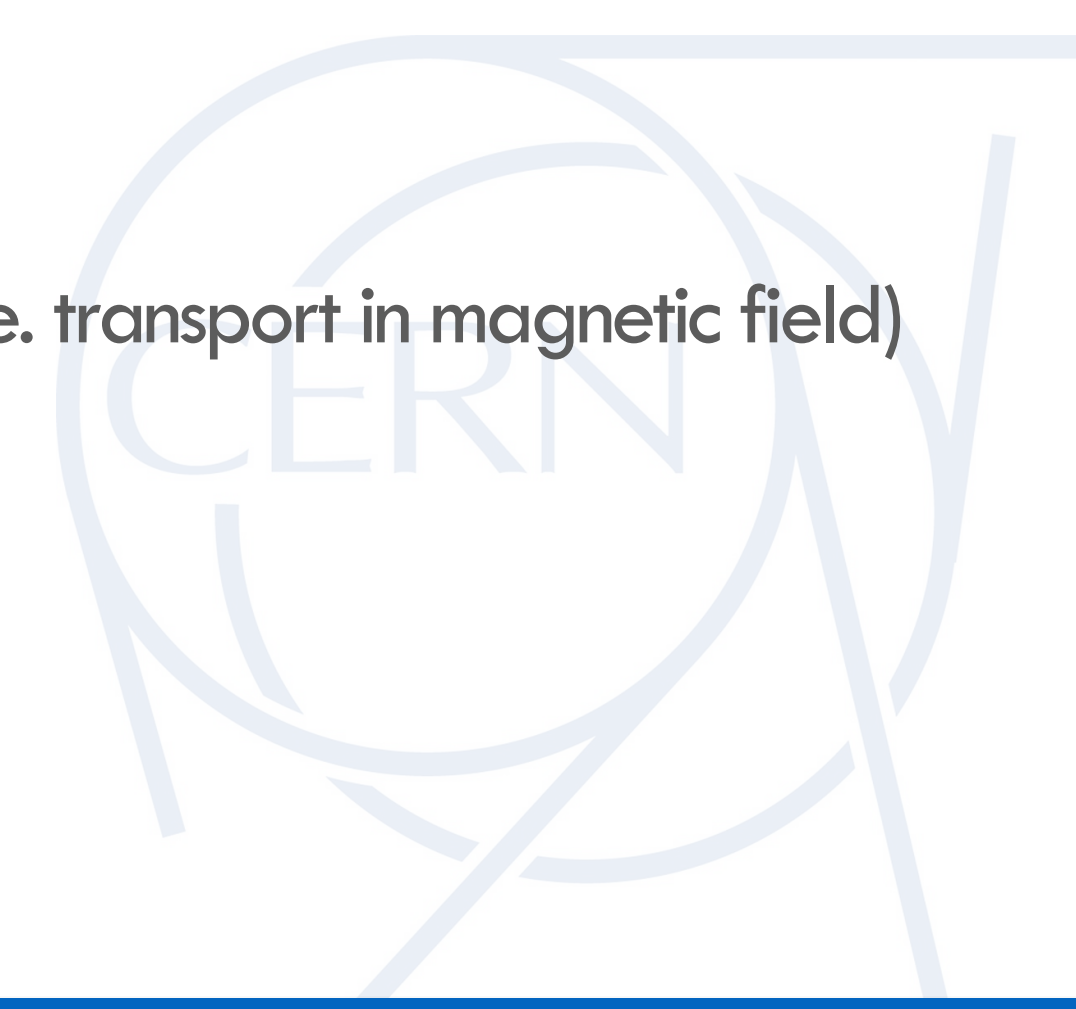
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GeantV project is hosted at: <https://gitlab.cern.ch/GeantV/geant>  
GeantV website: <http://geant.cern.ch>





# THANKS FOR THE ATTENTION!



## QUESTIONS?



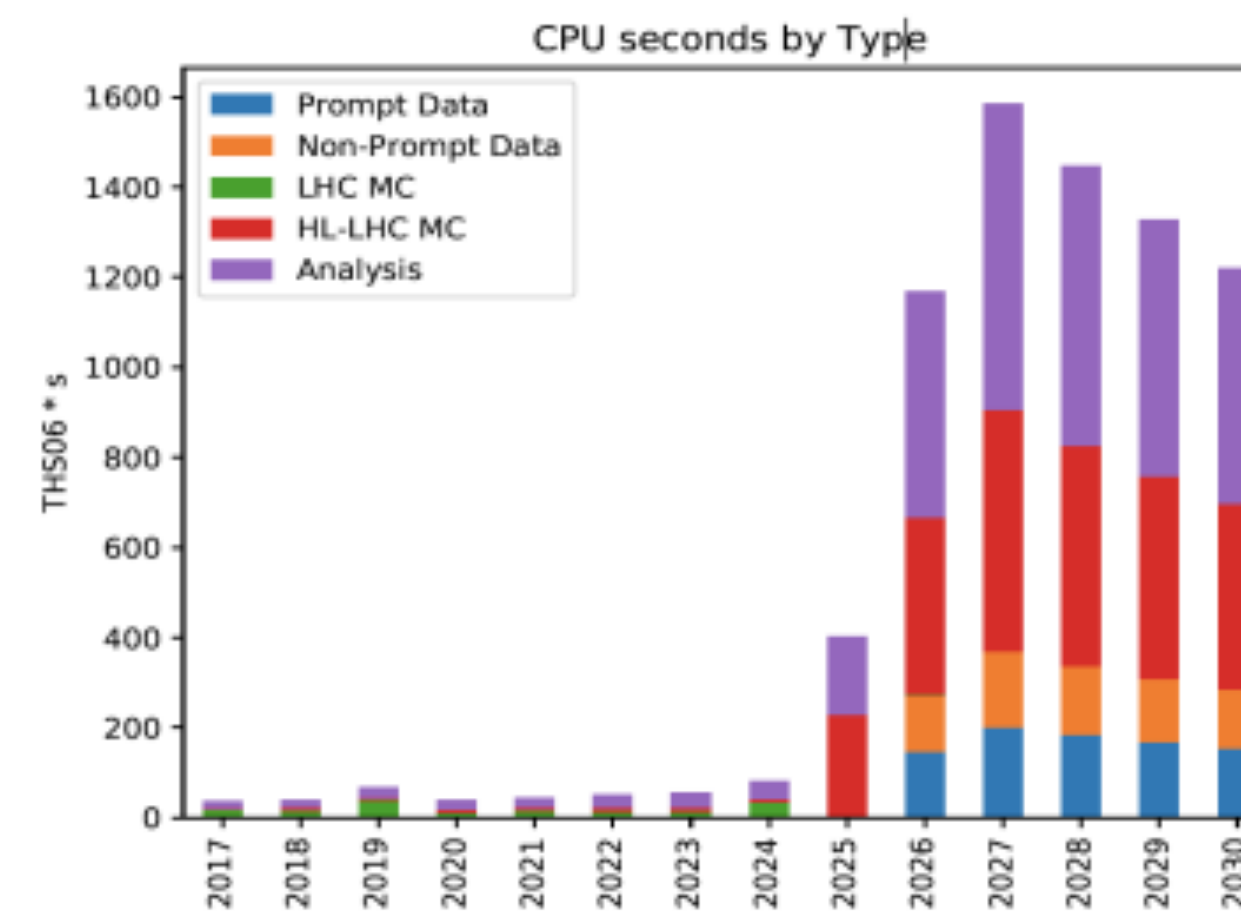
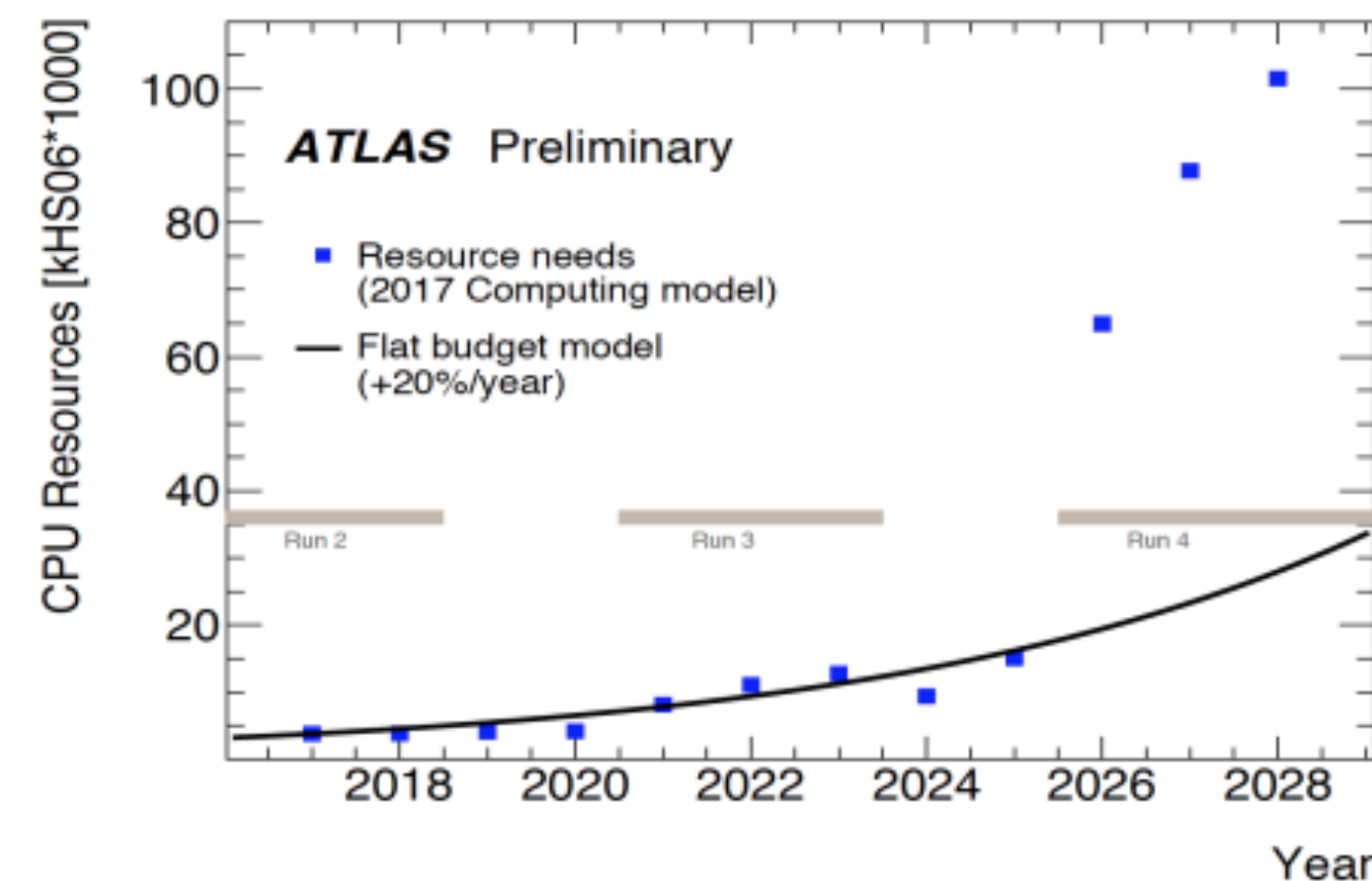
# BACKUP



# NEED FOR FASTER SIMULATION CODE FOR HEP COMMUNITY

- During the first two runs, the LHC experiments produced, reconstructed, stored, transferred, and analysed **tens of billions** of simulated events
- As part of the high-luminosity LHC physics program (HL-LHC), the upgraded experiments expect to collect **150 times more data** than in Run 1
- More than **50%** of WLCG power used for simulations
- **GeantV**: path towards a faster toolkit **2-5 x Geant4**

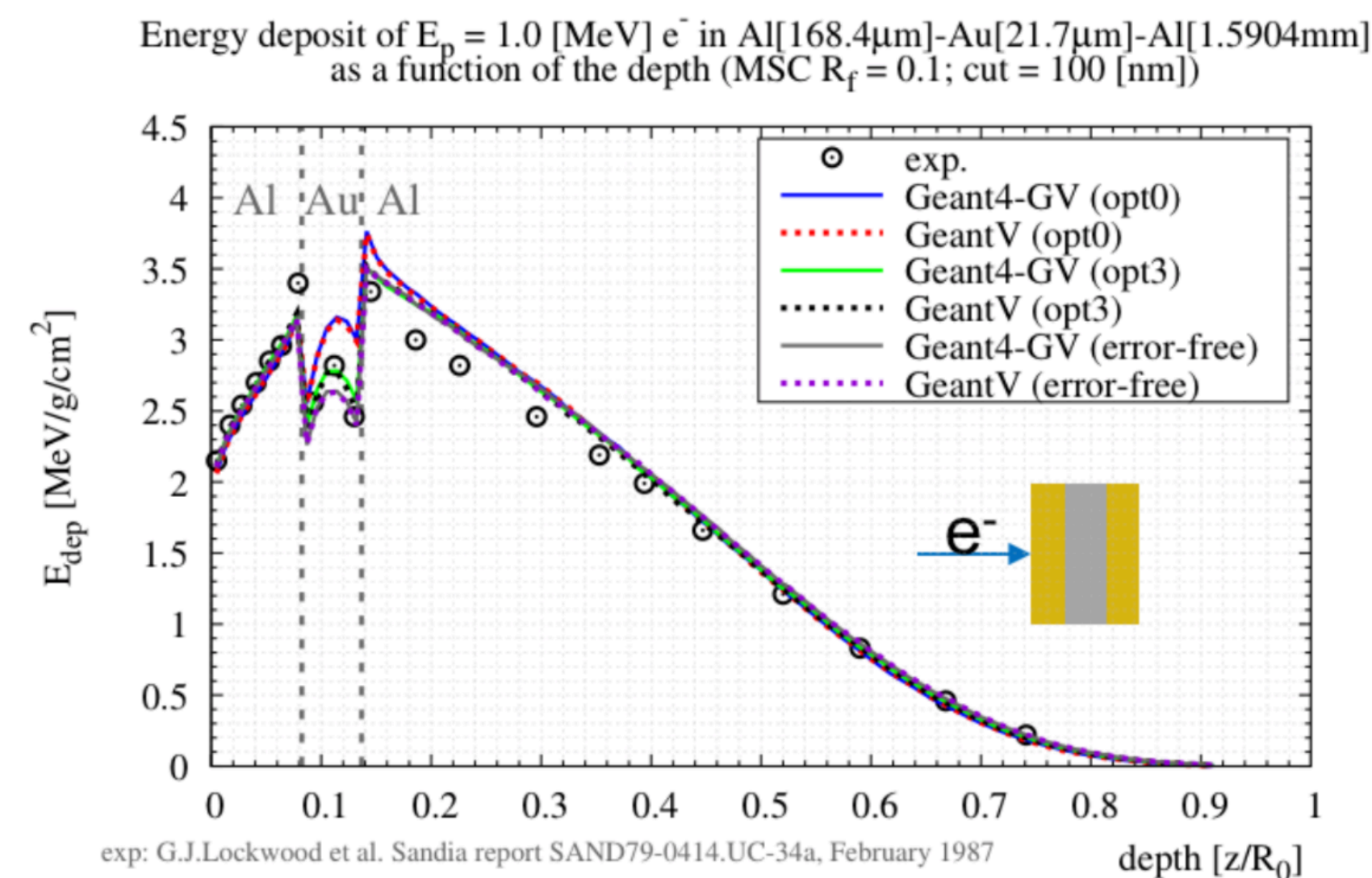
Estimated ~10x CPU needs for the HL-LHC era



CMS and Atlas estimated CPU needs for HL-LHC (source: CWP)



# EM PHYSICS MODELS VALIDATION



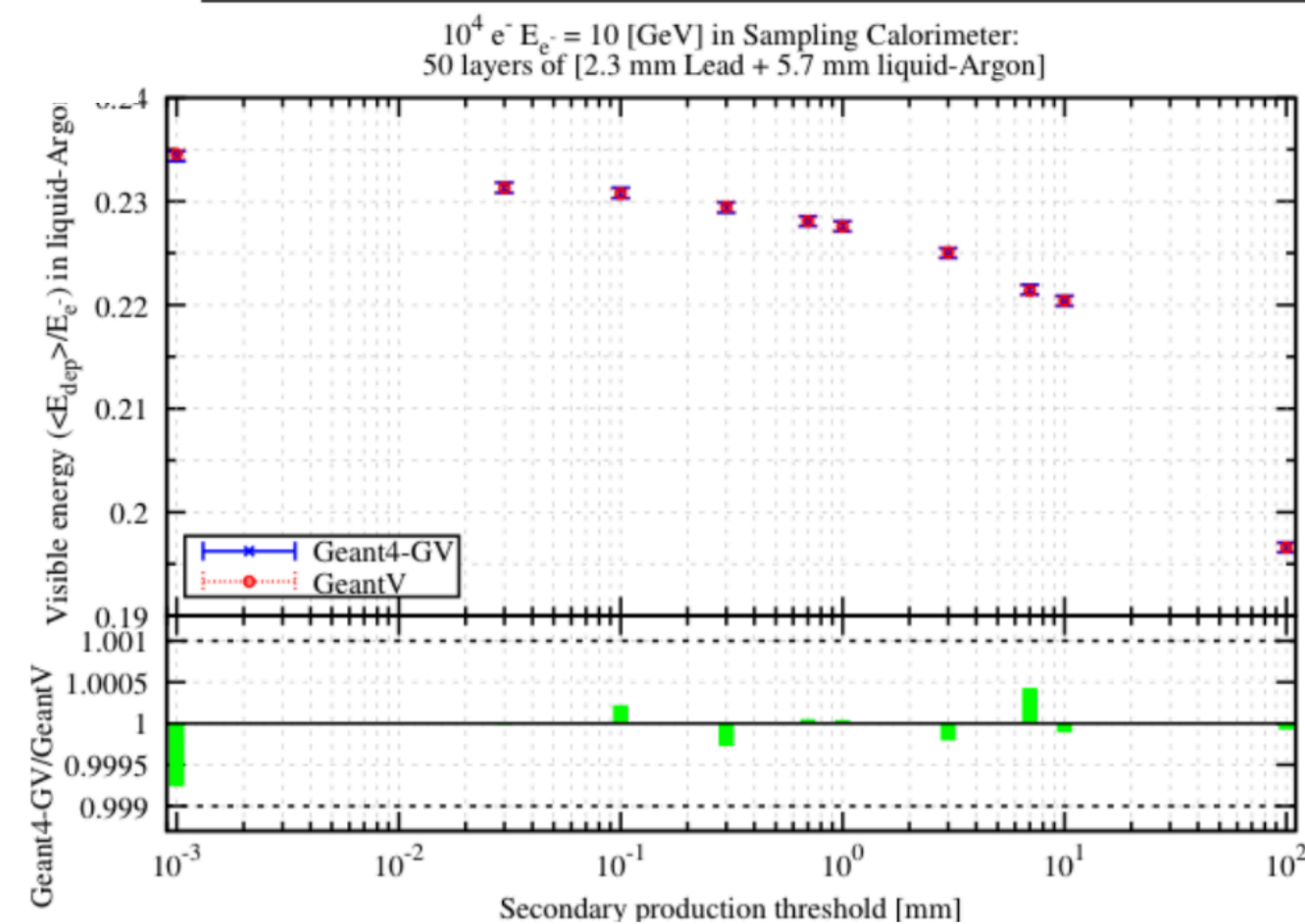
Multi-layered target

Work in progress on vectorization of all the EM physics - expected to be included in the beta release!

Scalar EM models revisited in a vectorization friendly way (e.g. vectorizable sampling) and validated against Geant4 version.

$10^5$  1 [GeV]  $e^-$  in ATLAS bar. simpl. cal. : 50 layers of [2.3 mm Pb + 5.7 mm lAr]; p.cut = 0.7 [mm]

	$e^-/e^+$ : ionisation, bremsstrahlung, msc; $\gamma$ : Compton, conversion							
	GeantV				Geant4			
material	$E_d$ [GeV]	rms [MeV]	tr.l. [m]	rms [cm]	$E_d$ [GeV]	rms [MeV]	tr.l. [m]	rms [cm]
Pb	0.69450	15.198	51.015	1.189	0.69448	15.234	51.016	1.192
lAr	0.22792	14.675	106.11	7.592	0.22796	14.656	106.13	7.582



Mean number of :

gamma	405.87	406.15
electron	9411.49	9419.44
positron	53.77	53.71
charged steps	11470	11476
neutral steps	49177	49222

credit: M. Novak

ATLAS simplified sampling calorimeter



# MAXIMUM SPEEDUP ACHIEVABLE

---

- Depends on the **vector width** but..
- Generally **is less than the vector register width**
  - some operations are **slower** for vector registers

Reciprocal Throughput\* for Division DP (SandyBridge)

Scalar	10-20 cycles
Vector	20-44 cycles

- Maximum speedup for division will be  $\sim 2$  for this CPU
  - **Overhead** payed to gather data into SIMD vectors
- Another important factor is the **number of execution units** for particular instructions = number of instructions that can be executed simultaneously.

\*The average number of core clock cycles per instruction for a series of independent instructions of the same kind in the same thread.

\*\*

# RESULTS: MODEL LEVEL TEST BENCHMARKS

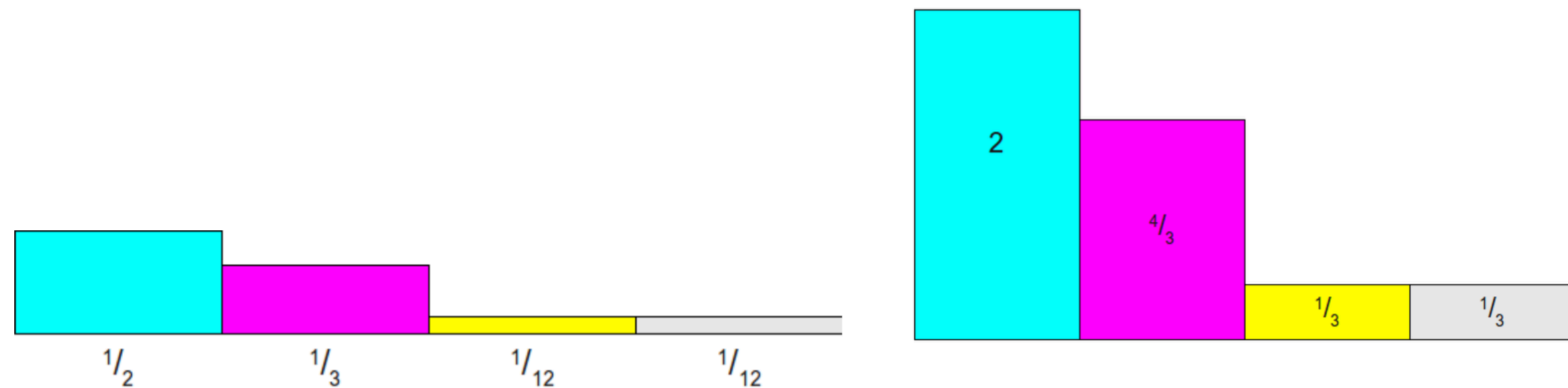
Model	Haswell (avx)	
	Scalar Time [ms]	SpeedUp
Klein-Nishina alias	56.4	2.2
Klein-Nishina rej	48.37	2.21
Moller-Bhabba alias	51.32	1.85
Moller-Bhabba rej	50.21	1.62
Seltzer-Berger brems alias	73.19	1.98
Seltzer-Berger brems rej	106.63	1.64
Relativistic brems alias	76.96	2
Relativistic brems rej	330.57	2
Bethe-Heitler pair alias	86.53	1.82
Bethe-Heitler pair rej	62.98	1.39
Relativistic pair alias	91.66	1.37
Relativistic pair rej	83.42	1.83
Positron2Gamma alias	60.78	2.23
Positron2Gamma rej	41.34	1.91
Sauter-Gavrila alias	66.4	1.45
Sauter-Gavrila rej	108.89	1.2

Test with Lead, #baskets: 256



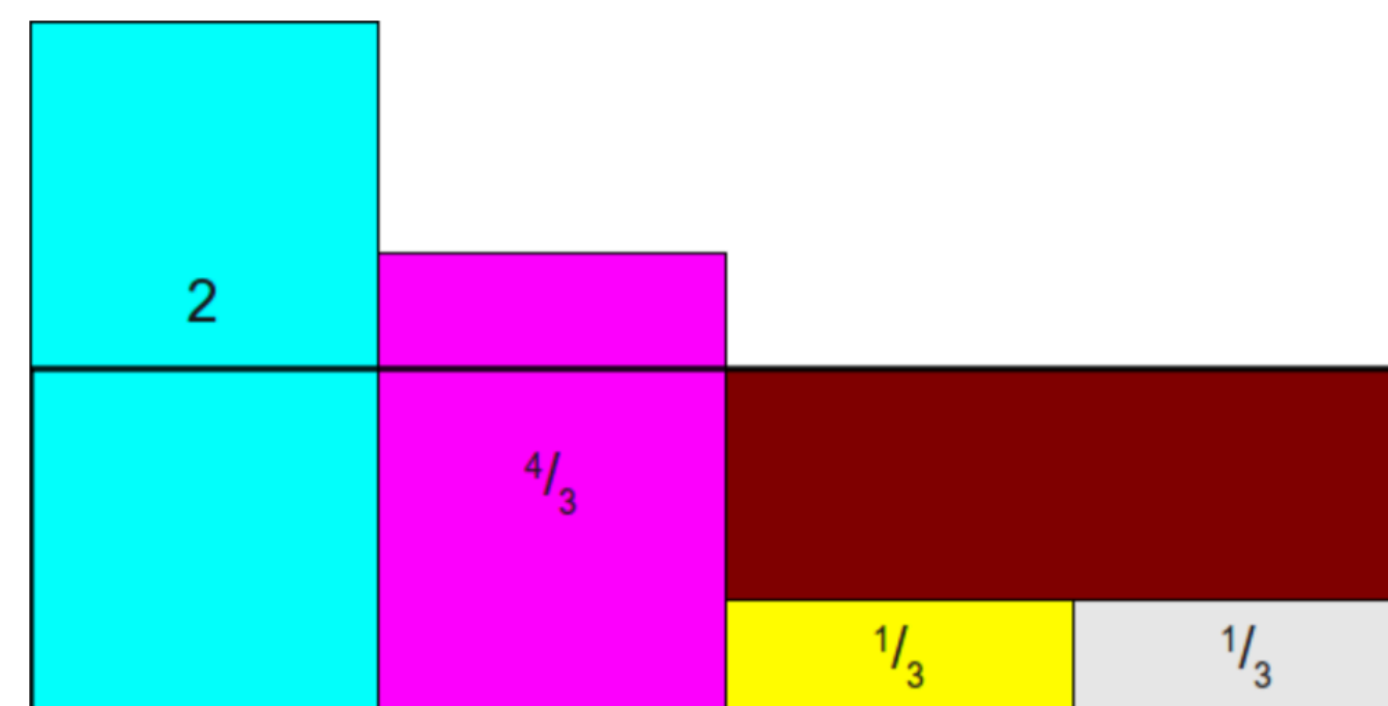
# ALIAS SAMPLING

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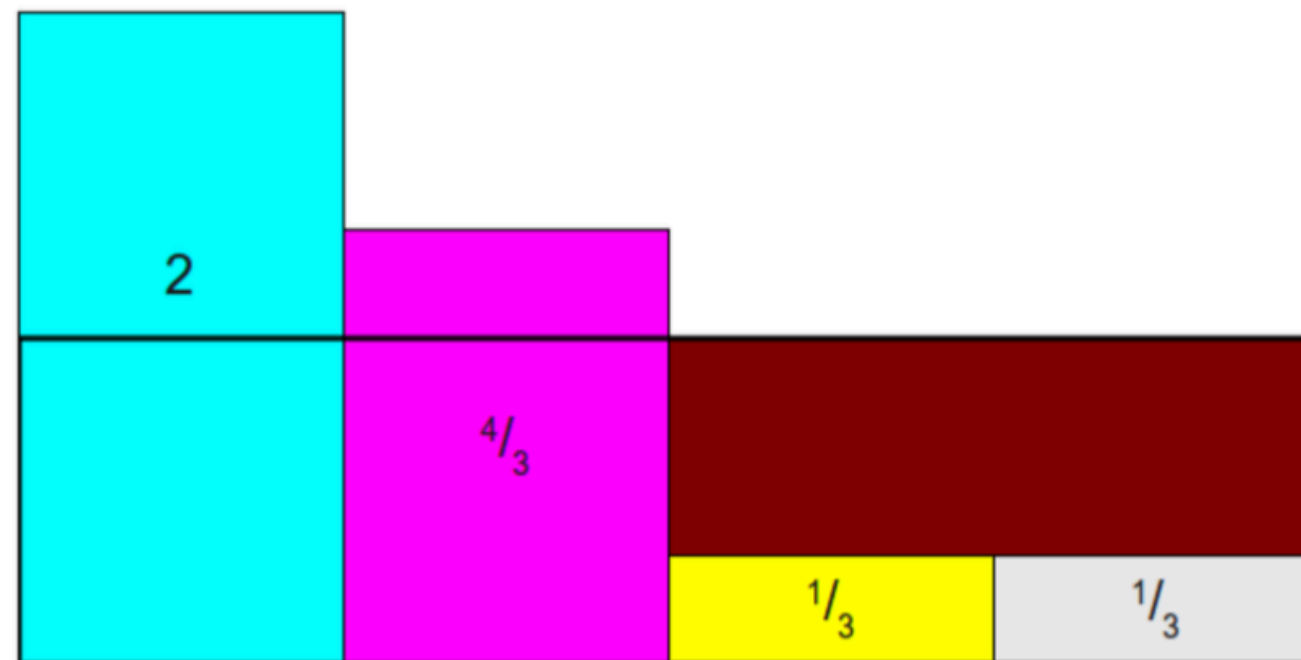
Initial pdf (equal likelihood=1/4)

Scaled probabilities so that a prob of 1/4 would weight 1



# ALIAS SAMPLING

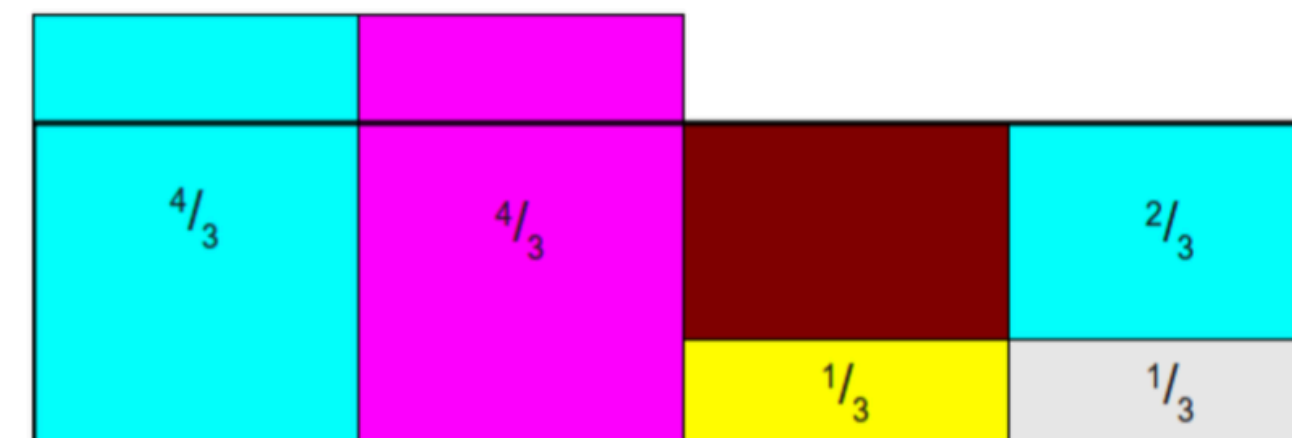
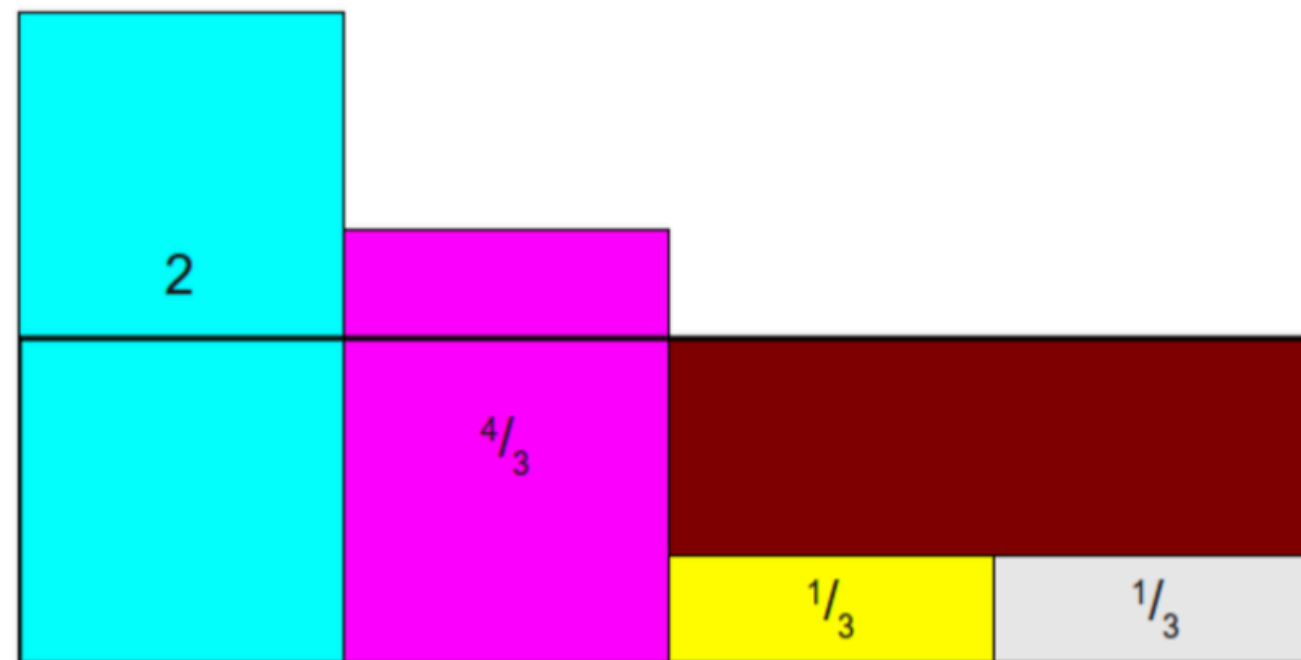
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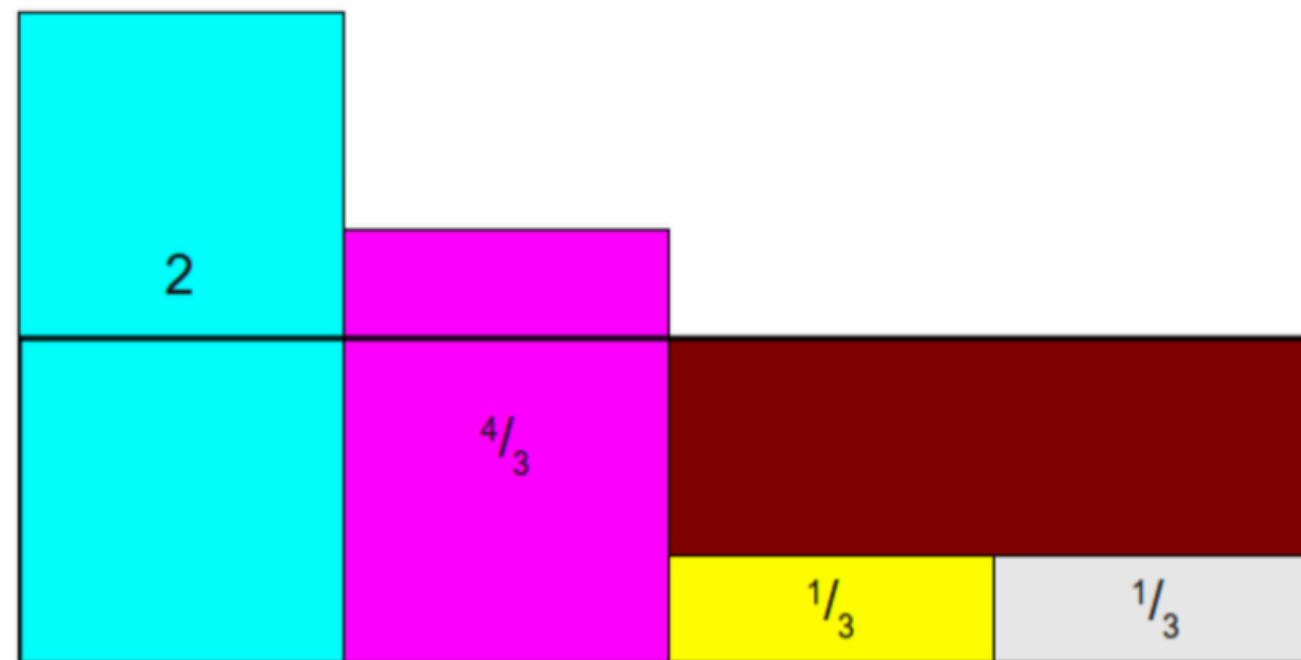
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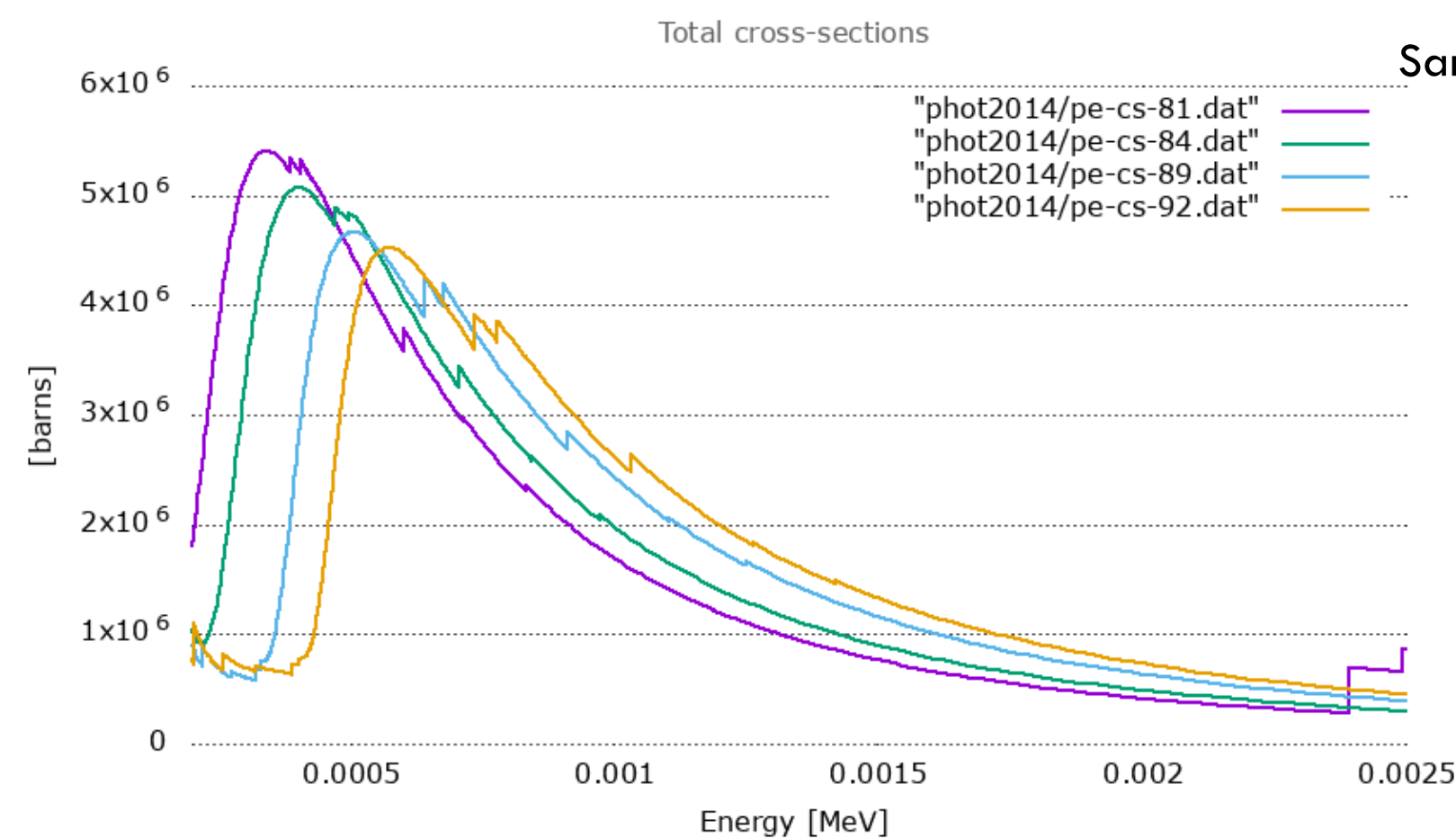
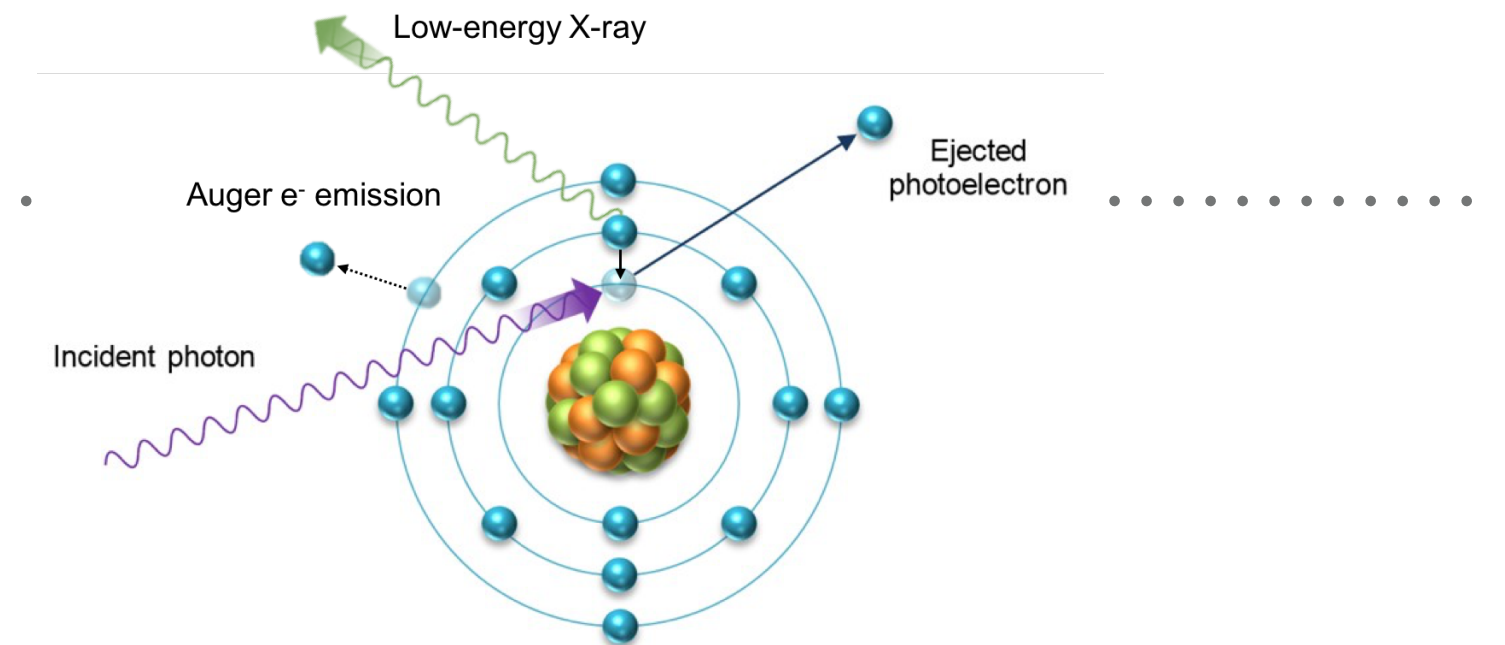
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Alias Probability

# EXAMPLE: PE EFFECT

- Photoelectric effect total cross-section is not an easy function
  - Fit in two different energy ranges, but not below k-shell binding energy
    - Tabulated cross-sections left for low energies
  - For the final state sampling one need to sample
    - the angle: described by the SauterGavrila differential cross-section
    - the subshell: This is going through a binary search algorithm (not vectorizable) + linear or spline interpolation



Sampling of the shell

KinE

Z

LET

Linear Interpolation

HET

Spline Interpolation

LEP

Parameterization (Polinomial fit)

HEP

Parameterization (Polinomial fit)

BINARY SEARCH OVER  
DIFFERENT TABLES  
(PER Z, PER SHELL)

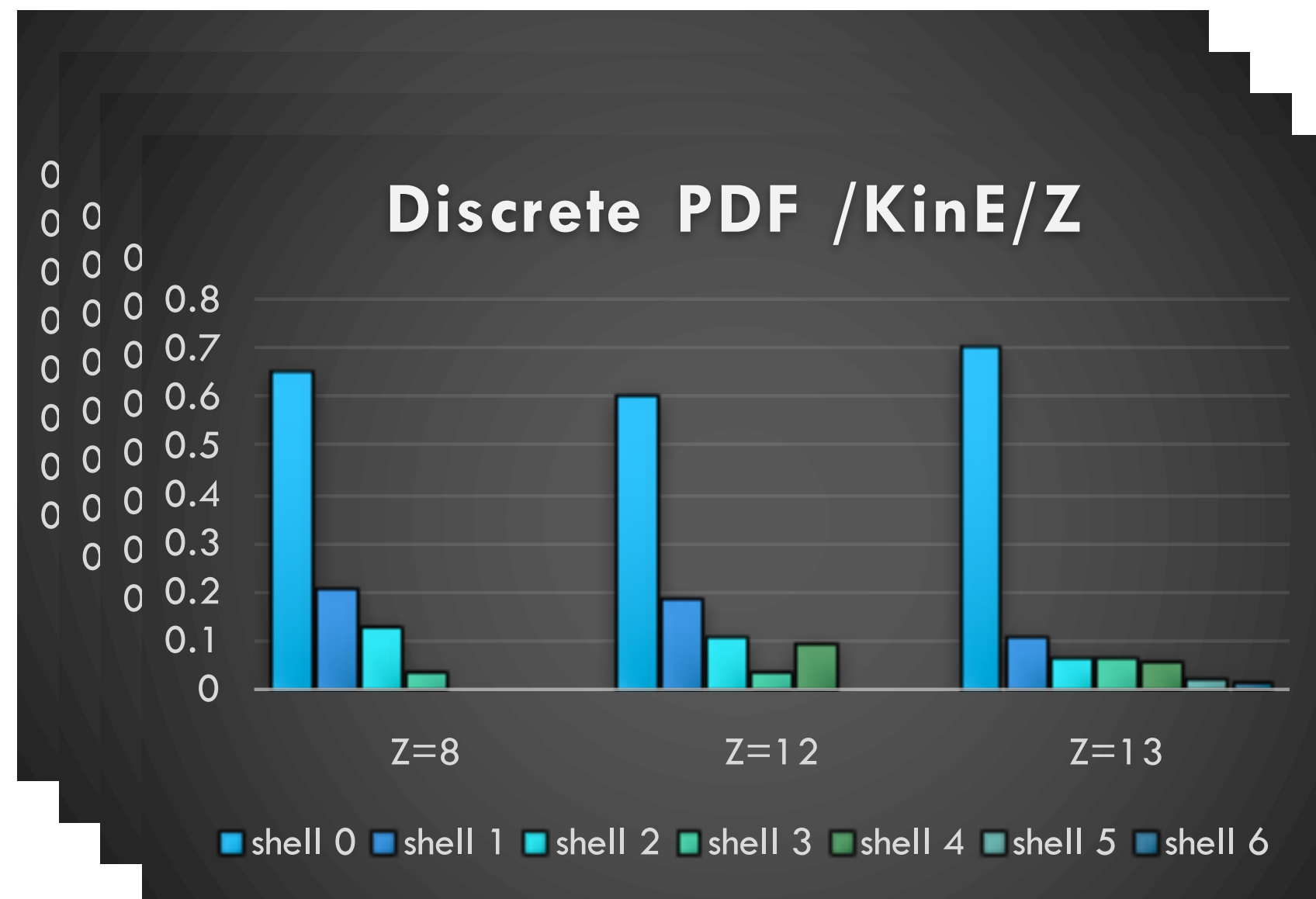
FETCH OF PARAMETERS  
(PER Z, PER SHELL)

Not easily  
vectorizable!

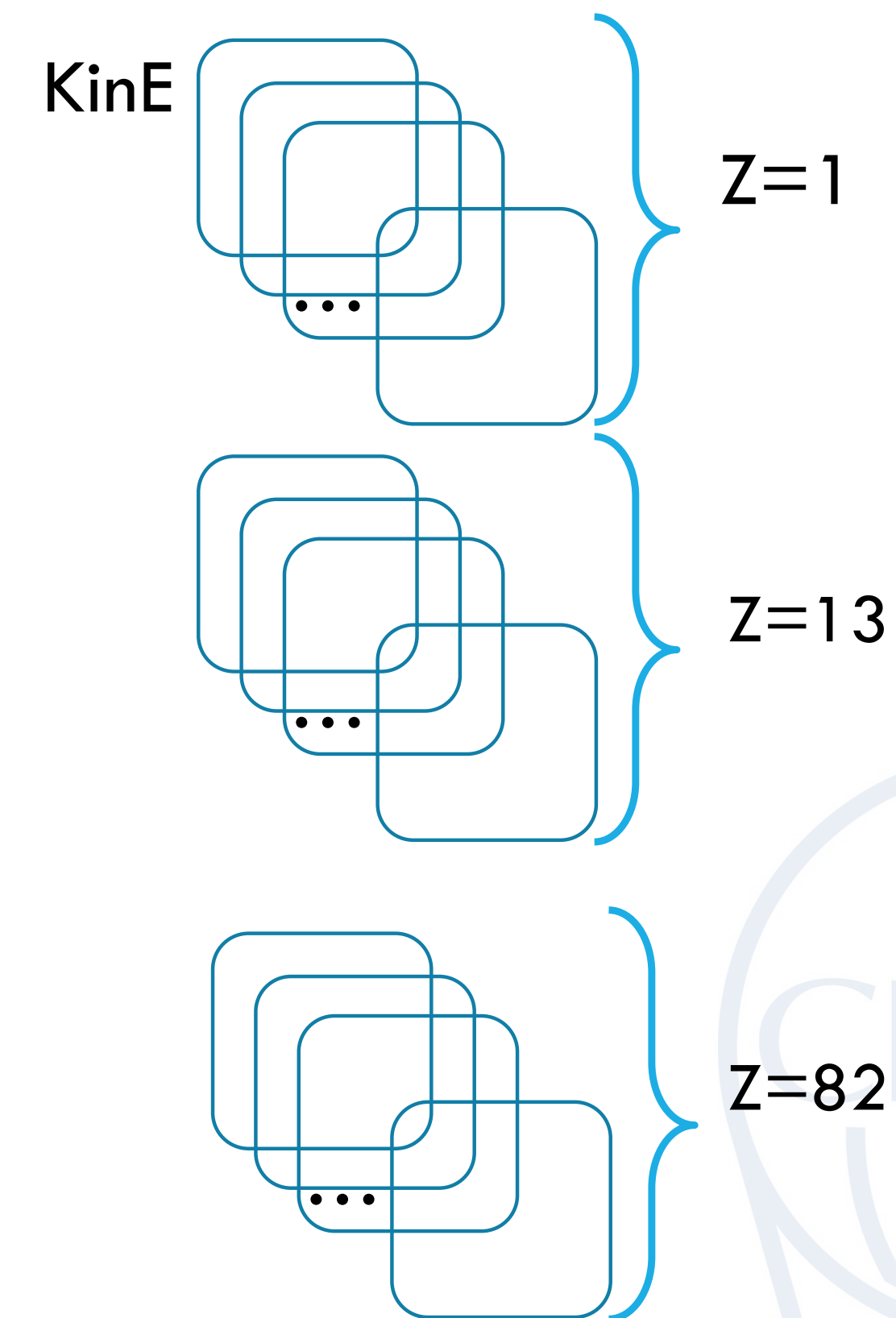
Not easily  
vectorizable!

Additional filtering of particles

# VECTORIZATION WITH DISCRETE ALIAS TABLES



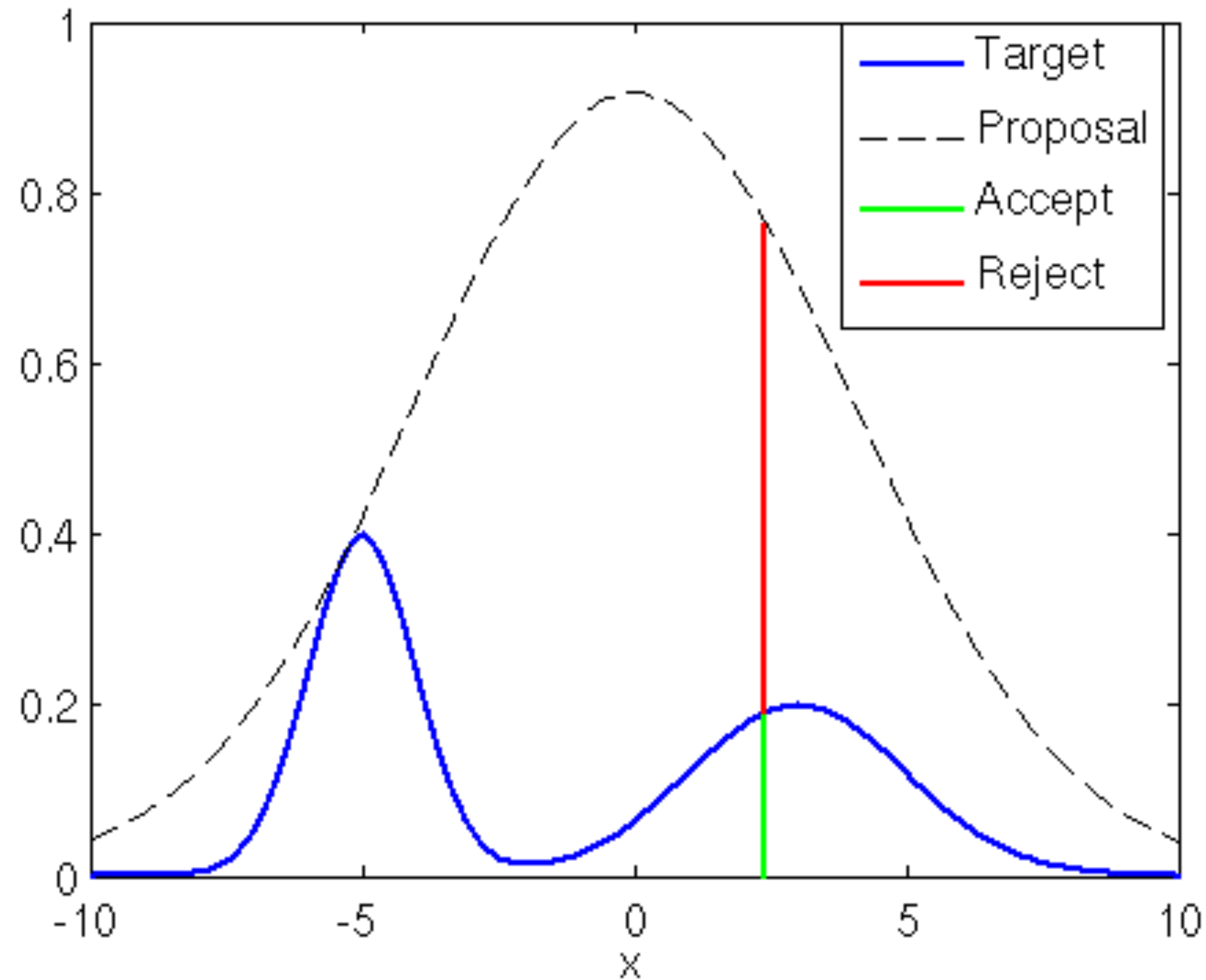
ALIAS TABLE FOR DISCRETE DISTRIBUTION



- We generated a denser ss-cs dataset
  - to build equally spaced (in energy) discrete PDFs for each element (linearly interpolated)
  - From them we can build Alias Table
    - PRO: sampling of shells with only one case
    - CONS: Gathering operations



# REJECTION SAMPLING



# VECTORIZATION OF REJECTION SAMPLING

.....



# VECTORIZATION OF REJECTION SAMPLING

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- 1 Prepare values that are needed for sampling, in form of arrays



# VECTORIZATION OF REJECTION SAMPLING

- 1 Prepare values that are needed for sampling, in form of arrays

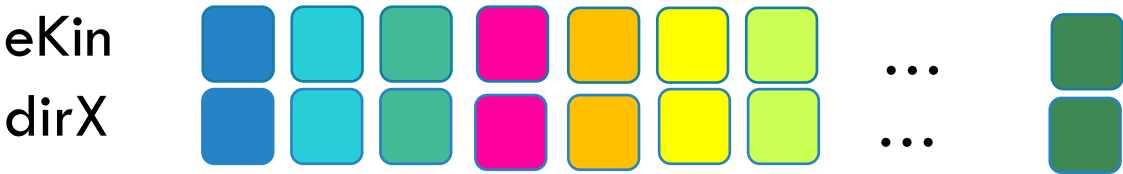
eKin     ... 





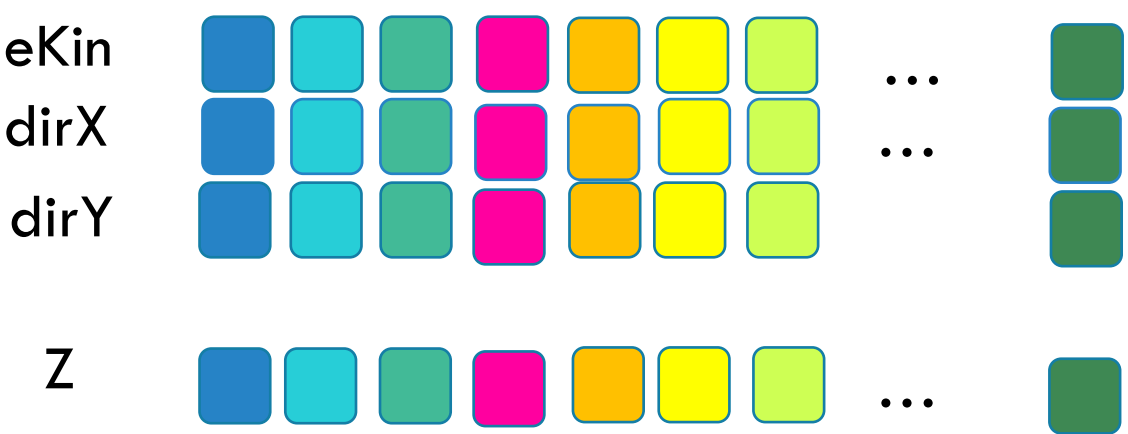
# VECTORIZATION OF REJECTION SAMPLING

1 Prepare values that are needed for sampling, in form of arrays



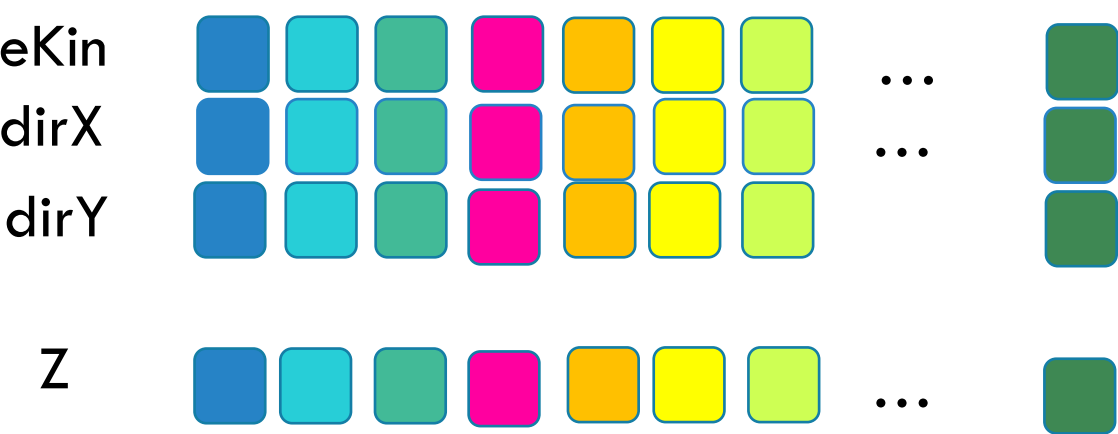
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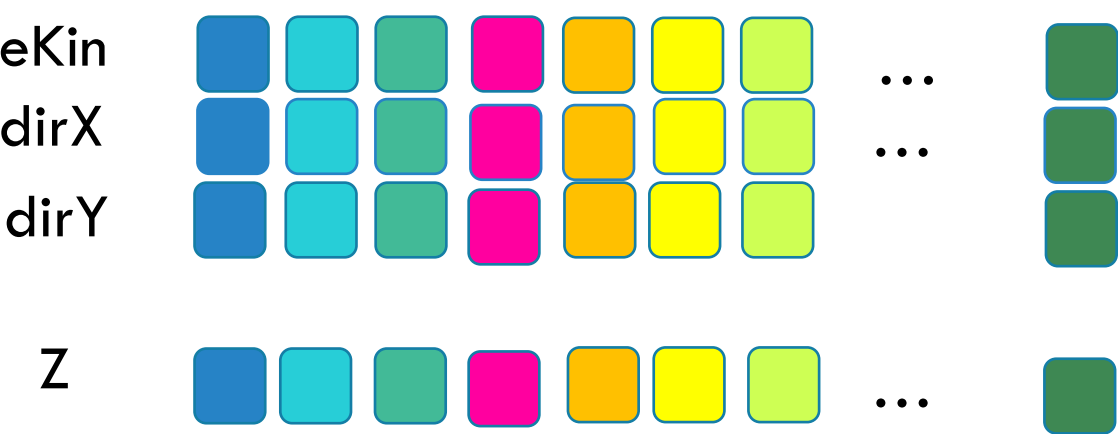
2

Store in SIMD vector the indexes of the current tracks that have to be sampled



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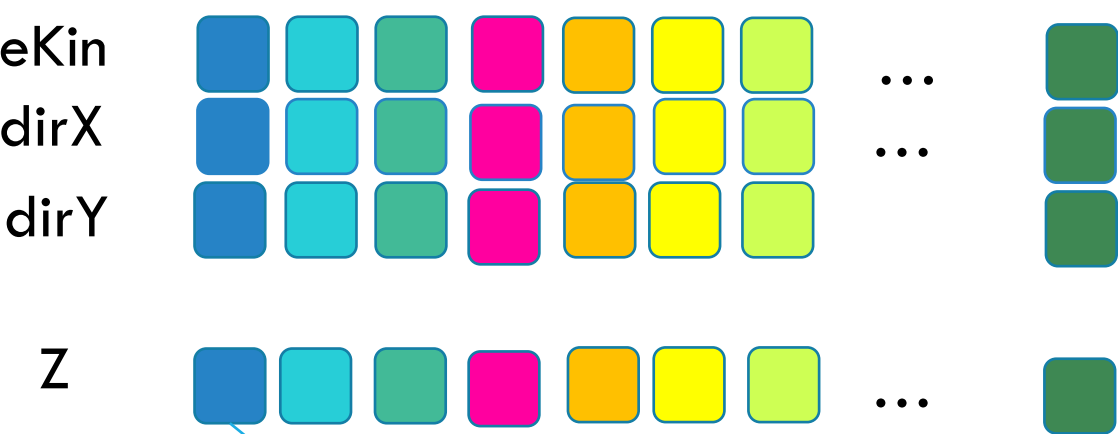
Store in SIMD vector the indexes of the current tracks that have to be sampled





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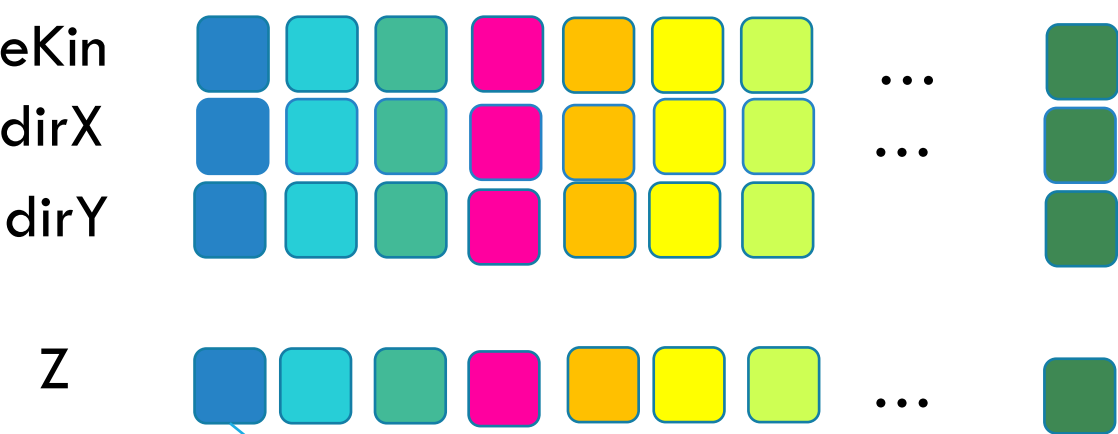


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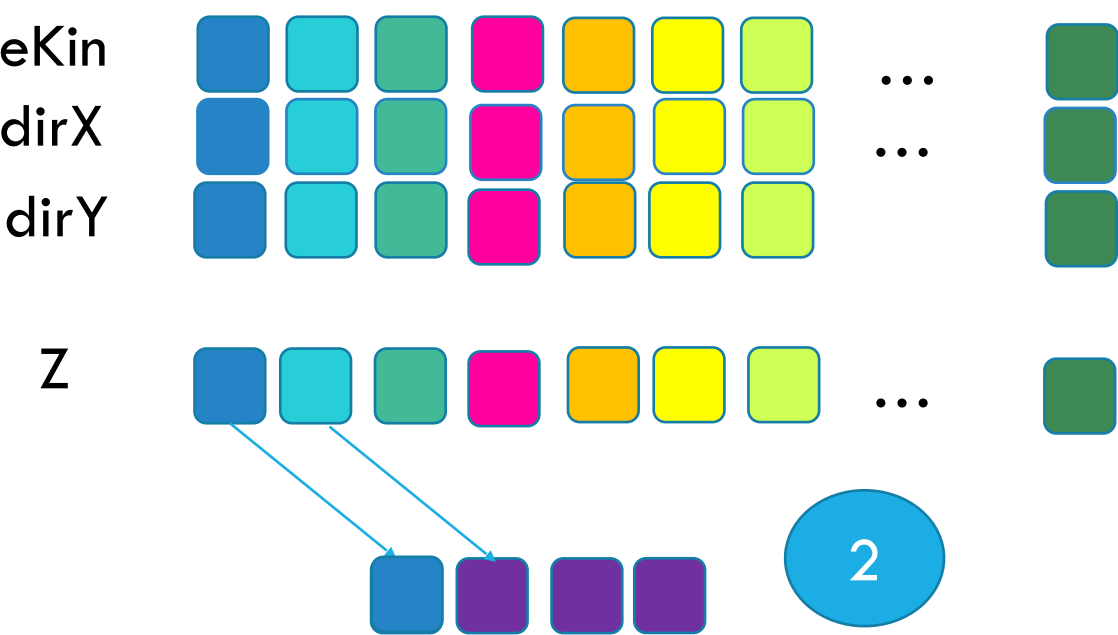


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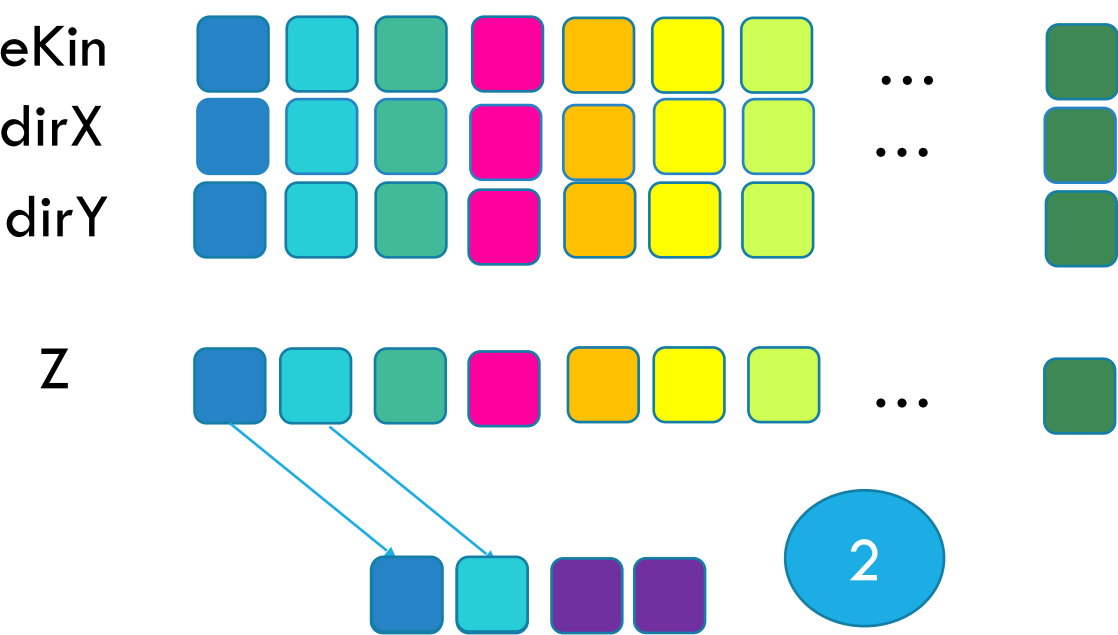


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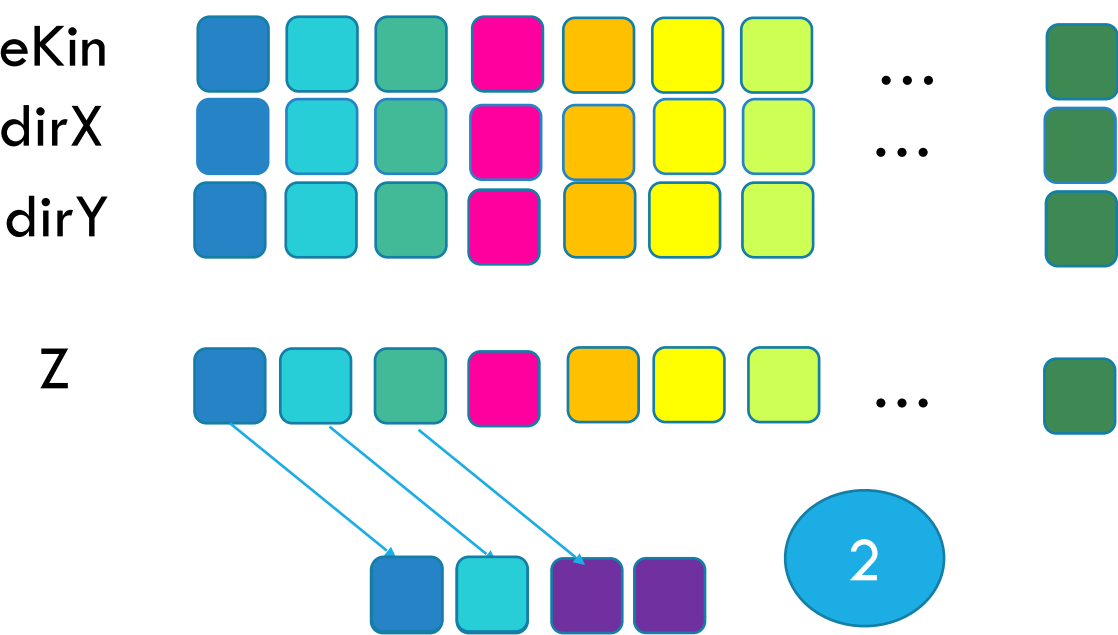
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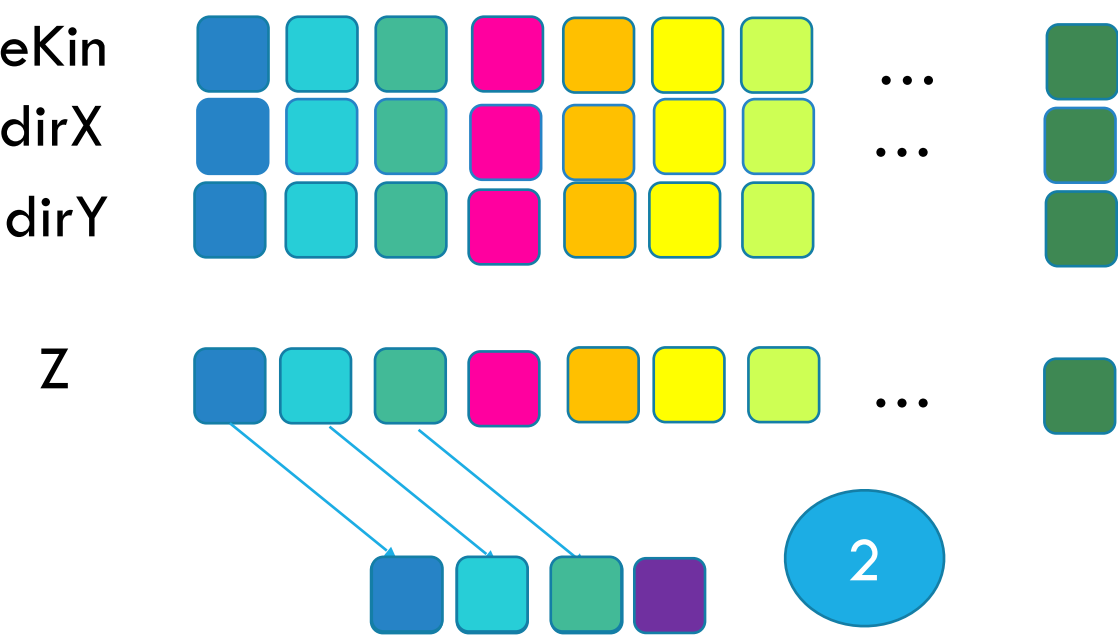


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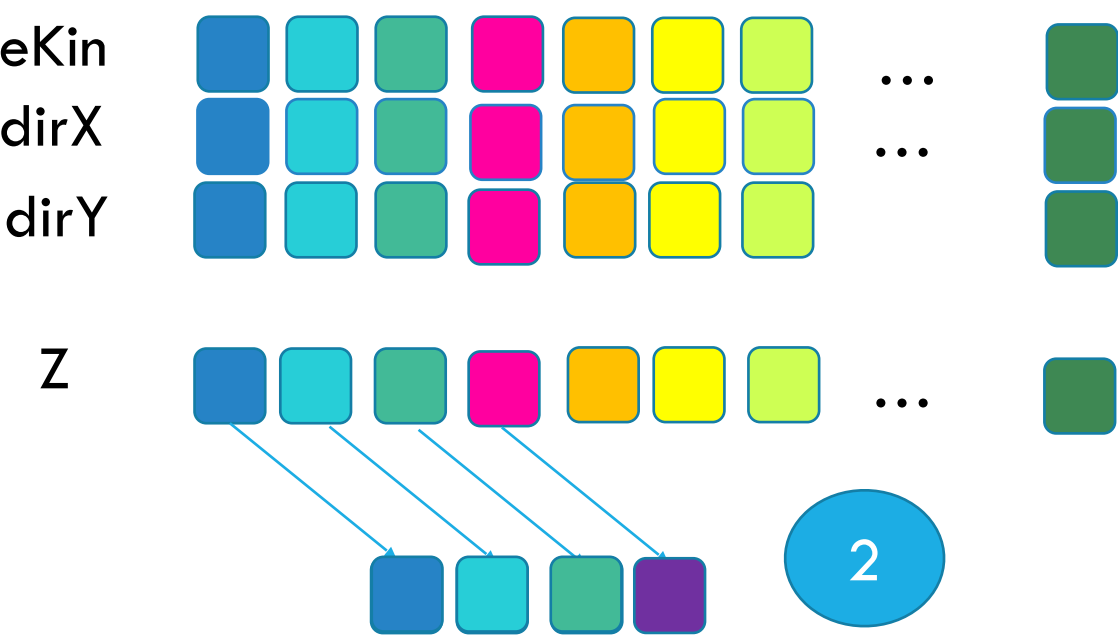


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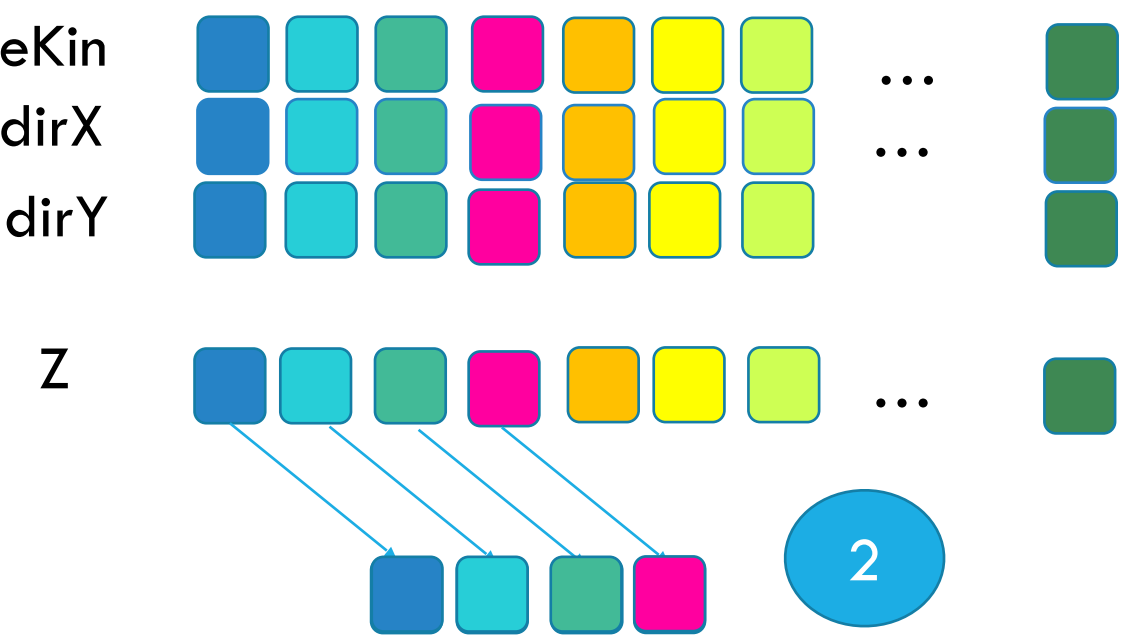


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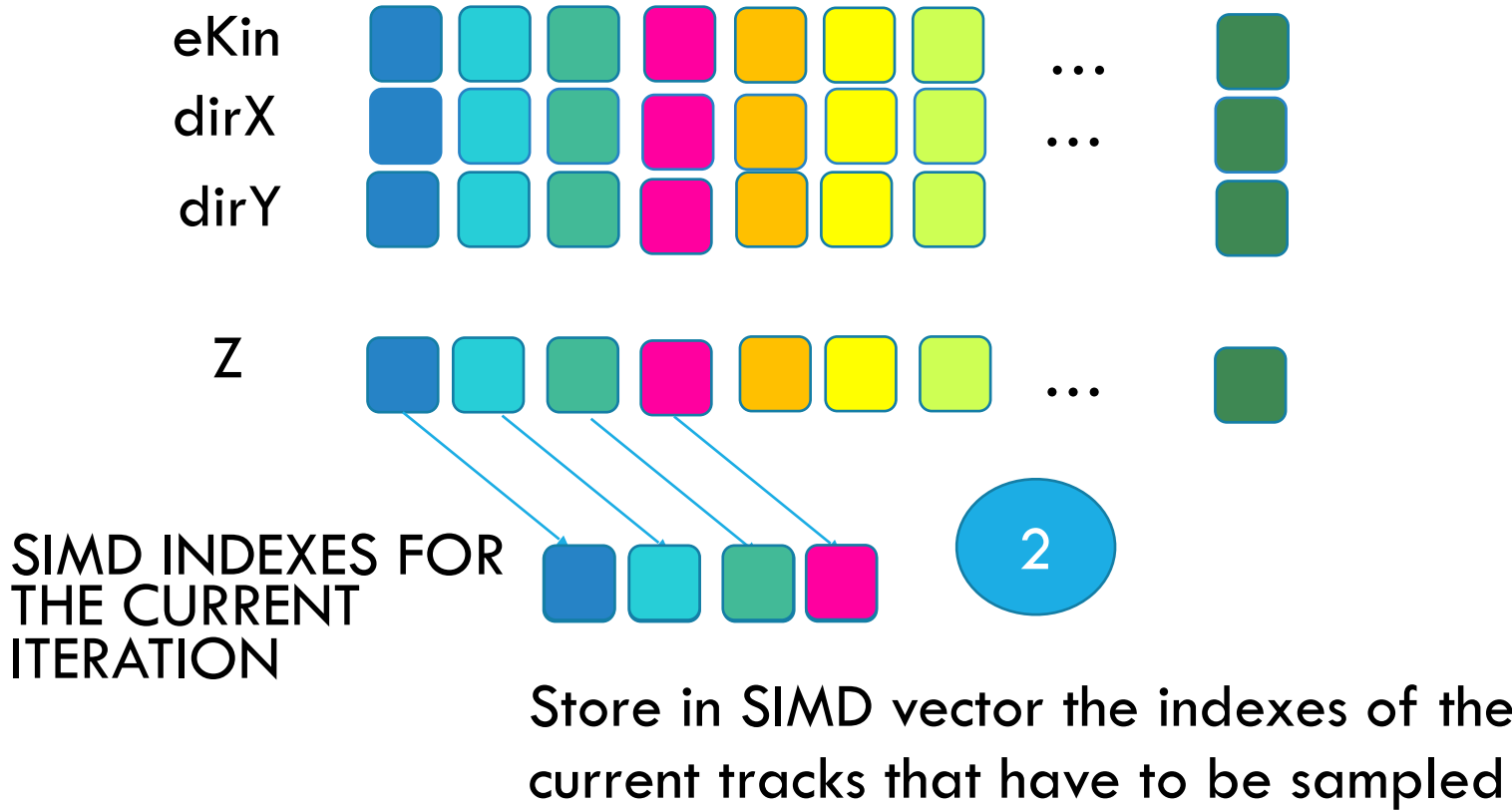
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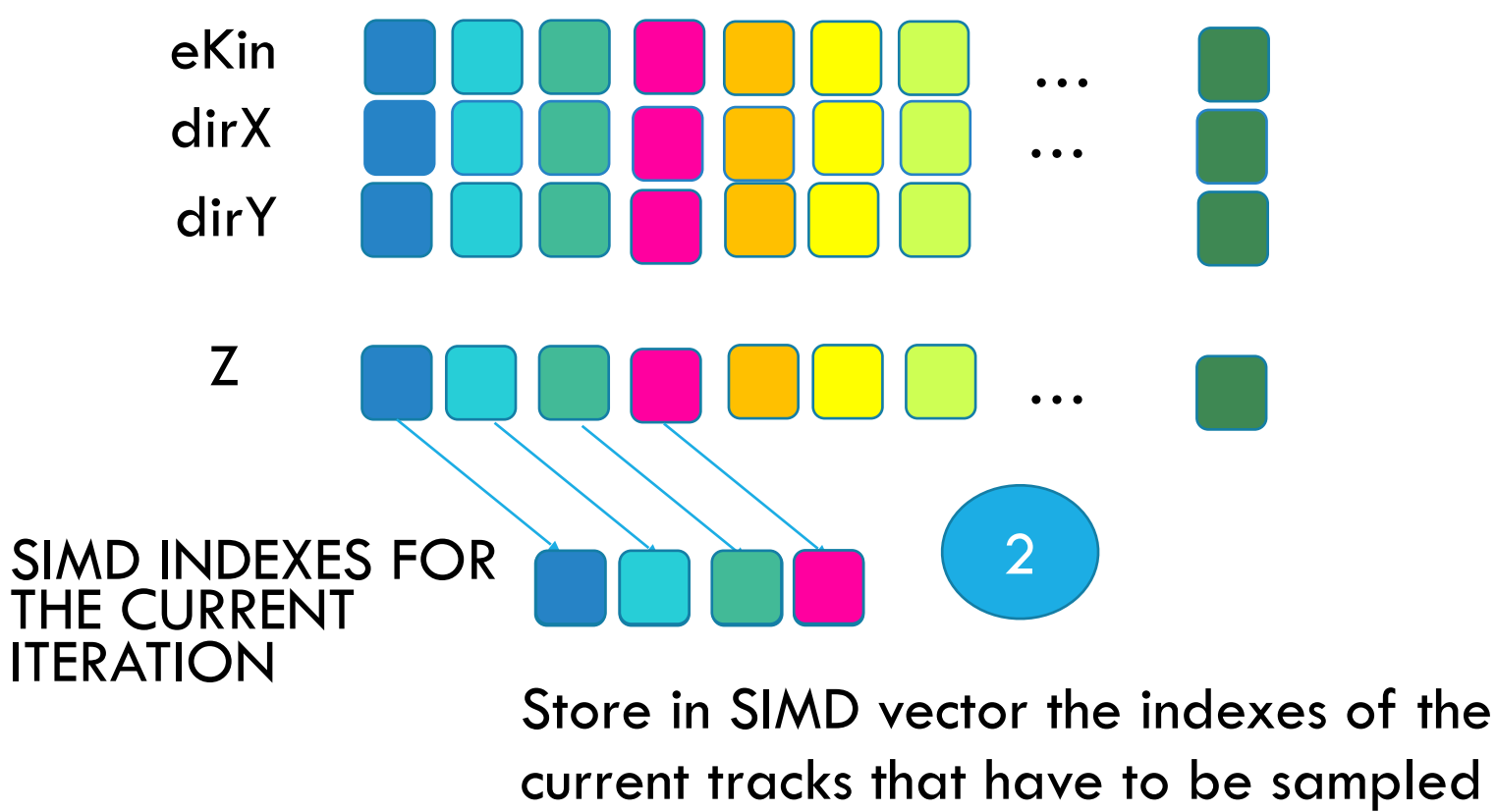
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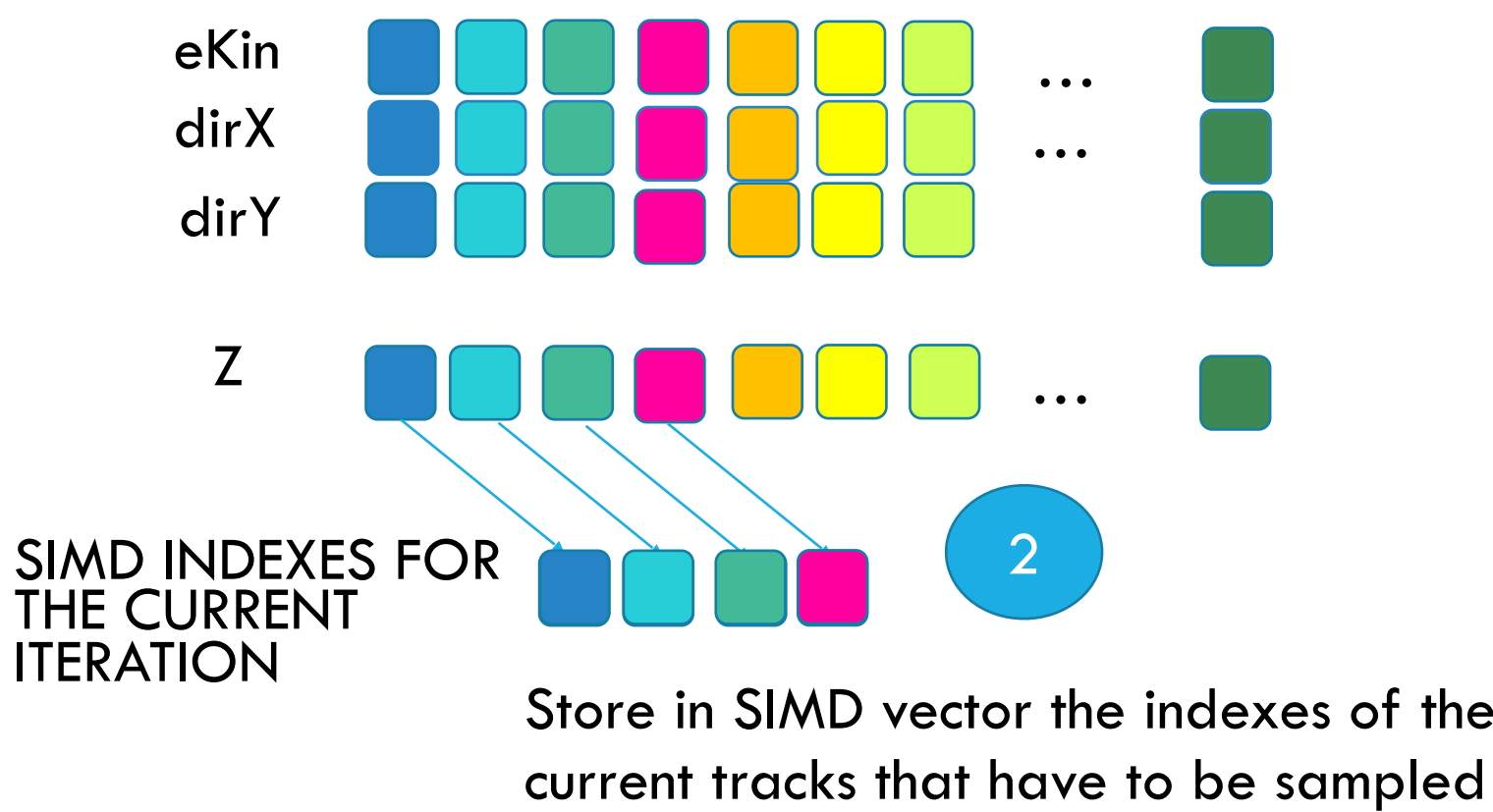


3 Gather values from array using this indexes

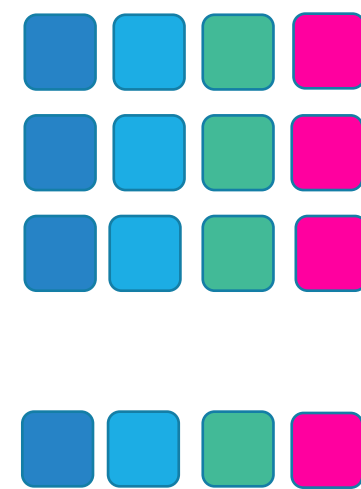


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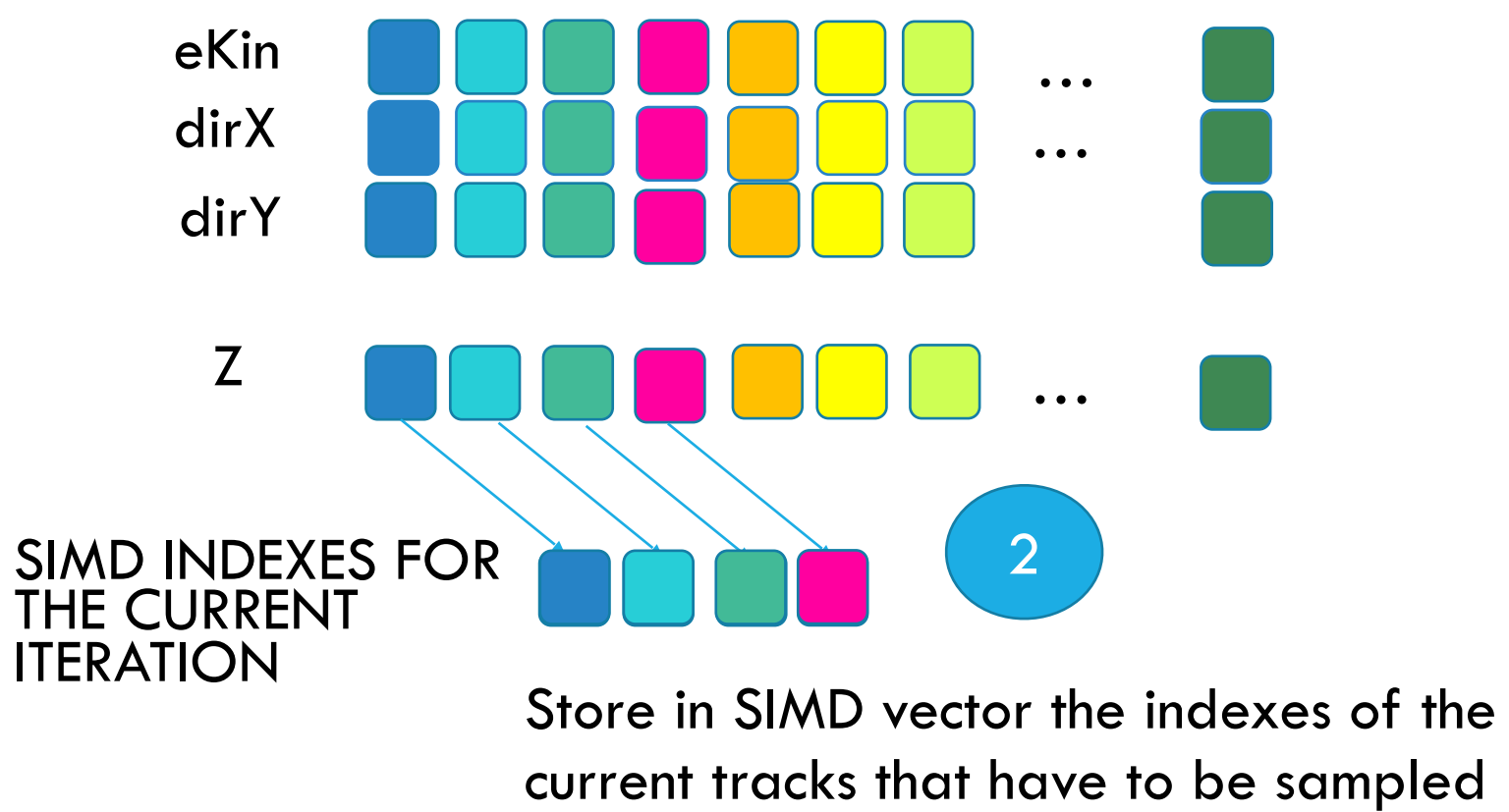


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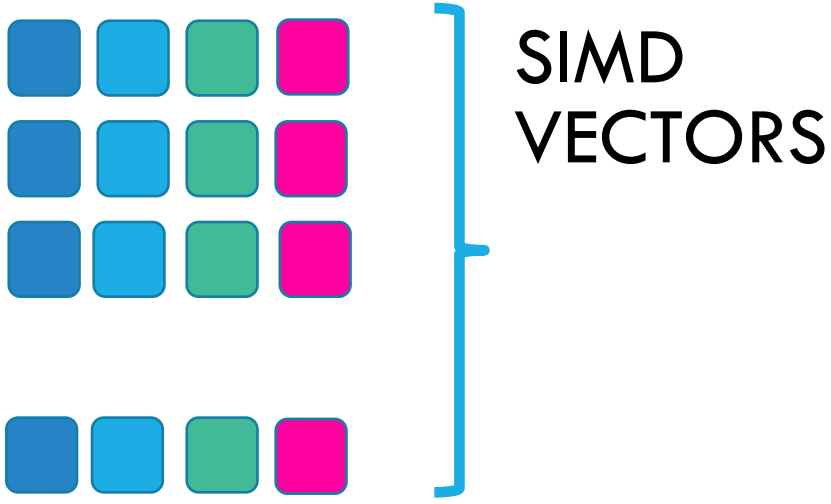


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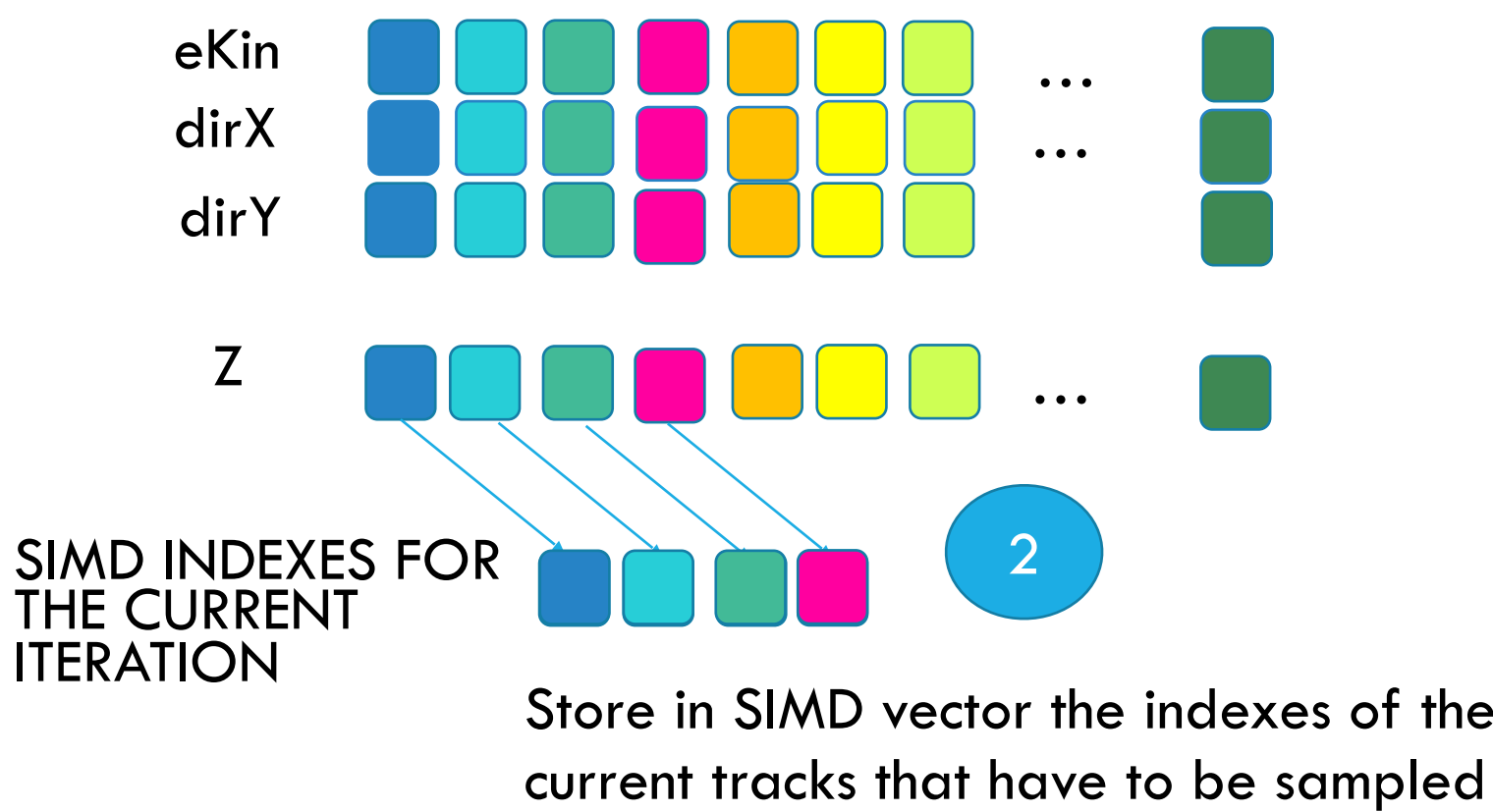


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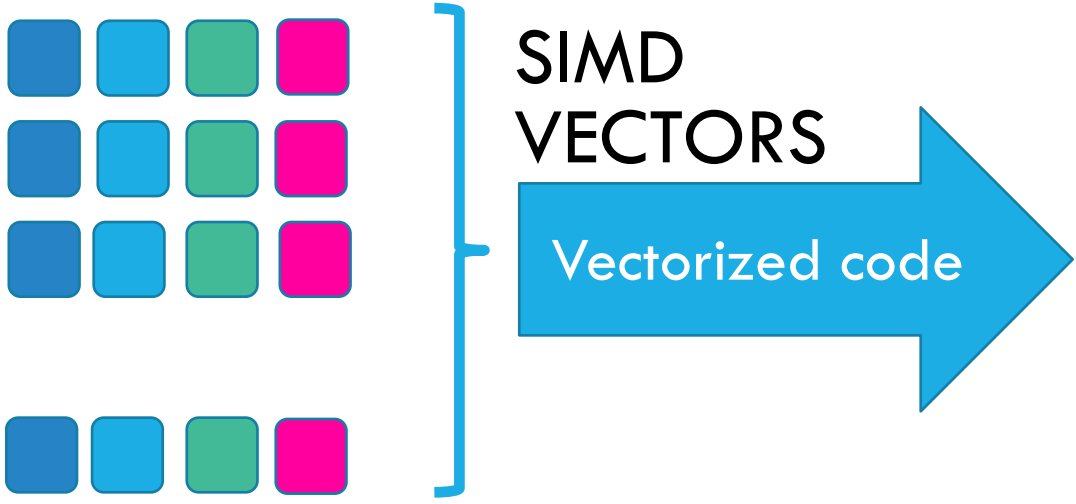


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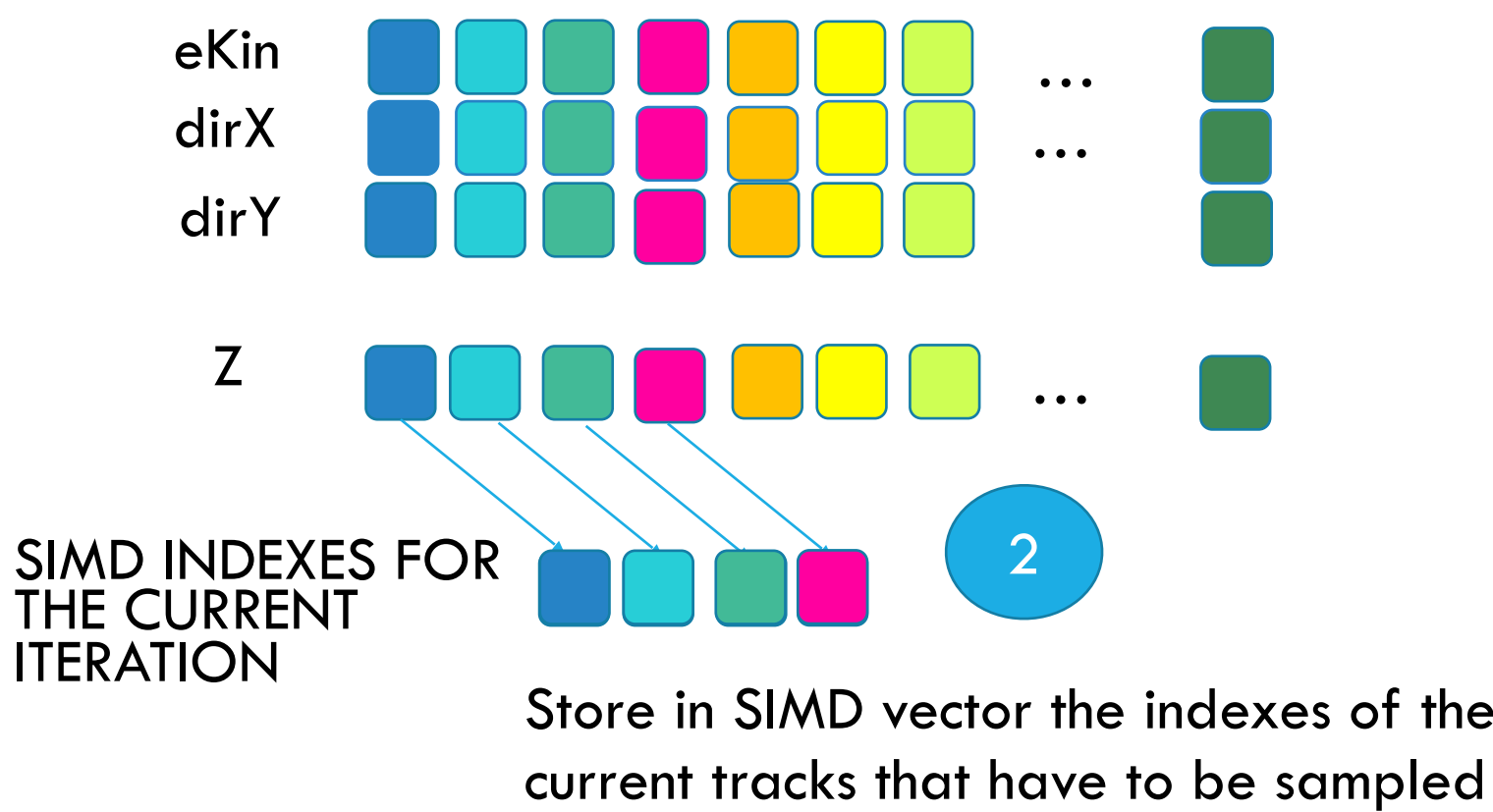
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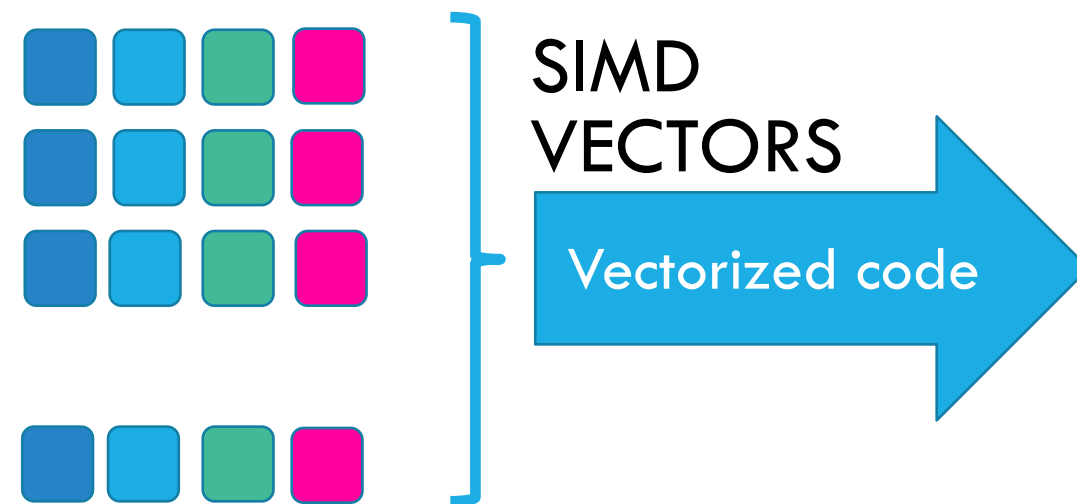


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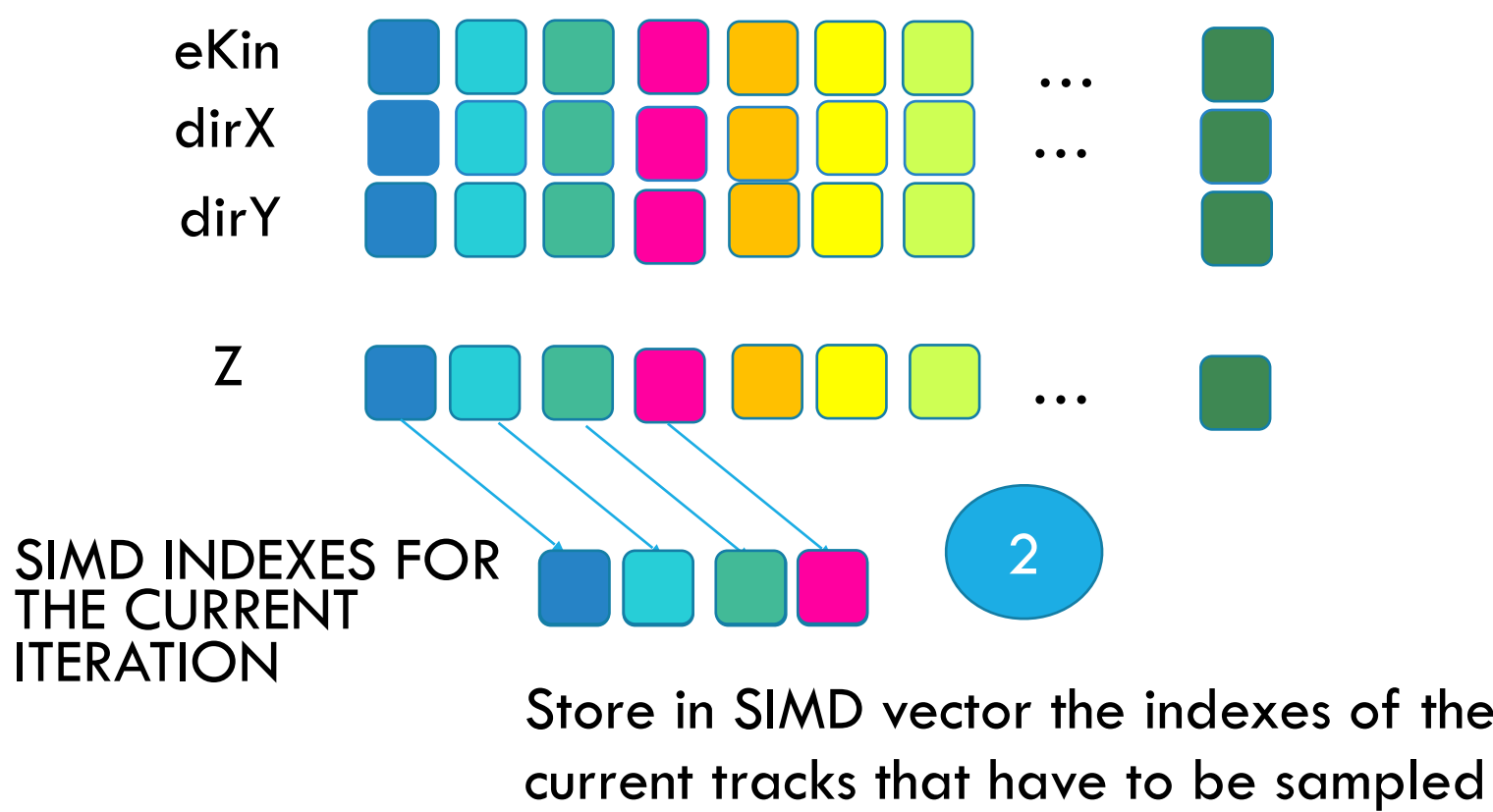


4 Sample and if accepted, scatter back the resulting value to the array at the corresponding indexes

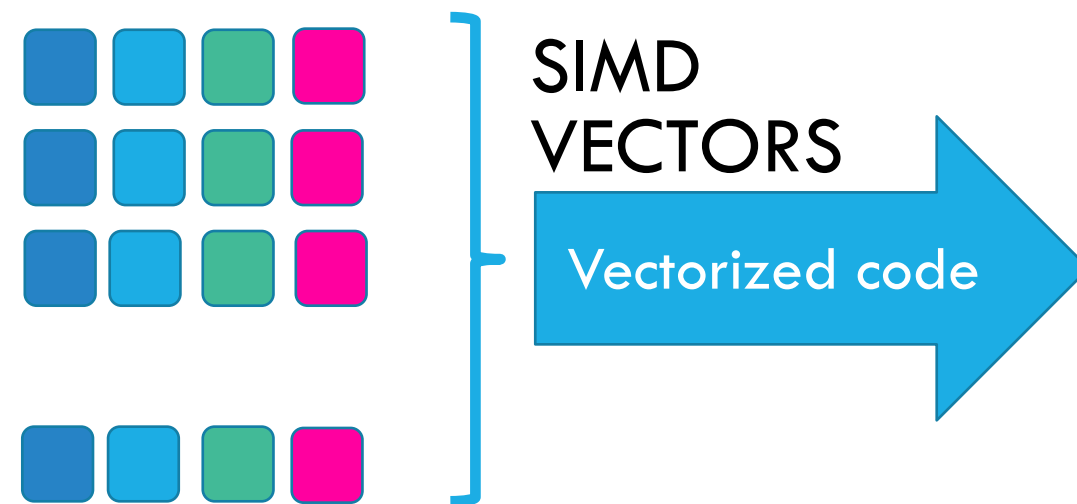


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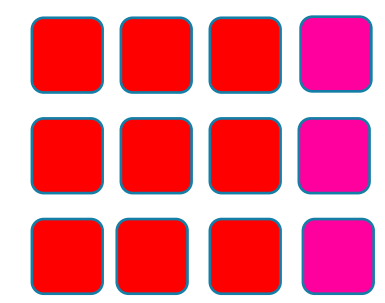
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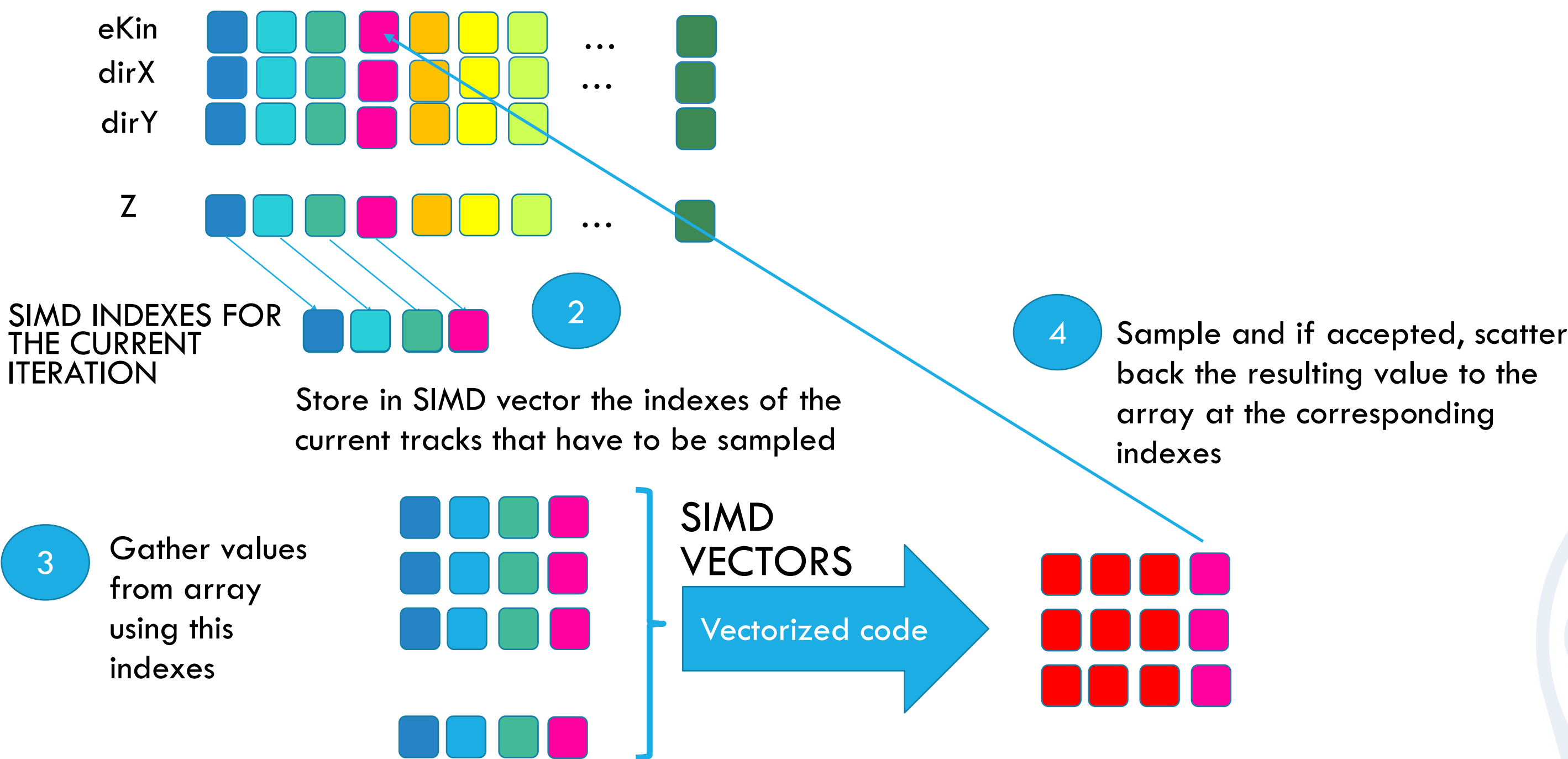


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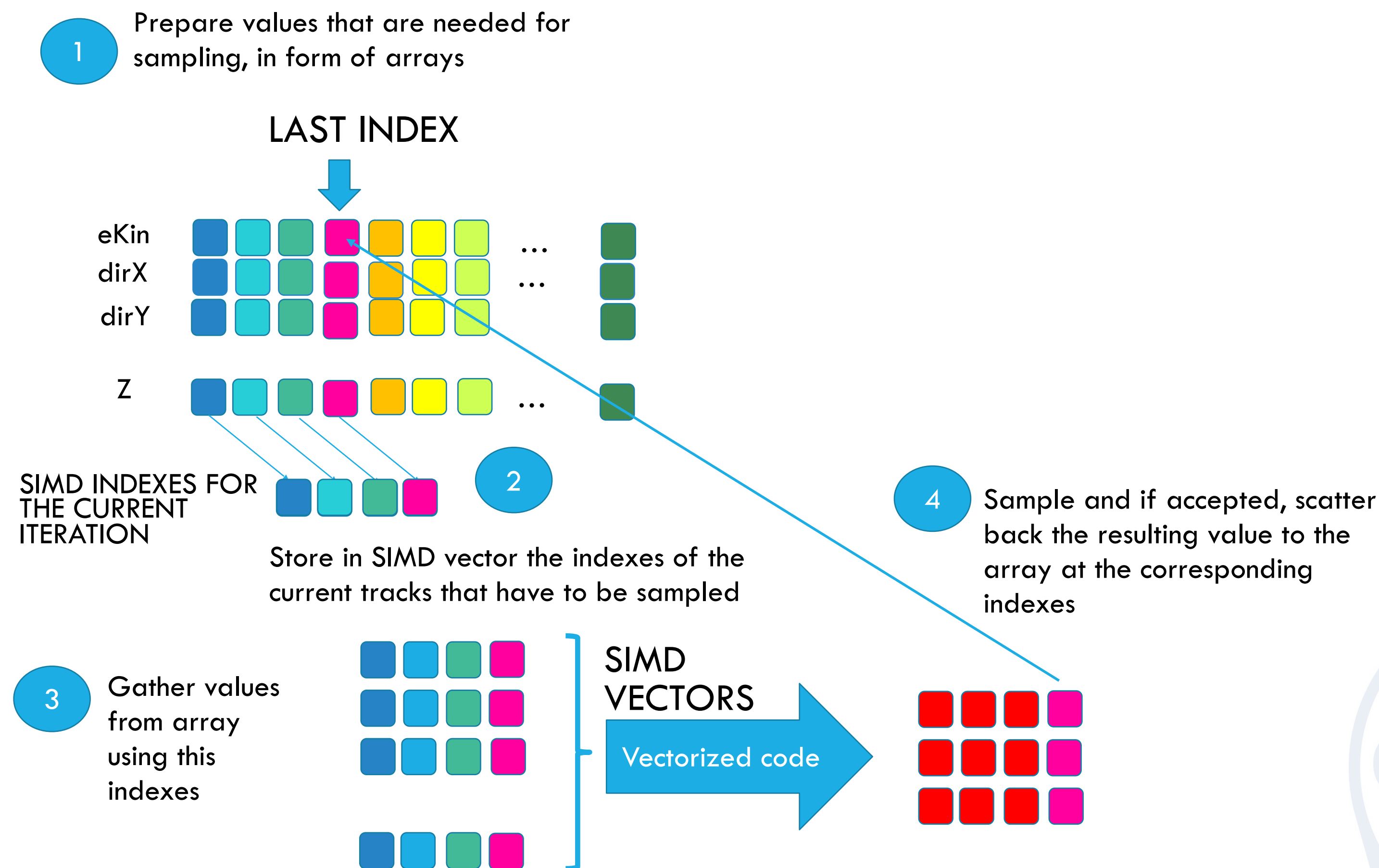


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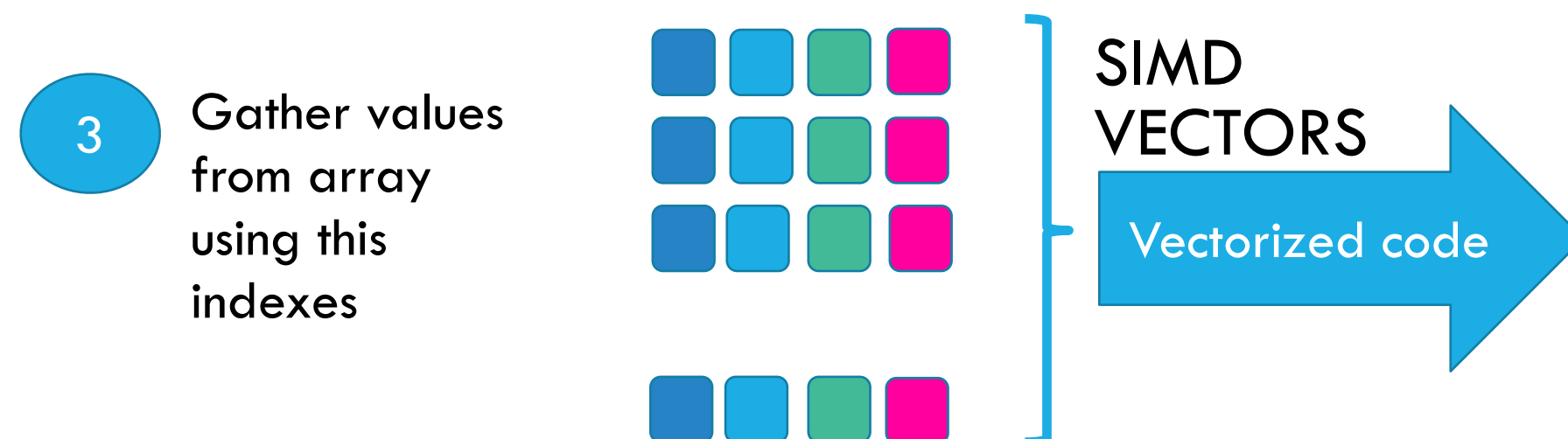
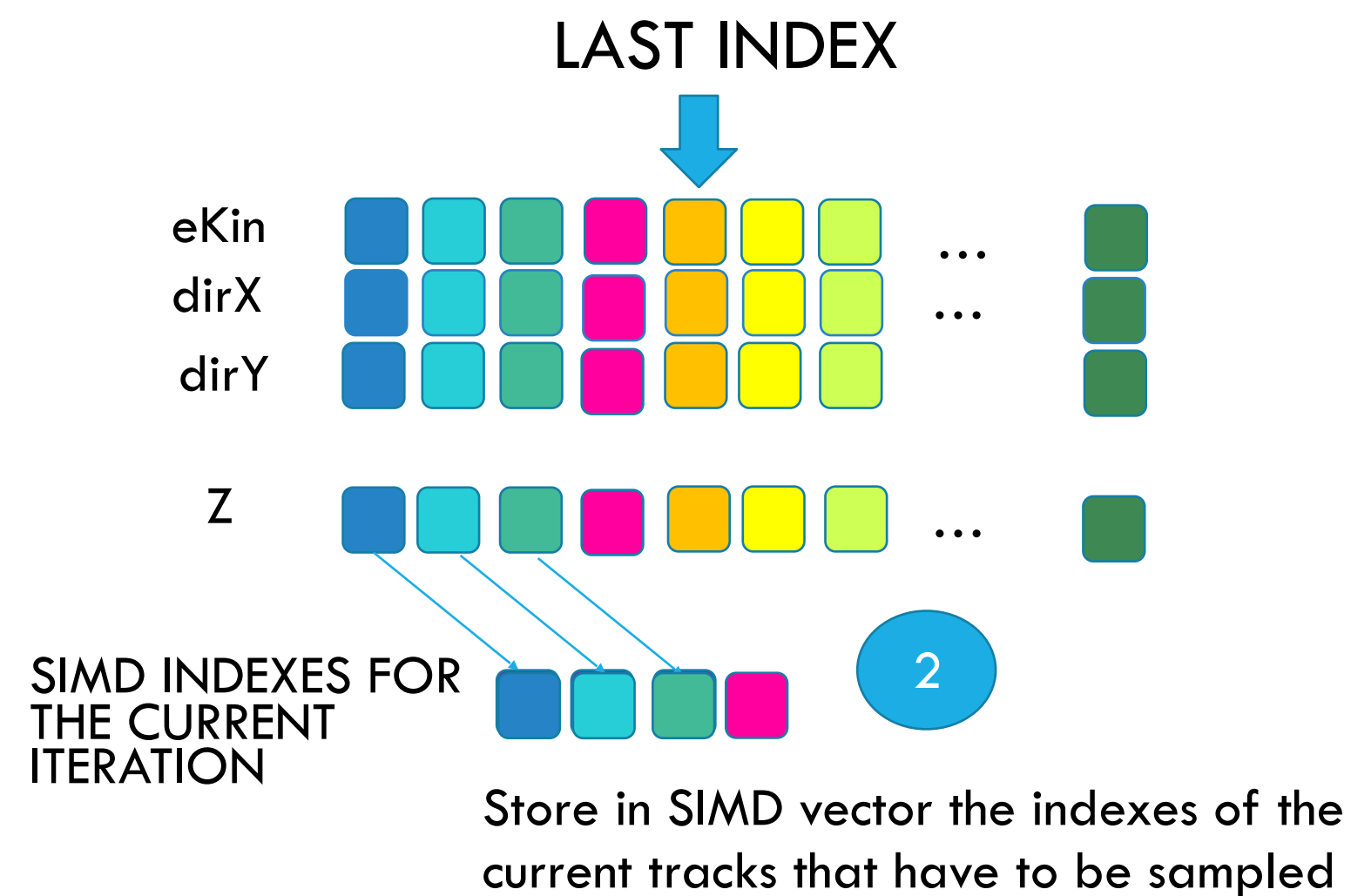


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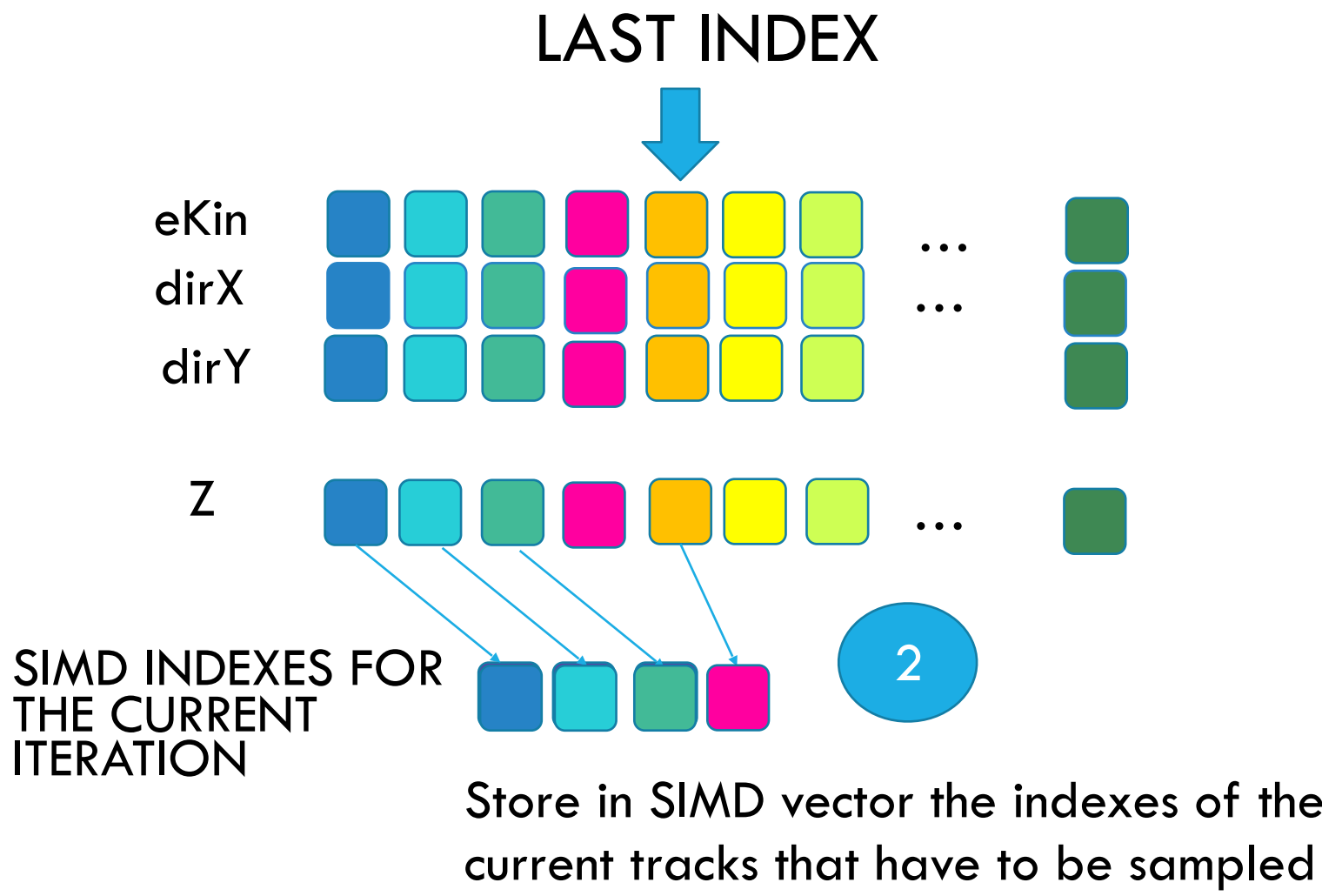
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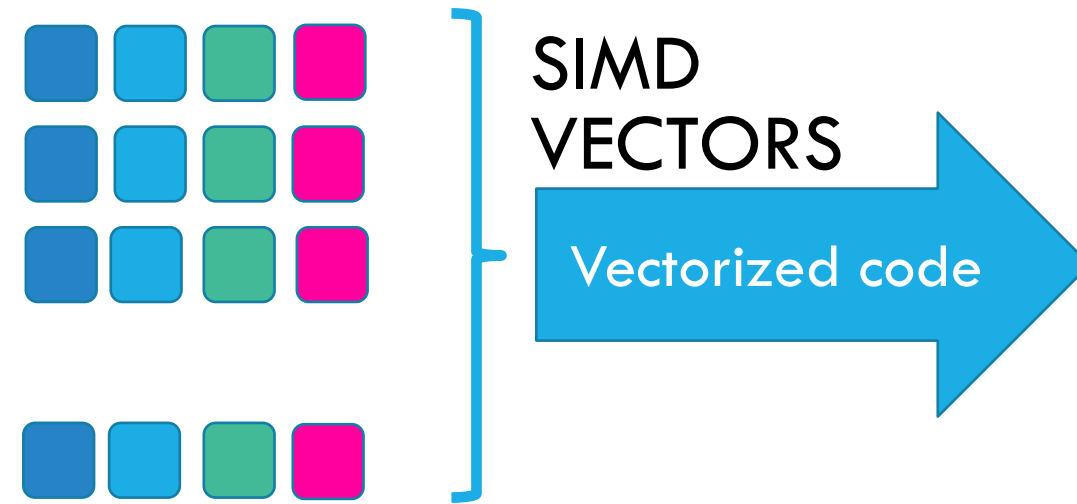


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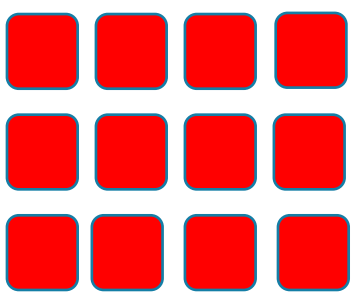
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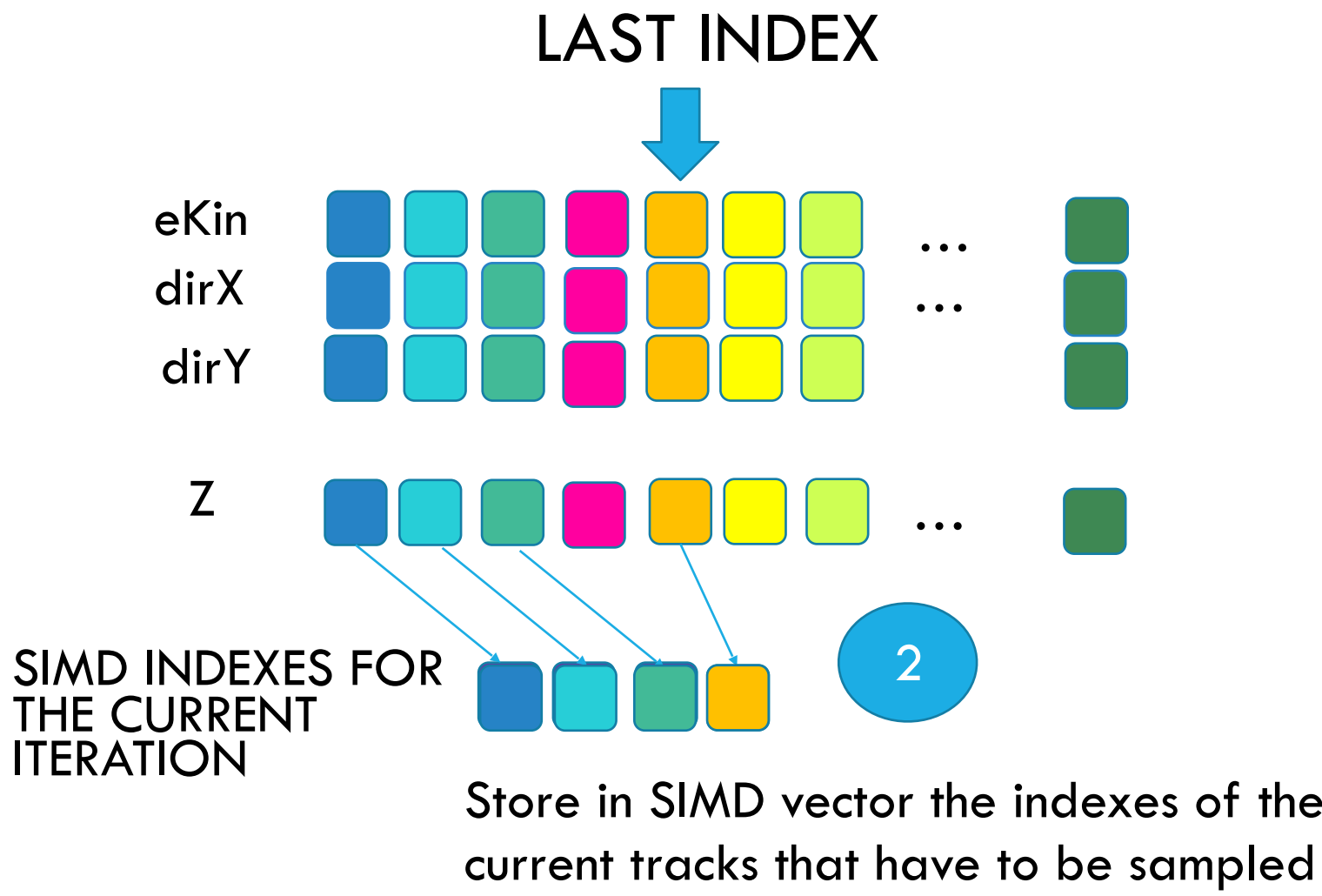


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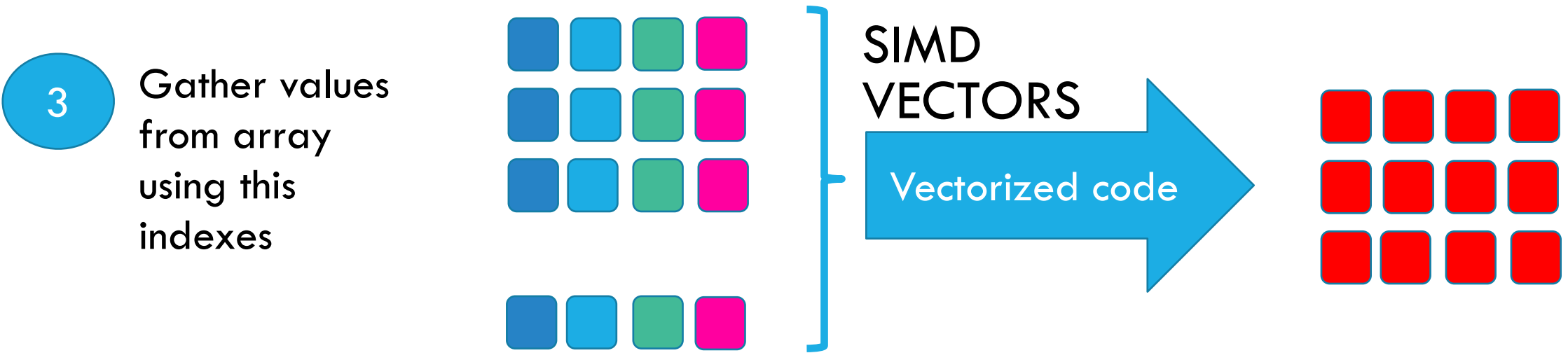


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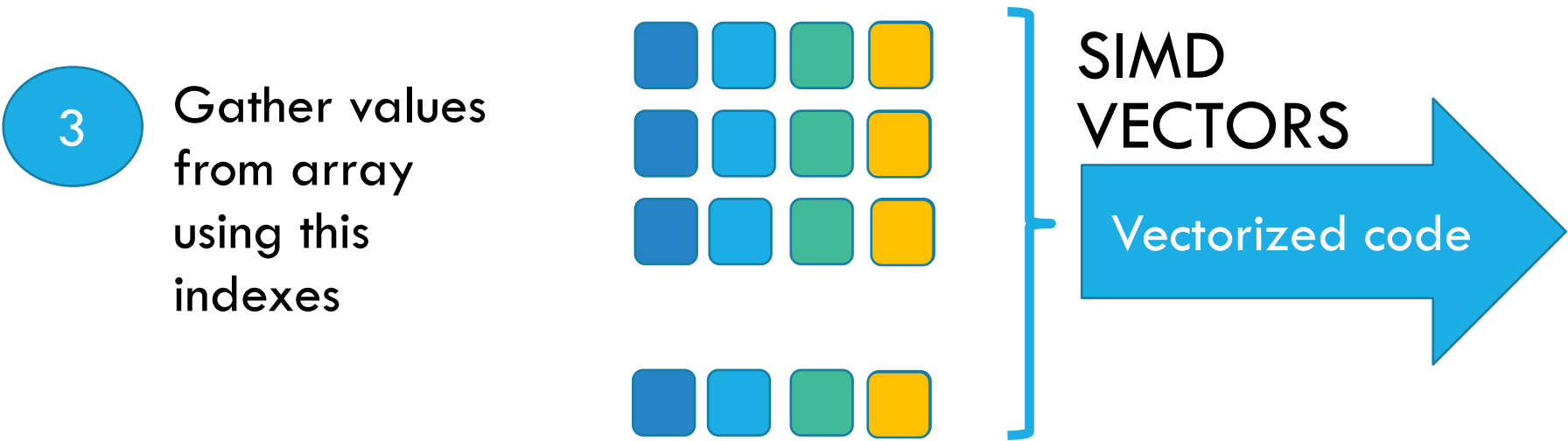
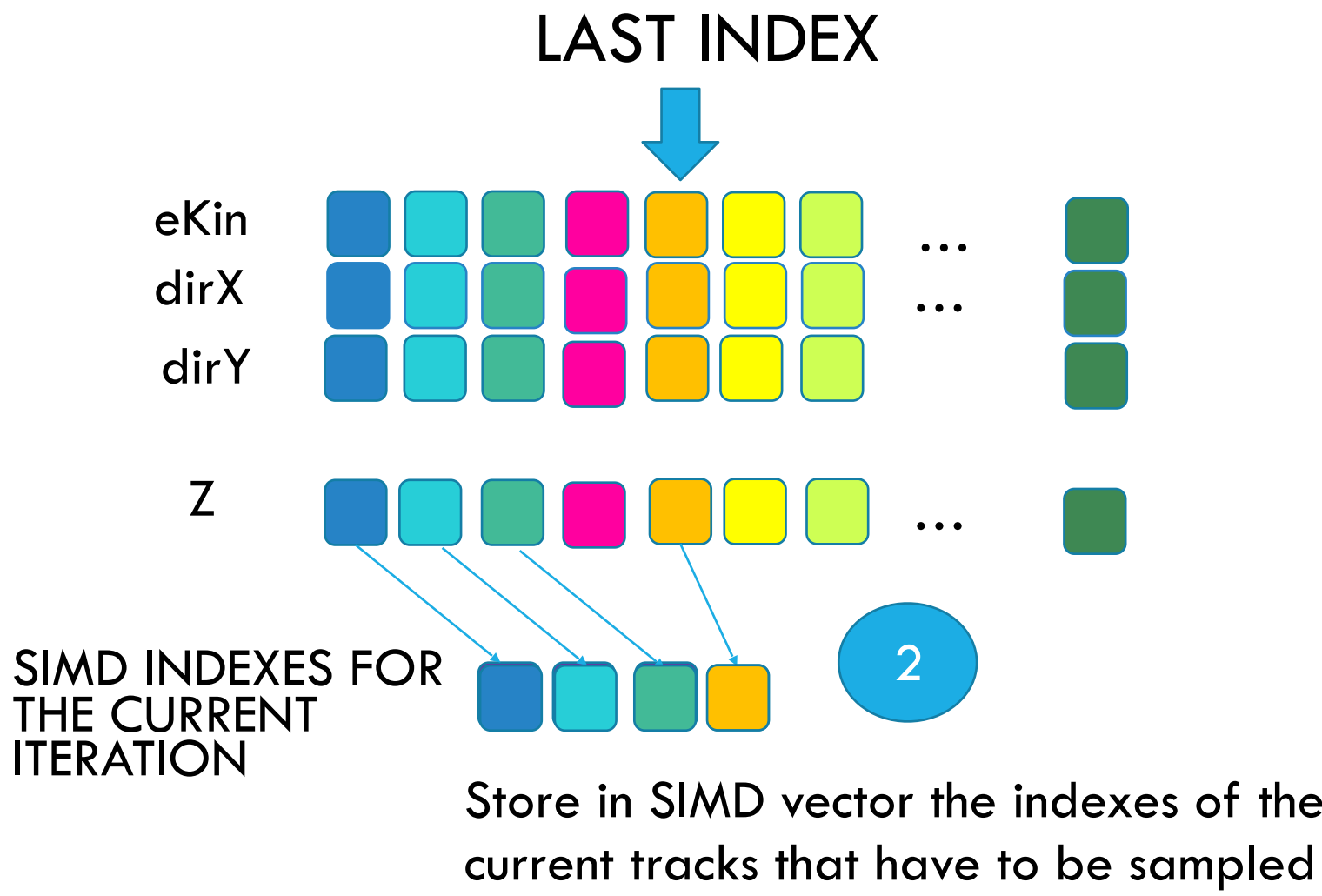


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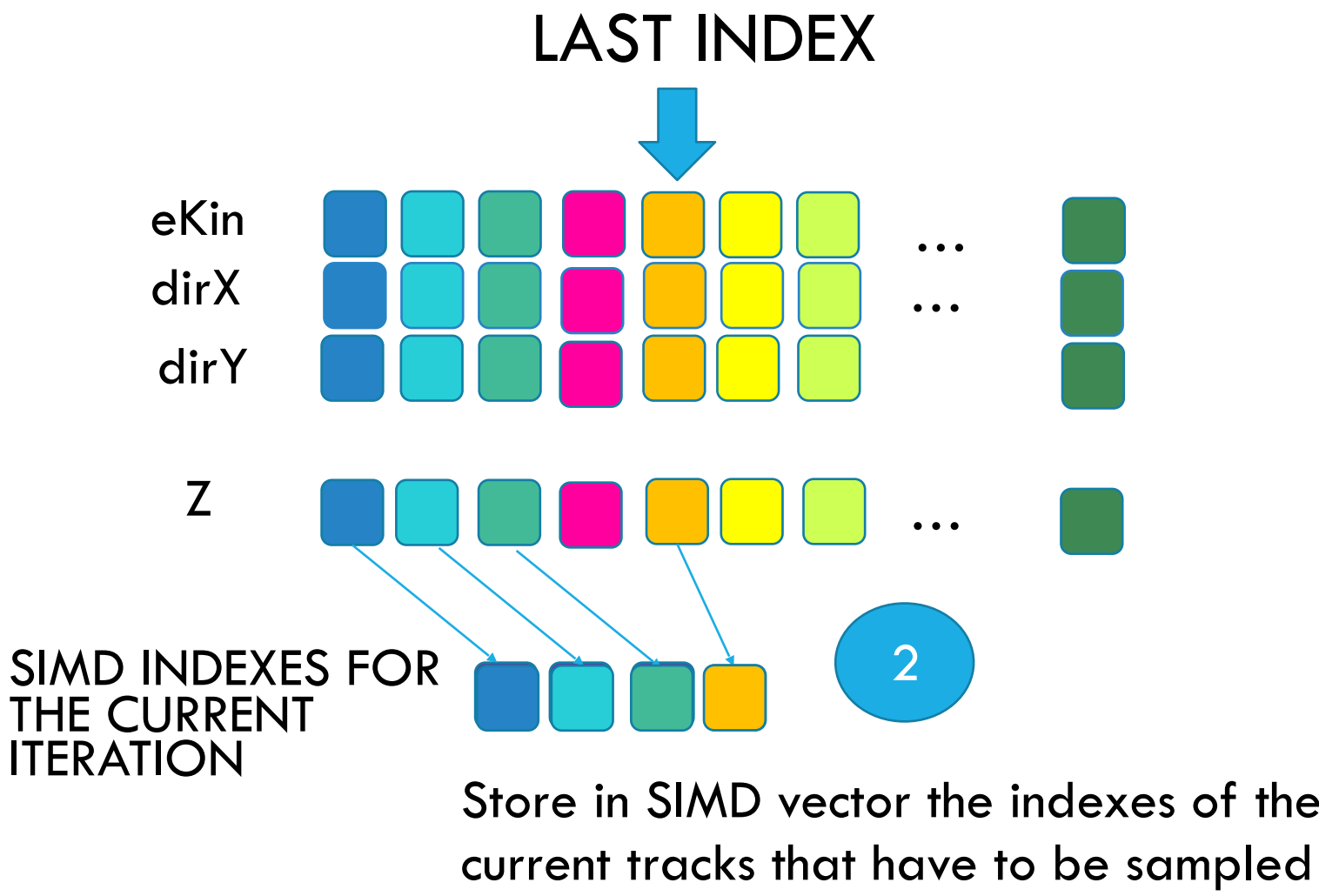


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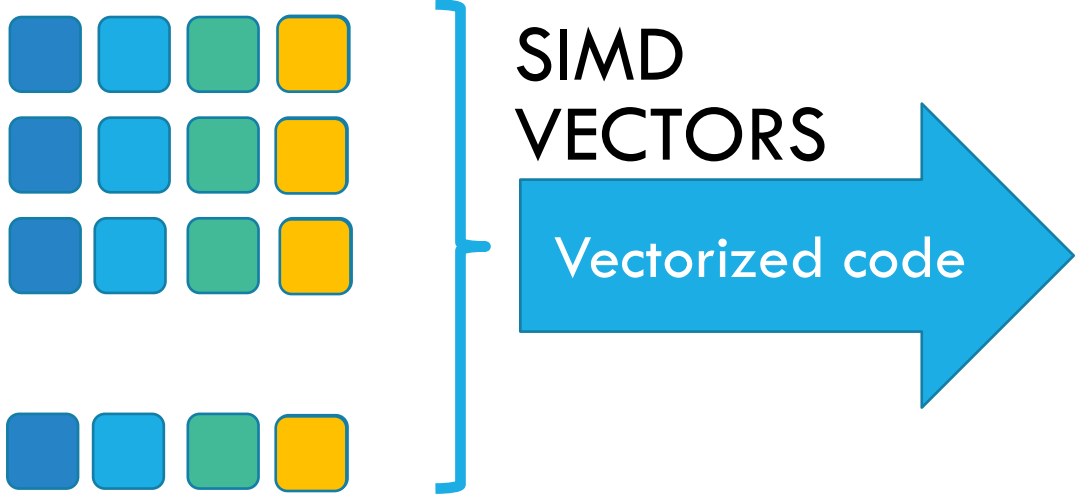


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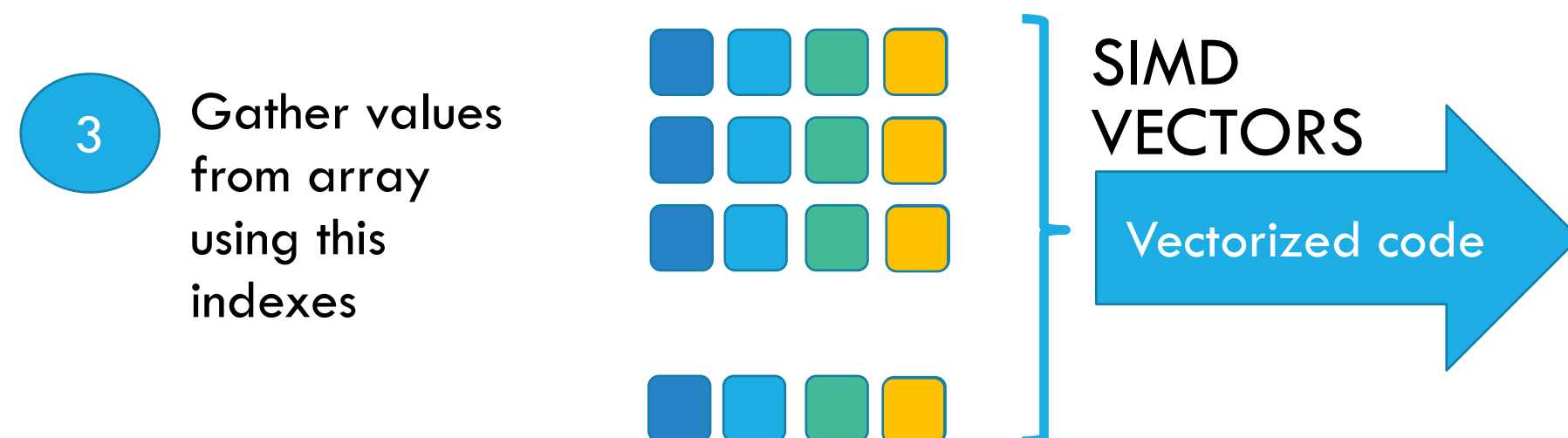
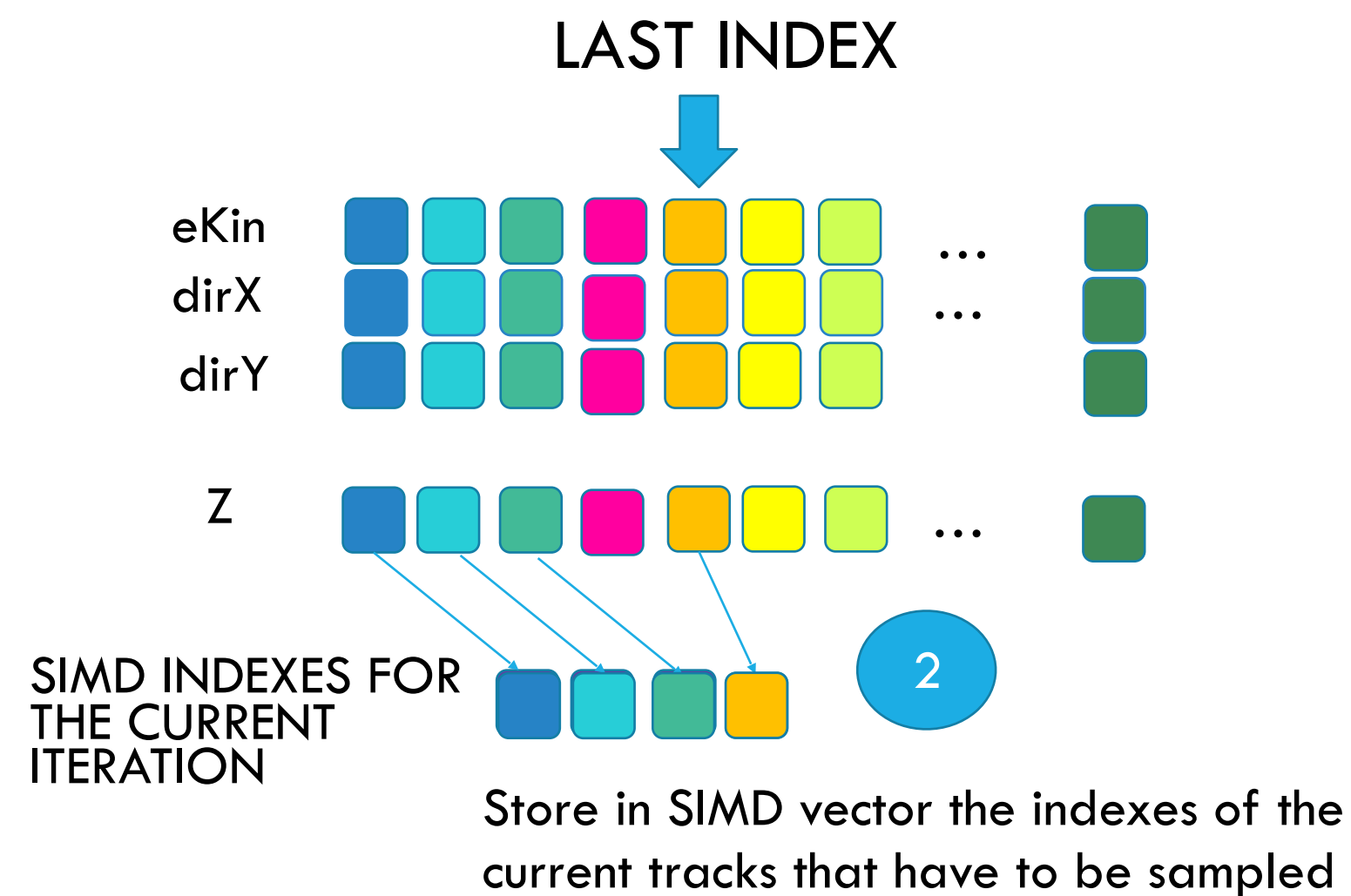


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