NuSTEC workshop on Shallow- and Deep-Inelastic Scattering

# DIS event generation in NEUT

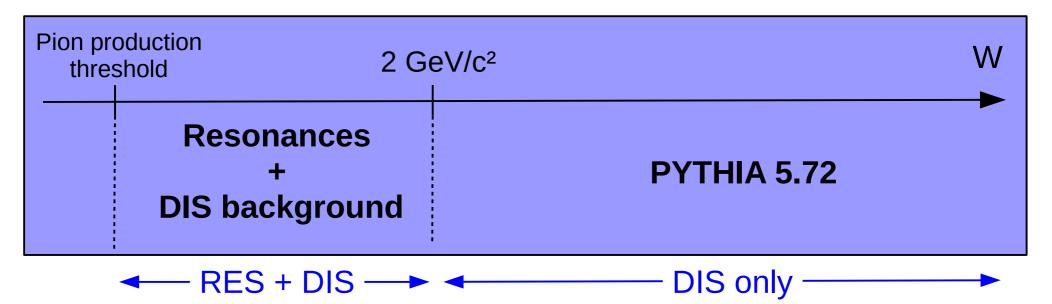
#### C. Bronner Kamioka Observatory, ICRR, Tokyo University



2018-10-13

# **DIS modes in NEUT**

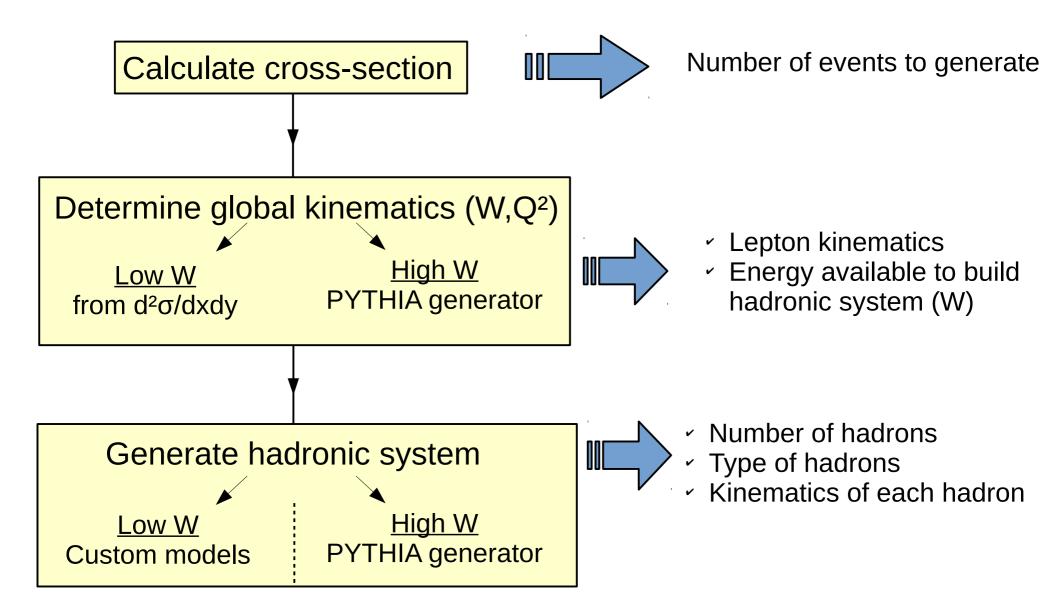
2 different DIS modes depending on the value of W



#### W<2 GeV region:

- Single particle production (lepton + baryon +X): resonances
- More than one particle (lepton + baryon +nX ,n≥2): custom DIS model "multi-pion" mode

# **DIS event generation**



In practice for the high W mode, the event is generated with PYTHIA for a given energy and target nucleon until an event with W>2 GeV is obtained.

#### **Cross-section calculation**

- The DIS cross-section is computed by numerically integrating d²  $\sigma/dxdy$  over x an y

$$\begin{aligned} \frac{d^2 \sigma^{\nu(\bar{\nu})}}{dx \ dy} &= \frac{G_F^2 M_N E_{\nu}}{\pi (1 + Q^2 / M_W^2)^2} \left\{ \left( y^2 x + \frac{m_\tau^2 y}{2E_{\nu} M_N} \right) F_1^{W^{\pm}} \right. \\ &+ \left[ \left( 1 - \frac{m_\tau^2}{4E_{\nu}^2} \right) - \left( 1 + \frac{M_N x}{2E_{\nu}} \right) y \right] F_2^{W^{\pm}} \\ &\pm \left[ xy(1 - \frac{y}{2}) - \frac{m_\tau^2 y}{4E_{\nu} M_N} \right] F_3^{W^{\pm}} \\ &+ \left. \frac{m_\tau^2 (m_\tau^2 + Q^2)}{4E_{\nu}^2 M_N^2 x} F_4^{W^{\pm}} - \frac{m_\tau^2}{E_{\nu} M_N} F_5^{W^{\pm}} \right\} \,. \end{aligned}$$

(From hep-ex/0208187, in the general case  $m_{\tau}$  is replaced by the lepton mass)

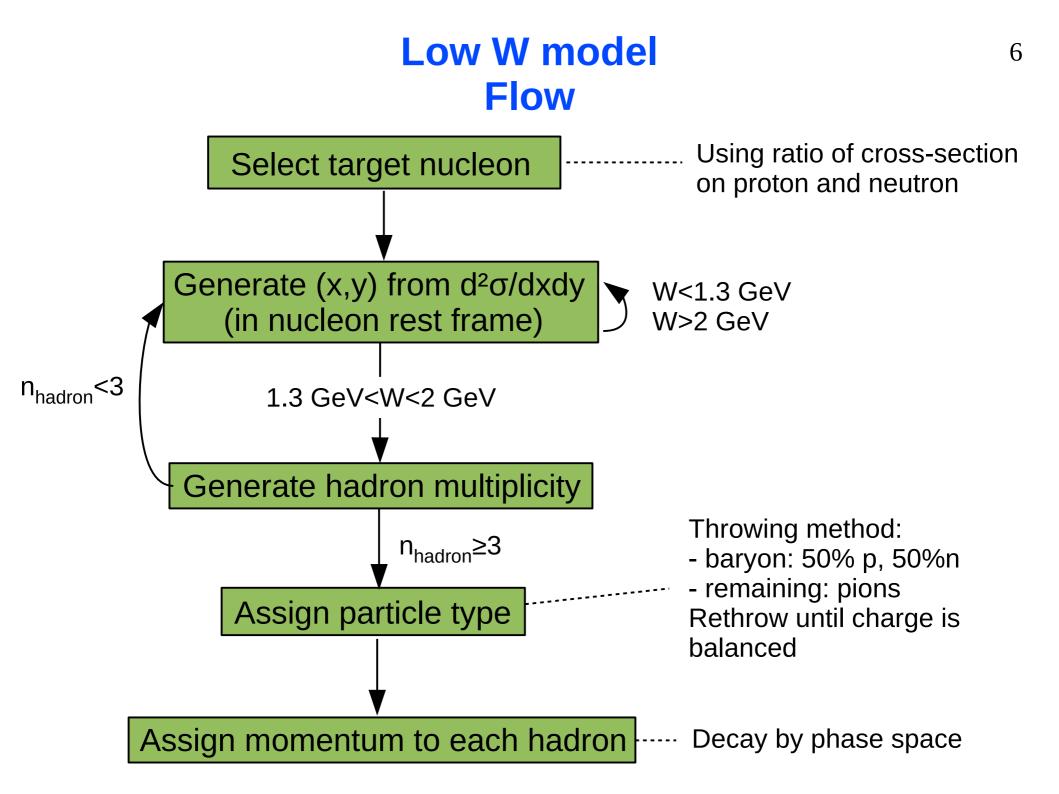
- The part coming from values of x and y giving W>2 GeV gives the high W mode cross-section
- for values of x and y giving 1.3<W<2, the cross-section is multiplied by the fraction of events having more than 2 pions at this W to give the low W mode cross-section

# **Double differential cross-section calculation** 5

- 5 structure functions needed for the double differential cross-section as a function of x and y.
- Calculate F2 and xF3 using Parton Distribution Functions PDFs: Bodek-Yang model from hep-ph/0508007 (modified GRV98 LO)
- Use modified Calland-Gross and Albright-Jarlskog relations to relate  ${\sf F}_1, {\sf F}_4, {\sf F}_5$  to  ${\sf F}_2$

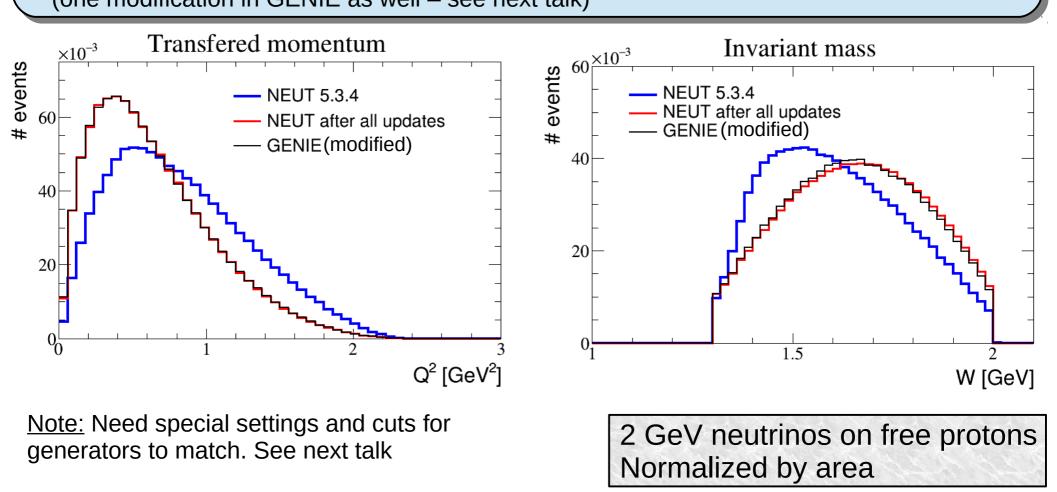
$$F_{1}(x,Q^{2}) = \frac{1}{2x} F_{2}(x,Q^{2}) \times \left(\frac{1+4M^{2}x^{2}/Q^{2}}{1+R(x,Q^{2})}\right)$$
$$F_{4}(x,Q^{2}) = 0$$
$$F_{5}(x,Q^{2}) = \frac{F_{2}(x,Q^{2})}{x}$$

(Those relations are approximations, see for example S. Kretzer and M. H. Reno, hep-ph:0208187v1)



# Low W model Updates

- NEUT and GENIE use similar method and inputs to generate (x,y)/(W,Q<sup>2</sup>) in their low W models
- Found when doing generator comparison that obtained distributions were different for the 2
  - $\rightarrow$  started systematic comparisons and updated NEUT as a result (one modification in GENIE as well see next talk)



# Low W model Updates

#### List of updates NEUT 5.3.4 to 5.4.0:

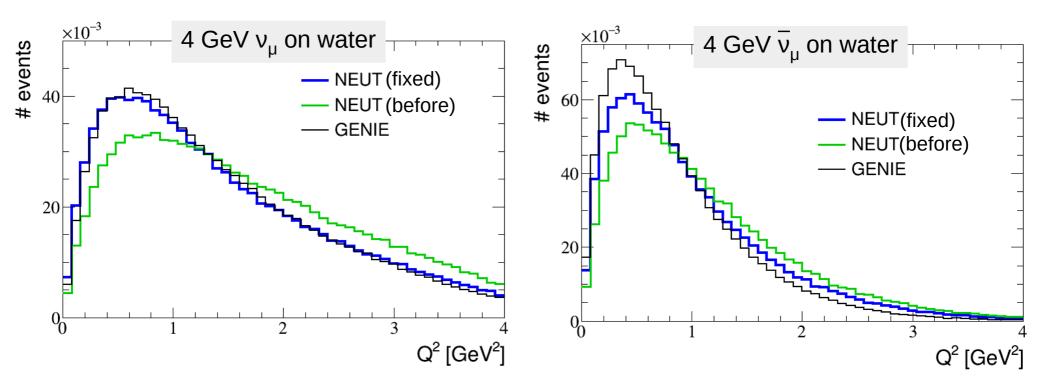
- Fix relation between  $Q^2$  and x (avoid double counting target mass corrections)
- Use different cross sections to generate kinematics of interactions on protons and on neutrons
- Fix a typo in the implementation of the Bodek-Yang corrections
- target nucleon is selected based on the ratio of cross-sections on proton and neutron at the interaction energy
- Update version of the Bodek-Yang corrections used hep-ex/0301036  $\rightarrow$  hep-ph/0508007
- Change the scaling variable to the Nachtmann variable when Bodek-Yang corrections are not used
- Separate structure functions between CC and NC (still need to put the right formula for NC events)
- Use CKM matrix elements when calculating structure functions from PDF
- Added the charm related CKM matrix elements in the calculation of the structure functions if W is large enough to produce charmed particles (enough to produce a proton + a D0)
- Updated values of the CKM matrix elements to PDG 2015
- Take into account effect of multiplicity on generation of x and y
- Added possibility to use different hadron multiplicity model:
  - current NEUT one (with a small fix of the parameters)
  - my fit of deuterium bubble chamber data
  - AGKY model (used in GENIE)
- Removed passage through a  $\Delta$  resonance

#### Low W model Fix relation between x and Q<sup>2</sup>

• In the NEUT code, the definition of x used to obtain  $Q^2$  was not the standard one:

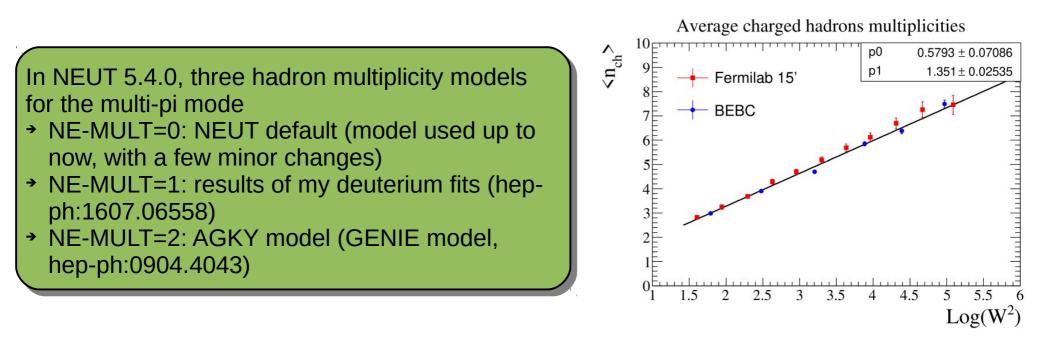
$$x = \frac{Q^2}{2M_{nuc}Ey}$$
 (1) but instead:  $x = \frac{Q^2}{2M_{nuc}Ey + M_{nuc}^2}$  (2)

 It seems this is an old definition to take into account target mass effects, but they are already taken into account in corrections by Bodek and Yang In 5.3.4, x was generated assuming definition (1) but then (2) was used to deduce Q<sup>2</sup>



#### Low W model updates Multiplicity model

To determine the number of hadrons produced, use a multiplicity model Gives the probability to produce a given number of hadrons as a function of W, v/v and target nucleon



To avoid double counting between RES and DIS, keep only events with  $n_{had} \ge 3$ 

This multiplicity model has a large impact on low W model

10

#### Low W model updates Multiplicity model – effect on W

11

- $(x,y)/(W,Q^2)$  generated based on d<sup>2</sup> $\sigma$ /dxdy
- Number of hadrons generated for this W using multiplicity model
- Only keep event if n<sub>had</sub> ≥3
  - $\rightarrow$  probability of a given throw to be accepted depend on multiplicity model

#### Neutrino on proton Neutrino on neutron Invariant mass events events Model 0 (default) Model 0 (default) 30 Model 1 (deuterium) 20 Model 1 (deuterium) Model 2 (AGKY) Model 2 (AGKY) 25 15 20 15 10 10 5 1.41.9 1.81.9 W [GeV] W [GeV] 5 GeV $v_{\mu}$ (area normalized)

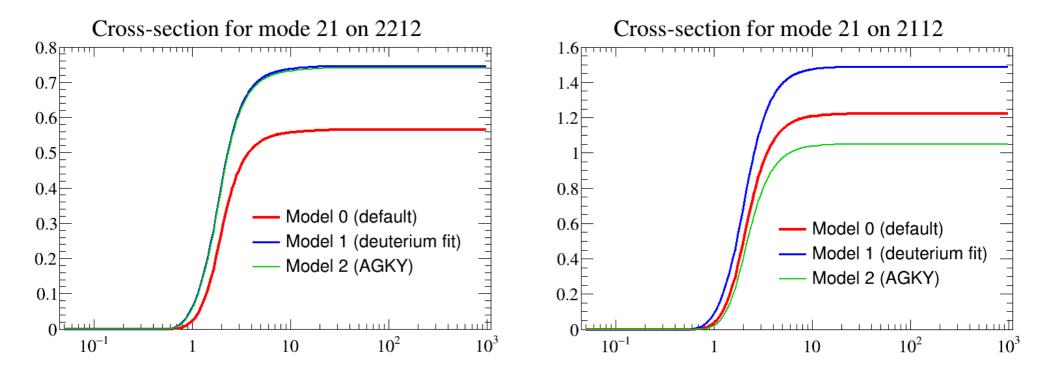
#### Low W model updates Multiplicity model – effect on cross-section

Multi-pi mode cross-section is obtained by multiplying the total DIS cross section for W<2 GeV by the fraction of events that have at least two pions

#### Neutrino on proton

Neutrino on neutron

12



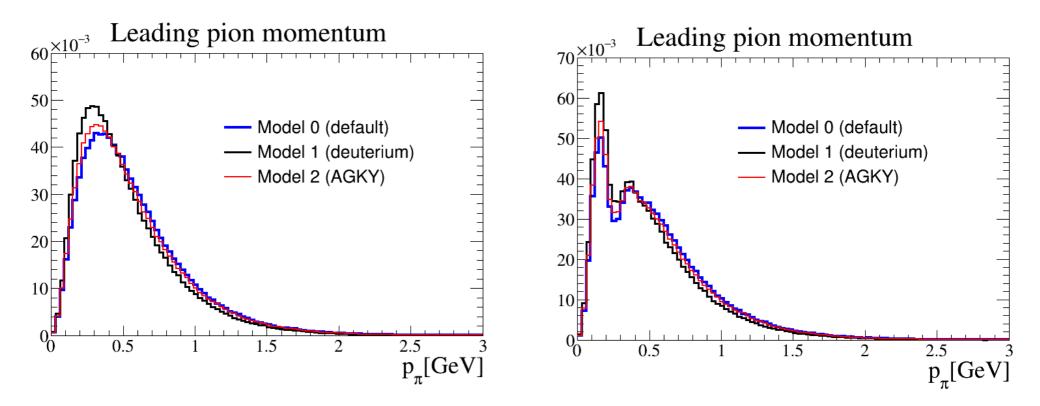
In current implementation (5.4.0), cross-sections computed with model 0 are always used, regardless of the multiplicity model used

#### Low W model updates Multiplicity model – effect on kinematics

More particles => less available energy per particle  $\rightarrow$  Multiplicity model will also affect hadron kinematics

#### Before FSI

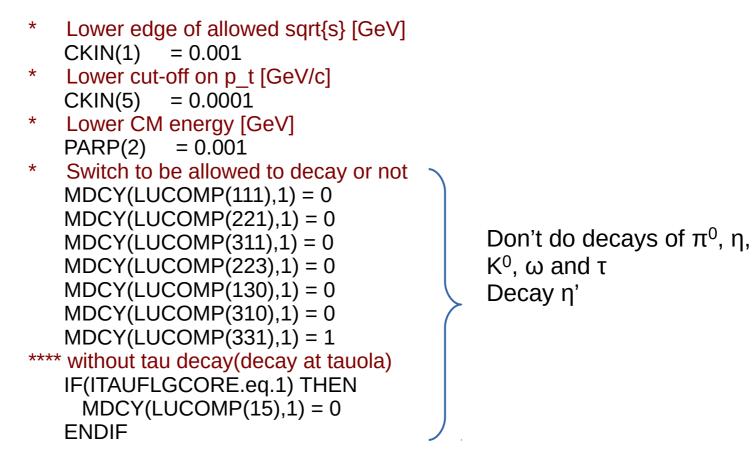
With FSI



5 GeV  $v_{\mu}$  on CH, interactions on protons only, area normalized

# **High W mode**

• For W>2 GeV/c<sup>2</sup>, all events are DIS and generated using PYTHIA 5.72 Mostly default settings except:

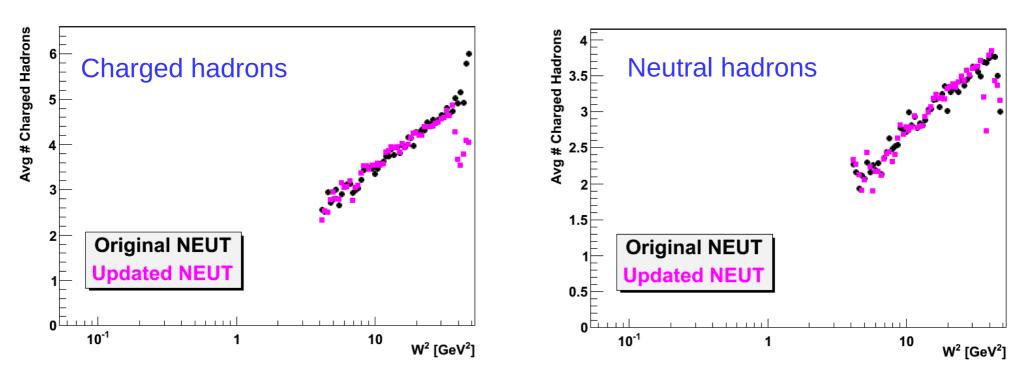


 Only provide neutrino and target nucleon four-momenta to PYTHIA Keep event if type (CC/NC) is the one desired, and W>2 GeV Redo PYTHIA generation with same inputs else

#### High W mode Pythia 6 tests (J. Morrison - MSU)

- Other generators (NuWro, GENIE) use PYTHIA 6
- Does not allow E<sub>CM</sub><5.3 GeV: other generators pass hit quark, spectator diquark and W to Pythia and just use fragmentation routines

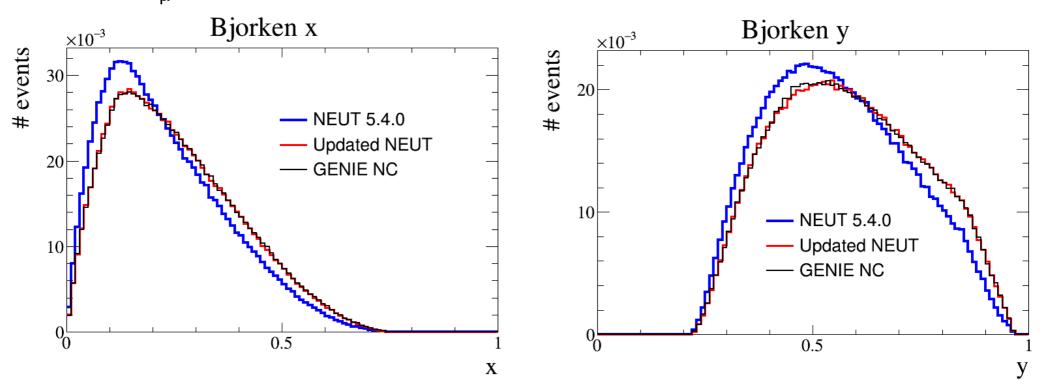
#### Tests in NEUT with PYTHIA 6 and 25 GeV neutrinos



Hadronization looks similar, main difference with other generators is (W,Q<sup>2</sup>) generated by PYTHIA 5 vs according to  $d^2\sigma/dxdy$ 

#### **Neutral current modes**

- So far only presented CC DIS modes In 5.4.0, NC DIS modes uses CC structure functions (without CKM matrix element), and NC DIS cross-section obtained from CC one
- Started working on implementing correct NC structure functions.
  After this updates, low W NC mode compatible with GENIE
  (2 GeV v<sub>u</sub> on free neutrons, usual settings to have agreement)



> Next step will be to compute NC cross-section by integrating  $d^2\sigma/dxdy$ 

# **Summary**

- 2 DIS modes in NEUT:
  - → W<2 GeV: "multi-pion" mode, custom model for events with 3 or more hadrons produced
  - → W≥2: based on PYTHIA 5.72
- Many updates from NEUT 5.3.4 to 5.4.0 After the updates, the multi-pion mode predictions of (W,Q<sup>2</sup>) agree with GENIE low W models (for free nucleons, when used in the same conditions)
- Given the way the transition from resonances to DIS is done, the hadron multiplicity model has a large impact on the predictions of the multi-pion mode
- Planning updates of the neutral current DIS modes in the future