

top FCNC and axion

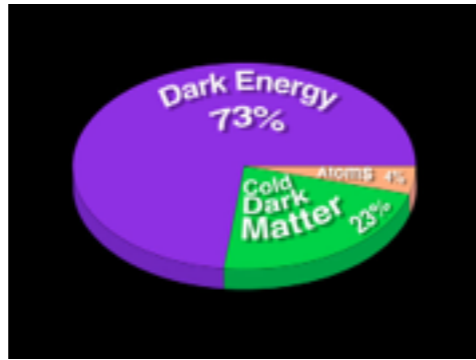
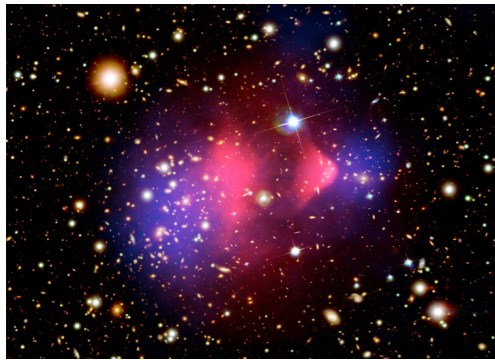
Michihisa Takeuchi (Kavli IPMU, Univ. of Tokyo)

based on JHEP11(2015)057 [arXiv:1507.04354], PhysRevD.97.035015 [arXiv:1711.02993], arxiv:1806.XXXX

at Benasque on 30th May 2018

Two big problems in particle physics

Existence of DM (serious problem)



Naturalness (Fine tuning in Higgs sector)

$$m_{h,\text{phys}}^2 = m_{h,\text{tree}}^2 + \delta m_h^2 \sim 125^2 \text{GeV}^2 \sim 10^4 \text{GeV}^2$$

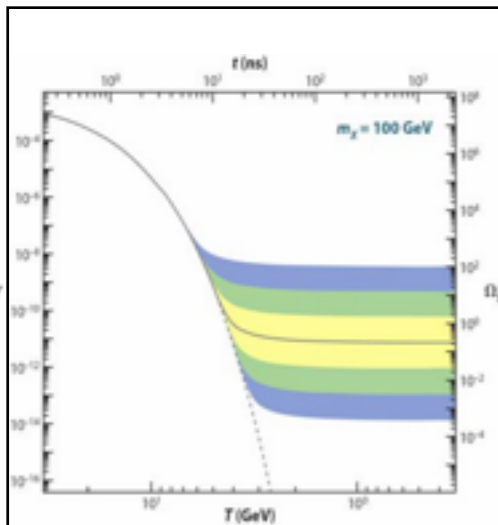
$$\delta m_h^2 \sim \text{---} \circlearrowleft \text{---} \sim -\frac{3}{4\pi} y_t^2 \Lambda_{\text{SM}}^2$$

t

$$\sim 10^{38} \text{GeV}^2 (\Lambda_{\text{SM}} = M_{\text{Planck}})$$

$$\sim 10^6 \text{GeV}^2 (\Lambda_{\text{SM}} = 1 \text{TeV})$$

Weak scale SUSY, or TeV scale SUSY elegantly solve both problems



WIMP miracle

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{\alpha^2} \sim 10^9 \text{GeV}^2$$

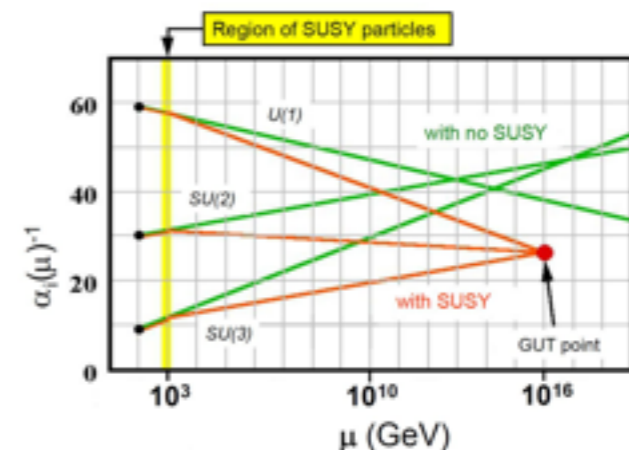
neutralino DM

perfect WIMP DM

new partner particle, same coupling by symmetry

$$\delta m_h^2 \sim \text{---} \circlearrowright \text{---} \sim +\frac{3}{4\pi} y_t^2 \Lambda^2$$

\tilde{t}

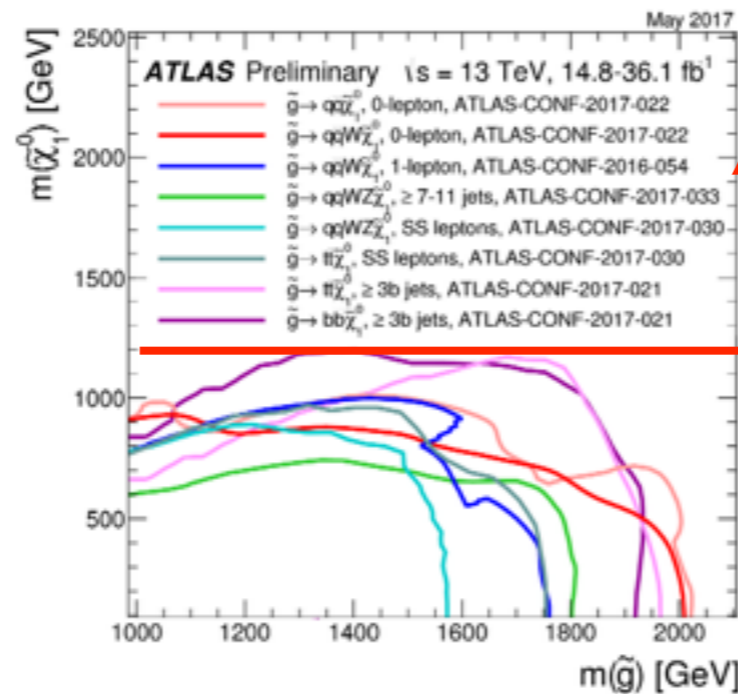


gauge coupling unification also suggests new states at TeV
SUSY would be the most attractive candidate

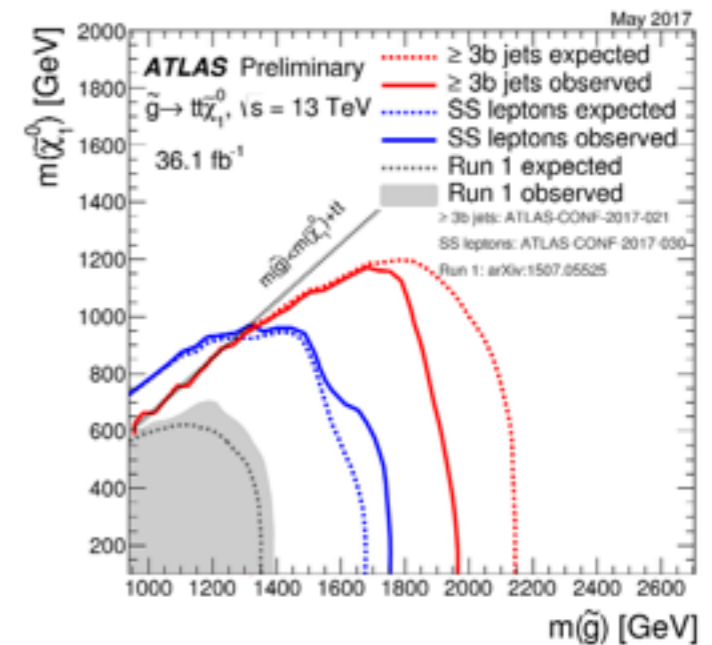
SUSY search results at LHC 13TeV with $\sim 36 \text{ fb}^{-1}$

For massless LSP

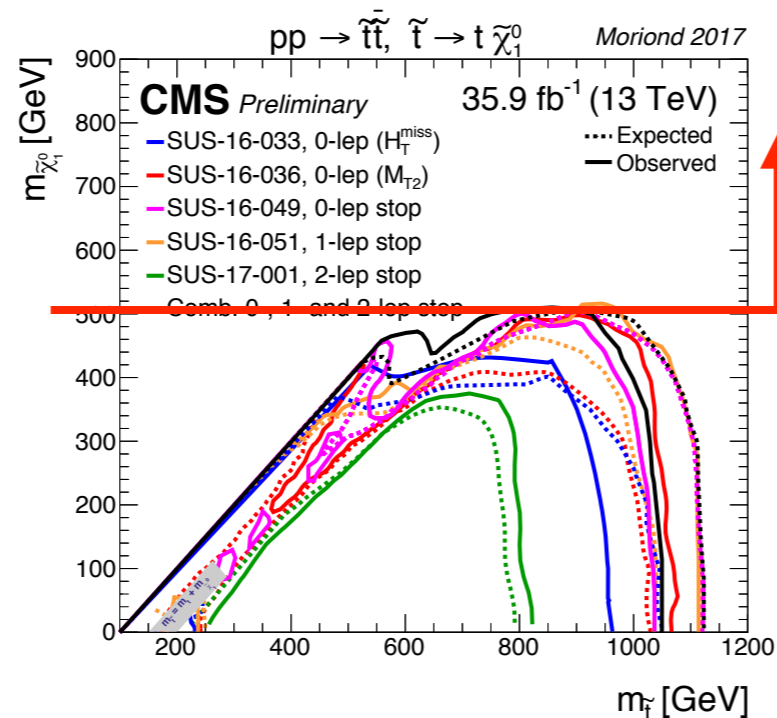
$\sim 2 \text{ TeV}$ gluino excluded



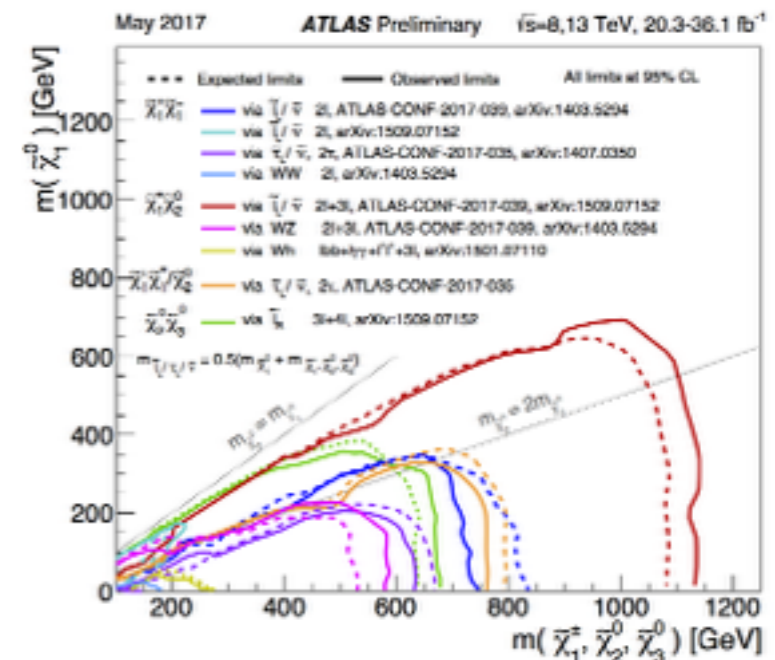
no constraint
LSP $> 1.2 \text{ TeV}$



$\sim 1 \text{ TeV}$ stop excluded



no constraint
LSP $> 500 \text{ GeV}$



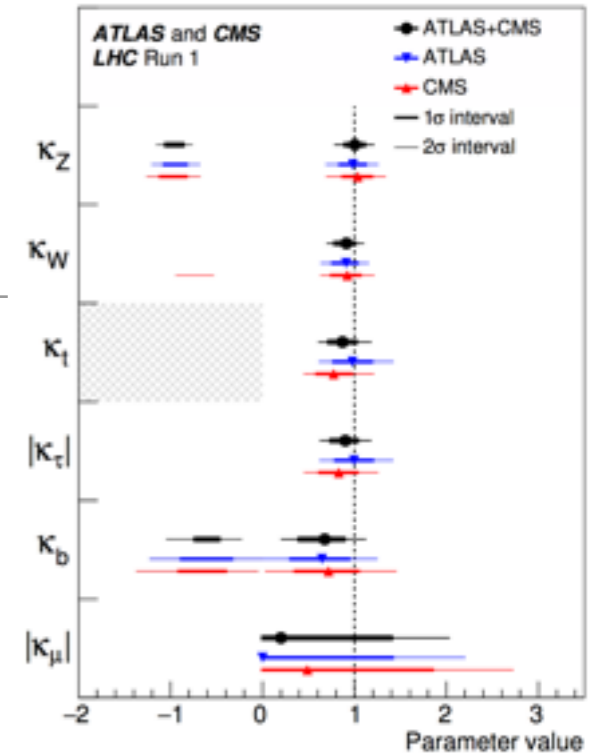
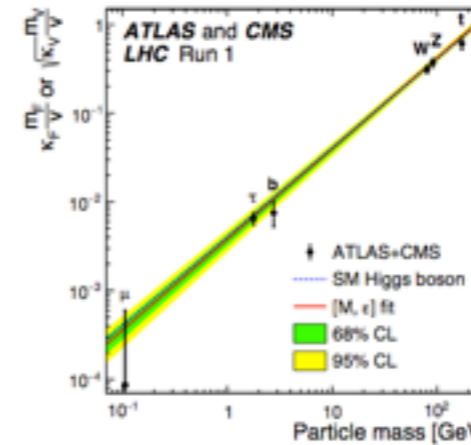
$\sim 600 \text{ GeV}$ EWkino (W/Z) excluded
(highly depends on BR)

when LSP is heavy enough no constraints we can set.

SM Higgs, no evidence of heavy higgses

Higgs couplings: consistent to SM Higgs at 10-20%

MSSM can realize it in decoupling limit and enough room for 10-20% deviations

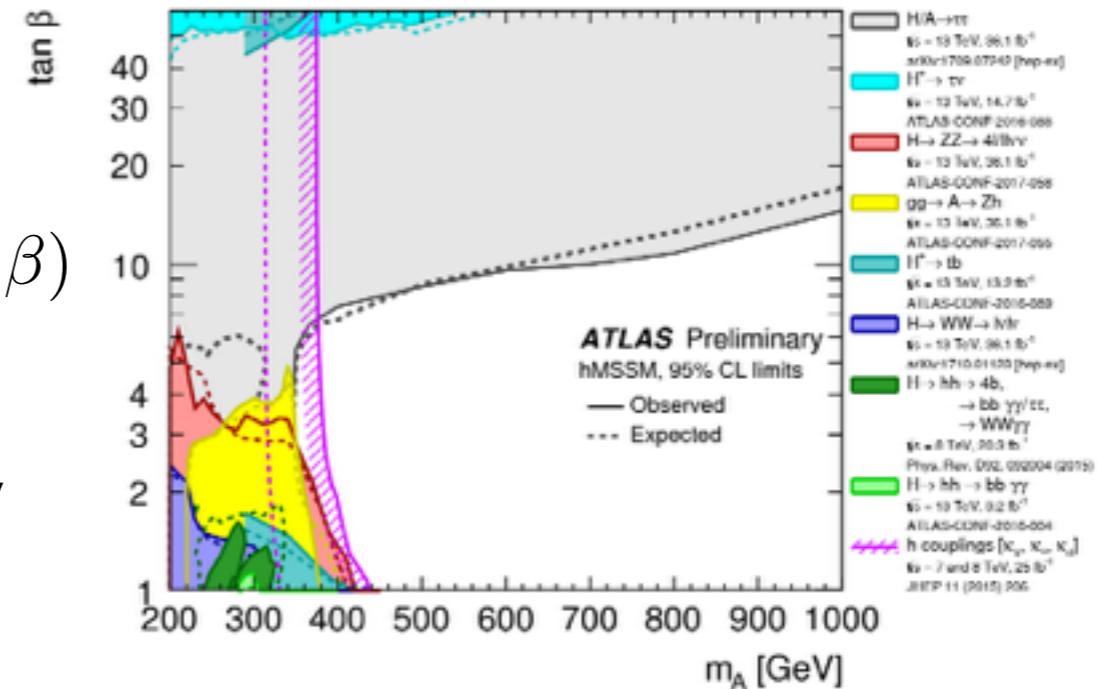


Heavy higgs searches

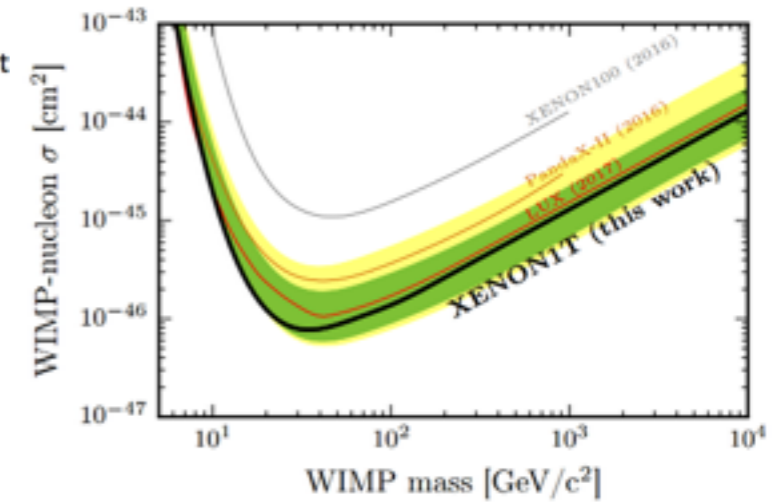
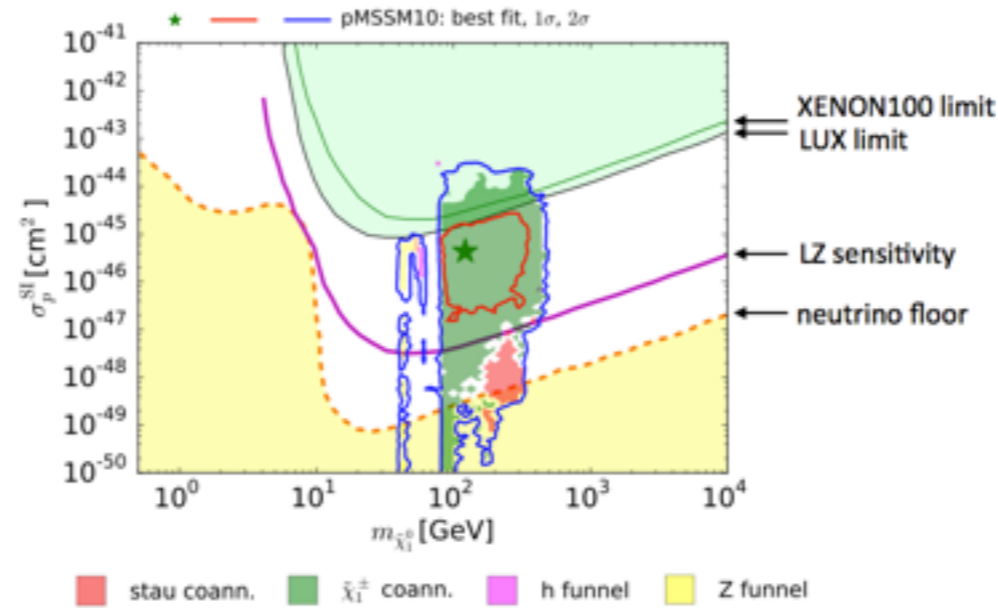
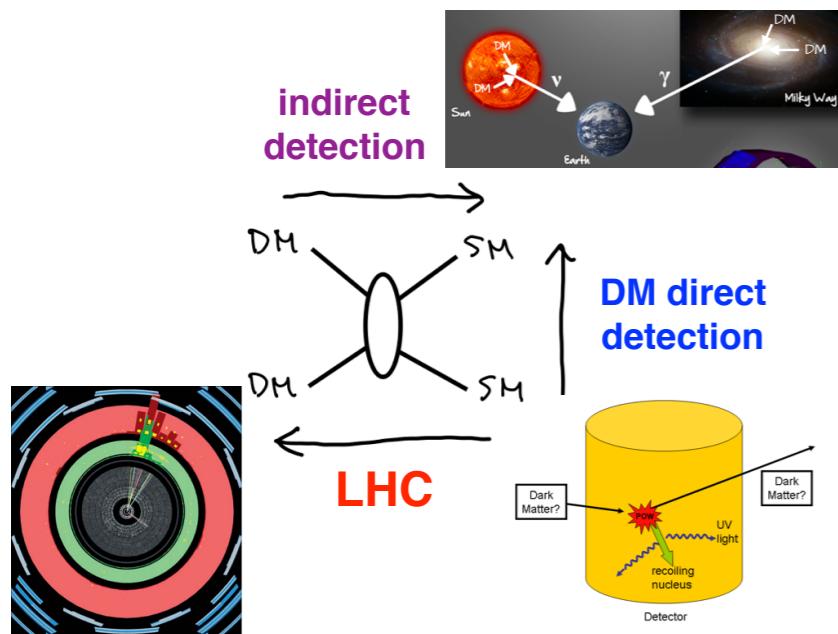
For large $\tan\beta$, $A \rightarrow \tau\tau$ dominates

MSSM Higgs sector : parametrized by $(m_A, \tan\beta)$
not like in a general 2HDM

→ Light higgs coupling measurements already constrain $m_A \gtrsim 400\text{GeV}$

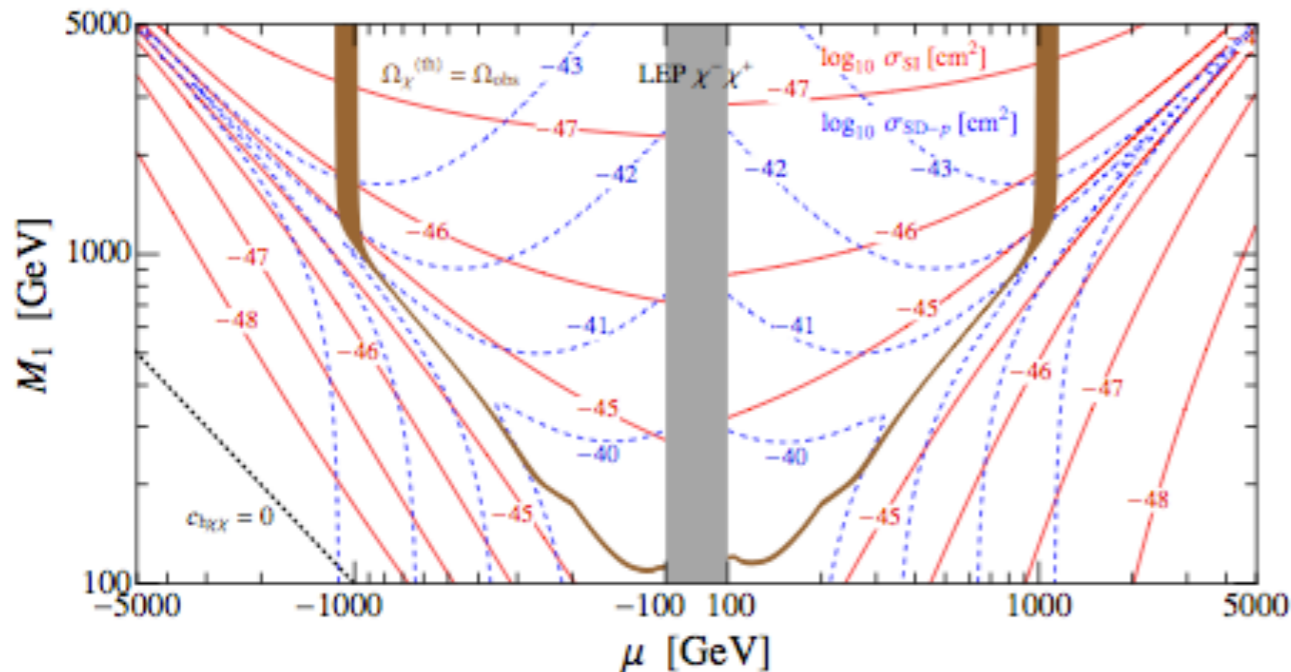


Null results from DM Direct Detection experiments



$$\sigma_{SI} < 10^{-45} \sim 10^{-46} \text{ cm}^2$$

$\tilde{B} - \tilde{H}$ mixture $\tan \beta = 20$



Typically, spin independent cross section in MSSM

$$10^{-44} \sim 10^{-47} \text{ cm}^2$$

not all excluded, remaining parameter space mainly

pure states, blind spots, co-annihilation

XENON1T starts to find something?

No signature of SUSY anywhere yet

no evidence of SUSY anywhere: Higgs measurement, Direct-Detection...

SUSY dead ? still attractive as a solution of the big hierarchy problem
(don't confuse with the "little" hierarchy)

why attractive: can solve DM and the fine tuning problem

Another fine tuning problem: strong CP problem Why $\theta_{\text{eff}} < 10^{-11}$? $\mathcal{L}_\theta = \frac{\theta}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$

attractive solution: PQ mechanism -> Axion : good DM candidate

similarly attractive and don't require new particles

-> naturally explain the current situation

Strong CP problem

QCD Lagrangian contains the total derivative term: θ -term

$$\mathcal{L}_\theta = \frac{\theta}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \quad \longleftrightarrow \quad |\theta\rangle = \sum_{n=-\infty}^{\infty} e^{in\theta} |n\rangle \quad \theta\text{-vacuum}$$

$$|n\rangle \rightarrow |m\rangle \quad \text{but} \quad |\theta\rangle \rightarrow |\theta\rangle$$

Note that θ is physical $0 \leq \theta < 2\pi$

Furthermore, chiral tr. $q \rightarrow e^{i\alpha\gamma_5} q$ induces $\theta \rightarrow \theta - 2\alpha$
 massive fermion mass term is also changed.

$$\theta_{\text{eff}} = \theta + \arg \det[M^u M^d] \quad \text{is invariant under the chiral tr.}$$

$$\propto \arg \det[v^6 Y^u Y^d]$$

$$\theta_{\text{eff}} \text{ can be measured from Neutron EDM } |d_n| = 4.5 \times 10^{-15} \theta_{\text{eff}} \text{ ecm}$$

$$|d_n^{\text{obs}}| < 2.9 \times 10^{-26} \text{ ecm}$$

Why $\theta_{\text{eff}} < 10^{-11}$?

while the origin of θ and $\arg M$ is completely different
 Fine tuning problem

Peccei-Quinn mechanism

[R. D. Peccei, H. R. Quinn, PhysRevLett.38.1440]

If the theory has $U(1)_{PQ}$, which spontaneously breakdowns to provide axion,

1. introduce a field a , axion.
2. assuming axial U(1) sym. which is spontaneously broken at η above QCD scale
3. impose appropriate PQ charges into quarks so that there exists $U(1)_{PQ}$ -SU(3)-SU(3) anomaly

Due to the anomaly, $U(1)_{PQ}$ current is not conserved, $\partial^\mu j_\mu^{PQ} = -\frac{g^2}{32\pi^2} AG^{a\mu\nu} \tilde{G}_{\mu\nu}^a$,

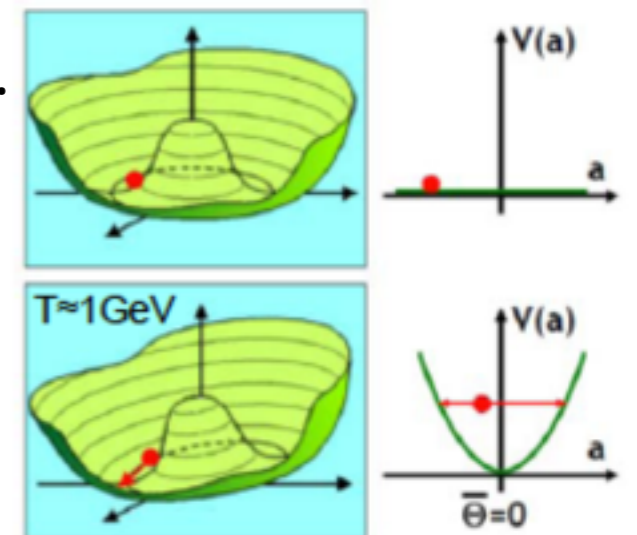
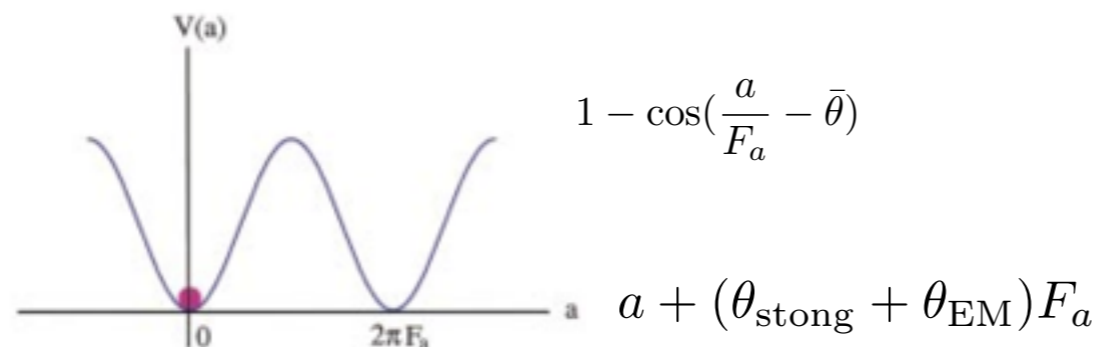
$\frac{a}{\eta} \rightarrow \frac{a}{\eta} + \epsilon$ induces $\delta\mathcal{L} = -\frac{g^2}{32\pi^2} \epsilon AG^{a\mu\nu} \tilde{G}_{\mu\nu}^a$, induce the potential in the effective lagrangian

$$\mathcal{L}_{\text{eff}} = -\frac{1}{4} G^{a\mu\nu} G_{\mu\nu}^a - \frac{1}{2} \partial_\mu a \partial^\mu a - \frac{g^2}{32\pi^2} \frac{a}{F_a} G^{a\mu\nu} \tilde{G}_{\mu\nu}^a - \frac{\bar{\theta} g^2}{32\pi^2} G^{a\mu\nu} \tilde{G}_{\mu\nu}^a$$

$$F_a = \eta/A$$

From the effective Lagrangian, effective potential to axion field can be computed.

QCD instanton effects give an axion a potential and minimizing it gives $\langle a \rangle = -\bar{\theta} F_a$.



Invisible Axions

Original axion model soon ruled out as axion is visible $\eta \sim v_{EW}$

people realized, η can be very high scale

$$U(1)_{PQ} : \quad \Phi \rightarrow e^{i\epsilon} \Phi. \quad V(\Phi) = \frac{\lambda}{4} (|\Phi|^2 - \eta^2)^2,$$

axion mass

$$m_a = \frac{\sqrt{z}}{1+z} \frac{f_\pi m_\pi}{F_a} \simeq 6\mu\text{eV} \frac{10^{12}\text{GeV}}{F_a}$$

photon coupling

$$\mathcal{L} = -\frac{g_{a\gamma\gamma}}{4} a F^{\mu\nu} \tilde{F}_{\mu\nu}$$

$$g_{a\gamma\gamma} = \frac{\alpha}{\pi} \frac{g_\gamma}{F_a}$$

$$g_\gamma = 0.97(\text{KSVZ}), -0.36(\text{DFSZ})$$

currently viable set up is categorized into two types

invisible axion model (KSVZ; Kim 1979, Shifman, Vainshtein, Zakharov 1980)

introducing new heavy quarks, $\mathcal{L}_Q = -y_Q \bar{Q}_L \Phi Q_R + \text{h.c.}$

invisible axion model (ZDFS; Zhitnitsky 1980, Dine, Fischler, Srednicki 1981)

$$V(\Phi_1, \Phi_2, \sigma) = \lambda_1 \left(|\Phi_1|^2 - \frac{v_1^2}{2} \right)^2 + \lambda_2 \left(|\Phi_2|^2 - \frac{v_2^2}{2} \right)^2 + \lambda \left(|\sigma|^2 - \frac{v^2}{2} \right)^2 \\ + a |\Phi_1|^2 |\sigma|^2 + b |\Phi_2|^2 |\sigma|^2 + \left(m \Phi_1^\dagger \Phi_2 \sigma + \text{h.c.} \right) \\ + d |\Phi_1^\dagger \Phi_2|^2 + e |\Phi_1|^2 |\Phi_2|^2.$$

Here, $\sigma = \Phi$

light quarks couples to either of φ through Yukawa couplings

No need to introduce new quarks

$U(1)_{PQ} :$

$$\varphi_1 \rightarrow e^{-i\epsilon} \varphi_1, \quad \varphi_2 \rightarrow e^{-i\epsilon} \varphi_2,$$

$$u_L \rightarrow u_L, \quad u_R \rightarrow e^{+i\epsilon} u_R,$$

$$d_L \rightarrow d_L, \quad d_R \rightarrow e^{+i\epsilon} d_R,$$

Axion as dark matter

Historically, axion not considered as a DM candidate

Original model axion is “visible” and soon ruled out

[T. Donnelly, S. Freedman, R. Lytel, R. Peccei and M. Schwartz, Phys.Rev. D18 (1978) 1607.]

invisible axions $\sim 1/f_a$

[J. E. Kim, Phys.Rev.Lett. 43 (1979) 103.]

[M. A. Shifman, A. Vainshtein and V. I. Zakharov, Nucl.Phys. B166 (1980) 493]

[M. Dine, W. Fischler and M. Srednicki, Phys.Lett. B104 (1981) 199]

[A. Zhitnitsky, Sov.J.Nucl.Phys. 31 (1980) 260]

invisibleness \rightarrow DM candidate! (coherent oscillation)

while extremely light, non-thermal production make them non-relativistic

\rightarrow Cold DM (consistent to structure formation)

[J. Preskill, M. B. Wise and F. Wilczek, Phys.Lett. B120 (1983) 127–132.]

[L. Abbott and P. Sikivie, Phys.Lett. B120 (1983) 133–136.]

[M. Dine and W. Fischler, Phys.Lett. B120 (1983) 137–141.]

$$\Omega_{a,0} h^2 = 0.095 \times (\bar{\theta}^{\text{ini}})^2 \left(\frac{g_{*,1}}{70}\right)^{-(n+2)/2(n+4)} \left(\frac{F_a}{10^{12}\text{GeV}}\right)^{(n+6)/(n+4)} \left(\frac{\Lambda_{\text{QCD}}}{400\text{MeV}}\right).$$

$$F_a < 10^{12}\text{GeV} \quad \longleftrightarrow \quad m_a > 1\mu\text{eV}$$

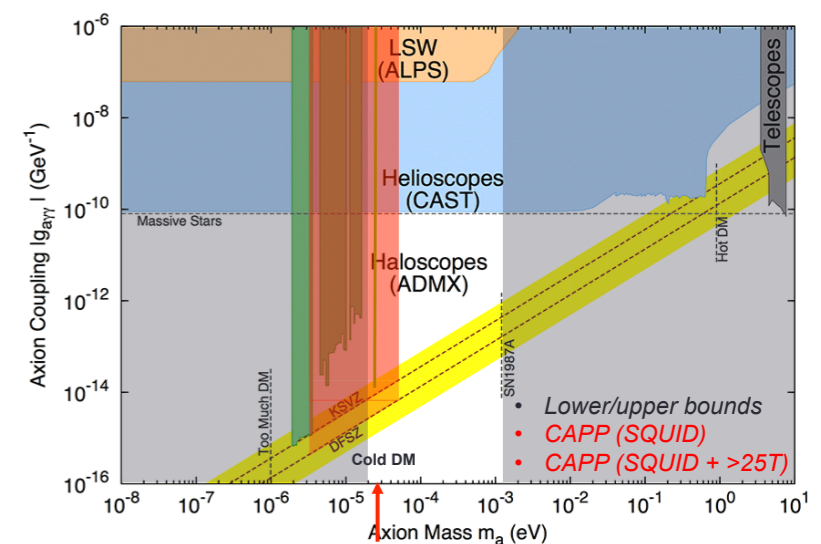


Current Axion DM searches

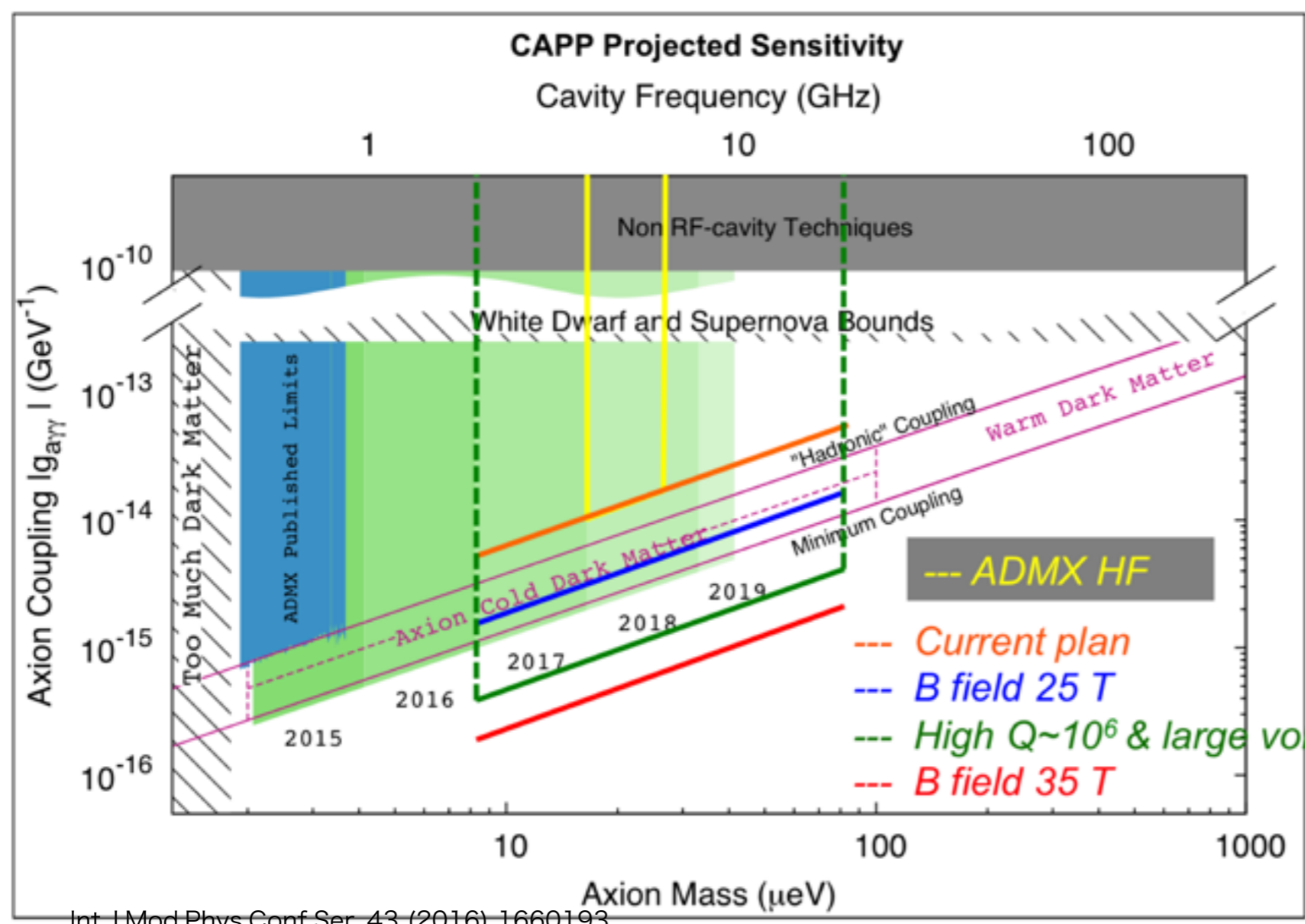
Axion DM abundance

$$F_a < 10^{12} \text{GeV} \iff m_a > 1 \mu\text{eV}$$

$$\Omega_{a,0} h^2 = 0.095 \times (\bar{\theta}^{\text{ini}})^2 \left(\frac{g_{*,1}}{70}\right)^{-(n+2)/2(n+4)} \left(\frac{F_a}{10^{12} \text{GeV}}\right)^{(n+6)/(n+4)} \left(\frac{\Lambda_{\text{QCD}}}{400 \text{MeV}}\right)$$



String tension: $26.3 \pm 3.4 \mu\text{eV}$ (Klaer & Moody 2017)



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Fig. 4. Projected sensitivities by CAPP/IBS for the axion coupling versus its mass (frequency) for different scenarios represented by lines in different colors. The blue area corresponds to the published exclusion region by ADMX,¹² while the green areas with different contrasts are the projected sensitivities by ADMX for the next 5 years. The yellow lines represent the limits expected by the ADMX-HF.

Scanning rate:

$$\frac{df}{dt} = \frac{f}{Qt} \approx \frac{1 \text{ GHz}}{\text{year}} (g_{\text{ay}} 10^{15} \text{GeV}^{-1})^4 \left(\frac{5 \text{ GHz}}{f}\right)^2 \left(\frac{4}{\text{SNR}}\right)^2 \left(\frac{0.25 \text{ K}}{T}\right)^2$$

$\left(\frac{B}{25T}\right)^4 \left(\frac{c}{0.6}\right) \left(\frac{V}{5l}\right)^2 \left(\frac{Q}{10^5}\right)$

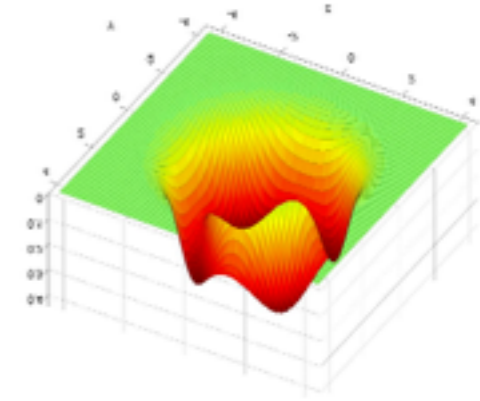
CAPP/IBS axion target plan

- Major improvement elements:
 - High field solenoid magnets, $B: 9\text{T} \rightarrow 25\text{T} \rightarrow 40\text{T}$
 - High volume magnets/cavities, $V: 5l \rightarrow 50l$
 - High quality factor of cavity, $Q: 10^5 \rightarrow 10^6$
 - Low noise amplifiers, $T_N: 2\text{K} \rightarrow 0.25\text{K}$
 - Low physical temperature, $T_{\text{ph}}: 1\text{K} \rightarrow 0.1\text{K}$

Scanning rate improvement: 25×10^6
 Improvement in coupling constant: 70

ibs CAPP director:
 Prof. Yannis Semertzidis's talk
 interesting region for DM covered in 5 years

Domain wall problem



$$U(1)_{PQ} \rightarrow Z_N, \quad N = \left| \sum_i^{N_g} (2q_i + u_i + d_i) \right| \quad \text{number of PQ charged quarks}$$

QCD instanton effects give an axion a potential of the form $1 - \cos(aN/\eta)$ and minimizing it gives $\langle a \rangle = \theta_{\text{eff}} = 0$. So as $\langle a \rangle = \frac{2\pi n}{N}\eta$ ($n = 0, \dots, N-1$)

for invisible axion model (KSVZ model) $N_{DM} = 1$ a periodic in $2\pi\eta \Leftrightarrow \theta$ periodic in $2\pi\eta/N$

for invisible axion model (ZDFS model)

$$\begin{aligned} V(\Phi_1, \Phi_2, \sigma) = & \lambda_1 \left(|\Phi_1|^2 - \frac{v_1^2}{2} \right)^2 + \lambda_2 \left(|\Phi_2|^2 - \frac{v_2^2}{2} \right)^2 + \lambda \left(|\sigma|^2 - \frac{v^2}{2} \right)^2 \\ & + a |\Phi_1|^2 |\sigma|^2 + b |\Phi_2|^2 |\sigma|^2 + \left(m \Phi_1^\dagger \Phi_2 \sigma + \text{h.c.} \right) \\ & + d |\Phi_1^\dagger \Phi_2|^2 + e |\Phi_1|^2 |\Phi_2|^2. \end{aligned}$$

$$N_{DW} = \left| \frac{N}{h_1 + h_2} \right| = N_g \quad [\text{C.Q. Geng, J. N. Ng, PhysRevD.41.3848}]$$

$N_g = 1$ is free from domain wall problem.

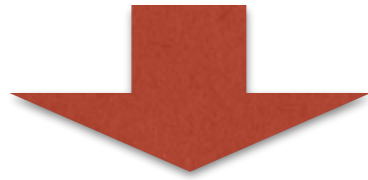
only 1 quark couples with PQ-charged Higgs solves the domain wall problem

Variant Axion model PQ charges: $u_3 = -1, h_2 = -1, \sigma = 1$

[R.D. Peccei, T.T. Wu and T. Yanagida, Phys. Lett. B172, 435 (1986)]

[C-R Chen, P. Frampton, F. Takahashi, T. T. Yanagida JHEP1006(2010)059]

Strong CP problem



PQ solution with axion

very attractive
rapid progress in axion DM searches



invisible axion models

KSVZ

$$N_{DM} = 1$$

heavy Q introduced
no problem but no low energy phenomenology
(not interesting)

ZDFS

$$N_{DM} = 6$$

$$\Phi_1^\dagger \Phi_2 \sigma^2$$

two Higgs doublet model,
no new fermion necessary introduced
can discuss low energy phenomenology

$$N_{DM} = 3$$

$$m \Phi_1^\dagger \Phi_2 \sigma$$

but suffer from Domain wall problem



$$N_{DM} = 1$$

only 1 quark coupled to PQ-Higgs
domain wall problem absent

top-specific Variant Axion model

σ field integrated out, the effective theory is just a 2HDM

$$V(\Phi_1, \Phi_2) = m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - (m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1)$$

$$L^u = -\Phi_1 \bar{u}_{Ra} [Y_{u1}]_{ai} Q_i - \Phi_2 \bar{u}_{R3} [Y_{u2}]_i Q_i + \text{h.c.}$$

Φ_2 only couple with u_{R3}

other quarks only couples with Φ_1

$$Y_{u1} = \begin{pmatrix} * & * & * \\ * & * & * \\ 0 & 0 & 0 \end{pmatrix}, \quad Y_{u2} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ * & * & * \end{pmatrix}$$

two Higgs easily results in FCNC. Usually people impose Z2 sym. to avoid FCNC.

	Φ_1	Φ_2	u_R	d_R	ℓ_R	Q_L, L_L
Type-I	+	-	-	-	-	+
Type-II	+	-	-	+	+	+
Type-X	+	-	-	-	+	+
Type-Y	+	-	-	+	-	+

when we take top as the special one,

top FCNC is the prediction

third gen. is identical to type II

top-specific VA Model

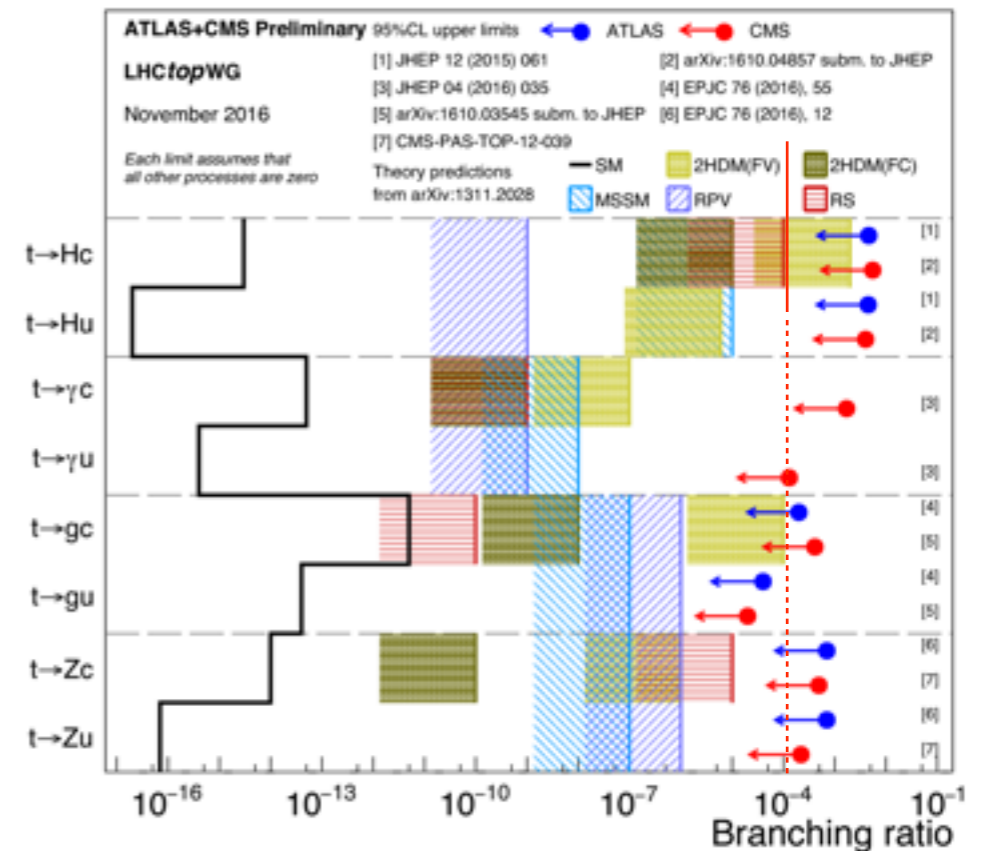
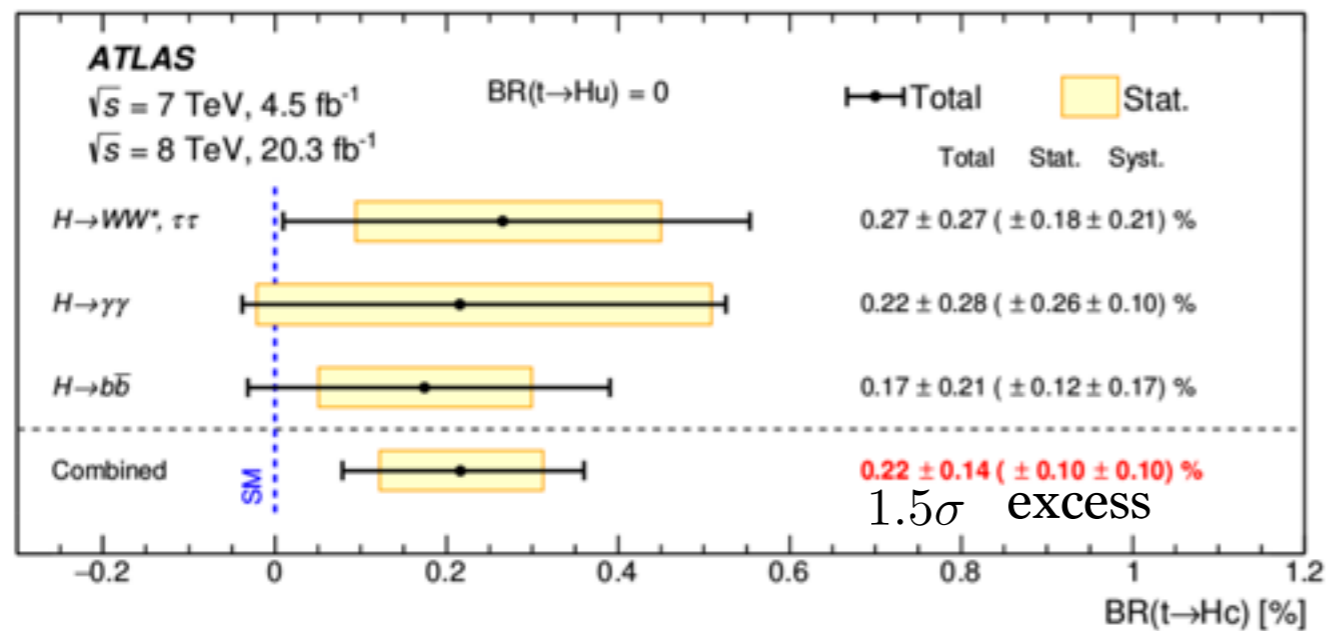
	Φ_1	Φ_2	t_R	c_R	u_R	d_R	ℓ_R	Q_L	L_L
top-specific VA Model	+	-	-	+	+	+	+	+	+

top-specific Variant Axion model

top FCNC is the prediction

$$BR(t \rightarrow ch) = 0.22 \pm 0.14\%$$

ATLAS 8TeV [JHEP 1512, 061 (2015)]



13 TeV ATLAS result set $BR < 0.22\%$

no hope for MSSM, FC 2HDM

Experimentalists can cite our model as a well motivated model to predict $t \rightarrow ch$

	Φ_1	Φ_2	t_R	c_R	u_R	d_R	ℓ_R	Q_L	L_L	top FCNC is the prediction
top-specific VA Model	+	-	-	+	+	+	+	+	+	third gen. is identical to type Π

top-specific Variant Axion model

$$L^u = -\Phi_1 \bar{u}_{Ra} [Y_{u1}]_{ai} Q_i - \Phi_2 \bar{u}_{R3} [Y_{u2}]_i Q_i + \text{h.c.}$$

Φ_2 only couple with u_{R3}

other quarks only couples with Φ_1

$$Y_{u1} = \begin{pmatrix} * & * & * \\ * & * & * \\ 0 & 0 & 0 \end{pmatrix}, \quad Y_{u2} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ * & * & * \end{pmatrix}$$

in the Higgs basis

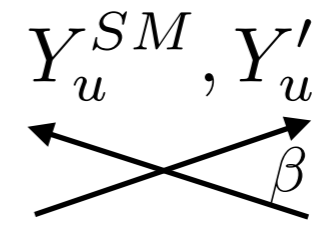
$$\begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix} = R_\beta \begin{pmatrix} \Phi^{\text{SM}} \\ \Phi' \end{pmatrix}, \quad \text{with } R_\theta = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}, \quad (1)$$

$$\text{with } \Phi^{\text{SM}} = \begin{pmatrix} G^+ \\ (v_{\text{SM}} + h^{\text{SM}} + iG^0)/\sqrt{2} \end{pmatrix}, \quad \Phi' = \begin{pmatrix} H^+ \\ (h' + iA^0)/\sqrt{2} \end{pmatrix}, \quad (2)$$

$$\begin{pmatrix} H \\ h \end{pmatrix} = R_{\beta-\alpha} \begin{pmatrix} h^{\text{SM}} \\ h' \end{pmatrix}$$

$$Y_u^{\text{SM}} = \cos \beta Y_{u1} + \sin \beta Y_{u2}, \quad Y'_u = -\sin \beta Y_{u1} + \cos \beta Y_{u2} = \begin{pmatrix} -\tan \beta & & \\ & -\tan \beta & \\ & & \cot \beta \end{pmatrix} Y_u^{\text{SM}}.$$

top-specific 2HDM



$$L^u = -\Phi_1 \bar{u}_{Ra} [Y_{u1}]_{ai} Q_i - \Phi_2 \bar{u}_{R3} [Y_{u2}]_i Q_i + \text{h.c.} \quad Y_{u1} = \begin{pmatrix} * & * & * \\ * & * & * \\ 0 & 0 & 0 \end{pmatrix}, \quad Y_{u2} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ * & * & * \end{pmatrix}$$

$$Y_u'^{\text{diag}} = \begin{pmatrix} -\tan \beta & & \\ & -\tan \beta & \\ & & \cot \beta \end{pmatrix} Y_u^{\text{diag}} + (\tan \beta + \cot \beta) H_u Y_u^{\text{diag}},$$

$$H_u \equiv V \begin{pmatrix} 0 & & \\ & 0 & \\ & & 1 \end{pmatrix} V^\dagger - \begin{pmatrix} 0 & & \\ & 0 & \\ & & 1 \end{pmatrix} \rightarrow \frac{1}{2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 - \cos \rho & \sin \rho \\ 0 & \sin \rho & \cos \rho - 1 \end{pmatrix}$$

using $\begin{pmatrix} H \\ h \end{pmatrix} = R_{\beta-\alpha} \begin{pmatrix} h^{\text{SM}} \\ h' \end{pmatrix}$

$$\xi_f \equiv \begin{cases} \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha) & (\text{for } f = t) \\ \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) & (\text{for } f \neq t) \end{cases}$$

as usual in 2HDM

$$\mathcal{L}_Y \equiv - \sum_{f=e,\dots,u,\dots,d,\dots} \xi_f \frac{m_f}{v_{\text{SM}}} h \bar{f} f + \mathcal{L}_{\text{FCNC}}$$

with $\mathcal{L}_{\text{FCNC}} = -a \sum_{f,f'=u,c,t} (H_u)_{ff'} \frac{m_{f'}}{v_{\text{SM}}} h \bar{f}_R f'_L + \text{h.c.}$

$$a \equiv (\tan \beta + \cot \beta) \cos(\beta - \alpha).$$

FC effect proportional to a and m_{f_L}

prediction in VA

$$\mathcal{L}_{tc} = -\frac{a}{2v_{\text{SM}}} h (\bar{c}_R \quad \bar{t}_R) \begin{pmatrix} m_c(1 - \cos \rho) & m_t \sin \rho \\ m_c \sin \rho & m_t(\cos \rho - 1) \end{pmatrix} \begin{pmatrix} c_L \\ t_L \end{pmatrix} + \text{h.c.}$$

Small (under $m_c \sin \rho$) Large (under $m_t \sin \rho$)

top FC decay $t \rightarrow ch$

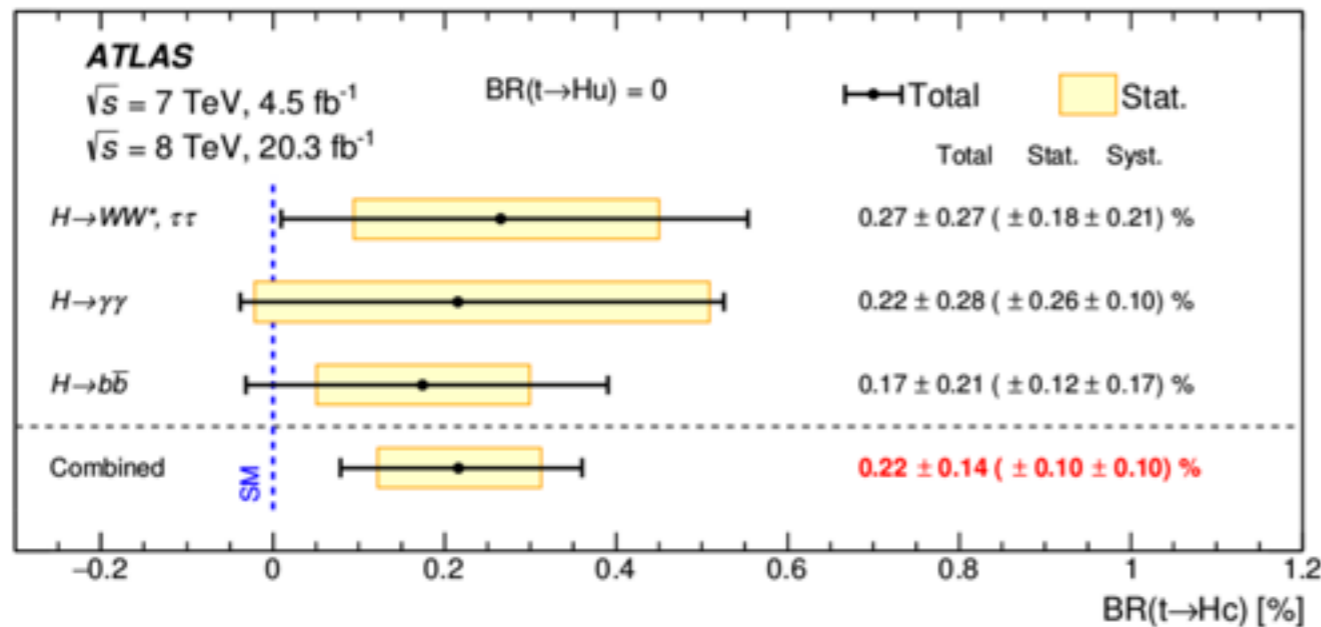
Large

$$\mathcal{L}_{tc} = -\frac{a}{2v_{\text{SM}}} h (\bar{c}_R \quad \bar{t}_R) \begin{pmatrix} m_c(1 - \cos \rho) & m_t \sin \rho \\ m_c \sin \rho & m_t(\cos \rho - 1) \end{pmatrix} \begin{pmatrix} c_L \\ t_L \end{pmatrix} + \text{h.c.} \quad \rho = 0 \rightarrow \text{no FCNC}$$

Small

$$\text{BR}(t \rightarrow ch) = \frac{(1 - r_h^2)^2}{8(1 - r_W^2)^2(1 + 2r_W^2)|V_{tb}|^2} a^2 \sin^2 \rho \simeq (3.24 \times 10^{-2}) a^2 \sin^2 \rho .$$

$$\text{BR}(t \rightarrow ch) = 0.22 \pm 0.14\% \quad \text{ATLAS 8TeV [JHEP 1512,061 (2015)]} \quad 1.5\sigma \text{ excess}$$



13 TeV ATLAS BR < 0.22% marginal

$$a^2 \sin^2 \rho = 0.068$$

future exp. 2×10^{-4} (3000 fb^{-1} at 14 TeV) with $h \rightarrow \gamma\gamma$

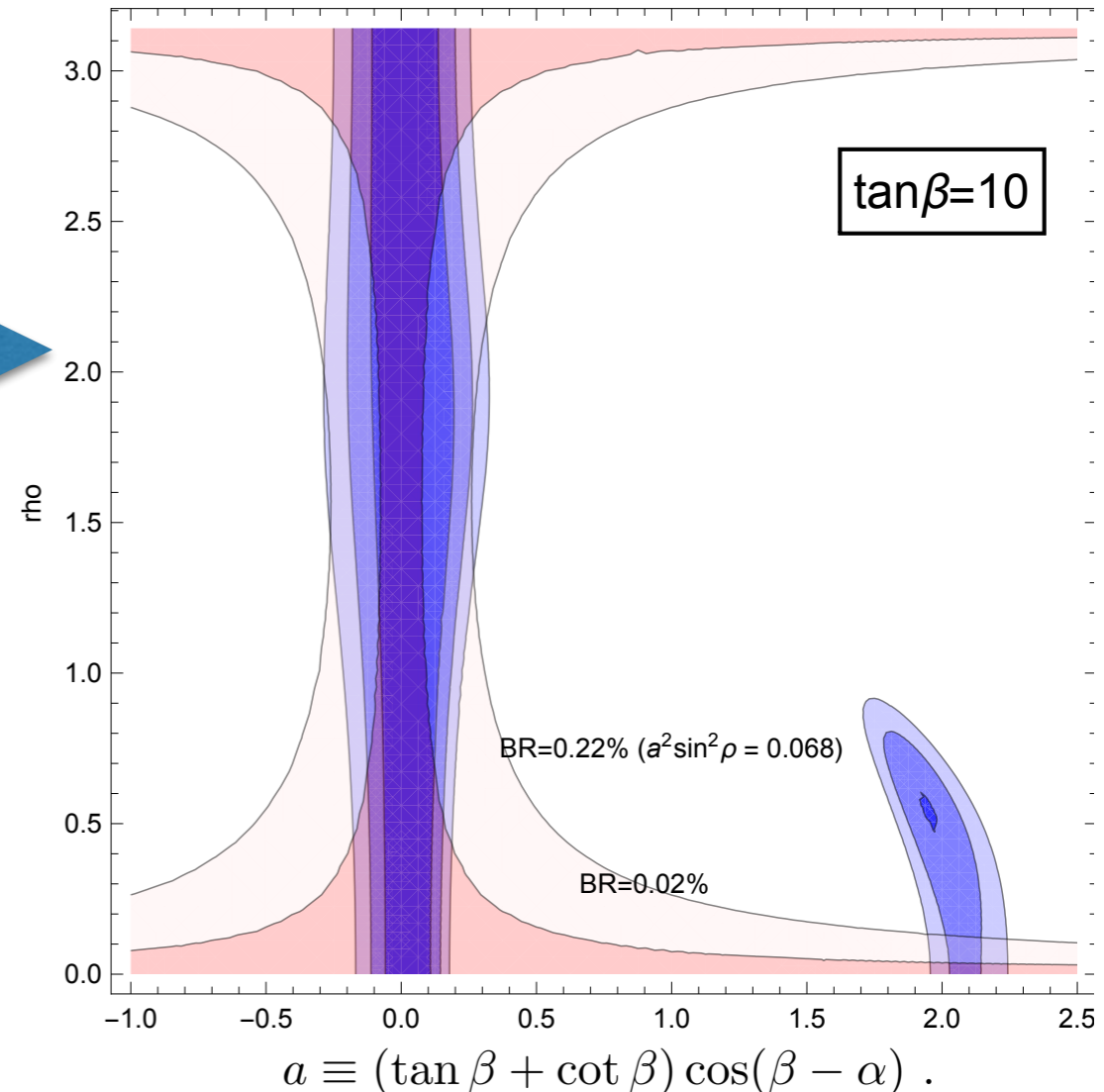
can be improved compared with $N(\text{top}) \sim 10^{10}$ for a whole LHC lifetime?

Higgs global fit (with latest data)

blue : Higgs data, red: $t \rightarrow ch$

model parameter: $\tan\beta$, $\cos(\beta-\alpha)$, ρ

	$\gamma\gamma$	ZZ	WW	$\tau\tau$	$b\bar{b}$
$ggF^{7.8\text{TeV}}$	$1.10^{+0.23}_{-0.22}$	$1.13^{+0.34}_{-0.31}$	0.84 ± 0.17	1.0 ± 0.6	-
$ggF^{13\text{TeV}}_{\text{ATLAS}}$	$0.8^{+0.19}_{-0.18}$ [54]	1.11 ± 0.245 [53]	-	-	-
$ggF^{13\text{TeV}}_{\text{CMS}}$	$1.11^{+0.19}_{-0.18}$ [51]	$1.20^{+0.22}_{-0.21}$ [49]	$0.9^{+0.4}_{-0.3}$ [65]	$1.17^{+0.47}_{-0.40}$ [66]	$2.3^{+1.8}_{-1.6}$ [68]
$VBF^{7.8\text{TeV}}$	1.3 ± 0.5	$0.1^{+1.1}_{-0.6}$	1.2 ± 0.4	1.3 ± 0.4	-
$VBF^{13\text{TeV}}_{\text{ATLAS}}$	2.1 ± 0.6 [54]	4.0 ± 1.77 [53]	$3.2^{+4.4}_{-4.2}$ [59]	-	$-3.9^{+2.8}_{-2.7}$ [61]
$VBF^{13\text{TeV}}_{\text{CMS}}$	$0.54^{+0.6}_{-0.5}$ [51]	$0.06^{+1.03}_{-0.06}$ [49]	1.4 ± 0.8 [65]	$1.11^{+0.34}_{-0.35}$ [66]	$-3.7^{+2.4}_{-2.5}$ [62]
$VH^{7.8\text{TeV}}$	0.5 ± 1.1	-	2.3 ± 1.0	-0.2 ± 1.1	0.63 ± 0.3
$VH^{13\text{TeV}}_{\text{ATLAS}}$	$0.7^{+0.9}_{-0.8}$ [54]	< 3.8 [53]	$1.7^{+1.1}_{-0.9}$ [59]	-	$1.20^{+0.42}_{-0.36}$ [55]
$VH^{13\text{TeV}}_{\text{CMS}}$	$2.29^{+1.1}_{-1.0}$ [51]	< 2.8 [49]	-0.3 ± 1.3 [65]	-	-
$ttH^{7.8\text{TeV}}$	$2.2^{+1.6}_{-1.3}$	-	$5.0^{+1.8}_{-1.7}$	$-1.9^{+3.7}_{-3.3}$	1.1 ± 1.0
$ttH^{13\text{TeV}}_{\text{ATLAS}}$	0.5 ± 0.6 [54]	(WW)	$2.5^{+1.3}_{-1.1}$ [56]	(WW)	$2.1^{+1.0}_{-0.9}$ [56]
$ttH^{13\text{TeV}}_{\text{CMS}}$	$2.22^{+0.9}_{-0.8}$ [51]	(WW)	1.5 ± 0.5 [67]	$0.72^{+0.62}_{-0.53}$ [64]	-0.19 ± 0.80 [63]



for $\rho=0$, 3rd gen is identical to type2 THDM

$$\xi_f = \begin{cases} \sin(\beta - \alpha) + \left(\cot \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & \text{(for } f = t \text{) ,} \\ \sin(\beta - \alpha) - \left(\tan \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & \text{(for } f = c \text{) ,} \\ \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) & \text{(for the others) .} \end{cases}$$

$$\mathcal{L}_{tc} = -\frac{a}{2v_{\text{SM}}} h \begin{pmatrix} \bar{c}_R & \bar{t}_R \end{pmatrix} \begin{pmatrix} m_c(1 - \cos \rho) & m_t \sin \rho \\ m_c \sin \rho & m_t(\cos \rho - 1) \end{pmatrix} \begin{pmatrix} c_L \\ t_L \end{pmatrix} + \text{h.c.}$$

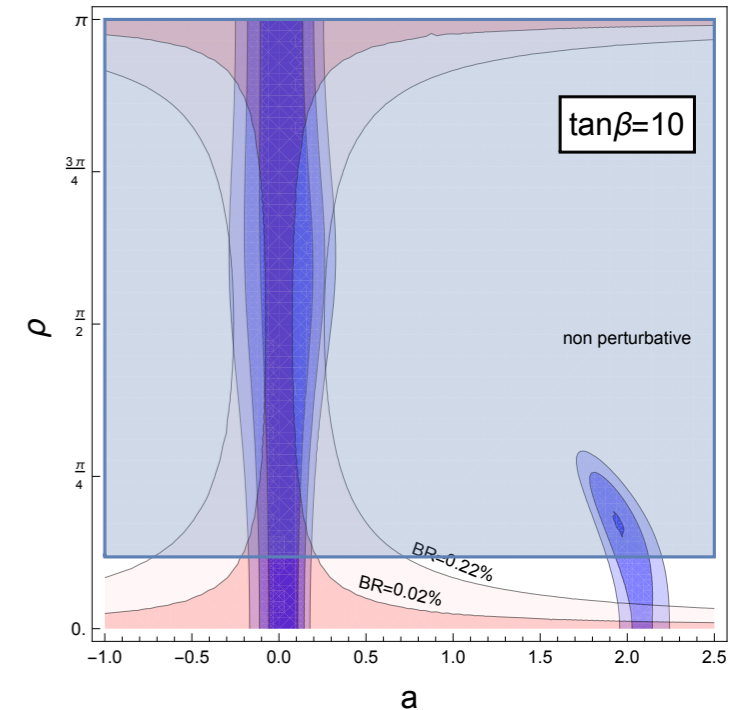
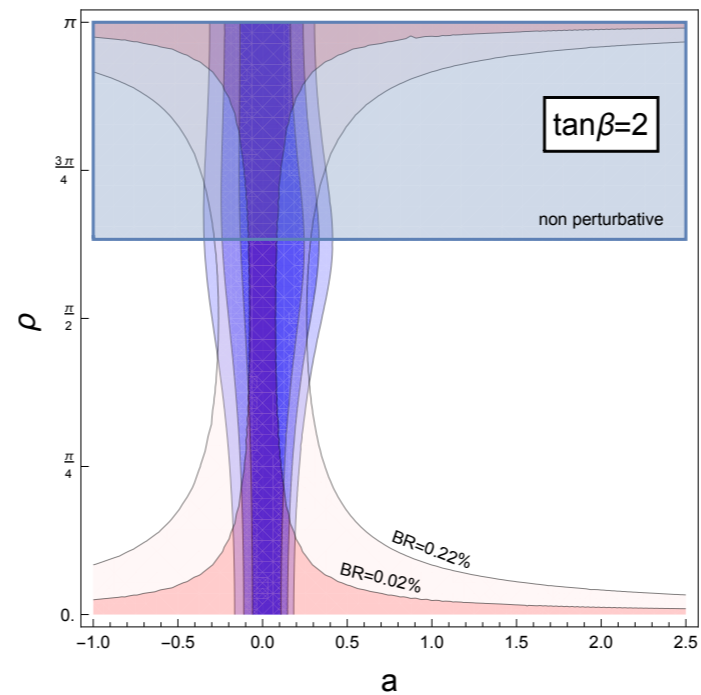
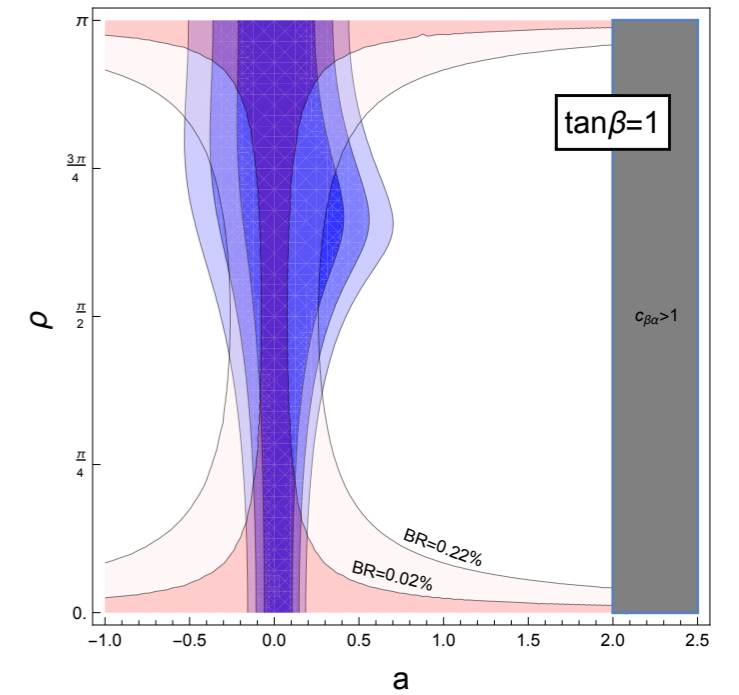
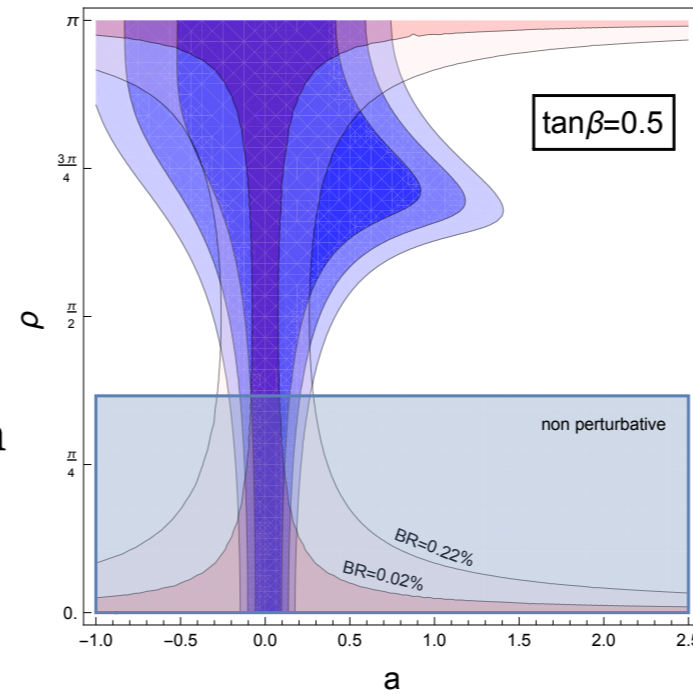
tan beta dependence

$$a \equiv (\tan \beta + \cot \beta) \cos(\beta - \alpha) .$$

low tan beta provide broader parameter region consistent with Higgs data

mainly by the condition $\xi_t/\xi_b = 1$

upper bound on tan beta
assuming BR=0.22%
and consistent with Higgs data



$$\xi_f = \begin{cases} \sin(\beta - \alpha) + \left(\cot \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta)\right) \cos(\beta - \alpha) & (\text{for } f = t) , \\ \sin(\beta - \alpha) - \left(\tan \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta)\right) \cos(\beta - \alpha) & (\text{for } f = c) , \\ \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) & (\text{for the others}) . \end{cases}$$

helicity structure in top FC decay

$t \rightarrow ch$

Large

$$\mathcal{L}_{tc} = -\frac{a}{2v_{\text{SM}}} h (\bar{c}_R \quad \bar{t}_R) \begin{pmatrix} m_c(1 - \cos \rho) & m_t \sin \rho \\ m_c \sin \rho & m_t(\cos \rho - 1) \end{pmatrix} \begin{pmatrix} c_L \\ t_L \end{pmatrix} + \text{h.c.}$$

Small

$h\bar{c}_R t_L$: always c_R observed ($m_c \ll m_t$) in $t \rightarrow ch$

from spin conservation, top helicity and direction of c_R is aligned.

Spin analyzing power: $\frac{1}{\Gamma_i} \frac{d\Gamma_i}{d\cos\theta_i} = \frac{1}{2} (1 + \kappa_i P \cos\theta_i)$

κ_{ℓ^+}	$\kappa_{\bar{d}}$	κ_u	κ_b	κ_c	κ_h	(LO)	$\kappa_f = -\bar{\kappa}_{\bar{f}}$
+1	+1	-0.32	-0.39	+1	-1		

Using spin correlation, we can check it.

at LHC, helicity basis is known to be a reasonably good spin axis

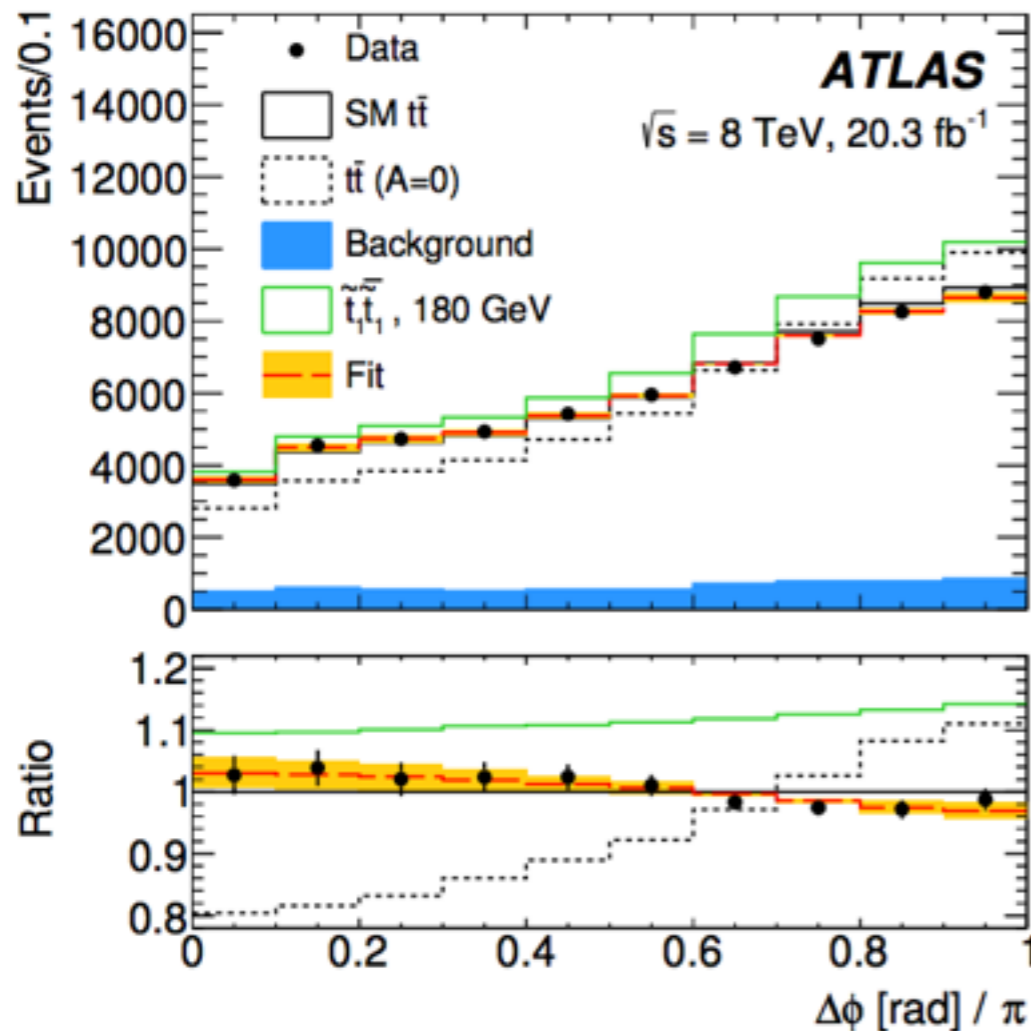
$$A_{\text{hel}} = \frac{N(t_{\uparrow}\bar{t}_{\uparrow}) + N(t_{\downarrow}\bar{t}_{\downarrow}) - N(t_{\uparrow}\bar{t}_{\downarrow}) - N(t_{\downarrow}\bar{t}_{\uparrow})}{N(t_{\uparrow}\bar{t}_{\uparrow}) + N(t_{\downarrow}\bar{t}_{\downarrow}) + N(t_{\uparrow}\bar{t}_{\downarrow}) + N(t_{\downarrow}\bar{t}_{\uparrow})} \sim 0.35 \quad (14\text{TeV})$$

helicity structure in top FC decay

$t \rightarrow ch$

$$\frac{1}{\Gamma_i} \frac{d\Gamma_i}{d\cos\theta_i} = \frac{1}{2} (1 + \kappa_i P \cos\theta_i)$$

$\kappa_{\ell+}$	$\kappa_{d\bar{}}$	κ_u	κ_b	κ_c	κ_h
+1	+1	-0.32	-0.39	+1	-1



Already measured by ATLAS, CMS

arXiv:1412.4742

CMS-PAS-TOP-13-015

$$A_{\text{hel}}^{\text{SM}, 8\text{TeV}} = 0.318 \pm 0.005$$

$$A_{\text{hel}}^{\text{ATLAS}, 8\text{TeV}} = 0.38 \pm 0.04$$

$$A_{\text{hel}} = \frac{N(t_{\uparrow}\bar{t}_{\uparrow}) + N(t_{\downarrow}\bar{t}_{\downarrow}) - N(t_{\uparrow}\bar{t}_{\downarrow}) - N(t_{\downarrow}\bar{t}_{\uparrow})}{N(t_{\uparrow}\bar{t}_{\uparrow}) + N(t_{\downarrow}\bar{t}_{\downarrow}) + N(t_{\uparrow}\bar{t}_{\downarrow}) + N(t_{\downarrow}\bar{t}_{\uparrow})} \sim 0.35 \quad (14\text{TeV})$$

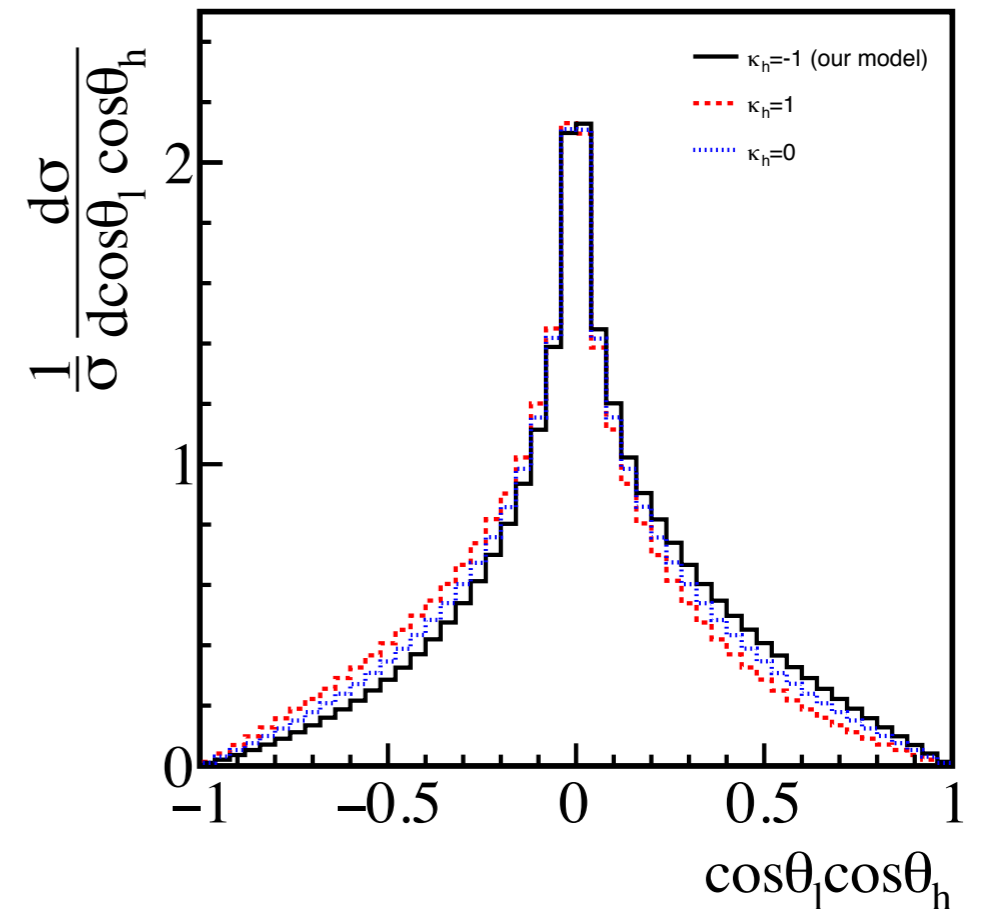
helicity structure in top FC decay

$t \rightarrow ch$

always c_R observed ($m_c \ll m_t$)

$$A_{\text{hel}} = \frac{N(t_{\uparrow}\bar{t}_{\uparrow}) + N(t_{\downarrow}\bar{t}_{\downarrow}) - N(t_{\uparrow}\bar{t}_{\downarrow}) - N(t_{\downarrow}\bar{t}_{\uparrow})}{N(t_{\uparrow}\bar{t}_{\uparrow}) + N(t_{\downarrow}\bar{t}_{\downarrow}) + N(t_{\uparrow}\bar{t}_{\downarrow}) + N(t_{\downarrow}\bar{t}_{\uparrow})} \sim 0.35$$

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\theta_i d\cos\theta_j} = \frac{1}{4} (1 + A_{\text{hel}} \kappa_i \bar{\kappa}_j \cos\theta_i \cos\theta_j)$$



rough estimate of the sensitivity:

$$A_{\ell h} = \frac{N(\cos\theta_\ell \cos\theta_h > 0) - N(\cos\theta_\ell \cos\theta_h < 0)}{N(\cos\theta_\ell \cos\theta_h > 0) + N(\cos\theta_\ell \cos\theta_h < 0)} = \frac{A_{\text{hel}} \kappa_\ell + \bar{\kappa}_h}{4} \sim 0.088 \bar{\kappa}_h.$$

$\Delta A_{\ell h} \simeq \Delta N/N \simeq 1/\sqrt{N} > 0.088 \rightarrow$ at least 130 signal events needed.

with $\sigma(tt) \sim 1 \text{ nb}$ for 3 ab^{-1} , 3×10^9 top pair expected

even for $BR(t \rightarrow ch)BR(h \rightarrow \gamma\gamma) = 2.2 \times 10^{-3} \times 2.3 \times 10^{-3}$,

~ 5000 of $t \rightarrow ch \rightarrow \gamma\gamma$ events expected

not so difficult

using $h \rightarrow b\bar{b}$ would improve the sensitivity 21

Summary

We consider top specific 2HDM, which predicts FCNC $t \rightarrow ch$

Strong CP problem



PQ solution with axion

promising axion DM searches near future



top-specific invisible axion model (ZDFS) $N_{DM} = 1$

a well motivated model for FV 2HDM

Central value of the current excess $BR=0.22\%$ and Higgs data is compatible to our model

We predict in general distinct helicity structure in FC higgs couplings.

As top pairs are produced copiously at LHC, we should be able to test it using the spin correlation for a reasonable $BR(t \rightarrow ch)$.

improving the analysis on this mode would be very important [LHC: top factory]

more detail: JHEP11(2015)057 [arXiv:1507.04354], PhysRevD.97.035015 [arXiv:1711.02993], arxiv:1806.XXXX

Backup

Up sector FCNC constraints

	$ Y_{ut}Y_{ct} , Y_{tu}Y_{tc} $	$< 7.6 \times 10^{-3}$
D^0 oscillations [49]	$ Y_{tu}Y_{ct} , Y_{ut}Y_{tc} $	$< 2.2 \times 10^{-3}$
	$ Y_{ut}Y_{tu}Y_{ct}Y_{tc} ^{1/2}$	$< 0.9 \times 10^{-3}$

t \rightarrow ch constraints $|\lambda_{ct}| < 0.09$ (BR < 0.22%)

the most stringent bound is

$$|\lambda_{ut}\lambda_{ct}| = |\lambda_{ct}|^2 |\lambda_{ut}/\lambda_{ct}| = 0.008 |\lambda_{ut}/\lambda_{ct}| < 7.6 \cdot 10^{-3}$$

$|\lambda_{ut}/\lambda_{ct}| \lesssim \mathcal{O}(1)$ is enough to avoid D-D mixing constraints

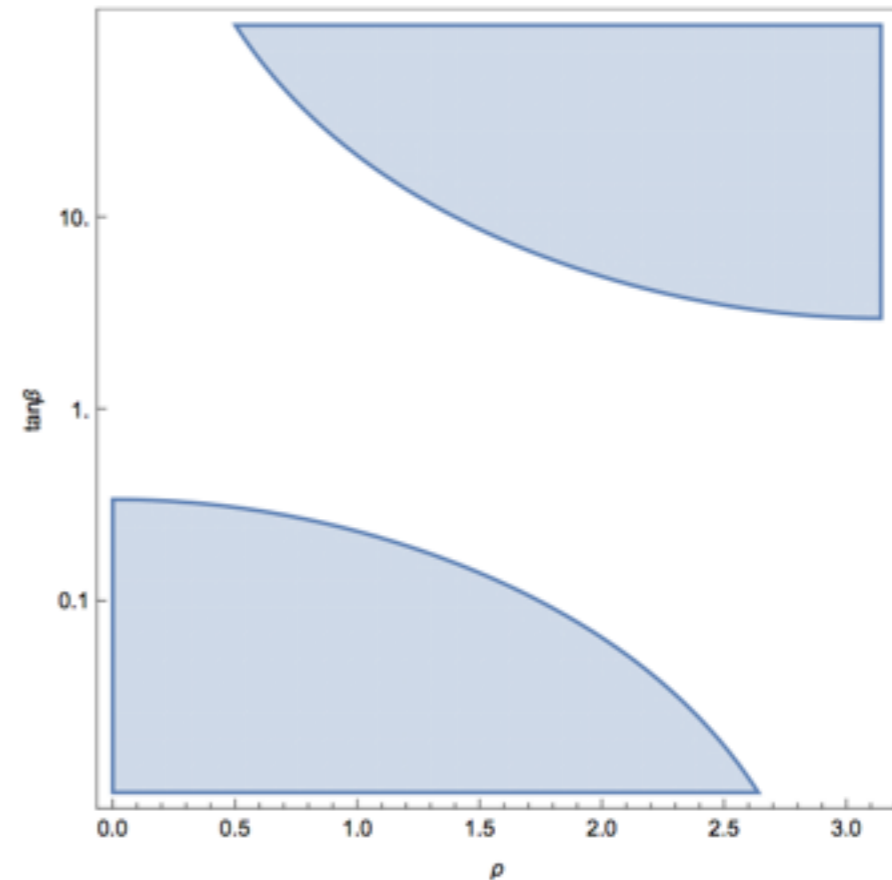
perturbativity

$$Y_u^{\prime, \text{diag}}{}_{ct} = (\tan \beta + \cot \beta) \frac{\sin \rho}{\sqrt{2}} \frac{m_t}{v}.$$

$$\begin{aligned} \mathcal{D}Y_j^d &= a_d Y_j^d + \sum_{k=1}^{n_H} T_{jk} Y_k^d \\ &\quad + \sum_{k=1}^{n_H} \left(-2 Y_k^u Y_j^{u\dagger} Y_k^d + \frac{1}{2} Y_k^u Y_k^{u\dagger} Y_j^d + Y_j^d Y_k^{d\dagger} Y_k^d + \frac{1}{2} Y_k^d Y_k^{d\dagger} Y_j^d \right), \end{aligned}$$

$$\begin{aligned} \mathcal{D}Y_j^u &= a_u Y_j^u + \sum_{k=1}^{n_H} T_{jk}^* Y_k^u \\ &\quad + \sum_{k=1}^{n_H} \left(-2 Y_k^d Y_j^{d\dagger} Y_k^u + \frac{1}{2} Y_k^d Y_k^{d\dagger} Y_j^u + Y_j^u Y_k^{u\dagger} Y_k^u + \frac{1}{2} Y_k^u Y_k^{u\dagger} Y_j^u \right), \end{aligned}$$

$$\mathcal{D}Y_j^e = a_e Y_j^e + \sum_{k=1}^{n_H} T_{jk} Y_k^e + \sum_{k=1}^{n_H} \left(Y_j^e Y_k^{e\dagger} Y_k^e + \frac{1}{2} Y_k^e Y_k^{e\dagger} Y_j^e \right),$$



$\tan \beta \sim 1$ is theoretically preferred

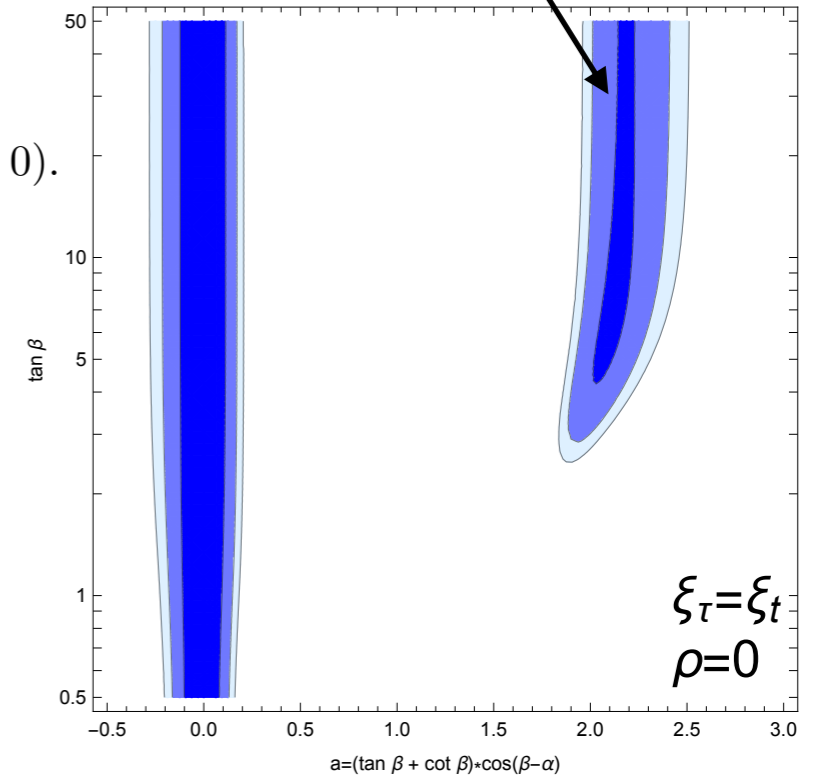
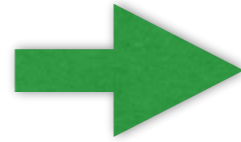
$$\xi_f = \begin{cases} \sin(\beta - \alpha) + \left(\cot \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & (\text{for } f = t), \\ \sin(\beta - \alpha) - \left(\tan \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & (\text{for } f = c), \\ \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) & (\text{for the others}). \end{cases}$$

$$\mathcal{L}_{tc} = -\frac{a}{2v_{\text{SM}}} h \begin{pmatrix} \bar{c}_R & \bar{t}_R \end{pmatrix} \begin{pmatrix} m_c(1 - \cos \rho) & m_t \sin \rho \\ m_c \sin \rho & m_t(\cos \rho - 1) \end{pmatrix} \begin{pmatrix} c_L \\ t_L \end{pmatrix} + \text{h.c.}$$

Higgs global fit

Observable	ATLAS [16]	CMS [17]
μ_{ZZ}^{GGF}	$1.7^{+0.5}_{-0.4}$	$0.883^{+0.336}_{-0.272}$
μ_{WW}^{GGF}	$0.98^{+0.29}_{-0.26}$	$0.766^{+0.228}_{-0.205}$
μ_{WW}^{VBF}	$1.28^{+0.55}_{-0.47}$	$0.623^{+0.593}_{-0.479}$
$\mu_{\gamma\gamma}^{\text{GGF}}$	1.32 ± 0.38	$1.007^{+0.293}_{-0.259}$
μ_{bb}^{VH}	0.52 ± 0.40	$1.008^{+0.527}_{-0.499}$
$\mu_{\tau\tau}^{\text{GGF}}$	$2.0^{+1.5}_{-1.2}$	$0.843^{+0.423}_{-0.382}$
$\mu_{\tau\tau}^{\text{VBF}}$	$1.24^{+0.59}_{-0.54}$	$0.948^{+0.431}_{-0.379}$

when FC effects switched off ($\rho = 0$).

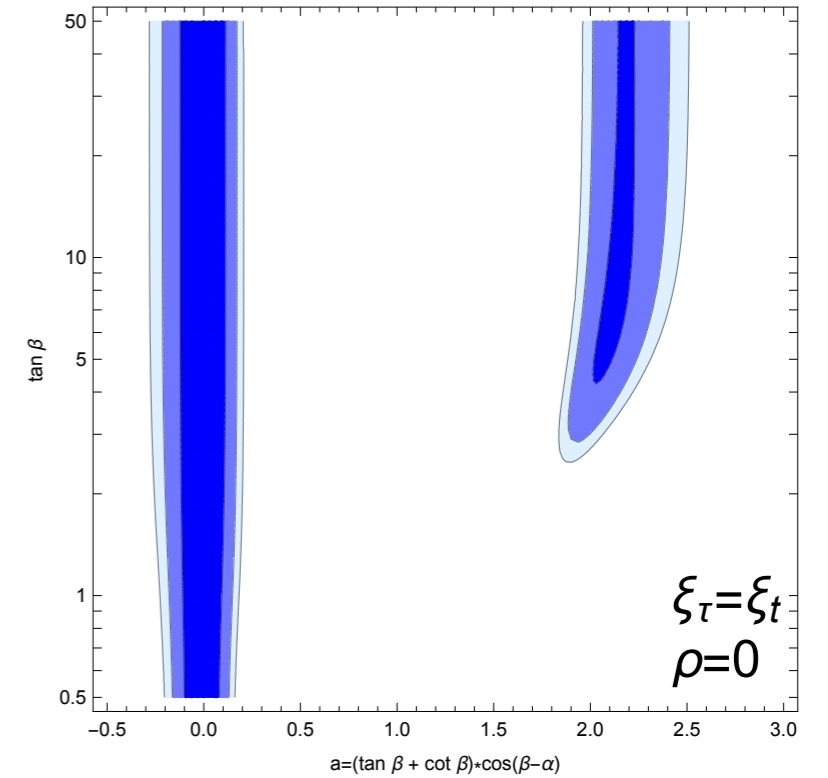
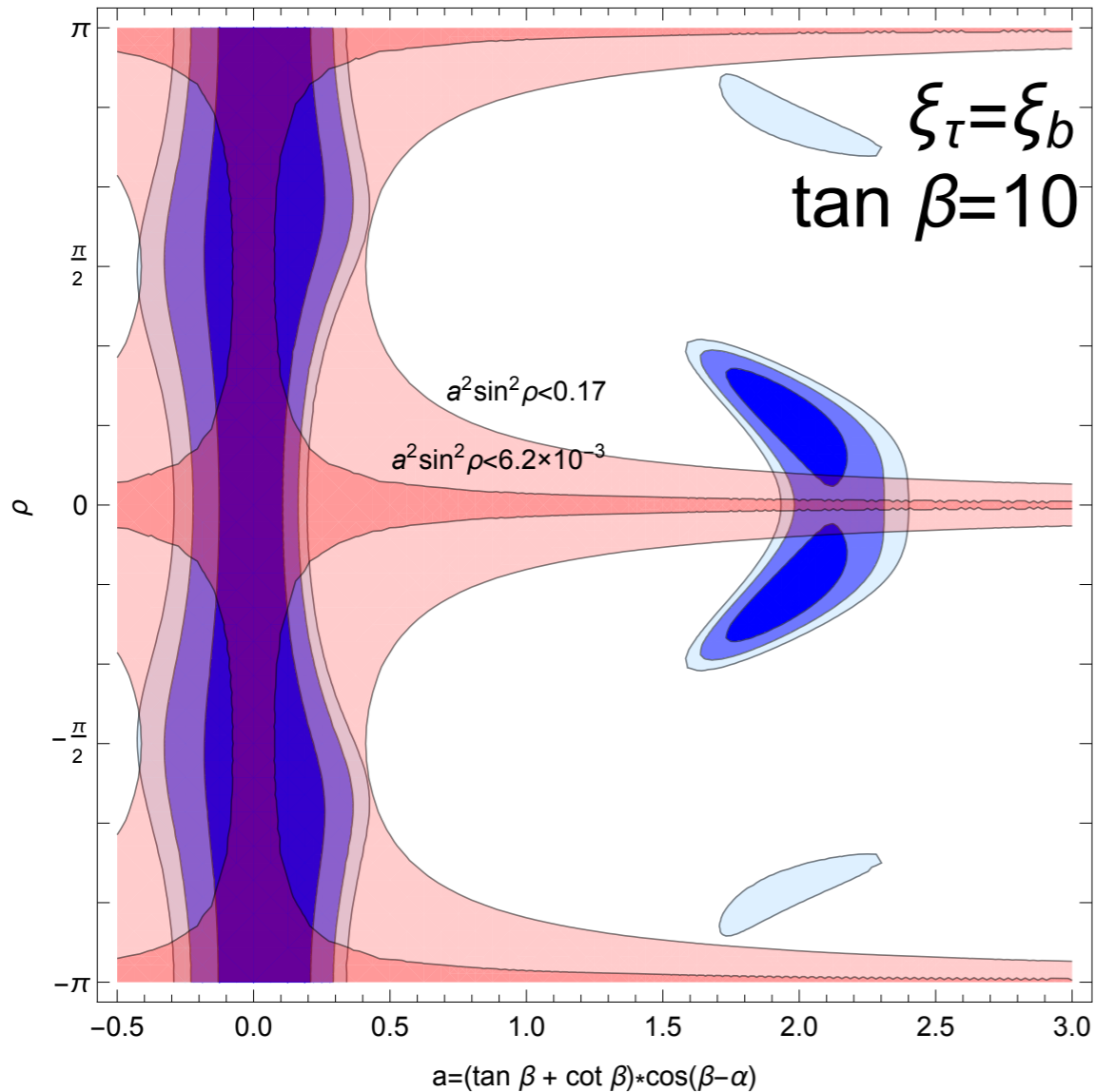


not sensitive to $\tan \beta$ (for > 5)

$$a \sim \tan \beta \cos(\beta - \alpha) \quad \text{for large } \tan \beta$$

$$\xi_f = \begin{cases} \sin(\beta - \alpha) + \left(\cot \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & \text{(for } f = t \text{),} \\ \sin(\beta - \alpha) - \left(\tan \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & \text{(for } f = c \text{),} \\ \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) & \text{(for the others).} \end{cases}$$

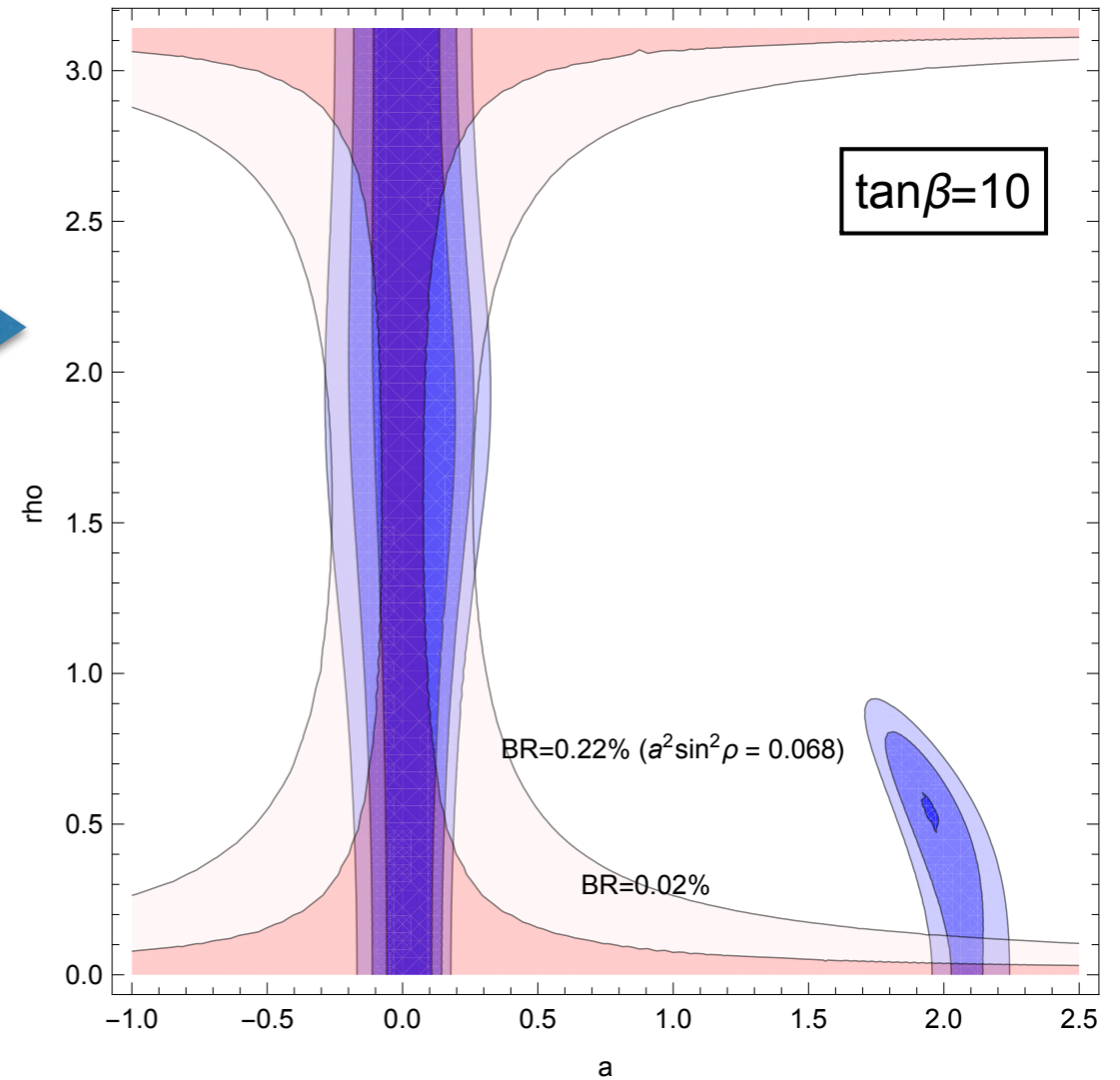
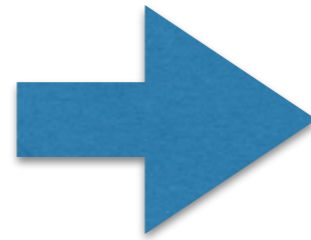
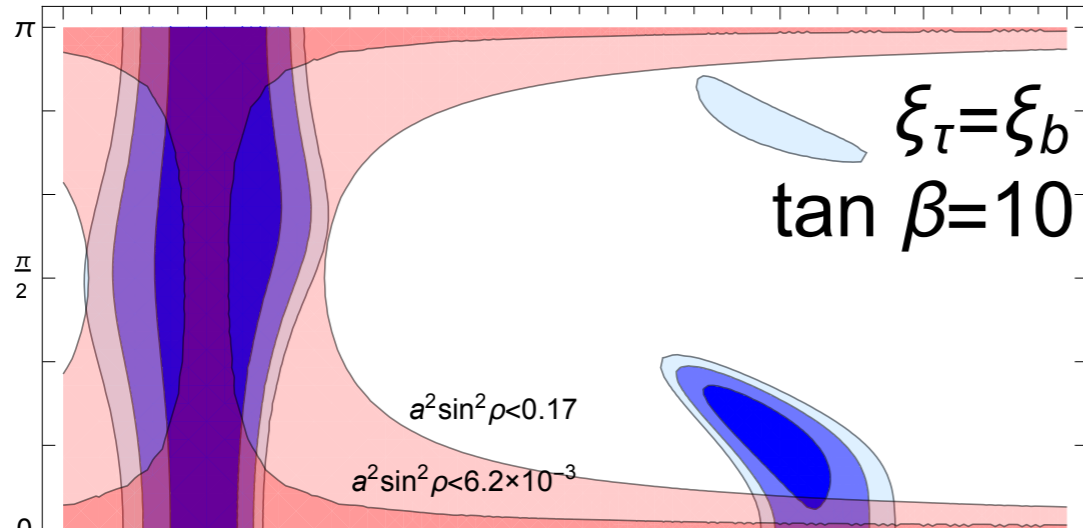
Higgs global fit



$$\xi_f = \begin{cases} \sin(\beta - \alpha) + \left(\cot \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & \text{(for } f = t \text{),} \\ \sin(\beta - \alpha) - \left(\tan \beta - \frac{1 - \cos \rho}{2} (\tan \beta + \cot \beta) \right) \cos(\beta - \alpha) & \text{(for } f = c \text{),} \\ \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) & \text{(for the others).} \end{cases}$$

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Higgs global fit (with latest data)



	$\gamma\gamma$	ZZ	WW	$\tau\tau$	$b\bar{b}$
$ggF^{7.8\text{TeV}}$	$1.10^{+0.23}_{-0.22}$	$1.13^{+0.34}_{-0.31}$	0.84 ± 0.17	1.0 ± 0.6	-
$ggF^{13\text{TeV}}_{\text{ATLAS}}$	$0.8^{+0.19}_{-0.18}$ [54]	1.11 ± 0.245 [53]	-	-	-
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$VBF^{7.8\text{TeV}}$	1.3 ± 0.5	$0.1^{+1.1}_{-0.6}$	1.2 ± 0.4	1.3 ± 0.4	-
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$VH^{13\text{TeV}}_{\text{CMS}}$	$2.29^{+1.1}_{-1.0}$ [51]	< 2.8 [49]	-0.3 ± 1.3 [65]	-	-
$ttH^{7.8\text{TeV}}$	$2.2^{+1.6}_{-1.3}$	-	$5.0^{+1.8}_{-1.7}$	$-1.9^{+3.7}_{-3.3}$	1.1 ± 1.0
$ttH^{13\text{TeV}}_{\text{ATLAS}}$	0.5 ± 0.6 [54]	(ww)	$2.5^{+1.3}_{-1.1}$ [56]	(ww)	$2.1^{+1.0}_{-0.9}$ [56]
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$$\mathcal{L}_{tc} = -\frac{a}{2v_{\text{SM}}} h (\bar{c}_R \quad \bar{t}_R) \begin{pmatrix} m_c(1 - \cos \rho) & m_t \sin \rho \\ m_c \sin \rho & m_t(\cos \rho - 1) \end{pmatrix} \begin{pmatrix} c_L \\ t_L \end{pmatrix} + \text{h.c.}$$