



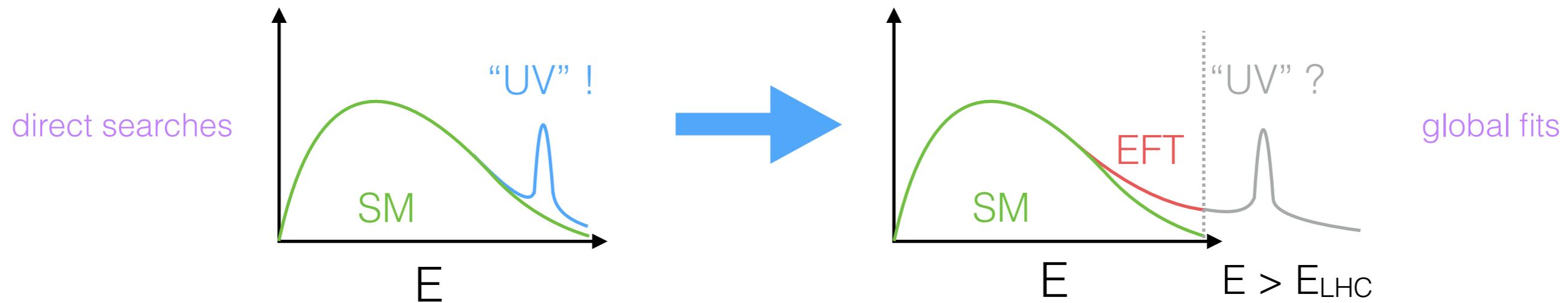
EFT aspects in top physics

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Higgs Toppings Workshop
Centro de Ciencias de Benasque Pedro Pascual

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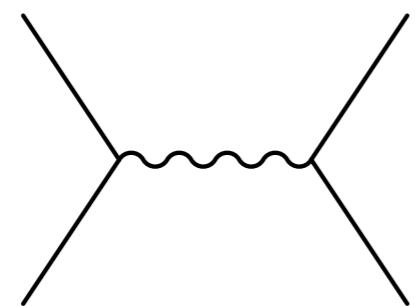
From bumps to tails



- Possibility that new states exist (just) beyond the energy reach of the LHC
 - We may still observe **indirect** effects of such particles in the kinematic **tails** of distributions, e.g., LEP limits on $\sim \text{TeV } Z'$
 - Intrinsically **small effects** that require precise theoretical control on signal and background predictions
- Framework: SM effective field theory (SMEFT)
 - Theoretically consistent, 'model independent' approach to **deviations** of interactions between SM fields

SMEFT

- Operator expansion: $\mathcal{L}_{\text{eff}} = \sum_i \frac{c_i \mathcal{O}_i^D}{\Lambda^{D-4}}$ more: fields derivatives
- Heavy states integrated out
 - Leaving only local operators built from SM fields
 - We are sensitive to these via large momentum flows through effective vertices (i.e. tails of energy distributions)
 - Truncated at dimension 6 (leading B & L preserving interactions)

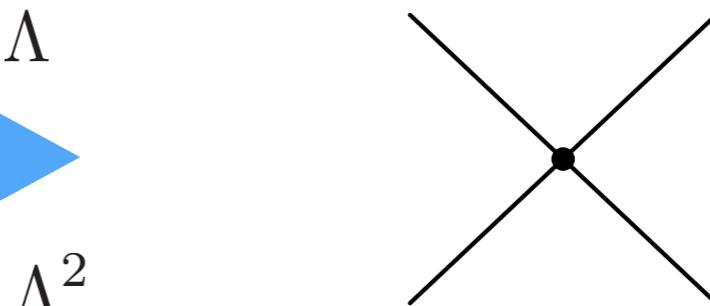


$$\frac{g^2}{p^2 - M^2}$$

$$M \equiv \Lambda$$

→

$$p^2 \ll \Lambda^2$$



D=6

$$-\frac{g^2}{\Lambda^2} \left[1 + \frac{p^2}{\Lambda^2} + \frac{p^4}{\Lambda^4} + \dots \right]$$

cf. Fermi Theory

SMEFT

- $SU(3)_C \times SU(2)_L \times U(1)_Y$ gauge invariant operator set
- Linear realisation of EW symmetry breaking
 - Higgs field is an $SU(2)_L$ doublet
 - Non-linear realisations also possible → different EFT
- Complete, non-redundant set of operators: Basis
 - Relations via SM EoM, field redefinitions, Fierz identities,...
- Dimension 6: 59 (76 real) - 2499 operators
 - Depends on CP/flavour assumptions [Buchmuller & Wyler; Nucl.Phys. B268 (1986) 621] [Grzadkowski et al.; JHEP 1010 (2010) 085]
- Dimension 8 now known ~ 895 - 36971 operators...
 - [Lehman et al.; PRD 91 (2015) 105014]
 - [Henning et al.; Commun.Math.Phys. 347 (2016) no.2, 363-388 & arXiv:1512.03433]

SILH
Warsaw
HISZ
Higgs

SMEFT - 0/2 fermions

'Warsaw' basis

X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi \square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	$Q_{u\varphi}$	• $(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\widetilde{W}}$	$\varepsilon^{IJK} \widetilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	• $(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \widetilde{W}}$	$\varphi^\dagger \varphi \widetilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	• $(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	• $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	• $(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	• $(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	• $(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	• $(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	• $(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \widetilde{W} B}$	$\varphi^\dagger \tau^I \varphi \widetilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	• $(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	• $i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

[Grzadkowski et al.; JHEP 1010 (2010) 085]

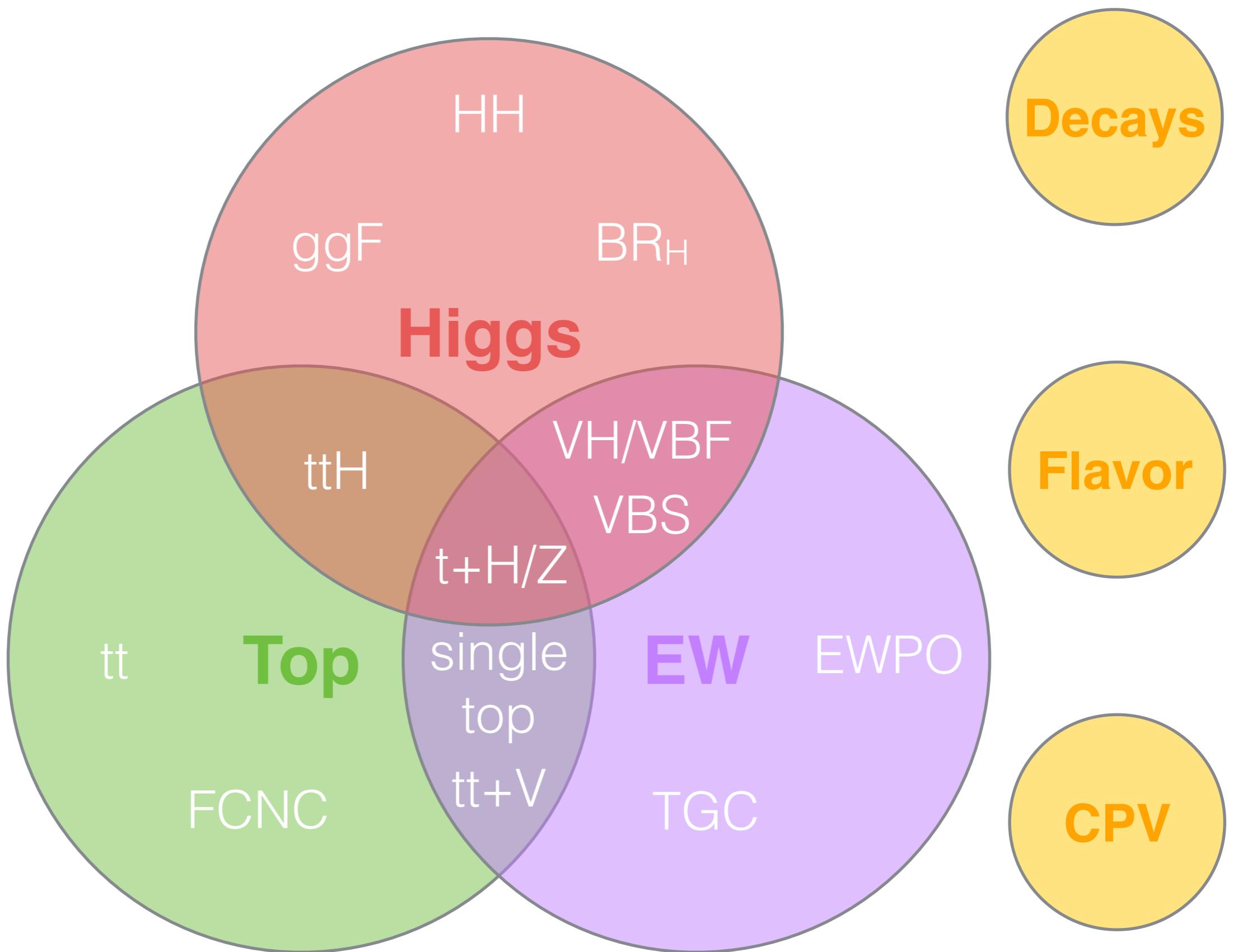
SMEFT - 4 fermions

Flavor indices = Most of the 2499

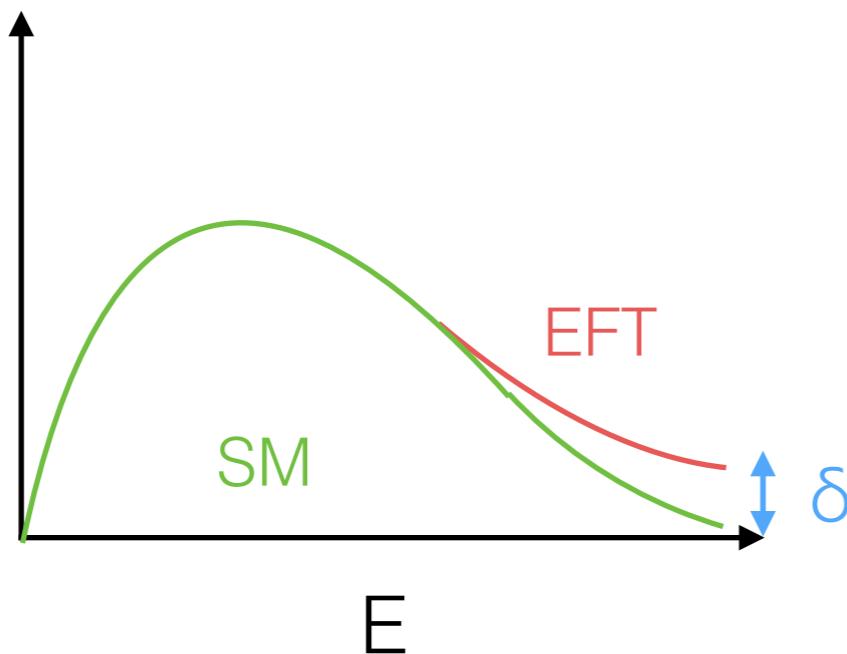
$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	• $(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	• $(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	• $(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	• $(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	• $(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	• $(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	• $(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	• $(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	• $(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	• $(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	• $(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	• $(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	• $(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	• $(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	•	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$	
$Q_{quqd}^{(1)}$	• $(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	•	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^\alpha)^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$	
$Q_{quqd}^{(8)}$	• $(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	•	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^\alpha)^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^n]$	
$Q_{lequ}^{(1)}$	• $(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	•	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^\alpha)^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^n]$	
$Q_{lequ}^{(3)}$	• $(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	•	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$	

[Grzadkowski et al.; JHEP 1010 (2010) 085]

SMEFT at the LHC: key players



SMEFT at the LHC



Higgs/EW interactions
Precision top physics
Blind directions from low
energy experiments (LEP,...)

- LHC has much to contribute towards global picture of SMEFT constraints
 - Many SM measurements & a few dedicated EFT interpretations
 - Important to ensure the EFT interpretation is possible
 - Precise MC tools for signal generation
 - Well designed analyses/measurements with control over energy scale
 - Awareness of correlations between different processes in SMEFT picture

General strategy

- Process that gets contributions from SMEFT operator(s)

- Step 1: sensitivity

- Process → sensitive observable(s)
 - Determine functional dependence of observable on Wilson coefficients

$$\sigma(\mu_0) = \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i(\mu_0) \sigma_i(\mu_0) + \sum_{i,j} \frac{1\text{TeV}^4}{\Lambda^4} C_i(\mu_0) C_j(\mu_0) \sigma_{ij}(\mu_0)$$

- One at a time → all together

- Step 2: LHC study

- Observable in fiducial detector volume
 - Unfolded detector effects but not to full phase space (model dependent)
 - Never sensitive to deviations outside the fiducial region

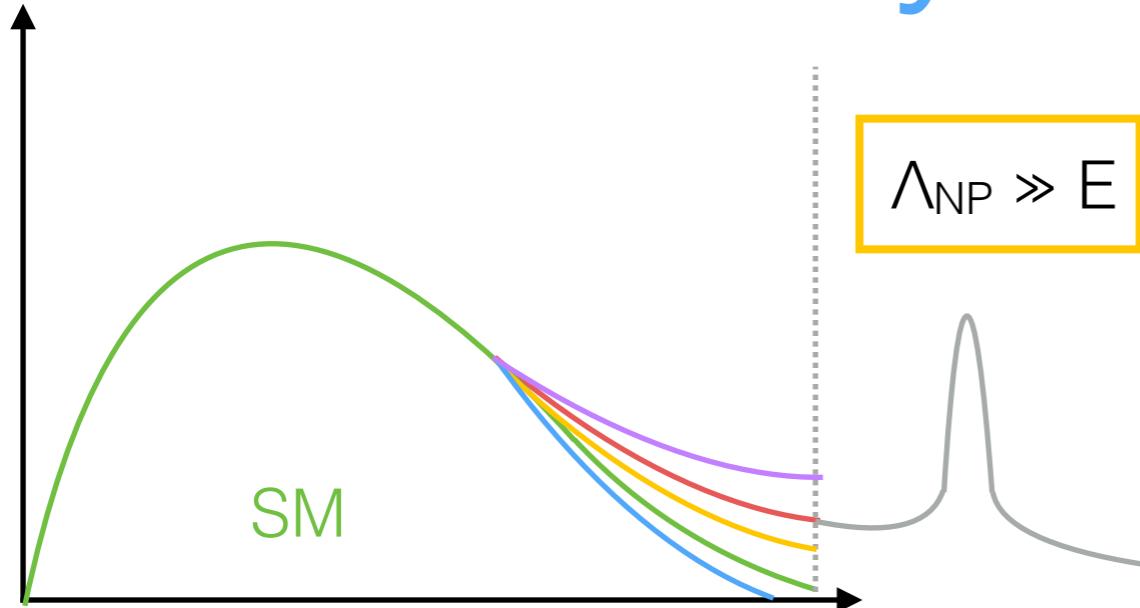
General strategy

- Step 3: LHC measurement
 - Unfolded to fiducial volume = reinterpretation without full/fast-sim
 - Reproducible event selection & background rejection
 - If MVA used: more complicated but not a showstopper
 - Easy to include in global fit
 - Dedicated EFT interpretation possible here
 - Control energy scale, binned observables or variable upper cuts
- Step 4: Input to global fit
 - Combine many such observables & perform statistical interpretation
 - Validity (energy scale vs cut-off) assessment *a posteriori*
 - Compare to UV models

Interpretation

- Global likelihood in SMEFT parameter space
- Individual & marginalised confidence intervals
 - Individual limits are useful to quantify degree of sensitivity to given coeff.
 - Marginalised intervals reveal degeneracies/blind directions
- Impact of including or not squared EFT terms
- Constraints as a function of cuts
 - Allow a wider range of model interpretations (different NP mass scales)
 - Perturbativity in Wilson coefficients
- Matching to UV models
 - Correlated Wilson coefficients → better limits
 - Validity & perturbativity in NP couplings

EFT validity



Q: How well does my EFT approximate full theory?
 A: Depends on the theory!
 Q: But I thought EFT was model independent....

- Two “expansions” occur
- Lagrangian level, (E/Λ_{NP}), truncated at operator dimension
 - Golden rule: cannot probe energies beyond Λ_{NP}
$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$
- Observable level, ($c_i E/\Lambda_{\text{NP}}$) truncated at... ?

$$\sigma = \sigma_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \sigma_i^{(6)} + \sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\Lambda^4} \sigma_{ij}^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \sigma_i^{(8)} + \dots$$

EFT expansion

- Practically: $\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$

A red diagonal line starts from the top right and slopes down towards the bottom left, passing through the term $\sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)}$ in the equation above.

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

- Observable:

$$\sigma = \sigma_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \sigma_i^{(6)} + \sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\boxed{\Lambda^4}} \sigma_{ij}^{(6)} + \sum_i \frac{c_i^{(8)}}{\boxed{\Lambda^4}} \sigma_i^{(8)} + \dots$$

A red diagonal line starts from the top right and slopes down towards the bottom left, passing through the term $\sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\boxed{\Lambda^4}} \sigma_{ij}^{(6)}$ in the equation above.

- To square or not to square...
 - Formally, D=6 squared part is of the same order as D=8 interference
 - D=8 part, in general, is unknown and/or not feasible
- Is the EFT invalid if (D=6 squared) > (D=6 interference)?
 - Depends on $c_i^{(6)}$, $c_{ij}^{(6)}$, $c_i^{(8)}$ and $\sigma_i^{(6)}$, $\sigma_{ij}^{(6)}$, $\sigma_i^{(8)}$ → model dependence
 - At most, the σ scale with energy as: $\sigma_i^{(6)} \sim E^2$, $\sigma_{ij}^{(6)} \sim E^4$, $\sigma_i^{(8)} \sim E^4$

Large coefficients

- If c is **large** e.g. Wilson coefficient is poorly constrained
- $(D=6)^2$ terms **could** be important without invalidating EFT

$$\frac{E^2}{\Lambda^2} < 1 < c_i^{(6)} \frac{E^2}{\Lambda^2} < c_i^{(6)} c_j^{(6)} \frac{E^4}{\Lambda^4}$$

- Truncating L at $D=6$, σ is not really a series expansion

$$\sigma = \sigma_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \sigma_i^{(6)} + \sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\Lambda^4} \sigma_{ij}^{(6)} + \text{nothing}$$

- Dropping the squared terms $\rightarrow \sigma$ **not positive-definite**
- If $(D=6)^2$ are relevant, UV interpretations lean towards strongly coupled models (large c 's)
 - Most model independent approach: assume nothing about the size of c 's

Non-interference

- Alternatively, one may have $\sigma^{(6)}_i < \sigma^{(6)}_{ij}$
 - Non-interference by e.g. helicity selection rules in the high energy limit
- High energy theorem
 - Many $2 \rightarrow 2$ amplitudes involving at least one transverse gauge boson mediated by D=6 operators do not interfere with the SM

[Cheung & Shen; PRL 115 (2015) 071601]
 [Azatov, Contino & Riva; PRD 95 (2017) 065014]

Interference?

X

Total Helicity

A_4	$ h(A_4^{\text{SM}}) $	$ h(A_4^{\text{BSM}}) $
$VVVV$	0	4,2
$VV\phi\phi$	0	2
$VV\psi\psi$	0	2
$V\psi\psi\phi$	0	2
$\psi\psi\psi\psi$	2,0	2,0
$\psi\psi\phi\phi$	0	0
$\phi\phi\phi\phi$	0	0

✓

V = Transverse vector

ϕ = Longitudinal vector or Higgs

ψ = Fermion

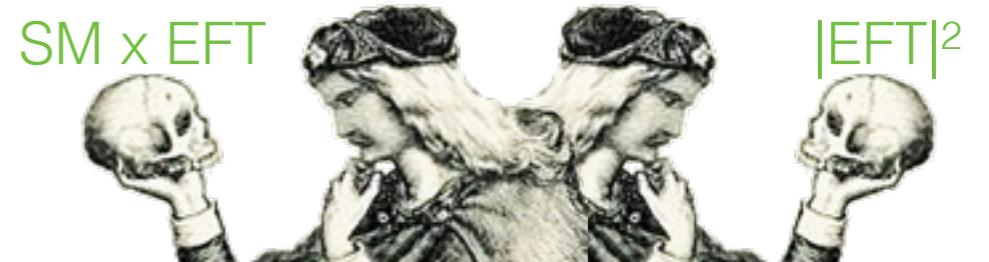
$p p \rightarrow ZH, WH, WW, WZ$

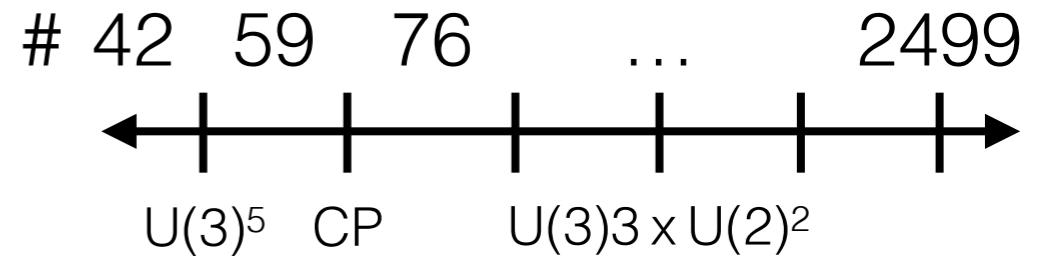
Interference can be recovered
considering finite mass effects or
higher order corrections ($2 \rightarrow 3,4$)

[Panico, Riva & Wulzer; CERN-TH-2017-85]
 [Azatov, et al. LHEP 1710 (2017) 027]

EFT “expansion”

- To square or not to square...
 - Model & process dependent
 - Better calculate both and check the effect of including or not the square
- Relation to the validity question
 - Depends on the sensitivity of each measurement/process
 - We can only constrain $(c/\Lambda) & \Lambda$ an arbitrary scale w.r.t to unknown Λ_{NP}
- Validity assessment is an *a posteriori* check at interpretation stage on a process-by-process basis
 - Publish limits as a function of experimental energy
[Contino et al.; JHEP 1607 (2016) 144]
- Realistically can't include D=8 without sufficient motivation
 - If $C^{(6)}_{ij}=0$ e.g. for neutral triple gauge boson couplings





Flavor symmetry

- SM fermion sector q^i, u^i, d^i, l^i, e^i
 - 5 $SU(3) \times SU(2) \times U(1)$ representations $\rightarrow U(3)^5$ flavor symmetry
 - Only **broken** by Yukawa interactions
- Some SMEFT operators also break it
 - Chirality flipping $F_L f_R$ structures (Yukawa-like)
 - Flavor violating (off diagonal/non-universal) entries
- Starting point: **flavor symmetric**
 - No chirality flipping & diagonal, universal structure
- Controlled departures
 - Minimal for top physics: $U(3)^3 \times U(2)^2$, single out q^3, u^3
 - Similarly MFV: expansion in Yukawa couplings

SMEFT for top physics

- Top quark is a crucial ingredient of the EW sector
 - Top-Higgs-W/Z couplings/masses are related in SM: unitarity cancellations
 - May reveal hints about the underlying nature of EWSB
- Coloured sector, strongly coupled to the Higgs
 - Large corrections to inclusive rates (~ 1 K-factors)
 - Non-trivial shape corrections at differential level
 - Non-trivial renormalisation/operator mixing from QCD
- Active research topic in SMEFT
 - Global fits, higher order corrections
- Many measurements at the LHC
 - Total, differential, boosted & rare processes e.g. $t\bar{t}+Z/W/\gamma$, tZj

Anomalous top interactions

- EFT interpretation of top quark data
 - Measurement of deviations from SM interactions of the top
 - = anomalous couplings (?)
- SMEFT
 - $SU(3) \times SU(2) \times U(1)$ gauge invariant construction
 - Correlations between interactions
 - $SU(2)$ multiplets: $t_L \leftrightarrow b_L$
 - Non Abelian gauge field strengths: $V \leftrightarrow VV \leftrightarrow VVV$
 - Higgs field insertions: $ffV \leftrightarrow ffVh$
- Important to exploit this
 - Global approach

Gluon interactions

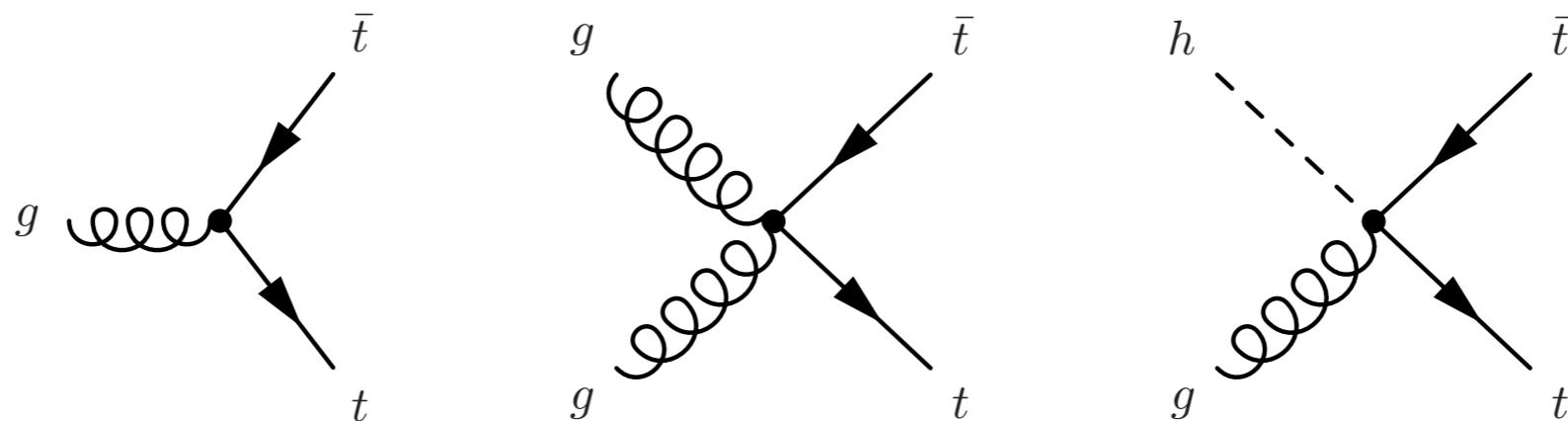
$$\mathcal{L}_{gtt} = \boxed{-g_s \bar{t} \frac{\lambda^a}{2} \gamma^\mu t G_\mu^a} - \boxed{g_s \bar{t} \lambda^a \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^g + i d_A^g \gamma_5) t G_\mu^a}$$

SM

Dipole

Fixed by SU(3)
gauge symmetry

$$\mathcal{O}_{tG} = i (\bar{Q} \sigma^{\mu\nu} T_A t) \tilde{\varphi} G_{\mu\nu}^A + \text{h.c}$$

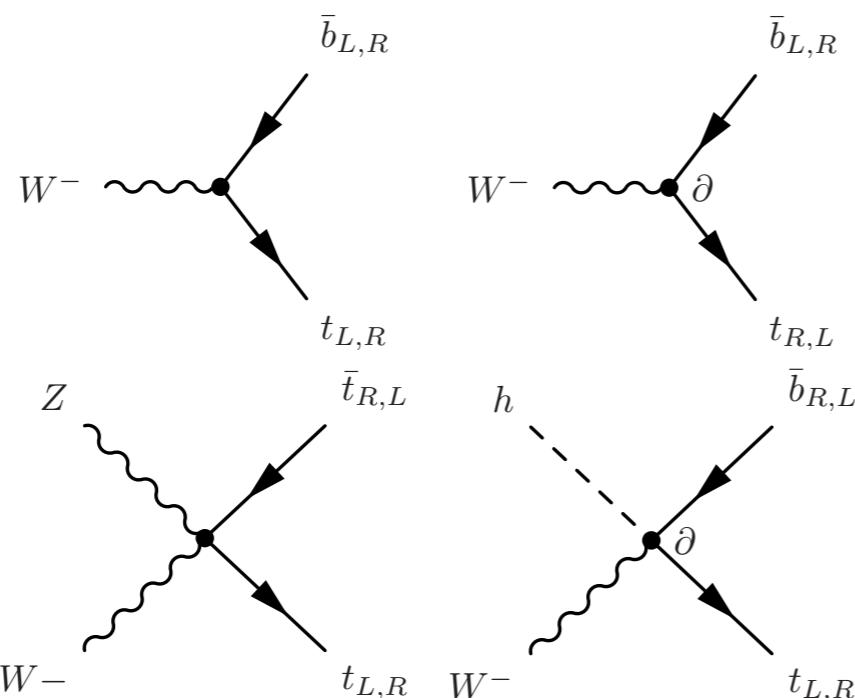


tt, ttH, H, HH, ...

W interactions

$$\mathcal{L}_{Wtb} = \begin{array}{l} \text{SM} \\ \boxed{-\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^-} \\ \boxed{-\frac{g}{\sqrt{2}} \bar{b} \frac{i \sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + \text{H.c.}} \end{array} \quad \text{RHCC} \quad \boxed{\text{Dipole}}$$

No gauge symmetry,
deviations after EWSB



$$\mathcal{O}_{\varphi Q}^{(3)} = i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \sigma^I \varphi)(\bar{Q} \gamma^\mu \sigma_I Q)$$

$$\mathcal{O}_{\varphi tb} = i(\tilde{\varphi} D_\mu \varphi)(\bar{t} \gamma^\mu b) + \text{h.c.}$$

$$\mathcal{O}_{tW} = i(\bar{Q} \sigma^{\mu\nu} \sigma_I t) \tilde{\varphi} W_{\mu\nu}^I + \text{h.c.}$$

$$\mathcal{O}_{bW} = i(\bar{Q} \sigma^{\mu\nu} \sigma_I b) \varphi W_{\mu\nu}^I + \text{h.c.}$$

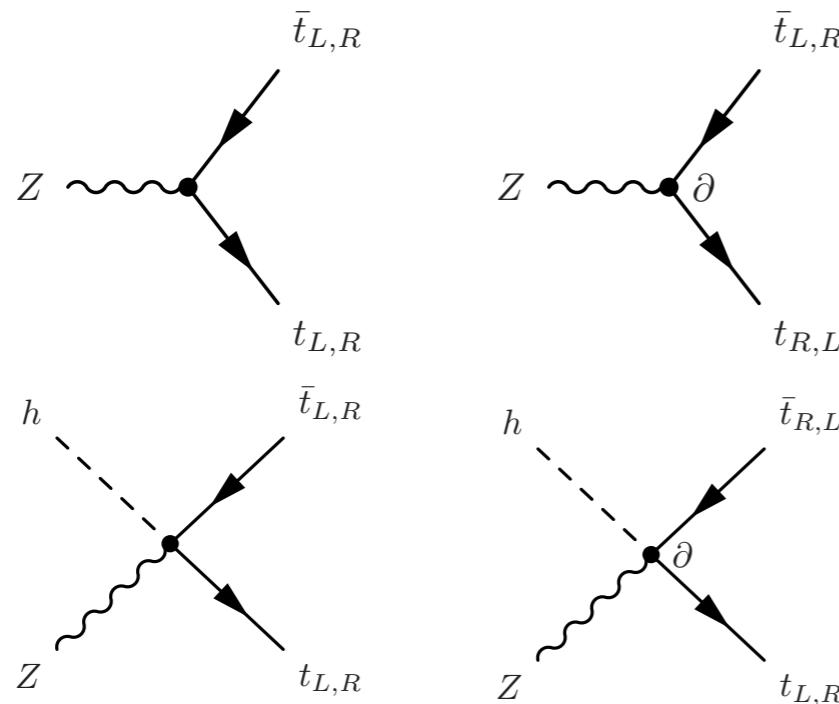
t-decay, single-t, tZj, tHj, ...

Z interactions

$$\mathcal{L}_{Ztt} = \boxed{-\frac{g}{2c_W}\bar{t}\gamma^\mu (X_{tt}^L P_L + X_{tt}^R P_R - 2s_W^2 Q_t) t Z_\mu} \text{SM}$$

$$\boxed{-\frac{g}{2c_W}\bar{t}\frac{i\sigma^{\mu\nu}q_\nu}{M_Z} (d_V^Z + id_A^Z\gamma_5) t Z_\mu,} \text{Dipole}$$

No gauge symmetry,
deviations after EWSB



$$\mathcal{O}_{\varphi t} = i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{t}\gamma^\mu t)$$

$$\mathcal{O}_{\varphi Q}^{(1)} = i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{Q}\gamma^\mu Q)$$

$$\mathcal{O}_{\varphi Q}^{(3)} = i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \sigma^I \varphi)(\bar{Q}\gamma^\mu \sigma_I Q)$$

ttZ, ttW, tZj, ...

Photon interactions

$$\mathcal{L}_{\gamma tt} = \boxed{-eQ_t \bar{t} \gamma^\mu t A_\mu} - \boxed{e \bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^\gamma + i d_A^\gamma \gamma_5) t A_\mu}$$

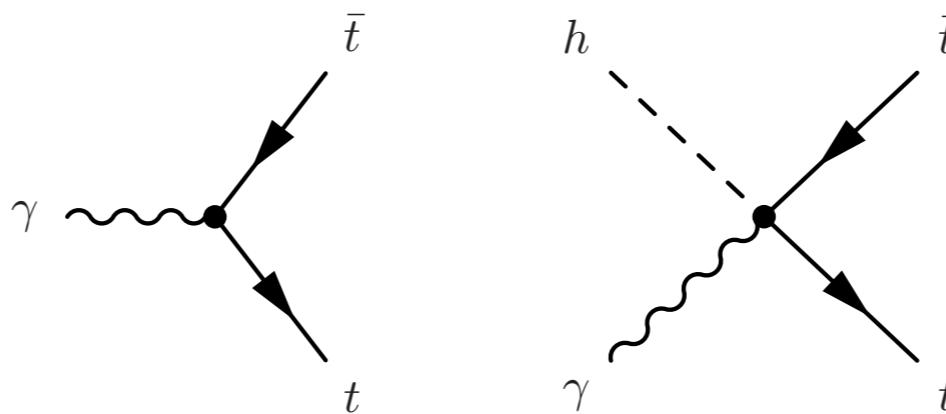
SM

Dipole

Fixed by QED
gauge symmetry

$$\mathcal{O}_{tW} = i (\bar{Q} \sigma^{\mu\nu} \sigma_I t) \tilde{\varphi} W_{\mu\nu}^I + \text{h.c}$$

$$\mathcal{O}_{tB} = i (\bar{Q} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu} + \text{h.c}$$



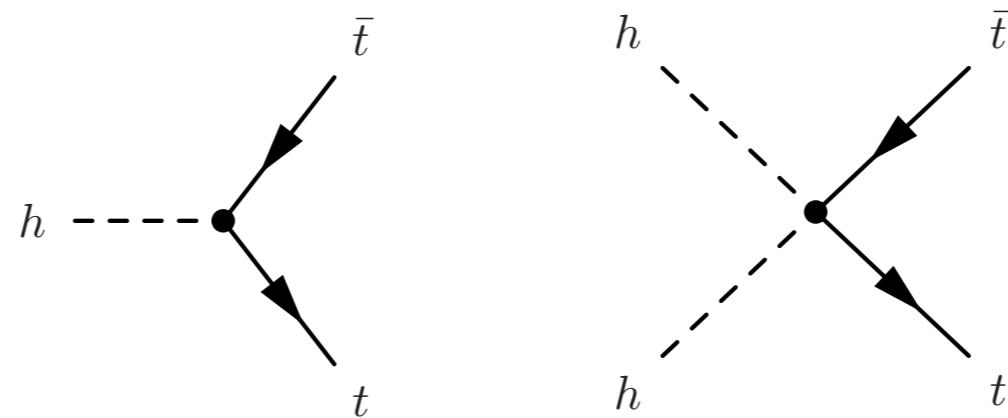
$tt\gamma, t\gamma j, \dots$

Higgs interaction

$$\mathcal{L}_{tth} = -\frac{m_t}{v} (\kappa_t h) + \frac{c_2}{v} h h (t_L \bar{t}_R + \text{h.c})$$

SM

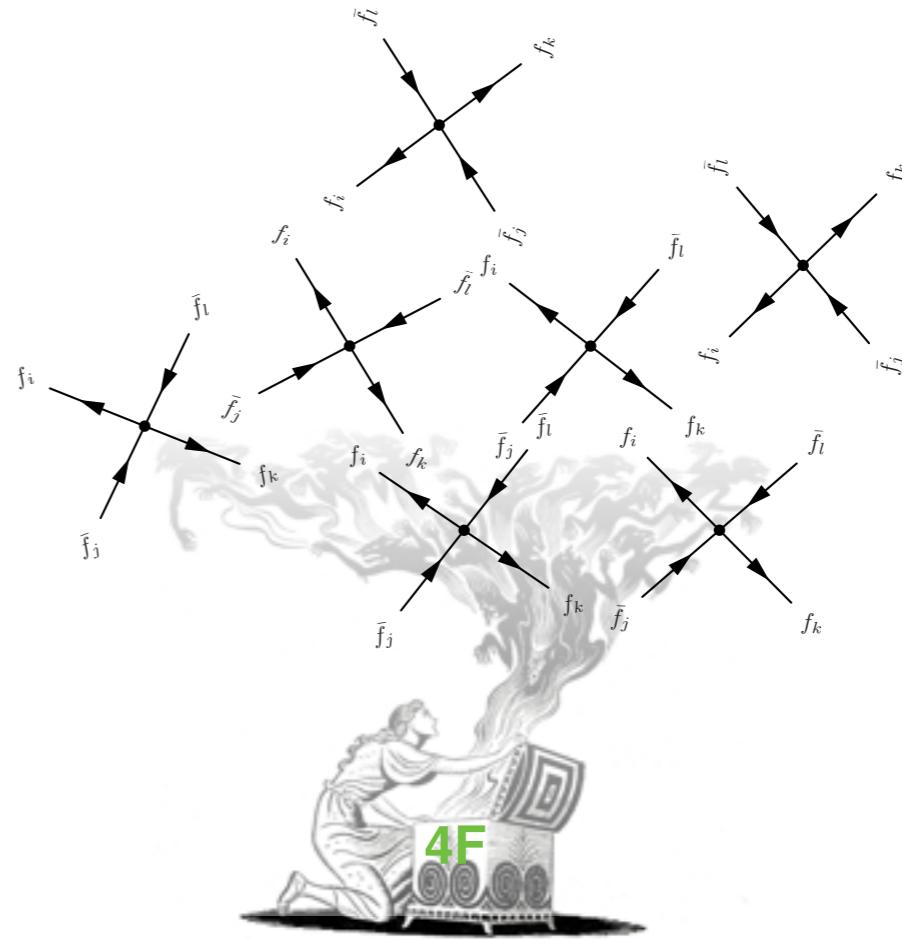
$$\mathcal{O}_{t\varphi} = i (\varphi^\dagger \varphi) (\bar{Q} t \tilde{\varphi}) + \text{h.c}$$



ttH, tHj, H, HH...

Four fermion

- Pandora's box of SMEFT
 - Huge number of flavor indices
 - Mostly flavor violating
- ~30 operators in minimal flavor symmetry assumption
 - Decompose into QQQQ, QQqq & QQII



$$U(3)^3 \times U(2)^2$$

tt, tt+W/Z/H/ γ , single-t, t+X, 4t, ttbb, ttjj, ...

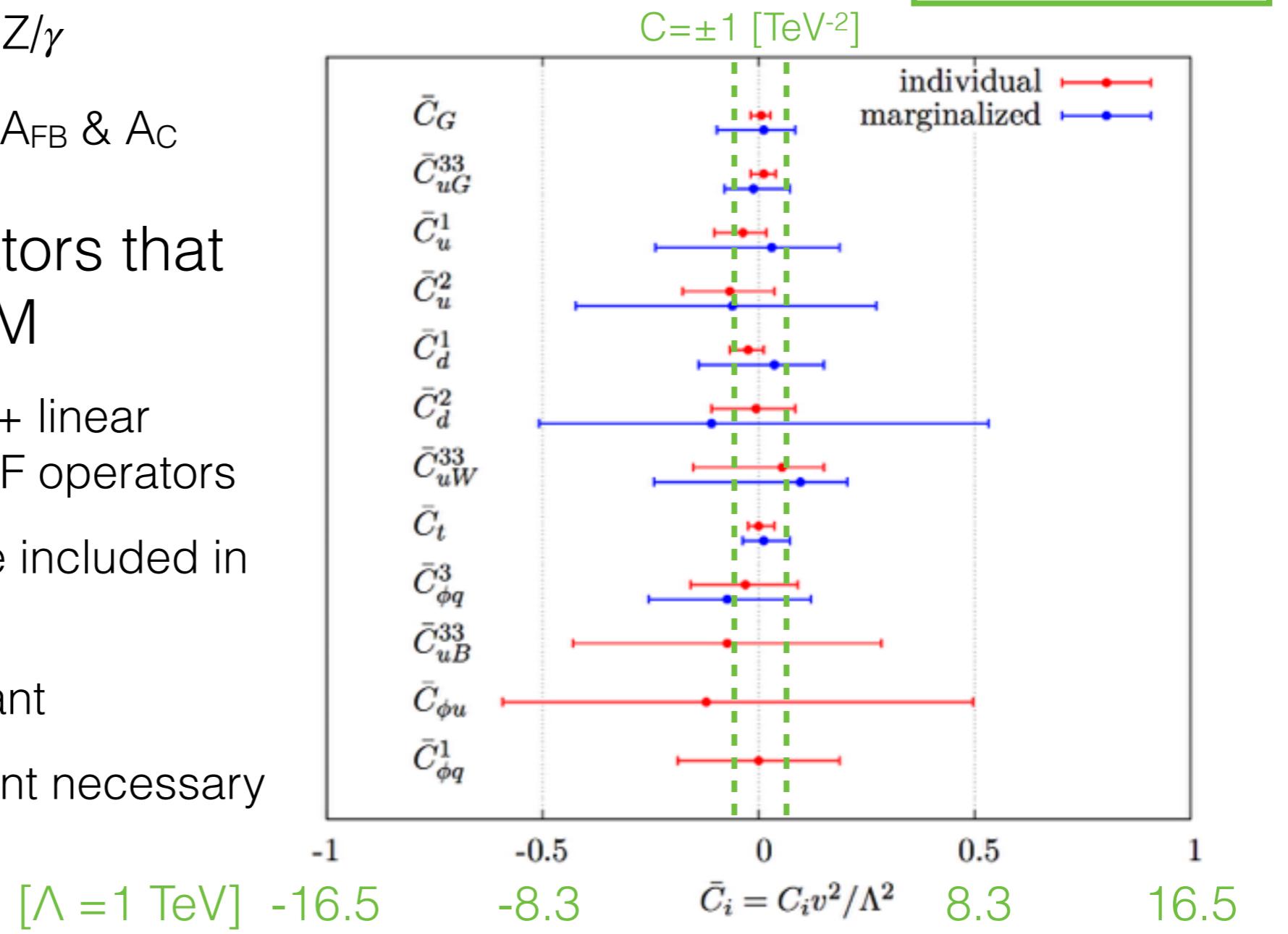
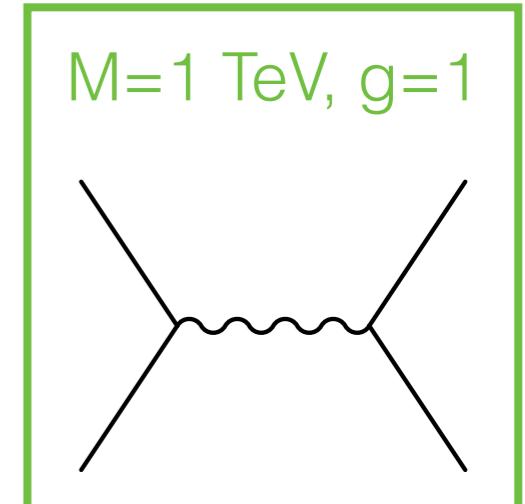
Status: global fits

- TopFitter collaboration: global SMEFT analysis of Top data
 - 195 measurements (of which 174 differential)

Dataset	\sqrt{s} (TeV)	Measurements	arXiv ref.	Dataset	\sqrt{s} (TeV)	Measurements	arXiv ref.	LHC 7 & 8 TeV
<i>Top pair production</i>								
Total cross-sections:								
ATLAS	7	lepton+jets	1406.5375	ATLAS	7	$p_T(t), M_{t\bar{t}}, y_t $	1407.0371	LHC 7 & 8 TeV
ATLAS	7	dilepton	1202.4892	CDF	1.96	$M_{t\bar{t}}$	0903.2850	Tevatron
ATLAS	7	lepton+tau	1205.3067	CMS	7	$p_T(t), M_{t\bar{t}}, y_t, y_{t\bar{t}}$	1211.2220	
ATLAS	7	lepton w/o b jets	1201.1889	CMS	8	$p_T(t), M_{t\bar{t}}, y_t, y_{t\bar{t}}$	1505.04480	
ATLAS	7	lepton w/ b jets	1406.5375	D \emptyset	1.96	$M_{t\bar{t}}, p_T(t), y_t $	1401.5785	
ATLAS	7	tau+jets	1211.7205	Differential cross-sections:				
ATLAS	7	$t\bar{t}, Z\gamma, WW$	1407.0573	ATLAS	7	$p_T(t), M_{t\bar{t}}, y_t $	1407.0371	
ATLAS	8	dilepton	1202.4892	CDF	1.96	$M_{t\bar{t}}$	0903.2850	
CMS	7	all hadronic	1302.0508	CMS	7	$p_T(t), M_{t\bar{t}}, y_t, y_{t\bar{t}}$	1211.2220	
CMS	7	dilepton	1208.2761	CDF	1.96	A_C (inclusive+ $M_{t\bar{t}}, y_{t\bar{t}}$)	1311.6742	
CMS	7	lepton+jets	1212.6682	D \emptyset	1.96	A_{FB} (inclusive+ $M_{t\bar{t}}, y_{t\bar{t}}$)	1402.3803	
CMS	7	lepton+tau	1203.6810	ATLAS	7	A_C (inclusive+ $M_{t\bar{t}}, y_{t\bar{t}}$)	1211.1003	
CMS	7	tau+jets	1301.5755	CMS	7	A_{FB} (inclusive+ $M_{t\bar{t}}, y_{t\bar{t}}$)	1405.0421	
CMS	8	dilepton	1312.7582	D \emptyset	1.96	A_{FB} (inclusive+ $M_{t\bar{t}}, y_{t\bar{t}}$)	1308.4050	
CDF + D \emptyset	1.96	Combined world average	1309.7570	CDF	1.96	Γ_{top}	1201.4156	
<i>Single top production</i>								
W-boson helicity fractions:								
ATLAS	7	t -channel (differential)	1406.7844	ATLAS	7		1205.2484	
CDF	1.96	s -channel (total)	1402.0484	CDF	1.96		1211.4523	
CMS	7	t -channel (total)	1406.7844	CMS	7		1308.3879	
CMS	8	t -channel (total)	1406.7844	D \emptyset	1.96		1011.6549	
D \emptyset	1.96	s -channel (total)	0907.4259	Run II data				
D \emptyset	1.96	t -channel (total)	1105.2788	CMS	13	$t\bar{t}$ (dilepton)	1510.05302	
<i>Associated production</i>								
ATLAS	7	$t\bar{t}\gamma$	1502.00586					
ATLAS	8	$t\bar{t}Z$	1509.05276					
CMS	8	$t\bar{t}Z$	1406.7830					

TopFitter

- Constrained a set of 12 operators at LO
 - tt, single-top & tt+Z/ γ
 - Helicity fractions, A_{FB} & A_C
- Selected operators that interfere with SM
 - ttg, tbW, ttZ, ggg + linear combinations of 4F operators
 - EFT² dependence included in observables
 - Impact is significant
 - Validity assessment necessary



Status: MC

- SM
 - NLO+PS predictions standard
 - FO EW corrections available
 - Automated tools abound
- SMEFT interpretations
 - Require their own MC tools
 - ‘Global’ implementation including all operators
 - EFT effects on signal & background
 - Higher order QCD predictions (see Marco’s talk on Monday)
 - Useful for sensitivity studies & experimental interpretations

Interpreting top-quark LHC measurements in the standard-model effective field theory

J. A. Aguilar Saavedra,¹ C. Degrande,² G. Durieux,³
 F. Maltoni,⁴ E. Vryonidou,² C. Zhang⁵ (editors),
 D. Barducci,⁶ I. Brivio,⁷ V. Cirigliano,⁸ W. Dekens,^{8,9} J. de Vries,¹⁰ C. Englert,¹¹
 M. Fabbrichesi,¹² C. Grojean,^{3,13} U. Haisch,^{2,14} Y. Jiang,⁷ J. Kamenik,^{15,16}
 M. Mangano,² D. Marzocca,¹² E. Mereghetti,⁸ K. Mimasu,⁴ L. Moore,⁴ G. Perez,¹⁷
 T. Plehn,¹⁸ F. Riva,² M. Russell,¹⁸ J. Santiago,¹⁹ M. Schulze,¹³ Y. Soreq,²⁰
 A. Tonero,²¹ M. Trott,⁷ S. Westhoff,¹⁸ C. White,²² A. Wulzer,^{2,23,24} J. Zupan.²⁵

- Consensus from the LHC top WG on SMEFT description for top physics
 - Classification of the relevant degrees of freedom (independent operators)
 - Prescription for staged implementation of flavor assumptions
 - Very nice overview & bigger picture discussion
- dim6top: FeynRules/UFO model provided
 - Useful to have a ‘unified’ & community validated tool
 - Avoid confusion of results presented in different bases, normalisations etc.
 - LO predictions only

All operators
previously
described
(including 4F)

<http://feynrules.irmp.ucl.ac.be/wiki/dim6top>

Going beyond

- State-of-the-art in MC event generation is well beyond LO
 - Software like FeynRules+NLOCT+MG5_aMC@NLO provides automated event generation at NLO in QCD from Lagrangian
- Some codes permit the inclusion of anomalous couplings
- SMEFT implementation is well motivated and a valuable addition to the NLO toolbox
- Great performance of the LHC for top processes
 - Complex/rare processes: differential tt, 4top, ttbb
 - EW induced: single-top, tt+Z/W/ γ /H, t+Z/H, tHW, ...
- Starting to probe full top/Higgs/EW sector

Going NLO

- Ultimate goal: a **precision global fit** of SMEFT to LHC observables at HL-LHC
- Step 1: **NLO QCD(+PS)** predictions
 - K-factors/shapes & control over PDF + scale uncertainties
- **NLO EW** corrections
 - Potentially important but much harder
 - Automation on the way with SHERPA, Madgraph5_aMC@NLO
- **RG-improved** predictions & **operator mixing**
 - Very helpful for cross checking NLO implementations
 - Compare to full NLO calculations, assess the importance of finite terms
[Alonso, Jenkins, Manohar & Trott; JHEP 1310 (2013) 087, JHEP 1401 (2014) 035 & JHEP 1404 (2014) 159]*

tH in SMEFT

$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu) \quad \gamma = \begin{pmatrix} -2 & 16 & 8 \\ 0 & -7/2 & 1/2 \\ 0 & 0 & 1/3 \end{pmatrix}$$

$$\begin{aligned} \mathcal{O}_{t\varphi} &= (\varphi^\dagger \varphi) (\bar{Q}_L \tilde{\varphi} t_R) \\ \mathcal{O}_{\varphi G} &= (\varphi^\dagger \varphi) G_{\mu\nu}^A G_A^{\mu\nu} \\ \mathcal{O}_{tG} &= (\bar{Q}_L \sigma_{\mu\nu} T^A t_R) \tilde{\varphi} G_A^{\mu\nu} \end{aligned}$$

- Operators involving the top/Higgs/gluon
 - gg→H & tt production partly constrain the Wilson coefficient space
 - ttH is the only direct probe of the Top-Higgs interaction
 - In principle 3-gluon \mathcal{O}_G and 4 fermion operators also contribute but turn out to be better constrained by tt and multi-jet measurements
- Different K-factors among SM/dim-6 operators
- Large Λ^{-4} effects in both shape & normalisation
 - Scenarios where “EFT-squared” terms are large but energy is below cutoff

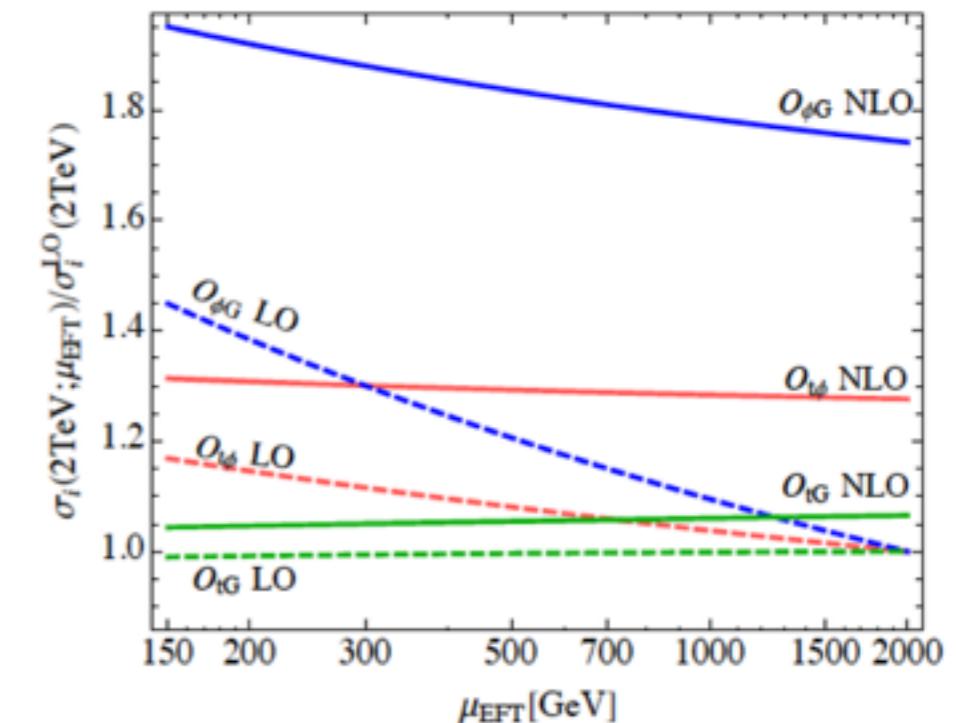
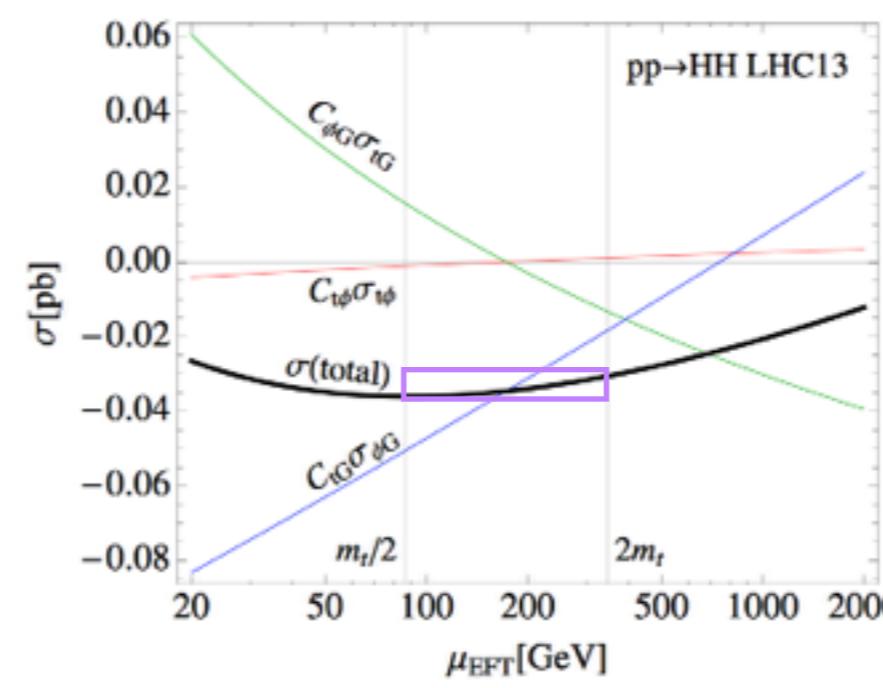
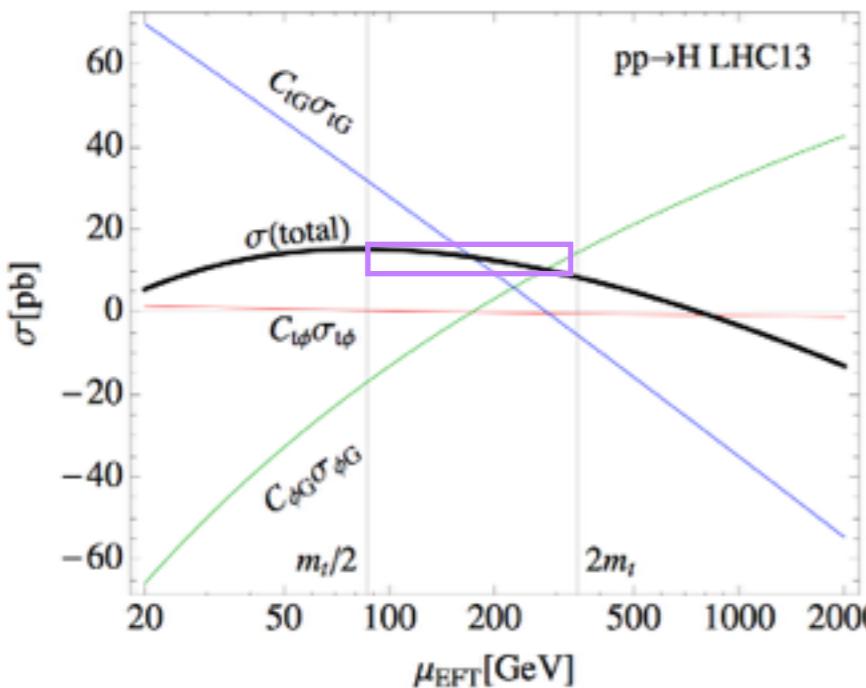
$$\frac{E^2}{\Lambda^2} < 1 < c_i^{(6)} \frac{E^2}{\Lambda^2} < c_i^{(6)} c_j^{(6)} \frac{E^4}{\Lambda^4}$$

tH in SMEFT

Update from ttH
signal strengths

$$c_{t\varphi} \subset [-6.5, 1.3] \text{ TeV}^{-2}$$

- Full NLO stable under scale variation
- Large finite terms: RG improved underestimates NLO
- EFT scale uncertainty estimate
 - Take c_i defined at scales $2\mu_0$ & $\mu_0/2$ and run back to the central scale



$\delta\mu_{\text{EFT}}$:
Does not cancel in
e.g. cross section
ratios

SMEFT@NLO

- MC tool for top/EW/Higgs sector of SMEFT
- Use Warsaw basis for definiteness

• Tools for translation between bases [Falkowski et al.; EPJC 75 (12) 1-14]
rosetta.hepforge.org

		Gauge/Higgs	
Higgs vev & kinetic term m_Z (cust. sym.)	\mathcal{O}_φ	$(\varphi^\dagger \varphi)^3$	—
	$\mathcal{O}_{\varphi \square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	—
	$\mathcal{O}_{\varphi D}$	$(\varphi^\dagger D_\mu \varphi)^\dagger (\varphi^\dagger D_\mu \varphi)$	—
	$\mathcal{O}_{\varphi G}$	$\varphi^\dagger \varphi G_A^{\mu\nu} G_{\mu\nu}^A$	$\mathcal{O}_{\varphi \tilde{G}}$
	$\mathcal{O}_{\varphi W}$	$\varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$	$\mathcal{O}_{\varphi \tilde{W}}$
	$\mathcal{O}_{\varphi B}$	$\varphi^\dagger \varphi B^{\mu\nu} B_{\mu\nu}$	$\mathcal{O}_{\varphi \tilde{B}}$
	$\mathcal{O}_{\varphi WB}$	$\varphi^\dagger \sigma^i \varphi W_i^{\mu\nu} B_{\mu\nu}$	$\mathcal{O}_{\varphi W \tilde{B}}$
	\mathcal{O}_{3W}	$\epsilon^{ijk} W_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^\mu$	$\mathcal{O}_{3\tilde{W}}$
		CP violation in v2	

SMEFT@NLO

Based on:

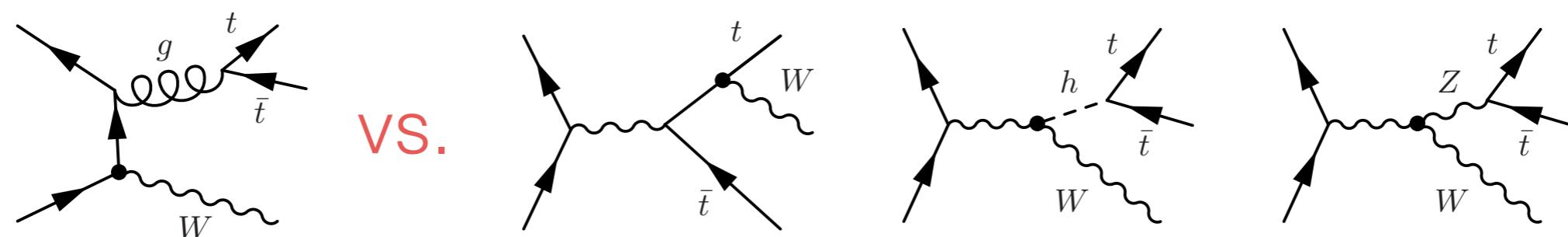
[Degrande et al; EPJC 77 (2017) 4, 262]
 [Maltoni et al; JHEP 1610 (2016) 123]
 [Bylund et al.; JHEP 1605 (2016) 052]
 [Zhang; PRL 116 (2016) 162002]

- Work in $U(3)^3 \times U(2)^2$ hypothesis, keeping only y_t non-zero
- Validate with existing implementations where available

	3 rd generation		Flavor universal 1 st & 2 nd	
	Top		Light	
Yukawa	$\mathcal{O}_{t\varphi}$	$(\varphi^\dagger \varphi) (\bar{Q} t) \tilde{\varphi}$	$\mathcal{O}_{\varphi l}^{(3)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{l} \gamma^\mu \sigma_i l)$
	\mathcal{O}_{tG}	$(\bar{Q} \sigma_{\mu\nu} T^A t) \tilde{\varphi} G_A^{\mu\nu}$	$\mathcal{O}_{\varphi l}^{(1)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{l} \gamma^\mu l)$
	\mathcal{O}_{tW}	$(\bar{Q} \sigma_{\mu\nu} \tau^i t) \tilde{\varphi} W_i^{\mu\nu}$	$\mathcal{O}_{\varphi u}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{e} \gamma^\mu e)$
	\mathcal{O}_{tB}	$(\bar{Q} \sigma_{\mu\nu} t) \tilde{\varphi} B^{\mu\nu}$	$\mathcal{O}_{\varphi q}^{(3)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{q} \gamma^\mu \sigma_i q)$
	$\mathcal{O}_{\varphi Q}^{(3)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{Q} \gamma^\mu \sigma_i Q)$	$\mathcal{O}_{\varphi q}^{(1)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{q} \gamma^\mu q)$
	$\mathcal{O}_{\varphi Q}^{(1)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{Q} \gamma^\mu Q)$	$\mathcal{O}_{\varphi u}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{u} \gamma^\mu u)$
	$\mathcal{O}_{\varphi t}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{t} \gamma^\mu t)$	$\mathcal{O}_{\varphi d}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{d} \gamma^\mu d)$
	$\mathcal{O}_{\varphi b}$	$i(\tilde{\varphi} D_\mu \varphi) (\bar{b} \gamma^\mu t)$	+ 4F operators from dim6top	

Case study: tZj/tHj

- Processes involving top+Higgs/W/Z
 - Interesting set of LHC-accessible processes to study EW sector + top
 - Unitarity cancellations \leftrightarrow top mass generation mechanism
- Previous $t\bar{t}+X$ EFT studies considered QCD contributions
 - In the SM, pure EW contributions 2 orders of magnitude smaller
 - EFT effects can strongly enhance these due to unitarity-violating behaviour



- SMEFT interpretation different from anomalous couplings
 - Quantitative power counting/expansion for high energy behaviour

Case study: tZj/tHj

- Alternative to tt+X: require a **single top quark**
 - Eliminates dominant QCD contribution
- Single top rate at 13 TeV LHC ~ 200 pb (1/4 of QCD tt)
 - Sensitive to **2 four-fermion** and **3 top/EW** operators that modify tbW vertex
- Require the presence of an additional **Z** or **Higgs**
 - Unique possibility of probing large set of top/Higgs/EW operators at once
 - Processes at the heart of EWSB sector
 - **Higher thresholds** may enhance EFT effects
- Recent LHC measurement of tZj cross section at 4.2σ
- Timely moment to perform EFT sensitivity study in this pair of challenging processes & showcase model implementation

Operators

tHj

tZj

both

NLO

\mathcal{O}_W	$\varepsilon_{IJK} W_{\mu\nu}^I W^{J,\nu\rho} W^{K,\mu}_{\rho}$	$\mathcal{O}_{\varphi Q}^{(3)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \tau_I \varphi)(\bar{Q} \gamma^\mu \tau^I Q) + \text{h.c.}$
• $\mathcal{O}_{\varphi W}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) W_I^{\mu\nu} W_{\mu\nu}^I$	• $\mathcal{O}_{\varphi Q}^{(1)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{Q} \gamma^\mu Q) + \text{h.c.}$
• $\mathcal{O}_{\varphi WB}$	$(\varphi^\dagger \tau_I \varphi) B^{\mu\nu} W_{\mu\nu}^I$	• $\mathcal{O}_{\varphi t}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{t} \gamma^\mu t) + \text{h.c.}$
• $\mathcal{O}_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^\dagger (\varphi^\dagger D_\mu \varphi)$	• $\mathcal{O}_{\varphi tb}$	$i(\tilde{\varphi} D_\mu \varphi)(\bar{t} \gamma^\mu b) + \text{h.c.}$
• $\mathcal{O}_{\varphi \square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	• $\mathcal{O}_{\varphi q}^{(1)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{q}_i \gamma^\mu q_i) + \text{h.c.}$
• $\mathcal{O}_{t\varphi}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) \bar{Q} t \tilde{\varphi} + \text{h.c.}$	• $\mathcal{O}_{\varphi q}^{(3)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \tau_I \varphi)(\bar{q}_i \gamma^\mu \tau^I q_i) + \text{h.c.}$
• \mathcal{O}_{tW}	$i(\bar{Q} \sigma^{\mu\nu} \tau_I t) \tilde{\varphi} W_{\mu\nu}^I + \text{h.c.}$	• $\mathcal{O}_{\varphi u}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{u}_i \gamma^\mu u_i) + \text{h.c.}$
• \mathcal{O}_{tB}	$i(\bar{Q} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu} + \text{h.c.}$	• $\mathcal{O}_{Qq}^{(3,1)}$	$(\bar{q}_i \gamma_\mu \tau_I q_i)(\bar{Q} \gamma^\mu \tau^I Q)$
• \mathcal{O}_{tG}^*	$i(\bar{Q} \sigma^{\mu\nu} T_A t) \tilde{\varphi} G_{\mu\nu}^A + \text{h.c.}$	• $\mathcal{O}_{Qq}^{(3,8)}$	$(\bar{q}_i \gamma_\mu \tau_I T_A q_i)(\bar{Q} \gamma^\mu \tau^I T^A Q)$

Constrained by electroweak precision tests (LEP)

RGE

Two blind directions in Warsaw basis:

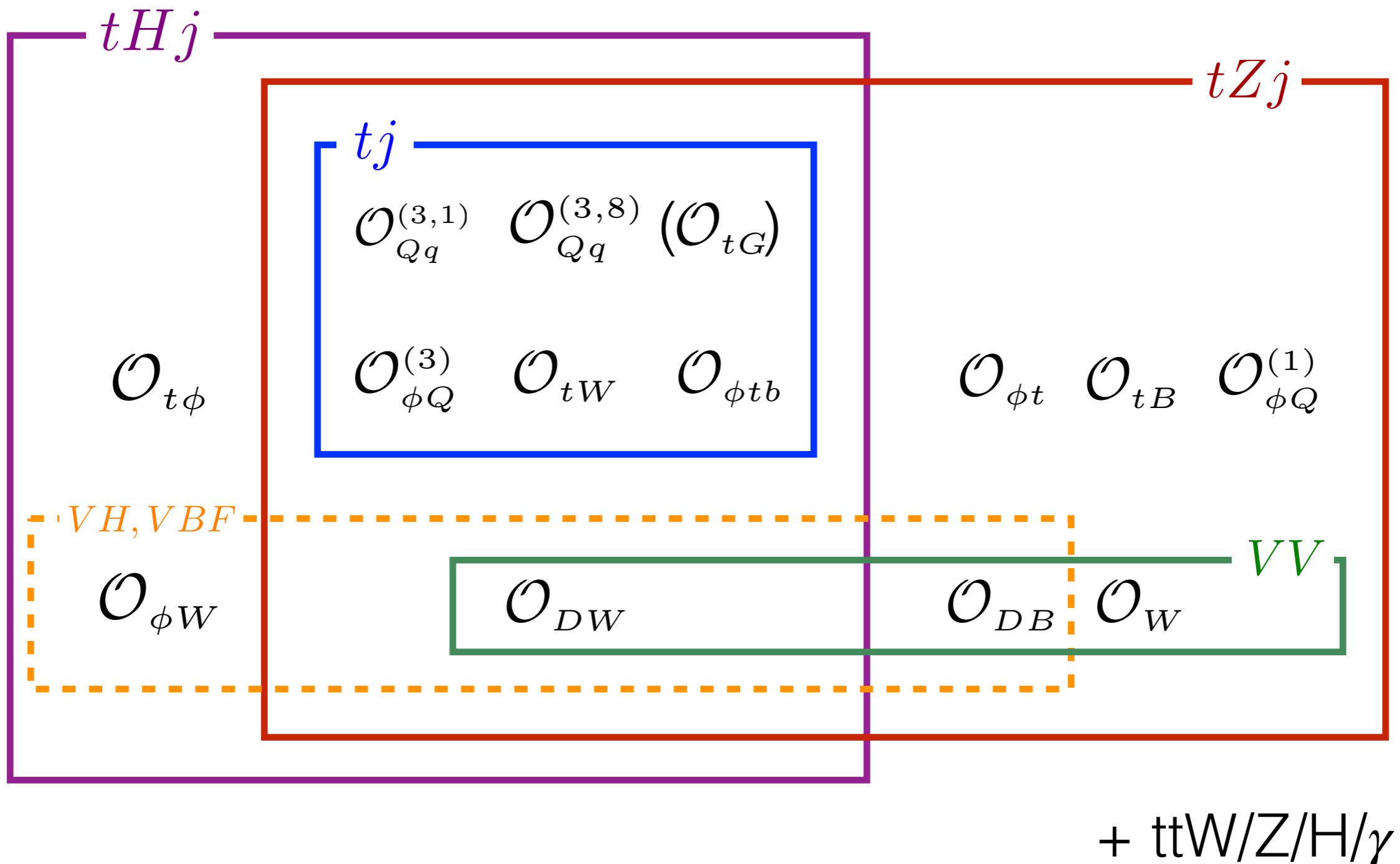
$$\mathcal{O}_{HW} = (D^\mu \varphi)^\dagger \tau_I (D^\nu \varphi) W_{\mu\nu}^I$$

$$\mathcal{O}_{HB} = (D^\mu \varphi)^\dagger (D^\nu \varphi) B_{\mu\nu}.$$

$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu), \quad \gamma = \begin{pmatrix} -2 & 0 & 0 \\ 0 & 2/3 & 0 \\ 0 & 0 & 2/3 \end{pmatrix}$$

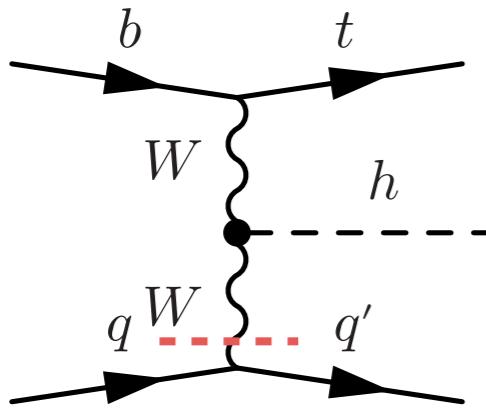
Consider these two instead to assess orthogonal sensitivity of tZj/tHj

Interplay



Anatomy of tHj/tZj

tHj (tZj = h \rightarrow Z)

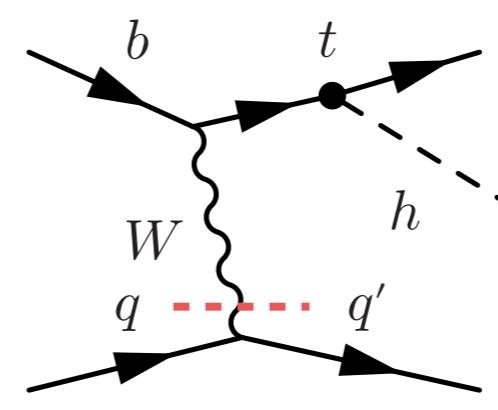


$$\mathcal{O}_{\varphi W} : \varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$$

HWW

TGC

$$\mathcal{O}_W : \epsilon^{ijk} W_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^{\mu}$$

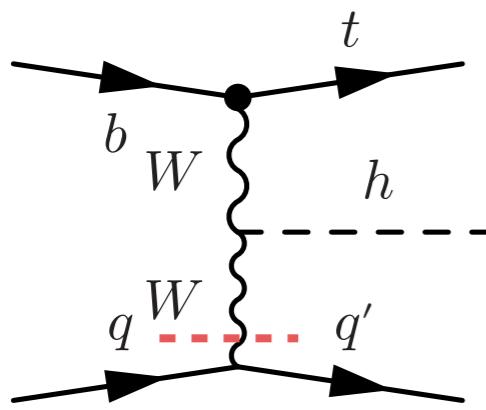


$$\mathcal{O}_{t\varphi}$$

top Yukawa

ttZ coupling

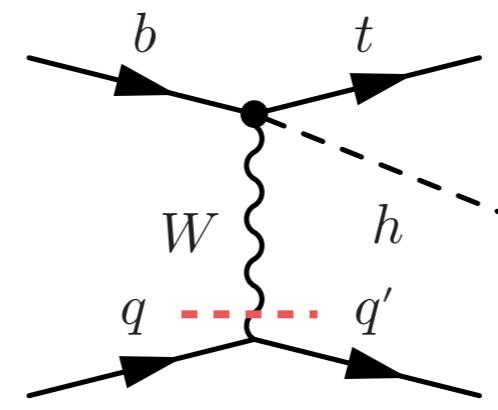
$$\mathcal{O}_{\varphi t}$$



$$\mathcal{O}_{\varphi Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi)(\bar{Q} \gamma^\mu \sigma_i Q)$$

Wtb vertex

$$\mathcal{O}_{\varphi tb} : i(\tilde{\varphi} D_\mu \varphi)(\bar{b} \gamma^\mu t)$$



$$\mathcal{O}_{\varphi Q}^{(3)}$$

Contact terms

$$\mathcal{O}_{tb}$$

- Accessing the bW \rightarrow tH & bW \rightarrow tZ sub-amplitudes
 - Rich interplay between EFT operators from different sectors
 - Different energy growth and interference with the SM

Anatomy of tHj

- LO helicity amplitudes

- High energy limit: $s \sim -t \gg v^2$

- Maximum energy growth

- SU(2) triplet current
- Interferes with leading SM
- RH Charged Current
- Weak dipole

- Fields strengths source transverse gauge bosons
- Not captured by Goldstone equiv.

- Subleading energy growth

- $\propto m_t$ & interferes with sub-leading SM amplitude → no growth

bW → tH (bW → tZ in backup)

$\lambda_b, \lambda_W, \lambda_t$	SM	$\mathcal{O}_{t\varphi}$	$\mathcal{O}_{\varphi Q}^{(3)}$	$\mathcal{O}_{\varphi W}$	\mathcal{O}_{tW}	\mathcal{O}_{HW}
-,-,-	s^0	s^0	$\sqrt{s(s+t)}$	s^0	s^0	$\sqrt{s(s+t)}$
-,-,+/-,+,-	$\frac{1}{\sqrt{s}}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W s}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$
-,-,-/-,-,+/-,+,-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$	$m_W\sqrt{-t}$	$\frac{m_W s}{\sqrt{-t}}$	$m_t\sqrt{-t}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
-,-,+/-,+,-	$\frac{1}{s}$	s^0	s^0	—	$\sqrt{s(s+t)}$	$\frac{1}{s}$
-,+,-/-,+,-	$\frac{1}{\sqrt{s}}$	—	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
-,+,-/-,+,-	s^0	—	s^0	s^0	s^0	$\frac{1}{s}$

$\mathcal{O}_{\varphi tb}, \lambda_b = +$			
λ_t	0	+	-
λ_W	0	+	-
+	$\sqrt{s(s+t)}$	$m_W\sqrt{-t}$	$\frac{1}{\sqrt{s}}$
-	$m_t\sqrt{-t}$	s^0	s^0

Consistent with non-interference theorem in $2 \rightarrow 2$

[Cheung & Shen;
PRL 115 (2015) 071601]
[Azatov, Contino & Riva;
PRD 95 (2017) 065014]

LHC sensitivity

Compare to single top which has a much larger rate

$r = \sigma_i / \sigma_{SM}$	tj $(p_T^t > 350 \text{ GeV})$	tj $(p_T^t > 350 \text{ GeV})$	tZj $(p_T^t > 250 \text{ GeV})$	tZj $(p_T^t > 250 \text{ GeV})$	tHj
σ_{SM}	224 pb	880 fb	839 fb	69 fb	75.9 fb
r_{tw}	0.0275	0.024	0.016	0.010	0.292
$r_{tw,tw}$	0.0162	0.35	0.095	0.67	0.940
$r_{\varphi Q^{(3)}}$	0.121	0.121	0.192	0.172	-0.132
$r_{\varphi Q^{(3)}, \varphi Q^{(3)}}$	0.0037	0.0037	0.029	0.114	0.21
$r_{\varphi tb, \varphi tb}$	0.00090	0.0008	0.0050	0.027	0.050
r_{tG}	0.0003	-0.01	0.00053	-0.0048	-0.0055
$r_{tG,tG}$	0.00062	0.045	0.0027	0.022	0.025
$r_{Qq^{(3,1)}}$	-0.353	-4.4	-0.59	-2.22	-0.39
$r_{Qq^{(3,1)}, Qq^{(3,1)}}$	0.126	11.5	0.65	5.1	1.21
$r_{Qq^{(3,8)}, Qq^{(3,8)}}$	0.0308	2.73	0.133	1.01	1.08

Increased sensitivity
for weak dipoles

Consistent with $2 \rightarrow 2$
subamplitude analysis

New energy growths
w.r.t single top

Single top should
eventually outperform
 tHj/tZj for four fermion
operators

Results

- Non-universal K-factors
- Reduction in scale+PDF uncertainties
 - EFT scale uncertainty subdominant
- Room for $O(1)$ deviations within existing limits
 - Relative impact of EFT contributions larger in tHj than tZj
 - tZj has much larger rate: differential measurements possible
- Future projections: high p_T tZj vs inclusive tHj
 - Competitive/improved sensitivity w.r.t existing limits (e.g. helicity fractions)
 - Weak dipole operators, RHCC, SU(2) triplet current
- High p_T single top measurements best for 4F operators

Global top/Higgs/EW

- Several interesting $2 \rightarrow 2$ sub-amplitudes

$$bW \rightarrow tH : tHj$$

$$bW \rightarrow tZ : tZj$$

photon final
states: $t\gamma j, \dots$

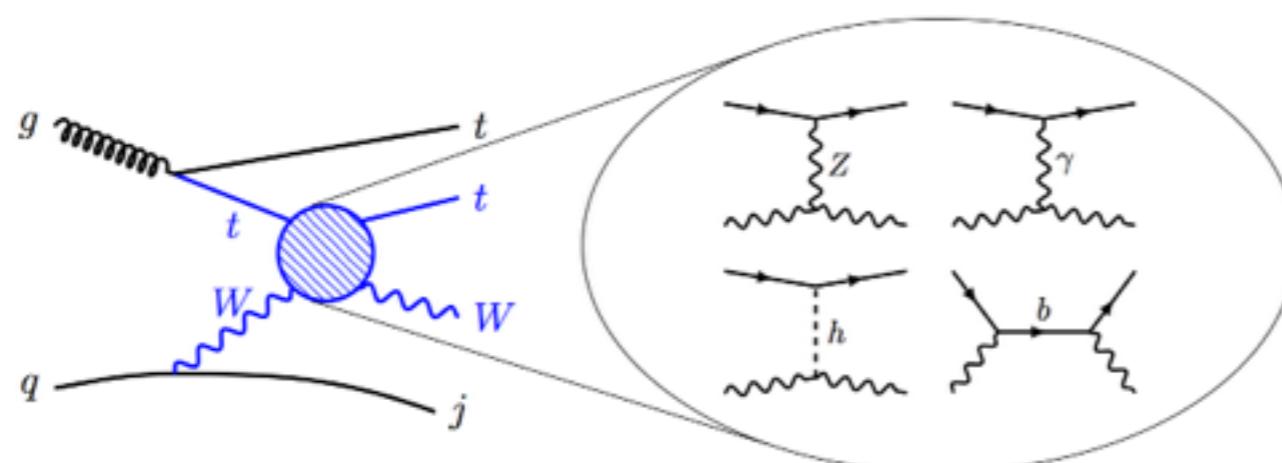
$$tW \rightarrow tW : ttW \text{ (EW)}$$

$$tZ \rightarrow tH : ttH \text{ (EW)}$$

$$tZ \rightarrow tZ : ttZ$$

$$tH \rightarrow tH : ttHH?$$

- Possibly access higher energies by e.g. $ttW+j$



Even more rare:
 $ttWW, ttZZ,$
 $ttZH, ttHH, \dots$

[Dror et al.; JHEP 01 (2016) 071]

Global top/Higgs/EW

- Clear that a **global effort** must be undertaken
- **Individual** measurements of these processes may not easily lend themselves to EFT interpretation
- e.g. CMS measurement of ttW/ttZ cross section ratio
 - “**Backgrounds**”: ttH, tqZ, tHq,...
 - Considerable statistical overlap between different top+EW measurements
 - Abundant use of multivariate methods
- SMEFT interpretation = going beyond individual processes
- Global fits to top & EW observables exist separately
 - Unifying top/Higgs/EW sector a valuable exercise
 - SMEFTatNLO model implementation a necessary ingredient

Top 4F operators

- Generated by heavy, new physics coupling to 3rd generation
 - Top mass generation
- Manageable set of operators
- Contain tttt, ttbb and bbbb interactions
 - Colour singlet & triplet
 - Vector & scalar currents

- $O_{QQ}^1 = (\bar{Q} \gamma_\mu Q) (\bar{Q} \gamma^\mu Q)$,
- $O_{QQ}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{Q} \gamma^\mu T^A Q)$,
- $O_{tt}^1 = (\bar{t} \gamma_\mu t) (\bar{t} \gamma_\mu t)$,
- $O_{tb}^1 = (\bar{t} \gamma_\mu t) (\bar{b} \gamma_\mu b)$,
- $O_{tb}^8 = (\bar{t} \gamma_\mu T^A t) (\bar{b} \gamma_\mu T^A b)$,
- $O_{Qt}^1 = (\bar{Q} \gamma_\mu Q) (\bar{t} \gamma^\mu t)$,
- $O_{Qt}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{t} \gamma^\mu T^A t)$,
- $O_{Qb}^1 = (\bar{Q} \gamma_\mu Q) (\bar{b} \gamma^\mu b)$,
- $O_{Qb}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{b} \gamma^\mu T^A b)$,
- $O_{QtQb}^1 = (\bar{Q} t) \varepsilon (\bar{Q} b)$,
- $O_{QtQb}^8 = (\bar{Q} T^A t) \varepsilon (\bar{Q} T^A b)$
- four top

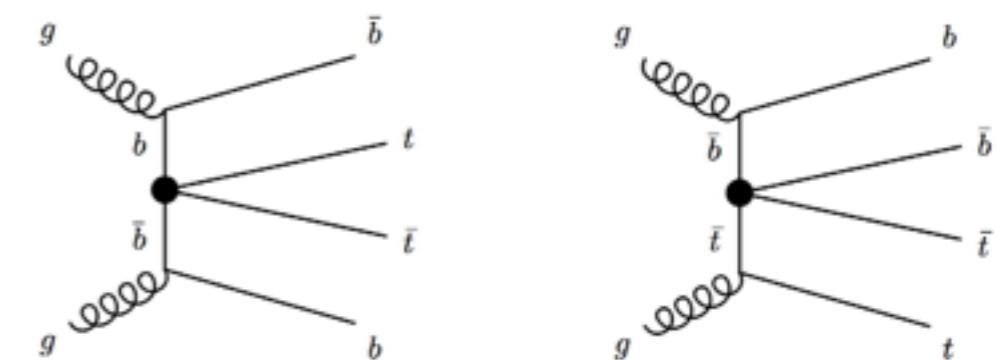
Four top production

- Very **rare** process at the LHC $\sim 9 \text{ fb}$
 - Best effort at the LHC about 4.6 times the SM [ATLAS-CONF-2016-104]
[Zhang; Chin. Phys. C42 (2018) 023104]
- Not a precision measurement
 - Sensitive to four heavy quark & 2 heavy + 2 light quark operators
 - High threshold $\sim 700 \text{ GeV}$
 - Sensitivity dominated by quadratic terms & beyond = validity issue?

$$\begin{aligned} c_{Qt}^1 & [-4.97, 4.90] \quad (E_{cut} = 3 \text{ TeV}) \\ [\text{TeV}^{-2}] \quad c_{Qt}^8 & [-10.3, 9.33] \quad (E_{cut} = 3 \text{ TeV}) \\ c_{tt}^1 & [-2.92, 2.80] \quad (E_{cut} = 3 \text{ TeV}) \end{aligned}$$

[Aguilar-Saavedra et al.; arXiv:1802.07237]

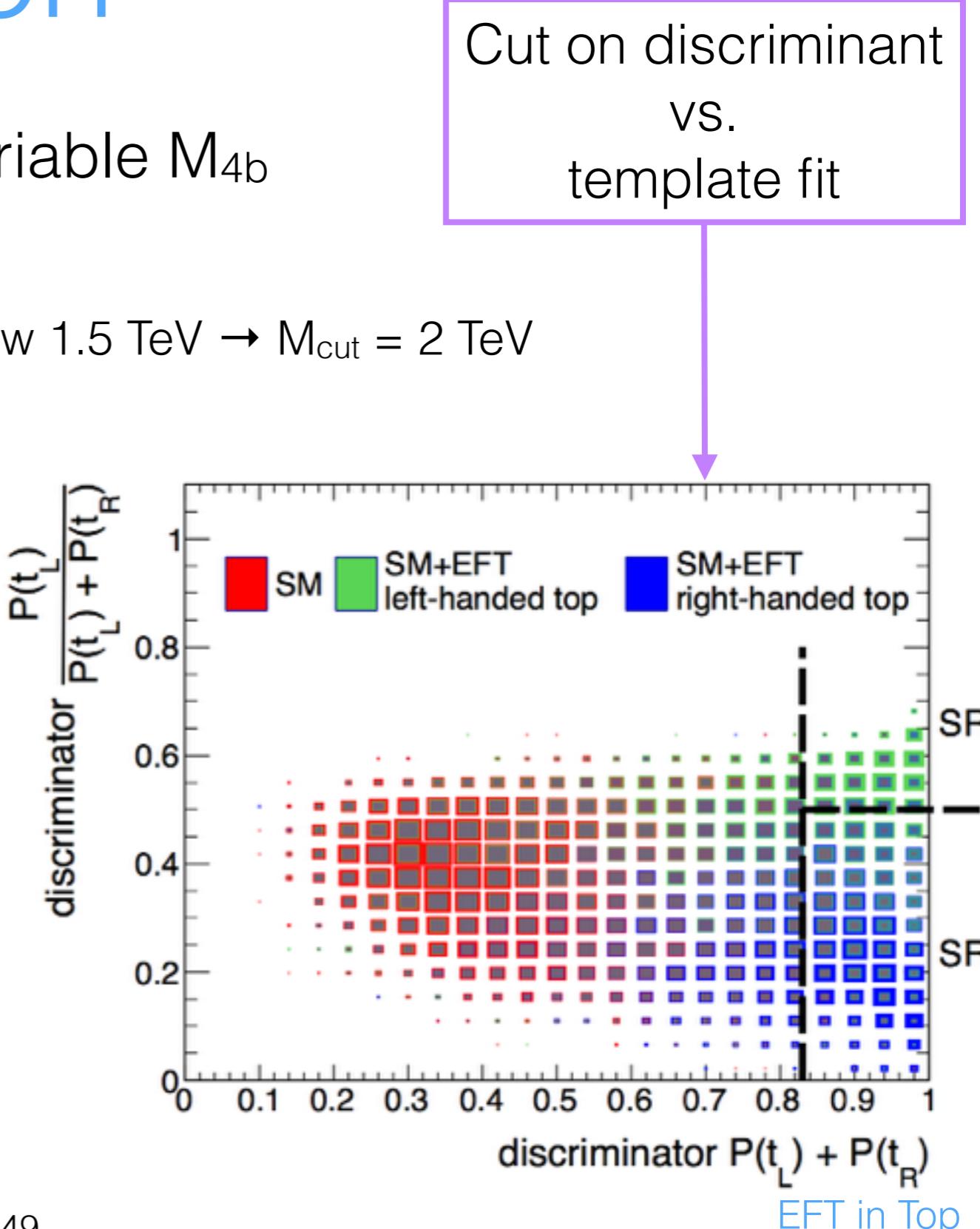
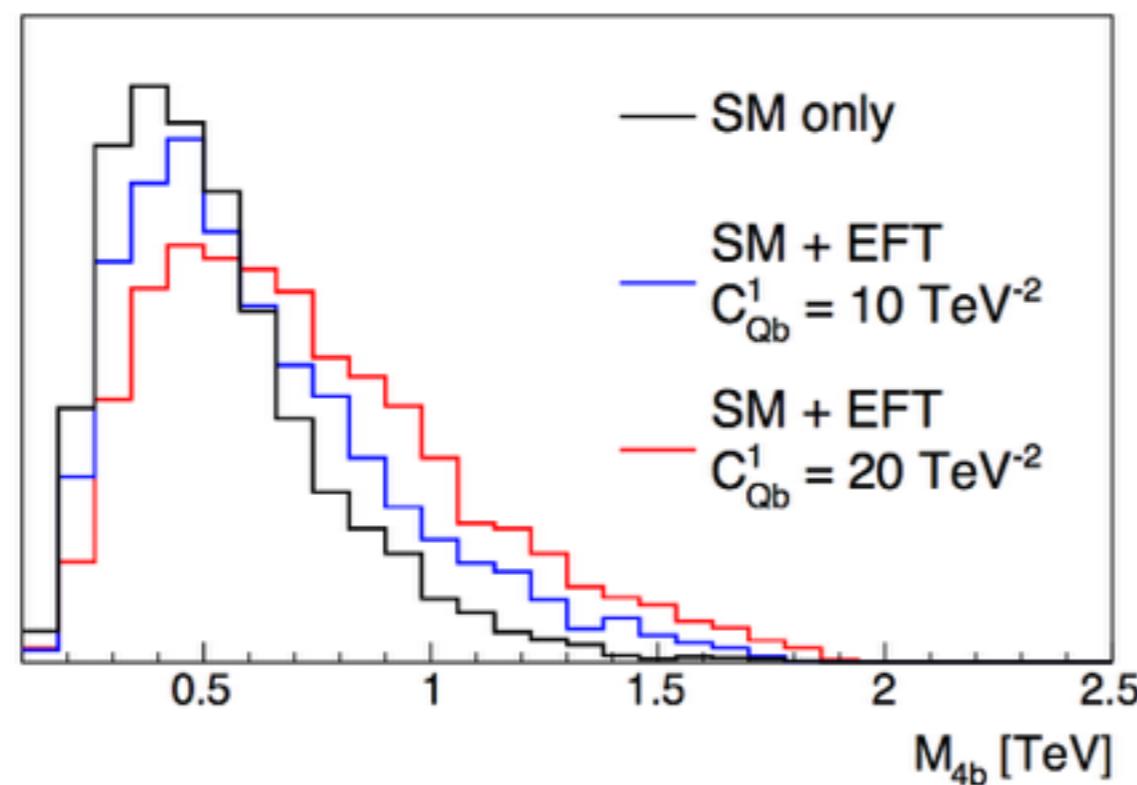
ttbb production



- Less rare process at the LHC $\sim 3 \text{ pb}$
 - Measured at the LHC with $\sim 30\%$ accuracy [CMS; PLB 776 (2018) 355-378]
 - Background for ttH(bb)
- Affected by all but one of the previous list of operators
 - Some of which have never been bounded before
[Degrande et al.; JHEP 03 (2011) 125]
- Sensitivity of ttbb to four heavy operators
 - Future projections of dedicated analyses optimised to EFT kinematics
 - Sensitivity may exceed that of 4 top for common operators
 - Modulo a resolution of the large theory uncertainties in the SM
 - Once again, dominated by quadratic terms

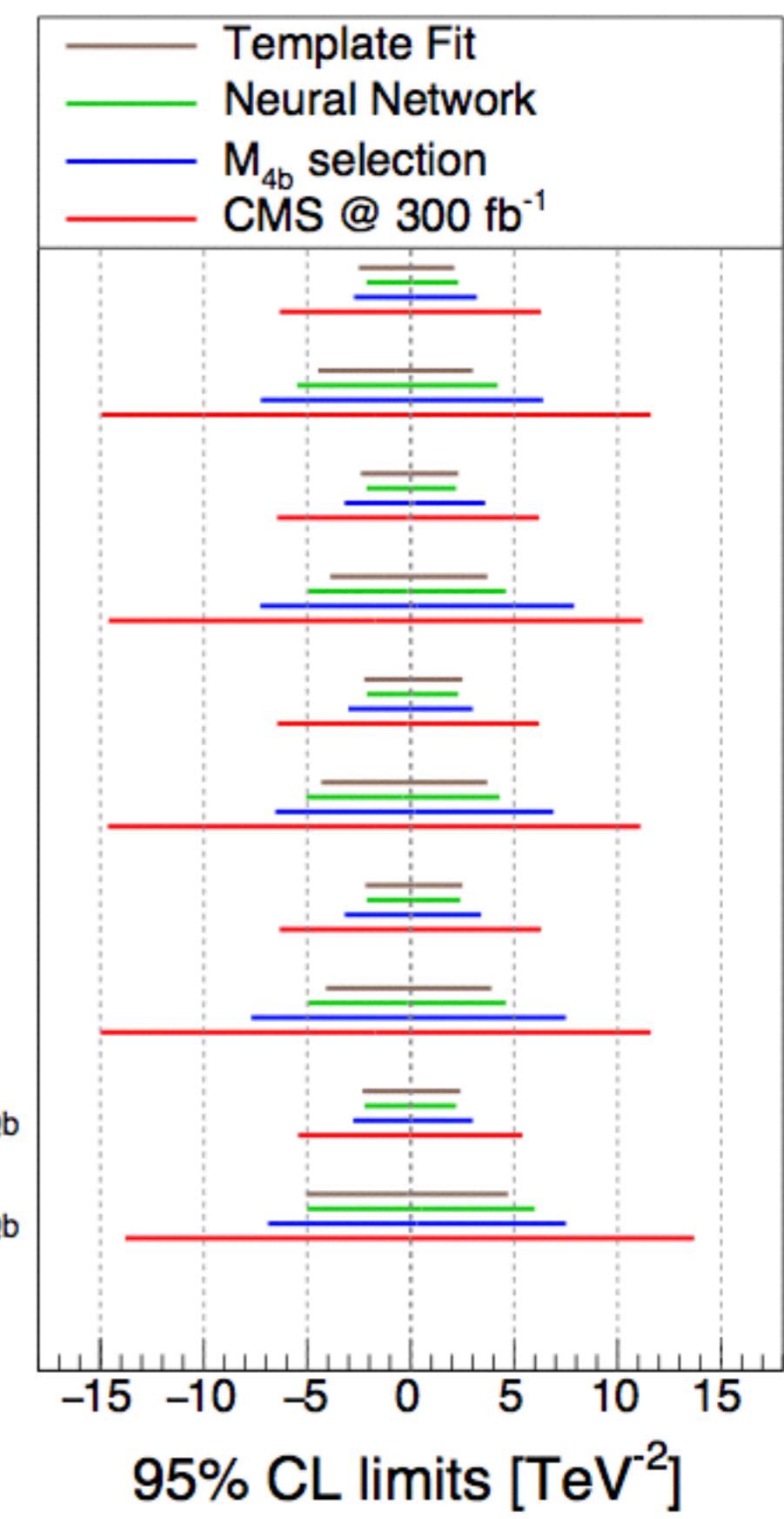
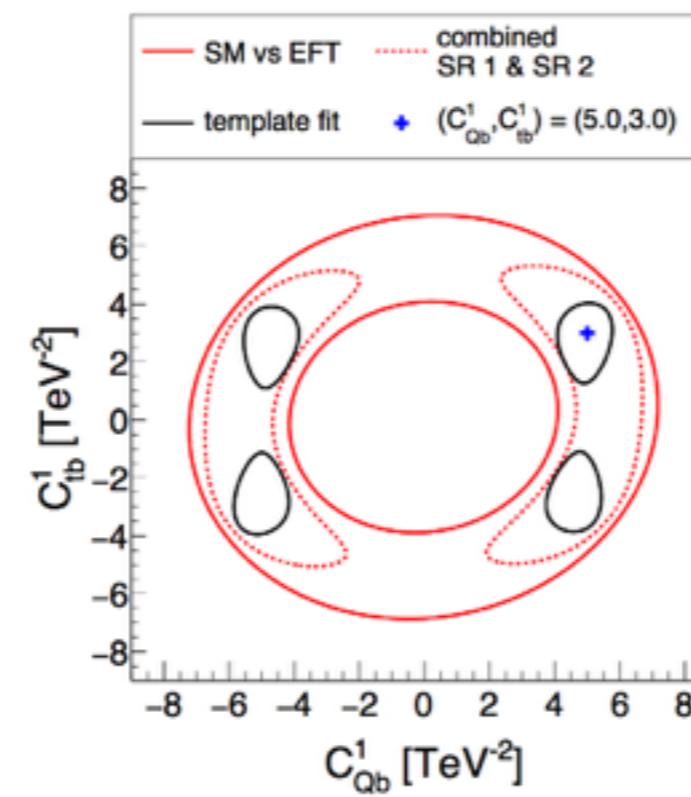
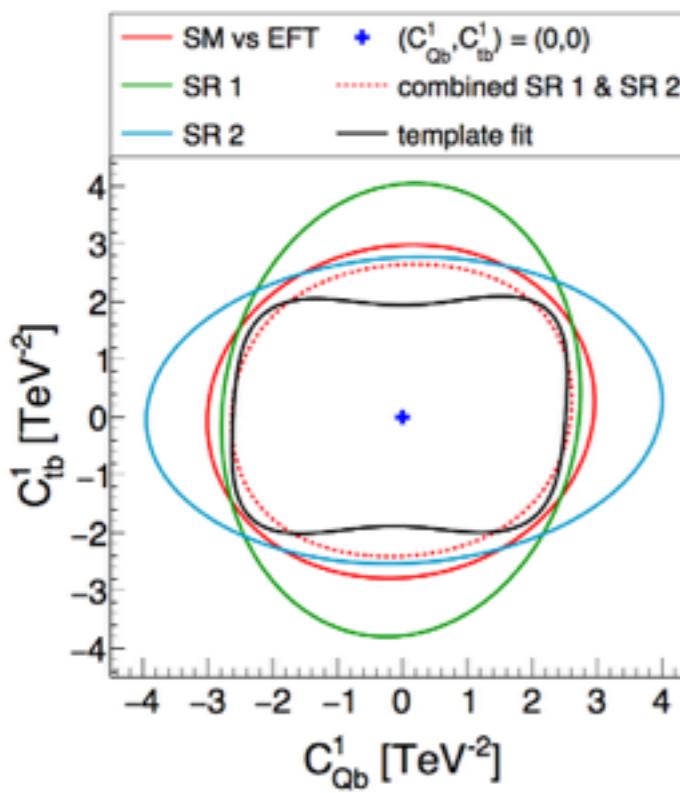
ttbb production

- “High energy” kinematic variable M_{4b}
 - Bulk of sensitivity to 4F operators
 - Sensitivity comes from events below 1.5 TeV $\rightarrow M_{\text{cut}} = 2 \text{ TeV}$
- Multi class NN discriminant
 - SM vs t_L operators vs t_R operators



ttbb production

- SM observation
 - Template fit to NN similar to M_{4b}
- EFT signal injection
 - NN focuses in on preferred parameters



Conclusion

- SMEFT: consistent framework to **stress-test** the SM
 - Theory consensus for global description & MC implementation
 - Extended to top/Higgs/EW sector & NLO in QCD
 - Towards a global likelihood
- **Global** view of top/Higgs/EW measurements
 - Blurring the line between **signal** & **background**
 - Different approach needed?
 - Ensure measurements can be interpreted by a global SMEFT fit
- Many unexplored processes
 - New sensitivity studies ripe for the picking!
 - Single MC tool available for all top/Higgs/EW processes at the LHC

Thank you

Anatomy of tZj

bW → tZj

$\lambda_b, \lambda_W, \lambda_t, \lambda_Z$	SM	$\mathcal{O}_{\varphi Q}^{(3)}$	$\mathcal{O}_{\varphi Q}^{(1)}$	$\mathcal{O}_{\varphi t}$	\mathcal{O}_{tB}	\mathcal{O}_{tW}	\mathcal{O}_W	\mathcal{O}_{HW}	\mathcal{O}_{HB}
-,-,0,-,0	s^0	$\sqrt{s(s+t)}$	-	-	-	s^0	s^0	$\sqrt{s(s+t)}$	s^0
-,-,0,+,0	$\frac{1}{\sqrt{s}}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$m_Z\sqrt{-t}$	$\frac{m_W(2s+3t)}{\sqrt{-t}}$	-	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$
-,-,-,-,0	$\frac{1}{\sqrt{s}}$	$m_W\sqrt{-t}$	-	-	-	-	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$m_W\sqrt{-t}$	$\frac{1}{\sqrt{s}}$
-,-,-,+,0	$\frac{1}{s}$	s^0	s^0	s^0	s^0	$\sqrt{s(s+t)}$	s^0	s^0	$\frac{1}{\sqrt{s}}$
-,-,0,-,-	$\frac{1}{\sqrt{s}}$	$m_W\sqrt{-t}$	-	-	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$\frac{m_W(ss_W^2+2t)}{\sqrt{-t}}$	$\frac{m_W s}{\sqrt{-t}}$
-,-,0,-,+	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
-,-,0,+, -	s^0	s^0	-	-	-	s^0	s^0	s^0	s^0
-,-,0,+, +	$\frac{1}{s}$	s^0	s^0	s^0	$\sqrt{s(s+t)}$	$\sqrt{s(s+t)}$	-	s^0	s^0
-,-,+,-,0	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
-,-,+,-,0	s^0	s^0	-	-	-	s^0	-	s^0	$\frac{1}{s}$
-,-,-,-,-	s^0	s^0	-	s^0	-	s^0	s^0	s^0	s^0
-,-,-,-,+	$\frac{1}{s}$	-	-	-	-	-	$\sqrt{s(s+t)}$	s^0	s^0
-,-,-,+,-	$\frac{1}{\sqrt{s}}$	-	-	-	-	$\frac{m_Z(s_W^2 t - 3 c_W^2 (2s+t))}{\sqrt{-t}}$	-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
-,-,-,+,+	-	-	-	$m_W\sqrt{-t}$	$m_Z\sqrt{-t}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$
-,-,+,-,-	$\frac{1}{s}$	-	-	-	-	$\sqrt{s(s+t)}$	s^0	s^0	s^0
-,-,+,-,+	s^0	s^0	-	-	-	-	s^0	s^0	s^0
-,-,+,-,-	$\frac{1}{\sqrt{s}}$	-	-	-	-	$m_t\sqrt{-t}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
-,-,+,-,+	$\frac{1}{\sqrt{s}}$	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$

$\mathcal{O}_{\varphi tb}, \lambda_b, \lambda_t = +, +$			
λ_W	0	+	-
λ_Z	$\sqrt{s(s+t)}$	$m_W\sqrt{-t}$	-
0	$\sqrt{s(s+t)}$	$m_W\sqrt{-t}$	-
+	$m_Z\sqrt{-t}$	s^0	-
-	-	-	s^0

$\mathcal{O}_{\varphi tb}, \lambda_b, \lambda_t = +, -$			
λ_W	0	+	-
λ_Z	$-$	$-$	s^0
0	$-$	$-$	s^0
+	s^0	$-$	$-$
-	s^0	$-$	$-$

Consistent with
non-interference
theorem in $2 \rightarrow 2$

[Cheung & Shen;
PRL 115 (2015) 071601]
[Azatov, Contino & Riva;
PRD 95 (2017) 065014]

σ [fb]	LO	NLO	K-factor
σ_{SM}	$57.56(4)^{+11.2\%}_{-7.4\%} \pm 10.2\%$	$75.87(4)^{+2.2\%}_{-6.4\%} \pm 1.2\%$	1.32
$\sigma_{\varphi W}$	$8.12(2)^{+13.1\%}_{-9.3\%} \pm 9.3\%$	$7.76(2)^{+7.0\%}_{-6.3\%} \pm 1.0\%$	0.96
$\sigma_{\varphi W, \varphi W}$	$5.212(7)^{+10.6\%}_{-6.8\%} \pm 10.2\%$	$6.263(7)^{+2.6\%}_{-7.8\%} \pm 1.3\%$	1.20
$\sigma_{t\varphi}$	$-1.203(6)^{+12.0\%}_{-15.6\%} \pm 8.9\%$	$-0.246(6)^{+144.5[31.4]\%}_{-157.8[19.0]\%} \pm 2.1\%$	0.20
$\sigma_{t\varphi, t\varphi}$	$0.6682(9)^{+12.7\%}_{-8.9\%} \pm 9.6\%$	$0.7306(8)^{+4.6[0.6]\%}_{-7.3[0.2]\%} \pm 1.0\%$	1.09
σ_{tW}	$19.38(6)^{+13.0\%}_{-9.3\%} \pm 9.4\%$	$22.18(6)^{+3.8[0.4]\%}_{-6.8[0.9]\%} \pm 1.0\%$	1.14
$\sigma_{tW, tW}$	$46.40(8)^{+9.3\%}_{-5.5\%} \pm 11.1\%$	$71.24(8)^{+7.4[1.5]\%}_{-14.0[6.9]\%} \pm 1.9\%$	1.54
$\sigma_{\varphi Q^{(3)}}$	$-3.03(3)^{+0.0\%}_{-2.2\%} \pm 15.4\%$	$-10.04(4)^{+11.1\%}_{-8.9\%} \pm 1.8\%$	3.31
$\sigma_{\varphi Q^{(3)}, \varphi Q^{(3)}}$	$11.23(2)^{+9.4\%}_{-5.6\%} \pm 11.2\%$	$15.28(2)^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.36
$\sigma_{\varphi tb}$	0	0	—
$\sigma_{\varphi tb, \varphi tb}$	$2.752(4)^{+9.4\%}_{-5.5\%} \pm 11.3\%$	$3.768(4)^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.54
σ_{HW}	$-3.526(4)^{+5.6\%}_{-9.5\%} \pm 10.9\%$	$-5.27(1)^{+6.5\%}_{-2.9\%} \pm 1.5\%$	1.50
$\sigma_{HW, HW}$	$0.9356(4)^{+7.9\%}_{-4.0\%} \pm 12.3\%$	$1.058(1)^{+4.8\%}_{-11.9\%} \pm 2.3\%$	1.13
σ_{tG}		$-0.418(5)^{+12.3\%}_{-9.8\%} \pm 1.1\%$	—
$\sigma_{tG, tG}$		$1.413(1)^{+21.3\%}_{-30.6\%} \pm 2.5\%$	—
$\sigma_{Qq^{(3,1)}}$	$-22.50(5)^{+8.0\%}_{-11.8\%} \pm 9.7\%$	$-20.10(5)^{+13.8\%}_{-13.3\%} \pm 1.1\%$	0.89
$\sigma_{Qq^{(3,1)}, Qq^{(3,1)}}$	$69.78(3)^{+8.0\%}_{-4.1\%} \pm 12.1\%$	$62.20(3)^{+11.5\%}_{-15.9\%} \pm 2.3\%$	0.89
$\sigma_{Qq^{(3,8)}}$	—	$0.25(3)^{+25.4\%}_{-27.1\%} \pm 4.7\%$	—
$\sigma_{Qq^{(3,8)}, Qq^{(3,8)}}$	$15.53(2)^{+8.0\%}_{-4.1\%} \pm 12.1\%$	$14.07(2)^{+11.0\%}_{-15.7\%} \pm 2.1\%$	0.91

K-factors not universal

Reduction of
QCD scale/PDF
uncertainties

EFT scale uncertainty
subdominant

Some very strong
dependence on EFT
operators

O(>1) deviations within
current bounds

σ [fb]	LO	NLO	K-factor
σ_{SM}	$660.8(4)^{+13.7\%}_{-9.6\%} \pm 9.7\%$	$839.1(5)^{+1.1\%}_{-5.1\%} \pm 1.0\%$	1.27
σ_w	$-7.87(7)^{+8.4\%}_{-12.6\%} \pm 9.7\%$	$-8.77(8)^{+8.5\%}_{-4.3\%} \pm 1.1\%$	1.12
$\sigma_{w,w}$	$34.58(3)^{+8.2\%}_{-3.9\%} \pm 13.0\%$	$43.80(4)^{+6.6\%}_{-15.1\%} \pm 2.8\%$	1.27
σ_{tB}	$2.23(2)^{+14.7[0.9]\%}_{-10.7[1.0]\%} \pm 9.4\%$	$2.94(2)^{+2.3[0.4]\%}_{-3.0[0.7]\%} \pm 1.1\%$	1.32
$\sigma_{tB,tB}$	$2.833(2)^{+10.5[1.7]\%}_{-6.3[1.9]\%} \pm 11.1\%$	$4.155(3)^{+4.7[0.9]\%}_{-10.1[1.4]\%} \pm 1.7\%$	1.47
σ_{tW}	$2.66(4)^{+18.8[0.9]\%}_{-15.3[1.0]\%} \pm 11.4\%$	$13.0(1)^{+15.8[2.1]\%}_{-22.8[0.0]\%} \pm 1.2\%$	4.90
$\sigma_{tW,tW}$	$48.16(4)^{+10.0[1.7]\%}_{-5.8[1.9]\%} \pm 11.3\%$	$80.00(4)^{+7.9[1.3]\%}_{-14.7[1.6]\%} \pm 1.9\%$	1.66
$\sigma_{\varphi dtR}$	$4.20(1)^{+14.9\%}_{-10.9\%} \pm 9.3\%$	$4.94(2)^{+3.4\%}_{-6.7\%} \pm 1.0\%$	1.18
$\sigma_{\varphi dtR,\varphi dtR}$	$0.3326(3)^{+13.6\%}_{-9.5\%} \pm 9.6\%$	$0.4402(5)^{+3.7\%}_{-9.3\%} \pm 1.0\%$	1.32
$\sigma_{\varphi Q}$	$14.98(2)^{+14.5\%}_{-10.5\%} \pm 9.4\%$	$18.07(3)^{+2.3\%}_{-1.6\%} \pm 1.0\%$	1.21
$\sigma_{\varphi Q,\varphi Q}$	$0.7442(7)^{+14.1\%}_{-10.0\%} \pm 9.5\%$	$1.028(1)^{+2.8\%}_{-7.3\%} \pm 1.0\%$	1.38
$\sigma_{\varphi Q^{(3)}}$	$130.04(8)^{+13.8\%}_{-9.8\%} \pm 9.5\%$	$161.4(1)^{+0.9\%}_{-4.8\%} \pm 1.0\%$	1.24
$\sigma_{\varphi Q^{(3)},\varphi Q^{(3)}}$	$17.82(2)^{+11.7\%}_{-7.5\%} \pm 10.5\%$	$23.98(2)^{+3.7\%}_{-9.3\%} \pm 1.4\%$	1.35
$\sigma_{\varphi tb}$	0	0	—
$\sigma_{\varphi tb,\varphi tb}$	$2.949(2)^{+10.5\%}_{-6.2\%} \pm 11.1\%$	$4.154(4)^{+5.1\%}_{-11.2\%} \pm 1.8\%$	1.41
σ_{HW}	$-5.16(6)^{+7.8\%}_{-12.0\%} \pm 10.5\%$	$-6.88(8)^{+6.4\%}_{-2.0\%} \pm 1.4\%$	1.33
$\sigma_{HW,HW}$	$0.912(2)^{+9.4\%}_{-5.2\%} \pm 12.0\%$	$1.048(2)^{+5.2\%}_{-12.8\%} \pm 2.1\%$	1.15
σ_{HB}	$-3.015(9)^{+9.9\%}_{-13.9\%} \pm 9.5\%$	$-3.76(1)^{+5.2\%}_{-1.0\%} \pm 1.0\%$	1.25
$\sigma_{HB,HB}$	$0.02324(6)^{+12.7\%}_{-8.5\%} \pm 9.9\%$	$0.02893(6)^{+2.3\%}_{-7.5\%} \pm 1.1\%$	1.24
σ_{tG}		$0.45(2)^{+93.0\%}_{-148.8\%} \pm 4.9\%$	—
$\sigma_{tG,tG}$		$2.251(4)^{+20.9\%}_{-30.0\%} \pm 2.5\%$	—
$\sigma_{Qq^{(3,1)}}$	$-393.5(5)^{+8.1\%}_{-12.3\%} \pm 10.0\%$	$-498(1)^{+8.9\%}_{-3.2\%} \pm 1.2\%$	1.26
$\sigma_{Qq^{(3,1)},Qq^{(3,1)}}$	$462.25(3)^{+8.4\%}_{-4.1\%} \pm 12.7\%$	$545.50(5)^{+7.4\%}_{-17.4\%} \pm 2.9\%$	1.18
$\sigma_{Qq^{(3,8)}}$	0	$-0.9(3)^{+23.3\%}_{-26.3\%} \pm 19.2\%$	—
$\sigma_{Qq^{(3,8)},Qq^{(3,8)}}$	$102.73(5)^{+8.4\%}_{-4.1\%} \pm 12.7\%$	$111.18(5)^{+9.3\%}_{-18.4\%} \pm 2.8\%$	1.08

tZj ~ 10 times bigger than tHj

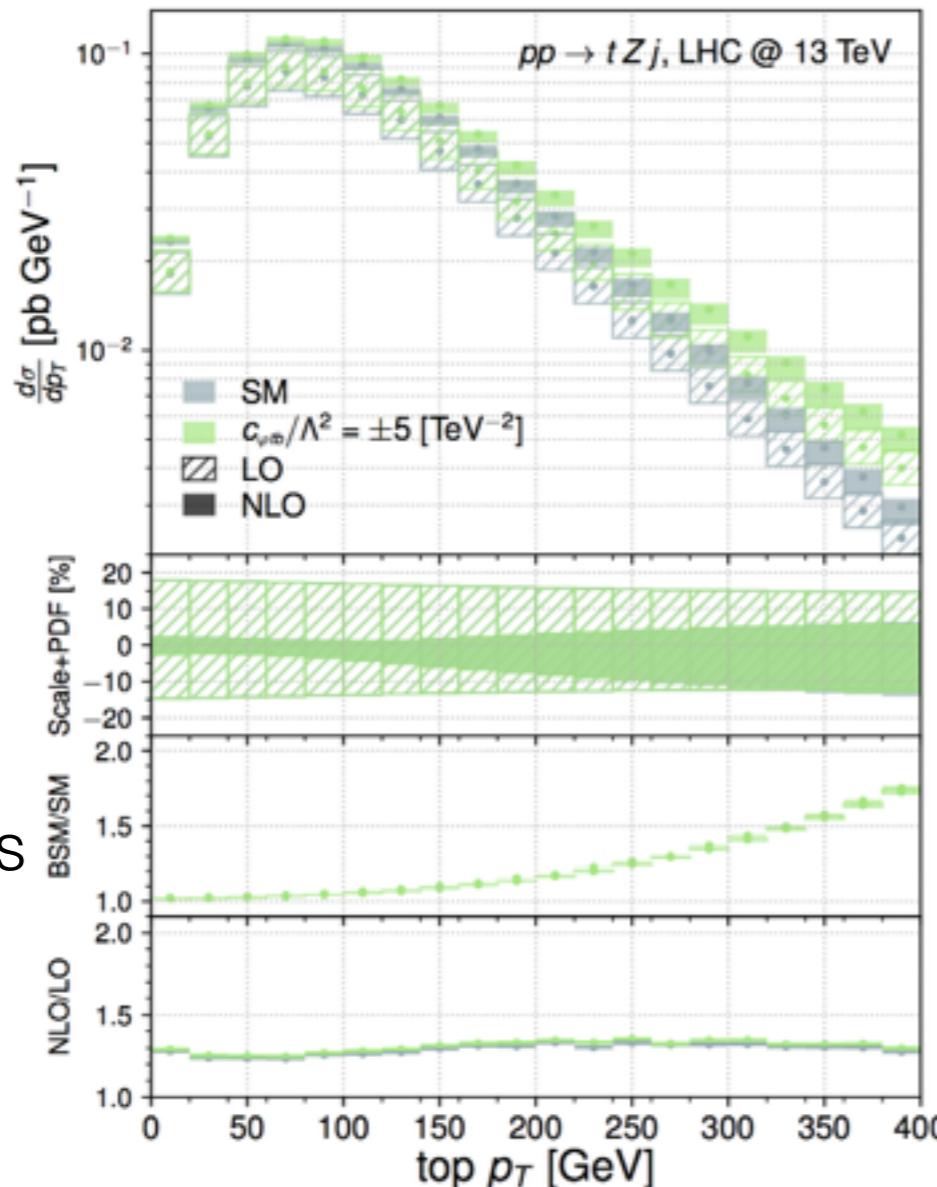
NLO corrections: similar features to tHj

EFT contributions smaller relative to SM

Higgs always radiated from top/EW gauge boson

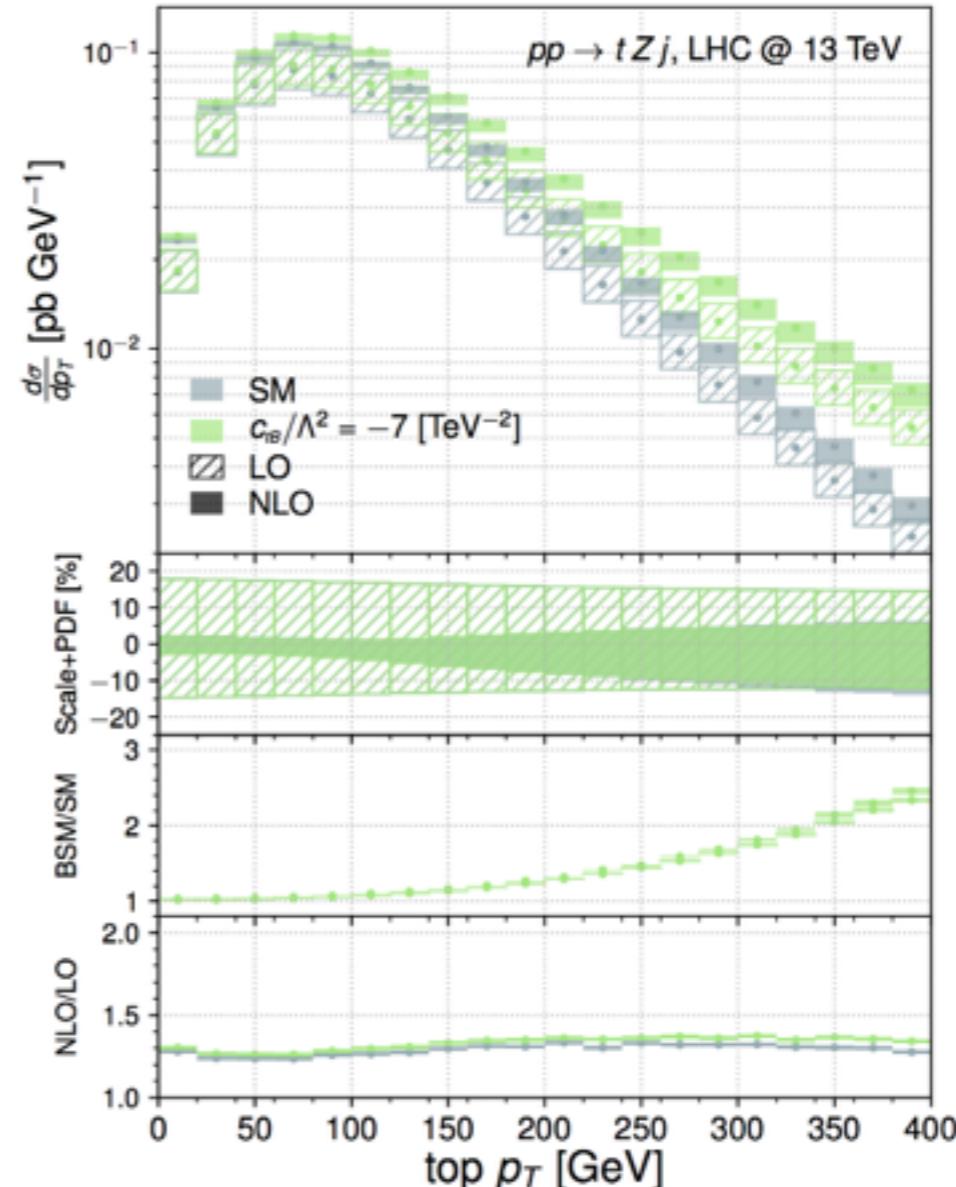
Z boson can also come from light quark leg

Differential tZj



Reduced
uncert.

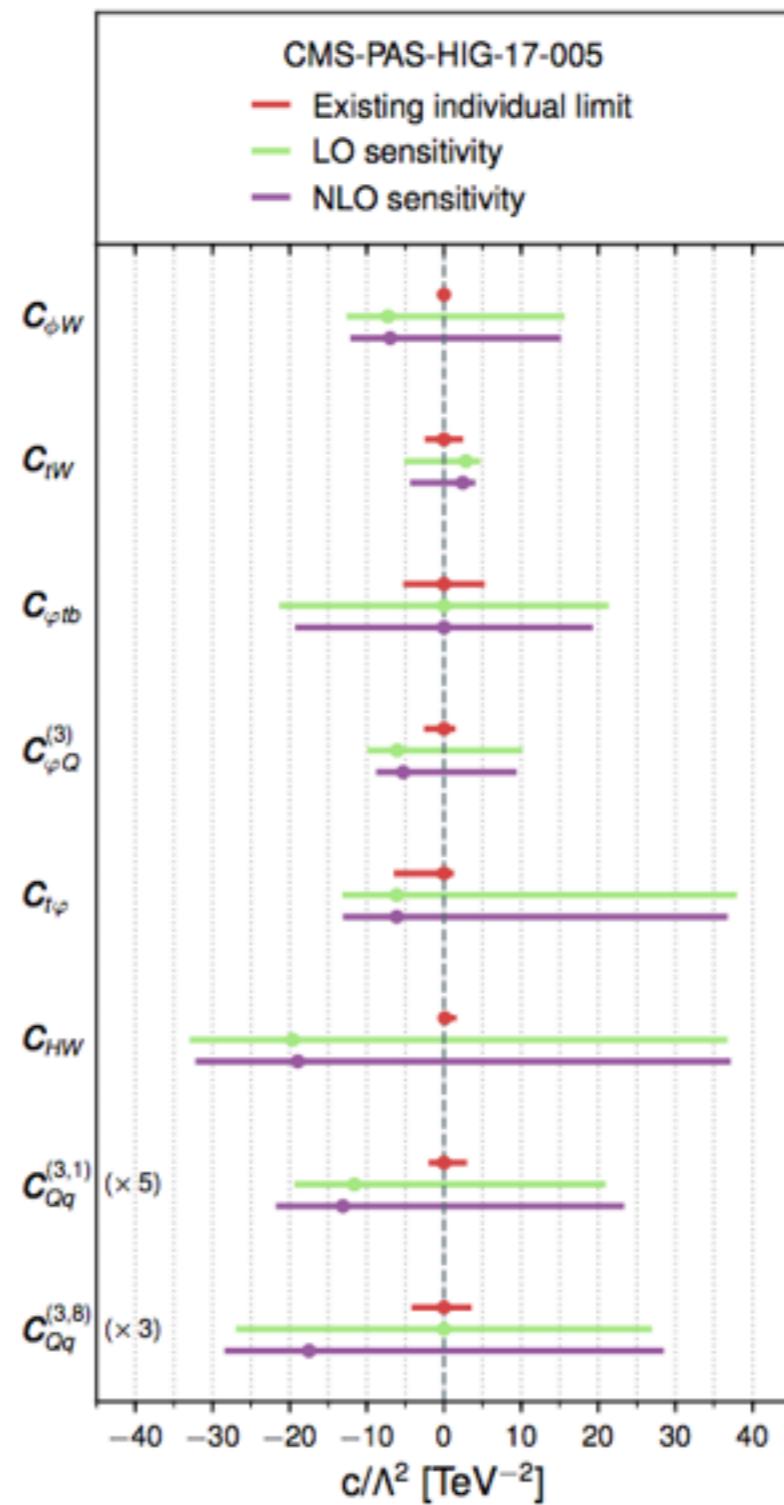
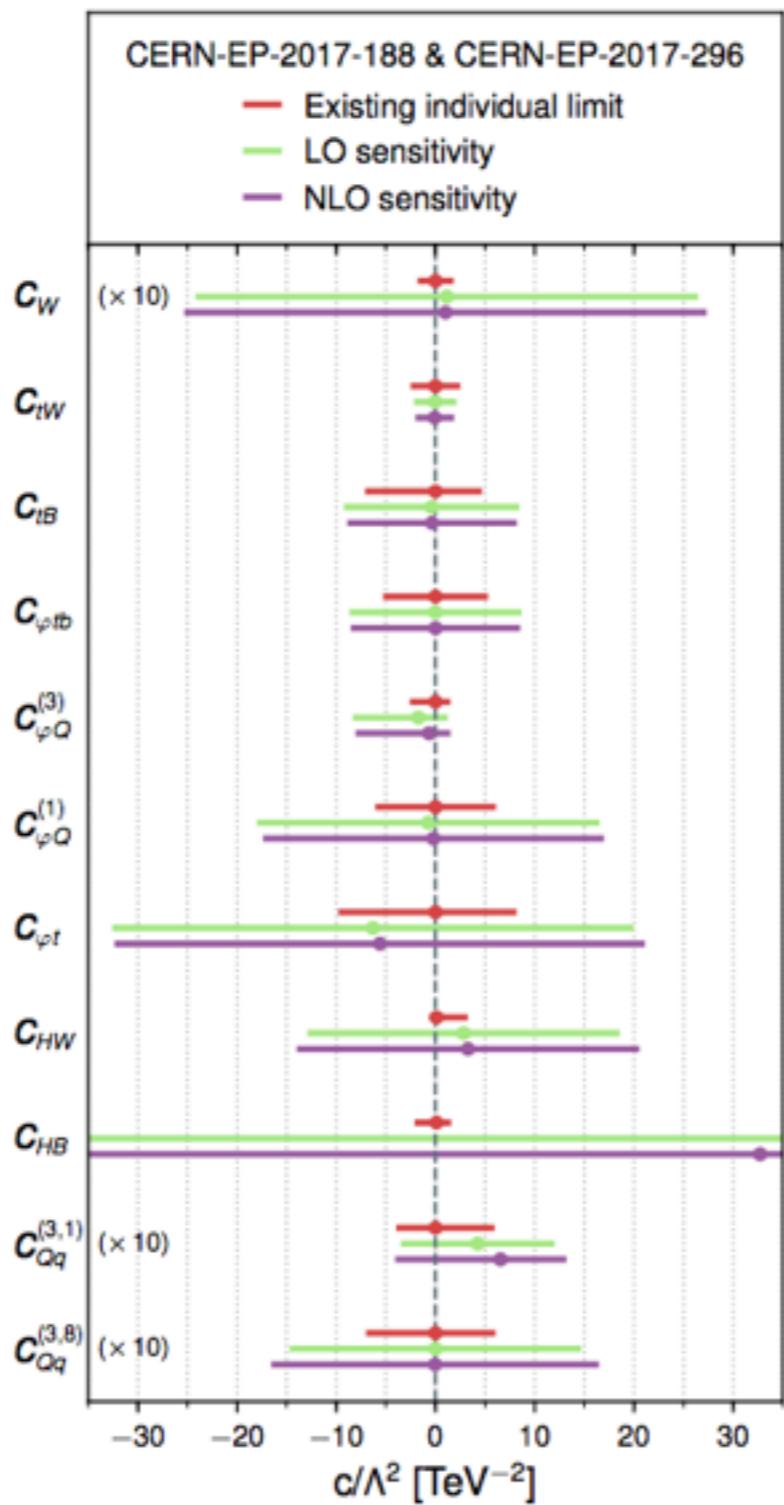
Large effects



Potentially large deviations in the tails (saturating current limits)
 tHj process is very rare, differential results not likely at LHC

Current sensitivity

tZj
TGC
Dipoles
RHCC
Currents
LEP
orthogonal
4-fermion

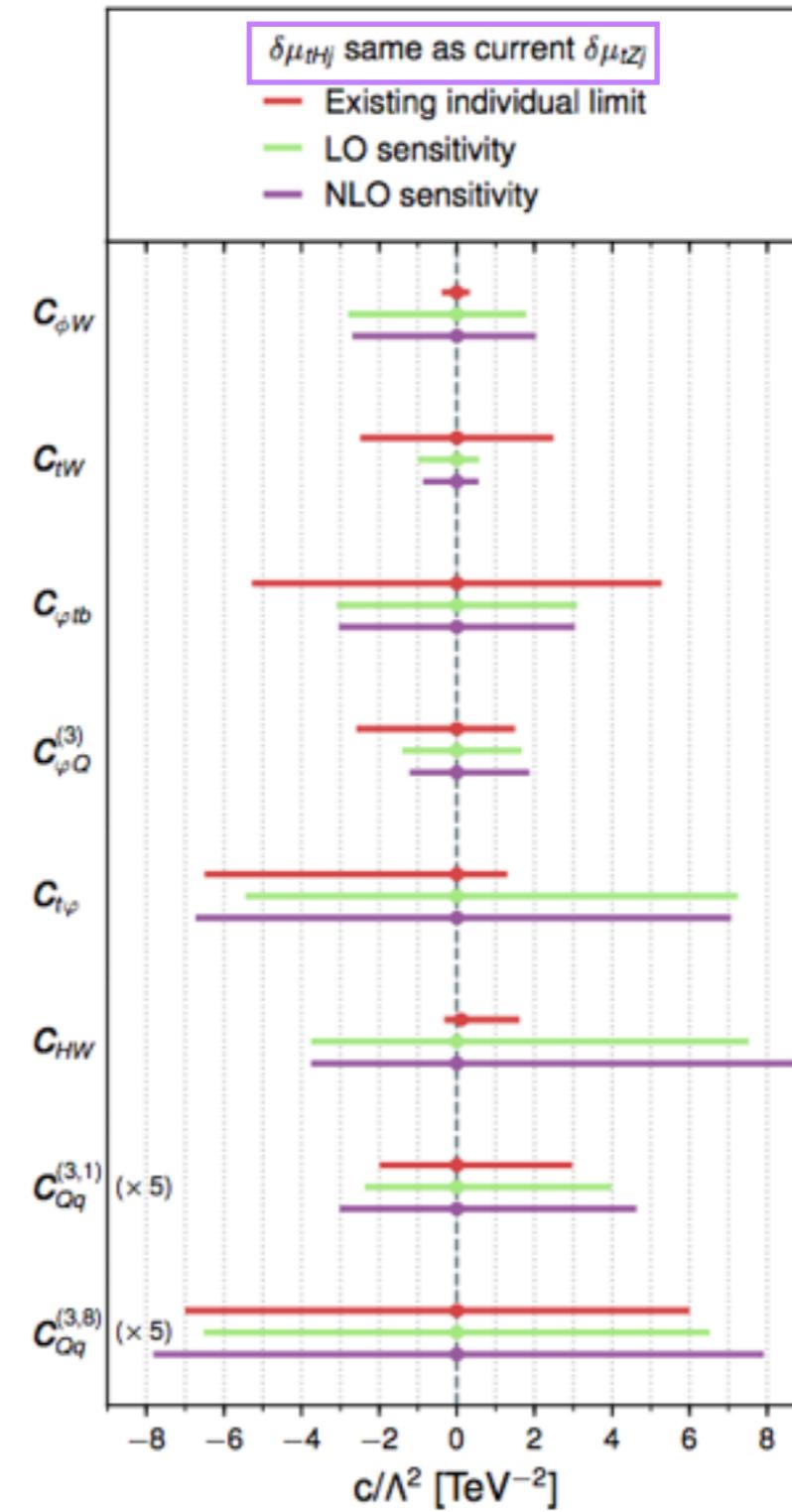
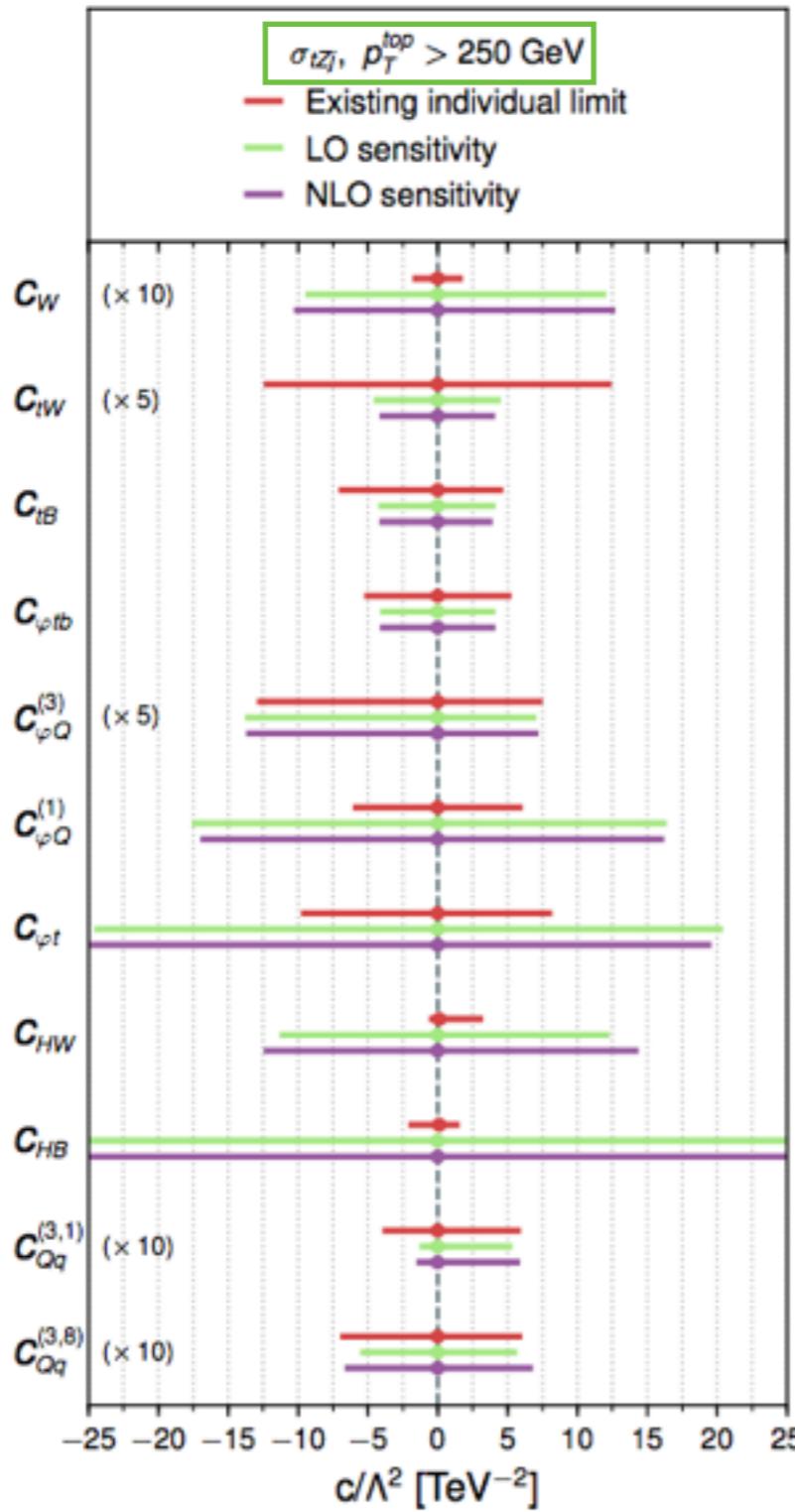


tHj
Gauge-Higgs
Dipole
RHCC
Currents
LEP
orthogonal
4-fermion

High p_T tZj: end of run II/HL-LHC
tHj: HL-LHC ?

Future sensitivity

tZj
TGC
Dipoles
RHCC
Currents
LEP
orthogonal
4-fermion



tHj
Gauge-Higgs
Dipole
RHCC
Currents
LEP
orthogonal
4-fermion

Dimension 8 in ttbb

- Sensitivity dominated by EFT squared ($1/\Lambda^4$) terms
 - Non-interference due to colour
 - Large Wilson coefficients \sim strong coupling regime $\frac{C^{(6)}E^2}{\Lambda^2} \gtrsim 1$
- Are higher dimension operators relevant?
- As long as $E < \Lambda$
 - 6 fermion operators: at least dim-10 $\sim (E/\Lambda)^6$
 - Dim-8 four fermion operators $\sim (E/\Lambda)^4$

schematically: $fffff D_\mu D_\nu$ & $fffff G_{\mu\nu}$

one coupling & one scale power counting:

$$\mathcal{L}_{\text{EFT}} = \frac{\Lambda_{NP}^4}{g_*^2} \mathcal{L} \left(\frac{D_\mu}{\Lambda_{NP}}, \frac{g_* H}{\Lambda_{NP}}, \frac{g_* f_{L,R}}{\Lambda_{NP}^{3/2}}, \frac{g F_{\mu\nu}}{\Lambda_{NP}^2} \right)$$

Power counting

$\frac{g^2}{p^2 - M^2}$

$p^2 \ll \Lambda^2$

dim-6 interference: $\frac{g_s^6 g_*^2 E^2}{\Lambda_{NP}^2}$

dim-6 quadratic term: $\frac{g_s^4 g_*^4 E^4}{\Lambda_{NP}^4}$

$D=6$ $D=8$ $\frac{C_{4F}^{(6)}}{\Lambda^2} \sim \frac{C_{4F}^{(8)}}{\Lambda^2} \sim \frac{g_*^2}{M^2}$

$$(g_*/g_s)^2 E^2 / \Lambda_{NP}^2 \approx 1. \rightarrow \text{SQ} \sim \text{INT}$$

$$f f f f D_\mu D_\nu \quad \frac{C_i^{(8)}}{\Lambda^2} \sim \frac{g_*^2}{M^2}$$

ttbb operator + 2 derivatives
gttbb contact term
ggttbb contact term

$$f f f f G_{\mu\nu} \quad \frac{C_i^{(8)}}{\Lambda^2} \sim \frac{g_*^2 g_s}{M^2}$$

dim-8 interference: $\frac{g_s^6 g_*^2 E^4}{\Lambda_{NP}^4}$

no g^* enhancement

FeynRules/NLOCT/UFO

- **FeynRules** [*Christensen & Duhr; Comp. Phys. Comm. 180 (2009) 1614*] [*Alloul et al.; Comp. Phys. Comm. 185 (2014) 2250*]
 - Framework: Lagrangian → Feynman rules → UFO model → MC events
- **Universal FeynRules Output (UFO)** [*Degrade et al.; Comp. Phys. Comm. 183 (2012) 1201*]
 - Model file with particle content, internal/external parameters, Feynman rules, Lorentz structures, counter-terms,...
 - Compatible with many MC event generators (MG5, Sherpa, Whizard,...)
- **NLOCT** [*Degrade; Comp. Phys. Comm. 197 (2015) 239*] [*Hahn; Comp. Phys. Comm. 140 (2001) 415*]
 - Automatic calculation of UV and R_2 counter-terms from FeynRules model
 - Implemented as additional Feynman rules in the UFO format
 - UV: on-shell renormalisation procedure for masses/wavefunction, MSbar for higher point functions
 - R_2 : numerical artefacts of dimensional regularisation