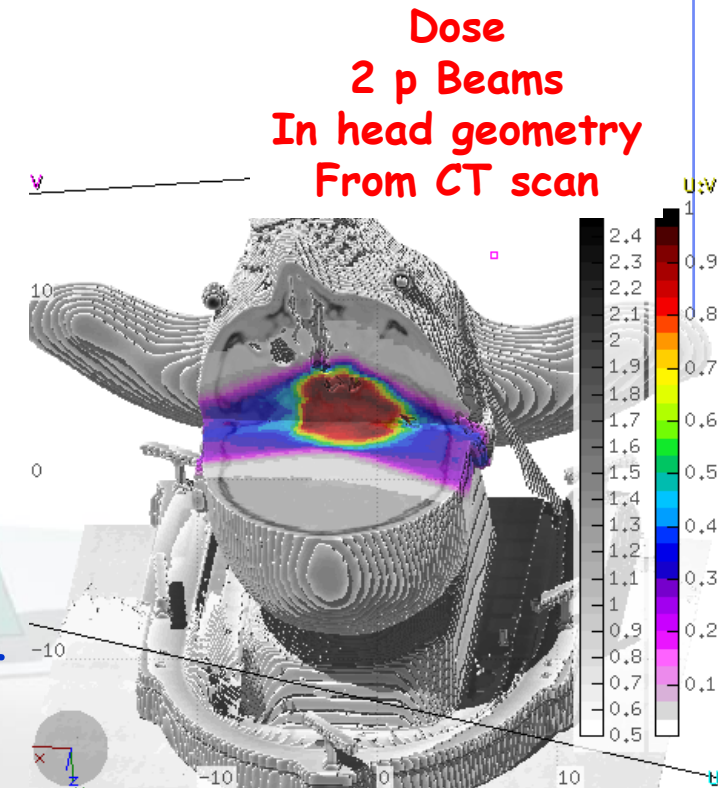
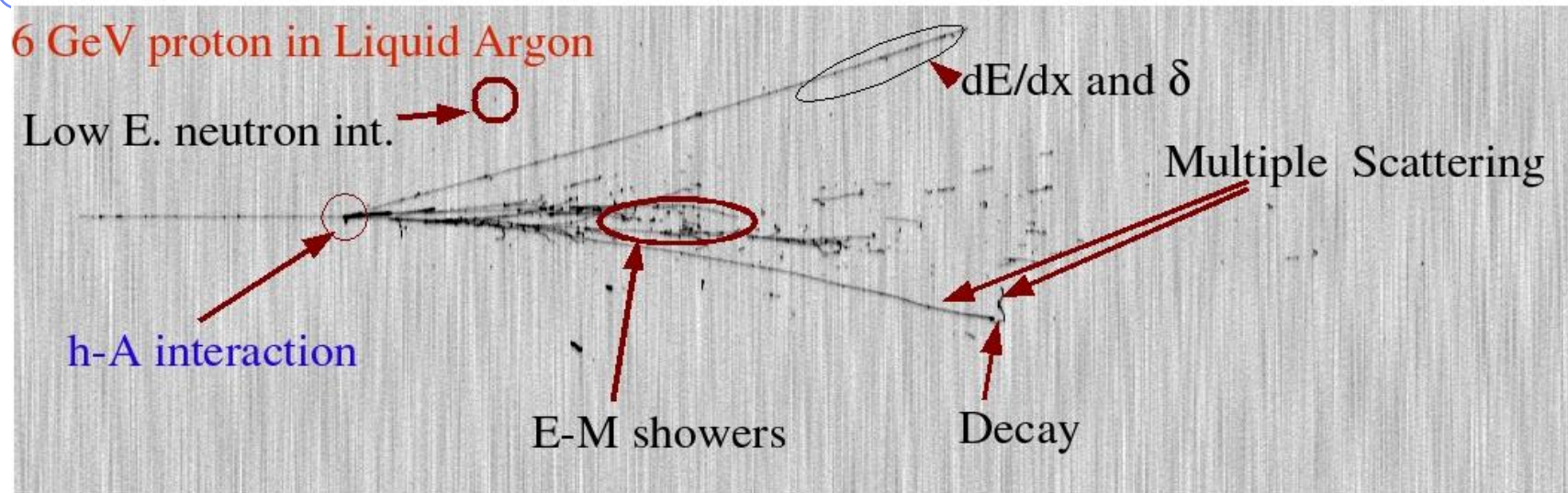




Neutrino interactions in FLUKA: NUNDIS

M. Antonello, G. Battistoni, A. Ferrari, M. Lantz, **P. Sala**, G. Smirnov

FLUKA : a multi-purpose Monte Carlo code



Developed and maintained under an INFN-CERN agreement
Copyright 1989-2018 CERN and INFN

Web Site: <http://www.fluka.org>

>10000 registered users

2 user courses /year

General framework

- Nuclear models in FLUKA have been developed along the years, initially for hadron-nucleus reactions,
- Then extended to treat also
 - Photonuclear reactions
 - Muon-nuclear and electro-nuclear via virtual photon exchange
 - Quasi-elastic electron scattering
 - Muon capture
 - Neutrino interactions
 - Anti-nucleon reactions
- All sharing the same generalized IntraNuclearCascade + Preequilibrium+Evaporation +Gamma deexcitation model
- All DIS share the same fragmentation
- PROs: well tested, valid for all target nuclei, consistent with detector simulations
- CONS : some details of nuclear structure missing, coherent effects have to be inserted ad-hoc

Neutrinos in FLUKA

- Generators of neutrino-nucleon interactions:
 - QuasiElastic
 - Resonance
 - DIS
- Embedded in FLUKA nuclear models for Initial State and Final State effects
- Only for Argon: absorption of few-MeV (solar) neutrinos on whole nucleus
- Elastic scattering on electrons - to be refreshed
- Products of the neutrino interactions can be directly transported in the detector (or other) materials
- Used for all ICARUS simulations/publications

Acta Phys.Polon. B40 (2009) 2491-2505
CERN-Proceedings-2010-001 pp.387-394.

Quasi Elastic and Resonant

QE

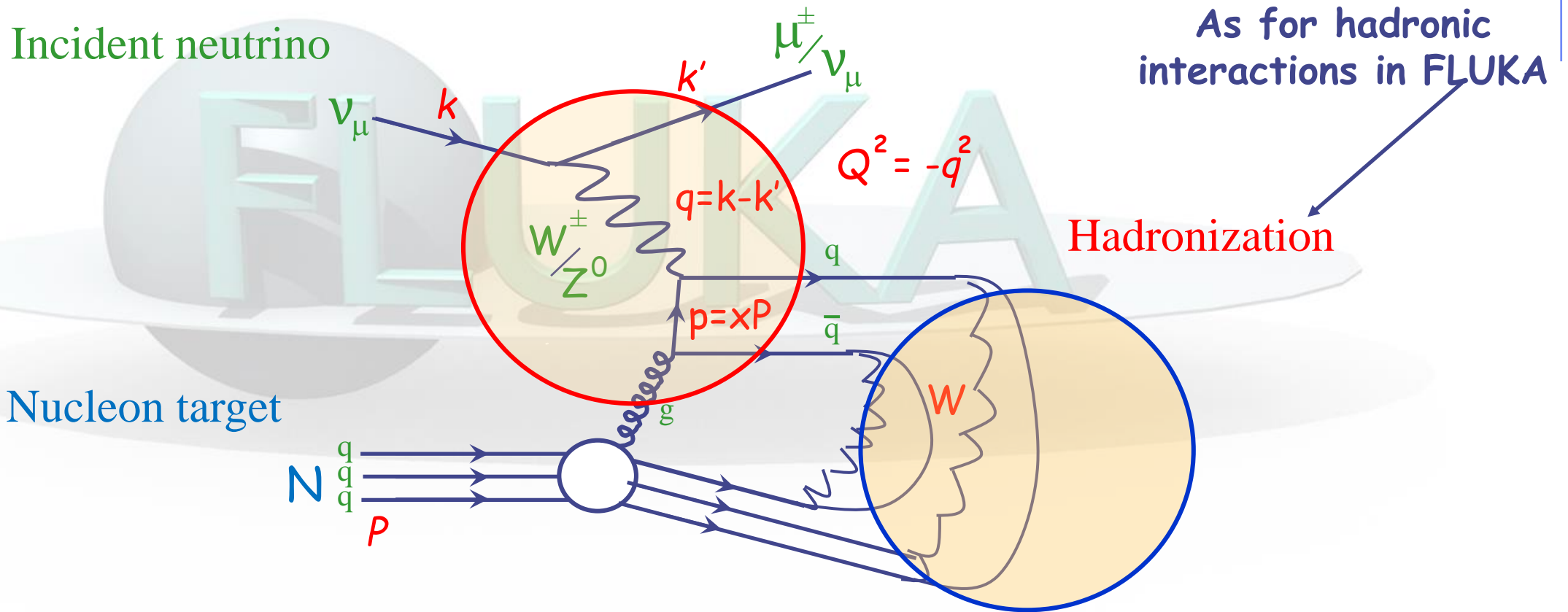
- Following Llewellyn Smith formulation
- $M_A = 1.03$, $M_V = 0.84$
- Lepton masses accounted for

Resonance production

- From Rein-Sehgal formulation
- Keep only Δ production
- No non-resonant background term, assuming that the non-resonant contribution comes from NunDIS
- **TRANSITION** from RES to DIS: linear decrease of both σ as a function of W

DIS (NUNDIS)

FLUKA hadronization and nuclear interactions work well independently of primary interaction vertex



Sample x and Q^2 from double differential cross sections

$$\frac{d^2\sigma}{dx dQ^2} = \frac{d^2\sigma}{dx dy} \cdot \frac{dy}{dQ^2} = \frac{d^2\sigma}{dx dy} \cdot \frac{1}{2ME_\nu x}$$

$$\frac{d^2\sigma}{dx dy} = \frac{G_F^2 M E_\nu}{\pi(1 + Q^2/M_{W/Z}^2)^2} \sum_{i=1}^5 A_i(x, y, E_\nu) F_i(Q^2, x)$$

Structure functions $F_i(Q^2, x)$

$$F_2^{\nu p}(Q^2, x) = 2x[d + \bar{u} + s + \bar{c}]$$

$$xF_3^{\nu p}(Q^2, x) = 2x[d - \bar{u} + s - \bar{c}]$$

Callan-Gross relation: $F_1 = \frac{F_2}{2x}$

To be updated to

$$2xF_1(Q^2, x) = F_2(Q^2, x) \frac{1 + 4M^2 x^2 / Q^2}{1 + R(Q^2, x)}$$

Albright-Jarlskog relations:

$$F_4 = 0,$$

$$F_5 = \frac{F_2}{x}.$$

$$A_1 = y \left(xy + \frac{m_\ell^2}{2ME_\nu} \right)$$

$$A_2 = 1 - y \left(1 + \frac{Mx}{2E_\nu} \right) - \frac{m_\ell^2}{4E_\nu^2}$$

$$A_3 = \pm y \left[x \left(1 - \frac{y}{2} \right) - \frac{m_\ell^2}{4ME_\nu} \right]$$

$$A_4 = \frac{m_\ell^2}{2ME_\nu} \left(y + \frac{m_\ell^2}{2ME_\nu x} \right)$$

$$A_5 = -\frac{m_\ell^2}{ME_\nu}$$

Quark dependence $q_i(Q^2, x)$ determined from Parton Distribution Functions (PDFs)

| | |
|--------------|---|
| GRV94 | Glück et al., Z. Phys. C67 (1995) 433. |
| GRV98 | Glück et al., Eur. Phys. J. C5 (1998) 461. |
| BBS | Bourelly et al., Eur. Phys. J. C23 (2003) 487. |
| CTEQ | J. High Energy Phys. 0207 (2002) 012. |
| MRST | arXiv:hep-ph/0211080. |
| Alekhin | Phys. Rev. D68 (2003) 014002. |
| | ... |

NUNDIS WORKS WITH THESE PDFs

DEFAULT OPTION

In the NLO (DIS) version
M. Glück, E. Reya and A. Vogt, Eur. Phys. J. C5
(1998) 461

Extrapolation from $Q^2 = 1.0 \text{ GeV}^2$ to $Q^2 = 0$

Solid lines: M. Bertini et al. 1996 (Default in NUNDIS)

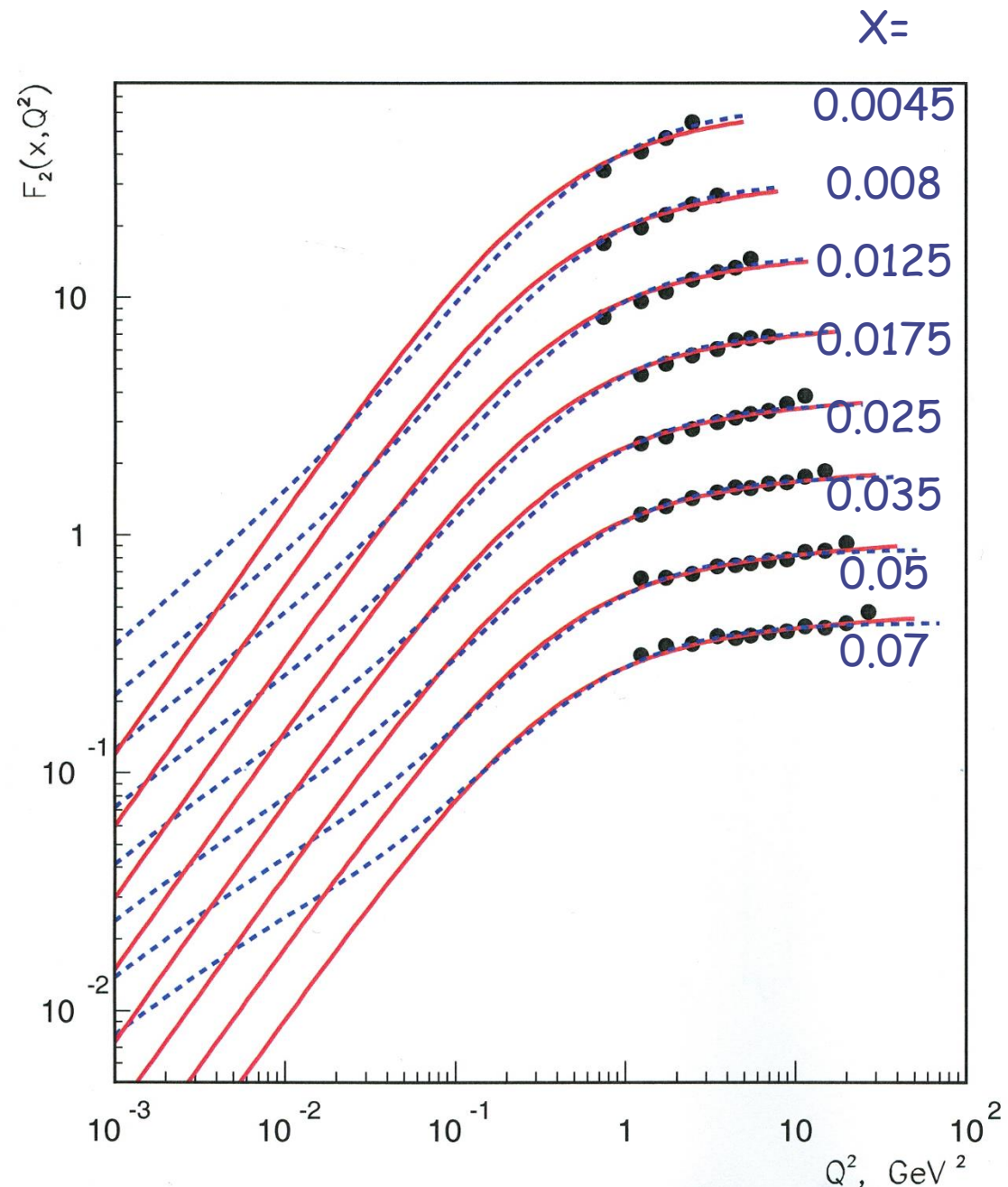
$$F_2(x, Q^2) = A \left[1 + \epsilon \ln(Q^2(1/x - 1) + M^2) \right] \ln(1 + Q^2/(Q^2 + a^2)) .$$

Dashed lines: Donnachie-Landshoff 1994

$$F_2(x, Q^2) \sim Ax^{-0.0808} \left(\frac{Q^2}{Q^2 + a} \right)^{1.0808} + Bx^{0.4525} \left(\frac{Q^2}{Q^2 + b} \right)^{0.5475}$$

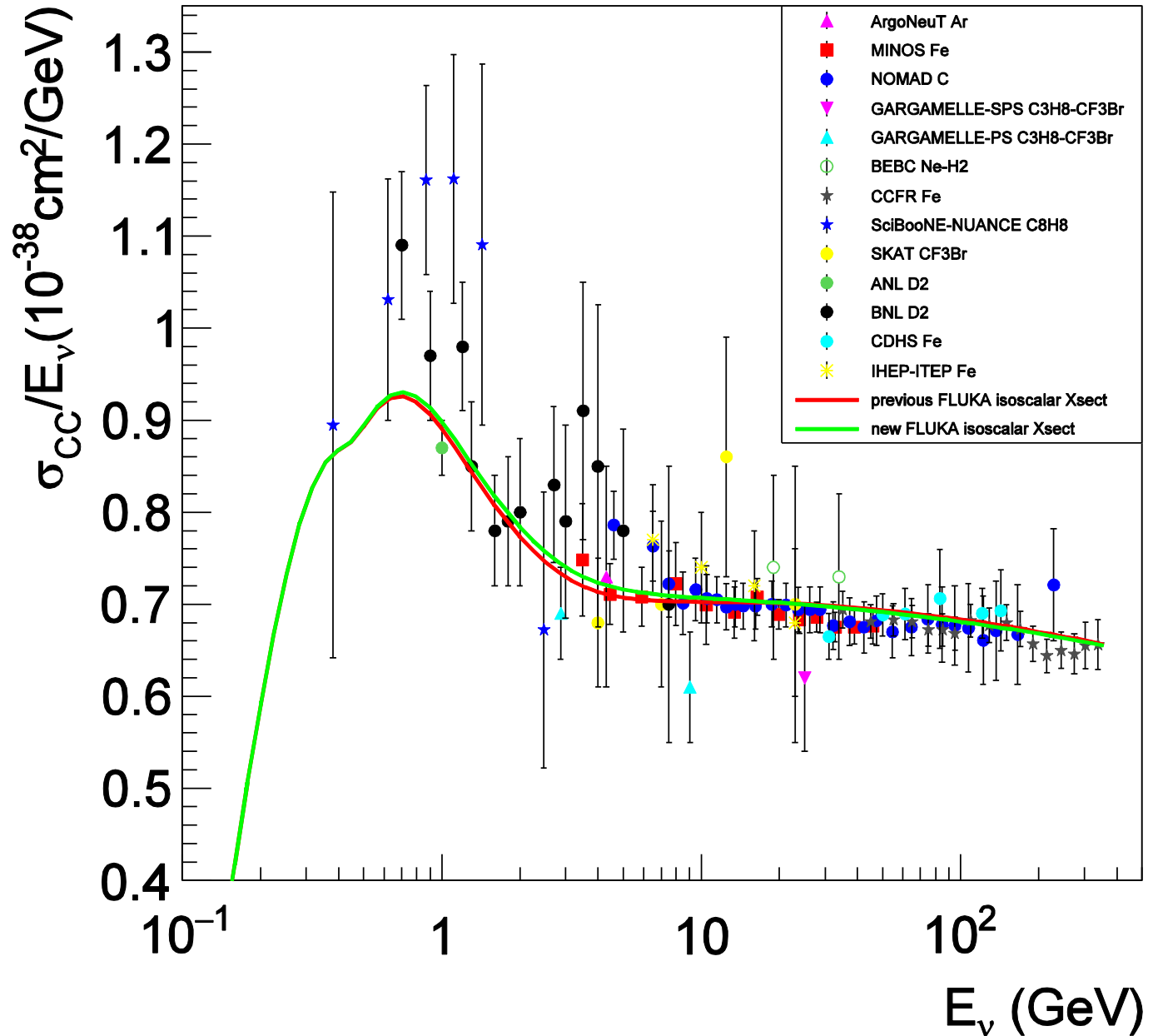
data points from NMC Collab., M. Arneodo et al., Nucl. Phys. B 483 (1997) 3-43

Data/cuves scaled for clarity, factors from 1 to 128



Comparison with data on total cross section

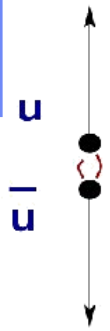
Isoscalar
 ν_μ - Nucleon total
CC cross section
Fluka (lines) with
two pdf options
Vs
Experimental data



The "hadronization" of chains

An example:

Low mass chain: just 2-3 meson/(anti)baryon resonances



- $u\bar{d}$
- $d\bar{u}$
- $\bar{u}u\bar{d}$
- udd
- $u\bar{s}$
- $s\bar{d}$
- $u\bar{d}$
- $q\bar{q}$
- $q\bar{q}$
- $---$
- $...$
- $d\bar{u}$

See LUND talk this morning.
Concepts are the same
Implementation FLUKA-native
(evolution of old BAMJET)

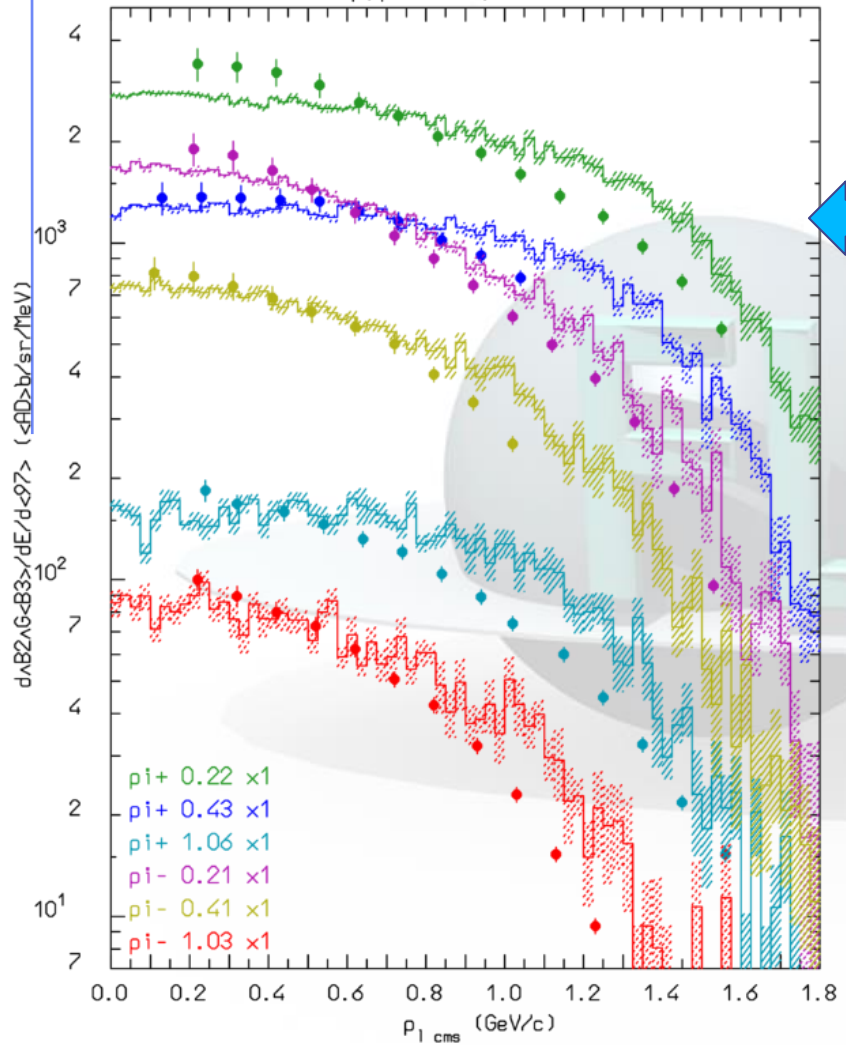
In FLUKA:

- Assumes chain universality
- Fragmentation functions from hard processes and $e+e-$ scattering
- Transverse momentum from uncertainty considerations
- Mass effects at low energies (change fragmentation function to account for the need to create real hadrons)
- Chains generated at very low energy \rightarrow create single/few resonances
- Chains generated at low energy \rightarrow "phase space explosion" constrained in p_T , including baryons, mesons, resonances.

The same functions and parameters for all reactions and energies

- Chains from ν DIS :
 - One quark-diquark chain if interaction on valence quark
 - One quark-diquark plus one q - $qbar$ chain if int on sea quark

Effect of "low energy explosion"

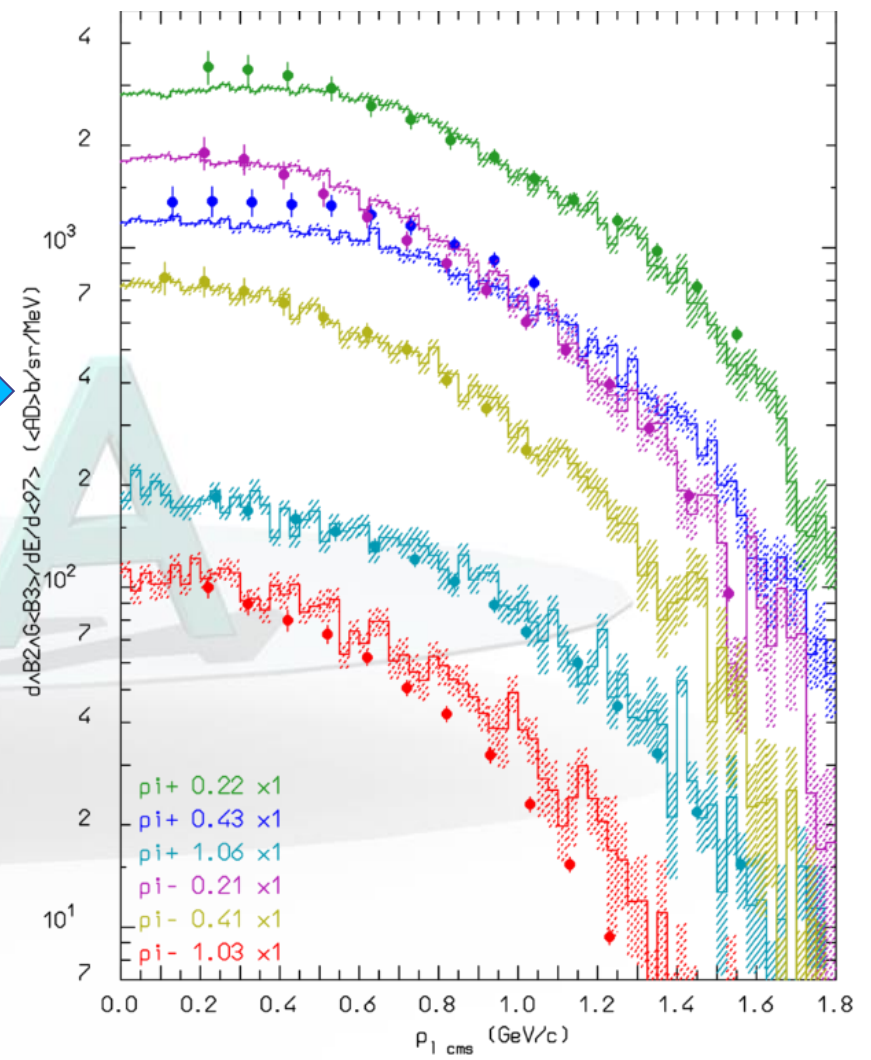


Fluka: histos
Data: symbols

← "standard" hadronization

With low-mass chain explosion →

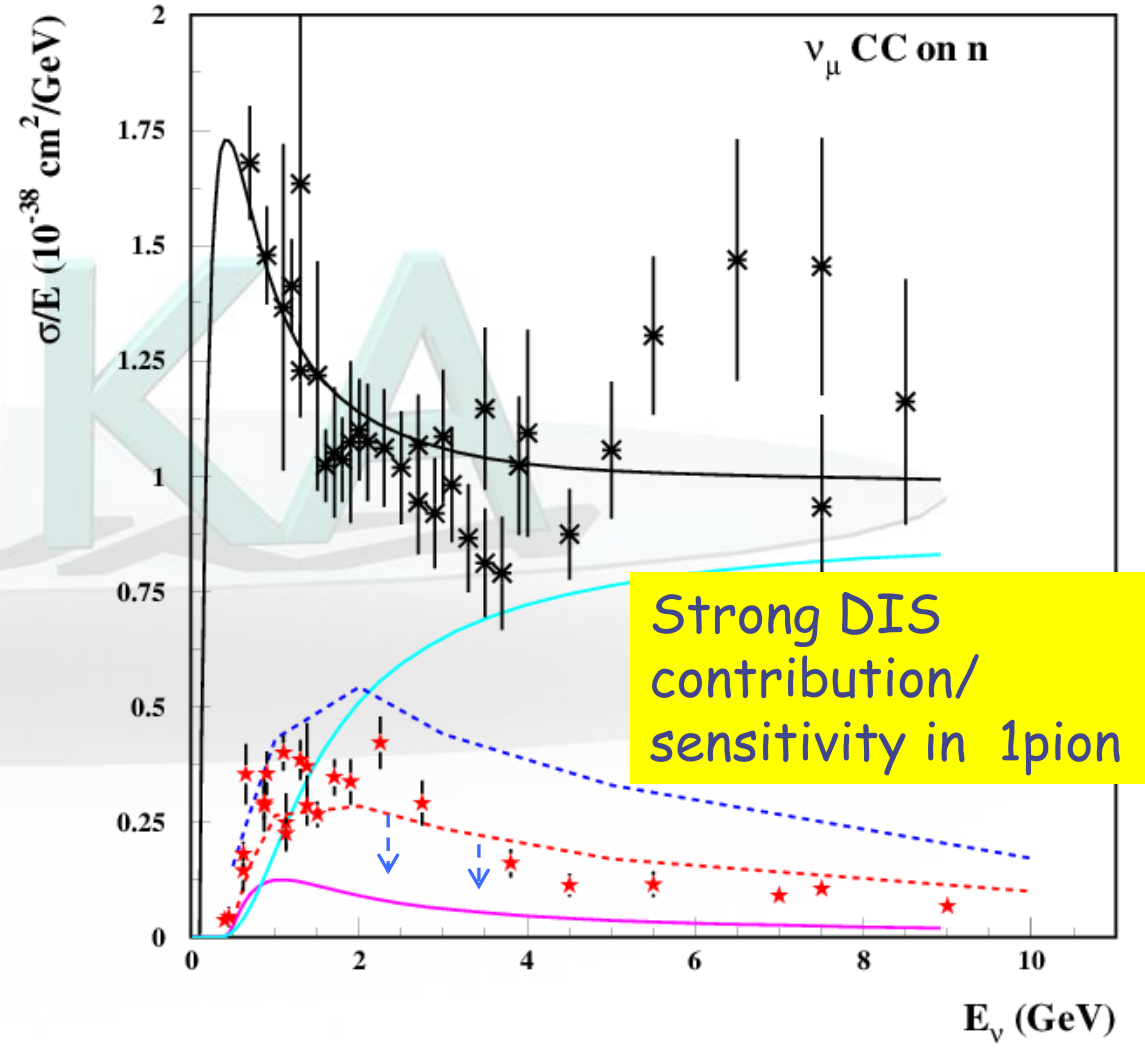
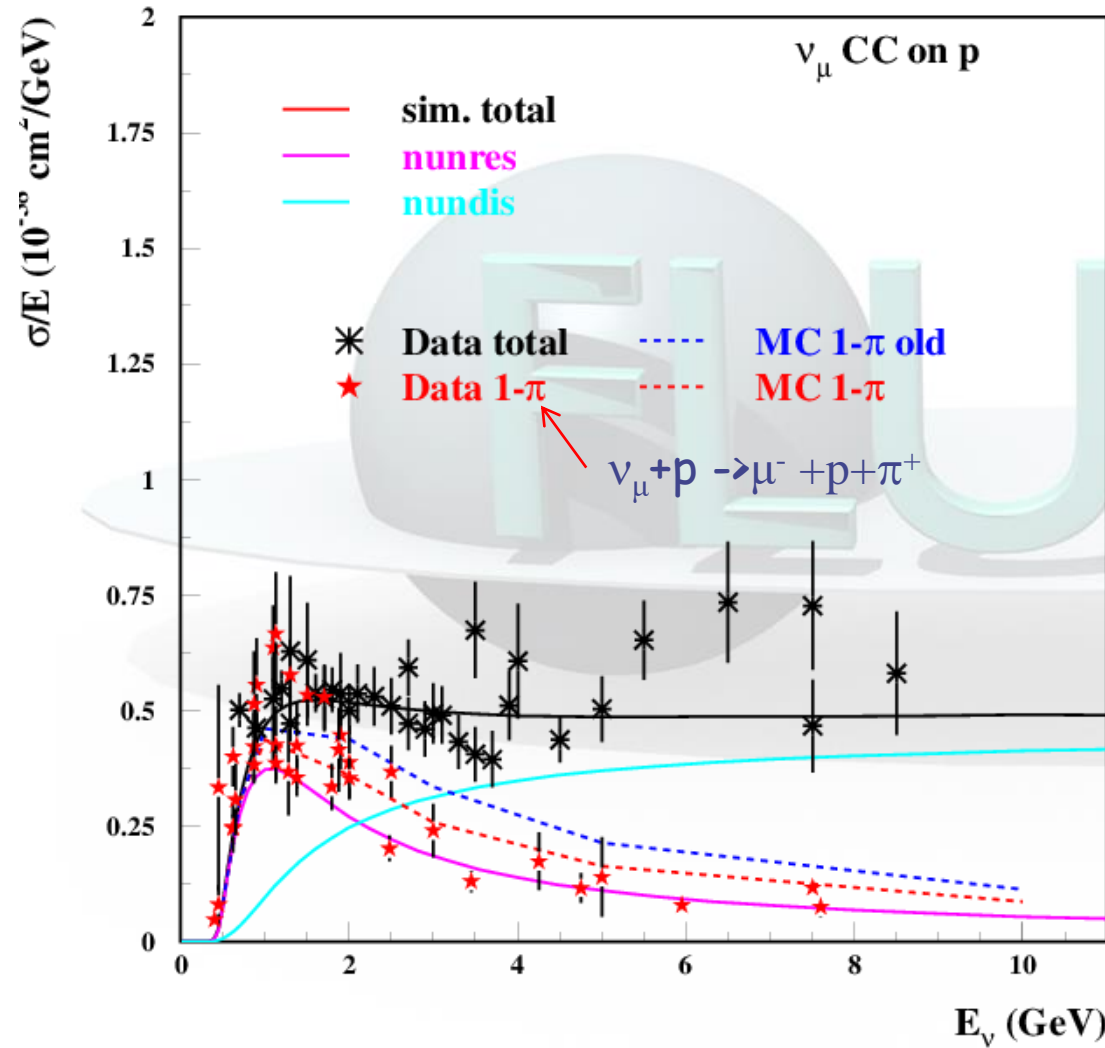
With low-mass chain explosion: much better agreement for forward emission



Pion+ and Pion- emission from proton-proton interactions at 12.6 GeV. Longitudinal momentum distributions at different transverse momenta

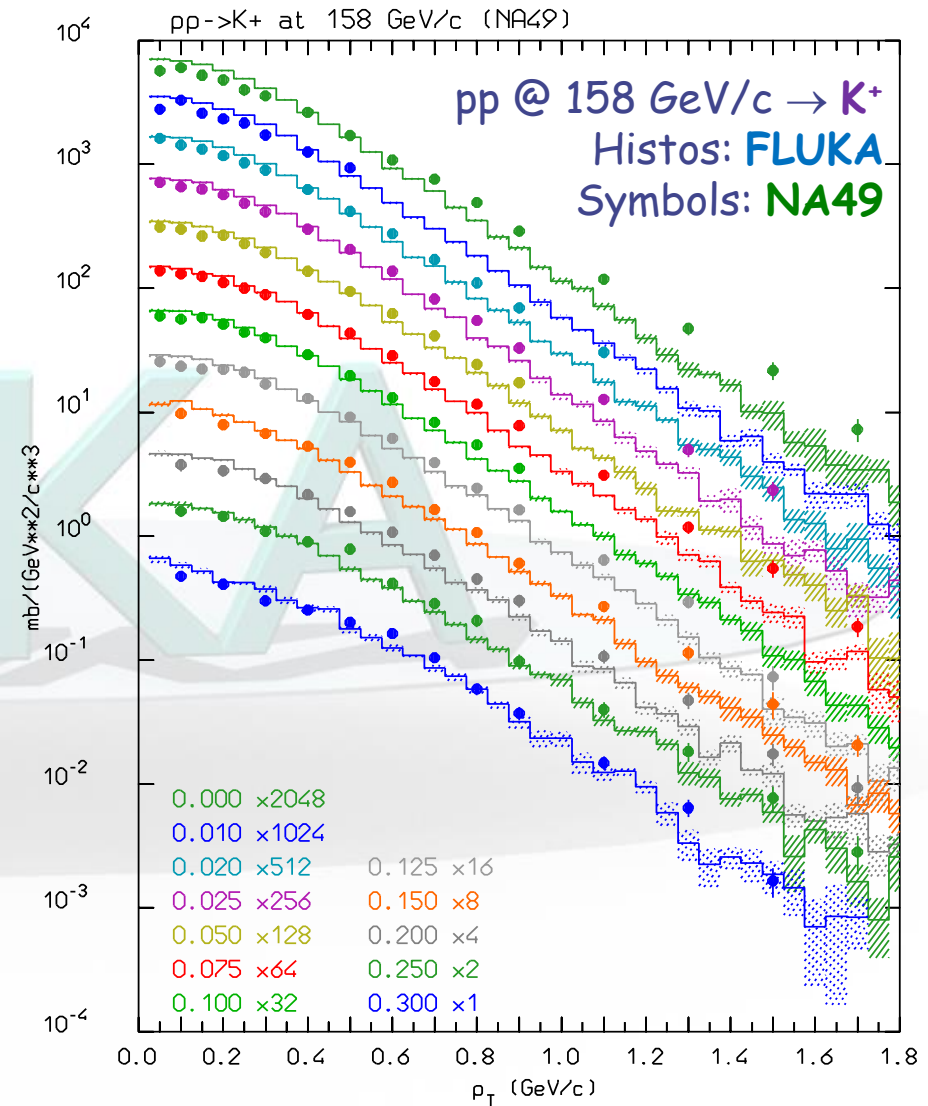
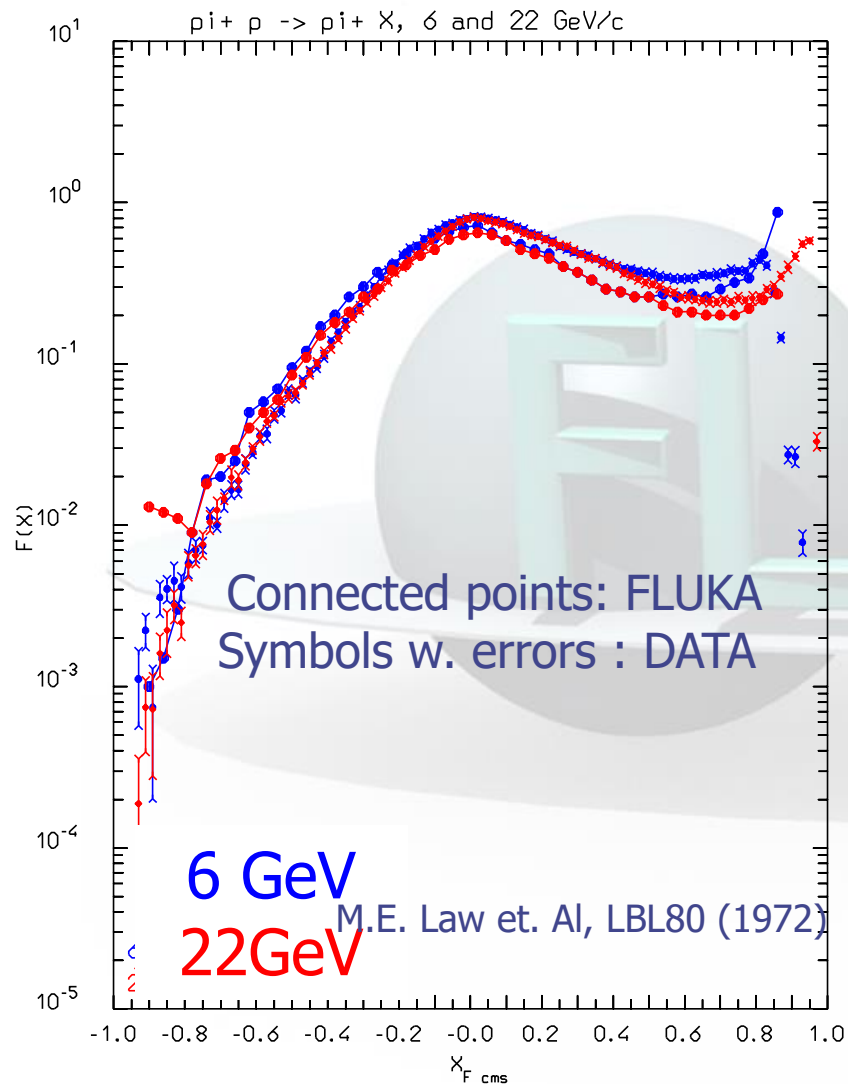
Single pion production

New *low-mass chain treatment of fragmentation* → improvements in the **RES-DIS** transition



Hadronization in hadron-nucleon: examples

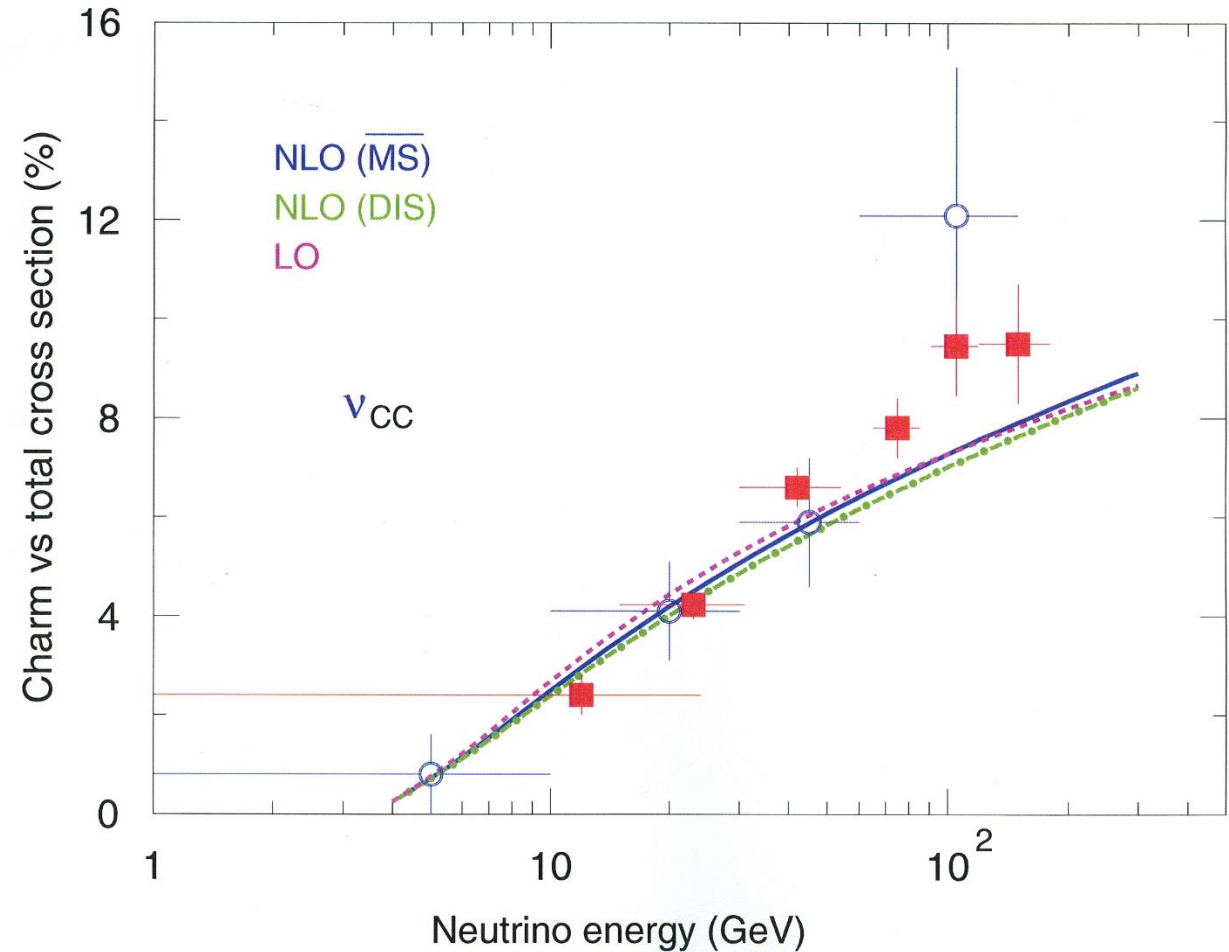
$\pi^+ + p \rightarrow \pi^+ + X$ (6 & 22 GeV/c)



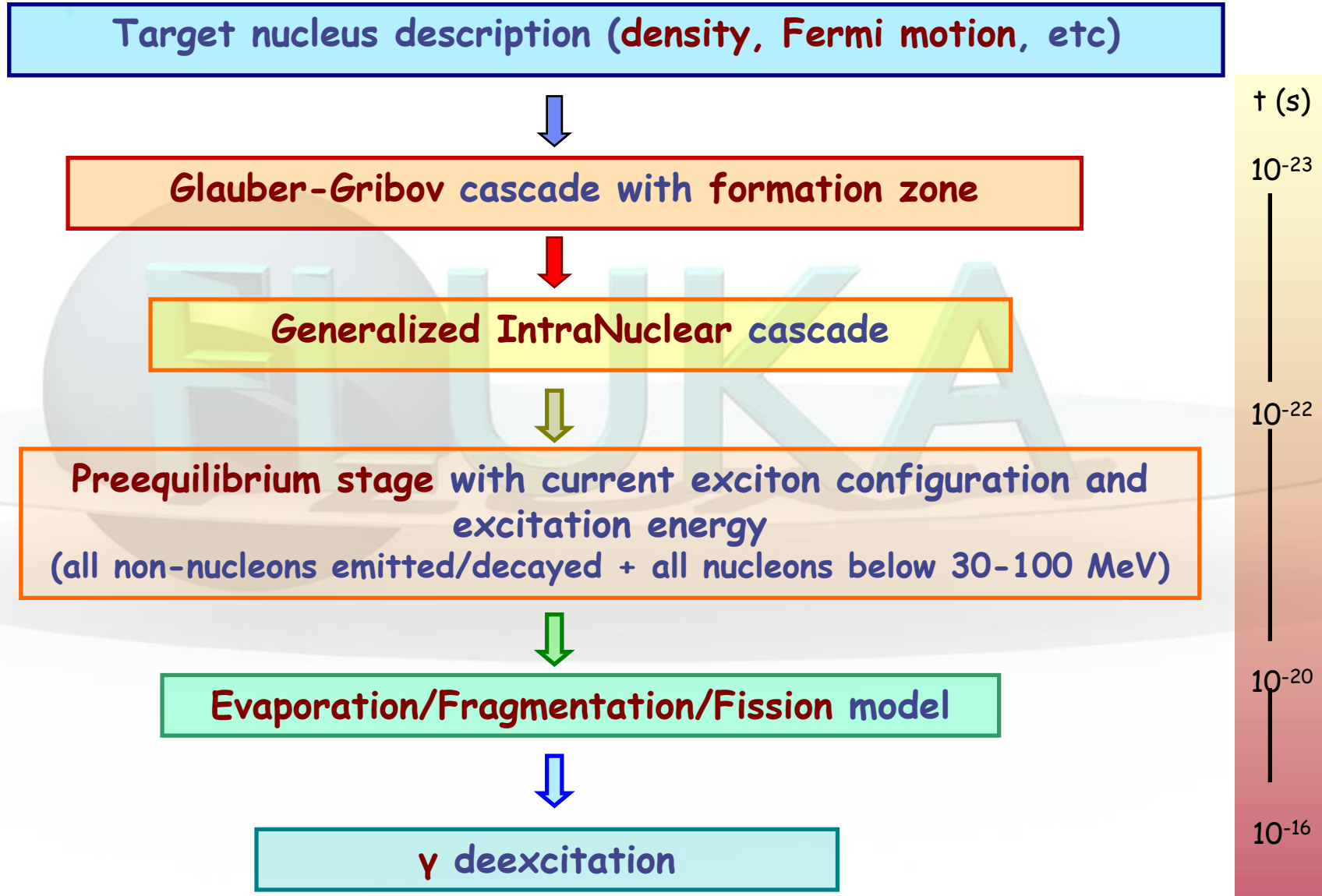
K⁺ yield as a function of p_T for different X_F bins, 158 GeV/c protons

Charm production in neutrino interactions

- Ratio of the charm to total cross sections
- Results of NUNDIS simulation with $M_c = 1.35$ GeV (curves) and experimental data: E531 (open circles) and CHORUS-2011 (filled squares).



Nuclear interactions in FLUKA: the PEANUT model



(Generalized) IntraNuclear Cascade

- Primary and secondary particles moving in the nuclear medium
- Target nucleons motion and nuclear potential well according to **local Fermi gas model**
- Interaction probability
 $\sigma_{free} + \text{Fermi motion} \times \rho(r) + \text{exceptions (ex. } \pi)$ σ_{free} includes inelastic
- Glauber cascade at higher energies ****not for neutrinos*****
- Classical trajectories (+) nuclear mean potential (**resonant for π**)
- Curvature from nuclear potential → **refraction and reflection**
- Interactions are incoherent and uncorrelated
- Interactions in projectile-target nucleon CMS
- Fully relativistic
- **Multibody absorption for π, μ^-**
- **Special for K^- , antinucleon, π** (phase shifts, annihilation)
- **Quantum effects** (Pauli, formation zone, correlations...)
- **Exact conservation** of energy, momenta and all additive quantum numbers, including nuclear recoil
- First **excited nuclear levels** accounted for (more levels in evaporation/gamma deexc)

Nucleon Fermi Motion in FLUKA

- Fermi gas model: Nucleons = Non-interacting Constrained Fermions

Momentum distribution

$$\propto \frac{dN}{dk} = \frac{|k|^2}{2\pi^2}$$

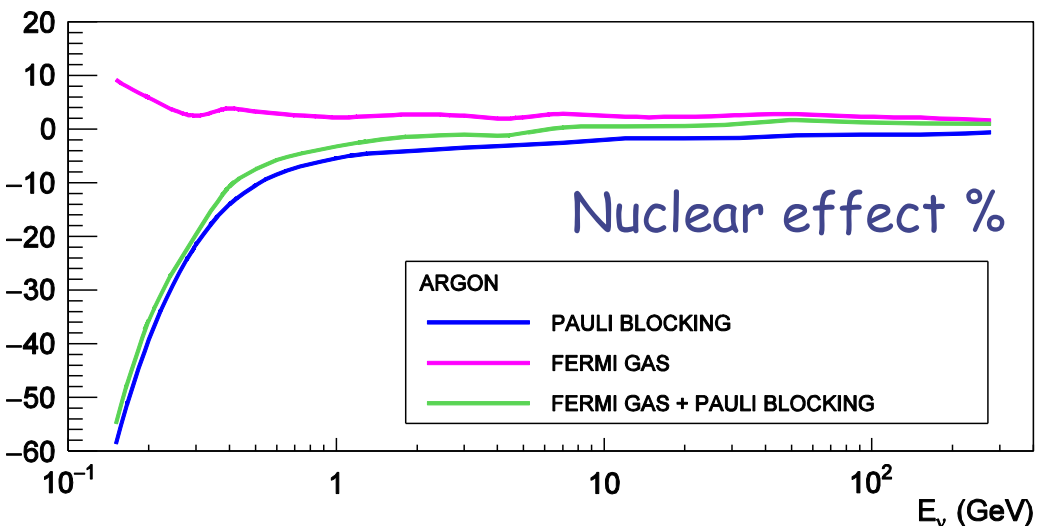
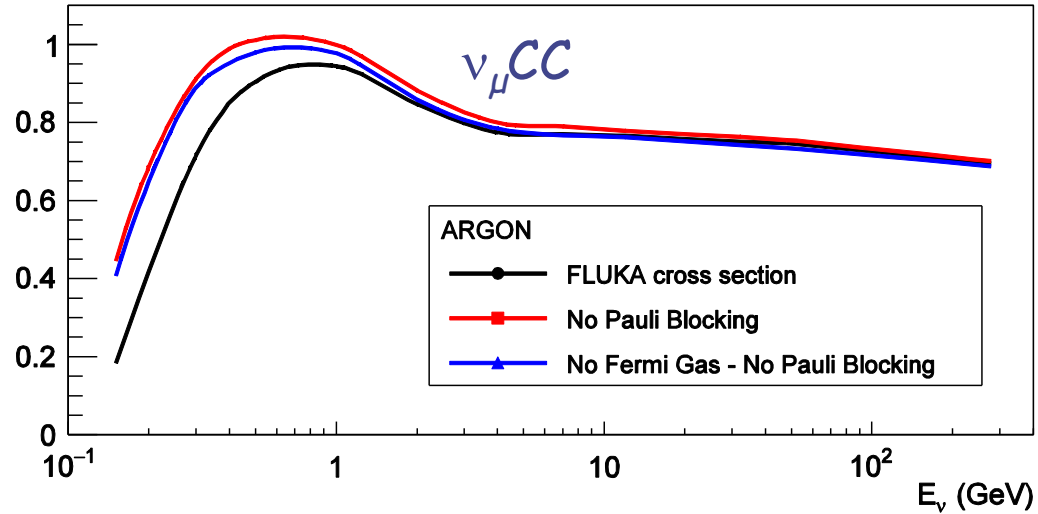
for k up to a **local** Fermi momentum $k_F(r)$ given by

$$k_F(r) = \left[3\pi^2 \rho_N(r) \right]^{\frac{1}{3}}$$

- **Momentum smearing** according to uncertainty principle assuming a position uncertainty = $\sqrt{2}$ fm
- Nuclear density given by symmetrized Woods-Saxon for $A > 16$ and by a harmonic oscillator shell model for light isotopes
- Proton and neutron densities are different
- Nucleons are **bound** in the nucleus

Total cross section: nuclear effects in Ar

$\sigma / E 10^{-38} \text{ cm}^2 / N$



$5 \text{ GeV} < E_\nu < 50 \text{ GeV}$
 Pauli Blocking effect
 and Fermi Gas effect
 separately have an
 impact of $\sim 2\text{-}3\%$
 Globally Nuclear
 effects stay within
 $\pm 1\%$

$E_\nu < 5 \text{ GeV}$

nuclear effects are
 dominated by the
 Pauli Blocking and
 rapidly increase to
 the order of 10% and
 above

Nuclear effects in Minerva

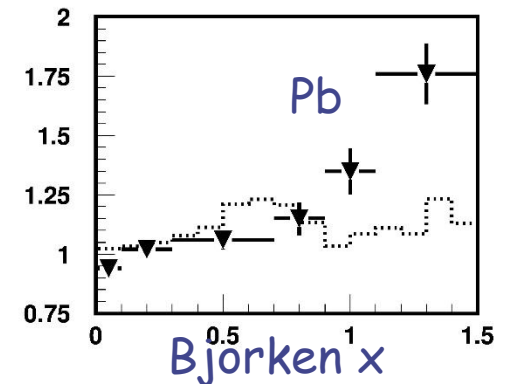
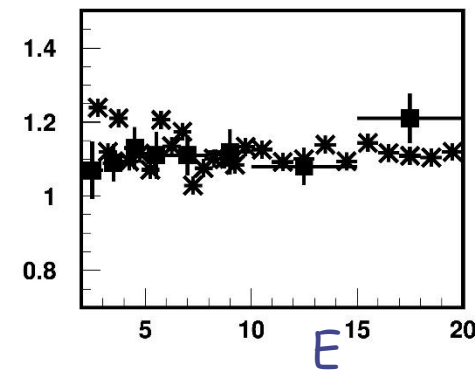
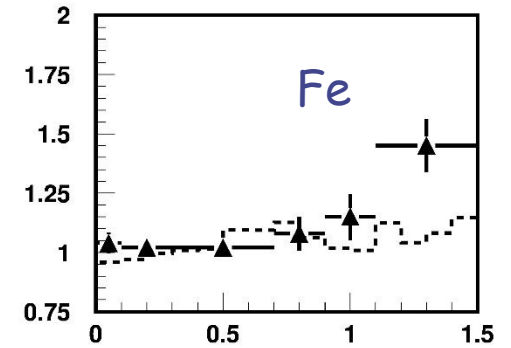
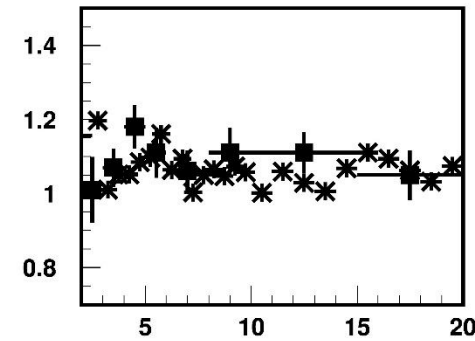
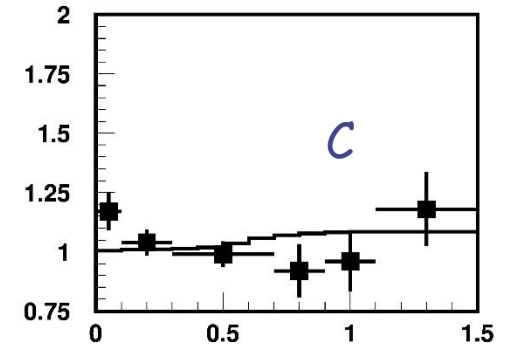
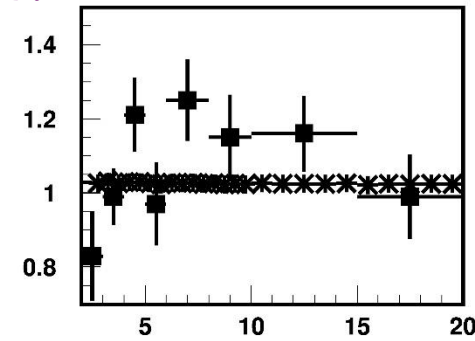
Beam: $\nu\mu$ NuMi Low Energy (average 4 GeV)
Main Target : CH

Measured also with C, Fe, Pb targets
PRL 112, 231801 (2014)

Here: ratio of cross sections / the one in CH

Left: total CC vs neutrino Energy :
squares: data
crosses: FLUKA

Right: $d\sigma/dx$
symbols: data histos: Fluka
expt: reduction at low x and
enhancement at high x with incr. A
Fluka: fails the highest x (same for
Genie)



Pions: nuclear medium effects

Free π N interactions \Rightarrow \Rightarrow Non resonant channel
 \Rightarrow P-wave resonant Δ production

Δ in nuclear medium \Rightarrow decay \Rightarrow elastic scattering, charge exchange
 \Rightarrow reinteraction \Rightarrow Multibody pion absorption

Assuming for the free resonant σ a Breit-Wigner form with width Γ_F

$$\sigma_{res}^{Free} = \frac{8\pi}{p_{cms}^2} \frac{M_\Delta^2 \Gamma_F^2(p_{cms})}{(s - M_\Delta^2)^2 + M_\Delta^2 \Gamma_F^2(p_{cms})}$$

An "in medium" resonant σ (σ_{res}^A) can be obtained adding to Γ_F the imaginary part of the (extra) width arising from nuclear medium

$$\frac{1}{2}\Gamma_T = \frac{1}{2}\Gamma_F - \text{Im}\Sigma_\Delta \quad \Sigma_\Delta = \Sigma_{qe} + \Sigma_2 + \Sigma_3 \quad (\text{Oset et al., NPA 468, 631})$$

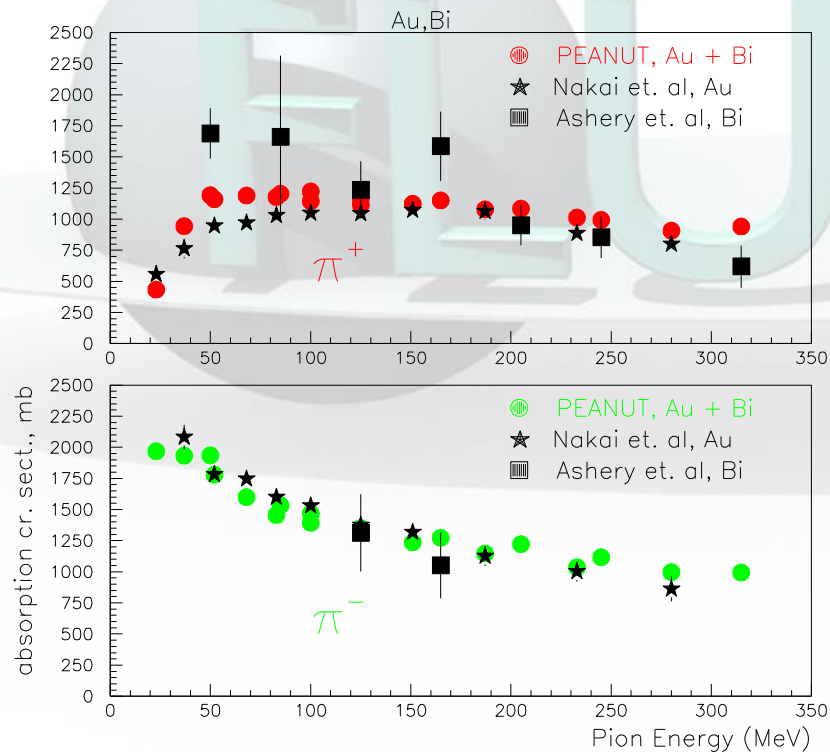
quasielastic scattering, two and three body absorption

The in-nucleus σ_t^A takes also into account a two-body s-wave absorption σ_s^A derived from the optical model

$$\sigma_t^A = \sigma_{res}^A + \sigma_t^{Free} - \sigma_{res}^{Free} + \sigma_s^A \quad \sigma_s^A(\omega) = \frac{4\pi}{p} \left(1 + \frac{\omega}{2m}\right) \text{Im} B_0(\omega) \rho$$

Pion absorption examples

Pion absorption cross section on Gold and Bismuth in the Δ resonance region (multibody absorption in PEANUT)

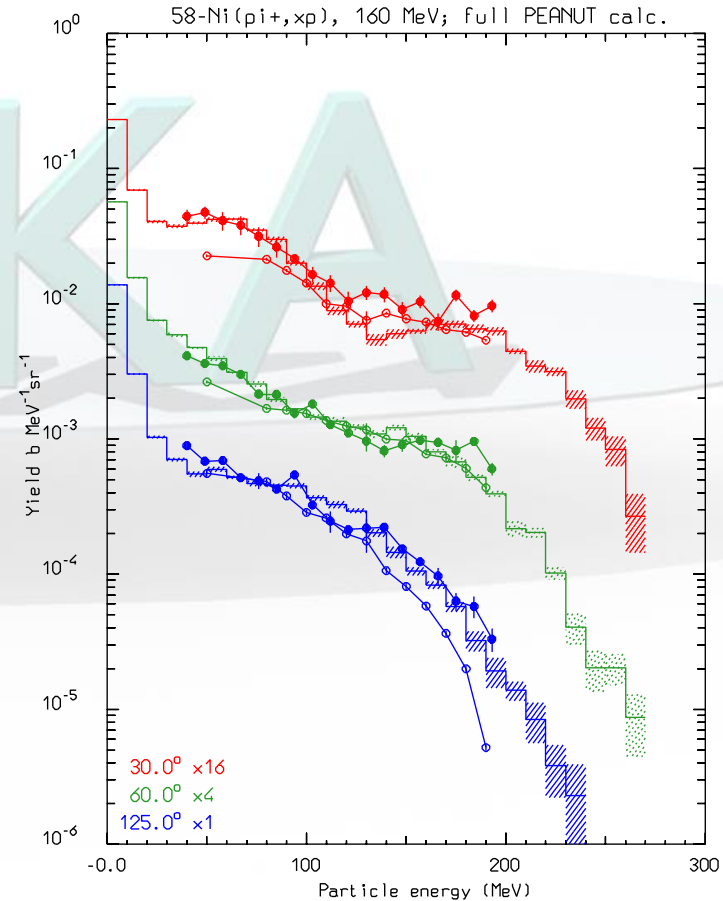


Emitted proton spectra at different angles, 160 MeV π^+ on ^{58}Ni

Phys. Rev. C41,2215 (1990)

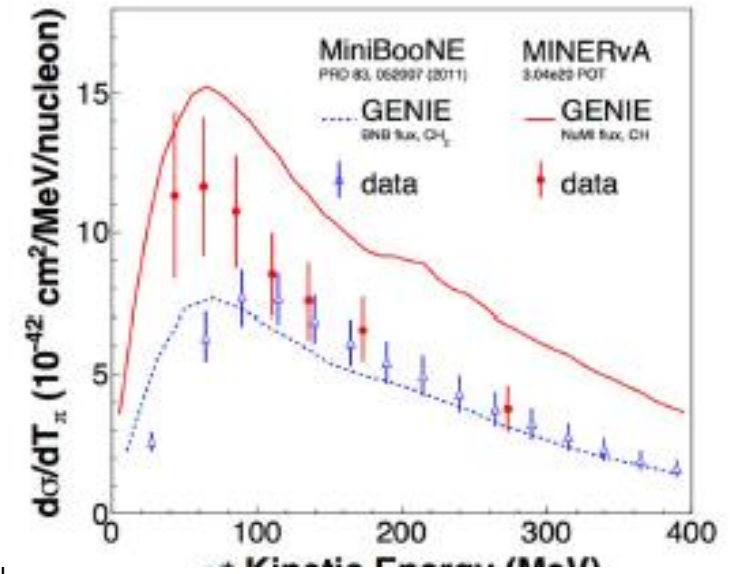
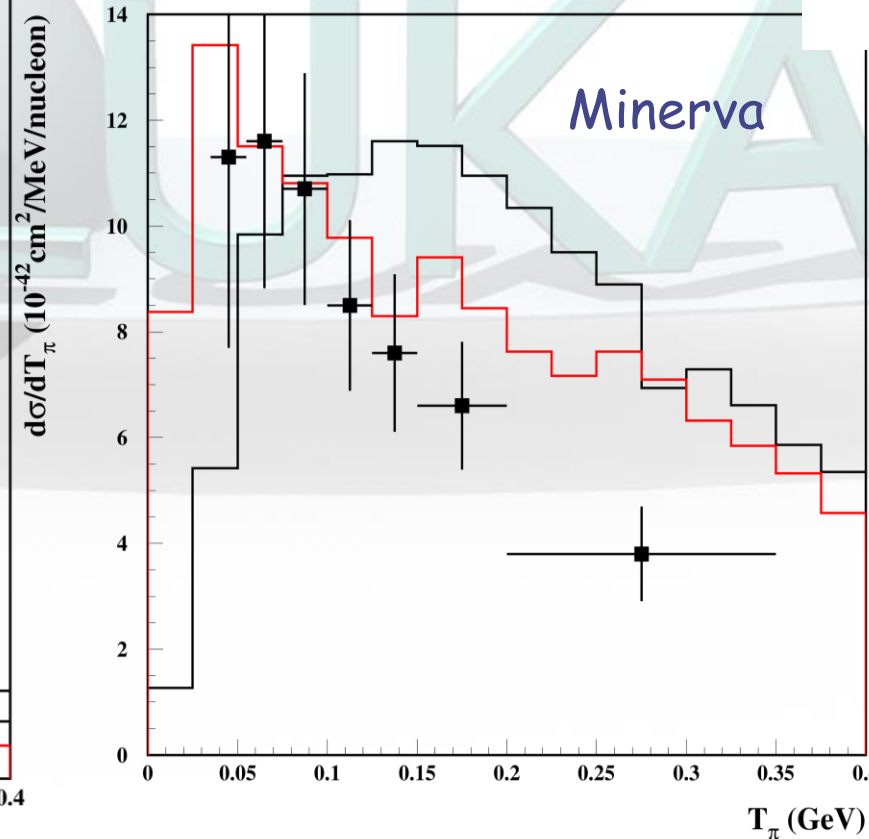
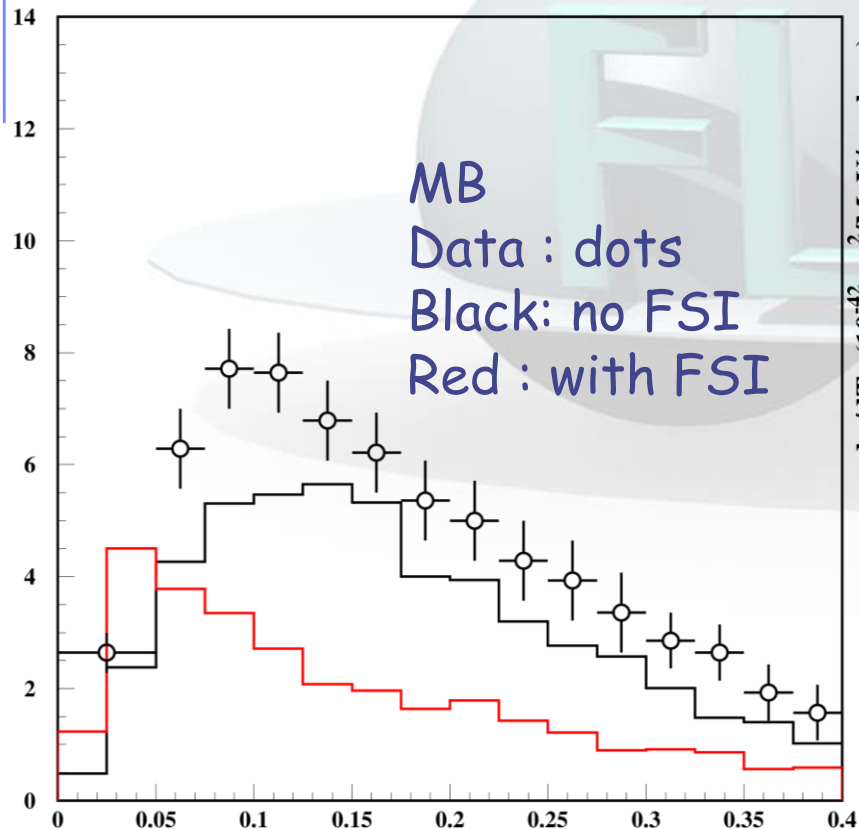
Phys. Rev. C24,211 (1981)

Proton spectra extend up to 300 MeV



Pions in MB and Minerva

Dytman
NUINT14
Genie+FSI



MiniBoone : CH_2 , $E_\nu \approx 0.8$ GeV, cut on single pion, PHYS. REV.D 83, 052007 (2011)

Minerva : CH, $E_\nu \approx 4$ GeV, cut on $W < 1.4$ arXiv:1406.6415v3 (2015)

Tension betw the two data sets vs models/ extent of FSI

another FSI : Formation zone

Naively: "materialization" time (originally proposed by Stodolski).

Qualitative estimate:

In the frame where $p_{||} = 0$

$$\bar{t} = \Delta t \approx \frac{\hbar}{E_T} = \frac{\hbar}{\sqrt{p_T^2 + M^2}}$$

Particle proper time

$$\tau = \frac{M}{E_T} \bar{t} = \frac{\hbar M}{p_T^2 + M^2}$$

Going to the nucleus system

$$\Delta x_{for} \equiv \beta c \cdot t_{lab} \approx \frac{p_{lab}}{E_T} \bar{t} \approx \frac{p_{lab}}{M} \tau = k_{for} \frac{\hbar p_{lab}}{p_T^2 + M^2}$$

Condition for possible reinteraction inside a nucleus: $\Delta x_{for} \leq R_A \approx r_0 A^{\frac{1}{3}}$

Decrease of the reinteraction probability

Applied also to DIS neutrino interactions and, in an analogue way, to QE neutrino interactions

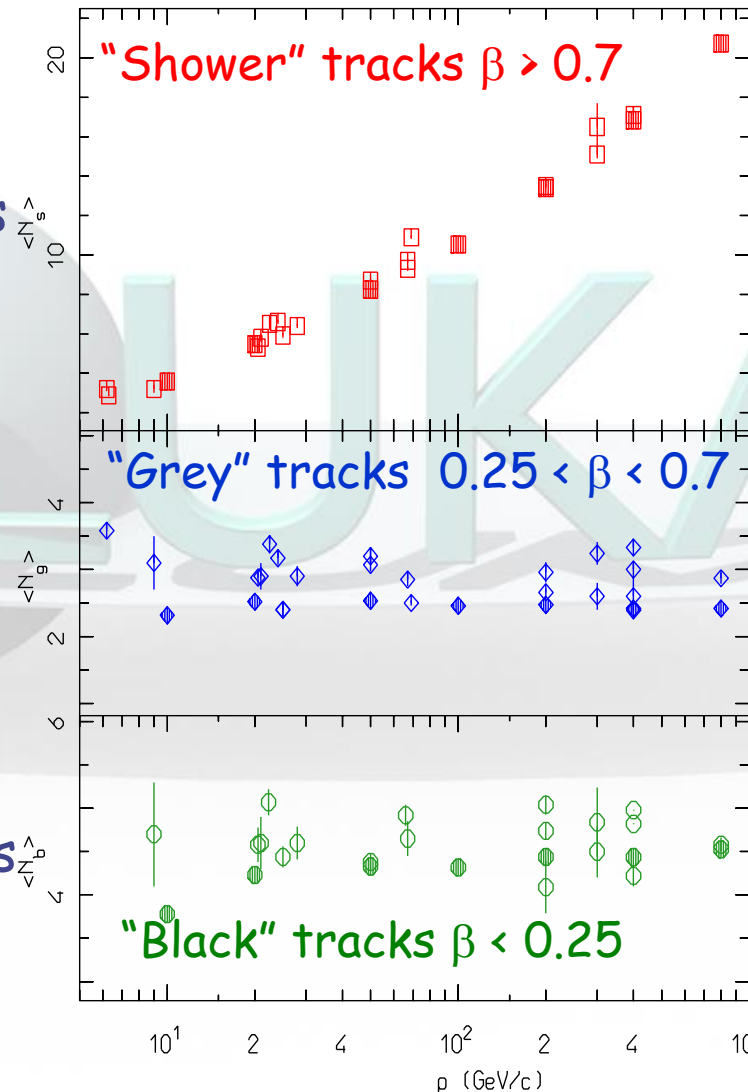
Particle production: multiplicities

Or: why do you use this funny formation zone?

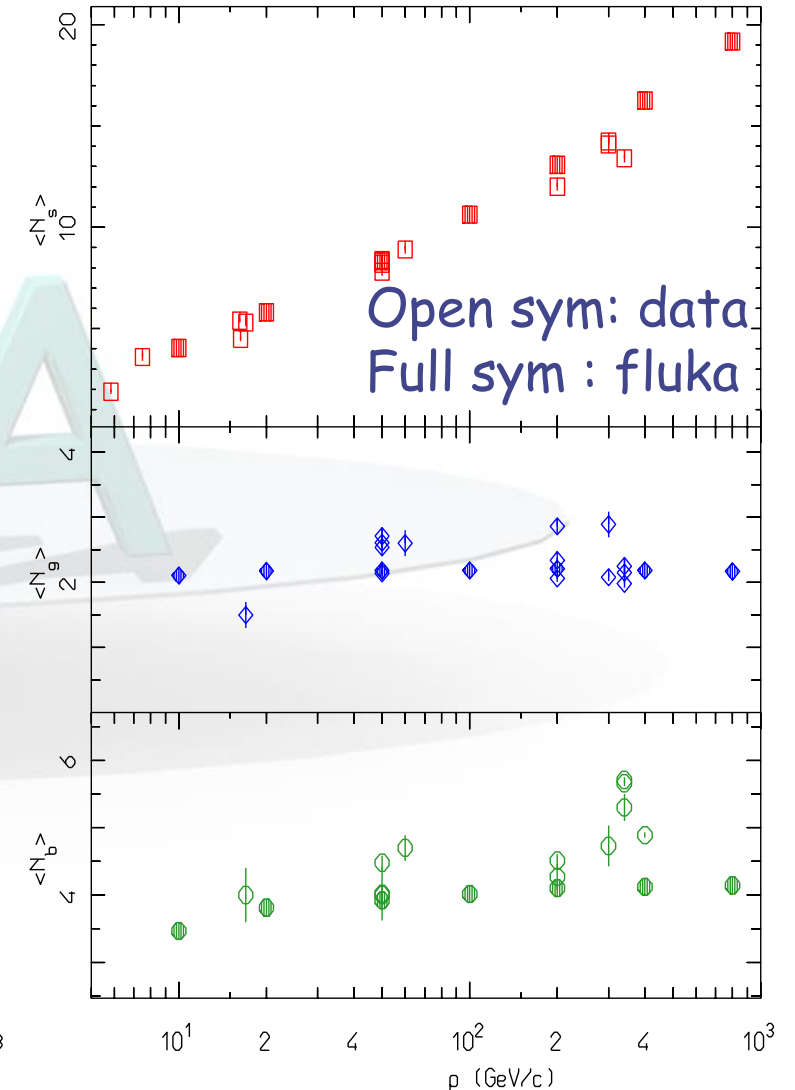
- shower particle multiplicities increase steadily with projectile energy
- multiplicities of grey and black tracks rapidly saturate at few tens of GeV, and stay constant
- Looks like fast particles are free to escape without inducing cascades
- Note that p-p cross section is rather flat vs energy
- → need mechanism

Data:
Phys. Rev. D42, 2187 (1990).
Phys. Rep.144, 187 (1987).

Protons on emulsion



Pion- on emulsion



Part. Prod. Versus projectile momentum.

Effect/Results on hadron-induced reactions

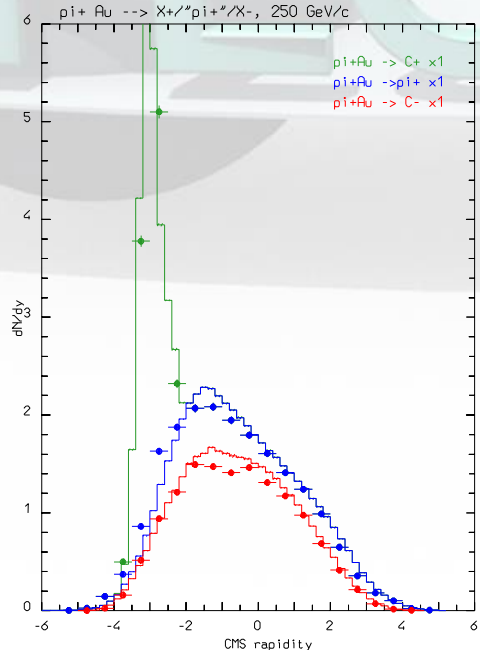
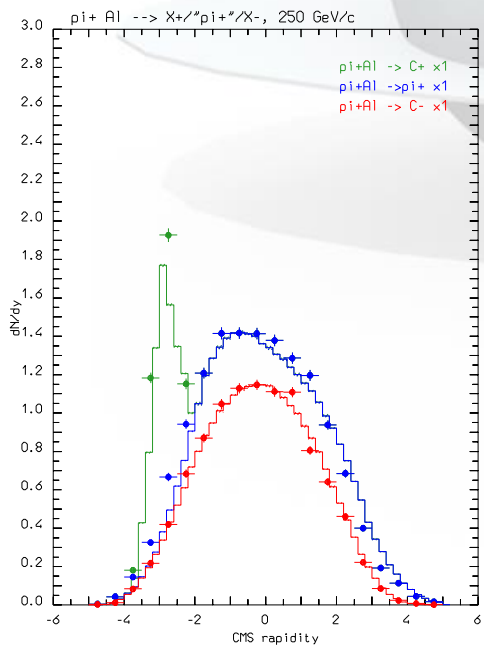
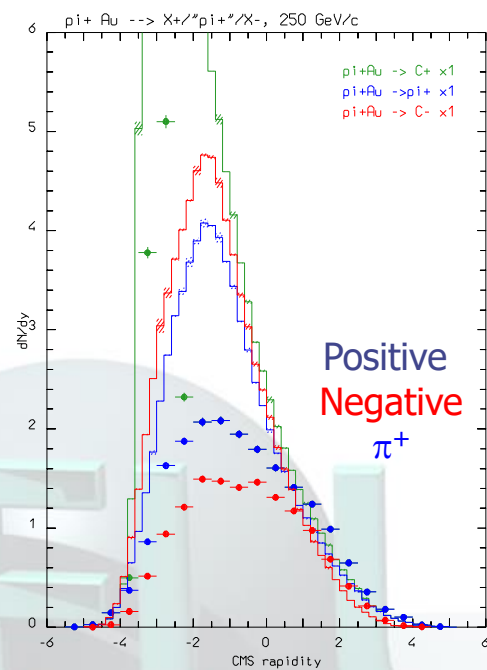
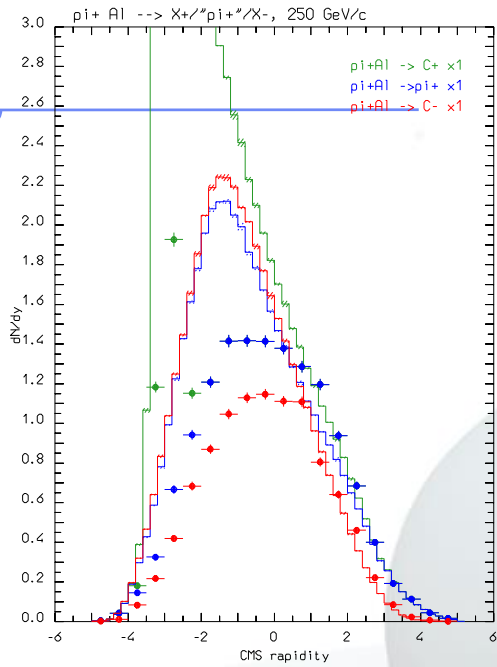
Rapidity distribution of charged particles produced in 250 GeV π^+ collisions on

Aluminum (left) and Gold (right)

Points: exp. data (Agababyan et al., ZPC50, 361 (1991)).

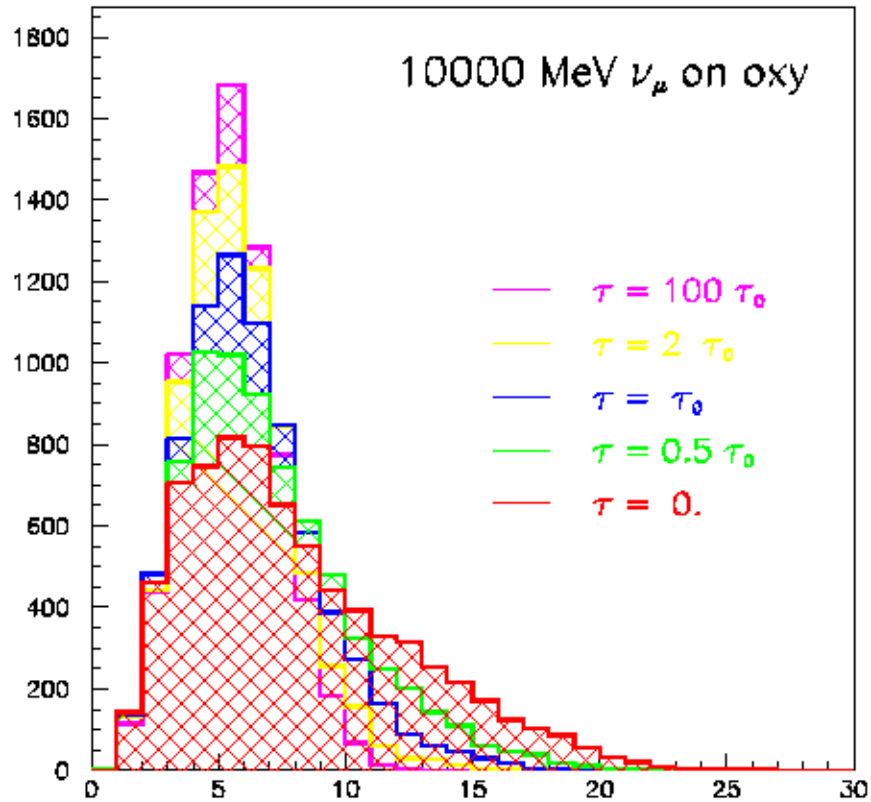
Top: without formation zone

Bottom: with formation zone

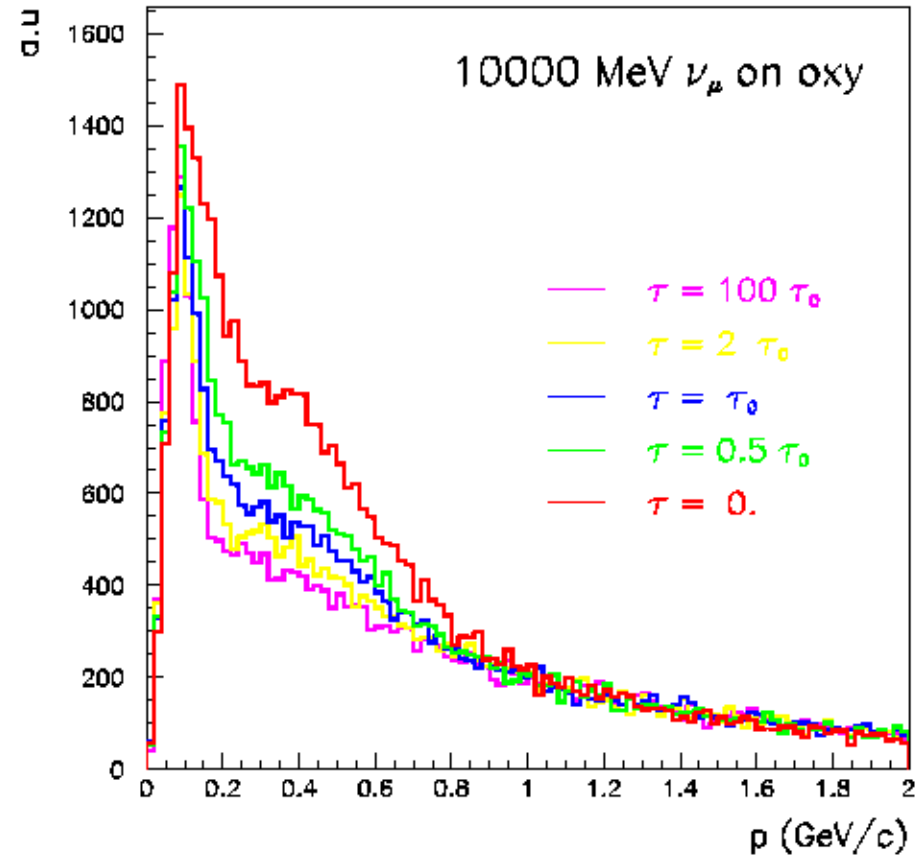


Effect of formation zone, neutrino int.

Total hadron multiplicity

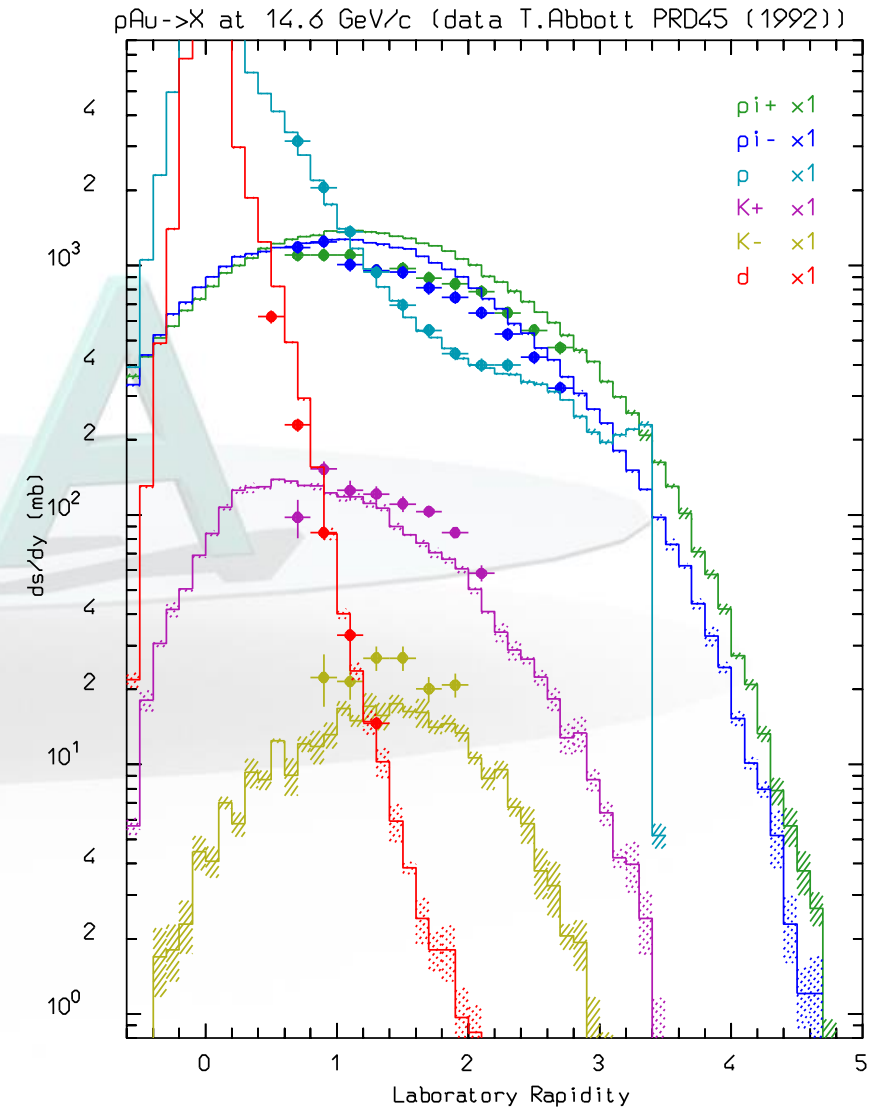
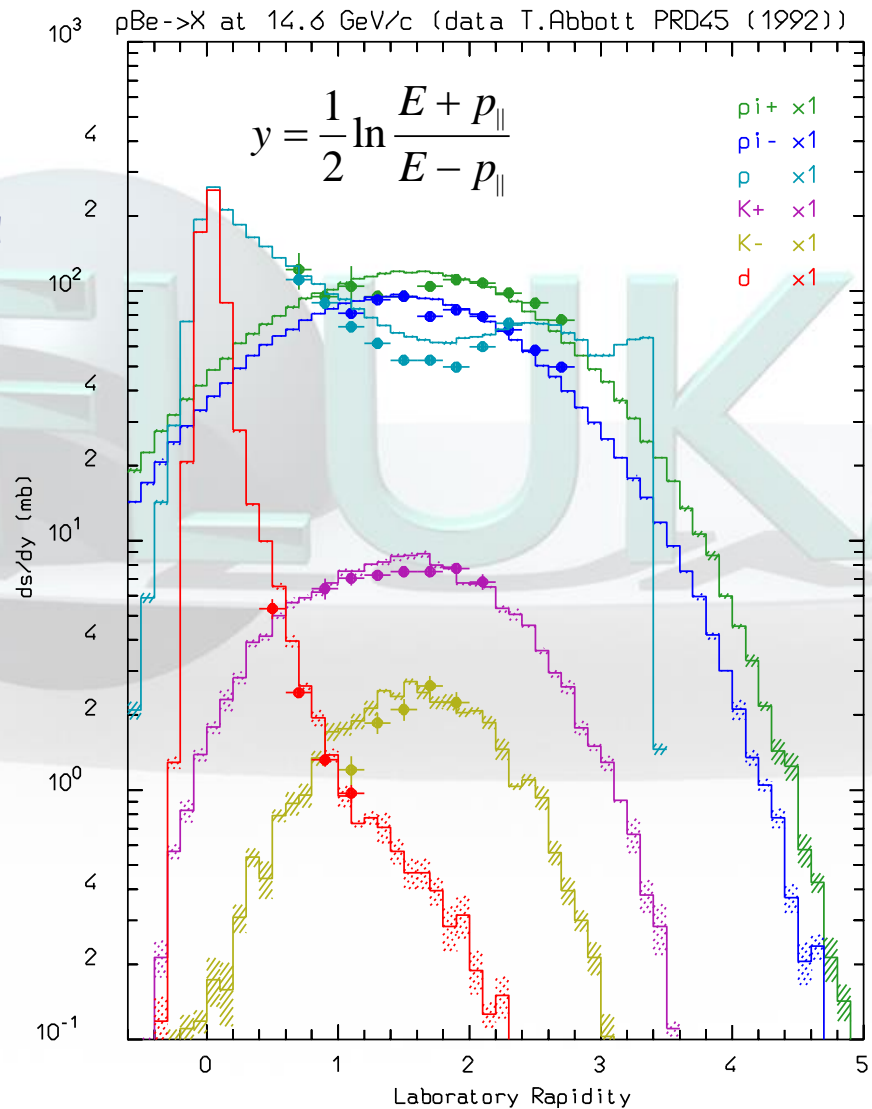


Charged hadron spectra

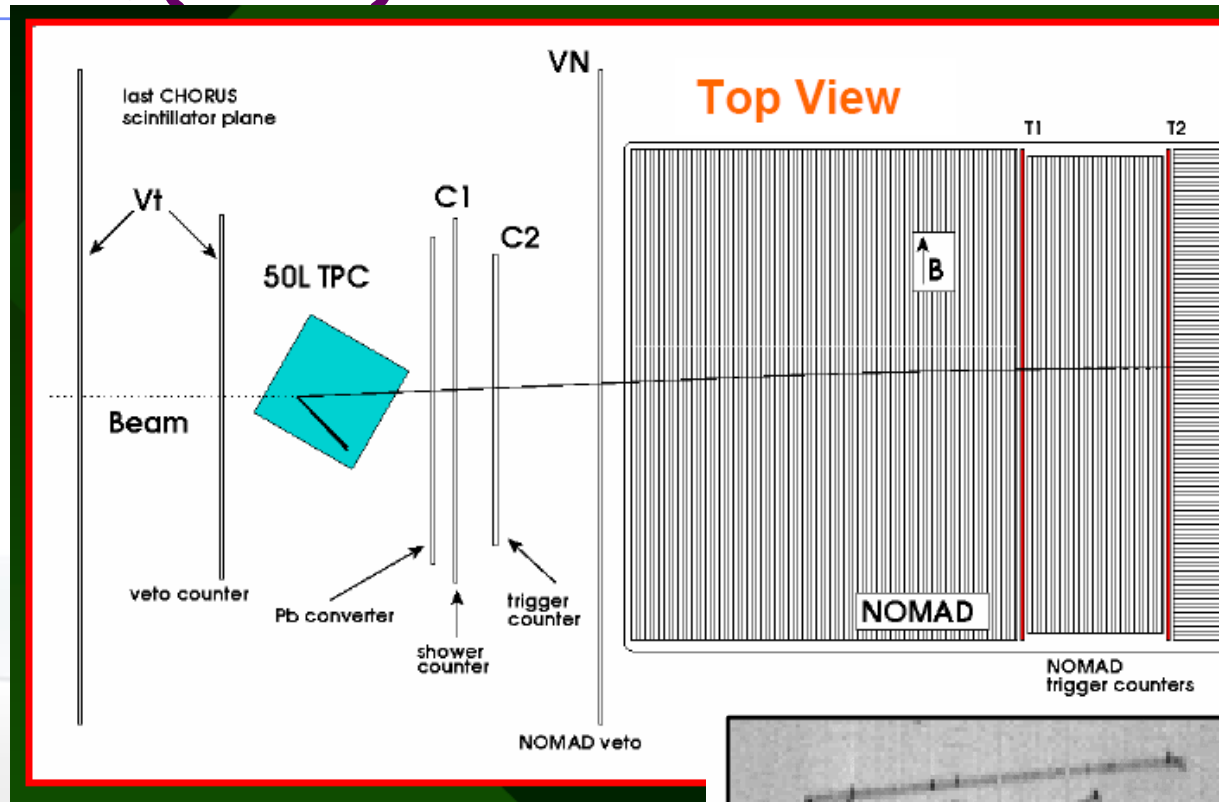


More particle production examples: 14.6 GeV/c

Particle prod from
protons on Be and Au
Fluka vs
E-802 at BNL



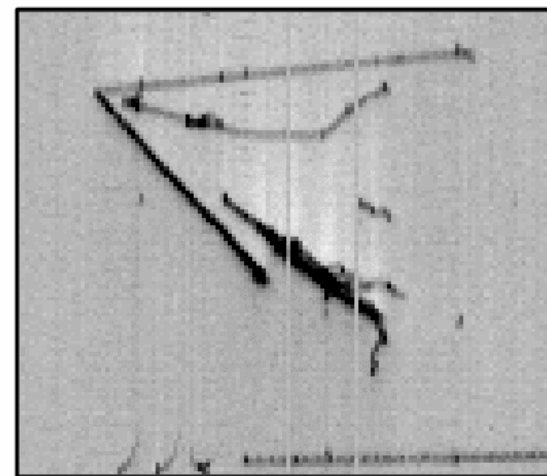
The 50l LAr TPC in the WANF neutrino beam(1997)



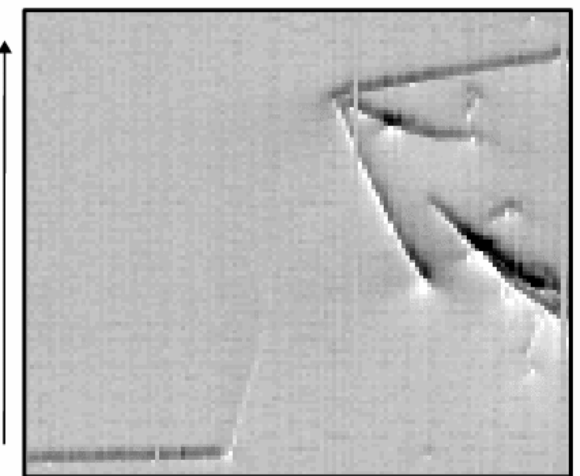
Trigger and μ
reconstruction: NOMAD

Event selection: "GOLDEN sample"
= 1 μ and 1 proton $>40\text{MeV}$ fully contained

Phys.Rev. D74 (2006) 112001



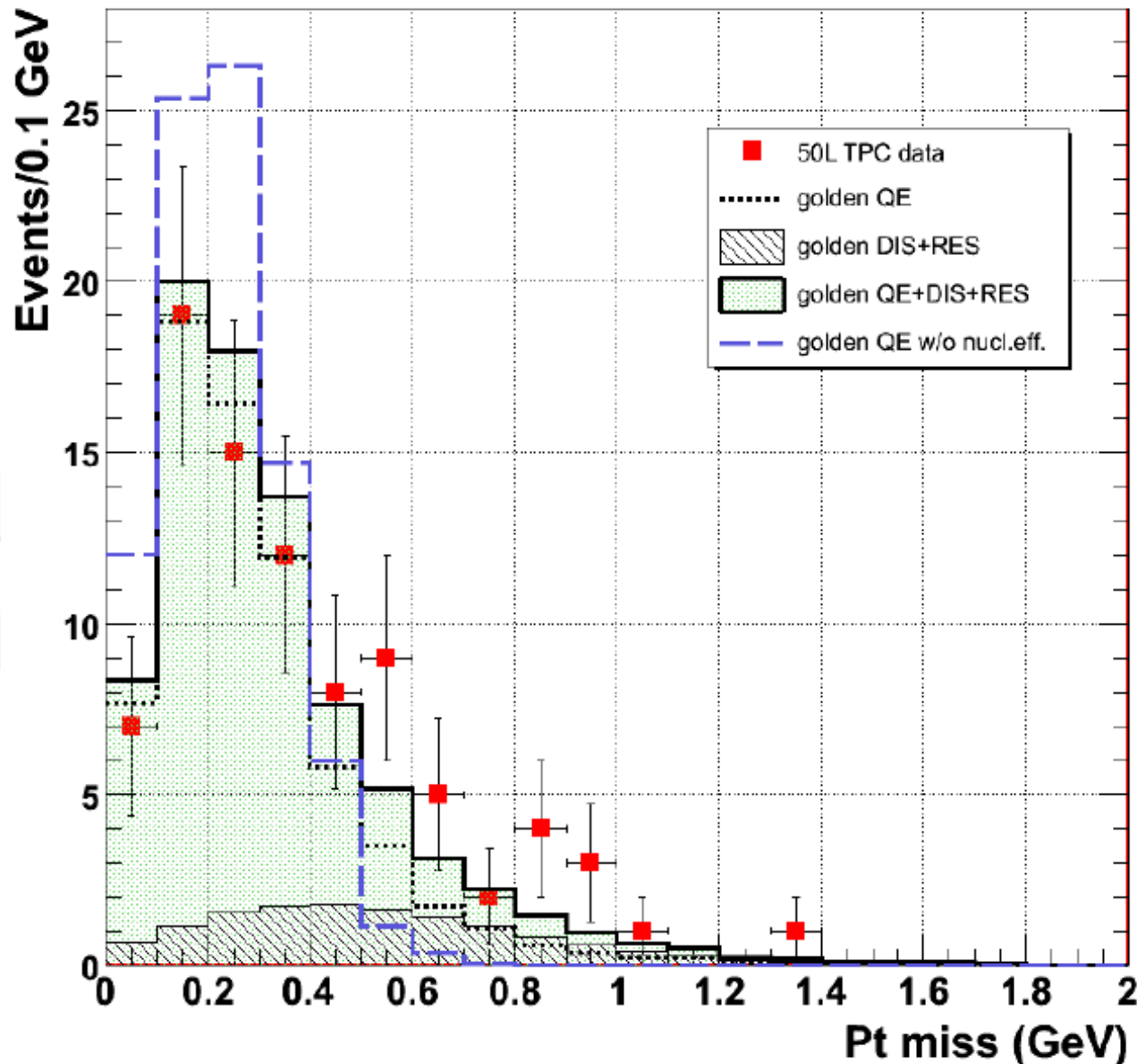
Collection wires. (128 wires: 32 cm.)



Induction wires. (128 wires: 32 cm.)

Time (1300 samples: 47 cm)

Missing transverse momentum



- from 400 QE - golden fraction 16%
- background - additional 20% finally expected

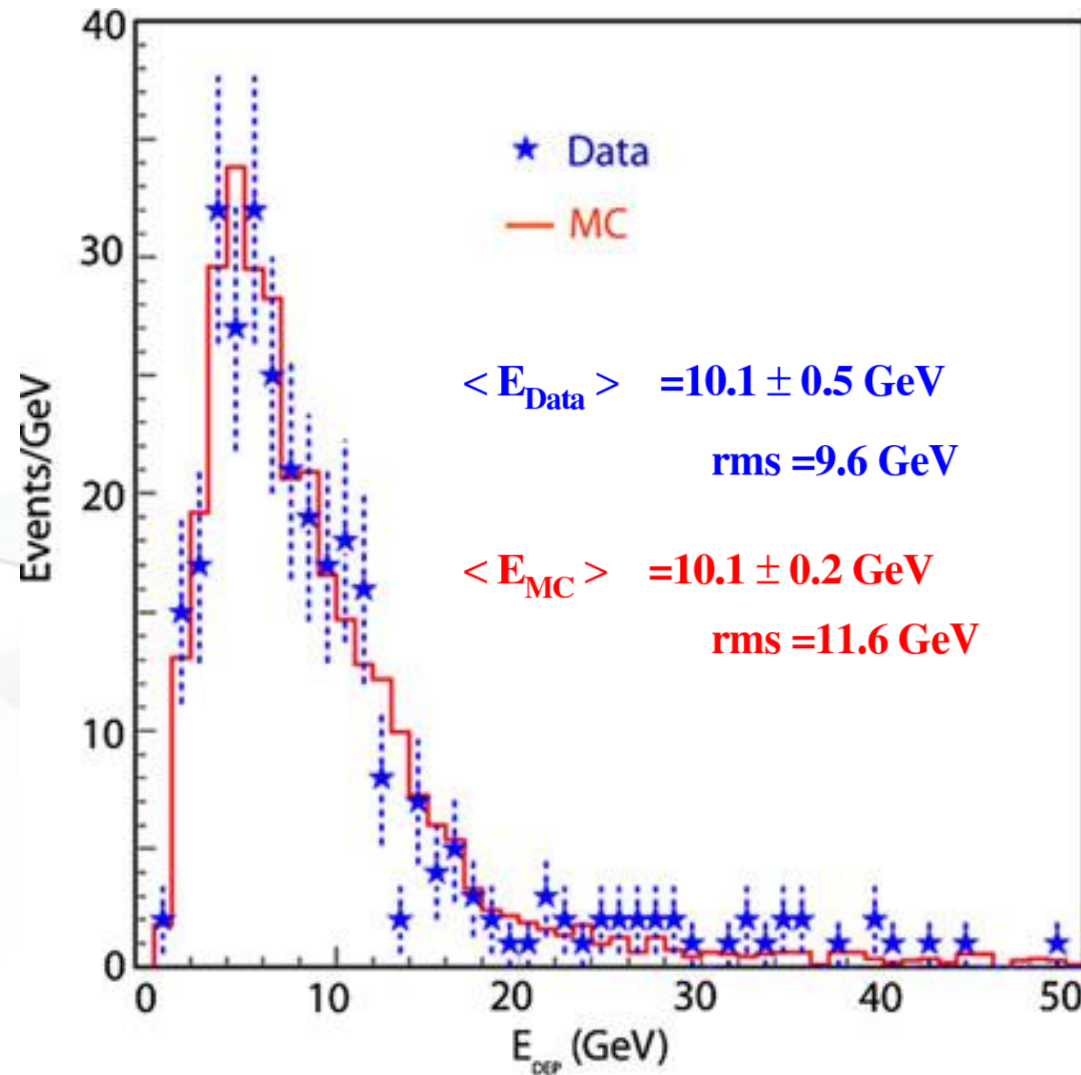
$80 \pm 9(\text{stat.}) \pm 13(\text{syst.}) \rightarrow$ mainly QE fraction and beam simul)

to be compared with **86** events observed

Very good consistency with expectations

Note: here DIS and RES from old coupling with the NUX code (A. Rubbia)

CNGS data



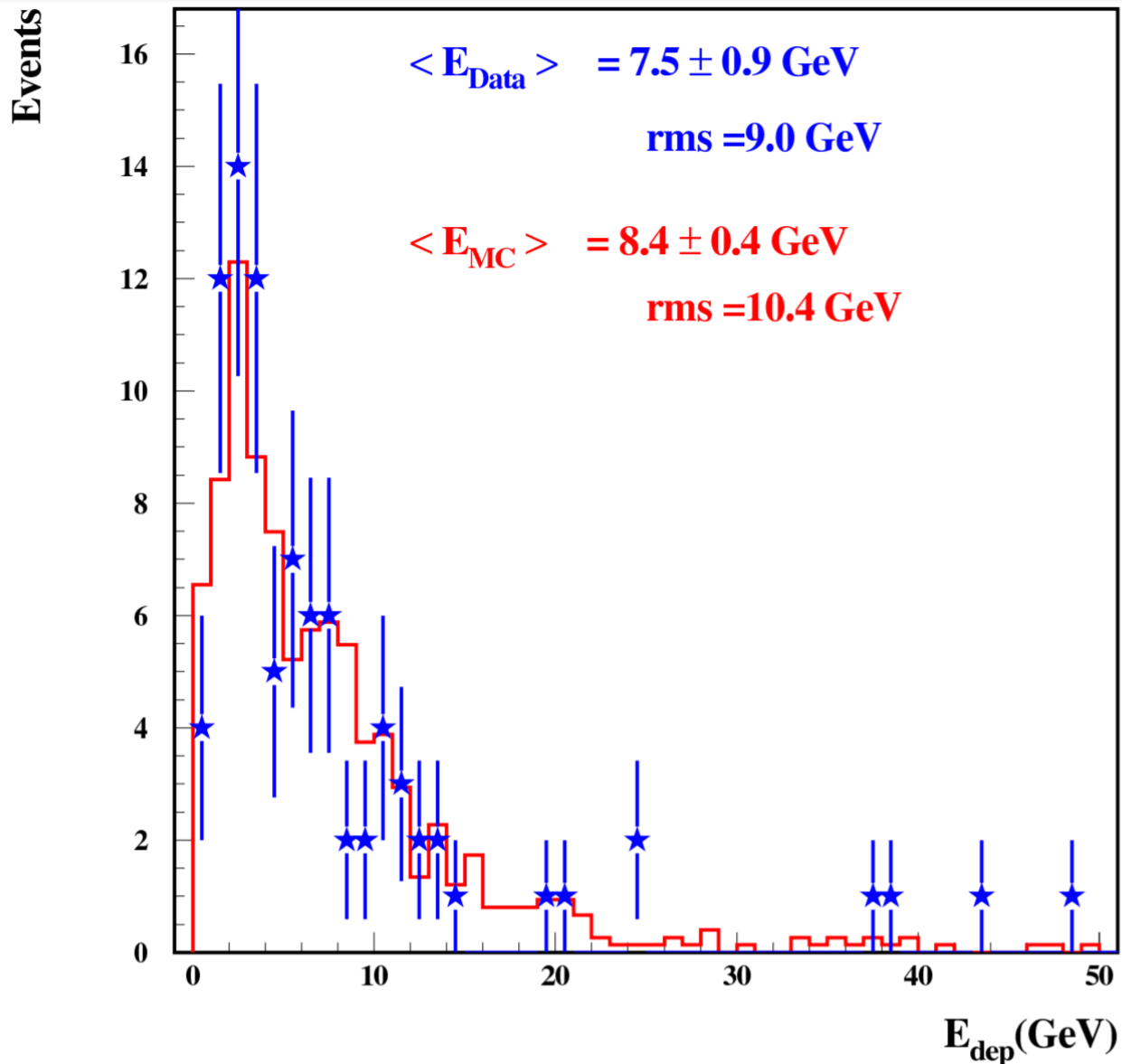
Distribution of total deposited energy in the T600 detector
CNGS numuCC events (~20 GeV E_{ν} peak)

Same reconstruction in MC and Data
Neutrino fluxes from FLUKA cngs simulations

Absolute agreement on neutrino rate within 6%

Eur. Phys. J. C (2013) 73:2345
Phys. Lett. B (2014)

CNGS data



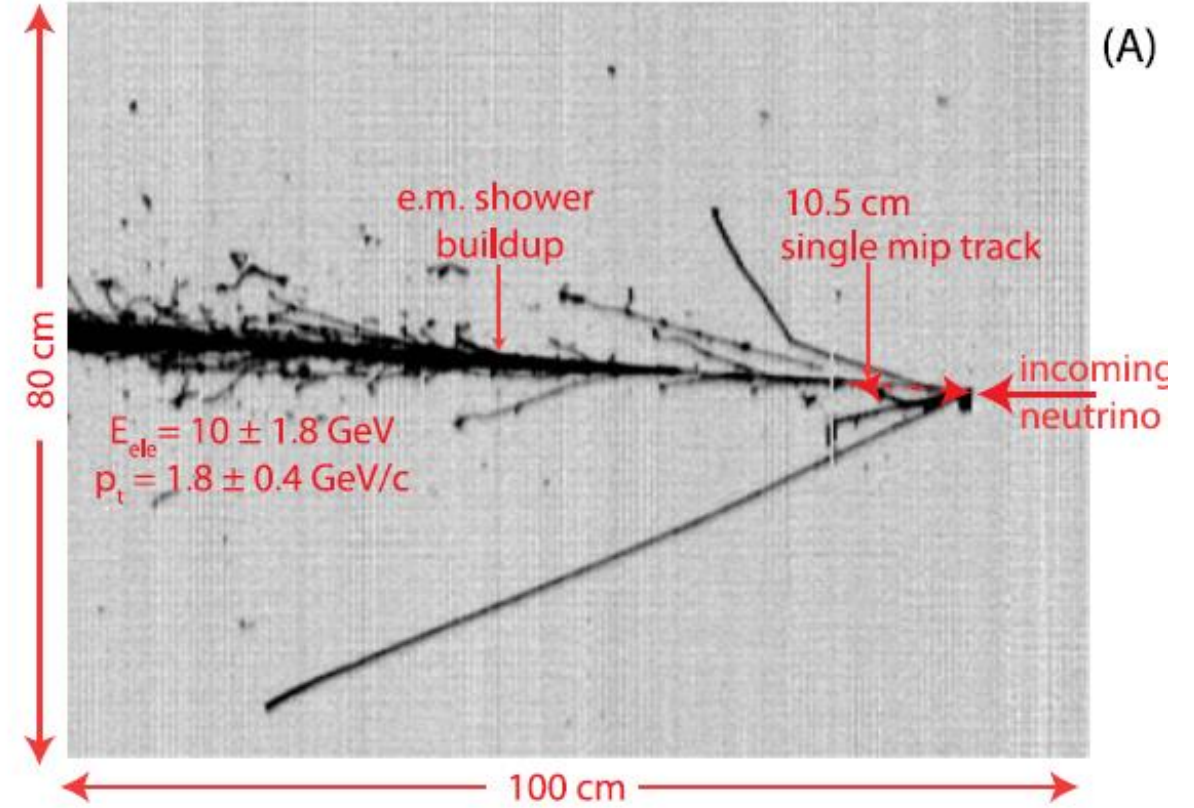
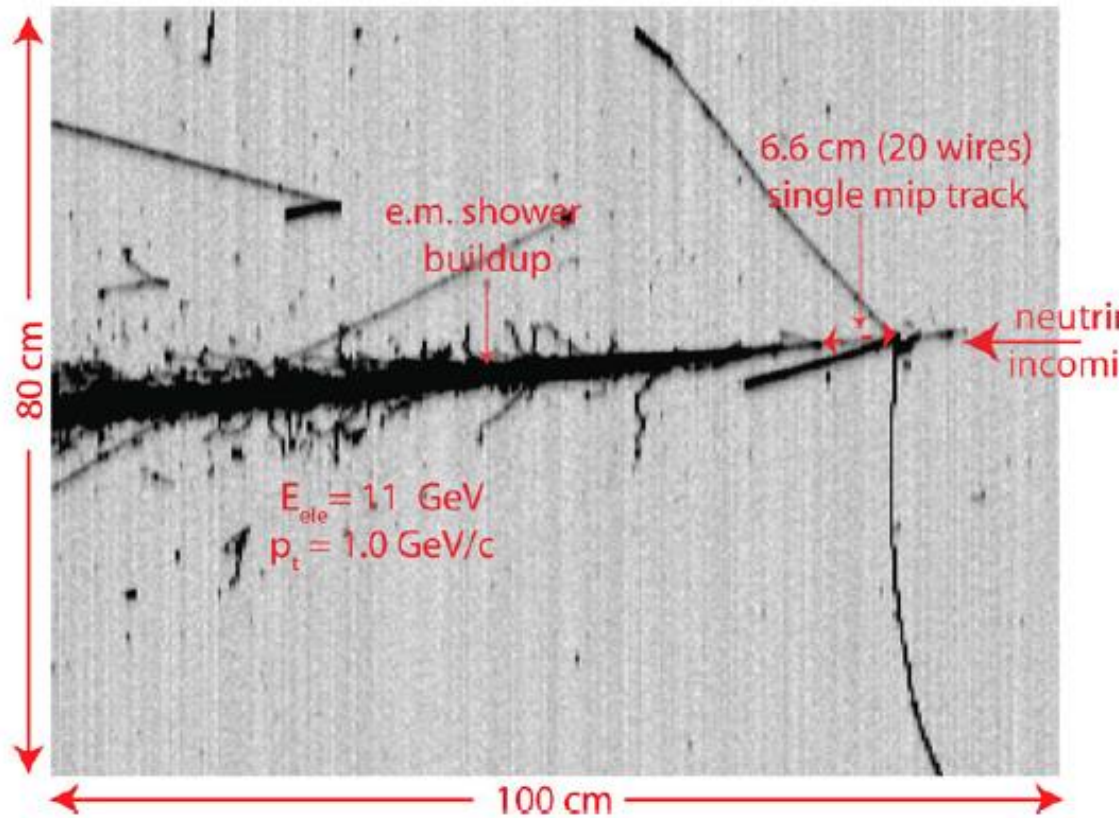
Distribution of total deposited energy in the T600 detector
CNGS nuNC

Same reconstruction in MC and Data
Neutrino fluxes from FLUKA cngs simulations

Only events with $E_{\text{dep}} > 500$ Mev

ICARUS events

Eur. Phys. J. C (2013) 73:2345 ICARUS T600 at LNGS, CNGS beam



One is real, the other simulated

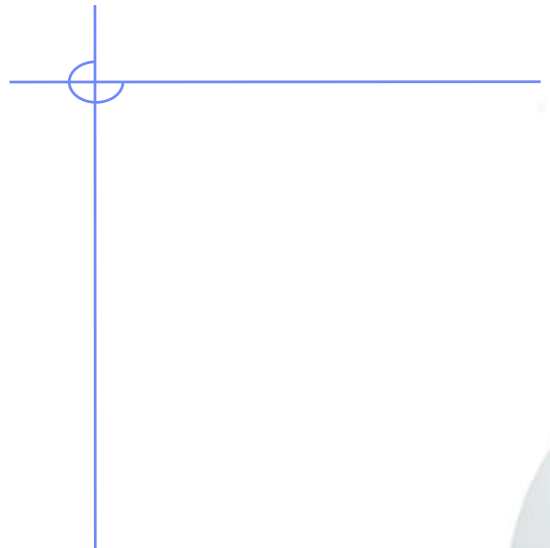
Last steps of the reaction

- The INC in FLUKA is carried on until all involved nucleons drop below 30-50 MeV kinetic (smooth threshold, depends on number of excited nucleons)
- A **PRE-EQUILIBRIUM** steps comes in : nucleon-hole pairs sharing statistically the residual excitation energy. Exciton number increased by "collisions", particle emission still possible.
- When the exciton number reaches equilibrium, **EVAPORATION / FISSION** comes in. Statistical, includes nucleons and heavy fragments, includes sub-barrier emission, takes into account single excited levels.
- At excitation energies $<$ separation energy \rightarrow **emission of gamma rays** (actually also in competition with evaporation) . Uses **atlas of excited levels/transitions** whenever available. **See ArgoNeut talk at NUINT**

Conclusions and perspectives

- A neutrino event generator (NUNDIS) is implemented in FLUKA
- QE, RES, DIS interactions
- Hadronization as for hadronic interactions in FLUKA
- Nuclear effects from the FLUKA nuclear models
- Encouraging comparisons with expt data

- More has to be done:
 - Coherent pion production
 - Coherent effects (see high x in Minerva and proton pairs in Argoneut)
 - More coherent / nuclear structure effects for low energy QE
 - Meson exchange in QE (high x in Minerva)
 - Radiative corrections in DIS (ongoing)
 - Comparisons against data



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R. Garcia Alia, J. Idarraga Munoz, W. Kozłowska, A. Lechner, M. Magistris, A. Mereghetti, E. Nowak, S. Roesler, F.
Salvat-Pujol, P. Schoofs, E. Skordis, G. Smirnov, C. Theis, A. Tsinganis, Heinz Vincke, Helmut Vincke, V. Vlachoudis,
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Nuclear potential for pions

For pions, a complex nuclear potential can be defined out of the π -nucleon scattering amplitude to be used in conjunction with the Klein-Gordon equation

$$\left[(\omega - V_c)^2 - 2\omega U_{opt} - K^2 \right] \Psi = m_\pi^2 \Psi$$

In coordinate space (the upper/lower signs refer to π^+ / π^-):

$$2\omega U_{opt}(\omega, r) = -\beta(\omega, r) + \frac{\omega}{2M} \nabla^2 \alpha(\omega, r) - \nabla \frac{\alpha}{1 + g\alpha(\omega, r)} \nabla$$

$$\beta = 4\pi \left[\left(1 + \frac{\omega}{M} \right) \left(b_0(\omega) \mp b_1(\omega) \frac{N-Z}{A} \right) \rho(r) + \left(1 + \frac{\omega}{2M} \right) B_0(\omega) \rho^2(r) \right]$$

$$\alpha = 4\pi \left[\frac{1}{\left(1 + \frac{\omega}{M} \right)} \left(c_0(\omega) \mp c_1(\omega) \frac{N-Z}{A} \right) \rho(r) + \frac{1}{\left(1 + \frac{\omega}{M} \right)} C_0(\omega) \rho^2(r) \right]$$

Using standard methods to get rid of the non-locality, in momentum space

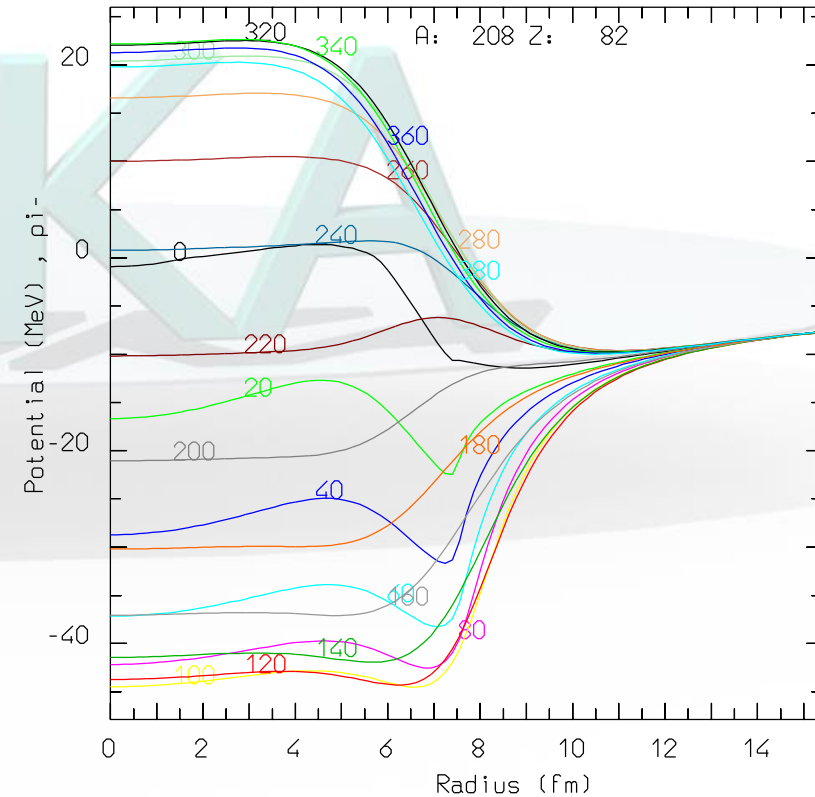
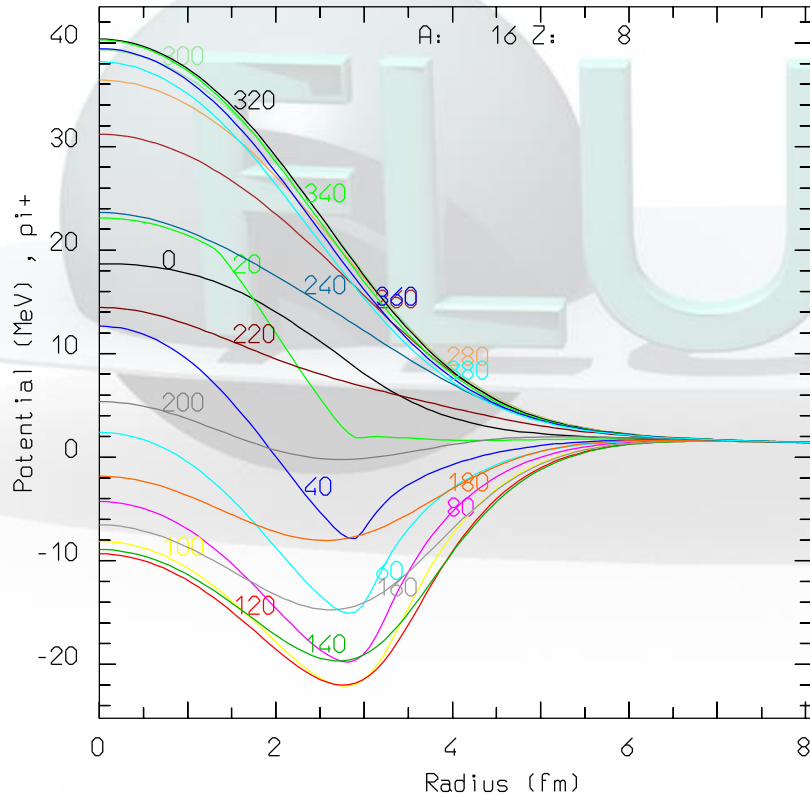
$$2\omega U_{opt}(\omega, r) = -\beta - K^2 \frac{\alpha}{1 + g\alpha} + \frac{\omega}{2M} \nabla^2 \alpha$$

$$K^2 = k_0^2 + V_c^2 - 2\omega V_c^2 - 2\omega U_{opt}(\omega, r) = \frac{k_0^2 + V_c^2 - 2\omega V_c^2 + \beta - \frac{\omega}{2M} \nabla^2 \alpha}{1 - \bar{\alpha}}$$

$$\bar{\alpha} = \frac{\alpha}{1 + g\alpha}$$

Nuclear potential for pions: examples

The real part of the pion optical potential for π^- on ^{16}O (left) and π^+ on ^{208}Pb (right) as a function of radius for various pion energies (MeV)

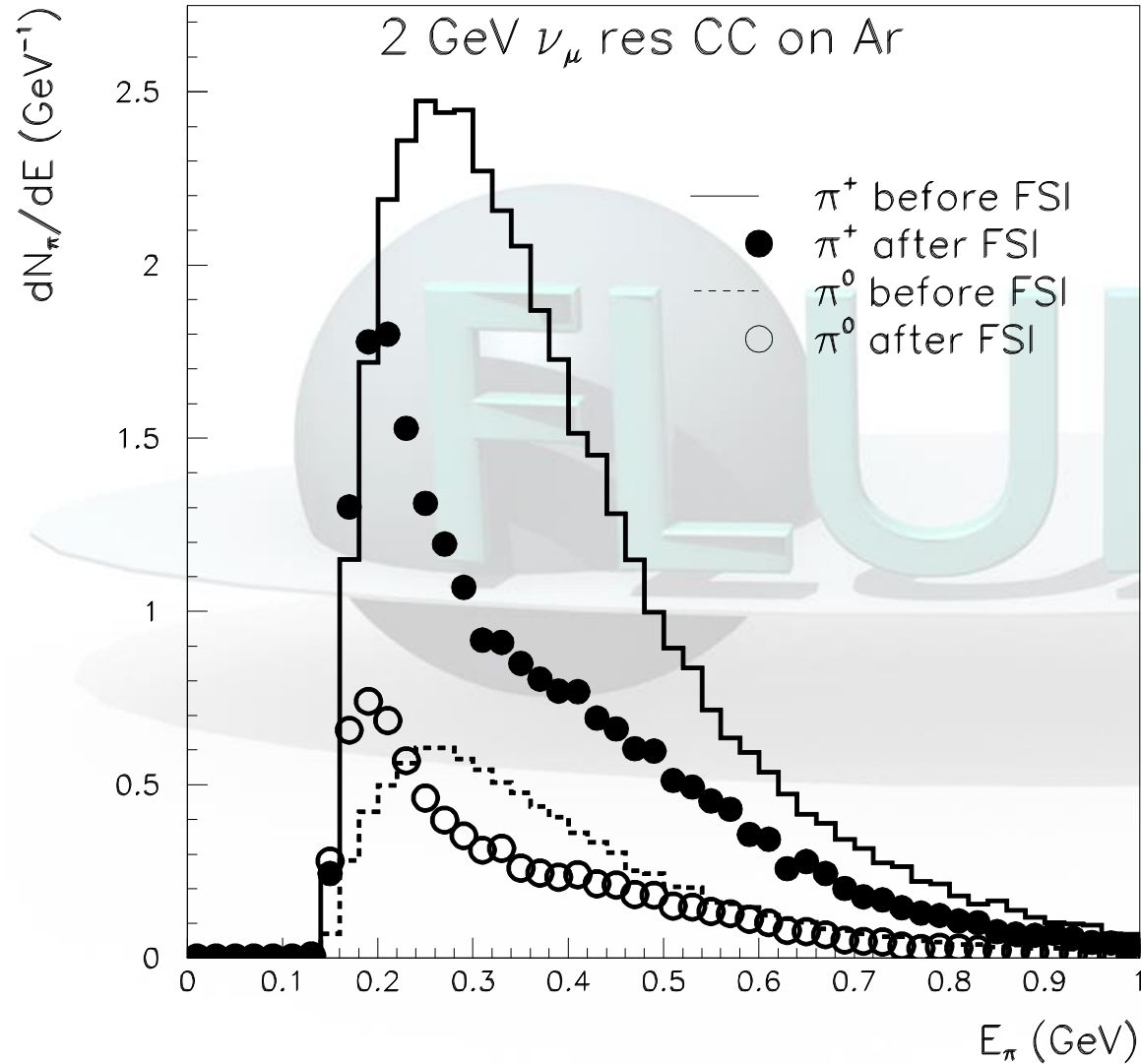


NUNDIS 2015: kinematics

- Considered kinematical limits for the *PDF* available from GRV94, GRV98, and BBS analyses.

| Variable | Required | GRV94 | | GRV98 | | BBS | |
|---------------------------------|---------------------------|-----------------|------------|-----------|------------|-----------|----------------|
| | | Default | Tested | Default | Tested | Default | Tested |
| E_{min} (GeV) | — | 0.050 | | | | | |
| E_{max} (GeV) | $\geq 10^4$ | $70 \cdot 10^3$ | | | 10^5 | | |
| Q_{min}^2 (GeV ²) | $\leq 5.5 \cdot 10^{-12}$ | 0.4 | 0.4 | 0.8 | 0.8 | 2 | 0.8 |
| Q_{max}^2 (GeV ²) | $\geq 1.9 \cdot 10^4$ | 10^6 | 10^9 | 10^6 | 10^9 | 10^4 | $2 \cdot 10^4$ |
| x_{min} | $\leq 1.4 \cdot 10^{-11}$ | 10^{-5} | 10^{-30} | 10^{-9} | 10^{-30} | 10^{-4} | 10^{-30} |
| x_{max} | 1 | 0.99999 | 0.99999 | 1 | 1 | 1 | 1 |

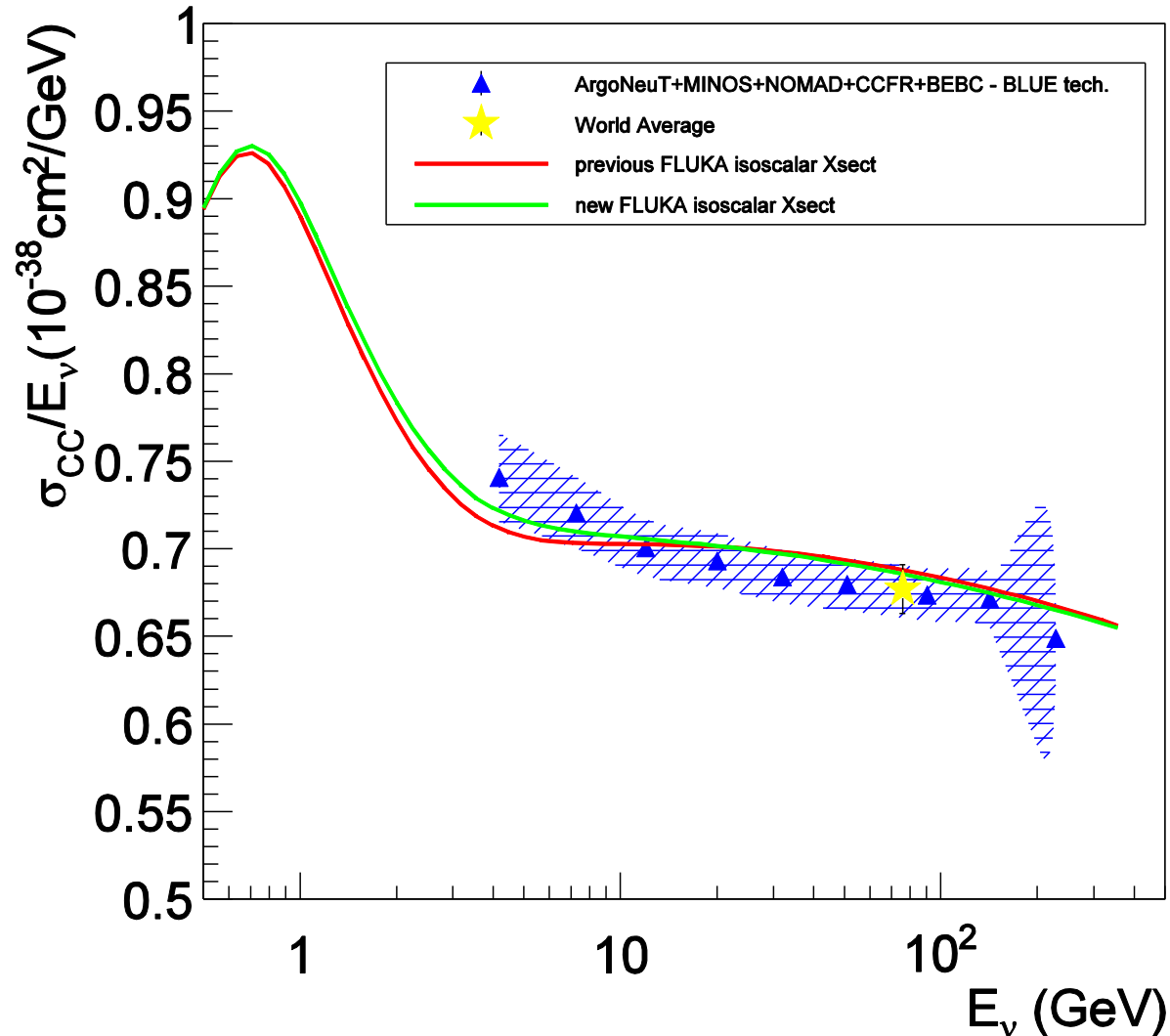
Expected effect in Ar



Example of expected effect:
2 GeV ν_μ CC RES interaction in Ar:
Pion production vs pion total E
Lines: before FSI
Symbols: after FSI

Solid and filled symbols: positive pions
Dashed and open symbols: pizero

Same, with evaluation of data systematics



Work in progress: Attempt to compare with a combined estimate from available data and relative systematic error, properly accounting for correlations

Focus on the CNGS energy range (5-30 GeV)

Recent experiments (like MINOS, NOMAD, CCFR 1997): measure the **shape** of neutrino flux, and get the **Absolute normalization** from **Old measurements** at high energy, performed using Narrow Band Beams (CCFR-E701 / CCFRR-E616 / CDHS) or Wide Band Beams (GARGAMELLE / BEBC)

→ Common systematic errors

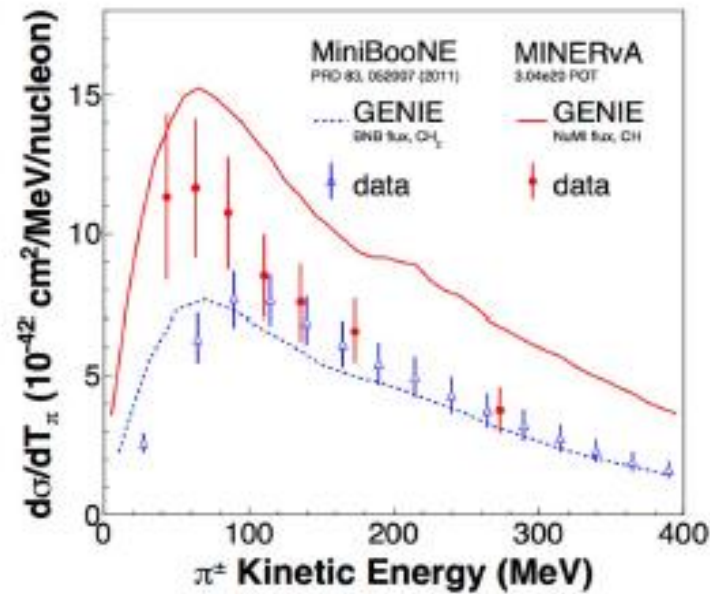
Data on pion production

Thoughts on MINERvA vs. MiniBooNE

- ▶ Shapes very similar, no significant dip in either!
- ▶ Small difference in slope (Kinematics, FF, nonres differences).
- ▶ Biggest difference is at low energy.

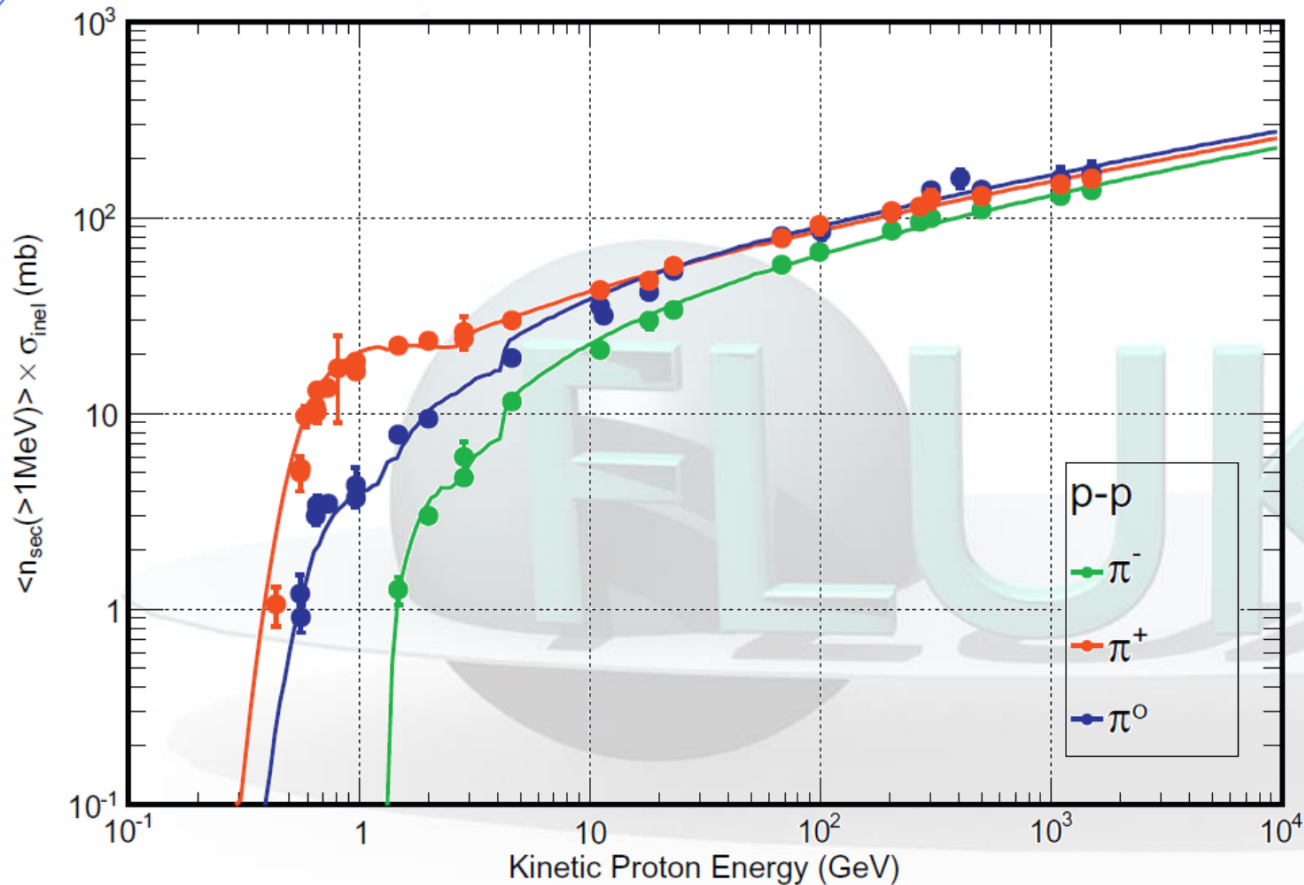
MiniBoone : CH₂, E_ν ≈ 0.8 GeV, cut on single pion, PHYS. REV.D 83, 052007 (2011)

Minerva : CH, E_ν ≈ 4 GeV, cut on W < 1.4 arXiv:1406.6415v3 (2015)



Tension betw the two data sets vs models/ extent of FSI

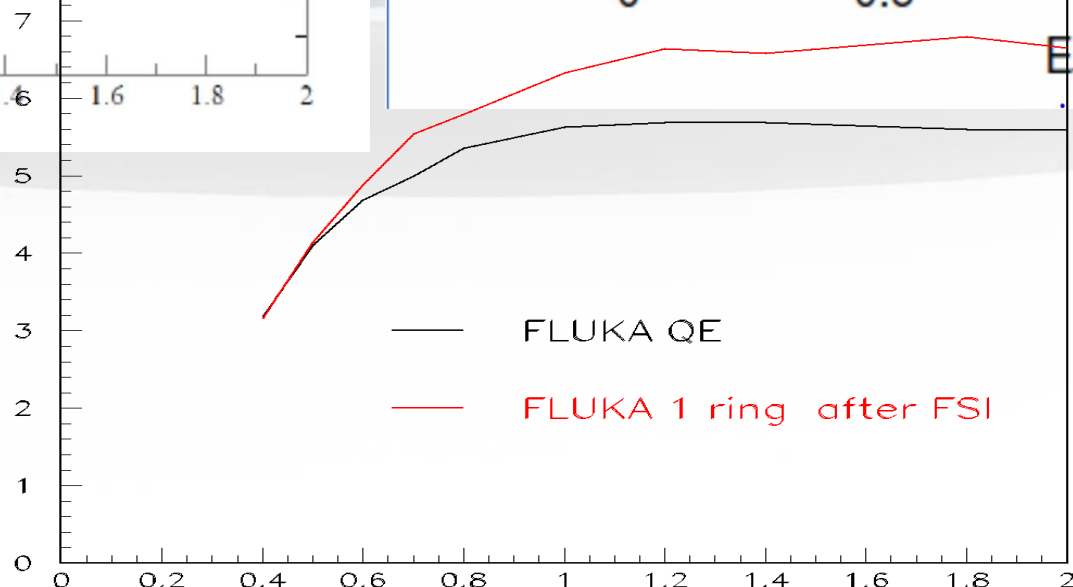
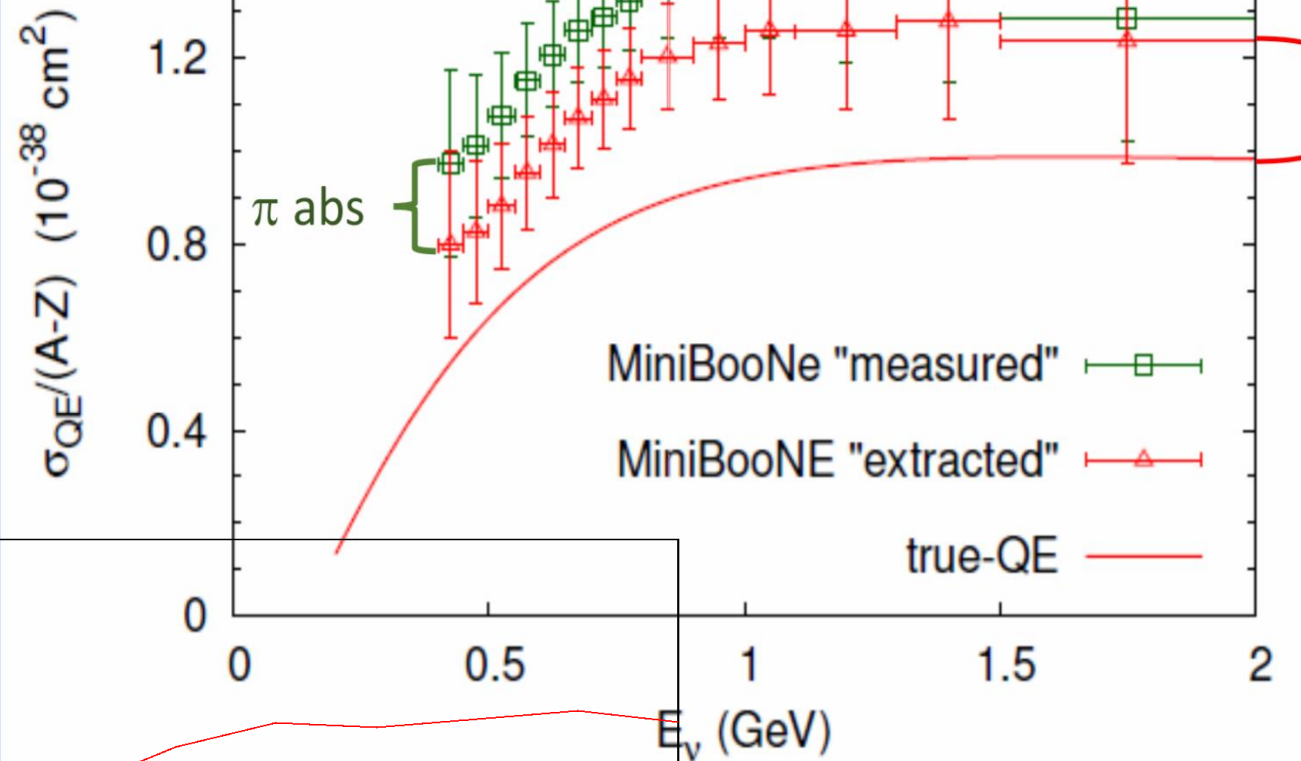
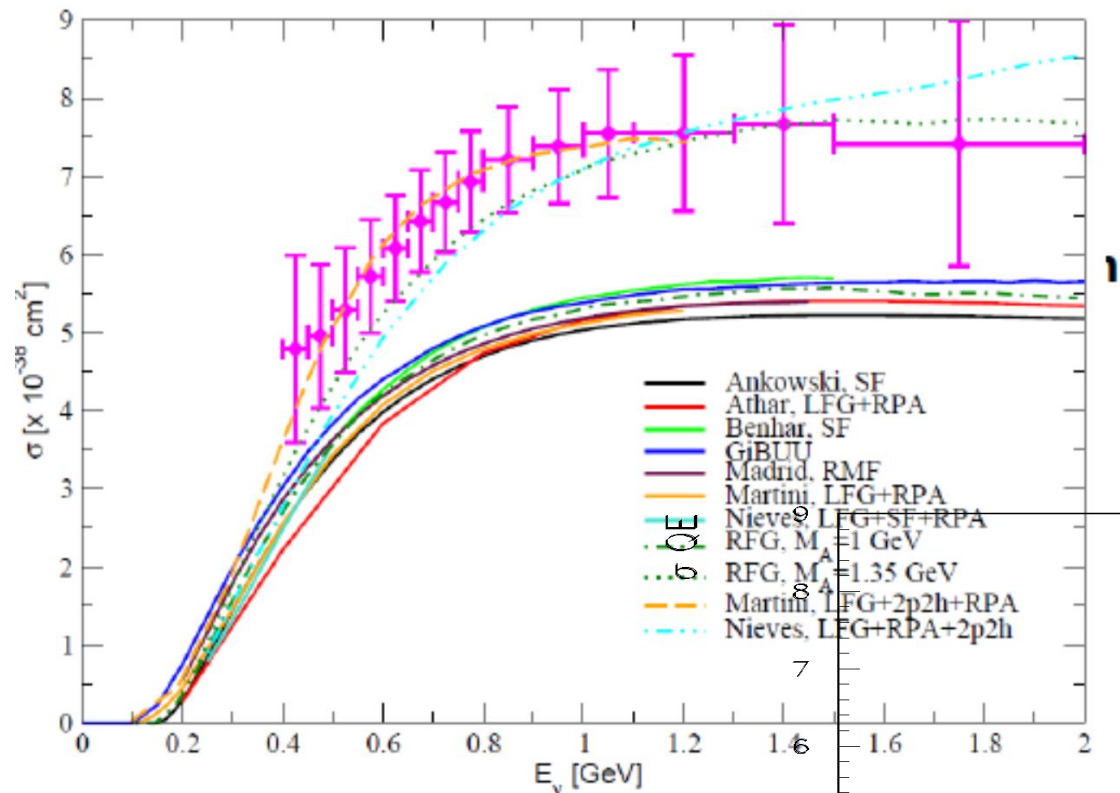
Pion production in p-p collisions:



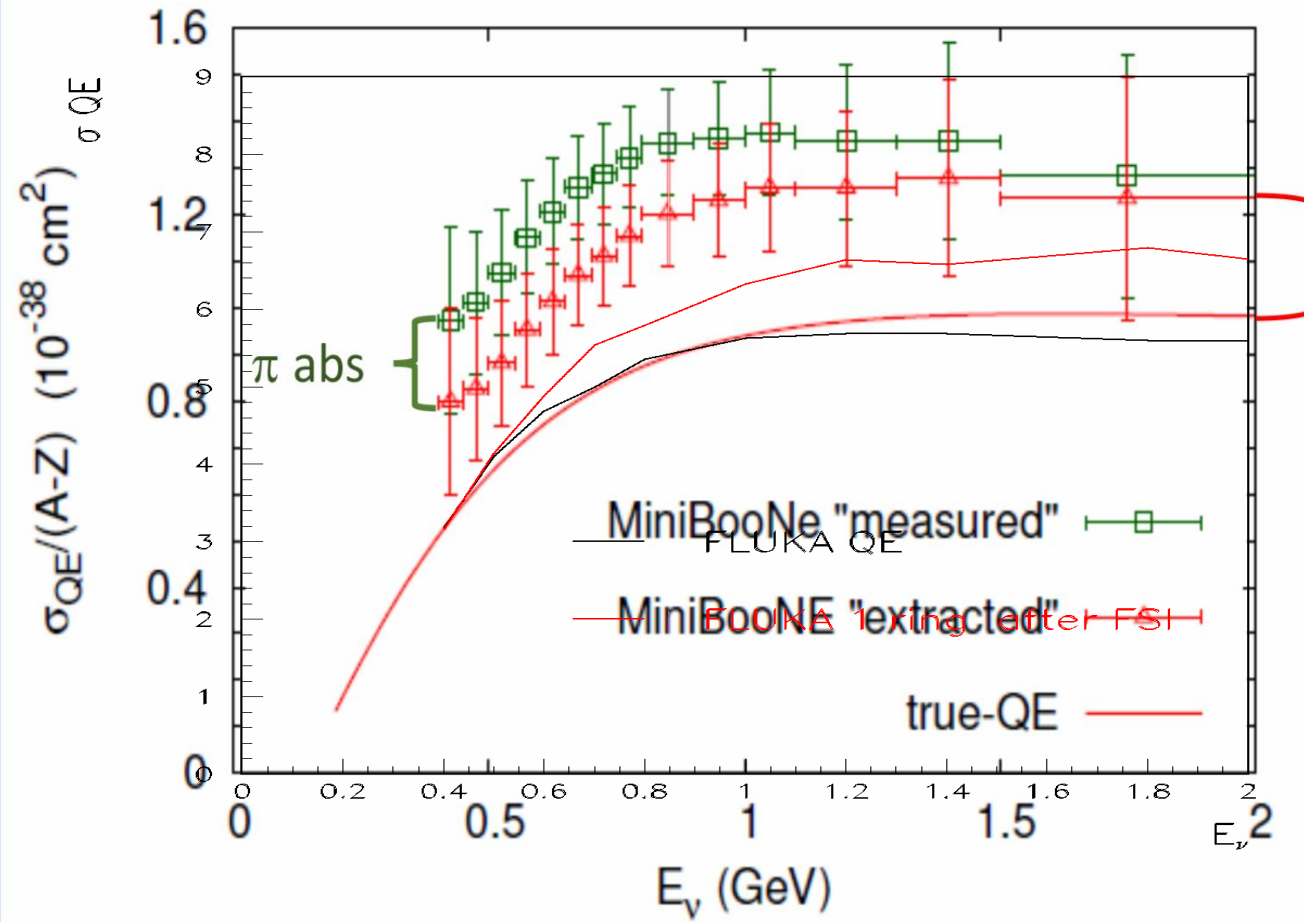
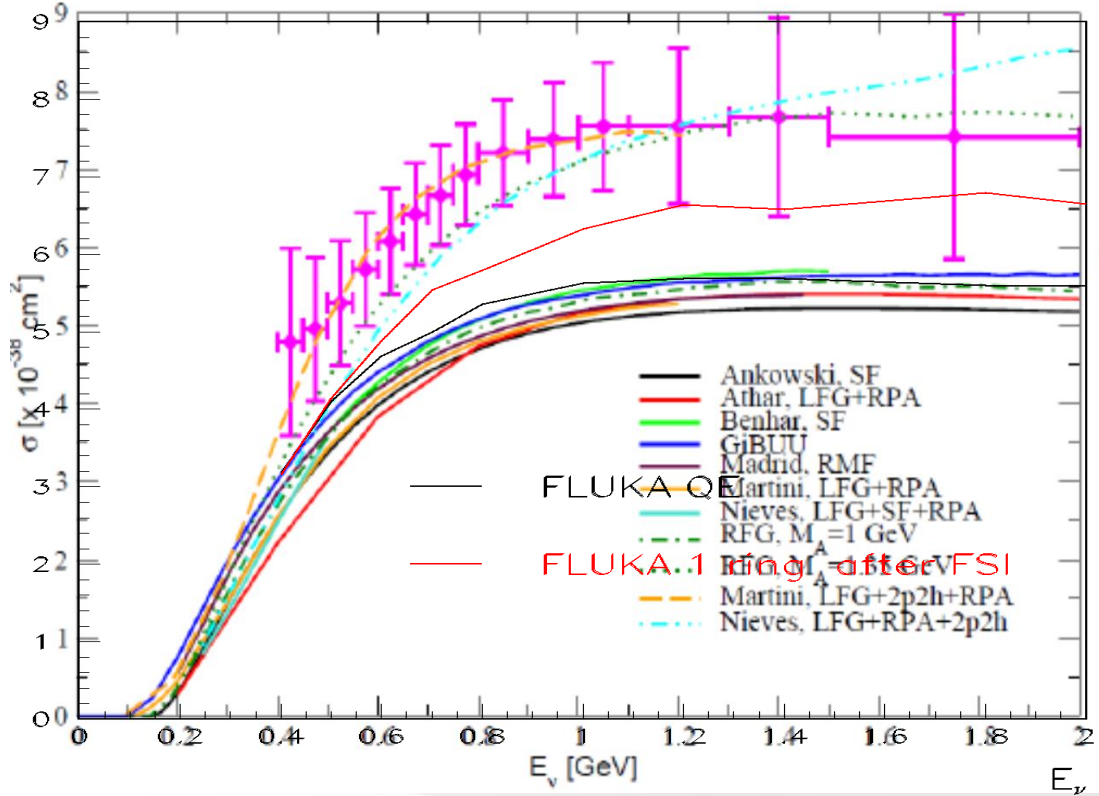
Inclusive cross section for the production of π^0 (blue), π^+ (red), and π^- (green) in p-p collisions as a function of the proton kinetic energy. Lines: simulations, symbols exp. Data. (figure from AstrPhys81, 21 (2016))

Fig. 2. Inclusive cross sections for the production of π^0 (blue), π^+ (red) and π^- (green) in p - p collision as function of the incoming proton kinetic energy. Lines: FLUKA simulation; points: data from Ref. [28]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

CCQE on ^{12}C



CCQE on ^{12}C



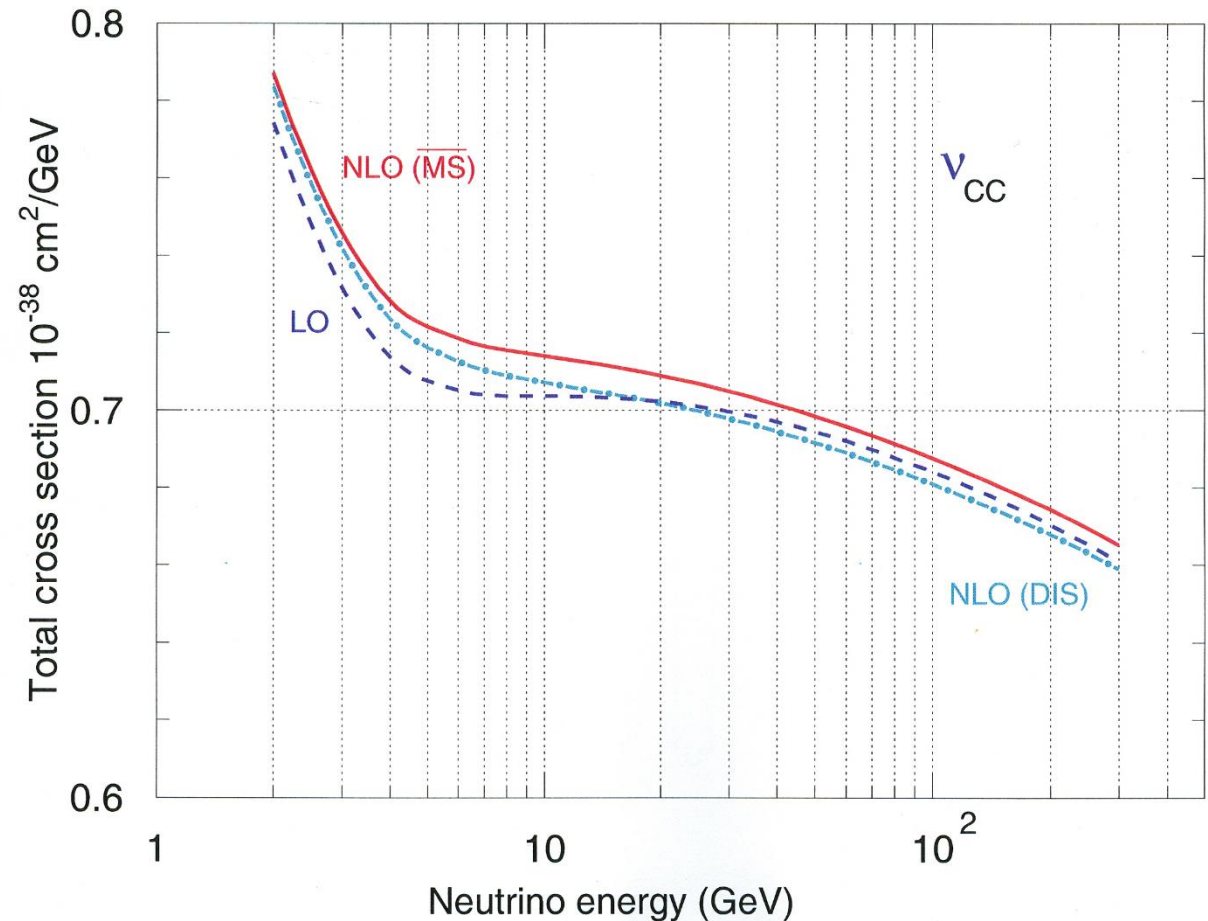
More on pdfs

Three versions of pdf from the GRV98 analysis are included as options for evaluating nucleon structure functions

1. Leading order analyses (LO)
2. Next to leading order analyses (NLO $\overline{\text{MS}}$)
3. Next to leading order analyses (NLO DIS)

An interesting feature of the GRV98 analysis is a low threshold for the transferred, 4-momentum, $Q^2 = 0.8 \text{ GeV}^2$

NLO (DIS) is chosen as a default option



Nucleon correlation function:

Correlation function: it can be computed within the Fermi-gas model

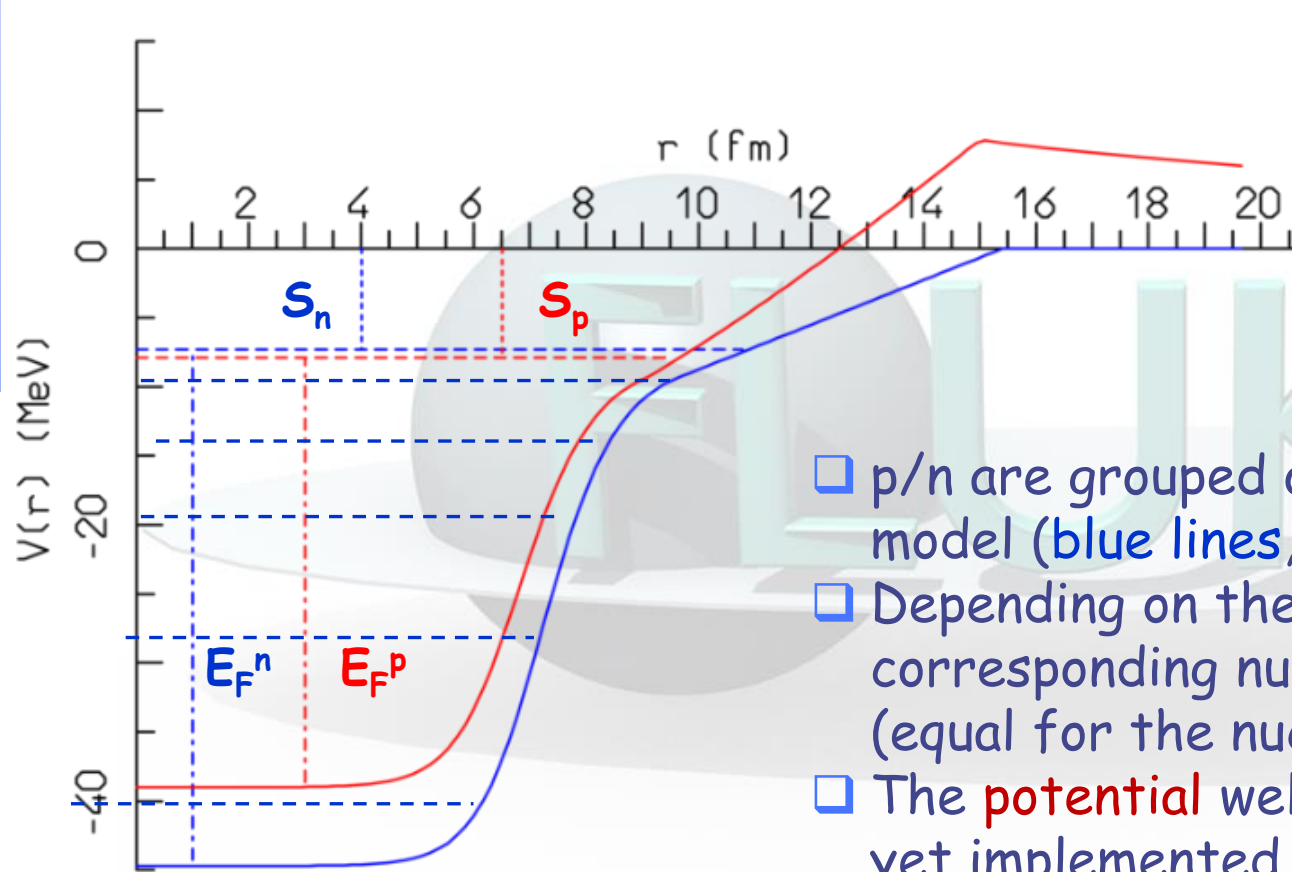
Due to the anti-symmetrization of the fermion's wave function, given a nucleon in a position \vec{r} in a nucleus with density ρ_0 , the probability of finding another like nucleon in a position \vec{r}' is decreased for small values of the distance $d = |\vec{r} - \vec{r}'|$ by a factor

$$g(x) = 1 - \frac{1}{2} \left[\frac{3}{x^2} \left(\frac{\sin x}{x} - \cos x \right) \right]^2$$

where $x = K_F d$, and the factor 1/2 in front of the parenthesis accounts for the two possible spin orientations.

Nucleon hard core effects are also taken into account, forbidding to "find" a nucleon of the same or different type at less than 1-1.5 fm distance. This check is applied at every possible re-interaction, checking against all nucleons already involved in previous interactions

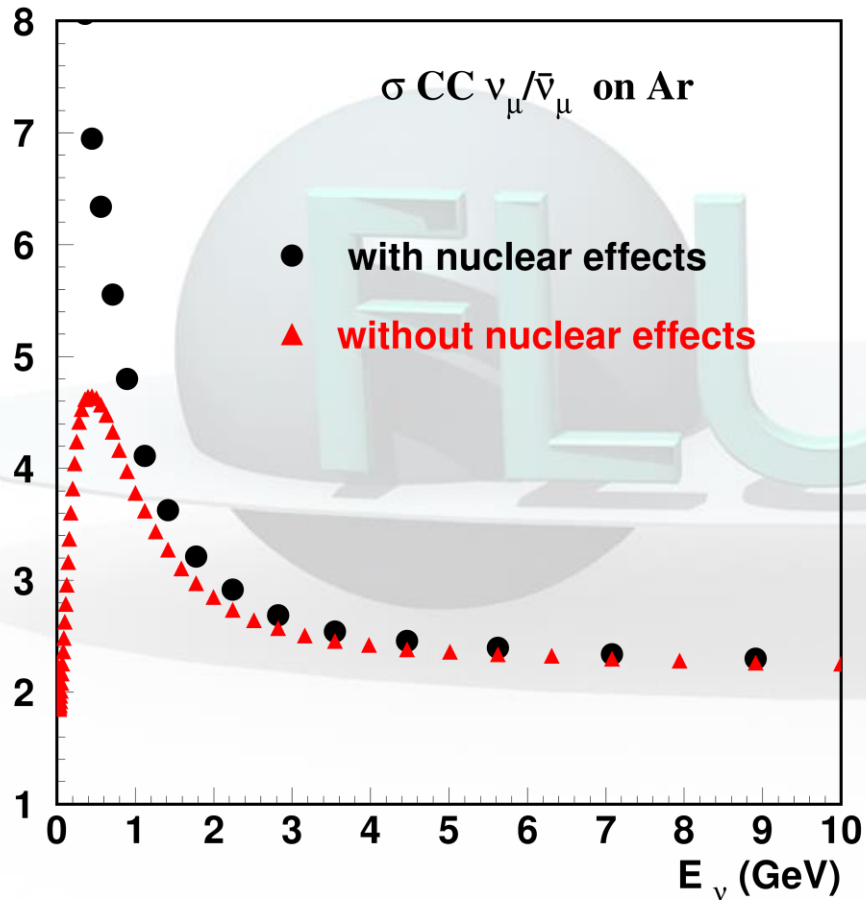
Nucleon levels inside the nuclear potential: schematic drawing



- Blue: neutron
- Red: proton

- p/n are grouped on energy levels space according to the shell model (blue lines, shown for neutrons)
- Depending on the level, the maximum radius for the corresponding nucleon is less or equal to the nucleus radius (equal for the nucleons on the Fermi level)
- The **potential** well depth **depends on the nucleon energy** (not yet implemented for neutrino and electron interactions)
- Hit nucleon must go above Fermi level, can stay below separation energy.

Effect of Pauli Blocking: example



Ratio of Neutrino/antineutrino σ_{CC} vs
(a) neutrino energy

For interactions in Ar nuclei, ν_{μ}

As calculated with FLUKA


Black: full calculation

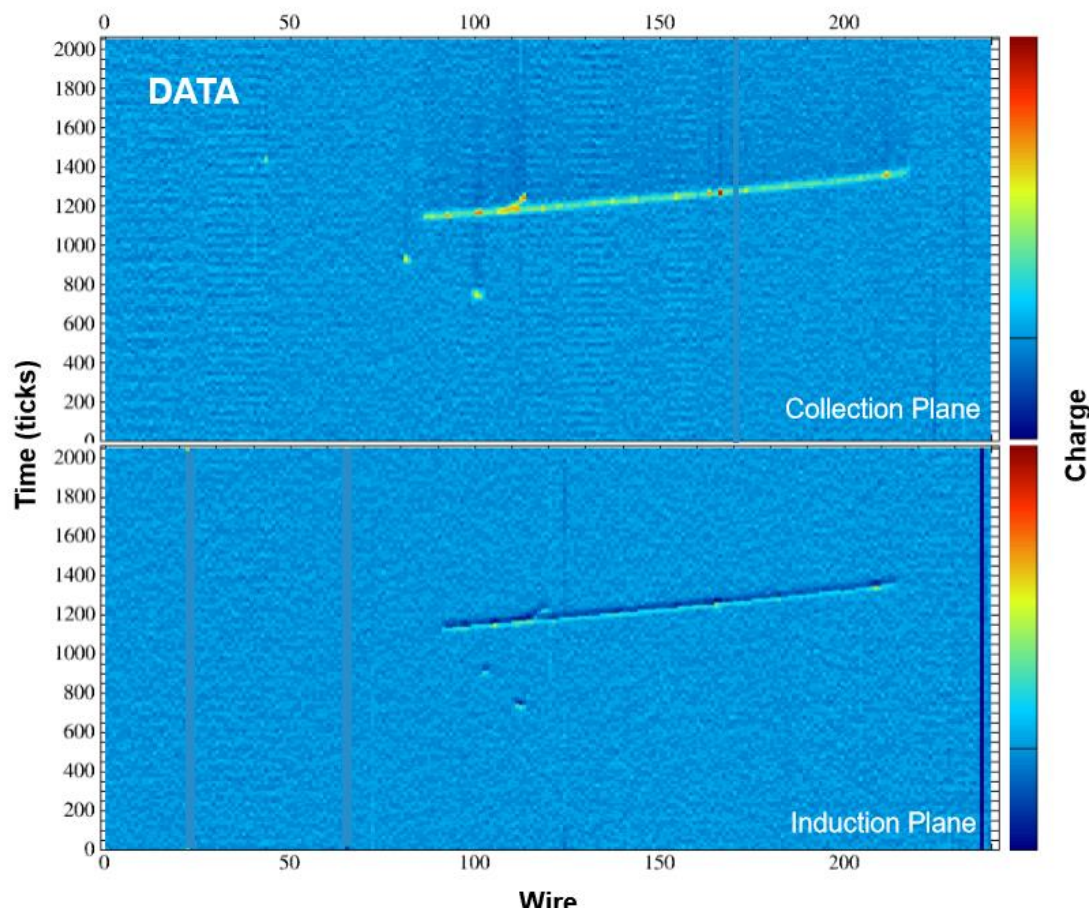
Red: simple sum of ν -N cross section

Smaller q^2 in anti-neutrino results in
higher Pauli-blocking probability

First Demonstration of LArTPC MeV-Scale Physics in ArgoNeuT

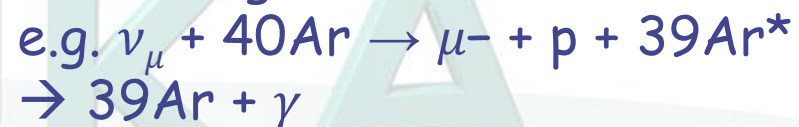
Ivan Lepetic *APS_April2018*

 ILLINOIS INSTITUTE OF TECHNOLOGY
For the ArgoNeuT Collaboration



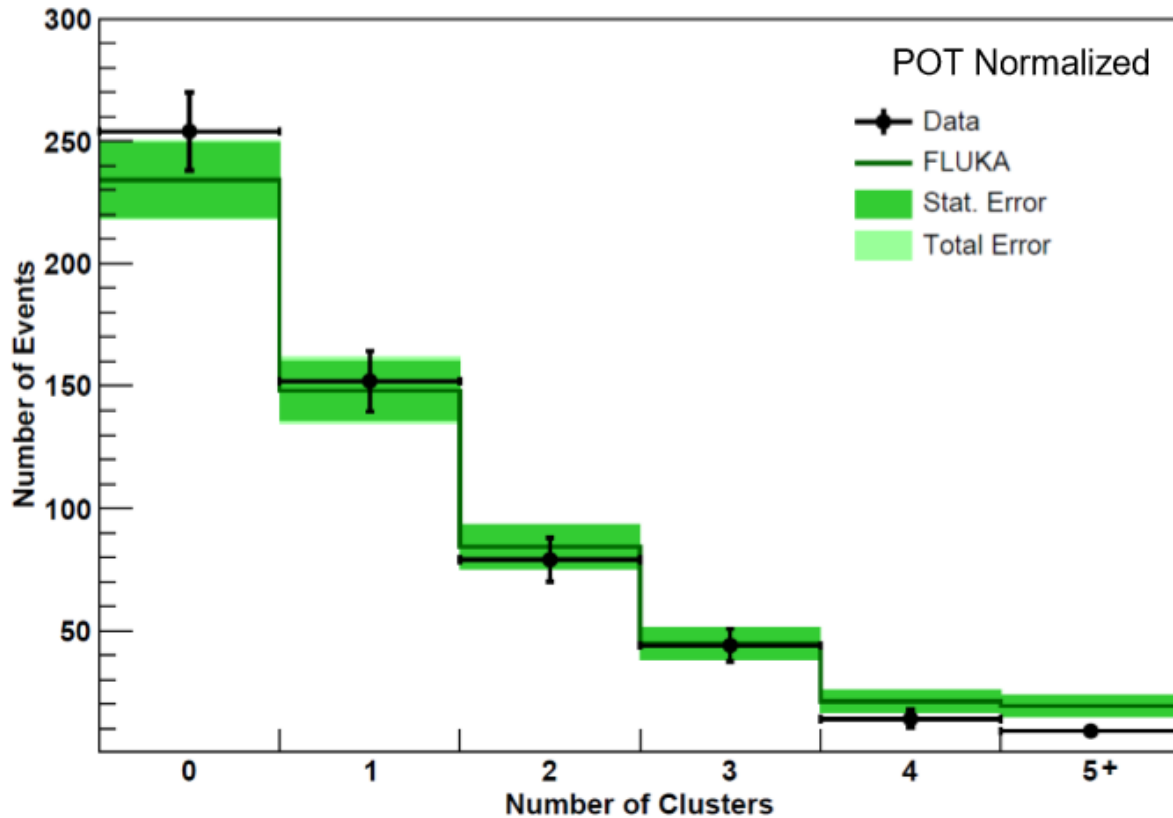
Low-energy gammas produced by neutrino-nucleus interactions in ArgoNeuT

Photons from **neutrino-produced nuclear de-excitation** and inelastic neutron scattering -



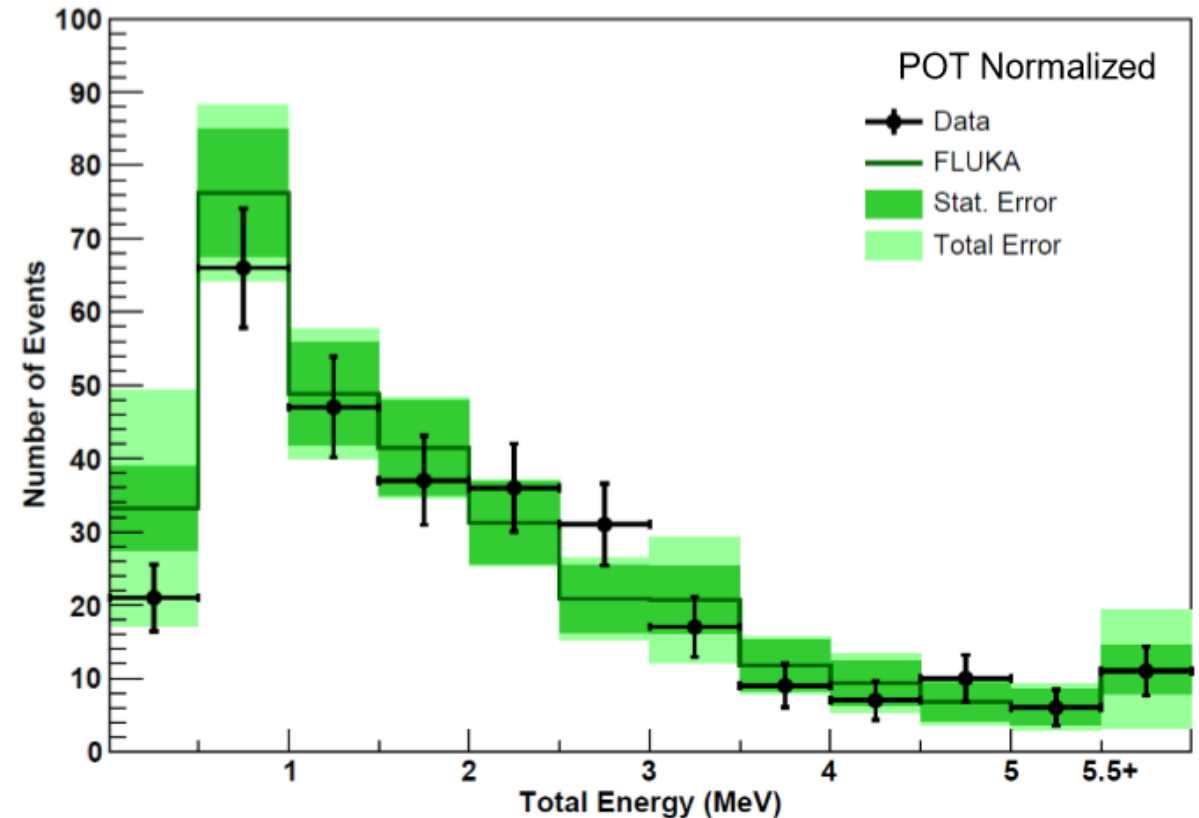
Data and FLUKA

Number of Clusters in an Event



$\chi^2/\text{ndf} = 9.62/6$. p-value = 0.14

Total Reconstructed Energy in an Event



$\chi^2/\text{ndf} = 7.74/12$. p-value = 0.81

Agreement is far worse if either de-excitation or neutron produced gammas are removed.

Effect of formation zone on residuals

Experimental and computed residual nuclei mass distribution

Ag(p,x)X at 300 GeV (top)

Au(p,x)X at 800 GeV (bottom)

Data from:

Phys. Rev. C19 2388 (1979) and

Nucl. Phys. A543, 703 (1992)

(The heavy fragment evaporation model is key for FLUKA predictions for $A < 30$)

Ag **with** and **without** form.zone:

$\langle \pi \rangle = 21.1$, $\langle E_\pi \rangle = 7.3$ GeV

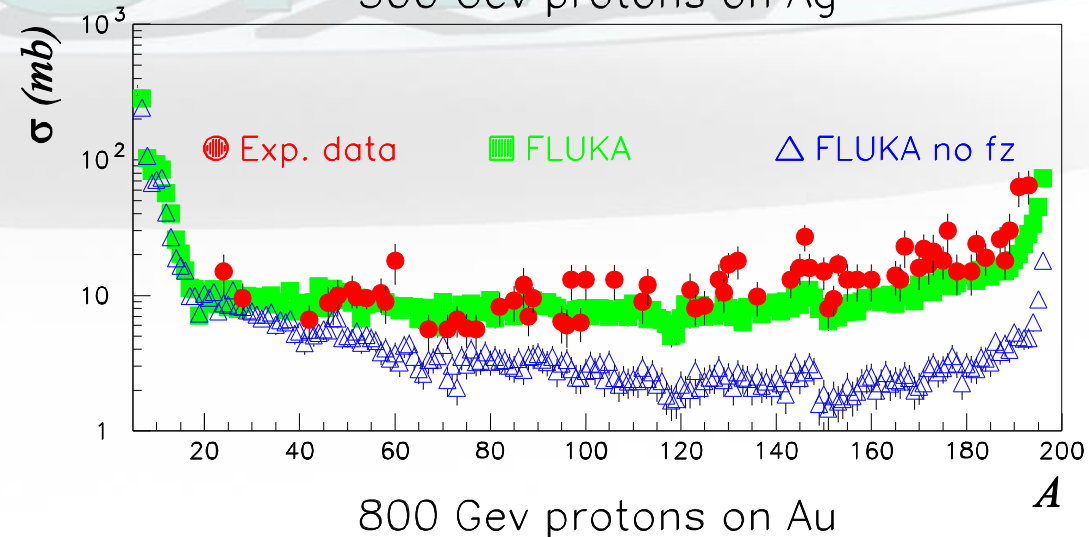
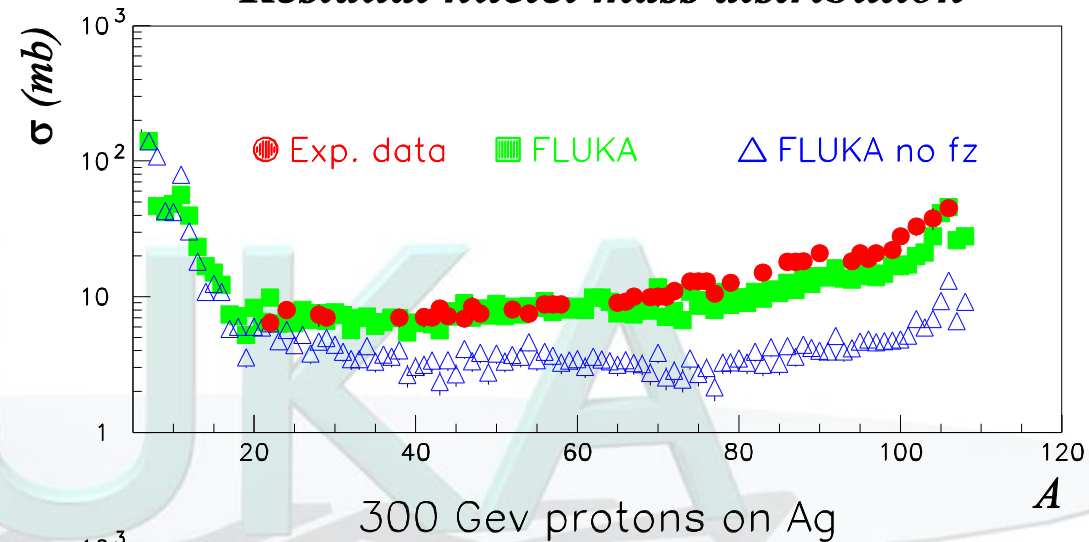
$\langle \pi \rangle = 49.7$, $\langle E_\pi \rangle = 3.4$ GeV

Au **with** and **without** form.zone:

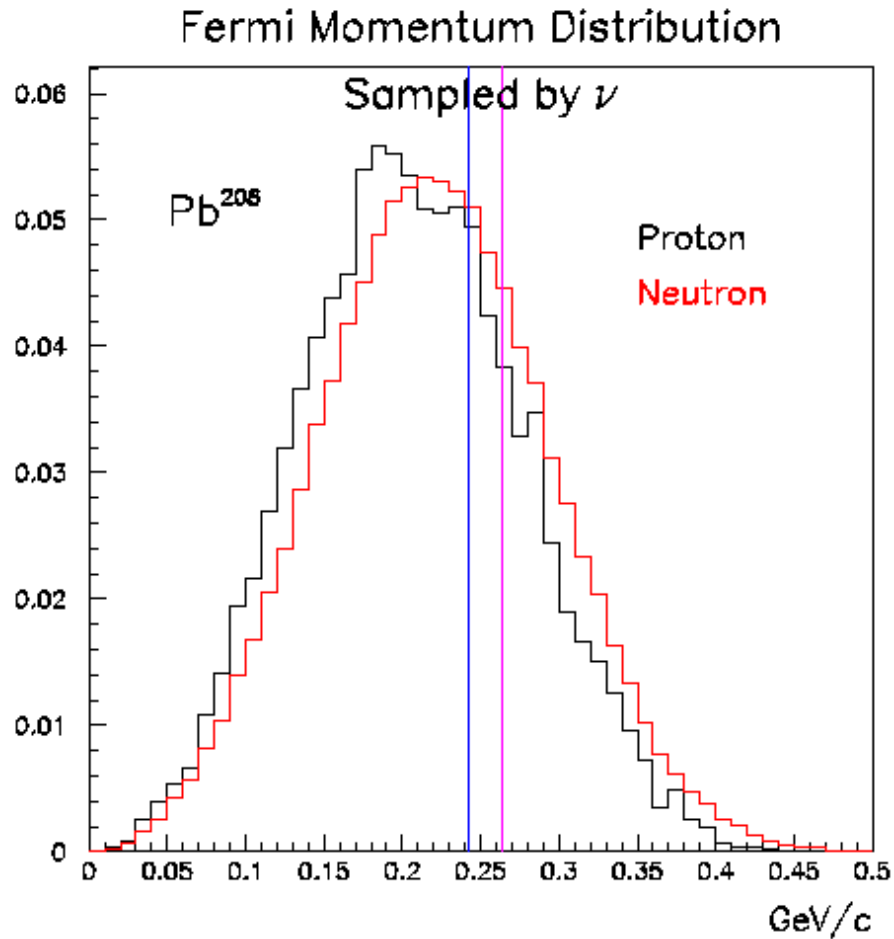
$\langle \pi \rangle = 30.1$, $\langle E_\pi \rangle = 12.5$ GeV

$\langle \pi \rangle = 96.0$, $\langle E_\pi \rangle = 4.6$ GeV

Residual nuclei mass distribution



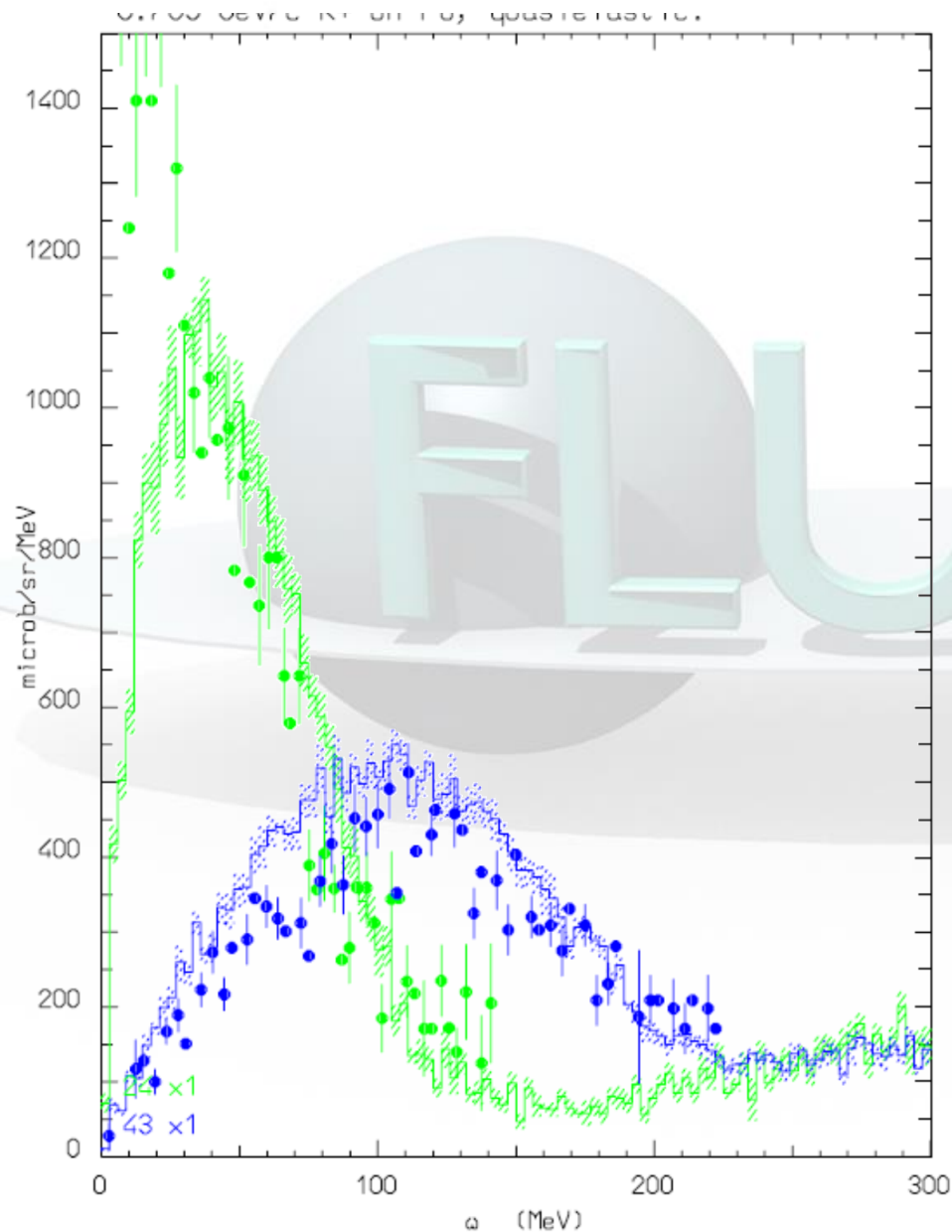
Example of Fermi distribution



Fermi momentum distribution as "seen" by interacting neutrinos on lead.

Vertical lines: maximum Fermi momentum according to un-smearred distribution

Positive kaons as a probe of Fermi motion



K^+ and K^0

- No low mass $S=1$ baryons
 - weak K^+N interaction
 - Only elastic and charge exchange up to ≈ 800 MeV/c

$K^+ Pb \rightarrow K^+ Pb$ 705 MeV/c

Residual excitation spectrum

With K^+ at 24° (green)

at 43° (blue)

Histogram : FLUKA

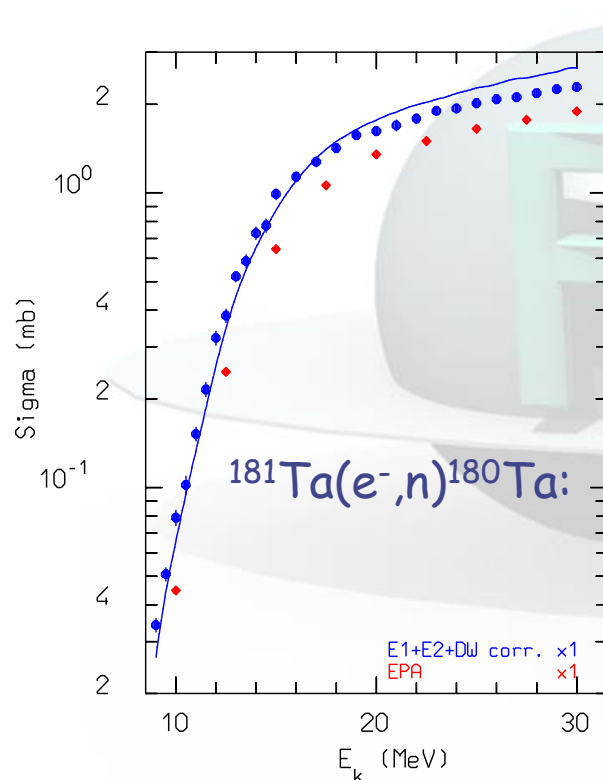
Dots : data (Phys. Rev. C51,669 (1995))

On free nucleon: recoil at 43 MeV or 117 MeV

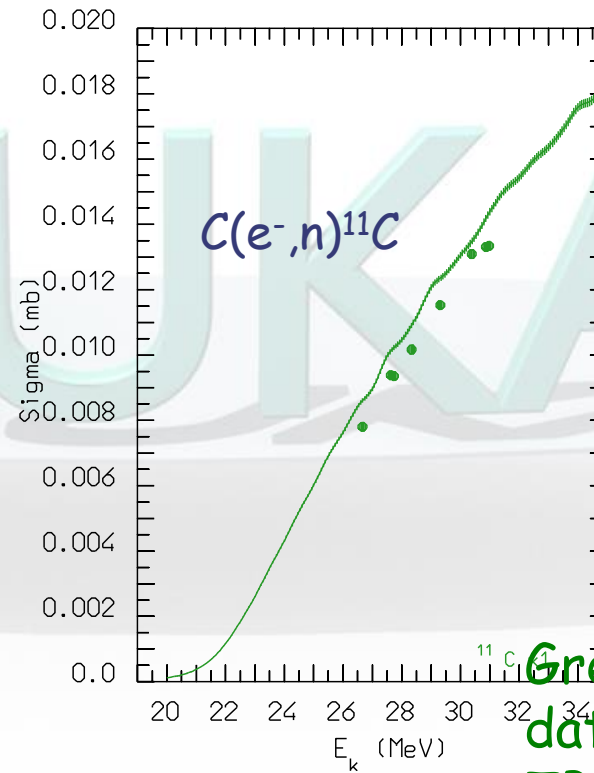
0-deg tail is elastic on nucleus, not included in sim

Electron scattering

- Quasi-Elastic on nucleon (+ all nuclear)
- Inelastic via virtual photon exchange, recently improved (E1+E2)



Blue symbols: data from JPG13,515
Blue line: FLUKA new
Red symbols: FLUKA with EPA



Green symbols:
data from
ZPA281,35
Green curve:
FLUKA

First checks with electrons

- **Quasi-Elastic scattering** of electrons on Lead, outgoing electron spectrum at 60°
- Inelastic tail not included in simulation
- To be improved with the inclusion of **energy-dependent nuclear well**, as already there for nucleon-induced reactions
- **Much more tests needed**

Data:

R.R. Whitney et al., Phys Rev C9,2230 (1974)

