

Dynamical coupled-channels approach to Resonance Region beyond $\Delta(1232)$

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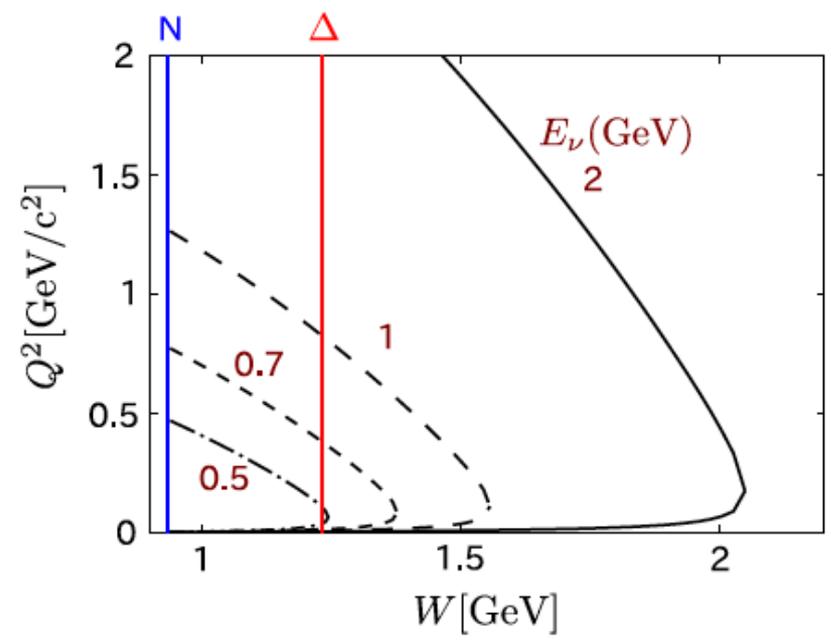
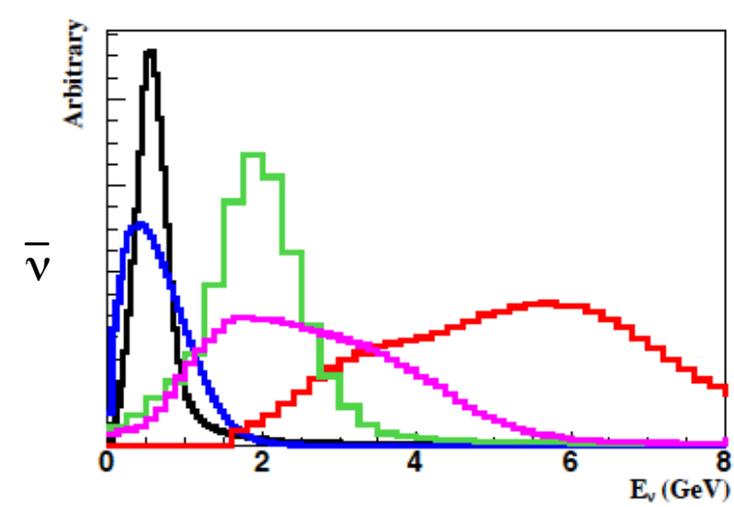
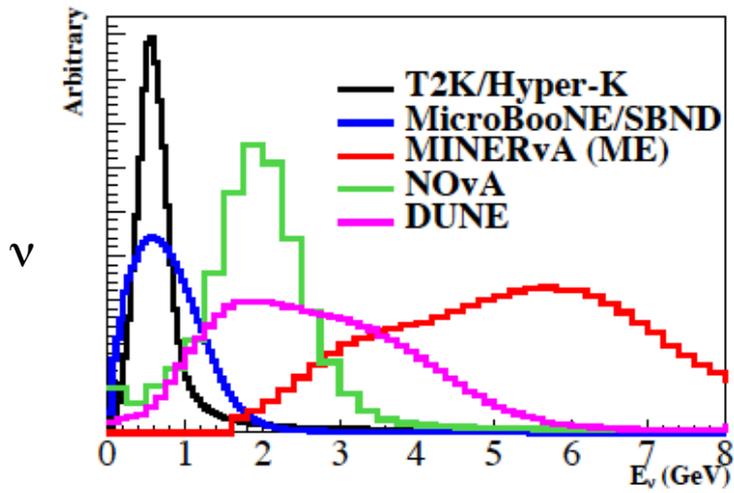
Collaborators: H. Kamano (Osaka U.), T. Sato (Osaka U.)

Introduction

Challenges in resonance region beyond $\Delta(1232)$

Neutrino interactions in resonance region beyond $\Delta(1232)$ are highly relevant to future neutrino oscillation experiments

T. Katori and M. Martini, J. Phys. G 45 (2017)



BAD NEWS ! (?)

Neutrino interactions in resonance region beyond $\Delta(1232)$
are much more difficult to understand than in $\Delta(1232)$ region

Neutrino interactions in resonance region beyond $\Delta(1232)$ is much more difficult to understand than in $\Delta(1232)$ region

$\Delta(1232)$ region

Resonance

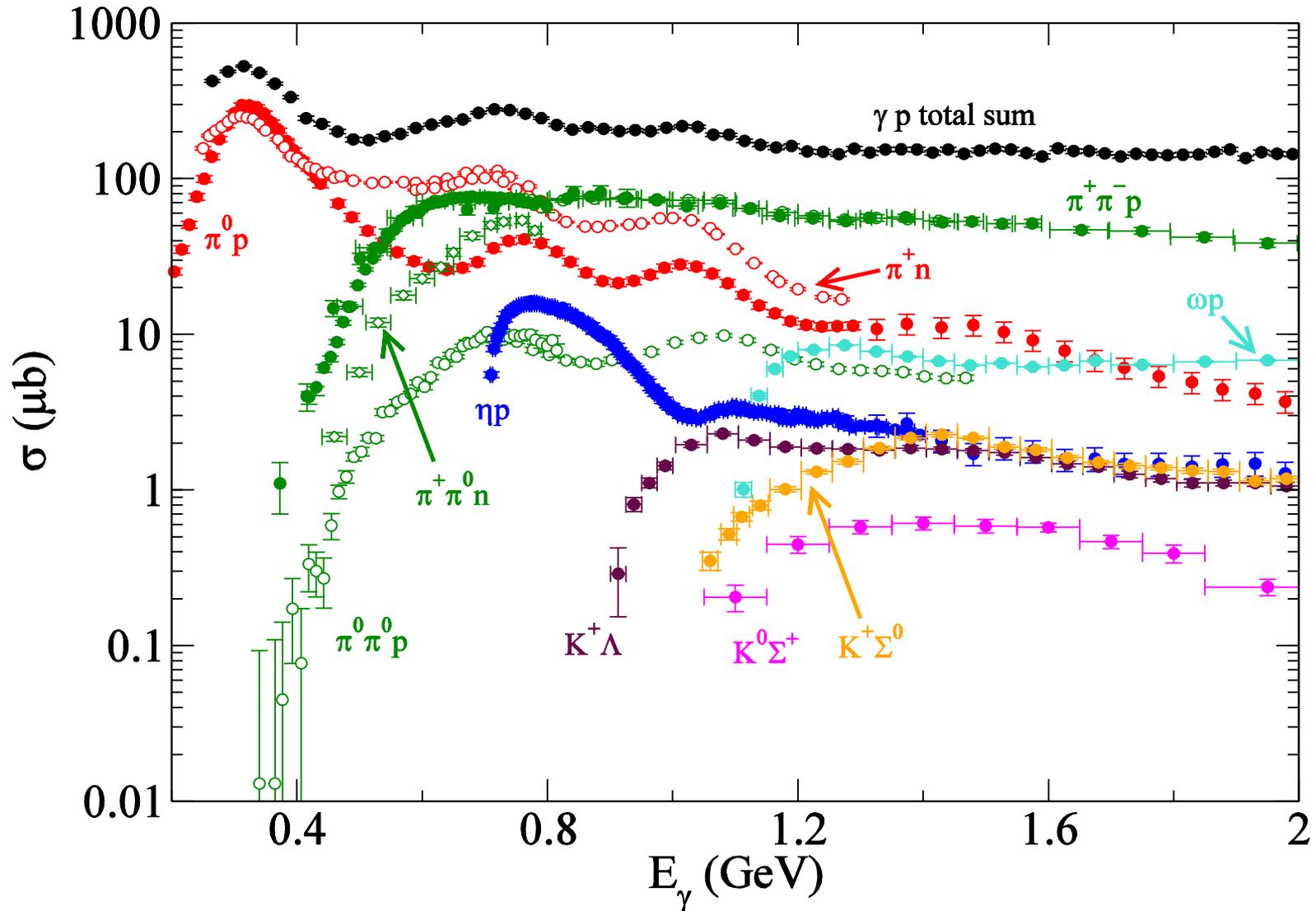
$\Delta(1232)$ dominates
No other resonances

Beyond $\Delta(1232)$ region ($W \lesssim 2$ GeV)

No single resonance dominate
Several comparable resonances overlap

Resonance region (single nucleon)

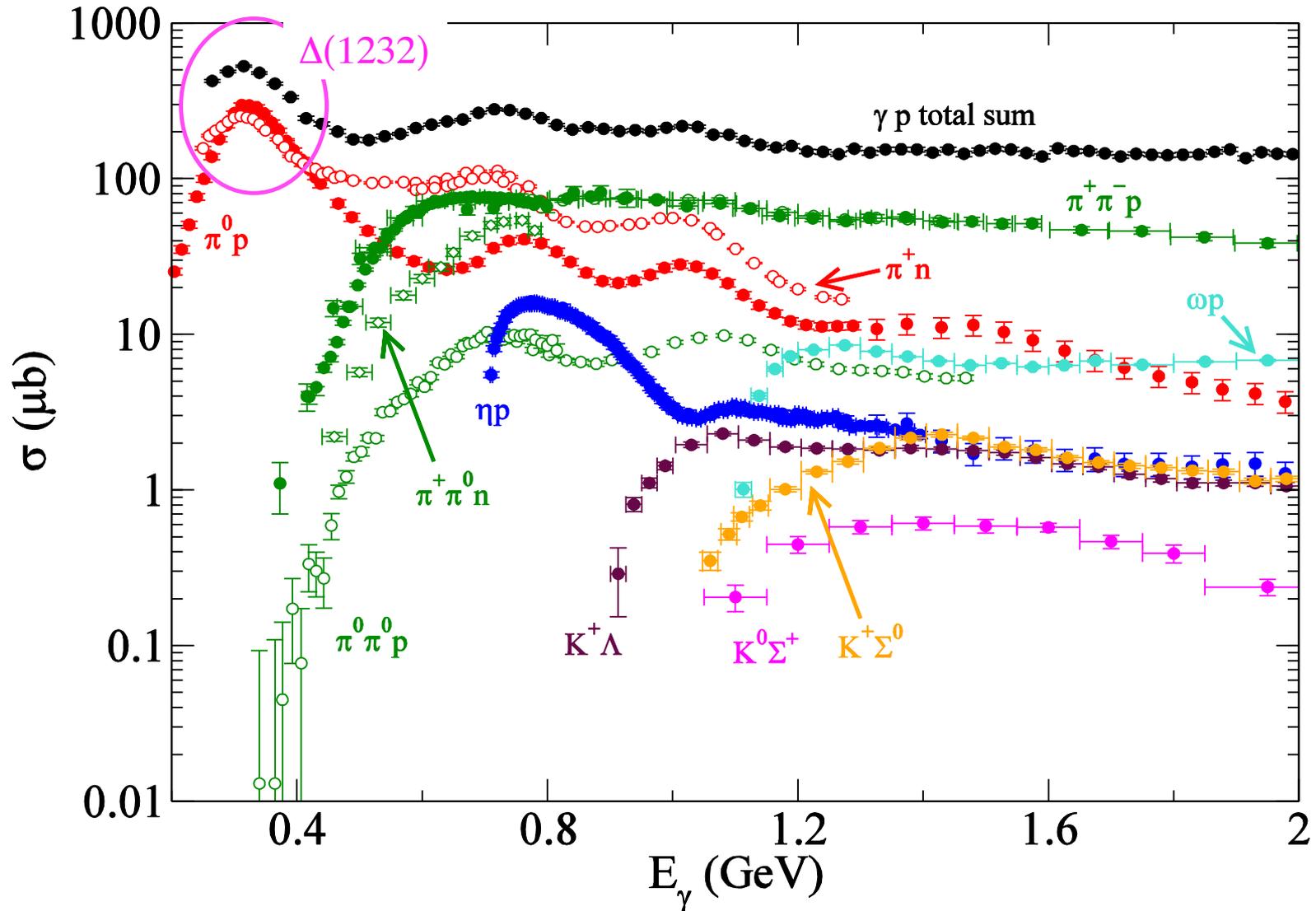
$\gamma N \rightarrow X$



Several resonances overlap to form characteristic peaks

Resonance region (single nucleon)

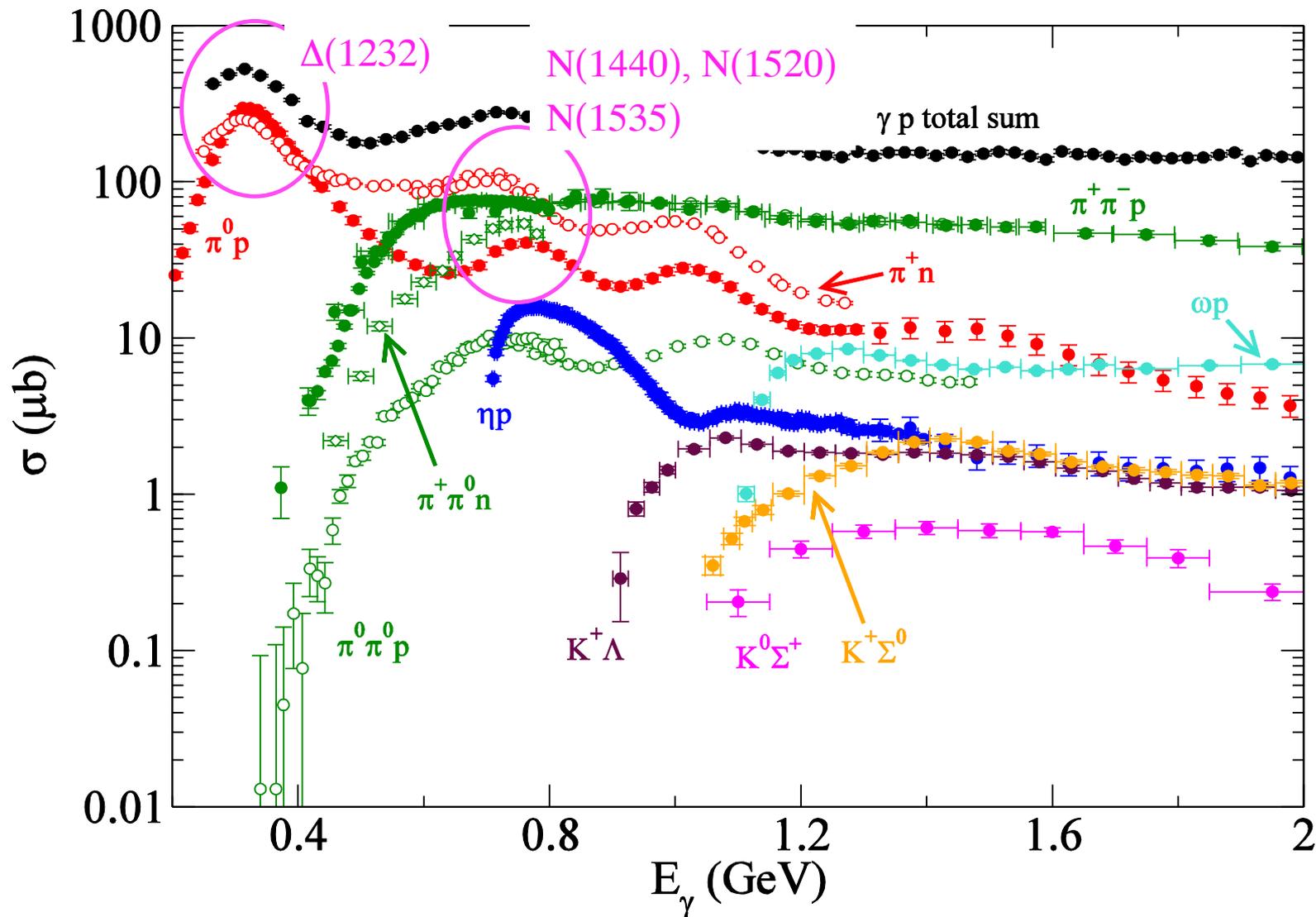
$\gamma N \rightarrow X$



Several resonances overlap to form characteristic peaks

Resonance region (single nucleon)

$\gamma N \rightarrow X$



Several resonances overlap to form characteristic peaks

Neutrino interactions in resonance region beyond $\Delta(1232)$ is much more difficult to understand than in $\Delta(1232)$ region

$\Delta(1232)$ region

Beyond $\Delta(1232)$ region ($W \lesssim 2$ GeV)

Resonance

$\Delta(1232)$ dominates
No other resonances

No single resonance dominate
Several comparable resonances overlap

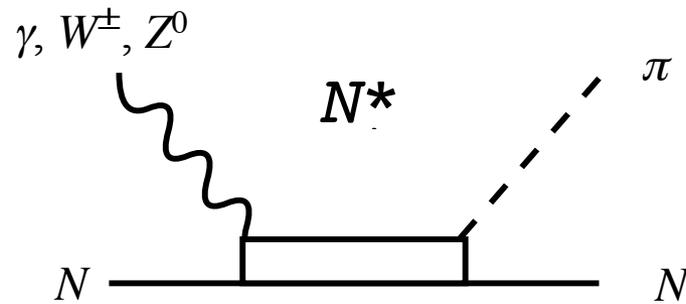
Non-resonant

Much smaller than $\Delta(1232)$
ChPT works \rightarrow well-controlled

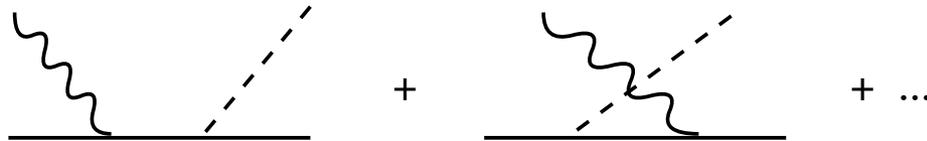
Comparable to resonant contributions
ChPT not work

Resonance region

(Main) reaction mechanism : resonance excitations



(Sub-leading) non-resonant mechanisms



Neutrino interactions in resonance region beyond $\Delta(1232)$ is much more difficult to understand than in $\Delta(1232)$ region

$\Delta(1232)$ region

Beyond $\Delta(1232)$ region ($W \lesssim 2$ GeV)

Resonance

$\Delta(1232)$ dominates
No other resonances

No single resonance dominate
Several comparable resonances overlap

Non-resonant

Much smaller than $\Delta(1232)$
ChPT works \rightarrow well-controlled

Comparable to resonant contributions
ChPT not work

Relative phases
among mechanisms

(fairly) well-controlled

Crucially important but not easy to control

Coupled-channels

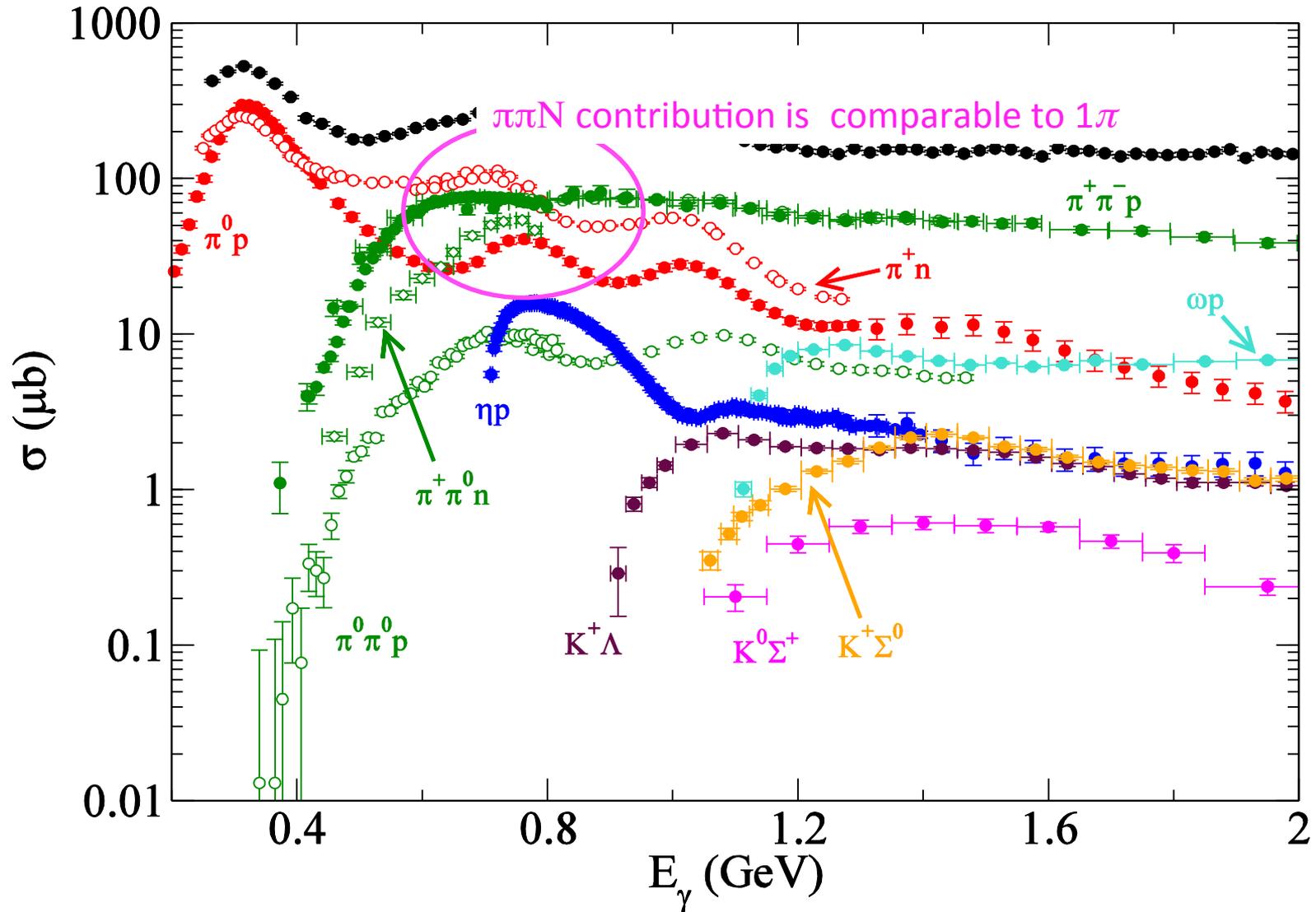
Only πN

πN and $\pi\pi N$ are comparable
and strongly coupled

ηN , $K\Lambda$, $K\Sigma$ channels are also coupled

Resonance region (single nucleon)

$\gamma N \rightarrow X$



Strategy to tackle neutrino reactions beyond $\Delta(1232)$

Vector current

1. EM couplings and Q^2 -dependence \leftarrow Analysis of electron-induced reaction data
(1π production and inclusive)
2. Isospin separation : $V_{CC} = V_{\text{isovector}} = V_{\text{proton}}^{\text{EM}} - V_{\text{neutron}}^{\text{EM}}$

Both proton- and neutron-target electron data need to be analyzed

Strategy to tackle neutrino reactions beyond $\Delta(1232)$

Axial current

Useful data are not available to determine axial current in this kinematical region

→ Guiding principle to derive the axial current : **PCAC relation** with πN reaction amplitude

$$\langle X | q \cdot A(Q^2 \sim 0) | N \rangle \sim i f_\pi \langle X | T | \pi N \rangle$$

Through a model $g_{AN \rightarrow N^*}(Q^2 \sim 0) \propto g_{\pi N \rightarrow N^*}$ for a dominant axial form factor

If $g_{\pi N \rightarrow N^*}$ is available (including its phase), $g_{AN \rightarrow N^*}(Q^2 \sim 0)$ is obtained (including its phase)

Both $\pi N \rightarrow \pi N$ and $AN \rightarrow \pi N$ reaction models need to be developed consistently with PCAC

Common procedure : $\Gamma(N^* \rightarrow \pi N)$ from PDG $\rightarrow g_{AN \rightarrow N^*}(Q^2 \sim 0) \propto |g_{\pi N \rightarrow N^*}|$

No information about phase is available

Axial current for $Q^2 \neq 0$

To determine axial form factors (Q^2 -dependence), we need

neutrino data or parity-violating electron scattering data

No useful data is available beyond $\Delta(1232)$ region to determine Q^2 -dependence

→ we need to assume it, dipole form is often used

$F_A(Q^2)$: axial form factors

non-resonant mechanisms $F_A(Q^2) = \left(\frac{1}{1 + Q^2 / M_A^2} \right)^2$ $M_A = 1.02 \text{ GeV}$

resonant mechanisms $F_A(Q^2) = \left(\frac{1}{1 + Q^2 / M_A^2} \right)^2$

Dynamical coupled-channels approach in and beyond $\Delta(1232)$ region

- ✓ Both proton- and neutron-target electron data need to be analyzed
- ✓ Both $\pi N \rightarrow \pi N$ and $AN \rightarrow \pi N$ reaction models developed consistently with PCAC
- ✓ Channel-couplings among πN , $\pi\pi N$, ηN , $K\Lambda$, $K\Sigma$ required by unitarity

Dynamical Coupled-Channels model
for meson productions
in and beyond $\Delta(1232)$ region

DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

Kamano et al., PRC **88**, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation for meson-baryon scattering

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$$\{a, b, c\} = \pi N, \eta N, \pi\pi N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma$$

By solving the LS equation, coupled-channel unitarity is fully taken into account

DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

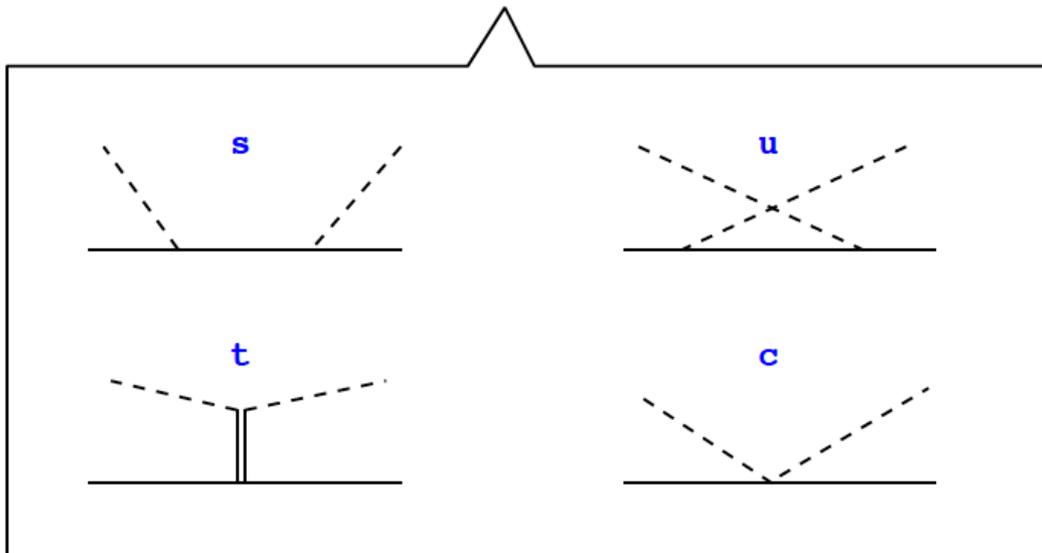
Kamano et al., PRC 88, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation for meson-baryon scattering

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$$\mathbf{V}_{ab} = \text{[diagram 1]} + \text{[diagram 2]}$$

The diagram shows the vertex \mathbf{V}_{ab} as the sum of two terms. The first term is a vertex with a solid horizontal line below and two dashed lines above meeting at a central black dot. The second term is a vertex with a solid horizontal line below, a rectangular box on the line, and two dashed lines above meeting at a central point. The text "bare N*" is written above the second diagram.



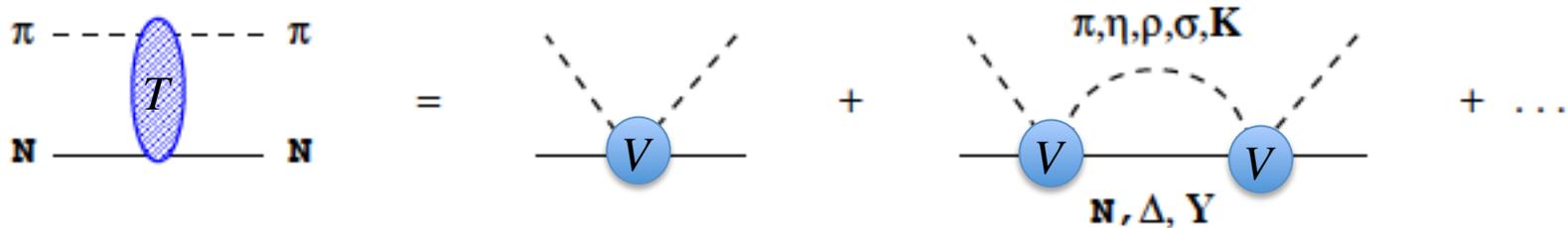
DCC (Dynamical Coupled-Channel) model

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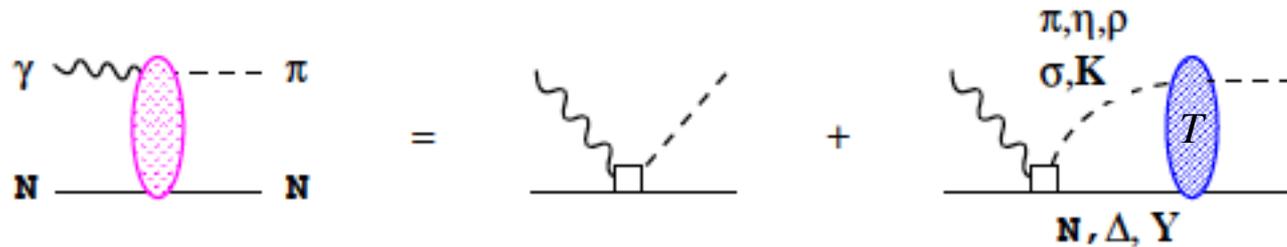
Kamano et al., PRC **88**, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation for meson-baryon scattering

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$



In addition, γN , $W^\pm N$, ZN channels are included perturbatively



DCC analysis of $\gamma N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$

and electron scattering data

DCC analysis of meson production data

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

Fully combined analysis of $\gamma N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$ data

$d\sigma / d\Omega$ and polarization observables ($W \leq 2.1$ GeV)

~ 27,000 data points are fitted

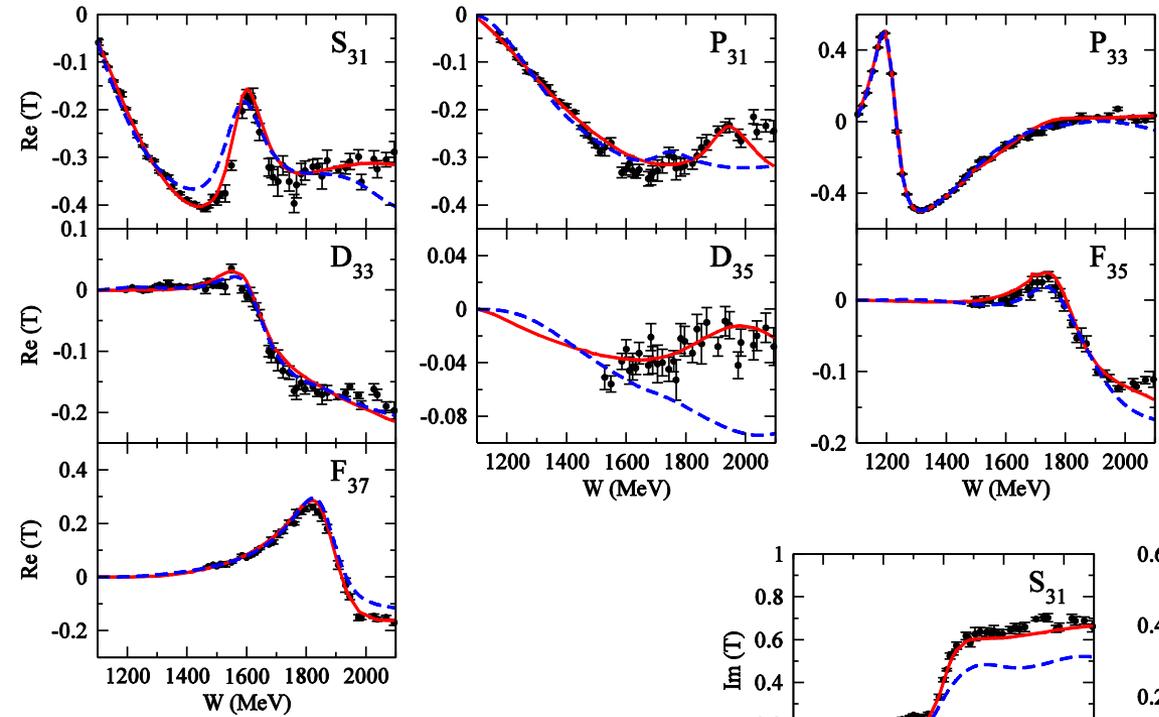
by adjusting parameters (N^* mass, $N^* \rightarrow MB$ couplings, cutoffs)



Data for electron scattering on proton and neutron are analyzed by adjusting

$\gamma^* N \rightarrow N^*$ coupling strength at different Q^2 values ($Q^2 \leq 3$ (GeV/c)²)

Partial wave amplitudes of πN scattering



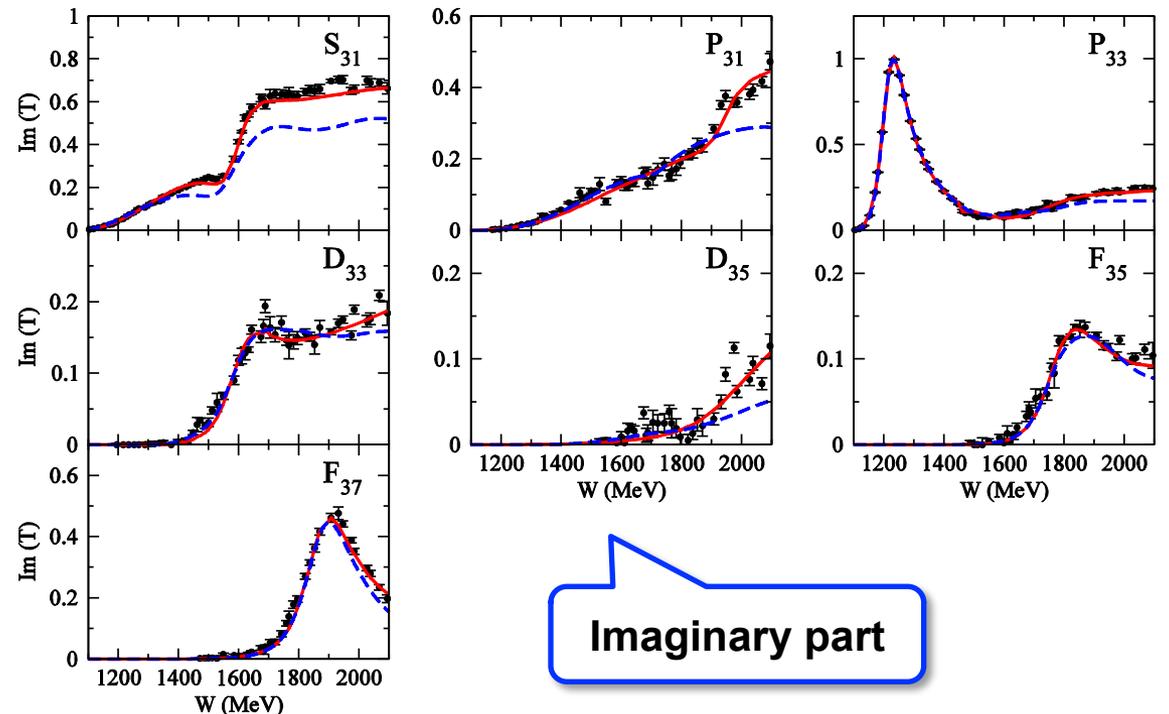
Real part

$$I = \frac{3}{2}$$

— Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

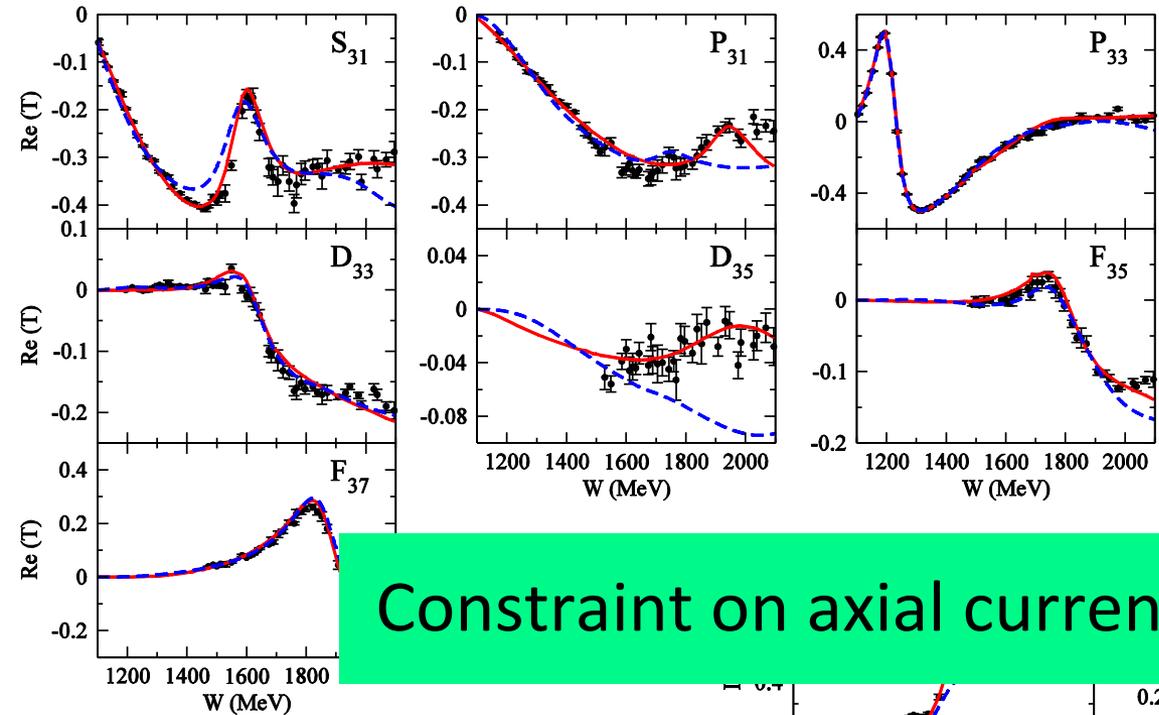
- - - Previous model (fitted to $\pi N \rightarrow \pi N$ data only) [PRC76 065201 (2007)]

Data: SAID πN amplitude



Imaginary part

Partial wave amplitudes of πN scattering



Real part

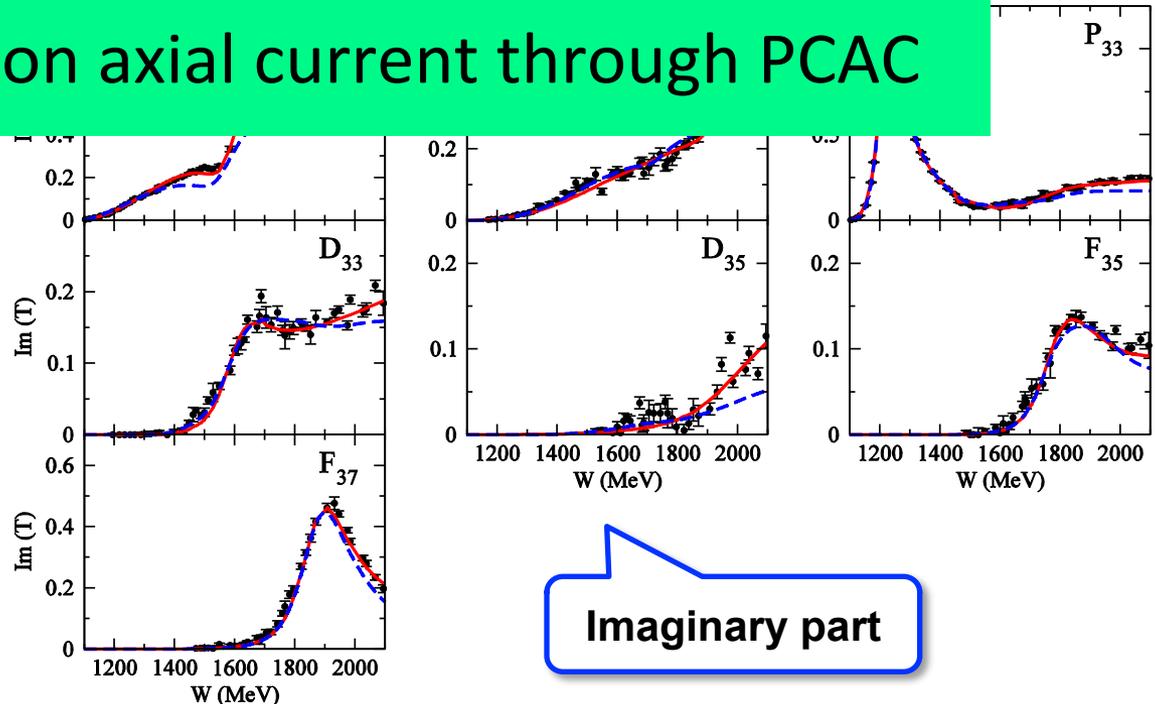
$$I = \frac{3}{2}$$

Constraint on axial current through PCAC

— Kamano, Nakamura, Lee, Sato,
PRC 88 (2013)

- - - Previous model
(fitted to $\pi N \rightarrow \pi N$ data only)
[PRC76 065201 (2007)]

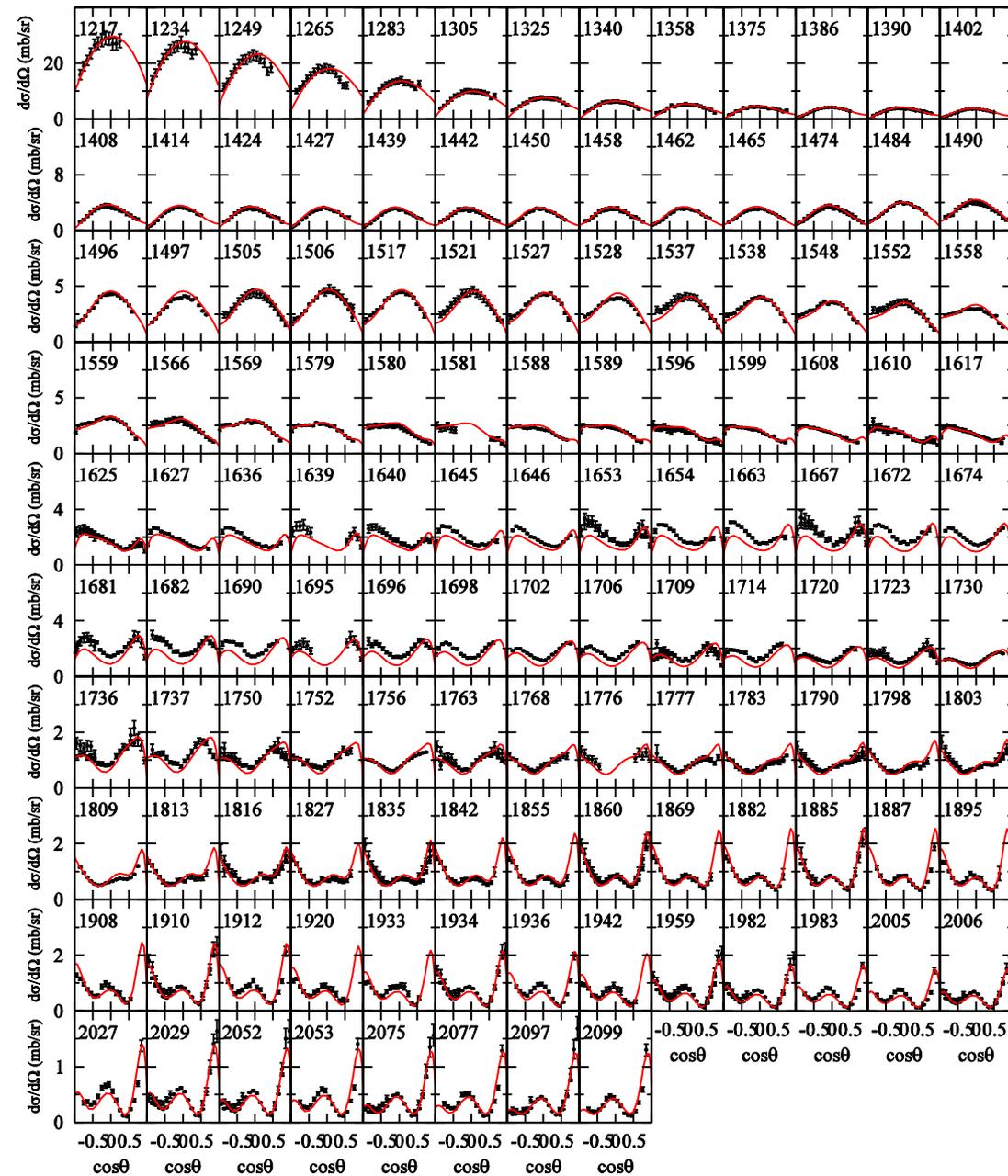
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Imaginary part

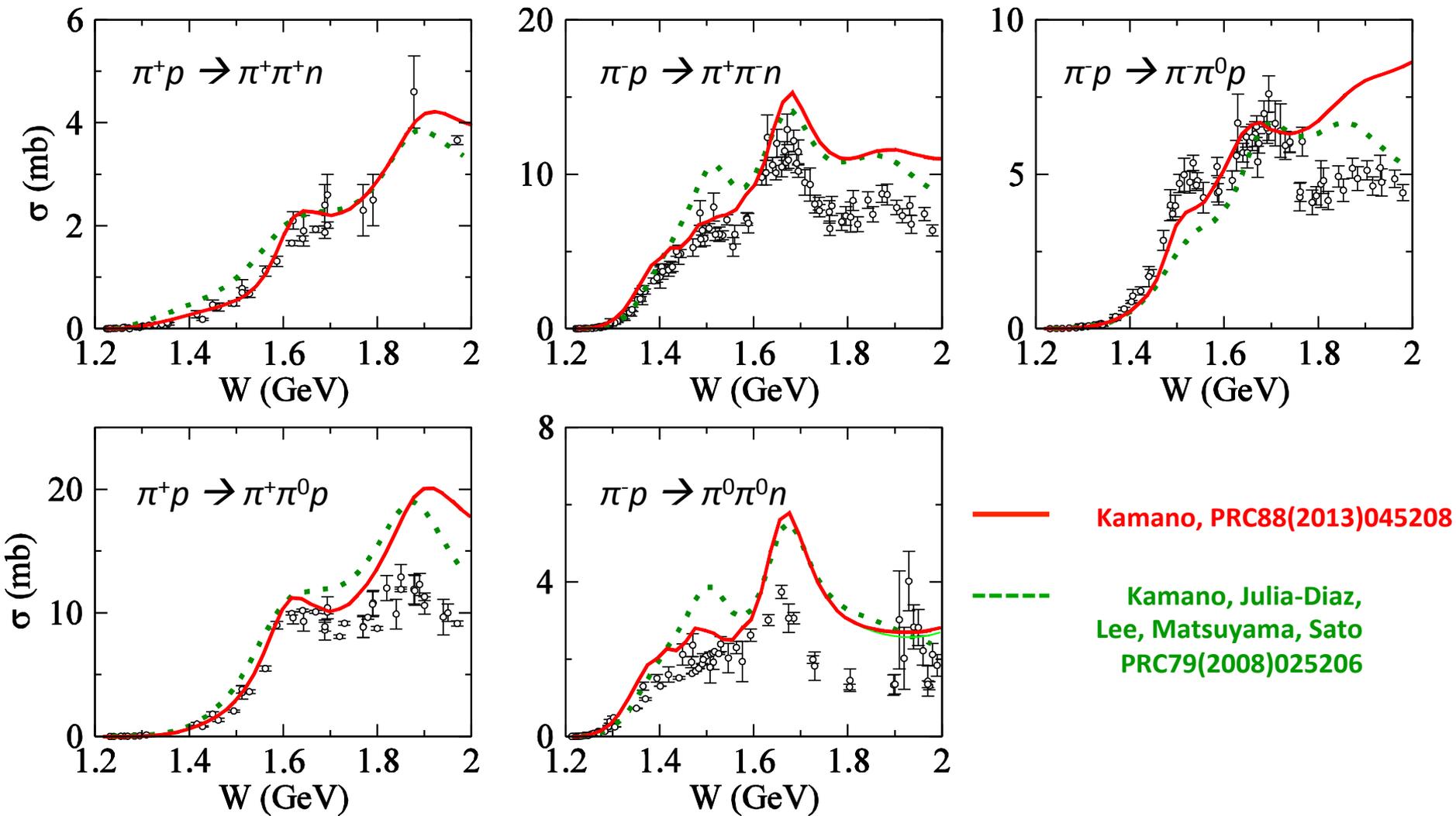
$\gamma p \rightarrow \pi^0 p$ $d\sigma/d\Omega$ for $W < 2.1$ GeV

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

Vector current ($Q^2=0$) for 1π

Production is well-tested by data

Predicted $\pi N \rightarrow \pi\pi N$ total cross sections with our DCC model



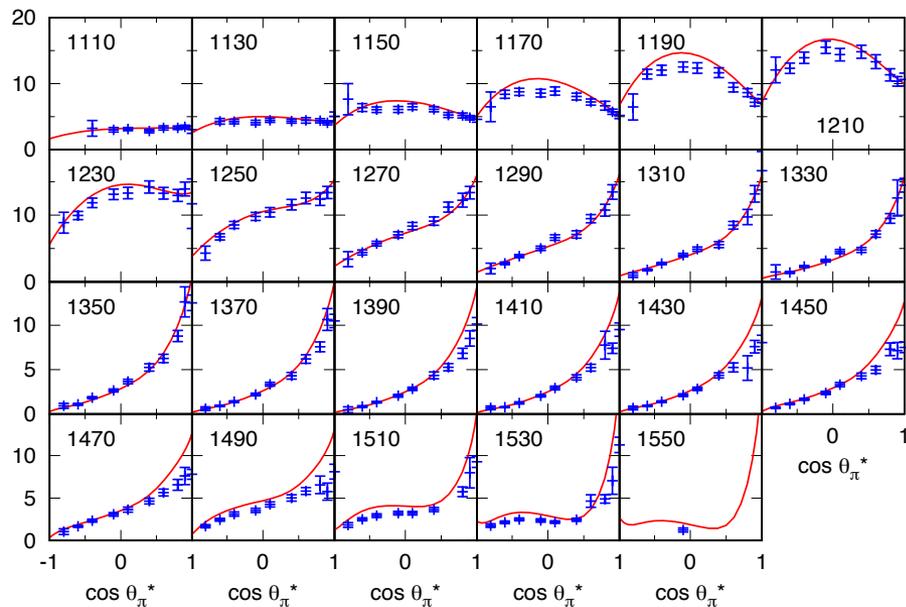
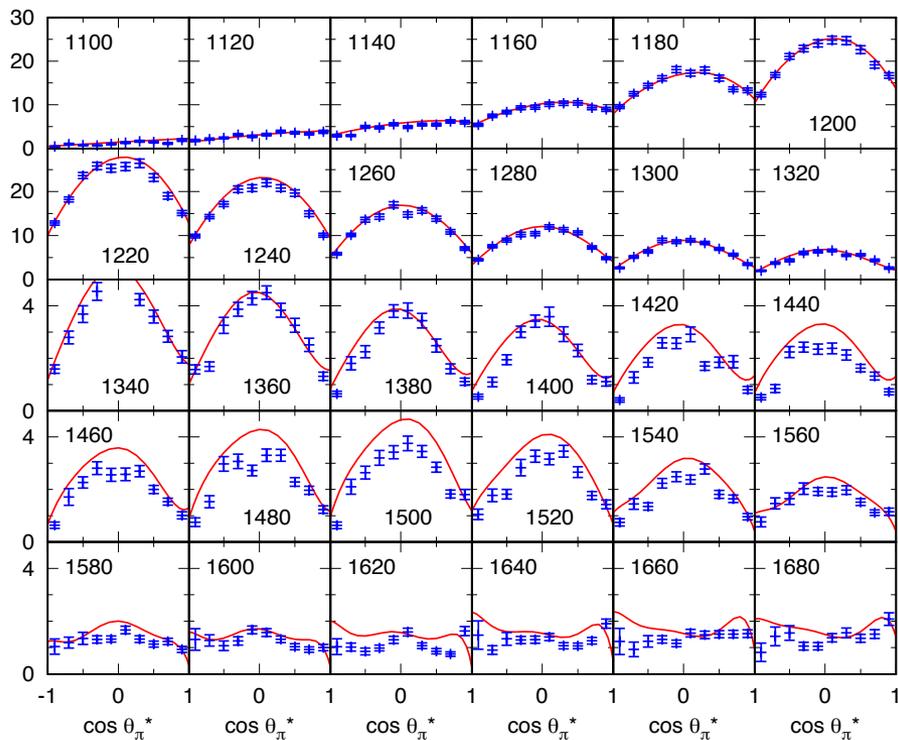
Single π production in electron-proton scattering

Purpose : Determine Q^2 -dependence of vector coupling of $p-N^*$: $VpN^*(Q^2)$

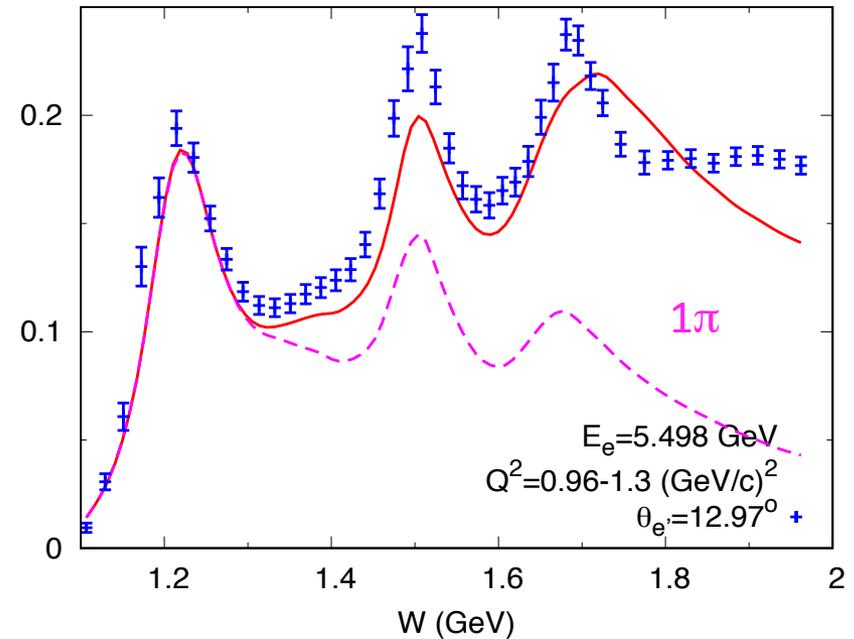
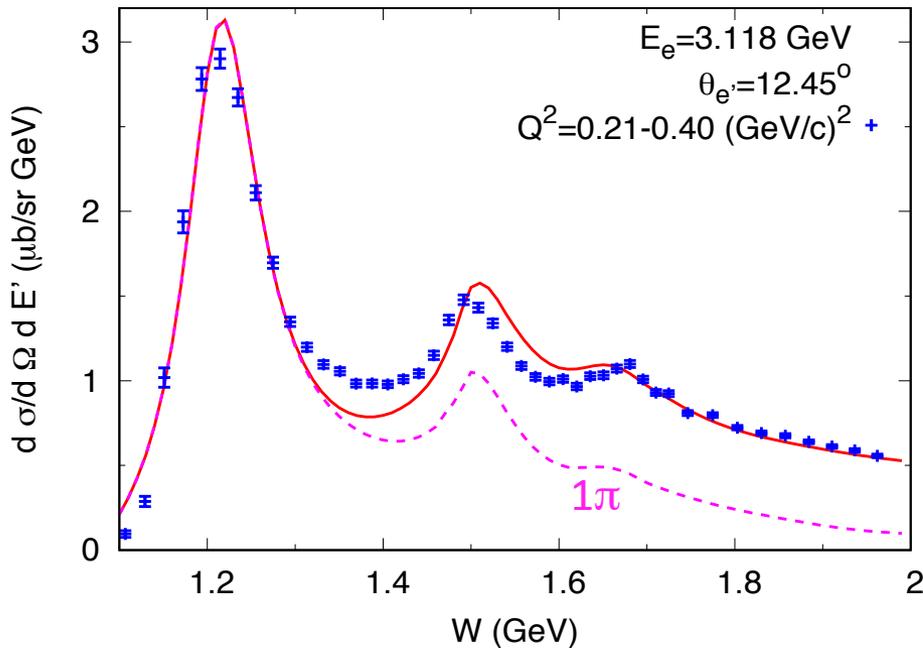
$\sigma_T + \varepsilon \sigma_L$ for $Q^2=0.40$ (GeV/c)² and $W=1.1 - 1.68$ GeV

$p(e, e' \pi^0) p$

$p(e, e' \pi^+) n$



Inclusive electron-proton scattering



Data: JLab E00-002 (preliminary)

- Reasonable fit to data for application to neutrino interactions
- Important 2π contributions for high W region

Similar analysis of **electron-neutron scattering** data has also been done

DCC vector currents has been tested by data for whole kinematical region

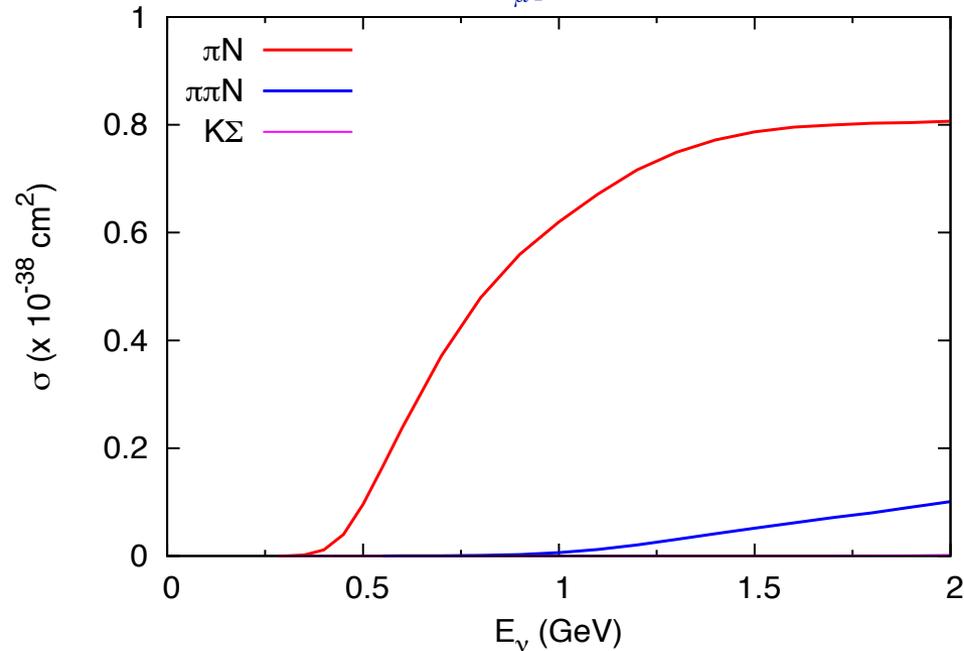
relevant to neutrino interactions of $E_\nu \leq 2$ GeV

Neutrino Results

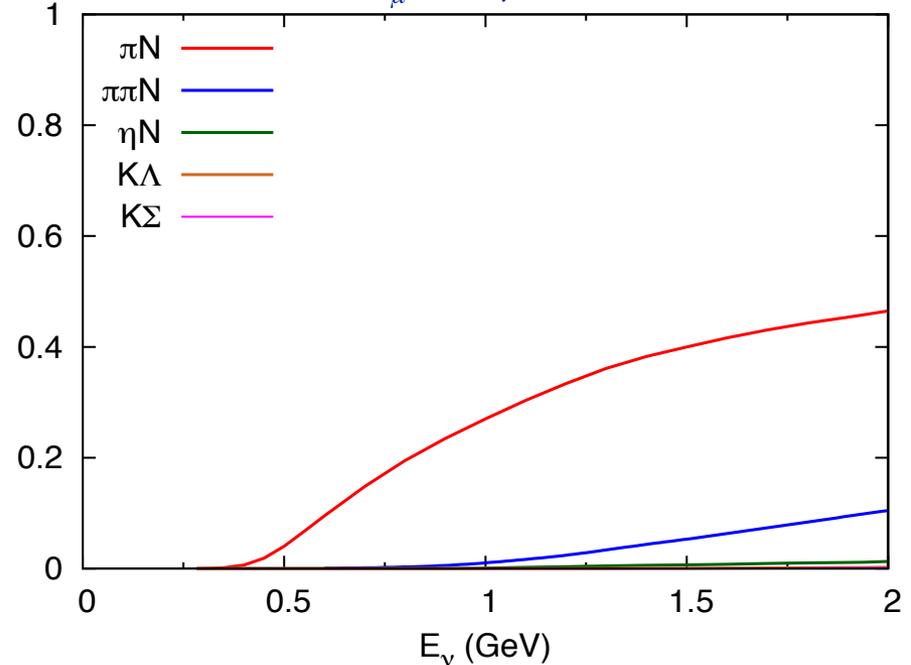
SXN et al., Phys. Rev. D **92**, 074024 (2015)

Cross section for $\nu_\mu N \rightarrow \mu^- X$

$\nu_\mu p \rightarrow \mu^- X$

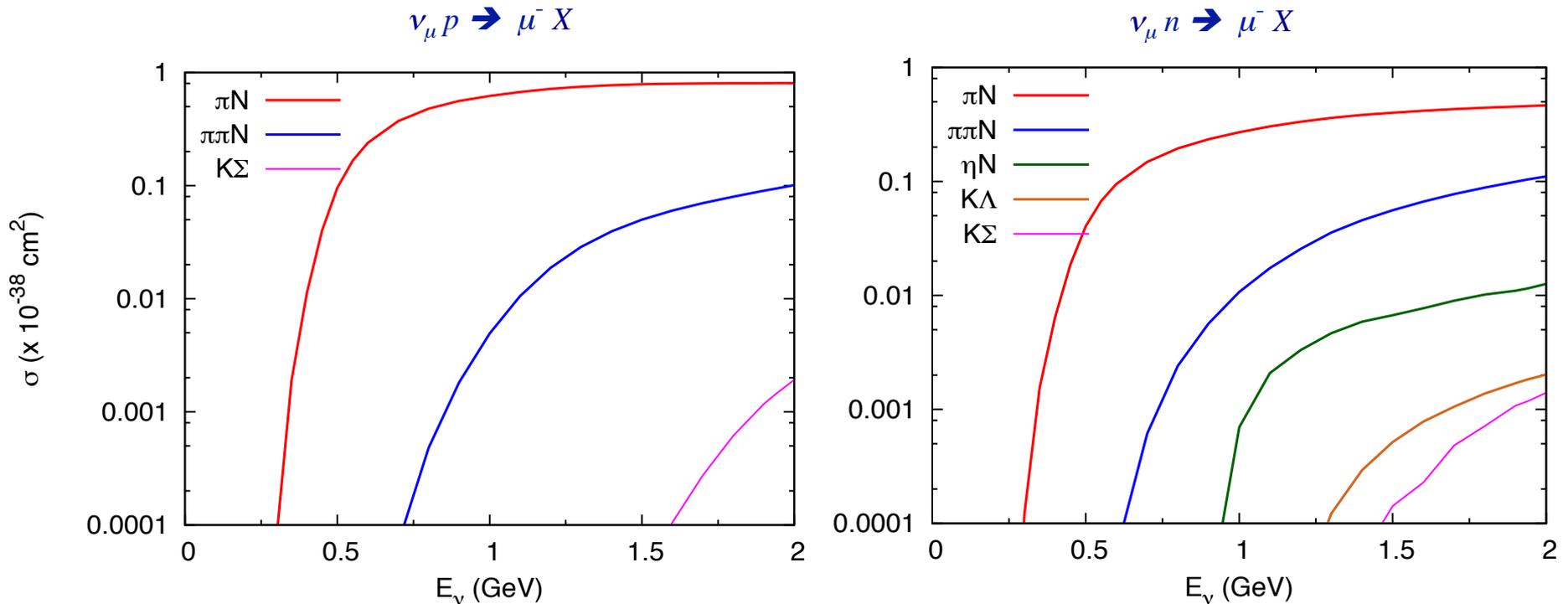


$\nu_\mu n \rightarrow \mu^- X$



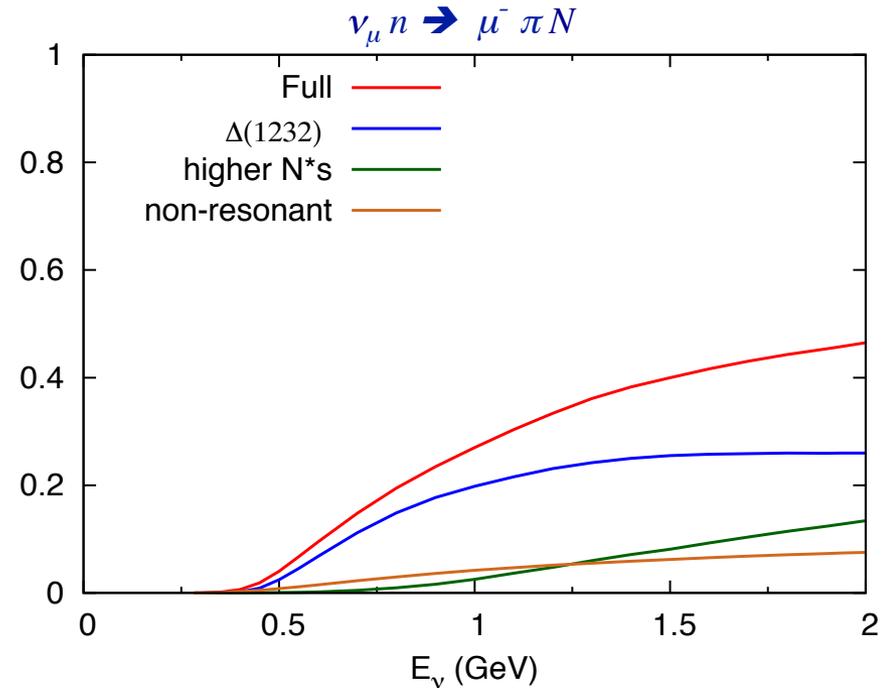
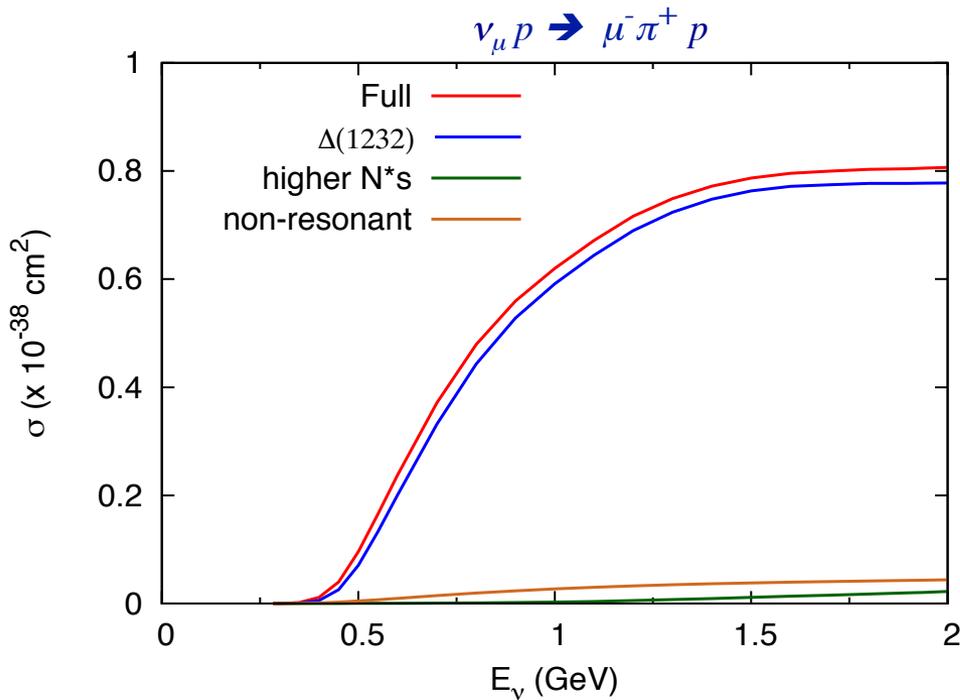
- πN & $\pi\pi N$ are main channels in few-GeV region
- DCC model gives predictions for **all final states**
- ηN , KY cross sections are $10^{-1} - 10^{-2}$ smaller

Cross section for $\nu_\mu N \rightarrow \mu^- X$



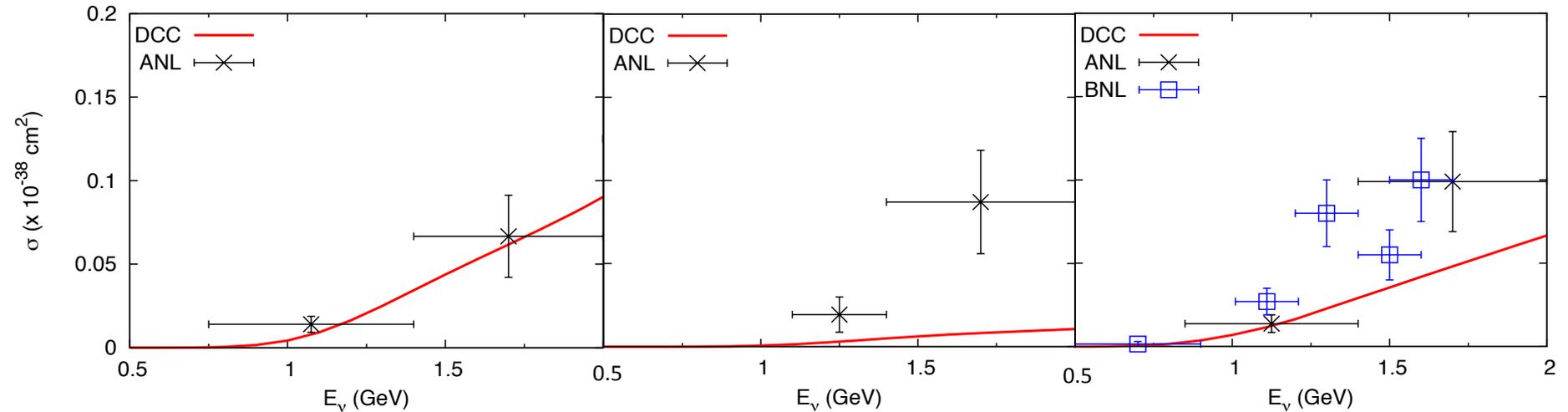
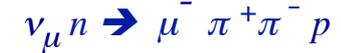
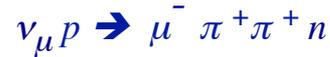
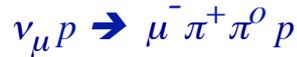
- πN & $\pi\pi N$ are main channels in few-GeV region
- DCC model gives predictions for **all final states**
- ηN , KY cross sections are $10^{-1} - 10^{-2}$ smaller

Mechanisms for $\nu_\mu N \rightarrow \mu^- \pi N$



- $\Delta(1232)$ dominates for $\nu_\mu p \rightarrow \mu^- \pi^+ p$ ($I=3/2$) for $E_\nu \leq 2$ GeV
- Non-resonant mechanisms contribute significantly
- Higher N^* s becomes important towards $E_\nu \approx 2$ GeV for $\nu_\mu n \rightarrow \mu^- \pi N$

Comparison with double pion data



Fairly good DCC predication

ANL Data : PRD **28**, 2714 (1983)

BNL Data : PRD **34**, 2554 (1986)

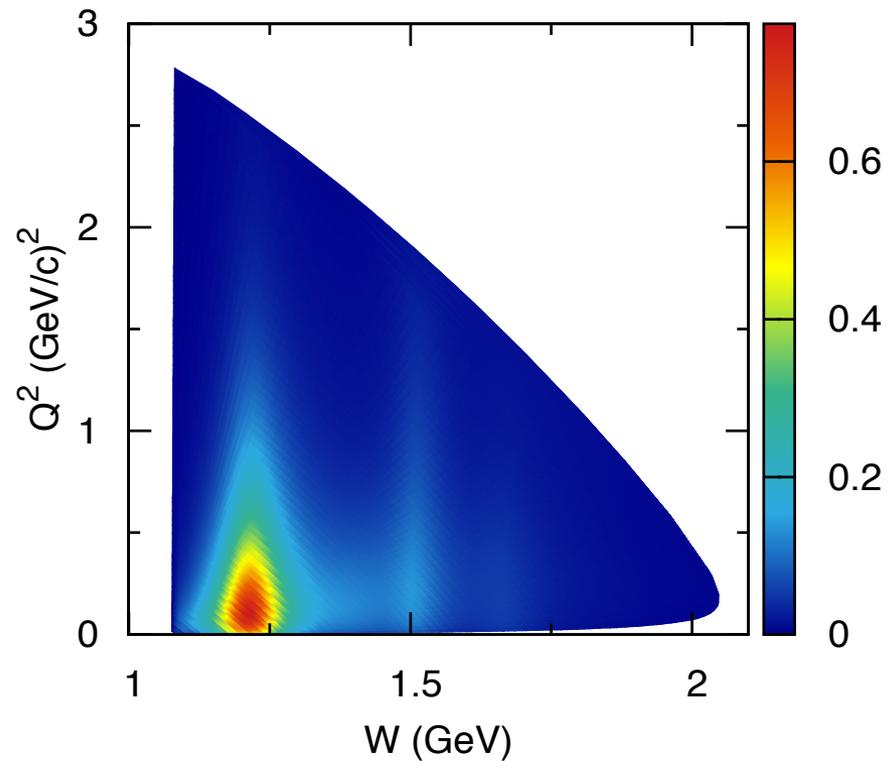
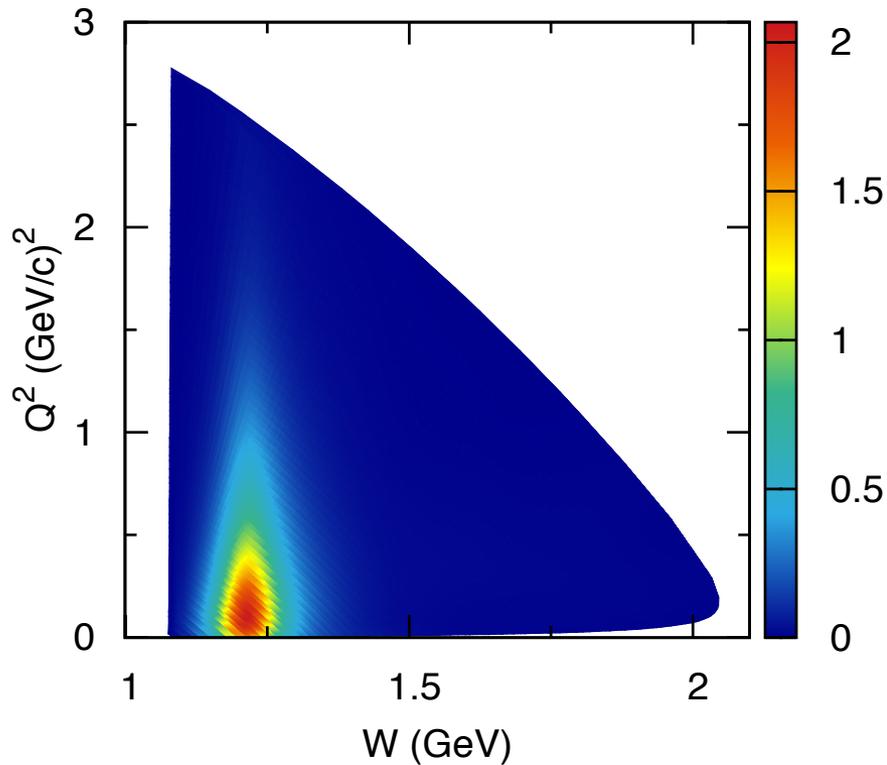
First dynamical model for 2 π production in resonance region

$$d\sigma / dW dQ^2 \quad (\times 10^{-38} \text{ cm}^2 / \text{ GeV}^2)$$

$$E_\nu = 2 \text{ GeV}$$

$$\nu_\mu p \rightarrow \mu^- \pi^+ p$$

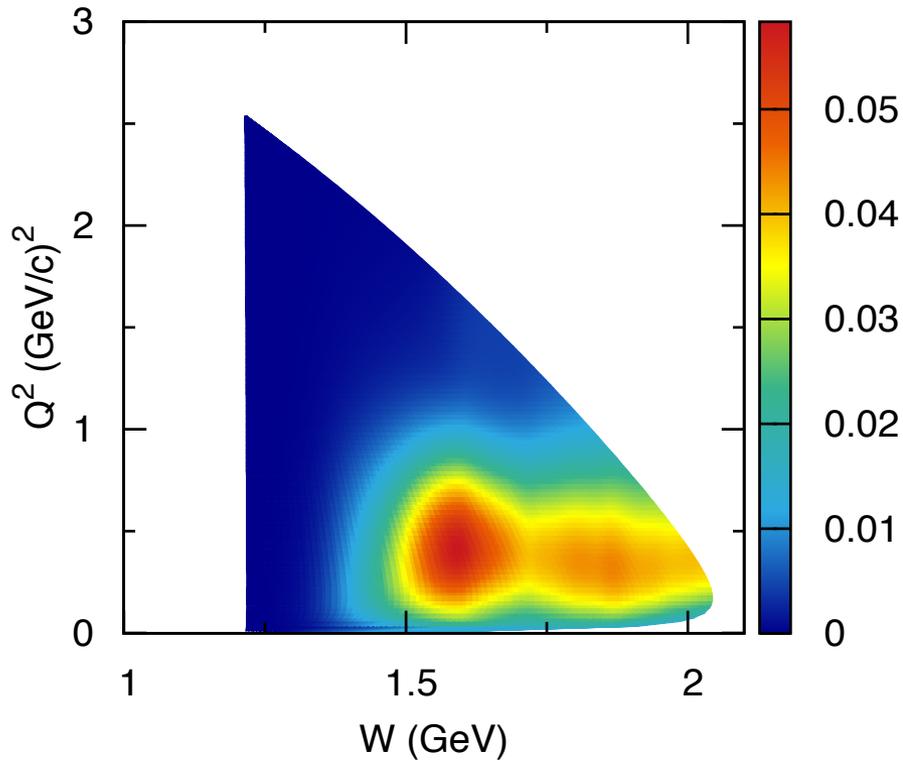
$$\nu_\mu n \rightarrow \mu^- \pi N$$



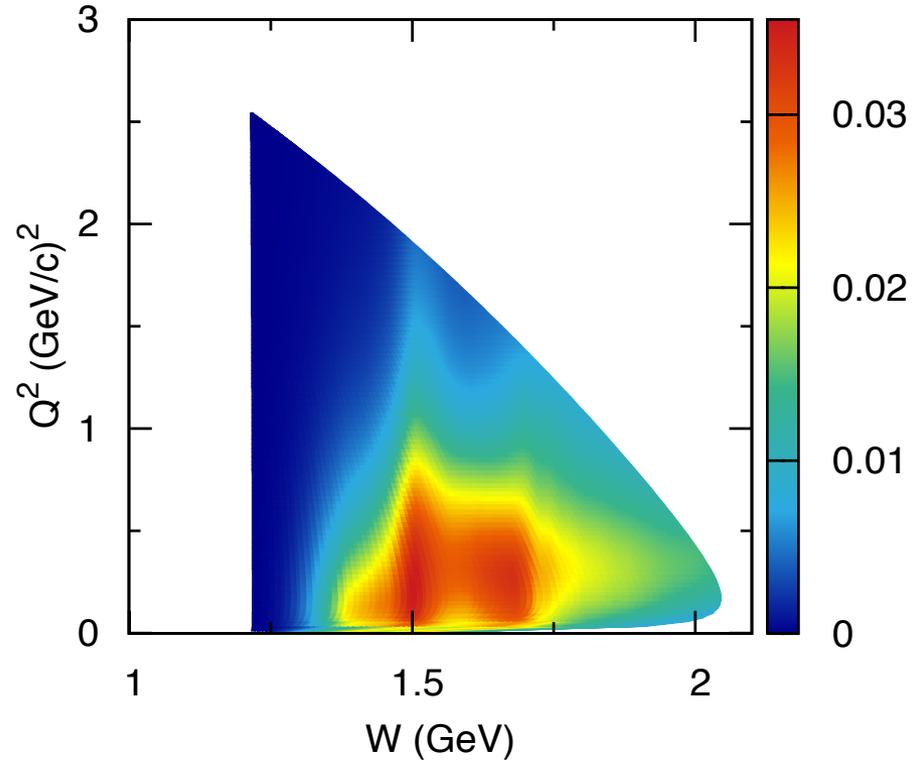
$$d\sigma / dW dQ^2 \quad (\times 10^{-38} \text{ cm}^2 / \text{GeV}^2)$$

$$E_\nu = 2 \text{ GeV}$$

$$\nu_\mu p \rightarrow \mu^- \pi^+ \pi^0 p$$



$$\nu_\mu n \rightarrow \mu^- \pi^+ \pi^- p$$

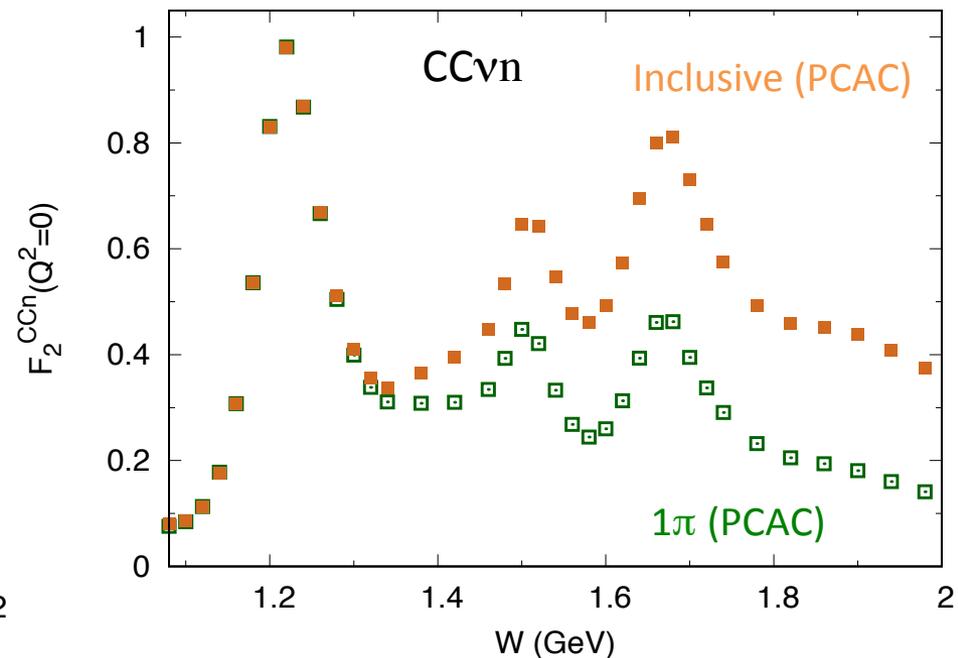
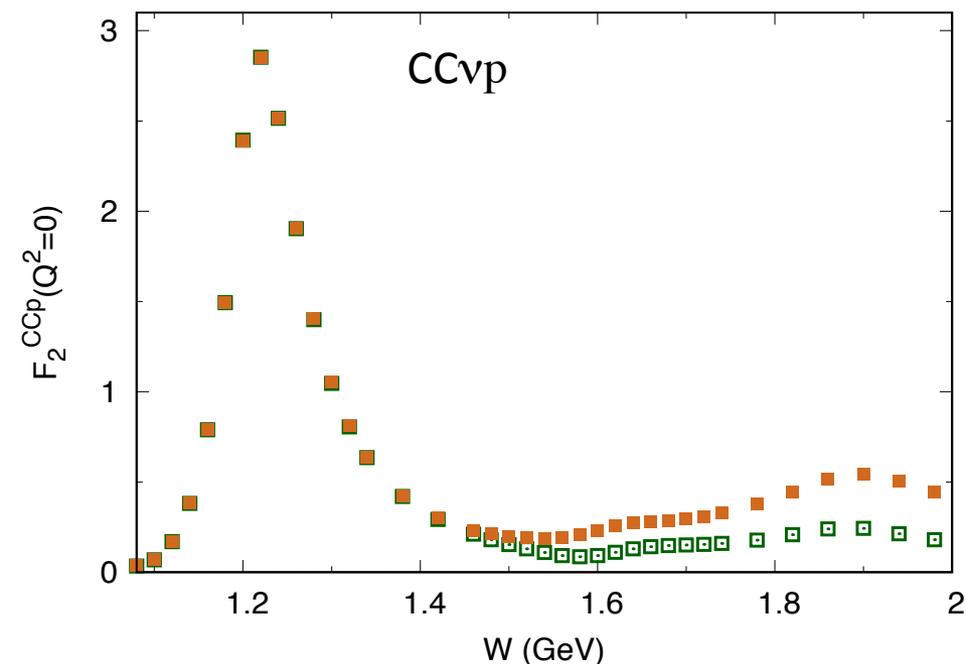


Neutrino-nucleon cross section at $Q^2=0$ ($m_\mu=0$)

$$\frac{d\sigma^{CC}}{dE_l d\Omega_l} = \frac{G_F^2 V_{ud}^2}{2\pi^2} \frac{E'^2}{E - E'} F_2,$$

PCAC

$$F_2 = \frac{2f_\pi^2}{\pi} \sigma_{tot}(\pi + N)$$



So far in this workshop, no model for resonance region beyond $\Delta(1232)$ has not been validated by neutrino-nucleon data \leftarrow ANL and BNL data are not very sensitive to this energy region

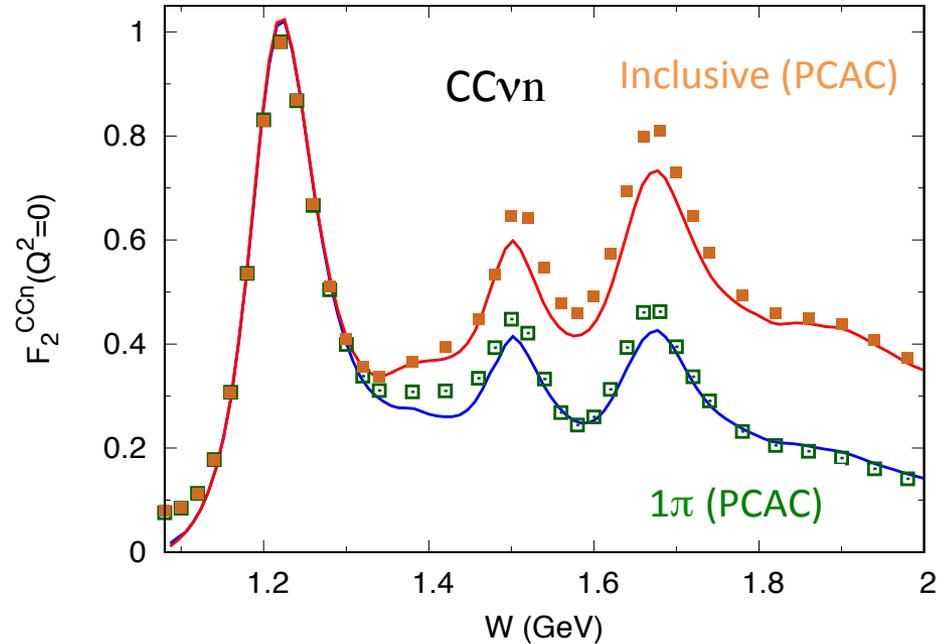
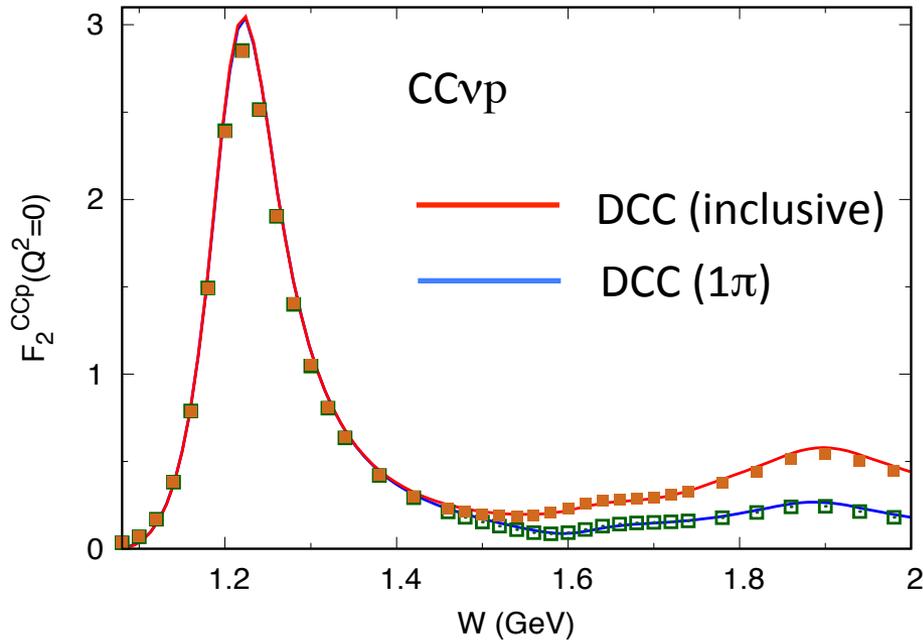
Suggestion: Validate all models for resonance region beyond $\Delta(1232)$ with this useful “data”

Cross section at $Q^2=0$ and $m_\mu=0$

$$\frac{d\sigma^{CC}}{dE_l d\Omega_l} = \frac{G_F^2 V_{ud}^2}{2\pi^2} \frac{E'^2}{E - E'} F_2,$$

PCAC

$$F_2 = \frac{2f_\pi^2}{\pi} \sigma_{tot}(\pi + N)$$



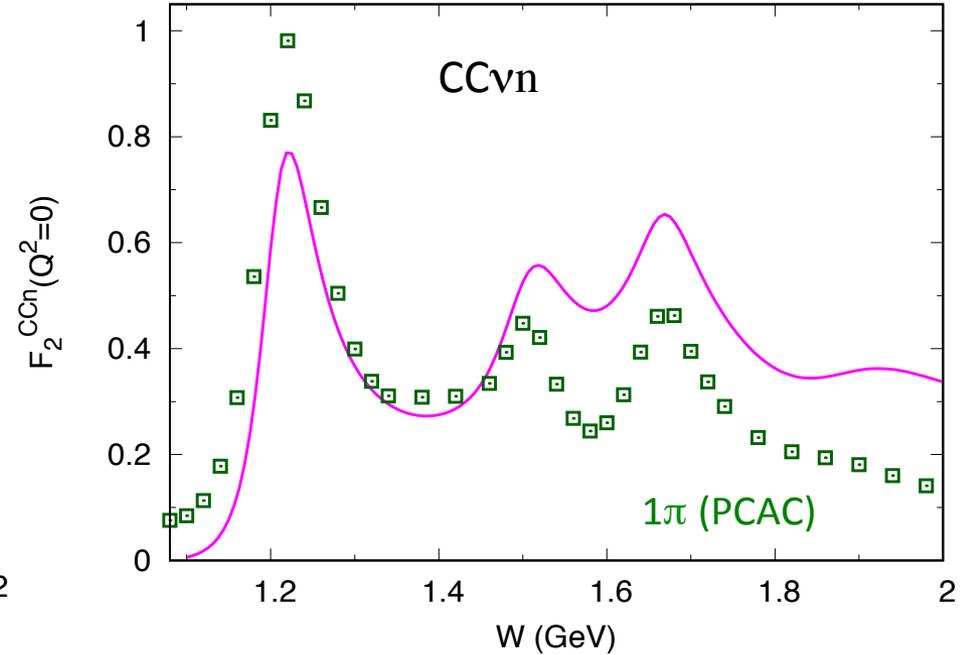
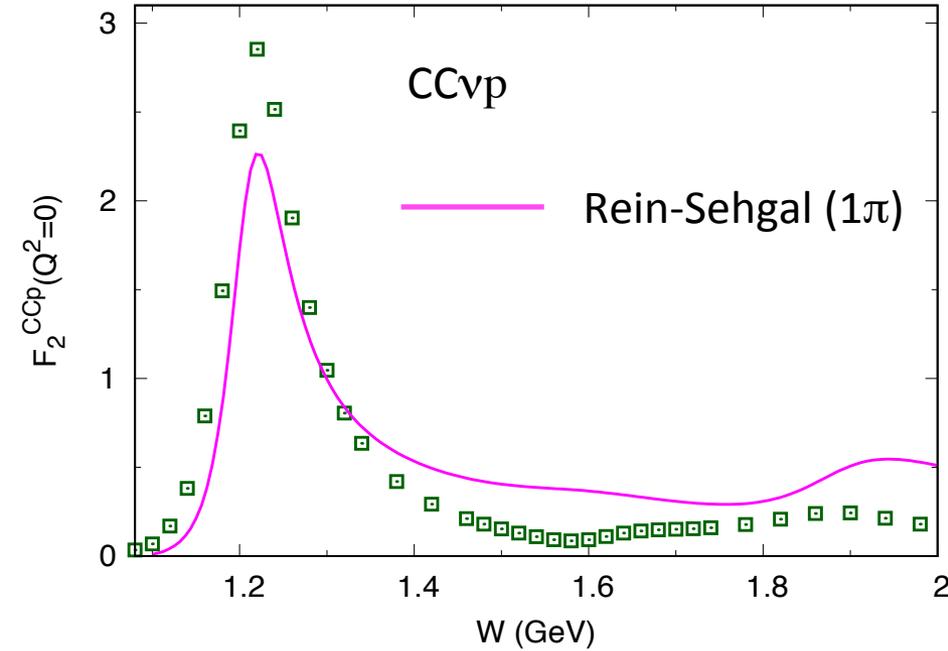
- $F_2(Q^2=0)$ from DCC model agrees with PCAC values ($\propto \pi N$ cross sections)
 \leftarrow DCC axial current and πN amplitude are consistent with PCAC relation

Cross section at $Q^2=0$ and $m_\mu=0$

$$\frac{d\sigma^{CC}}{dE_l d\Omega_l} = \frac{G_F^2 V_{ud}^2}{2\pi^2} \frac{E'^2}{E - E'} F_2,$$

PCAC

$$F_2 = \frac{2f_\pi^2}{\pi} \sigma_{tot}(\pi + N)$$



Rein and Sehgal, Annals Phys. 133 (1981)

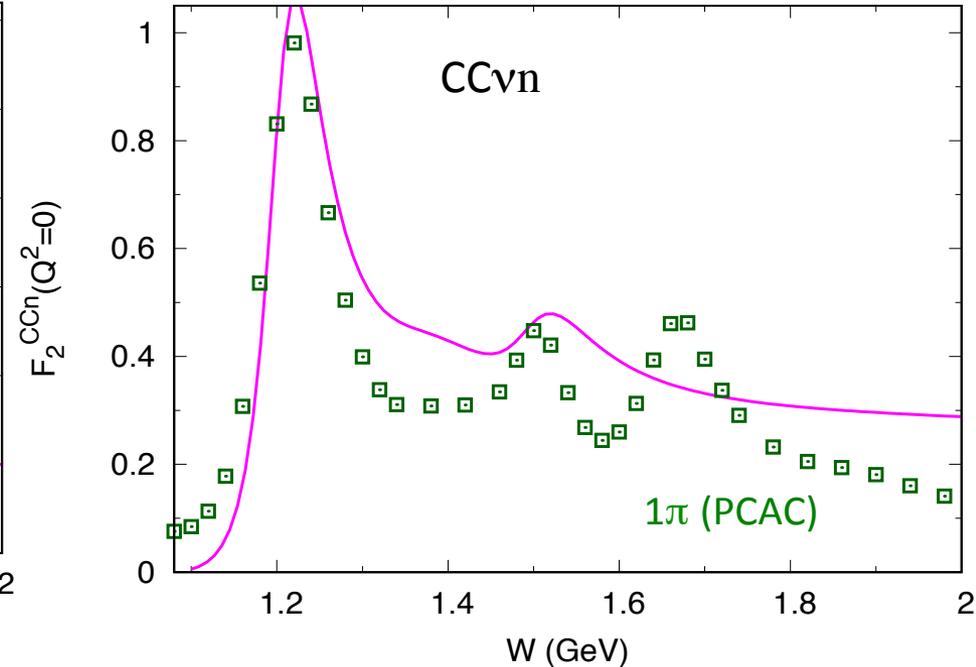
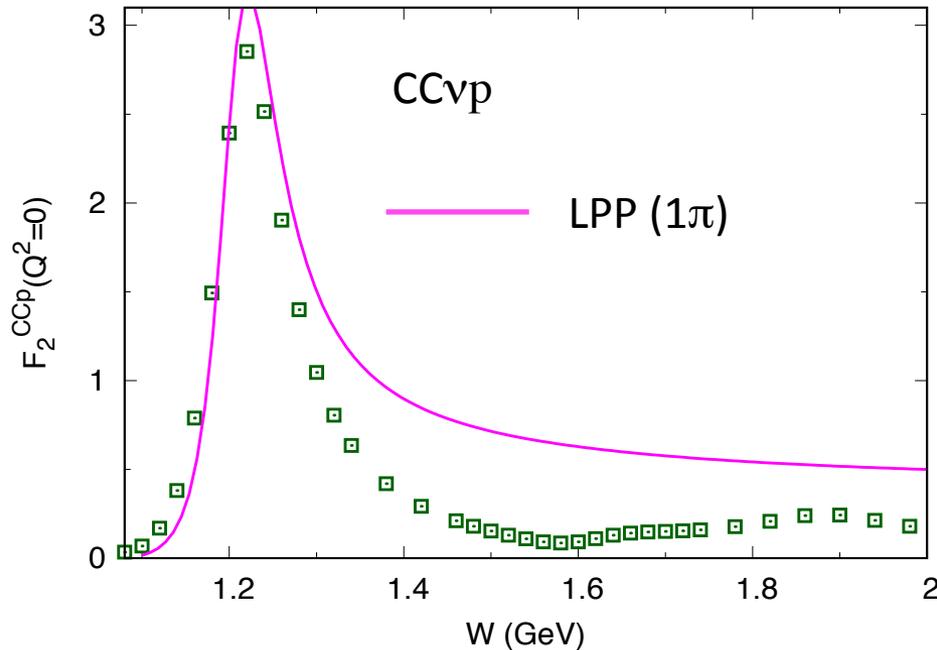
$F_2(Q^2=0)$ from RS model significantly overshoot PCAC values beyond $\Delta(1232)$ region

Cross section at $Q^2=0$ and $m_\mu=0$

$$\frac{d\sigma^{CC}}{dE_l d\Omega_l} = \frac{G_F^2 V_{ud}^2}{2\pi^2} \frac{E'^2}{E - E'} F_2,$$

PCAC

$$F_2 = \frac{2f_\pi^2}{\pi} \sigma_{tot}(\pi + N)$$



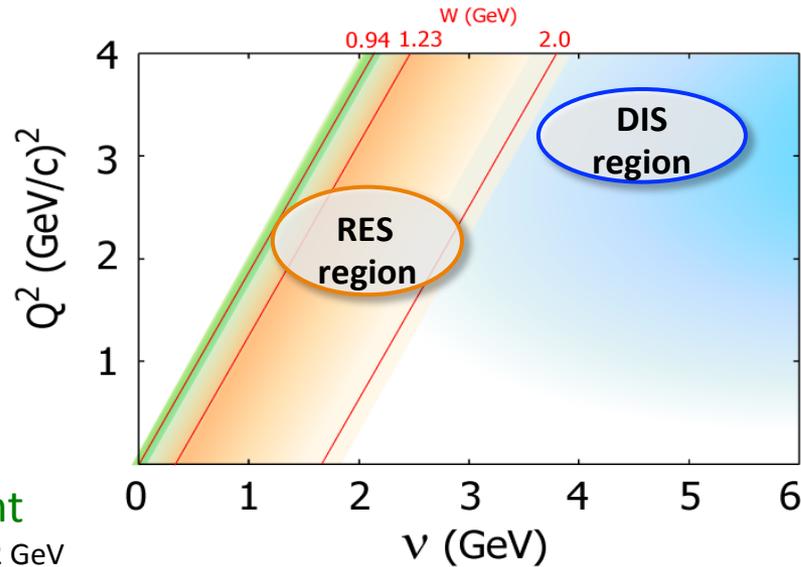
LPP: Lalakulich et al., PRD 74 (2006)

LPP model includes $\Delta(1232)$, $P_{11}(1440)$, $D_{13}(1520)$, $S_{11}(1535)$

$F_2(Q^2=0)$ from LPP model significantly overshoot PCAC values beyond $\Delta(1232)$ region

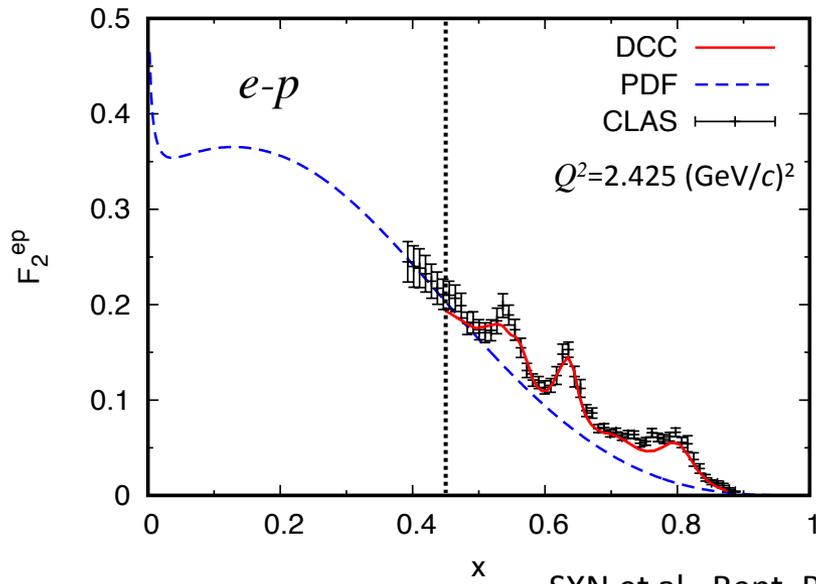
A remaining issue

Matching with DIS region



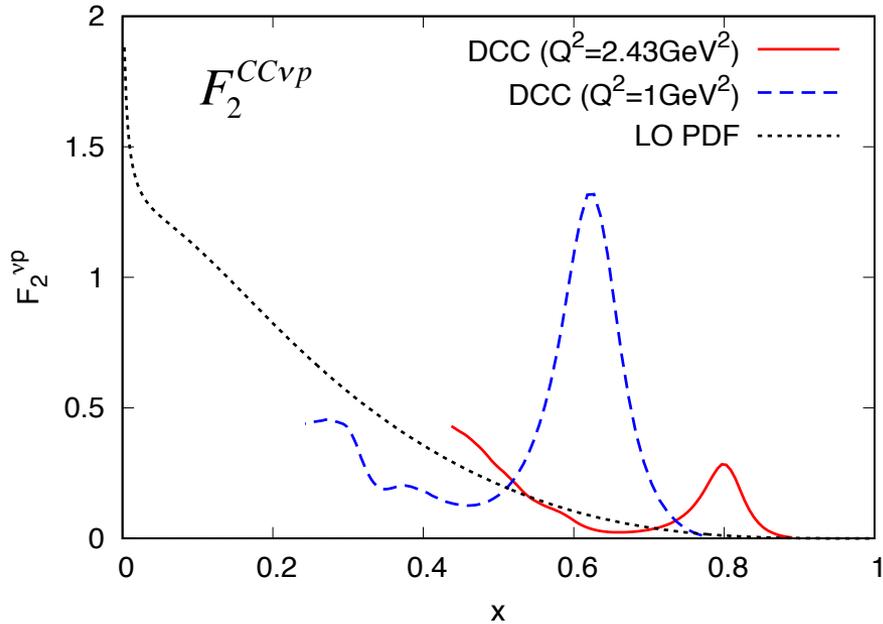
Electromagnetic current

$W=2$ GeV

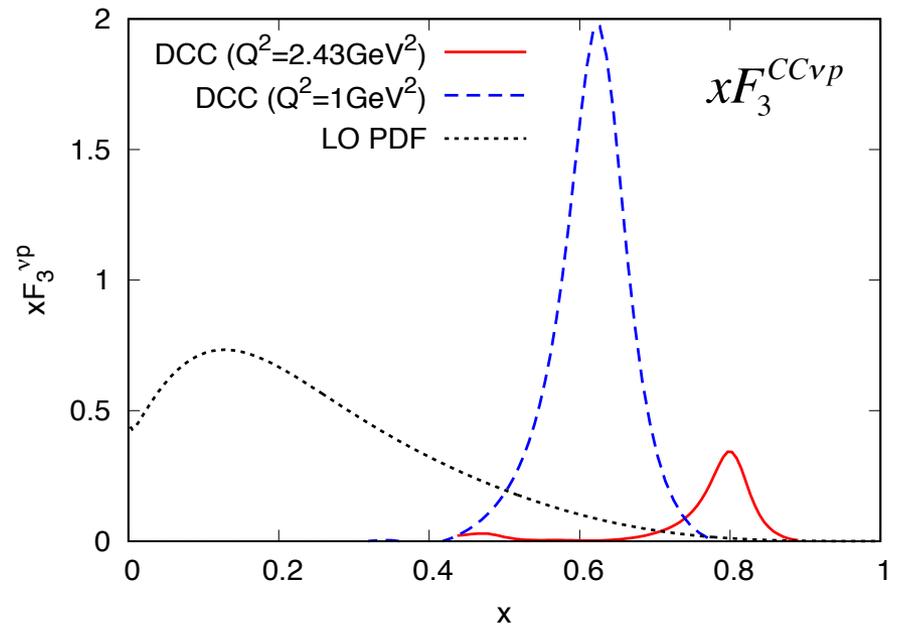


DCC smoothly connect to DIS region

Matching with DIS region



$$F_2^{CC} \sim |V|^2 + |A|^2$$



$$F_3^{CC} \sim \text{Re}(V A^*)$$

DCC axial current seems too weak in the matching region

- Dipole axial form factor may be causing too much damp
- Improvement is needed to fully cover high- Q^2 resonance region
 neutrino data, parity-violating electron data, fitting to PDF, etc.

Conclusion

DCC approach to resonance region beyond $\Delta(1232)$

Difficult problems that we must manage

- (several) Δ , N^* s, non-resonant overlap with comparable strengths
 - essential to understand interference pattern among them
- πN and $\pi\pi N$ channels are comparably important and are strongly coupled

Conclusion : DCC approach is promising

Extensively tested by $\gamma^{(*)}N$, $\pi N \rightarrow \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$ data

→ Well-validated vector current

→ Axial current consistent with the PCAC relation to πN interaction
interferences among different mechanisms are unambiguously fixed

→ Two-pion productions are calculated with all relevant resonance contributions

Should address remaining issues (high- Q^2 behavior of axial current, etc.)

BACKUP

Cross section at $Q^2=0$ and $m_\mu=0$

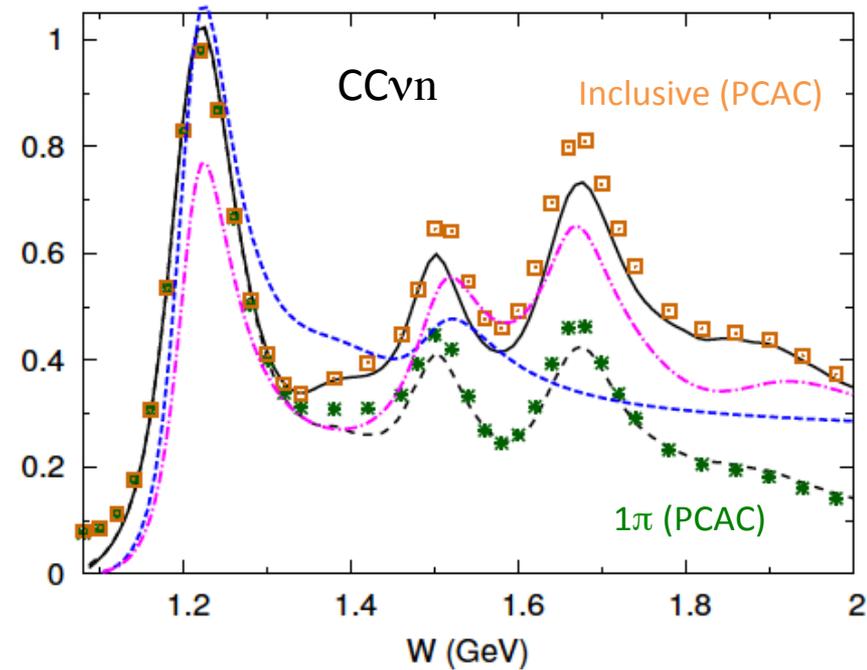
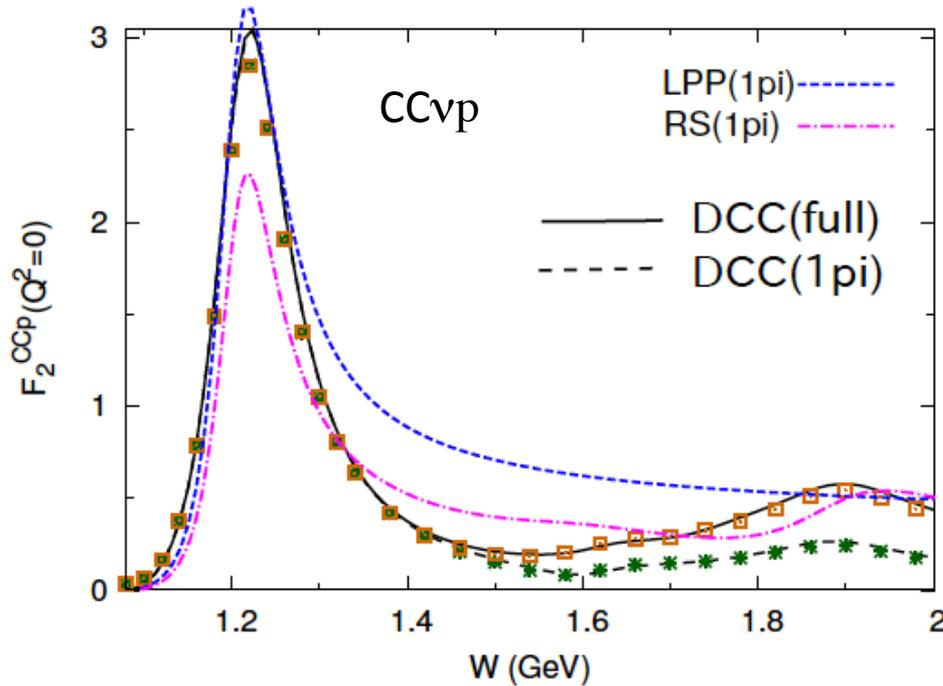
LPP: Lalakulich et al., PRD 74 (2006)

RS: Rein and Sehgal, Annals Phys. 133 (1981)

$$\frac{d\sigma^{CC}}{dE_1 d\Omega_1} = \frac{G_F^2 V_{ud}^2}{2\pi^2} \frac{E'^2}{E - E'} F_2,$$

PCAC

$$F_2 = \frac{2f_\pi^2}{\pi} \sigma_{tot}(\pi + N)$$

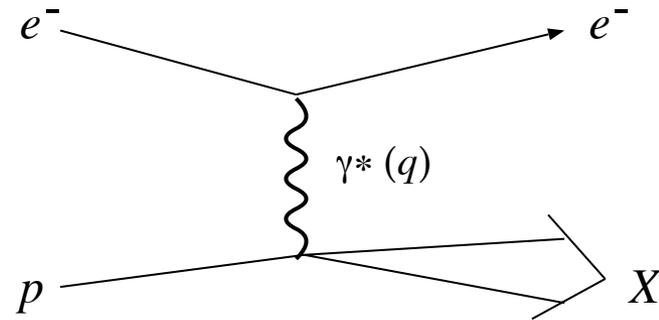


Useful quantity to check soundness of a model for energy region beyond $\Delta(1232)$

- F_2 from DCC model agrees with PCAC values ($\propto \pi N$ cross sections)
 \leftarrow DCC axial current and πN amplitude are consistent with PCAC relation
- F_2 from LPP and RS models deviate from PCAC values

Parity-violating electron-nucleon scattering and axial form factors

Inclusive electron-proton scattering ($e^- p \rightarrow e^- X$)



Differential cross section with respect to lepton kinematics

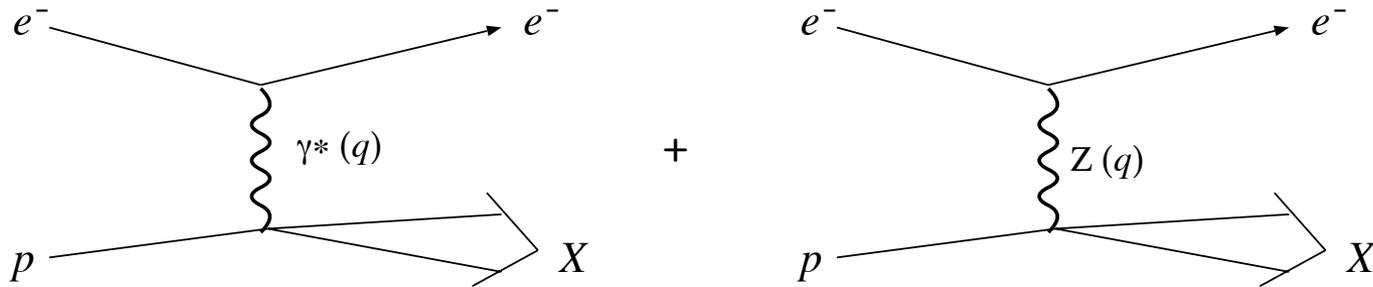
$$\frac{d\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2}{Q^4} \left[2W_1^{\text{em}} \sin^2 \frac{\theta}{2} + W_2^{\text{em}} \cos^2 \frac{\theta}{2} \right]$$

$W_i^{\text{em}}(W, Q^2)$: structure functions (all information of hadron dynamics encoded in)

$$W_1^{\text{em}} = \frac{1}{2} \bar{\sum}_i \sum_f \left(\left| \langle f | J_x^{\text{em}} | i \rangle \right|^2 + \left| \langle f | J_y^{\text{em}} | i \rangle \right|^2 \right) \delta^{(4)}(p_i + q - p_f)$$

$$W_2^{\text{em}} = \frac{Q^2}{|\vec{q}|^2} W_1^{\text{em}} + \frac{Q^2}{|\vec{q}|^2} \frac{Q^2}{|\vec{q}_c|^2} \bar{\sum}_i \sum_f \left| \langle f | J_0^{\text{em}} | i \rangle \right|^2 \delta^{(4)}(p_i + q - p_f)$$

Parity-violating inclusive electron-proton scattering



Parity-violating asymmetry

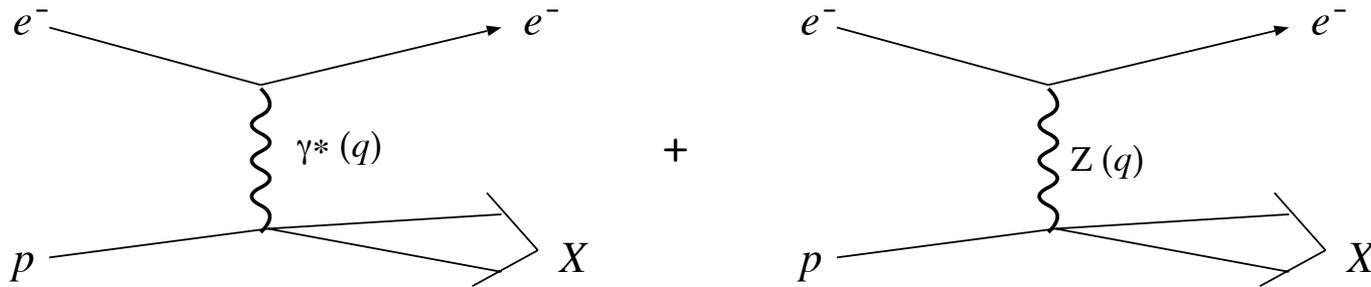
$$A = \frac{d\sigma(h_e = +1) - d\sigma(h_e = -1)}{d\sigma(h_e = +1) + d\sigma(h_e = -1)} = -\frac{Q^2 G_F}{\sqrt{2}(4\pi\alpha)} \frac{N}{D}$$

$$D = \cos^2 \frac{\theta}{2} W_2^{\text{em}} + 2 \sin^2 \frac{\theta}{2} W_1^{\text{em}}$$

$$N = \cos^2 \frac{\theta}{2} W_2^{\text{em-nc}} + 2 \sin^2 \frac{\theta}{2} W_1^{\text{em-nc}} + \sin^2 \frac{\theta}{2} (1 - 4 \sin^2 \theta_W) \frac{E + E'}{M} W_3^{\text{em-nc}}$$

$$J_{\text{nc}}^\mu = (1 - 2 \sin^2 \theta_W) J_{\text{em}}^\mu - V_{\text{isoscalar}}^\mu - A_3^\mu \quad \rightarrow \quad (1 - 2 \sin^2 \theta_W) D + \left(\cos^2 \frac{\theta}{2} W_2^{\text{em-is}} + 2 \sin^2 \frac{\theta}{2} W_1^{\text{em-is}} \right)$$

Parity-violating inclusive electron-proton scattering



Parity-violating asymmetry

$$A = -Q^2 \frac{G_F}{\sqrt{2}4\pi\alpha} \left(2 - 4\sin^2\theta_W + \Delta_V + \Delta_A \right)$$

$$\approx 8.99 \times 10^{-5} (\text{GeV}^{-2}) \approx 1.075 \text{ (main term)}$$

$$\Delta_V = \frac{\cos^2\frac{\theta}{2} W_2^{\text{em-is}} + 2\sin^2\frac{\theta}{2} W_1^{\text{em-is}}}{D}$$

$$\Delta_A = \frac{\sin^2\frac{\theta}{2} (1 - 4\sin^2\theta_W) \frac{E+E'}{M} W_3^{\text{em-nc}}}{D}$$

$$1 - 4\sin^2\theta_W \approx 0.08$$

- $2W_3^{\text{em-nc}} = W_3^{\text{CC}}$
 $\propto \langle f | V_{\text{iso-vector}} | i \rangle \langle f | A_{\text{iso-vector}} | i \rangle^*$

→ PV asymmetry data for backward electron kinematics can measure W_3 for neutrino CC process and axial matrix element (form factors)

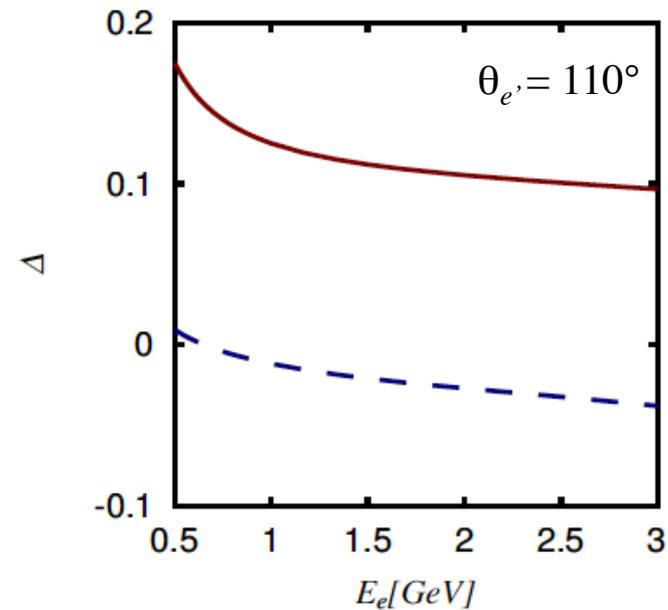
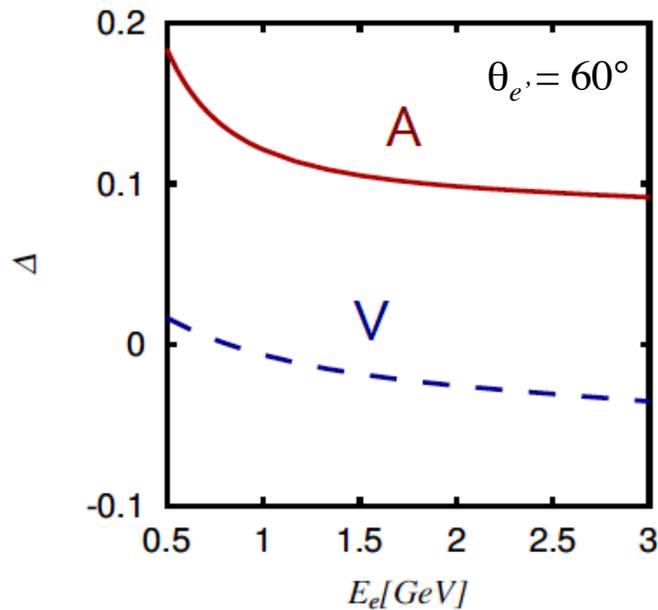
- Δ_V is proportional to isoscalar current
 → small in $\Delta(1232)$ region

$$A/Q^2 = -89.9 \times 10^{-6} (1.075 + \Delta_V + \Delta_A)$$

[1/GeV²]

$$\Delta_V = \frac{\cos^2 \frac{\theta}{2} W_2^{\text{em-is}} + 2 \sin^2 \frac{\theta}{2} W_1^{\text{em-is}}}{D},$$

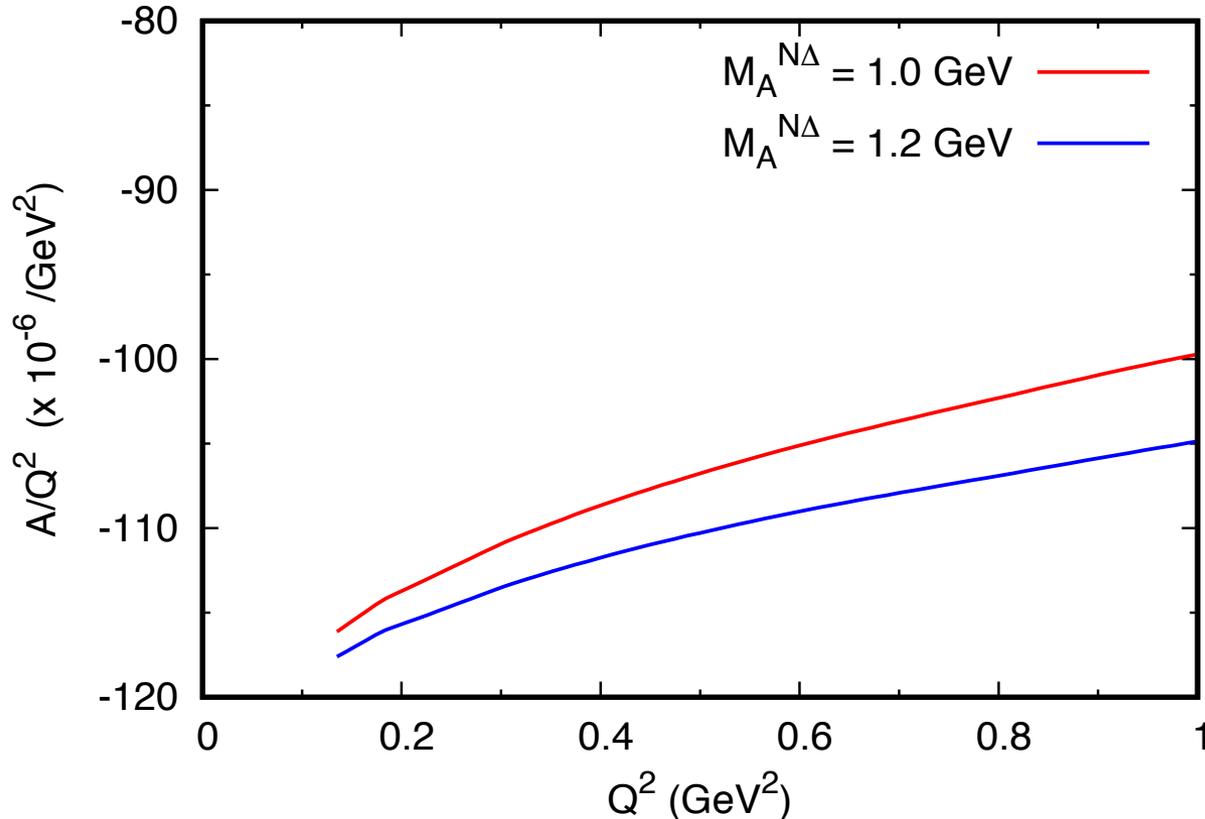
$$\Delta_A = \frac{\sin^2 \frac{\theta}{2} (1 - 4 \sin^2 \theta_W) \frac{E+E'}{M} W_3^{\text{em-nc}}}{D}$$



$p(\vec{e}, e'), W = 1.232 \text{ GeV}$

Δ_A gives $\sim 10\%$ correction to A

Sensitivity of PV asymmetry to $N \rightarrow \Delta(1232)$ axial form factor



$W = 1232$ MeV, $\theta_{e'} = 110^\circ$

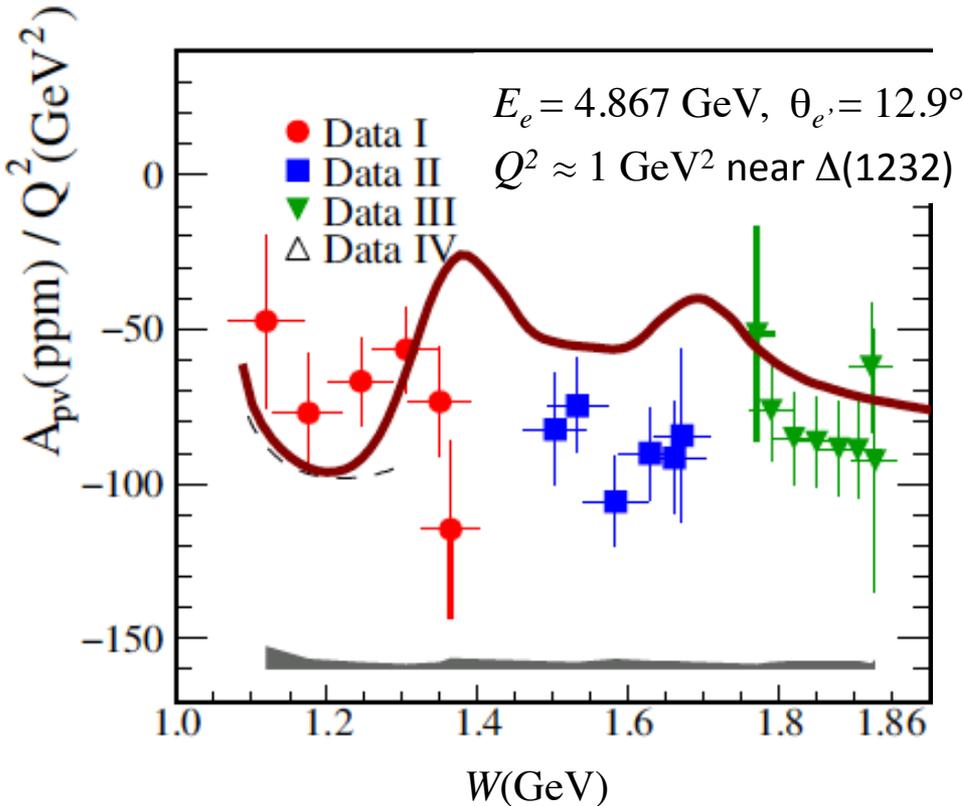
$$A/Q^2 = -89.9 (1.075 + \Delta_V + \Delta_A) \quad [10^{-6}/\text{GeV}^2]$$

$N \rightarrow \Delta(1232)$ dipole form factor
with $M_A^{N\Delta}$

- 5% precision PV asymmetry data may discriminate 0.2 GeV difference in the axial mass
- Sensitivity to $N \rightarrow N^*$, Δ^* (higher resonances) transition axial form factors can be studied with the DCC model

Comparison with PV asymmetry data from JLab

The PVDIS Collaboration, PRC 91 045506 (2015)



$$A = \frac{d\sigma(h_e = +1) - d\sigma(h_e = -1)}{d\sigma(h_e = +1) + d\sigma(h_e = -1)}$$

$$A / Q^2 = - 89.9 \times (1.075 + \Delta_V + \Delta_A) \quad [10^{-6}/\text{GeV}^2]$$

30-50% precision data for A already exist

→ Event rate measured at 0.3% precision

Deuteron target data

→ proton and neutron cross sections are simply summed in calculation

- Forward electron kinematics → axial current hardly contribute
- Deviation from data in $\Delta(1232)$ may be from nuclear effects (FSI, Fermi motion, etc.)
- Deviations in higher W region → calling improvement on the model (isospin separation)

Relation between neutrino and electron (photon) interactions

Charged-current (CC) interaction (e.g. $\nu_\mu + n \rightarrow \mu^- + p$)

$$L^{cc} = \frac{G_F V_{ud}}{\sqrt{2}} [J_\lambda^{cc} \ell_{cc}^\lambda + h.c.] \quad J_\lambda^{cc} = V_\lambda - A_\lambda \quad \ell_{cc}^\lambda = \bar{\psi}_\mu \gamma^\lambda (1 - \gamma_5) \psi_\nu$$

Electromagnetic interaction (e.g. $\gamma^{(*)} + p \rightarrow p$)

$$L^{em} = e J_\lambda^{em} A_{em}^\lambda \quad J_\lambda^{em} = V_\lambda + V_\lambda^{IS}$$

V and V^{IS} in J^{em} can be separately determined by analyzing photon ($Q^2=0$) and electron reaction ($Q^2 \neq 0$) data on both proton and neutron targets, because:

$$\langle p | V_\lambda | p \rangle = - \langle n | V_\lambda | n \rangle \quad \langle p | V_\lambda^{IS} | p \rangle = \langle n | V_\lambda^{IS} | n \rangle$$

Matrix element for the weak vector current is obtained from analyzing electromagnetic processes

$$\langle p | V_\lambda | n \rangle = \sqrt{2} \langle p | V_\lambda | p \rangle$$

DCC model for axial current

Because neutrino reaction data are scarce, axial current cannot be determined phenomenologically

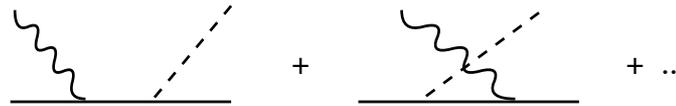
→ **Chiral symmetry** and **PCAC** (partially conserved axial current) are guiding principle

PCAC relation $\langle X' | q \cdot A | X \rangle \sim i f_\pi \langle X' | T | \pi X \rangle$

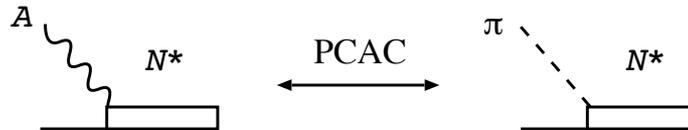
$Q^2=0$

non-resonant mechanisms

$$\partial_\mu \pi \rightarrow f_\pi A_\mu^{external}$$

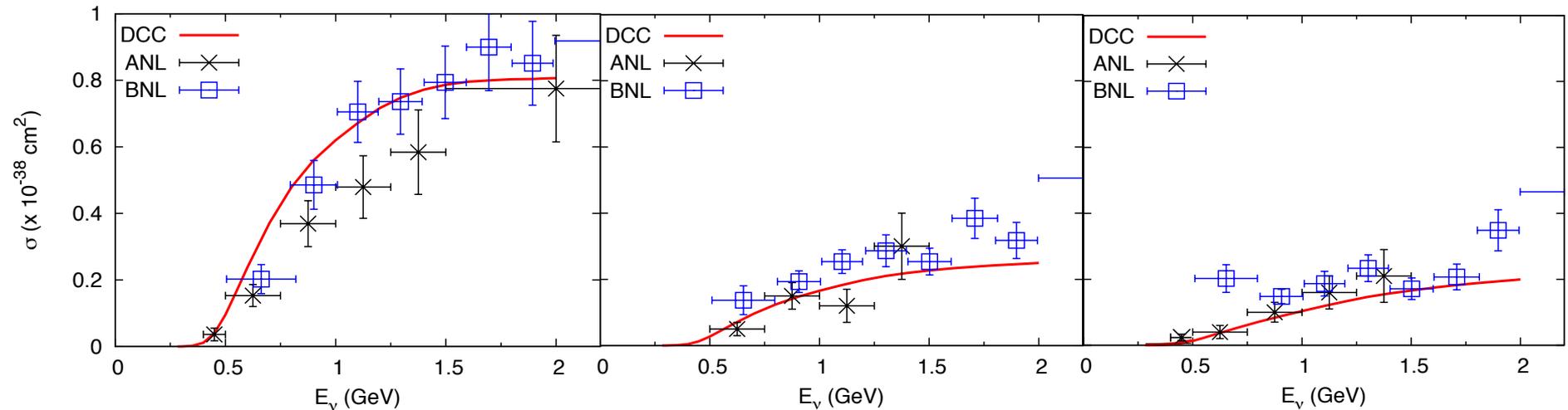


resonant mechanisms



Interference among resonances and background can be uniquely fixed within DCC model

Comparison with single pion data



DCC model prediction is consistent with data

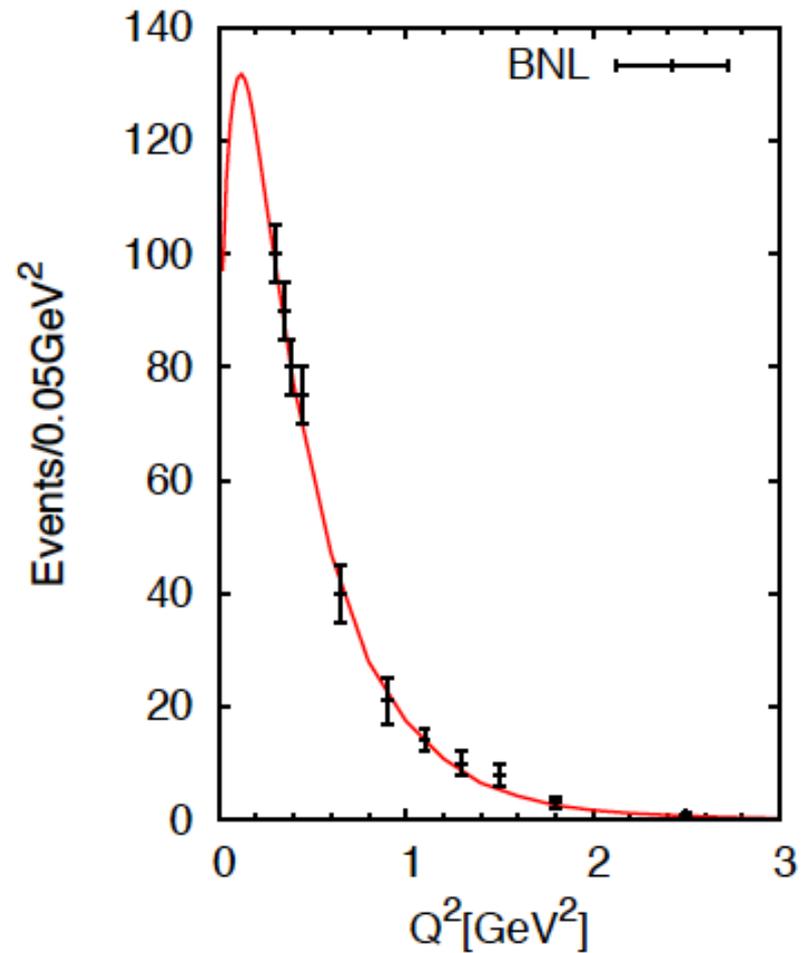
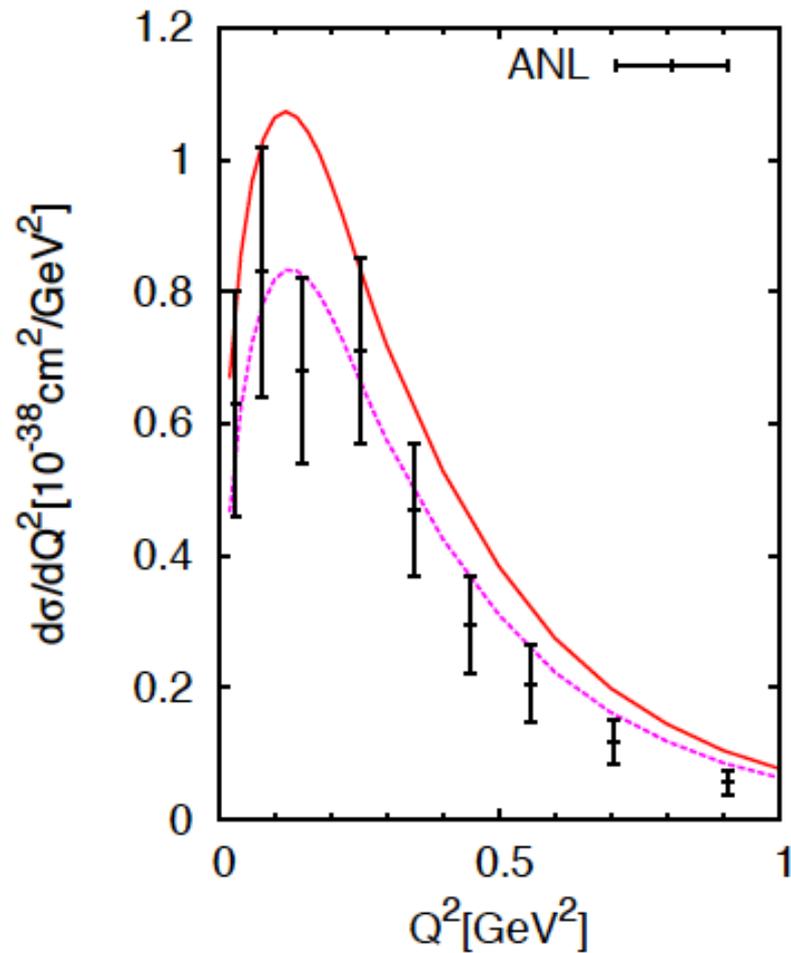
ANL Data : PRD **19**, 2521 (1979)

BNL Data : PRD **34**, 2554 (1986)

- DCC model has flexibility to fit data ($ANN^*(Q^2)$)
- Data should be analyzed with nuclear effects
(Wu et al. , PRC91, 035203 (2015); to be discussed later)

Q^2 – dependence

$$\nu_\mu p \rightarrow \mu^- \pi^+ p$$

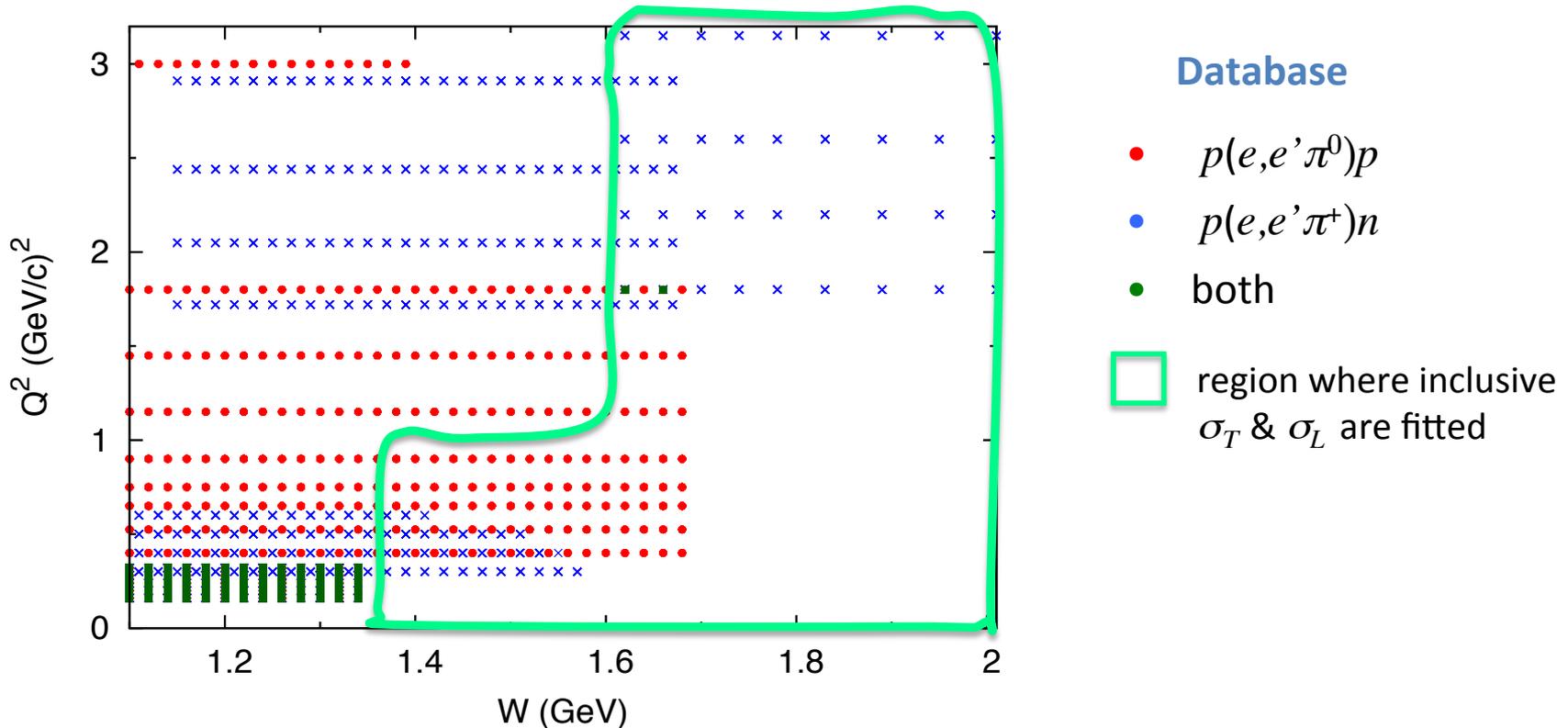


Analysis of electron-proton scattering data

Purpose : Determine Q^2 -dependence of vector coupling of p - N^* : $V_{pN^*}(Q^2)$

Data : * 1π electroproduction

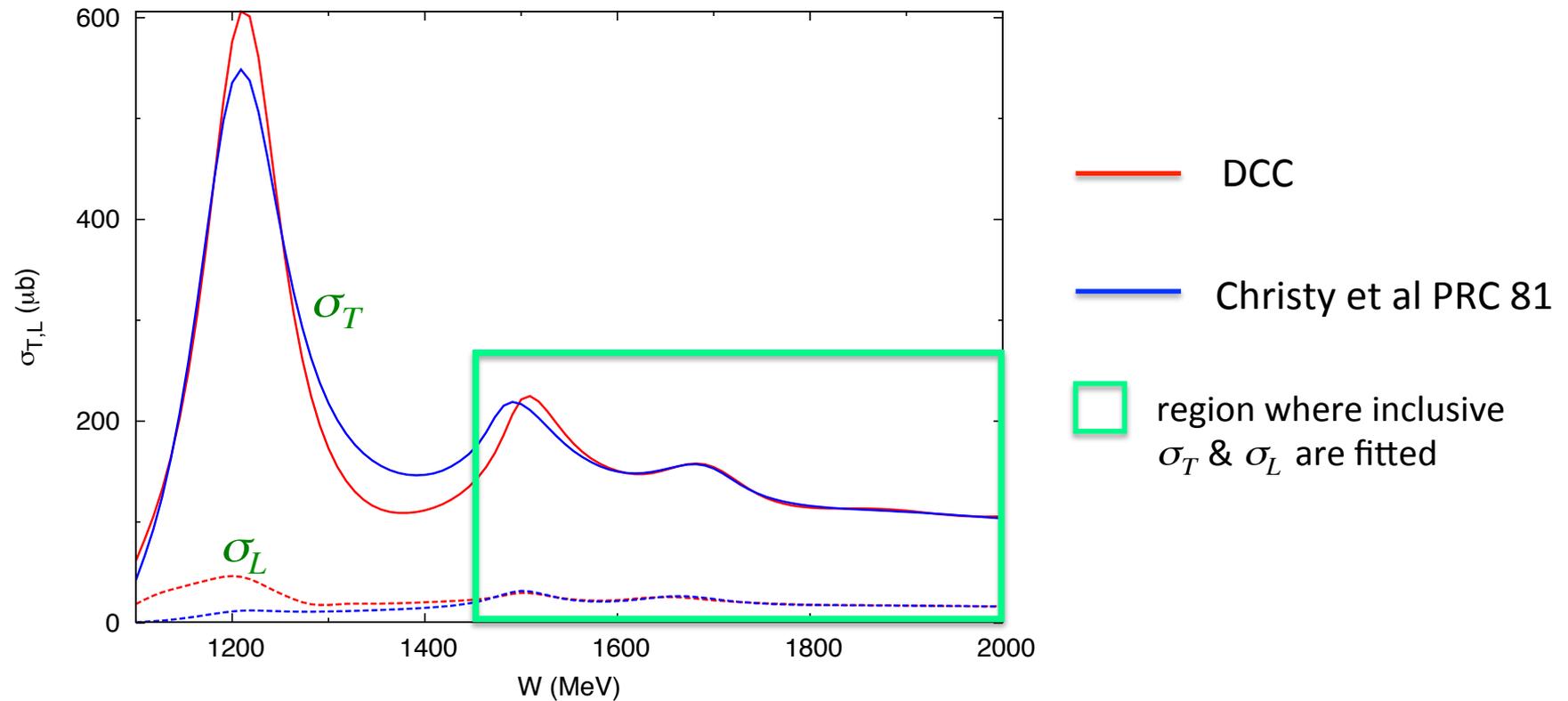
* Empirical inclusive inelastic structure functions σ_T, σ_L ← Christy et al, PRC 81 (2010)



Analysis result

$$Q^2=0.16 \text{ (GeV/c)}^2$$

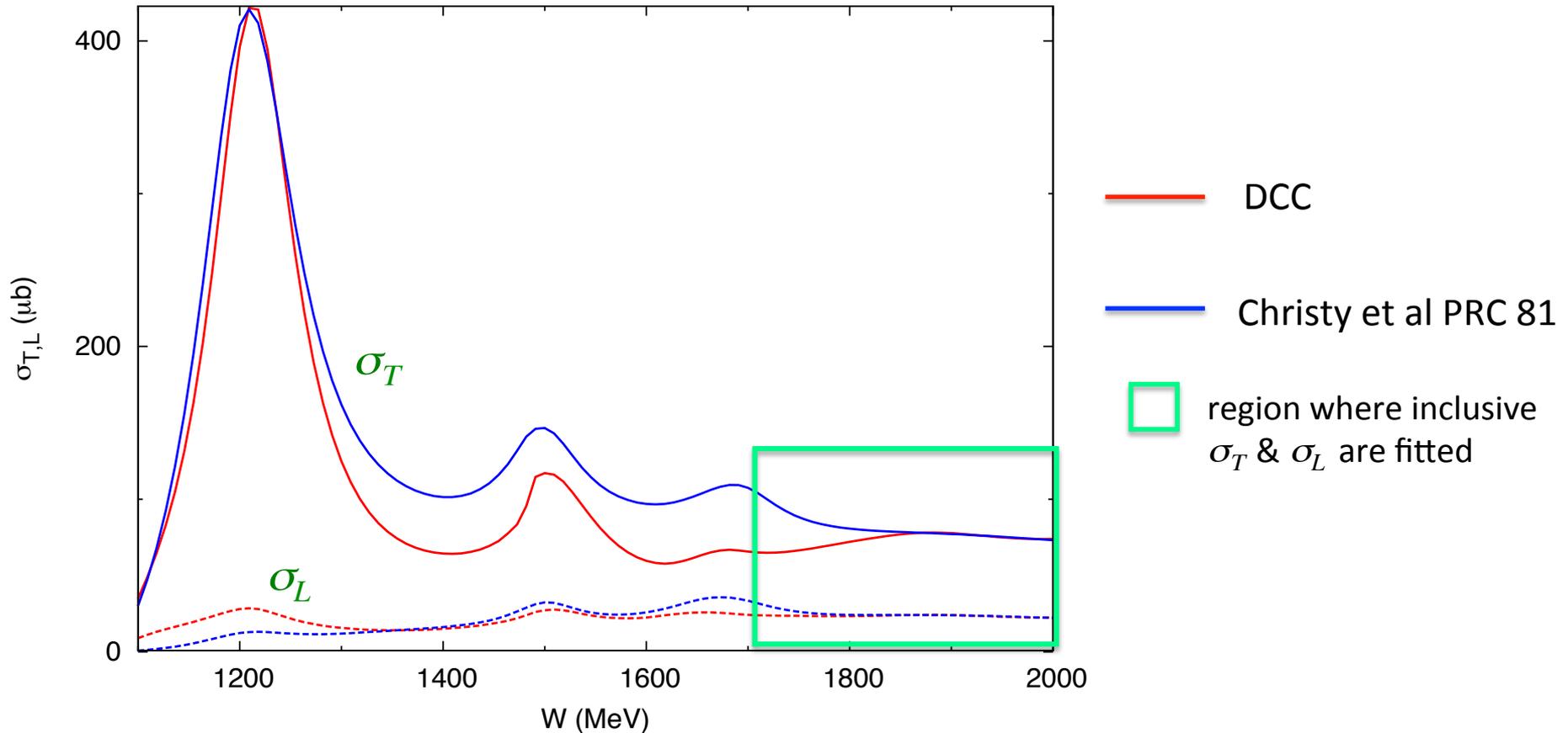
σ_T & σ_L (inclusive inelastic)



Analysis result

$Q^2=0.40 \text{ (GeV/c)}^2$

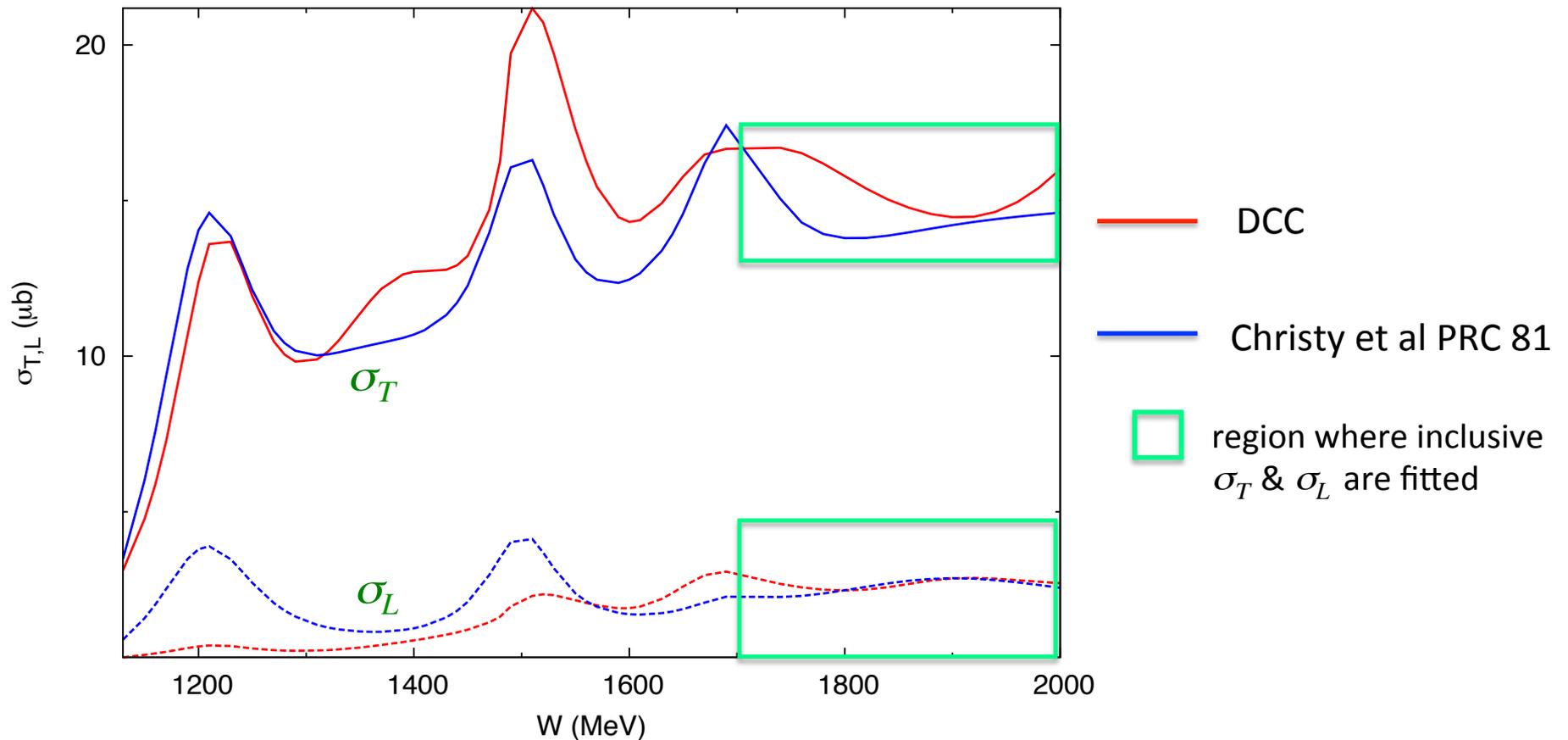
σ_T & σ_L (inclusive inelastic)



Analysis result

$$Q^2=2.95 \text{ (GeV/c)}^2$$

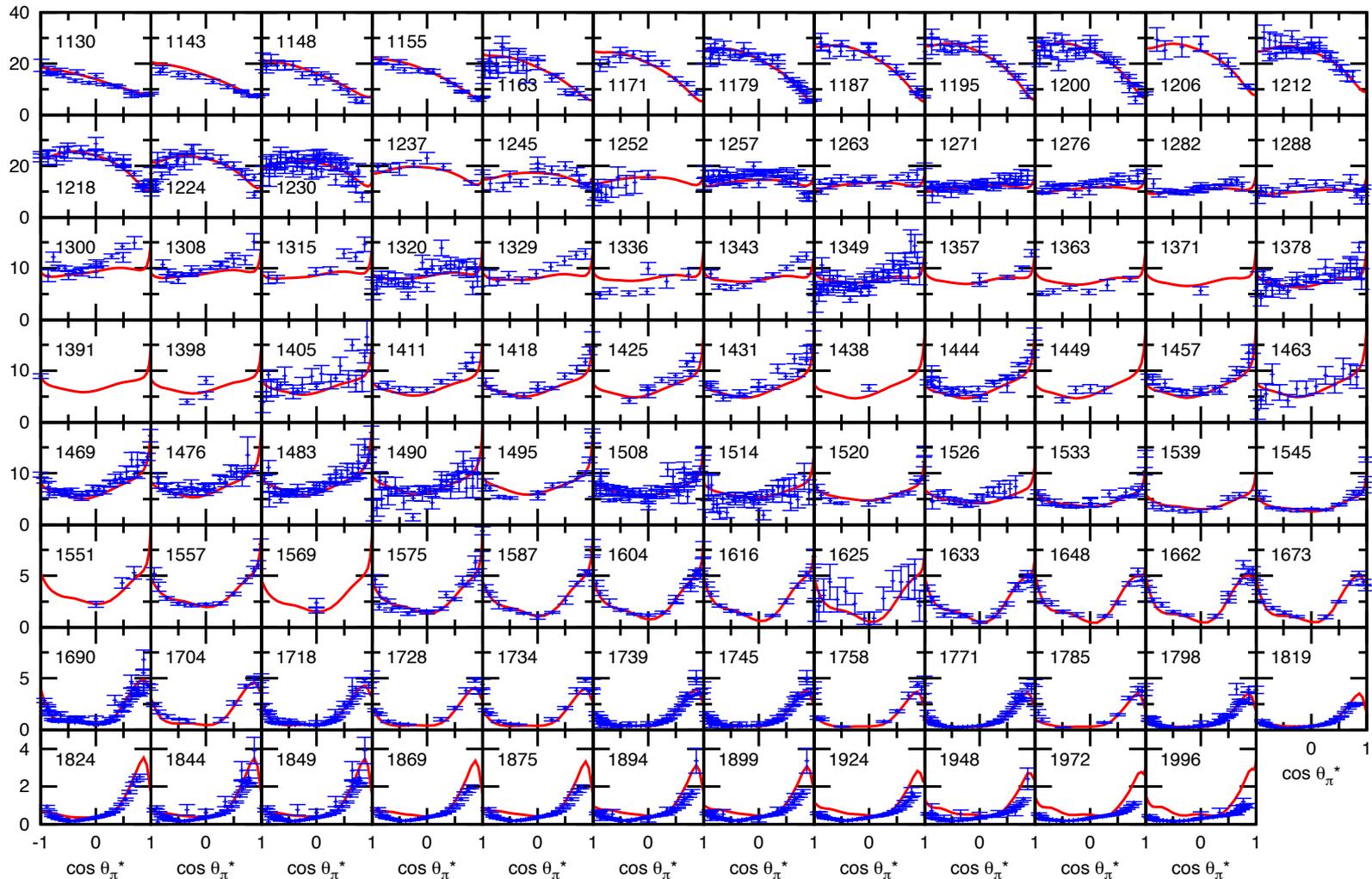
σ_T & σ_L (inclusive inelastic)



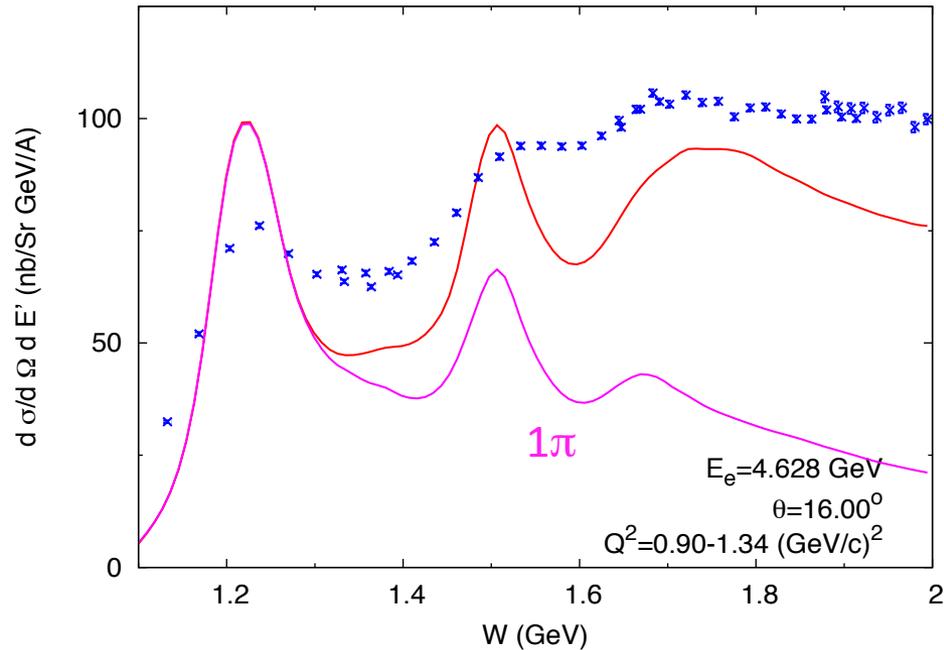
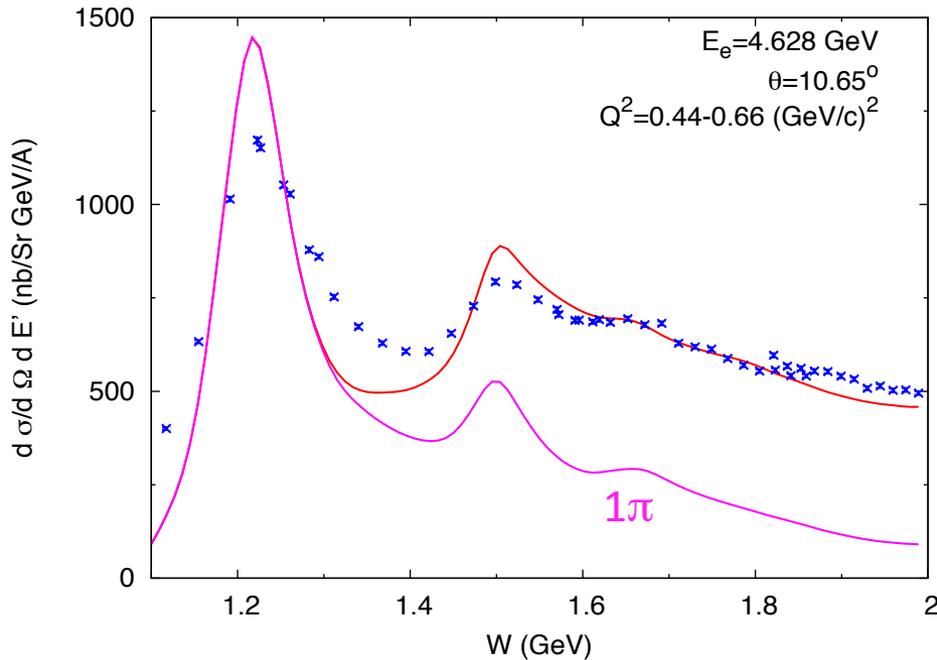
Analysis result (single π)

$$Q^2=0$$

$d\sigma / d\Omega$ ($\gamma n \rightarrow \pi^- p$) for $W=1.1 - 2.0$ GeV



Analysis result (inclusive e^-d)



Data: NP Proc. Suppl. 159, 163 (2006)

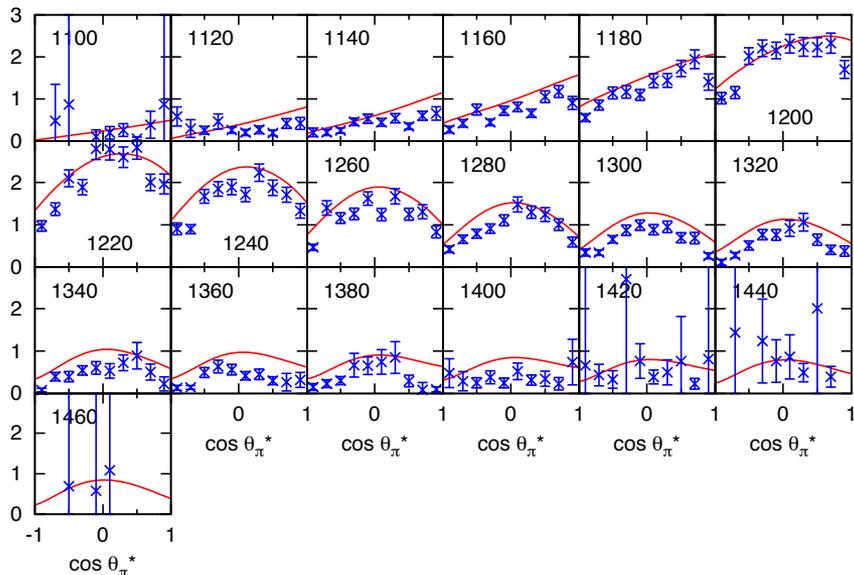
- Our calculation : $[\sigma(e^-p) + \sigma(e^-n)] / 2$
- Too sharp resonant peaks \rightarrow fermi motion smearing, other nuclear effects needed
- Reasonable starting point for application to neutrino interactions

Analysis result (single π)

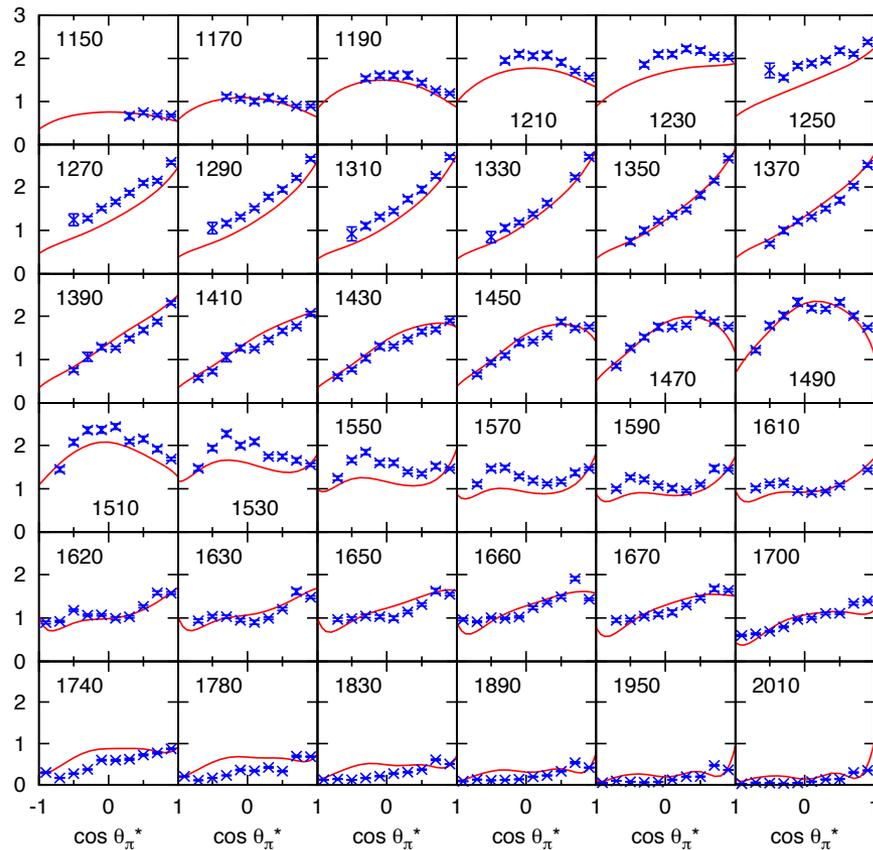
$$Q^2=1.76 \text{ (GeV/c)}^2$$

$\sigma_T + \varepsilon \sigma_L$ for $W=1.10 - 2.01 \text{ GeV}$

$p(e, e' \pi^0) p$



$p(e, e' \pi^+) n$

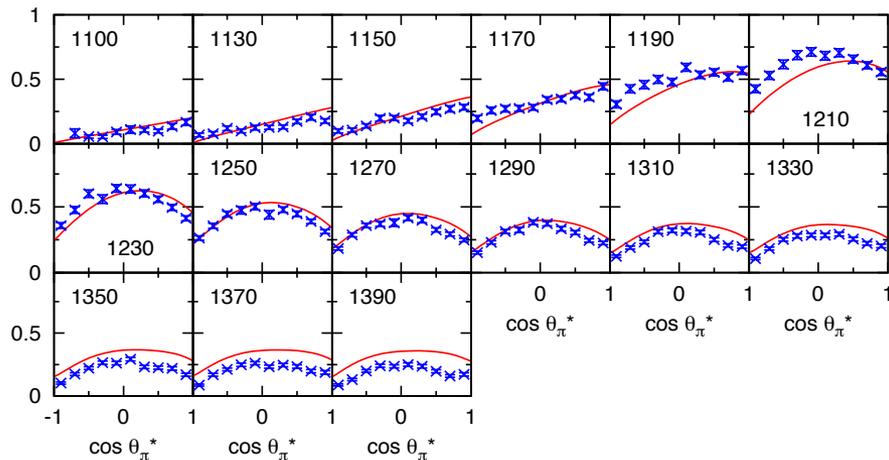


Analysis result (single π)

$$Q^2=2.91-3.00 \text{ (GeV}/c)^2$$

$\sigma_T + \varepsilon \sigma_L$ for $W=1.10 - 1.67 \text{ GeV}$

$p(e, e' \pi^0)p$



$p(e, e' \pi^+)n$

