

CHIRAL FIELD AND REGGE

THEORY IN THE TRANSITION

REGION

PION PRODUCTION IN A HYBRID MODEL

Natalie Jachowicz, R. González-Jimenez, A. Nikolakopoulos, K. Niewczas, J. Nys

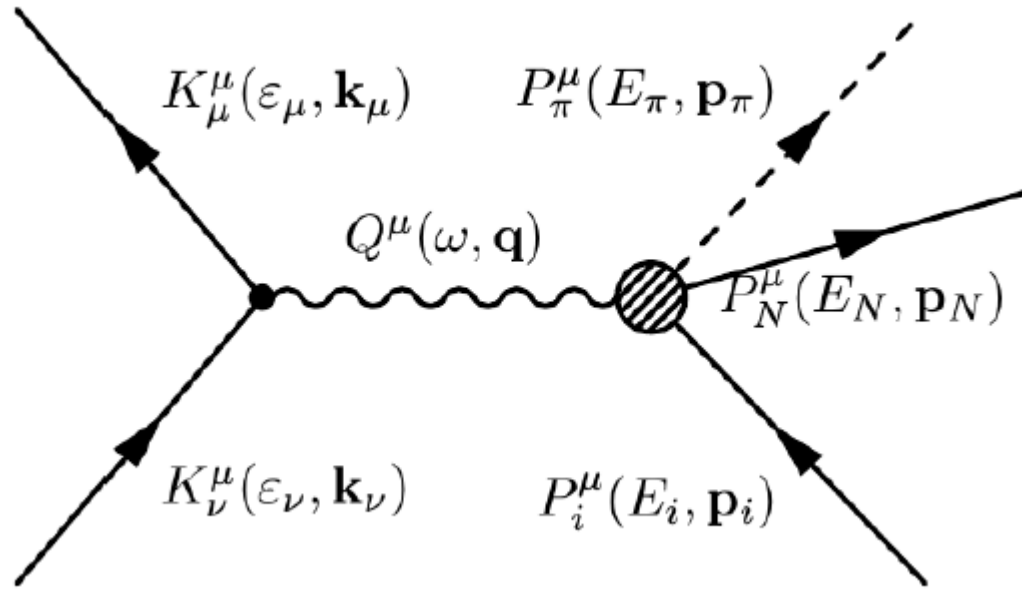
AIM

- Detailed microscopic cross sections calculations for neutrino-induced pion production
- Formalism valid over a broad energy range
- Taking into account as many nuclear physics aspects as feasible

References :

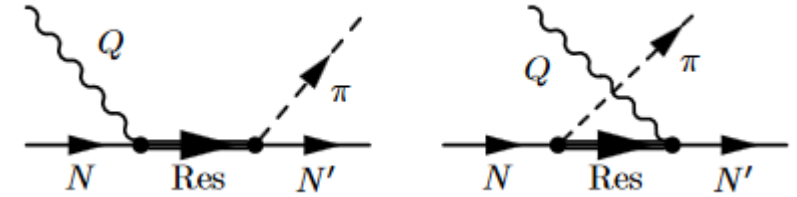
- 'Neutrino-induced pion production from nuclei at medium energies', C. Praet, O. Lalakulich, N. Jachowicz, J. Ryckebusch, Phys. Rev. C79, 044603 (2009) ; arXiv:0804.2750.
- Electroweak single-pion production off the nucleon : from threshold to high invariant masses' R. Gonzalez-Jimenez, N. Jachowicz, K. Niewczas, J. Nys, V. Pandey, T. Van Cuyck, N. Van Dessel, Phys. Rev. D95, 113007 (2017) ; arXiv:1612.05511.
- 'Pion production within the hybrid-RPWIA model at MiniBooNe and MINERvA kinematics, R. Gonzalez-Jimenez, K. Niewczas, N. Jachowicz, Phys. Rev. D97, 093008 (2018) ; arXiv:1710.08374.
- 'Modeling neutrino-induced charged pion production on water at T2K kinematics' A. Nikolakopoulos, R. Gonzalez-Jimenez, K. Niewczas, J. Sobczyk, N. Jachowicz, Phys. Rev. D97, 093008 (2018) ; arXiv:1803.03163.08374.

I. Single pion production on the nucleon – low energy model



Cfr. PRC 76, 033005 (2007), PRD87, 113009 (2013)

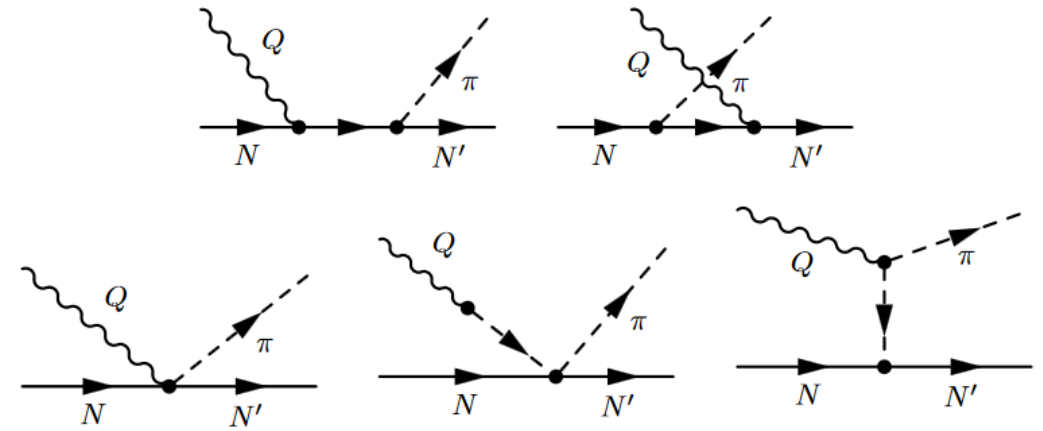
Resonances



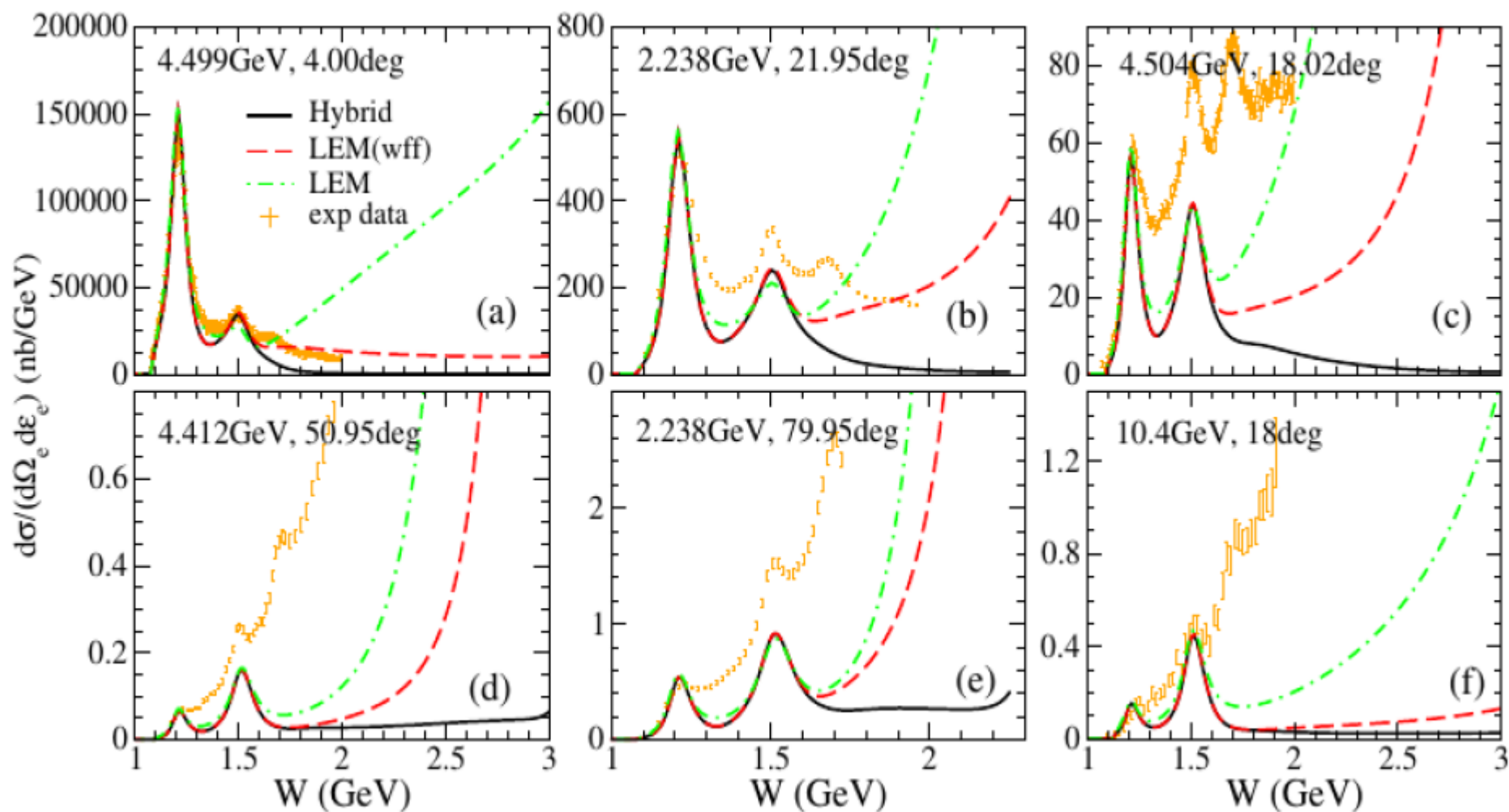
P33 (1232), P11(1440), D13 (1520), S11 (1535)

+

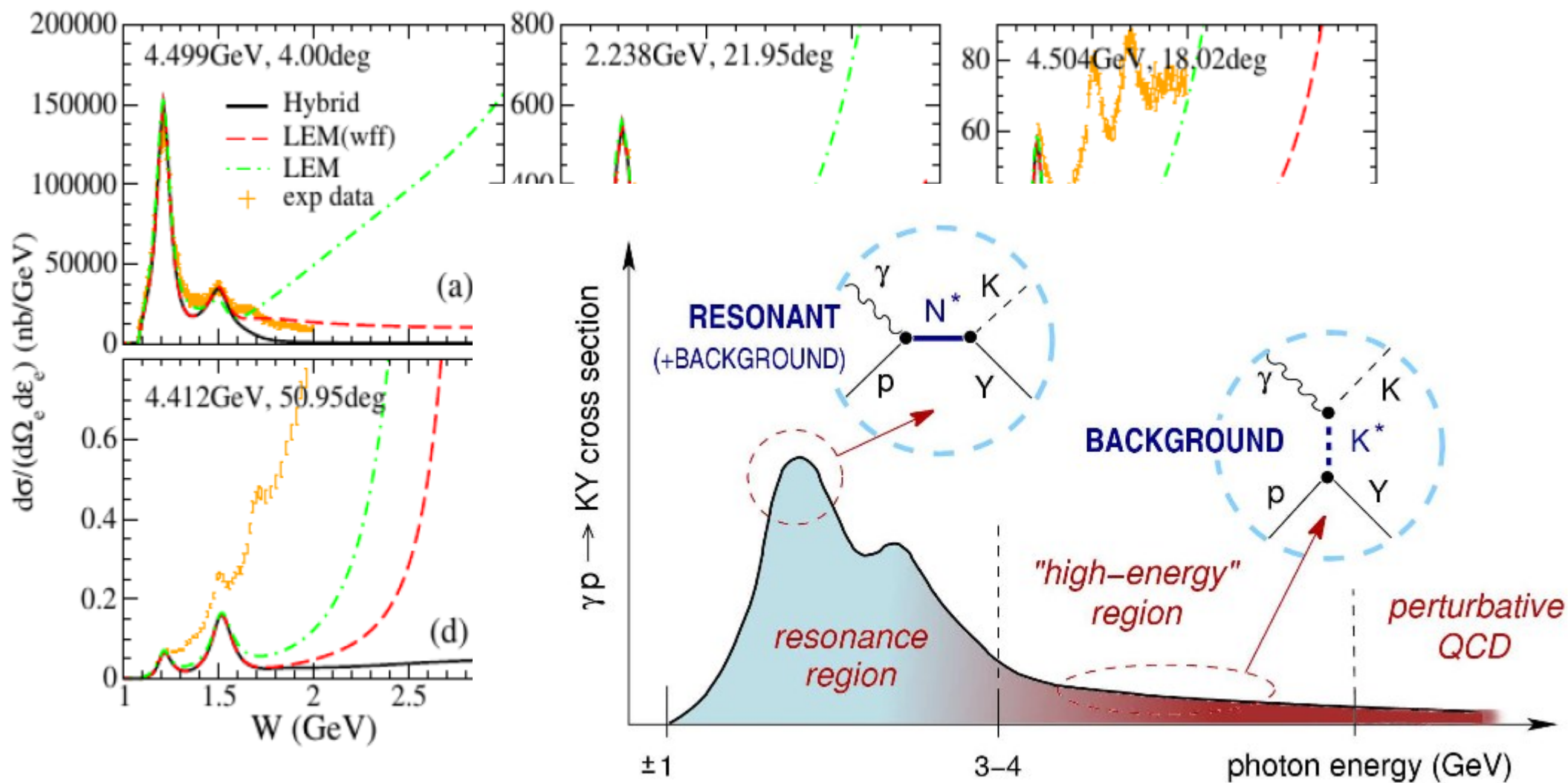
ChPT background



I. Single pion production on the nucleon – some issues of the LEM model ...



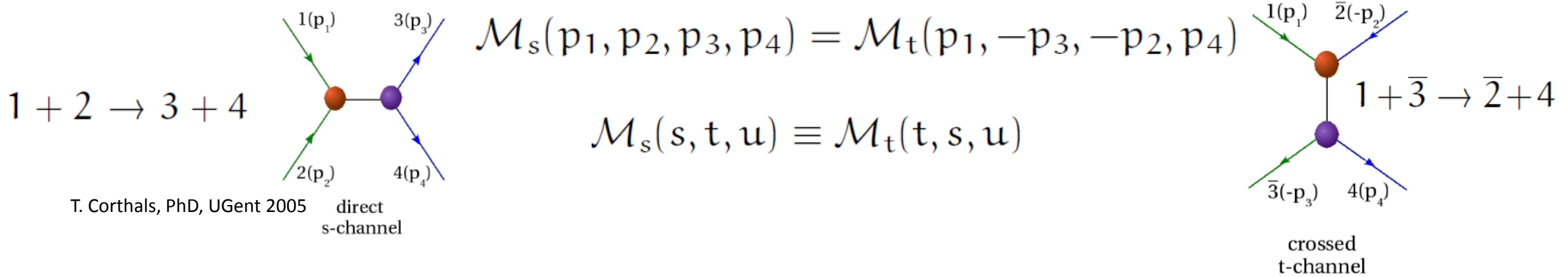
I. Single pion production on the nucleon – some issues of the LEM model ...



T. Corthals, PhD, UGent 2005

II. High energy model- Regge approach in a nutshell

- Based on crossing symmetry



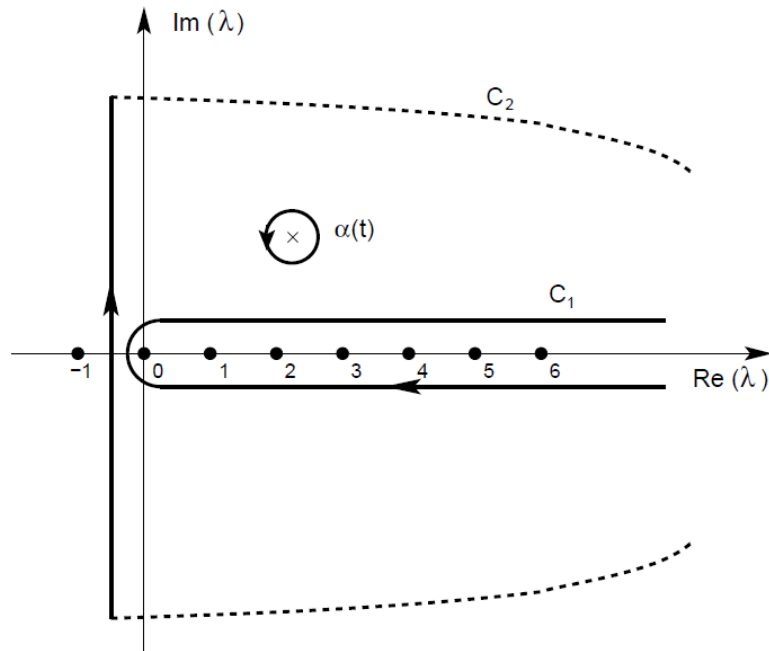
- Amplitude can be expanded in a Legendre series

$$\mathcal{M}_t(t, s) = \sum_{l=0}^{\infty} (2l + 1) \mathcal{M}_l(t) \mathcal{P}_l(\cos \theta_t) = \mathcal{M}_s(s, t)$$

II. High energy model- Regge approach in a nutshell

- The expansion expression can be transformed to a contour integral in the complex angular momentum plane

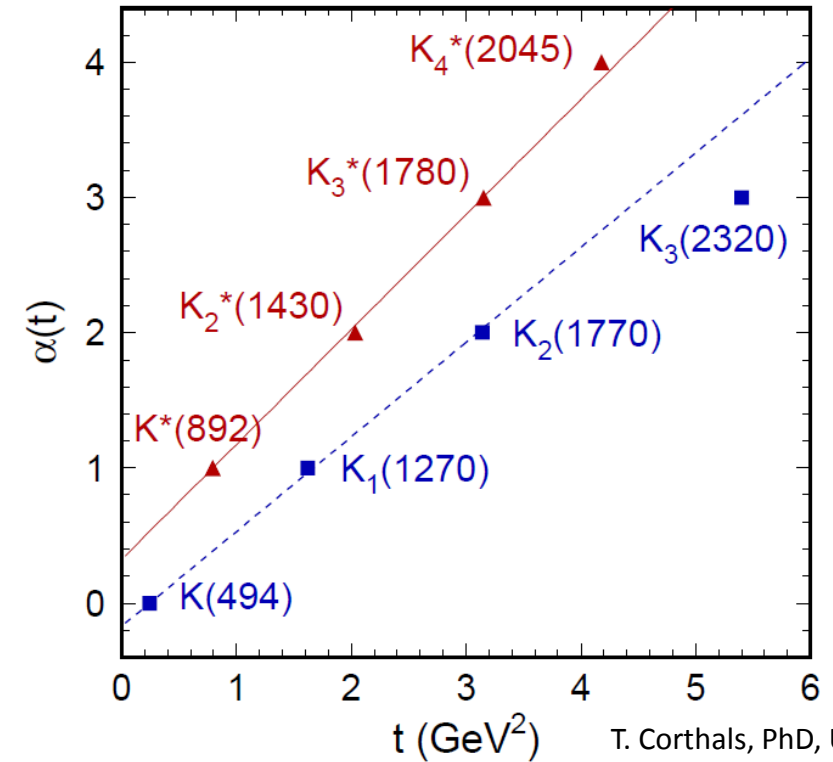
$$\mathcal{M}(s, t) = -\frac{1}{2i} \oint_{C_1} d\lambda \frac{(2\lambda + 1) \mathcal{M}_\lambda(t) P_\lambda(-\cos \theta_t)}{\sin(\pi\lambda)}$$



Poles $\lambda = \alpha_i(t)$

$$\alpha_i(t) = n$$

$$m = \sqrt{t}$$



T. Corthals, PhD, UGent 2005

II. High energy model- Regge approach in a nutshell

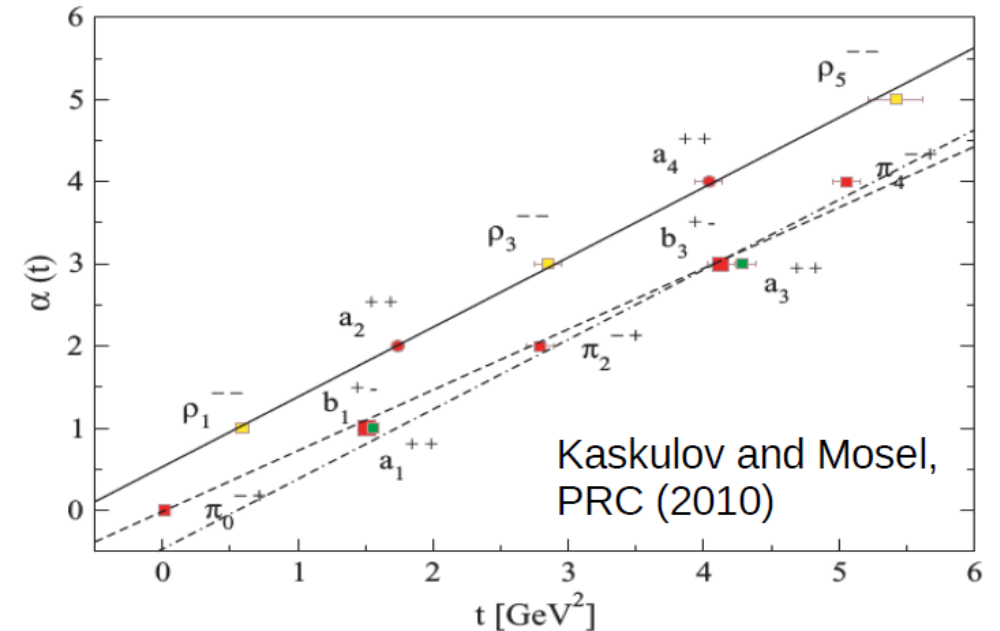
Regge recipe :

- Identify the appropriate Regge trajectories
- Establish t-dependence of amplitude
- Replace propagator by Regge propagator

$$\frac{1}{t - m_\pi^2}$$



$$\mathcal{P}_\pi(t, s) = -\alpha'_\pi \varphi_\pi(t) \Gamma[-\alpha_\pi(t)] (\alpha'_\pi s)^{\alpha_\pi(t)}$$

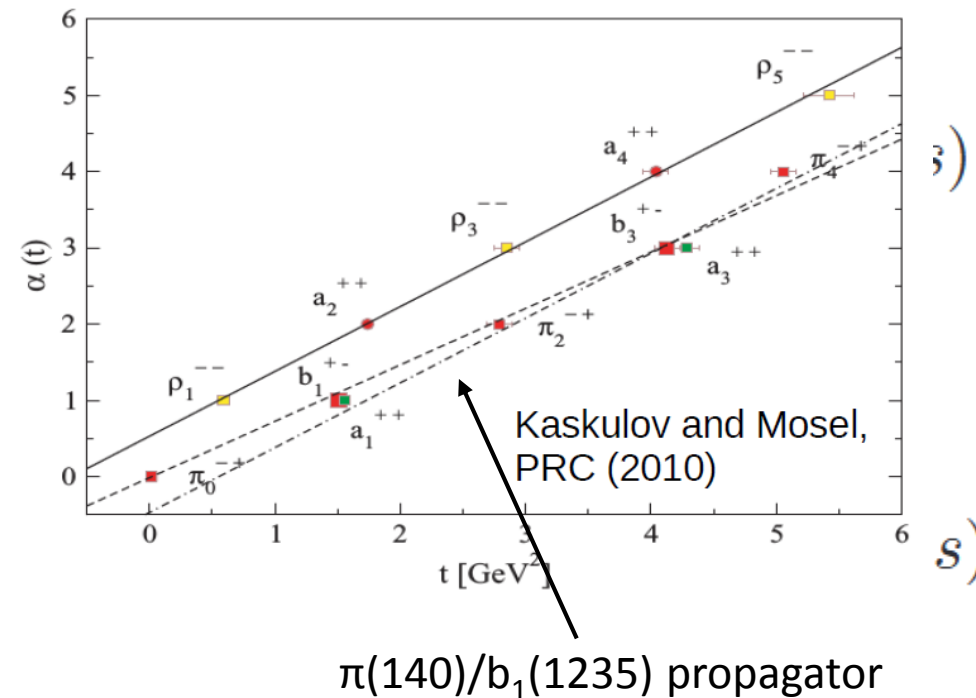
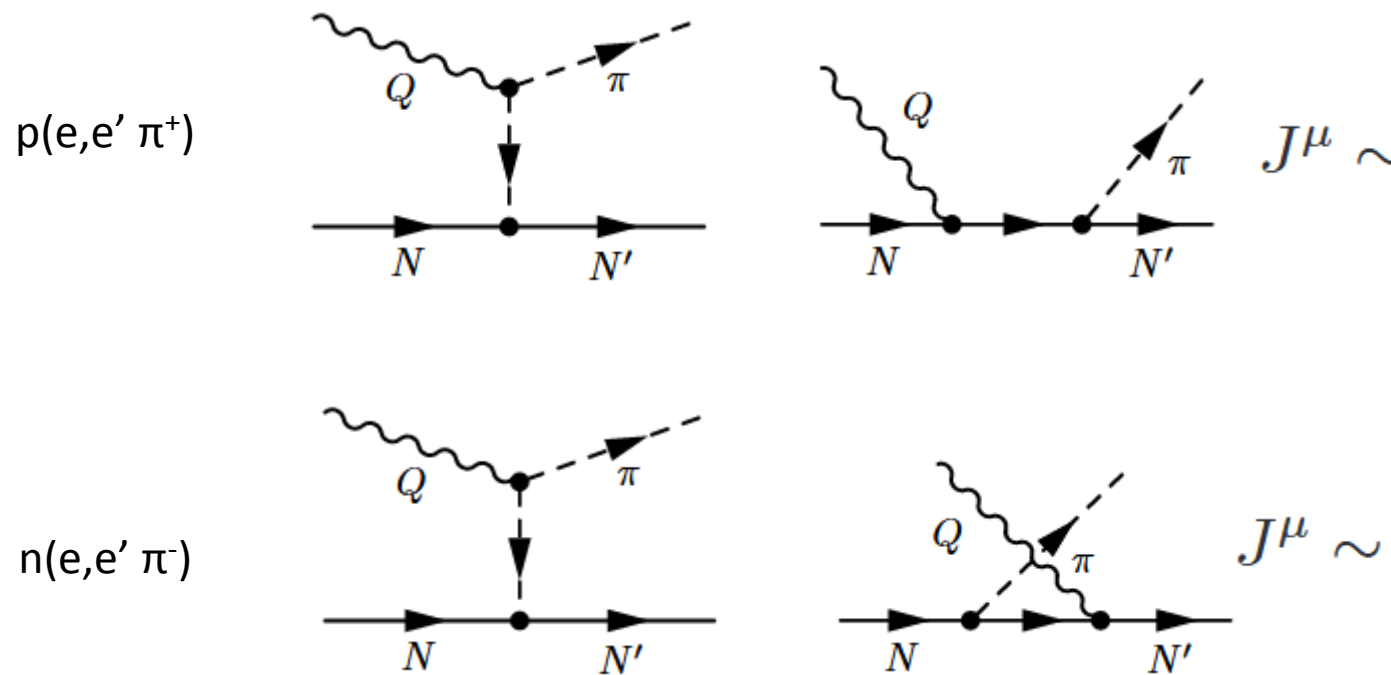


Regge theory provides the s dependence of the amplitude at high energies

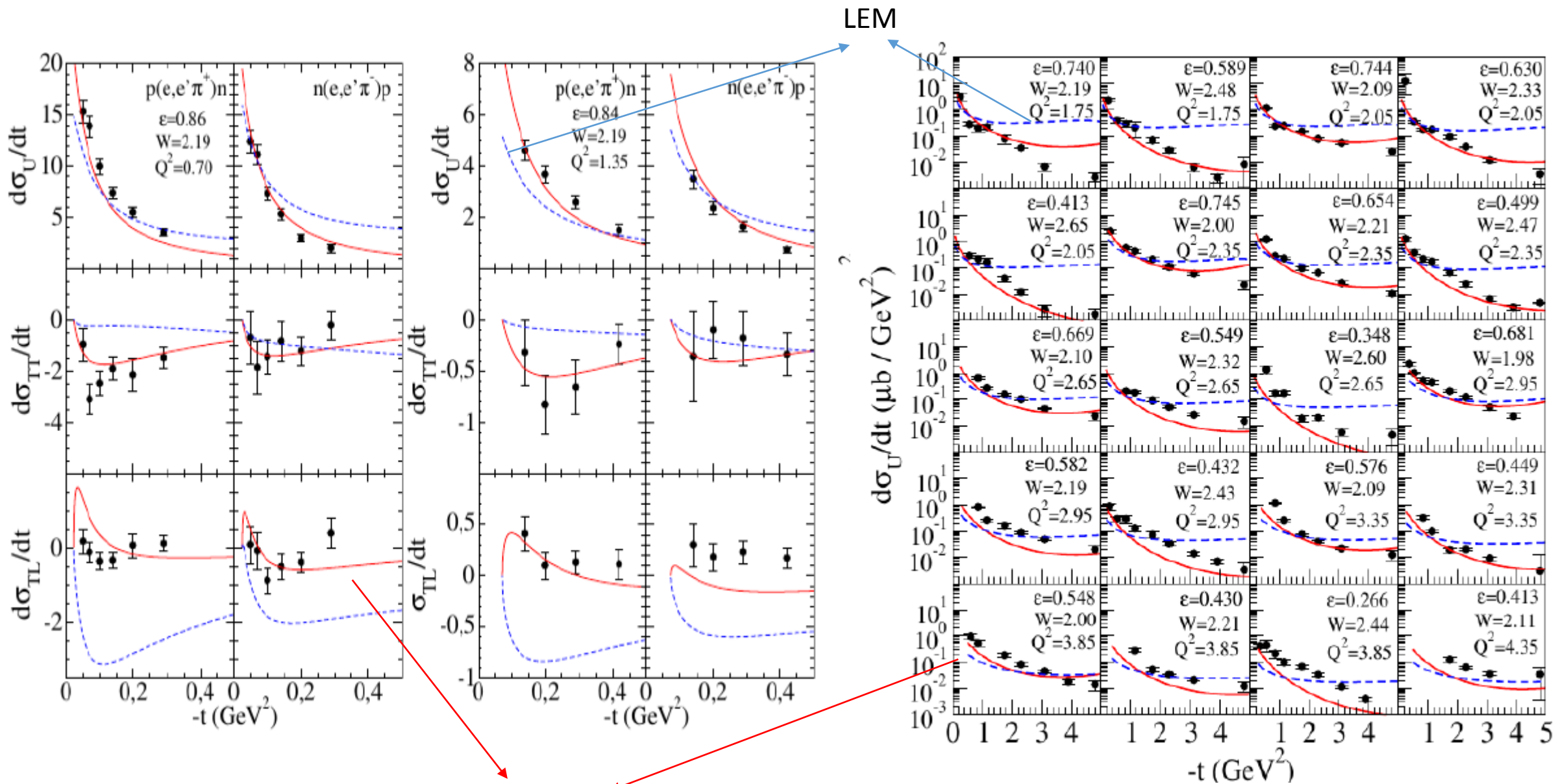
II. High energy model : vector part

Reggeizing the vector current : CVC – based on models for electroproduction of charged pions

- M. Guidal, J.-M. Laget, and M. Vanderhaeghen, Nucl. Phys. A627, 645 (1997).
- M. Kaskulov and U. Mosel, Phys. Rev. C81, 045202 (2010).
- M. Vanderhaeghen, M. Guidal, and J.-M. Laget, Phys. Rev. C57, 1454 (1998).
- T. Vrancx and J. Ryckebusch, Phys. Rev. C89, 025203 (2014).

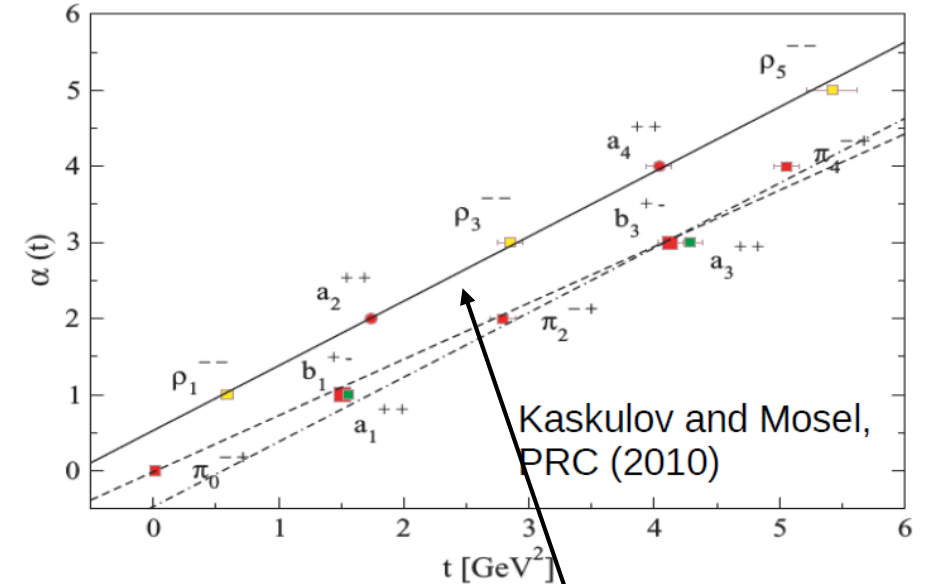
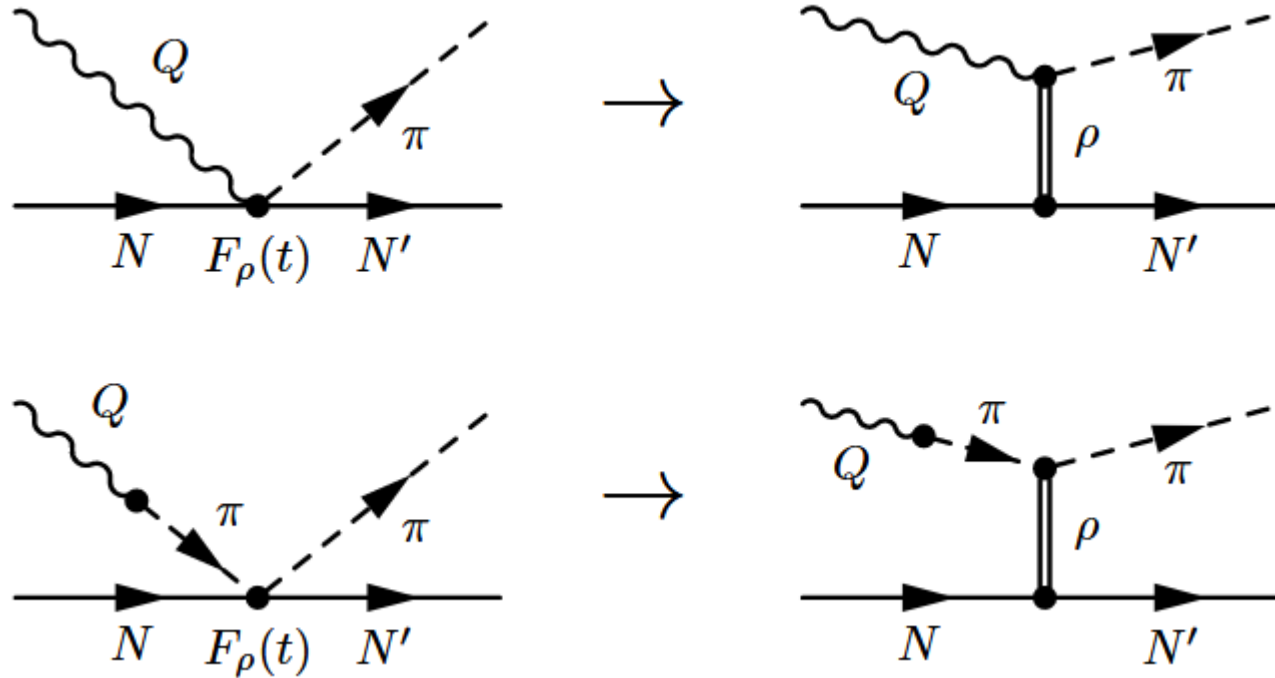


II. High energy model – results for electron scattering



II. High energy model : axial part

Identify the Regge trajectory for the axial current

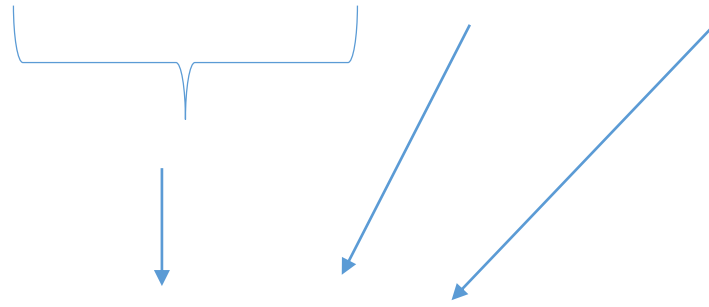


$\rho(770)/a_2(1320)$ propagator

II. High energy model : axial part

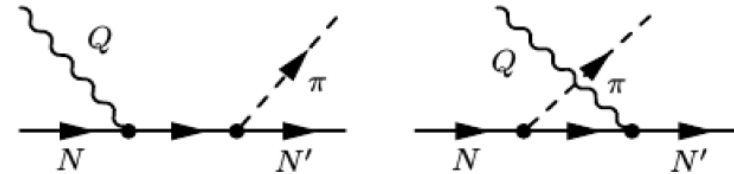
Reggeizing the axial current : PCAC –

CT ρ + PP ρ + Npa + CNPa



Fulfill PCAC

ReChi model: One free parameter in the boson-nucleon-nucleon vertex

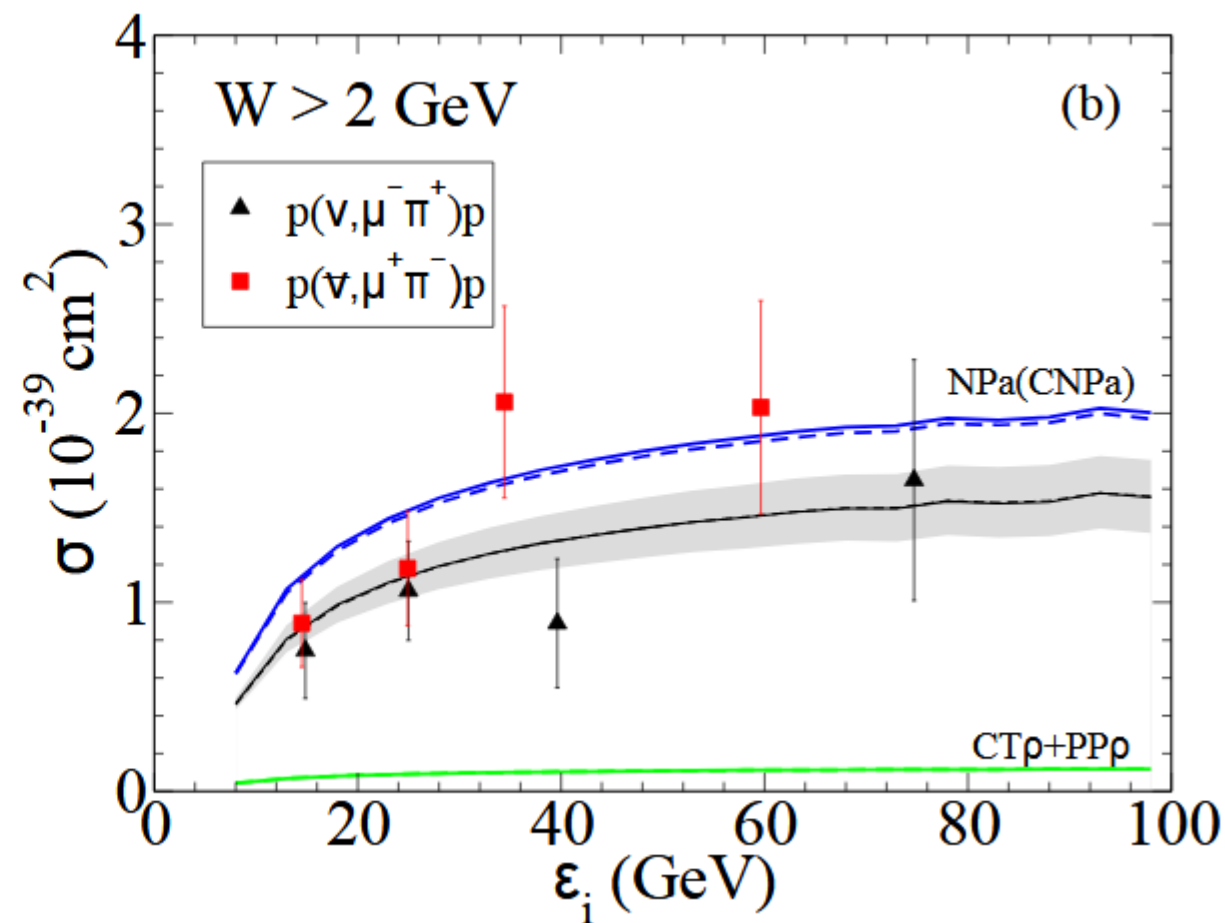
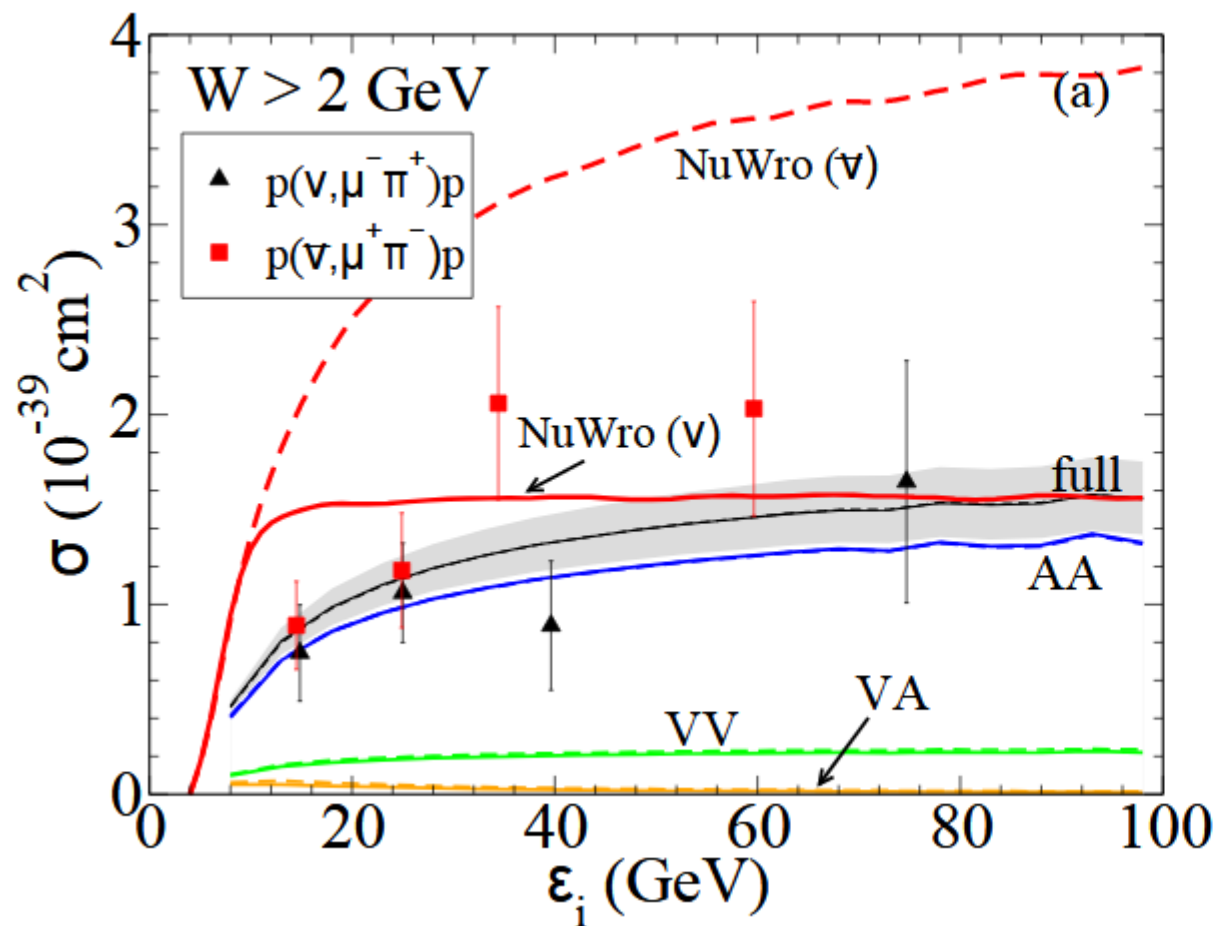


$$G_A[Q^2, s(u)] = g_A \left(1 + \frac{Q^2}{\Lambda_{Apn^*} [s(u)]^2} \right)^{-2}$$

$$\Lambda_{Apn^*}(s) = \Lambda_{Apn} + (\Lambda_{\infty}^A - \Lambda_{Apn}) \left(1 - \frac{M^2}{s} \right)$$

$$\Lambda_{\infty}^A = (7.20 \pm 2.09 \pm 1.32) \text{ GeV}$$

II. High energy model : results



Data :P. Allen et al. Nucl. Phys. B264, 221 (1986).

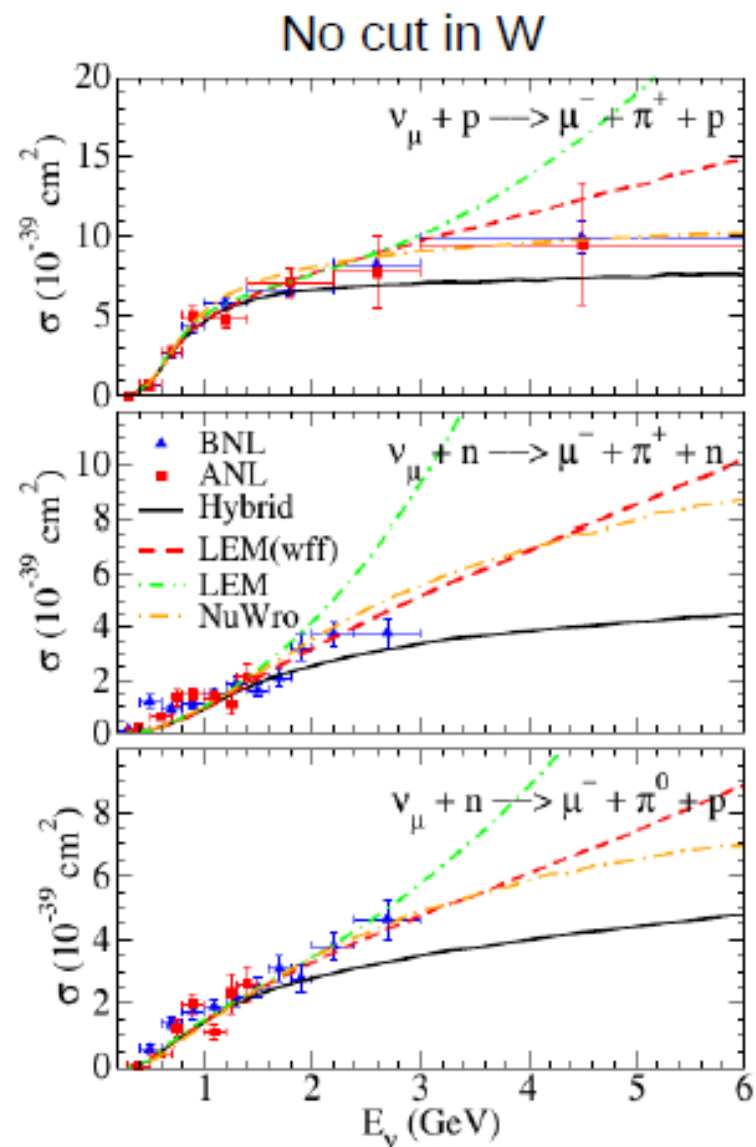
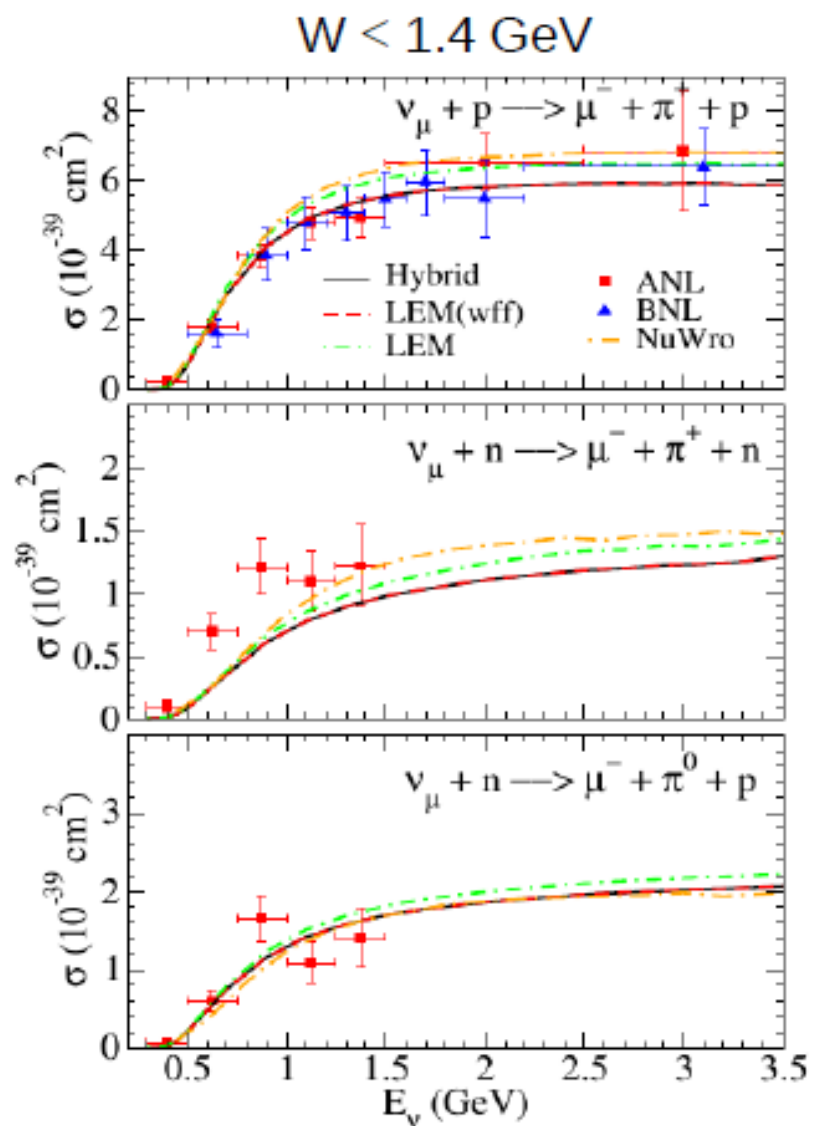
III. Hybrid model : merge both models in a phenomenological way

$$\tilde{\mathcal{O}} = \cos^2 \phi(W) \mathcal{O}_{ChPT} + \sin^2 \phi(W) \mathcal{O}_{ReChi}$$

$$\phi(W) = \frac{\pi}{2} \left(1 - \frac{1}{1 + \exp \left[\frac{W - W_0}{L} \right]} \right)$$

$W < 1.4$ GeV : LEM model : resonances + ChPT background
 $W > 2$ GeV : Regge background contributions

III. Hybrid model – results



IV. Hybrid model – put the nucleon in a nucleus

Plane waves (for the moment...)

$$J_{had}^{\mu} = \sum_i^A \int dr \bar{\Psi}_F(\mathbf{r}) \phi^*(\mathbf{r}) \hat{O}_{one-body}^{\mu}(\mathbf{r}) \Psi_B(\mathbf{r}) e^{i\mathbf{q}\cdot\mathbf{r}}$$

not yet

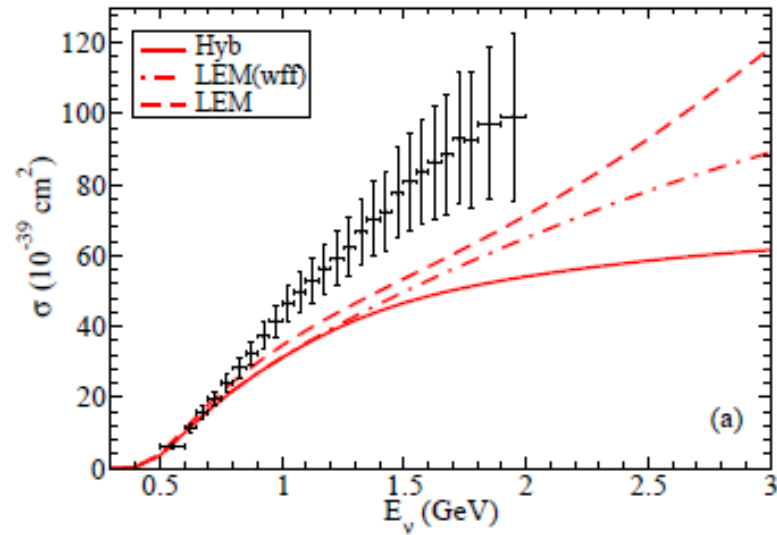
Relativistic mean-field
wave functions

+ comparison with NuWro final state

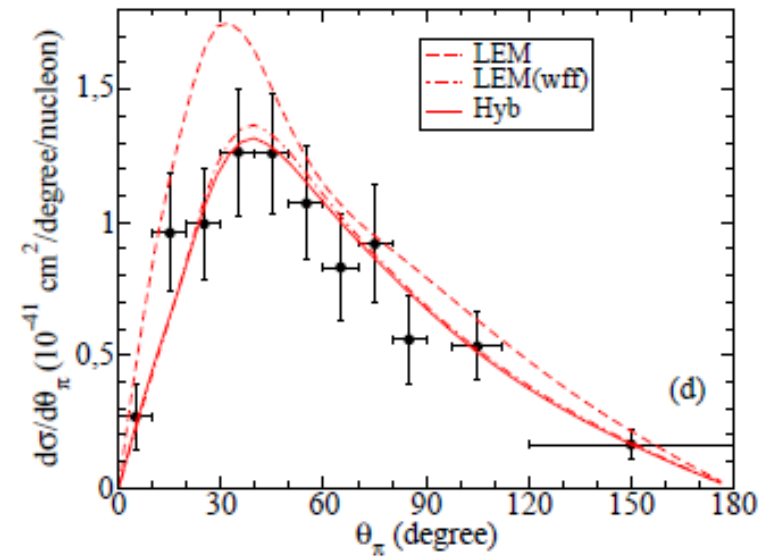
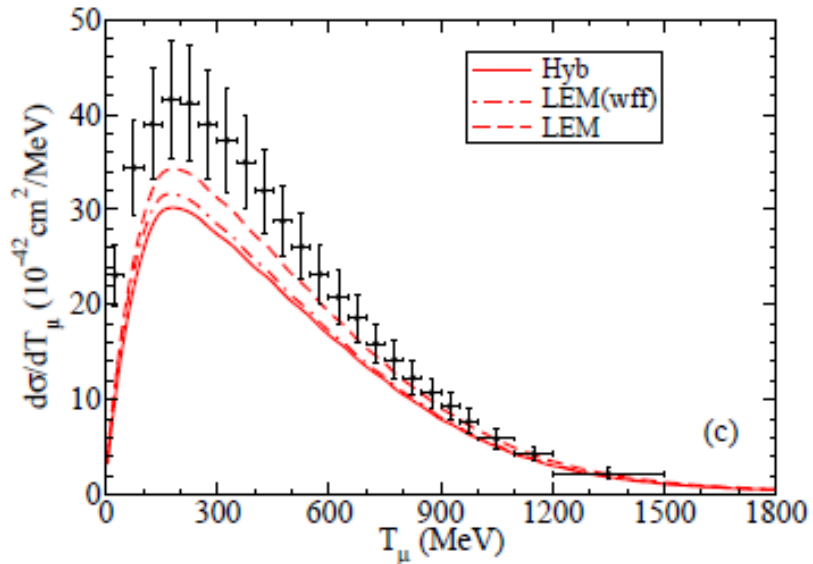
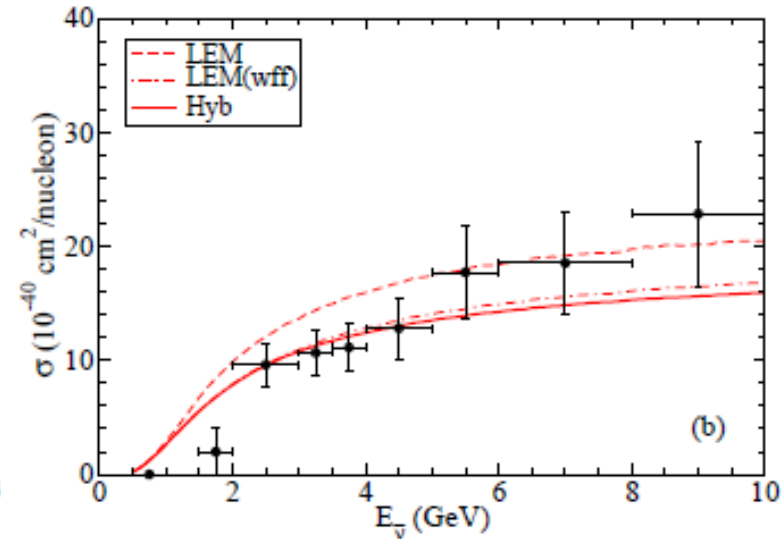
+ investigate effect of medium modifications

IV. Hybrid RPWIA model – results MiniBooNE and MINERvA

MiniBooNE $\nu\text{CC } 1\pi^+$

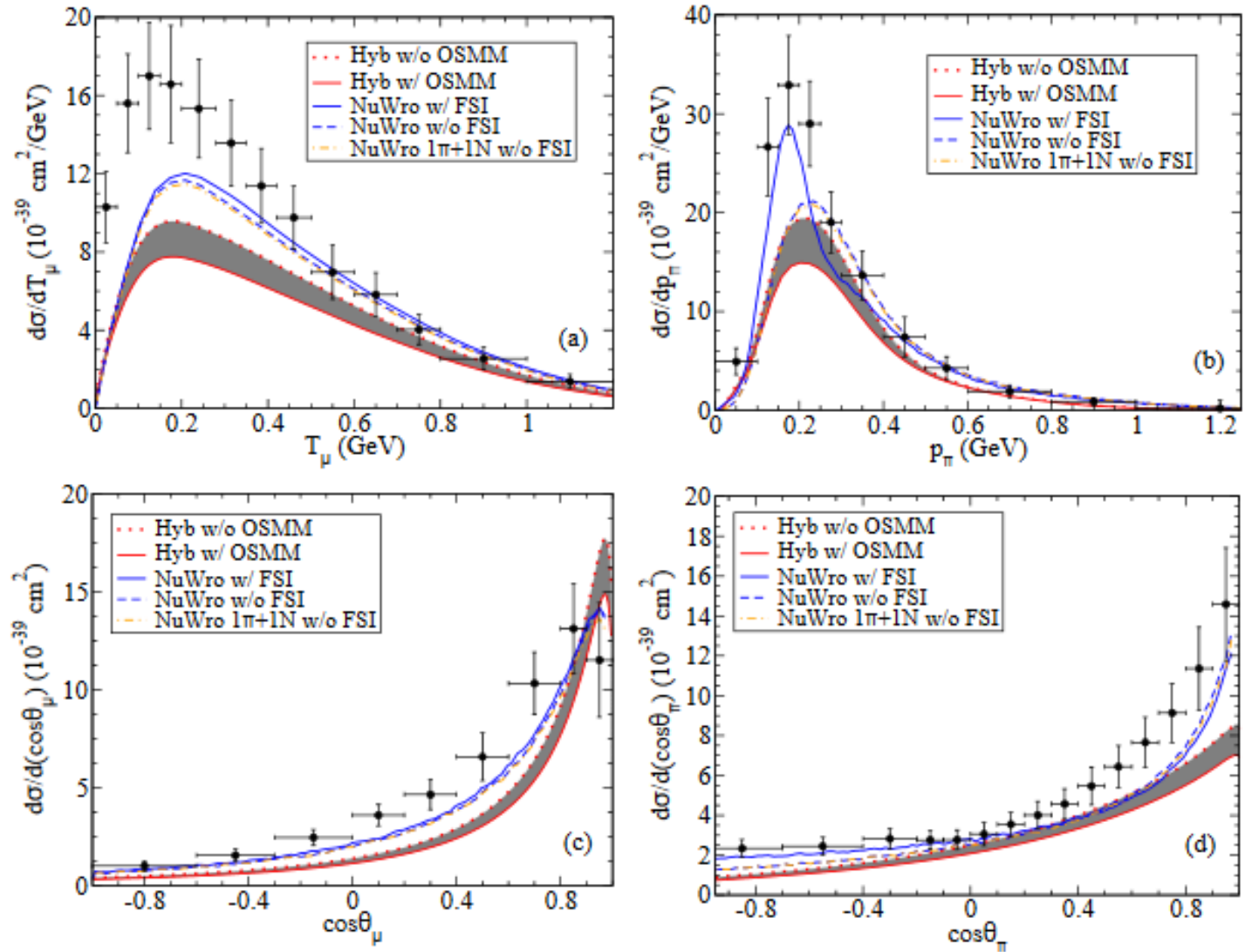


MINERvA $\bar{\nu}\text{CC } 1\pi^0$

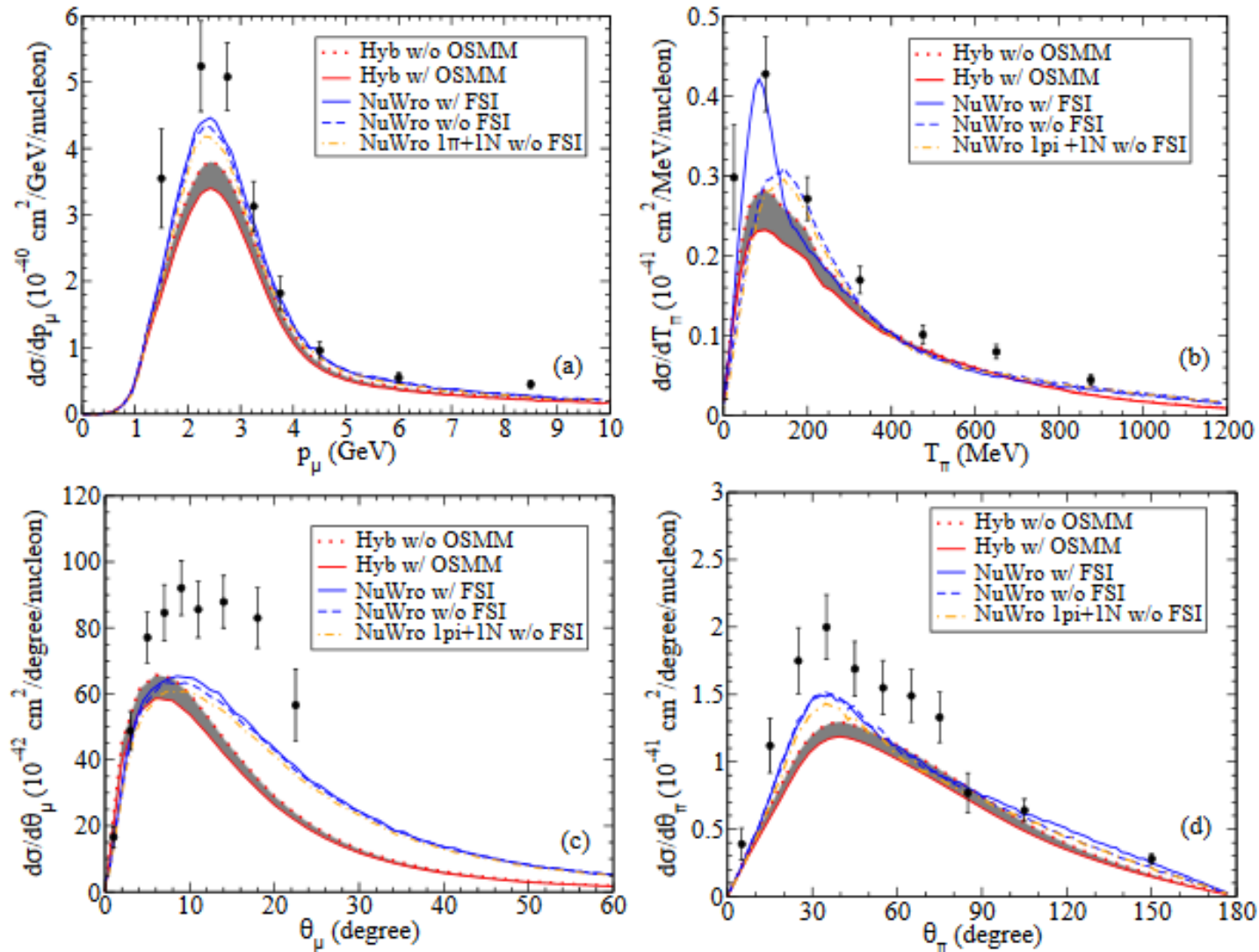


IV. Hybrid RPWIA model – results and comparison with NuWro

MiniBooNE ν CC $1\pi^0$

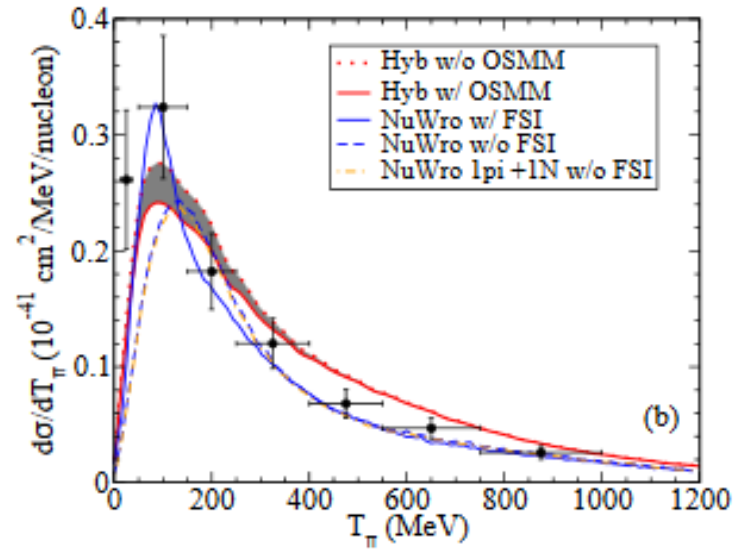
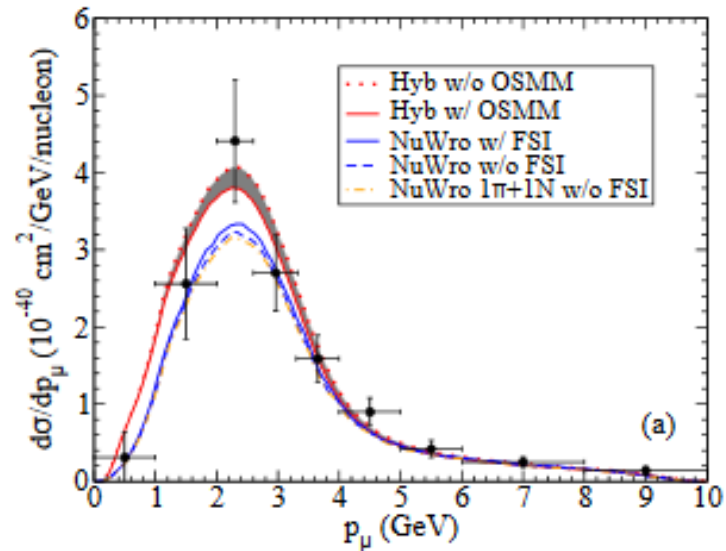


IV. Hybrid RPWIA model – results

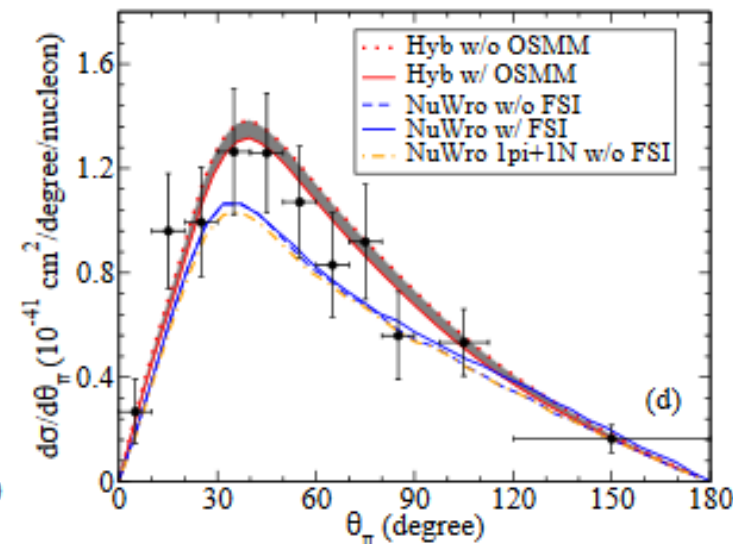
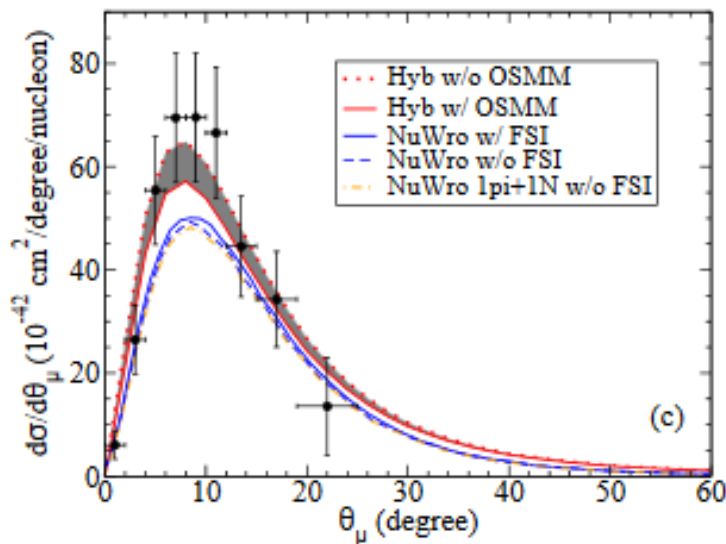


MINERvA $\nu_{CC} 1\pi^0$

IV. Hybrid RPWIA model – results

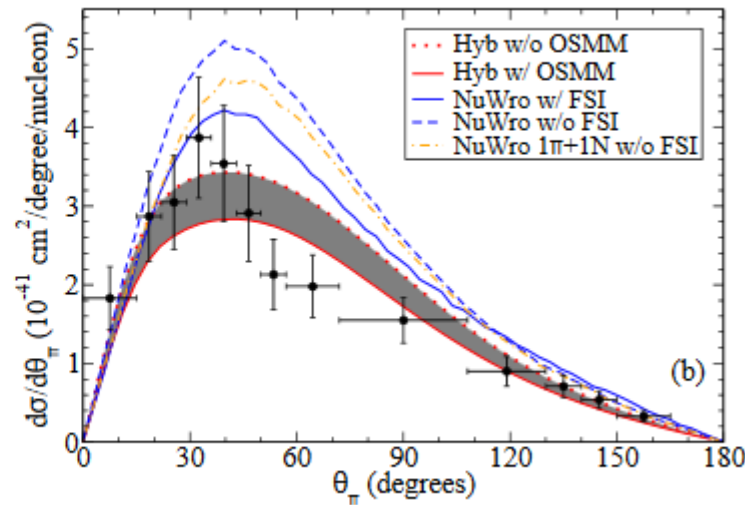
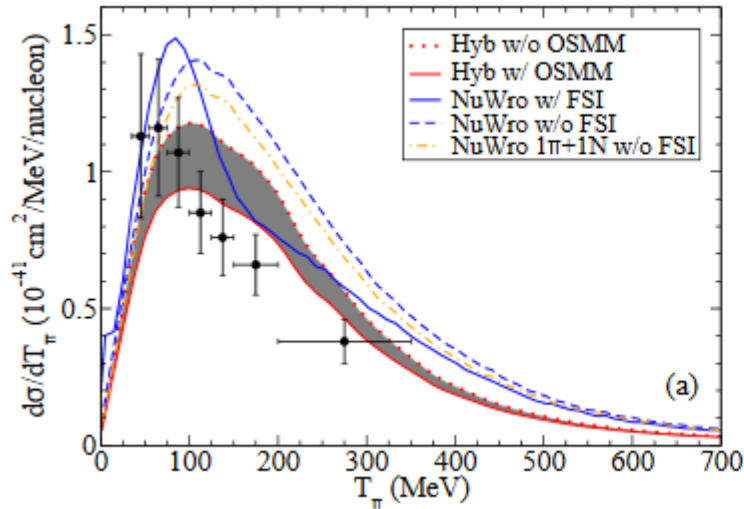
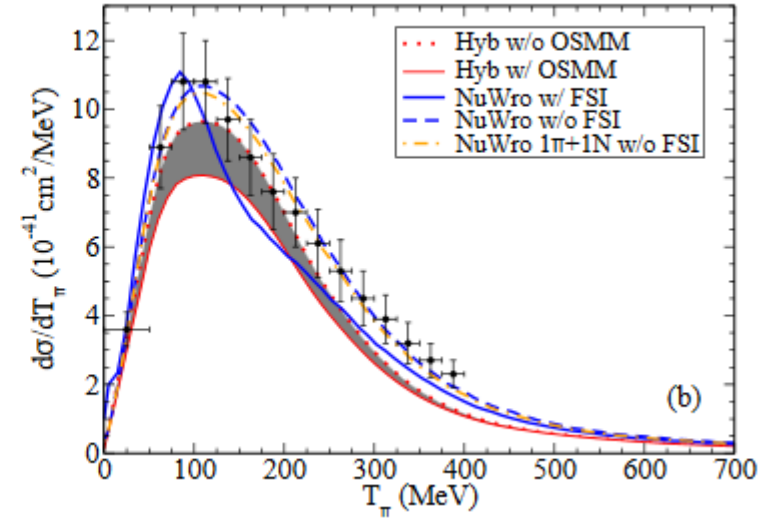
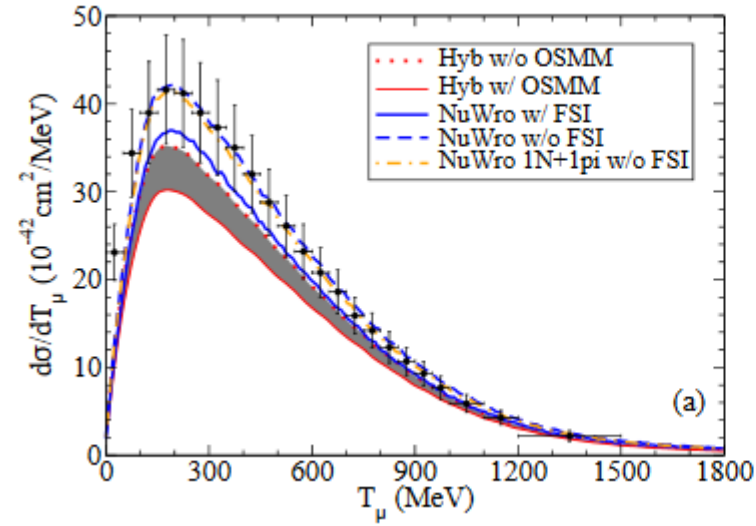


MINERvA $\bar{\nu}CC 1\pi^0$



IV. Hybrid RPWIA model – results

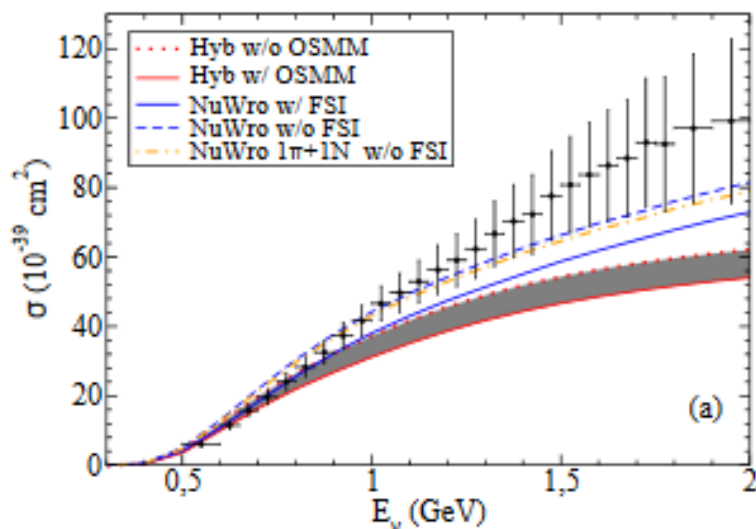
MiniBooNE ν CC $1\pi^+$



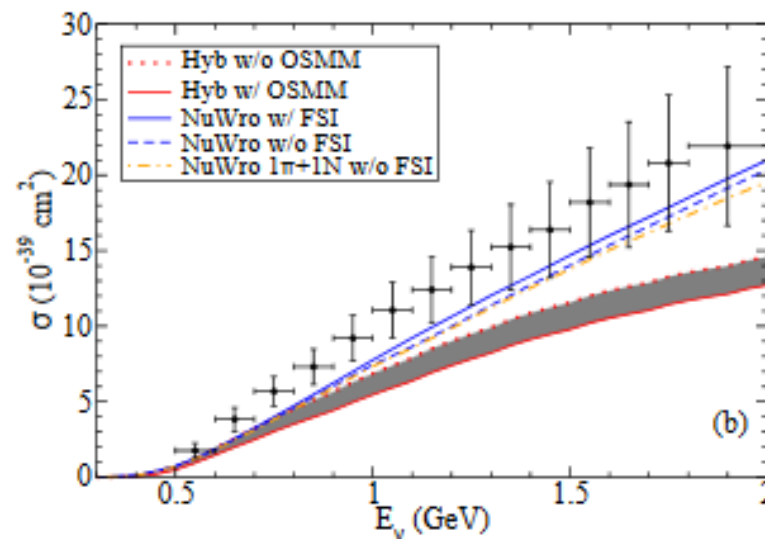
MINERvA ν CC $1\pi^+$

IV. Hybrid RPWIA model – results

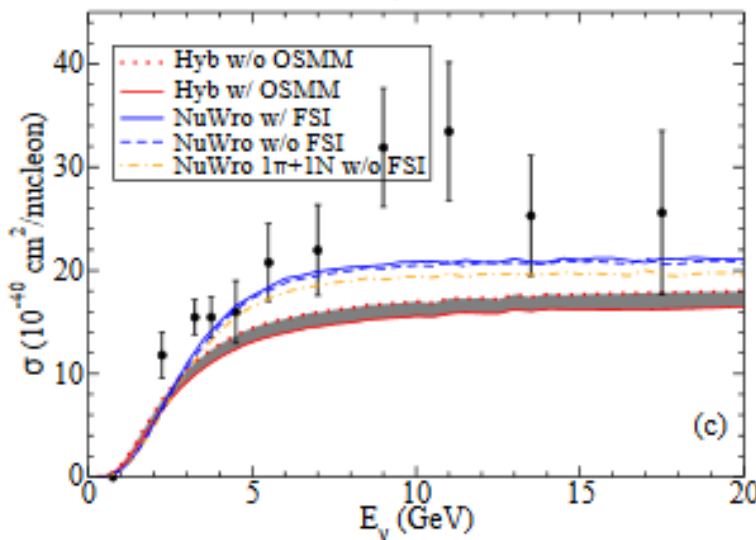
MiniBooNE $\nu\text{CC } 1\pi^+$



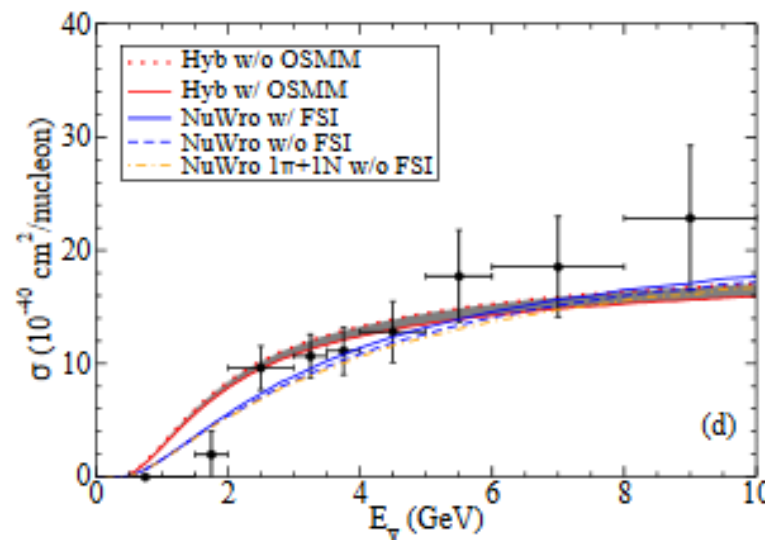
MiniBooNE $\nu\text{CC } 1\pi^0$



MINERvA $\nu\text{CC } 1\pi^0$

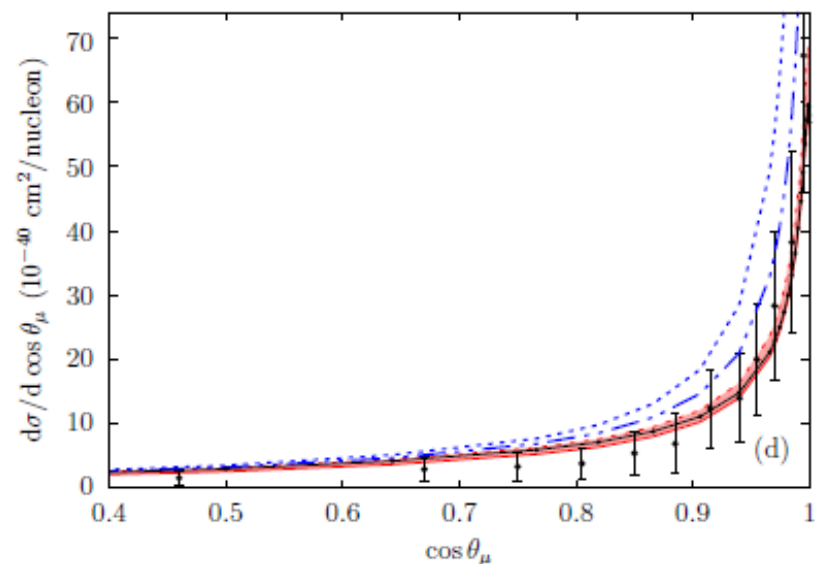
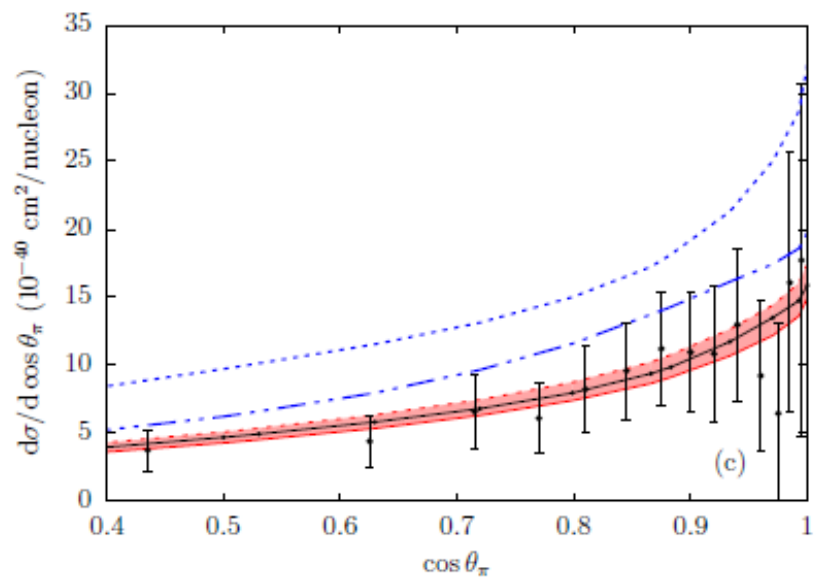
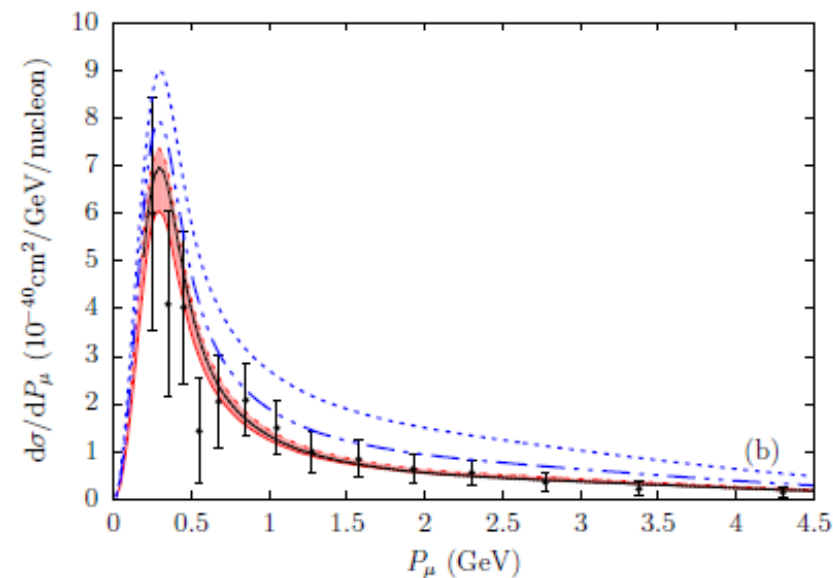
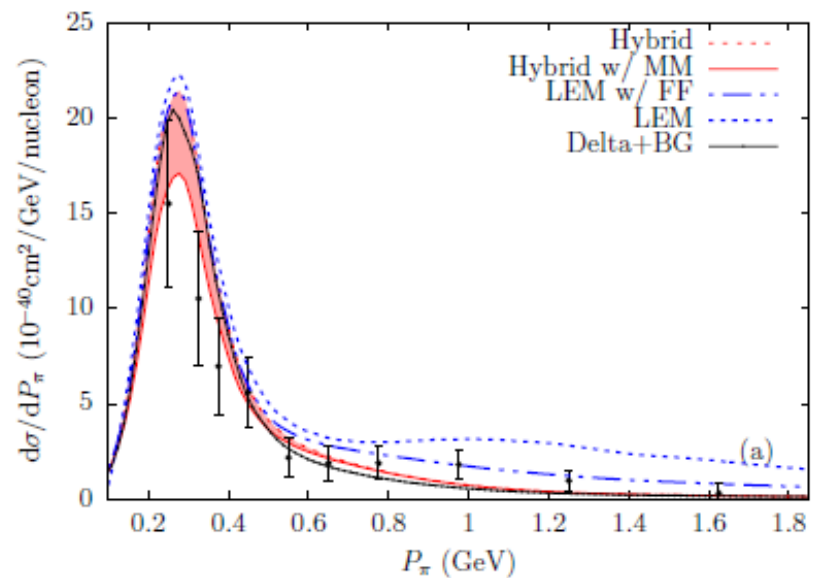


MINERvA $\bar{\nu}\text{CC } 1\pi^0$



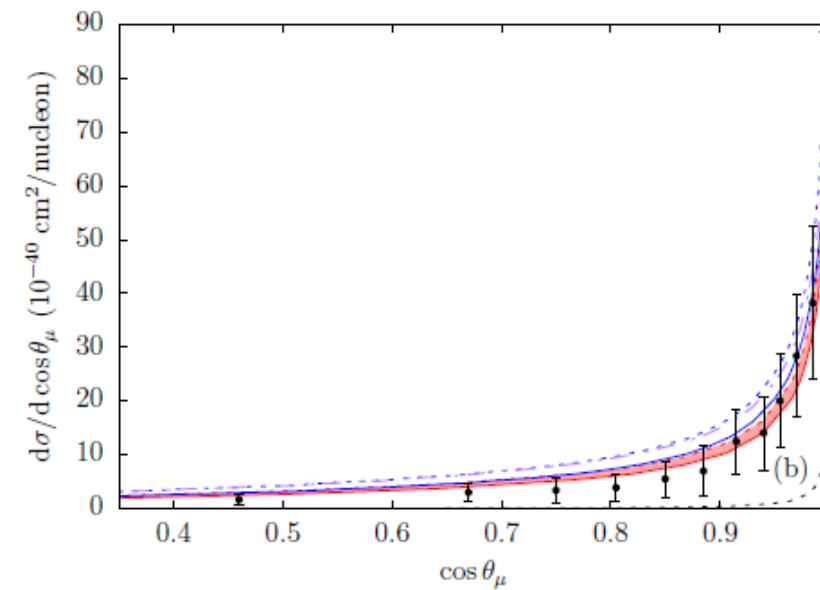
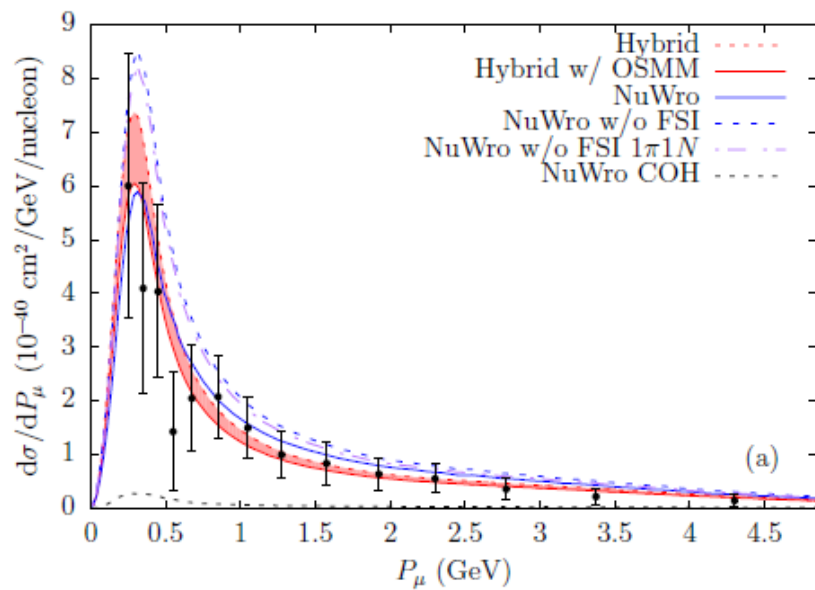
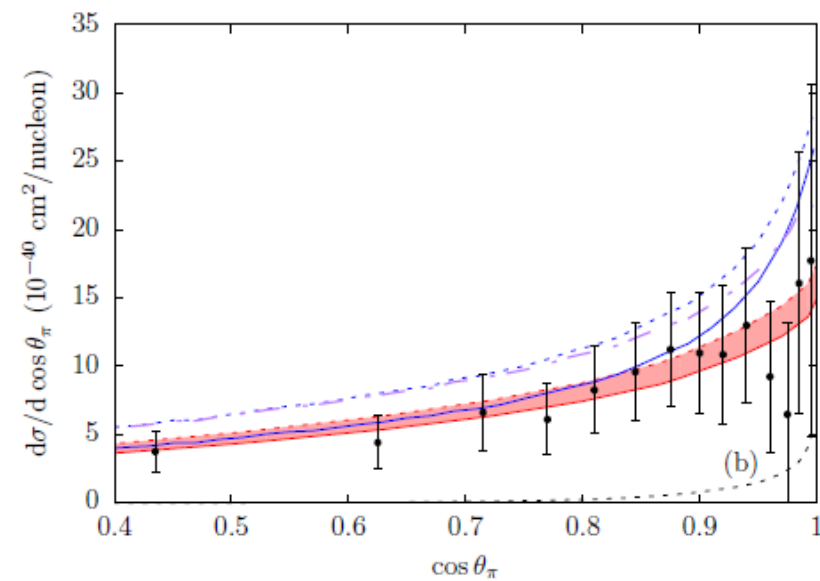
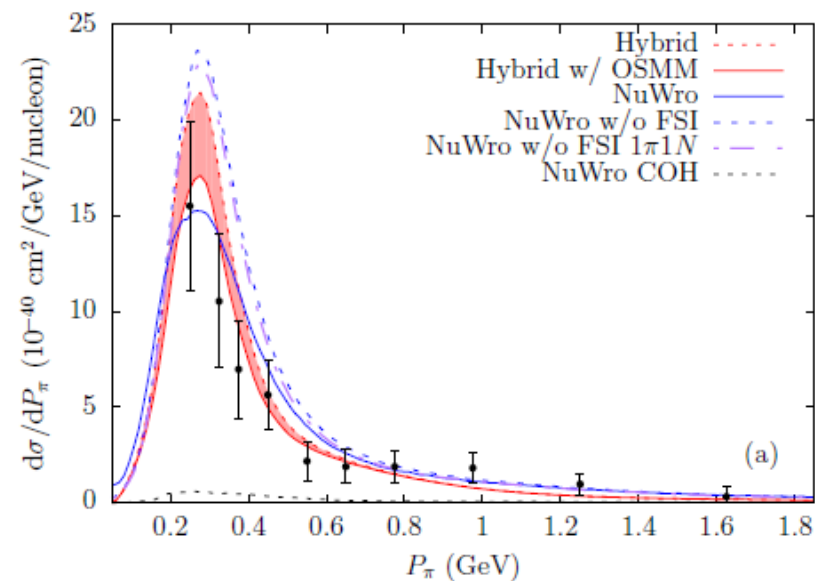
IV. Hybrid RPWIA model – results

T2K CC1 π^+



IV. Hybrid RPWIA model – results

T2K CC1 π^+



V. Extending the Hybrid model – distorted final state

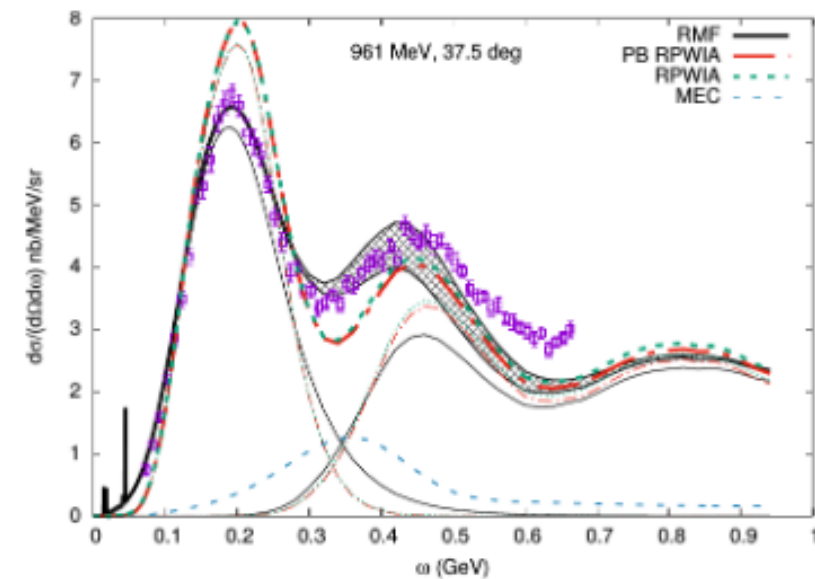
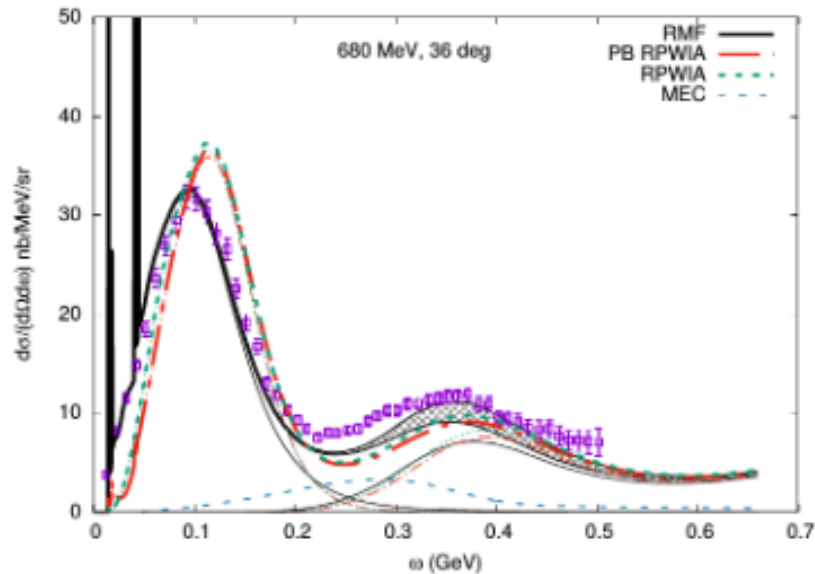
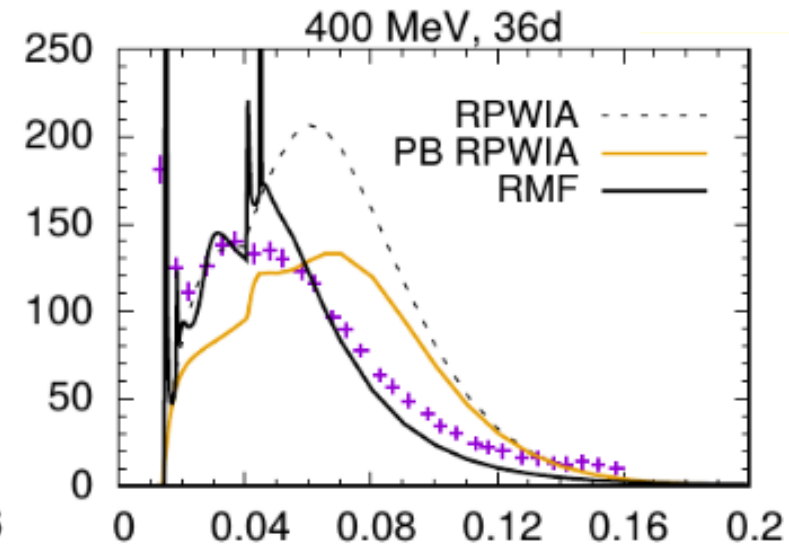
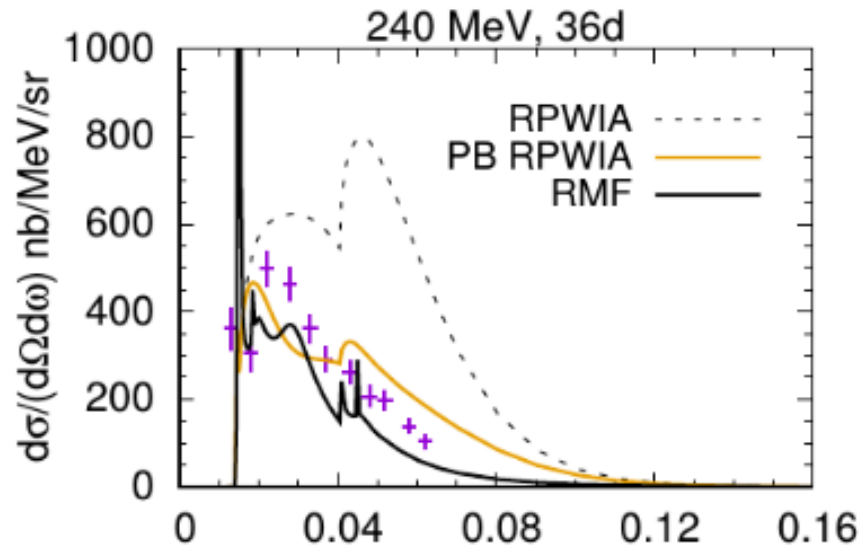
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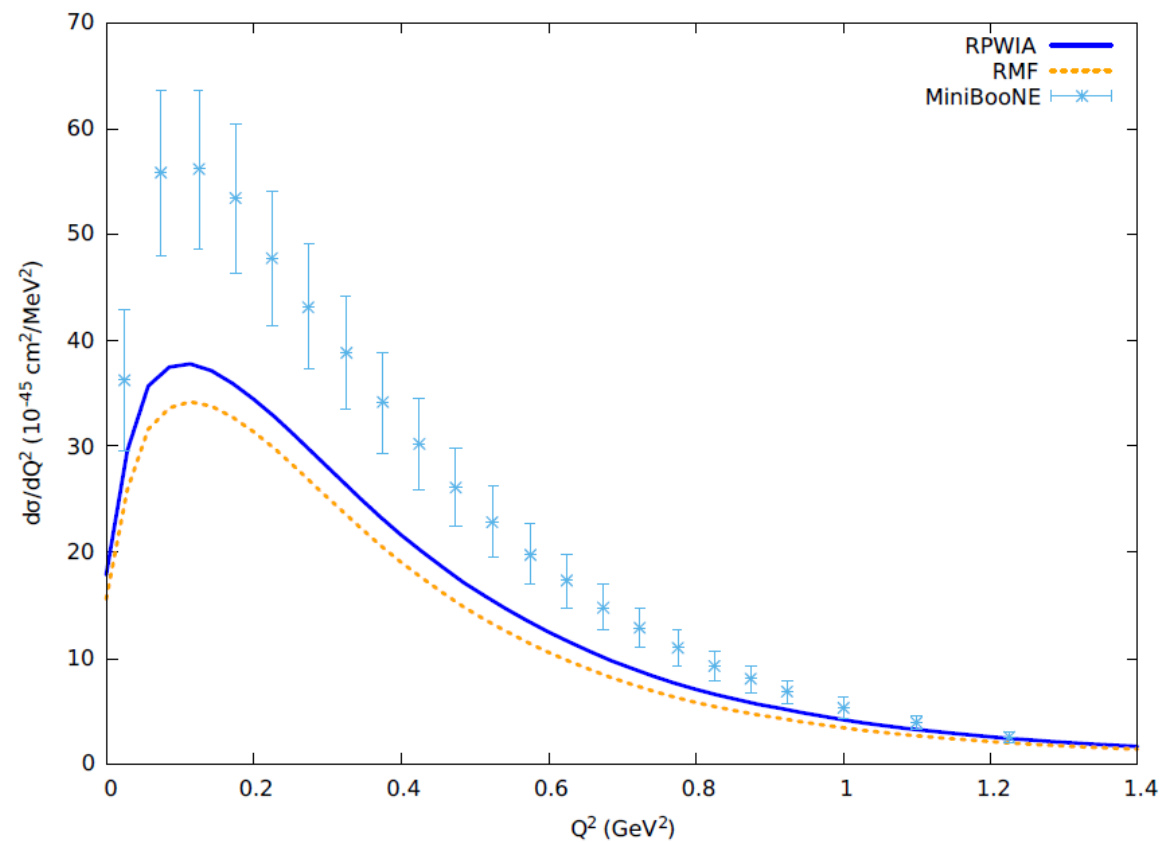
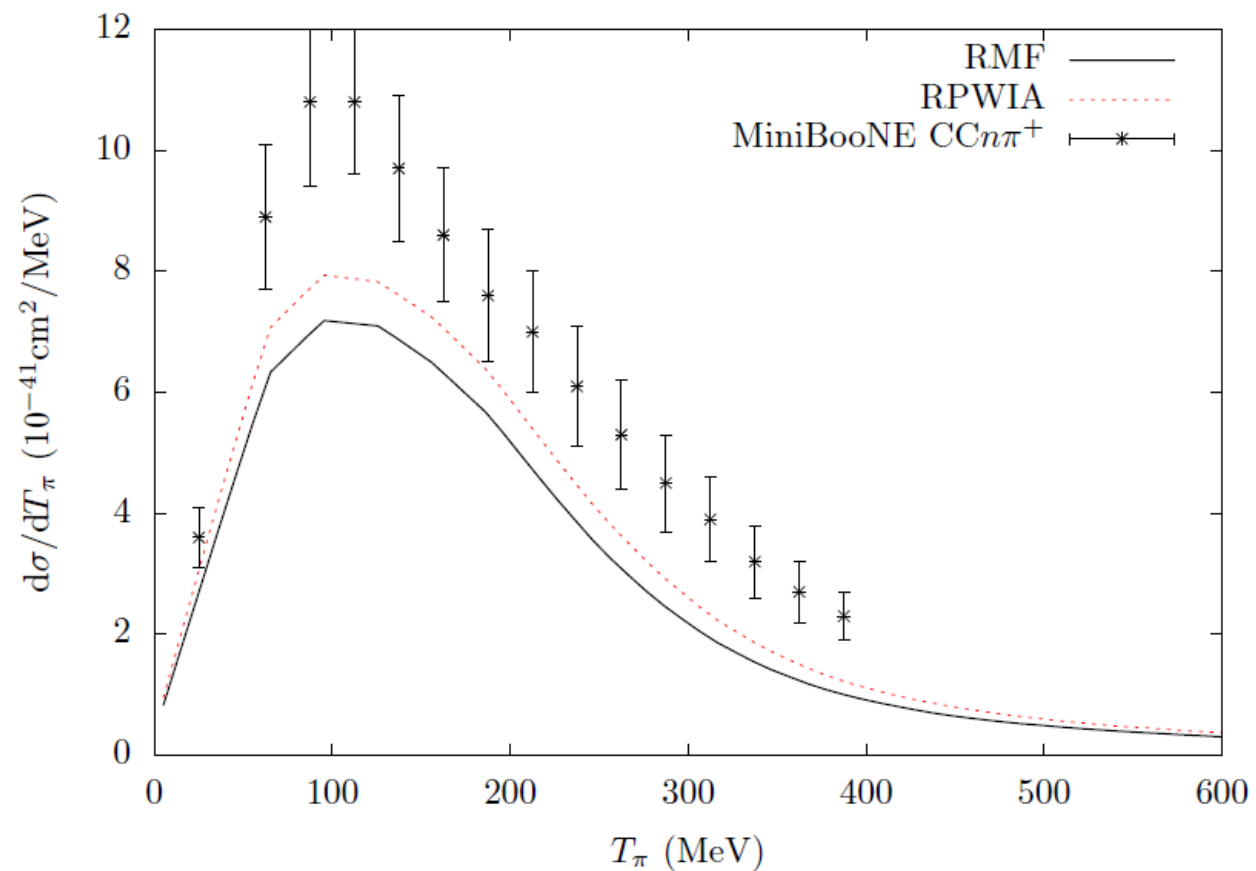
Relativistic mean-field wave functions

V. Extending the Hybrid model – distorted final state

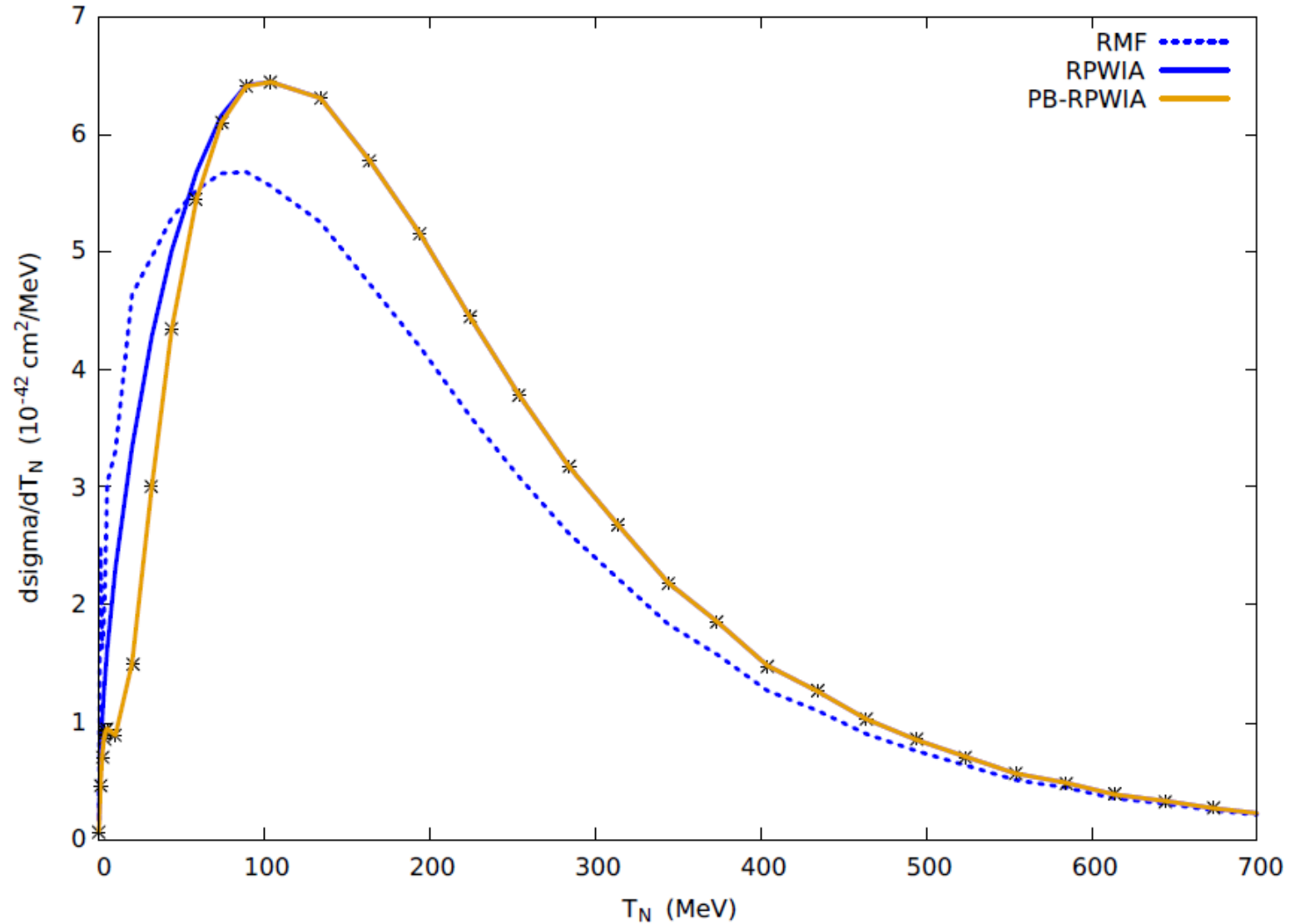
$^{12}\text{C}(e,e')$



V. Extending the Hybrid model – distorted final state



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Summary

- Detailed microscopic cross sections calculations for neutrino-induced pion production
- Formalism valid over a broad energy range
- Taking into account as many nuclear physics aspects as feasible
- Estimate effect of FSI in comparing with NuWro