



# UCLouvain

Institut de recherche en mathématique et physique

Centre de Cosmologie, Physique des Particules et Phénoménologie



New physics in double Higgs production  
Celine Degrande

# Plan

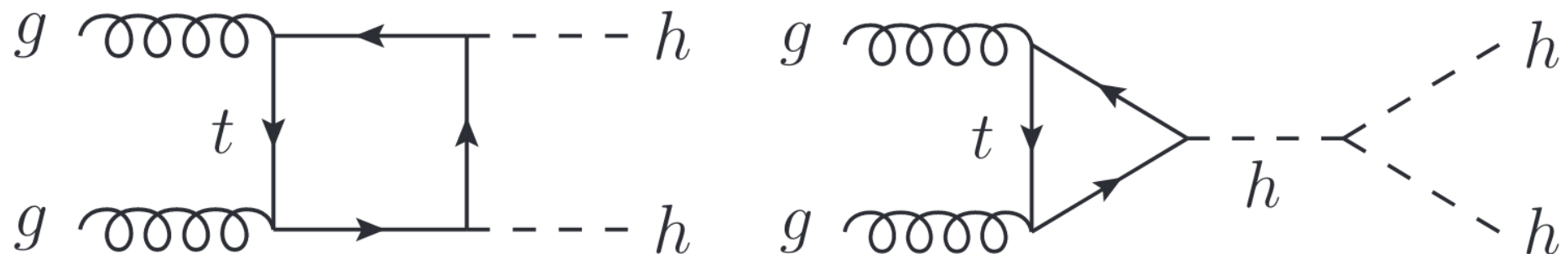
C. D., A. Tonerio, R. Rosenfeld, Andres Vasquez, JHEP 1905 (2019) 020

- Introduction : HH
- SMEFT operators for HH
- Results
- Other constraints
- Summary

Introduction: double HH

# HH at hadron colliders

Plehn, Spira & Zerwas, 1996



Stronger cancellation close to threshold

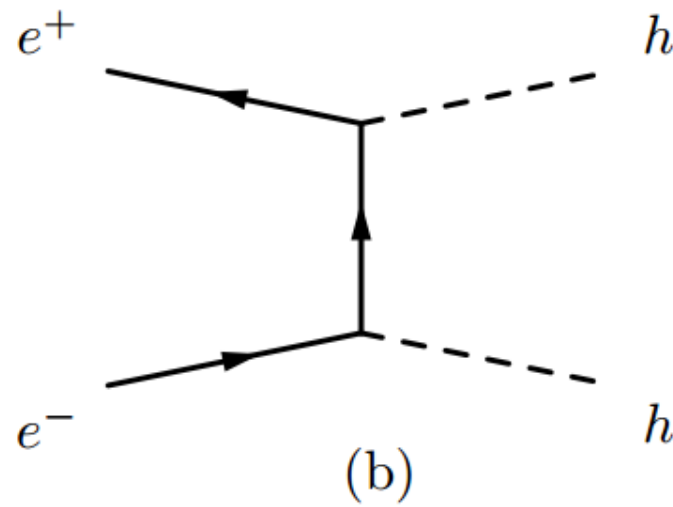
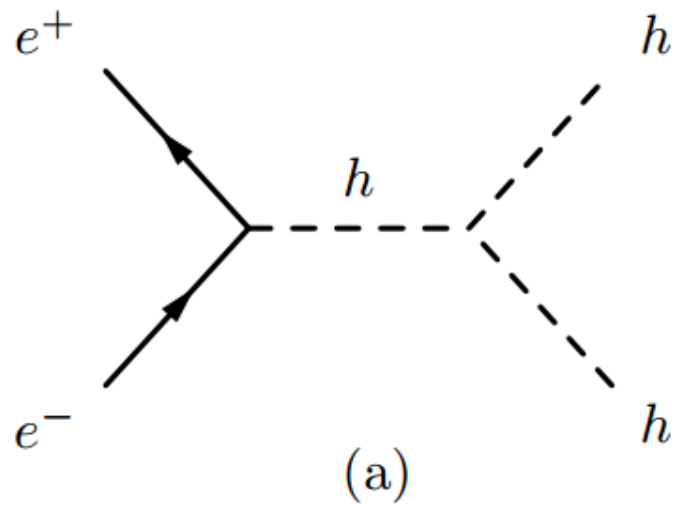
Li & Voloshin, 2013

Small in the SM = good for NP



# HH at lepton colliders

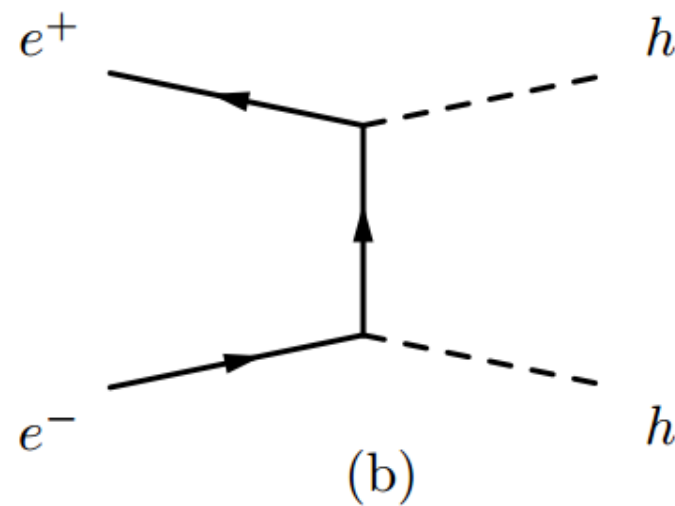
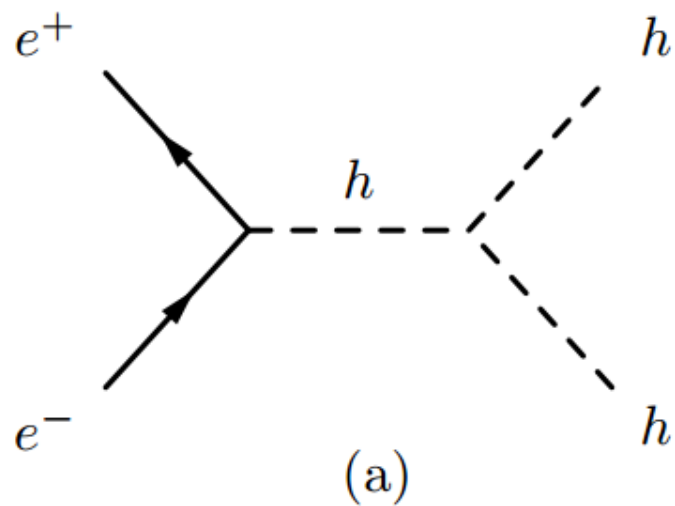
## Tree-level



$$\propto m_e \approx 0$$

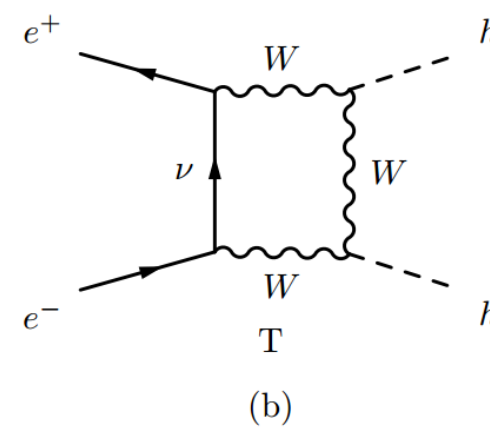
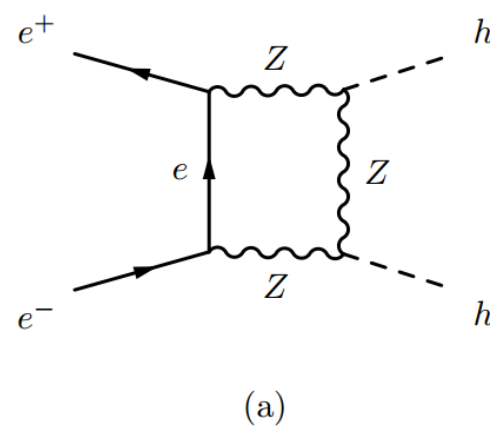
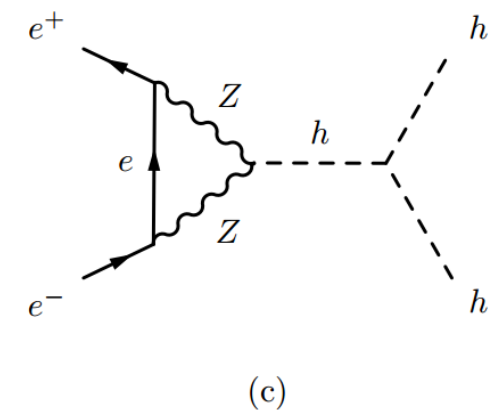
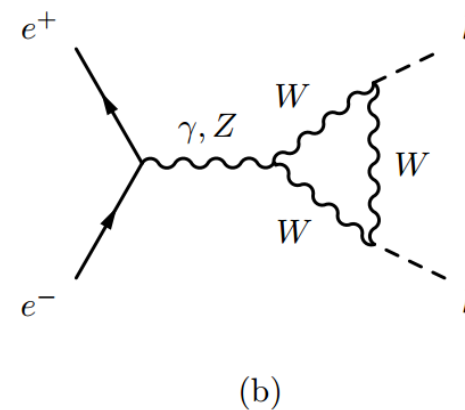
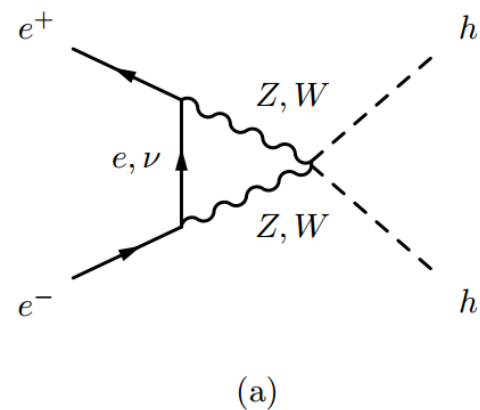
# HH at lepton colliders

## Tree-level

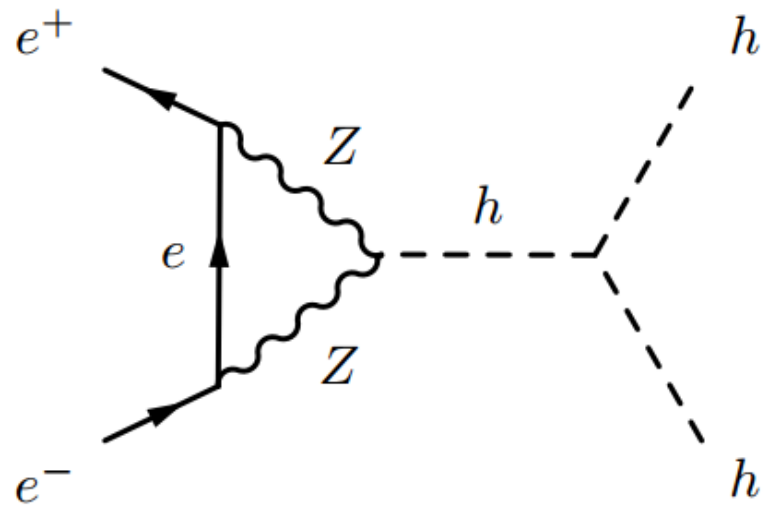


$$\propto m_e \approx 0$$

## One-loop

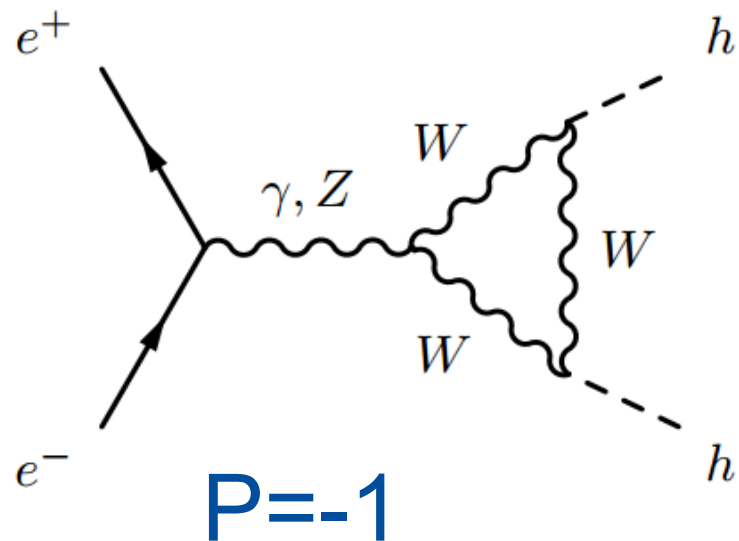


# HH at lepton colliders



$$\propto m_e \approx 0$$

correction to the electron Yukawa



$P=-1$

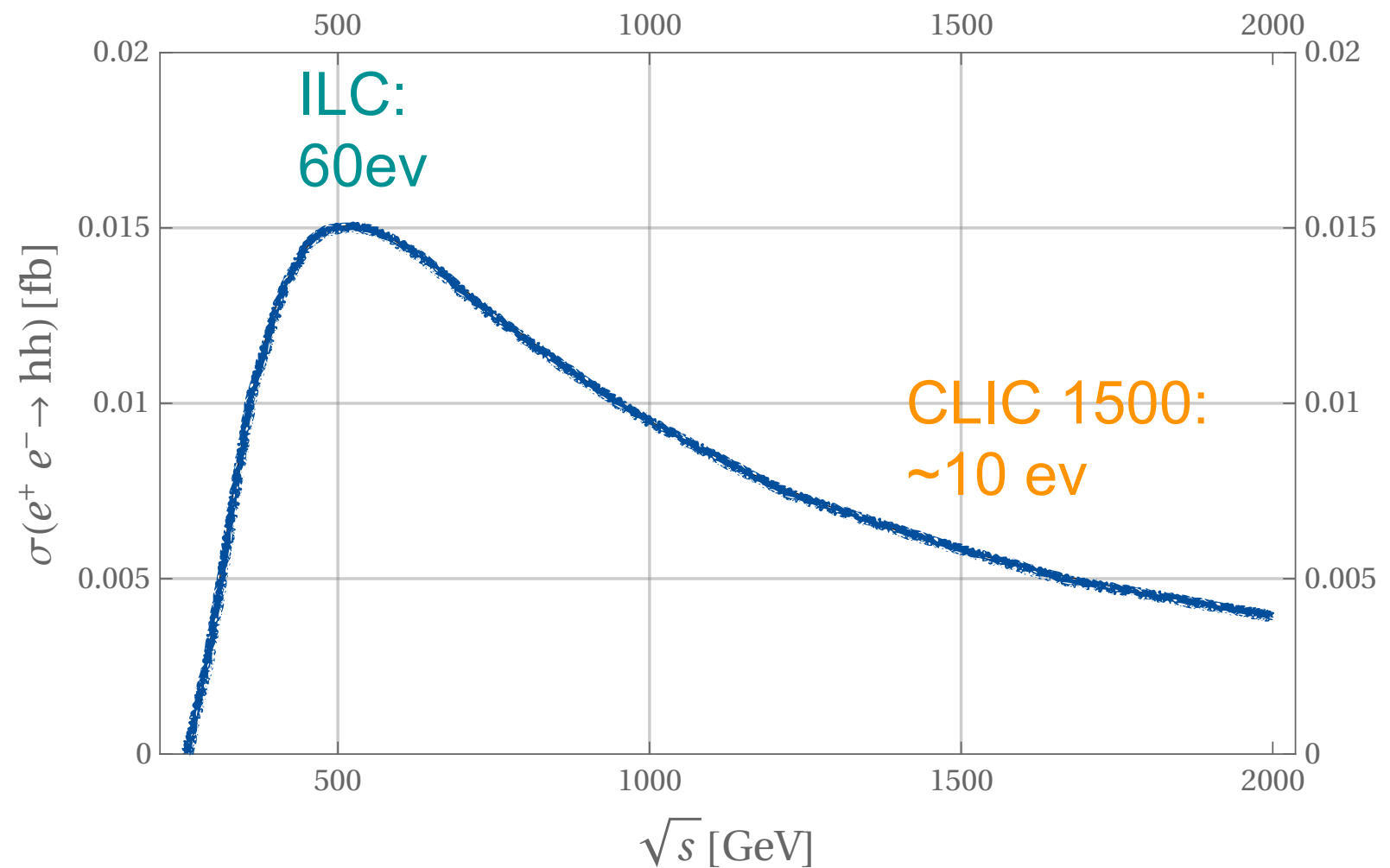
$P=+1$

= 0 by parity conservation

# HH at lepton colliders

$$|\mathcal{M}|^2 \sim \left| \begin{array}{c} e^+ \\ \swarrow \quad \searrow \\ \text{Z} \quad \text{Z} \\ \nearrow \quad \nwarrow \\ e^- \\ \swarrow \quad \searrow \\ \text{Z} \quad \text{Z} \\ \nearrow \quad \nwarrow \\ h \end{array} \right|^2$$

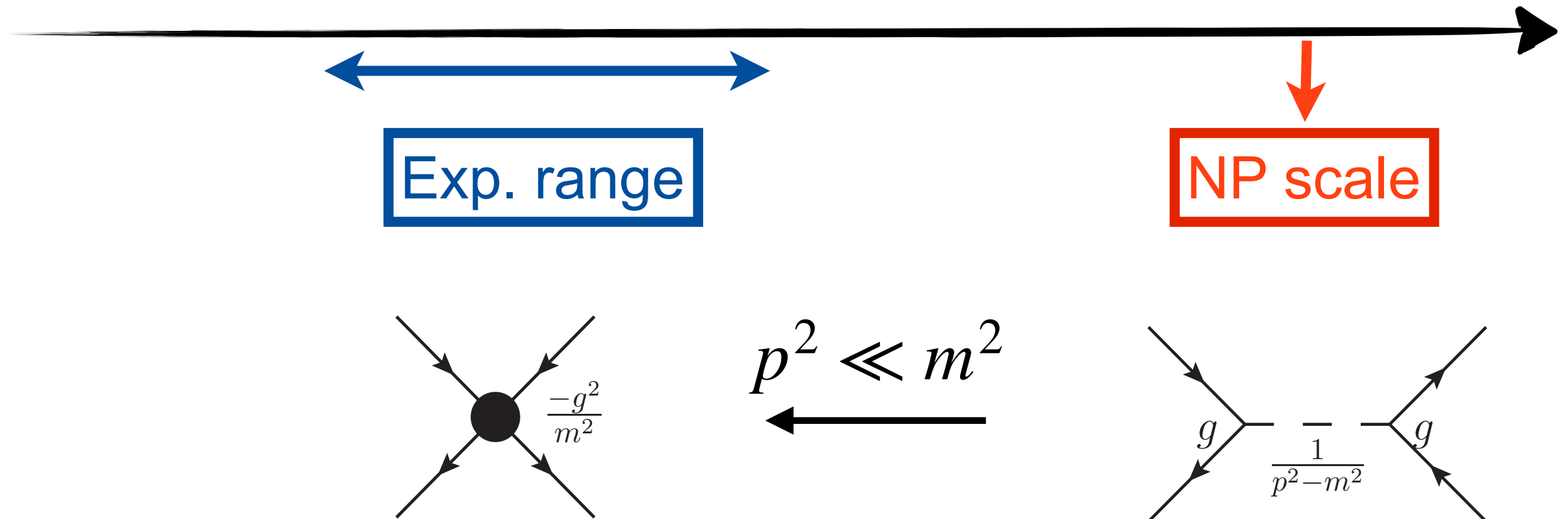
Benchmark	Experiment	$\sqrt{s}$ (GeV)	$L$ ( $\text{ab}^{-1}$ )
1	FCC-ee	350	2.6
2	CLIC	380	0.5
3	ILC	500	4
4	CLIC	1500	1.5
5	CLIC	3000	3.0



SMEFT operators for HH

# Indirect detection of NP

- Assumption : NP scale  $\gg$  energy probed in experiments  $E$



One assumption :  $p^2 \ll m^2$

Ex : Fermi theory  $-\frac{G_F}{\text{Sqrt}[2]} J^\mu J_\mu, \quad J_\mu = J_\mu^l + J_\mu^h, \quad J_\mu^l = \nu_l \gamma_\mu (1 - \gamma_5) l$

# Dim6 operators for HH

Grzadkowski et al., 2010

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} \mathcal{O}_i^6$$

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

Tree-level

One-loop  
thanks to eeZ,  
evW, hZZ, hWW  
modification:  
Constrained  
by LEP/LHC

Table 2: Dimension-six operators other than the four-fermion ones.

# Dim6 operators for HH

Most operators do not contribute (Parity/  $\propto m_e \approx 0$ )

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$Q_{duuu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

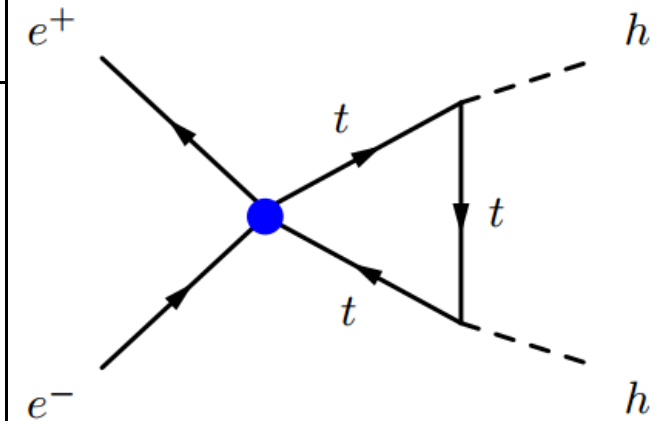


Table 3: Four-fermion operators.



# Dim6 operators for HH

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$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
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$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
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$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
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$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$Q_{duuu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

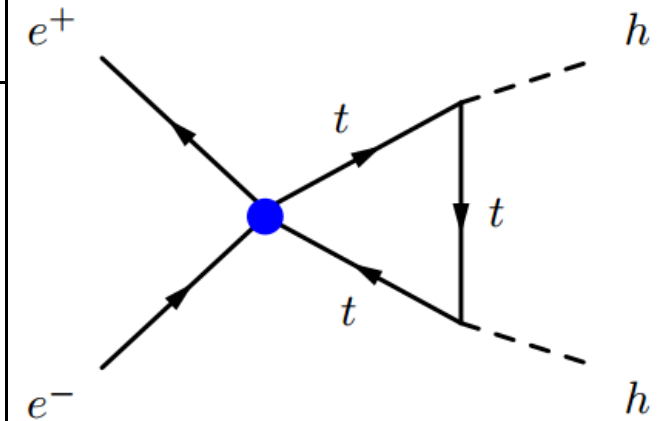
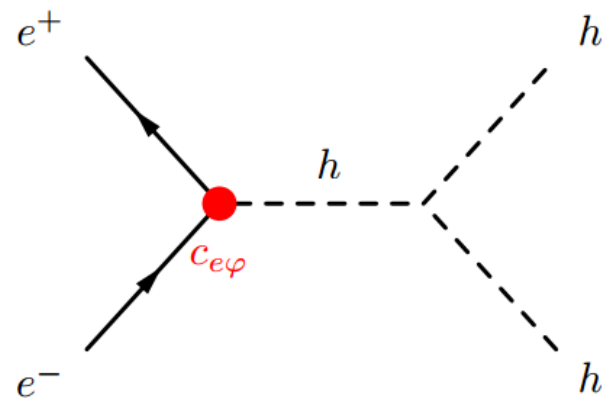


Table 3: Four-fermion operators.

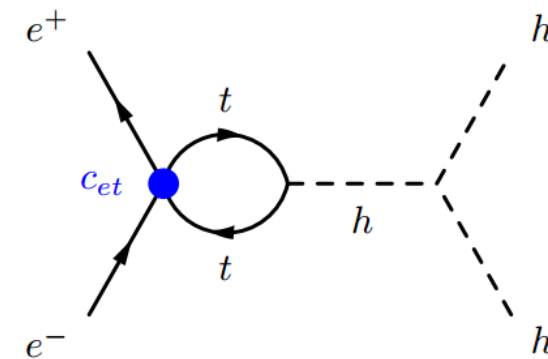
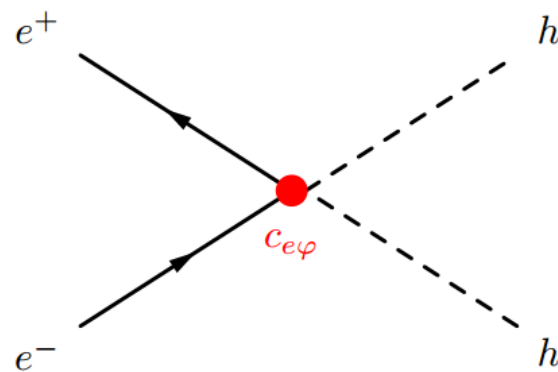
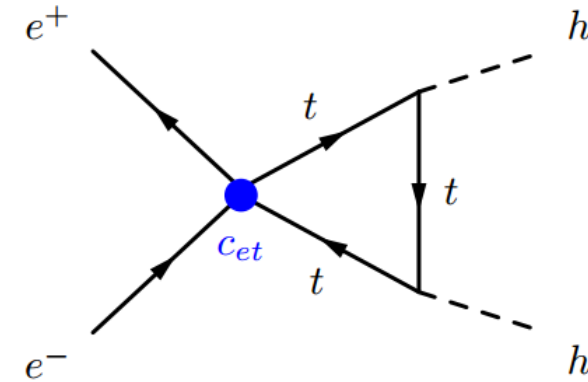
# Dim6 operators for HH

$$\frac{c_{e\varphi}}{\Lambda^2} (\varphi^\dagger \varphi - \frac{v^2}{2}) \bar{l}_L \varphi e_R$$



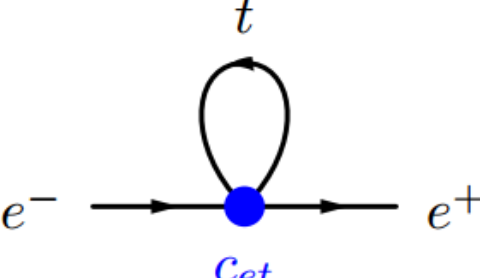
Correction to  
the electron  
Yukawa

$$\frac{c_{et}}{\Lambda^2} \epsilon_{ij} \bar{l}_L^i e_R \bar{q}_L^j t_R$$



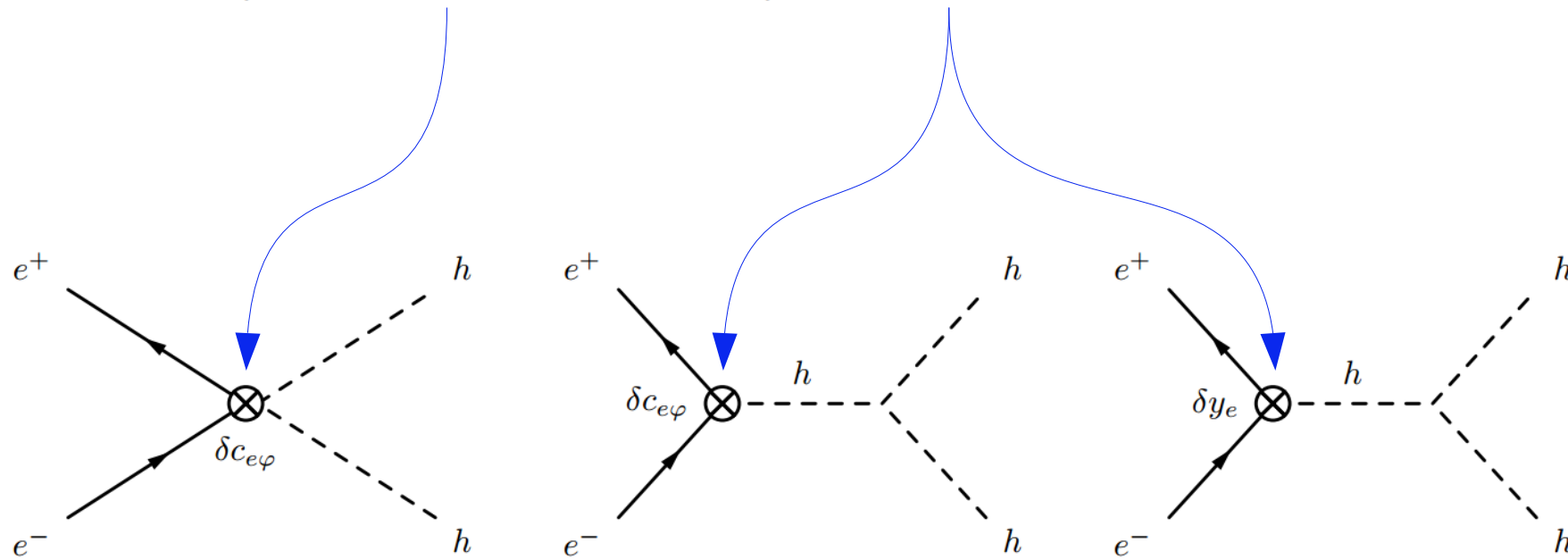
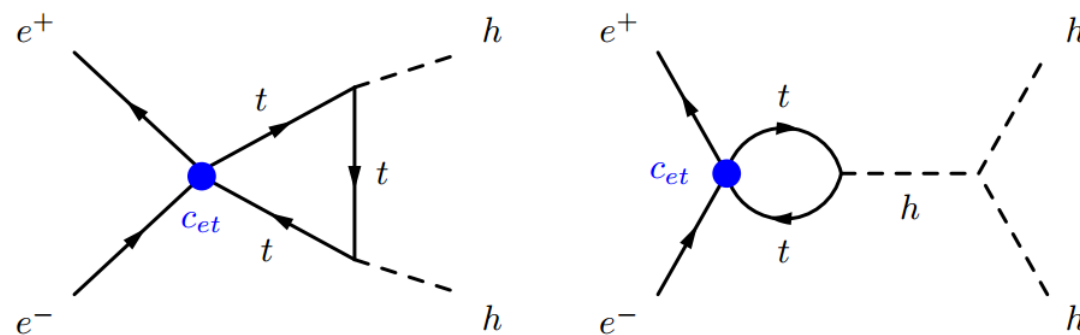
# Results

# Comments on the top loop



$$e^- \rightarrow e^+ \text{ (via } c_{et} \text{ and top loop)} = -i\Sigma_e = -i \frac{6}{(4\pi)^2} \frac{c_{et}}{\Lambda^2} m_t^3 \left( 1 + \frac{1}{\bar{\epsilon}} + \log \frac{\mu^2}{m_t^2} \right)$$

$$m_e = y_e \frac{v}{\sqrt{2}} + \frac{6}{(4\pi)^2} \frac{c_{et}}{\Lambda^2} m_t^3 \left( 1 + \log \frac{\mu^2}{m_t^2} \right)$$



$$\delta c_{e\varphi} = \frac{6}{(4\pi)^2} c_{et} y_t (y_t^2 - \lambda) \frac{1}{\bar{\epsilon}}$$

$$\delta y_e = -\frac{3}{(4\pi)^2} c_{et} v^2 y_t^3 \frac{1}{\bar{\epsilon}}$$

# Results for future colliders

$$\chi^2 \left( \sqrt{s}, \frac{c_{e\varphi}}{\Lambda^2}, \frac{c_{et}}{\Lambda^2} \right) = \frac{\left[ \sigma^{SMEFT} \left( \sqrt{s}, \frac{c_{e\varphi}}{\Lambda^2}, \frac{c_{et}}{\Lambda^2} \right) - \sigma^{SM} \left( \sqrt{s} \right) \right]^2}{\delta\sigma^2}$$

$$\delta\sigma^2 = \delta\sigma_{stat}^2 + \delta\sigma_{sys}^2$$

$$\delta\sigma_{stat} = \sqrt{\sigma^{SM}/L}$$

$$\delta\sigma_{sys} = \alpha\sigma^{SM} \quad (\alpha = 0.1)$$

Ind. 95% CL

Benchmark	Experiment	$\sqrt{s}$ (GeV)	$L$ (ab $^{-1}$ )	$ c_{e\varphi}/\Lambda^2 $ (TeV $^{-2}$ )	$ c_{et}/\Lambda^2 $ (TeV $^{-2}$ )
1	FCC-ee	350	2.6	$< 0.003$ ( $< 0.004$ )	$< 0.116$ ( $< 0.146$ )
2	CLIC	380	0.5	$< 0.004$ ( $< 0.006$ )	$< 0.143$ ( $< 0.184$ )
3	ILC	500	4	$< 0.003$ ( $< 0.004$ )	$< 0.068$ ( $< 0.083$ )
4	CLIC	1500	1.5	$< 0.003$ ( $< 0.003$ )	$< 0.027$ ( $< 0.035$ )
5	CLIC	3000	3.0	$< 0.002$ ( $< 0.002$ )	$< 0.012$ ( $< 0.015$ )

$$k = 1 \quad (k = 0.35)$$

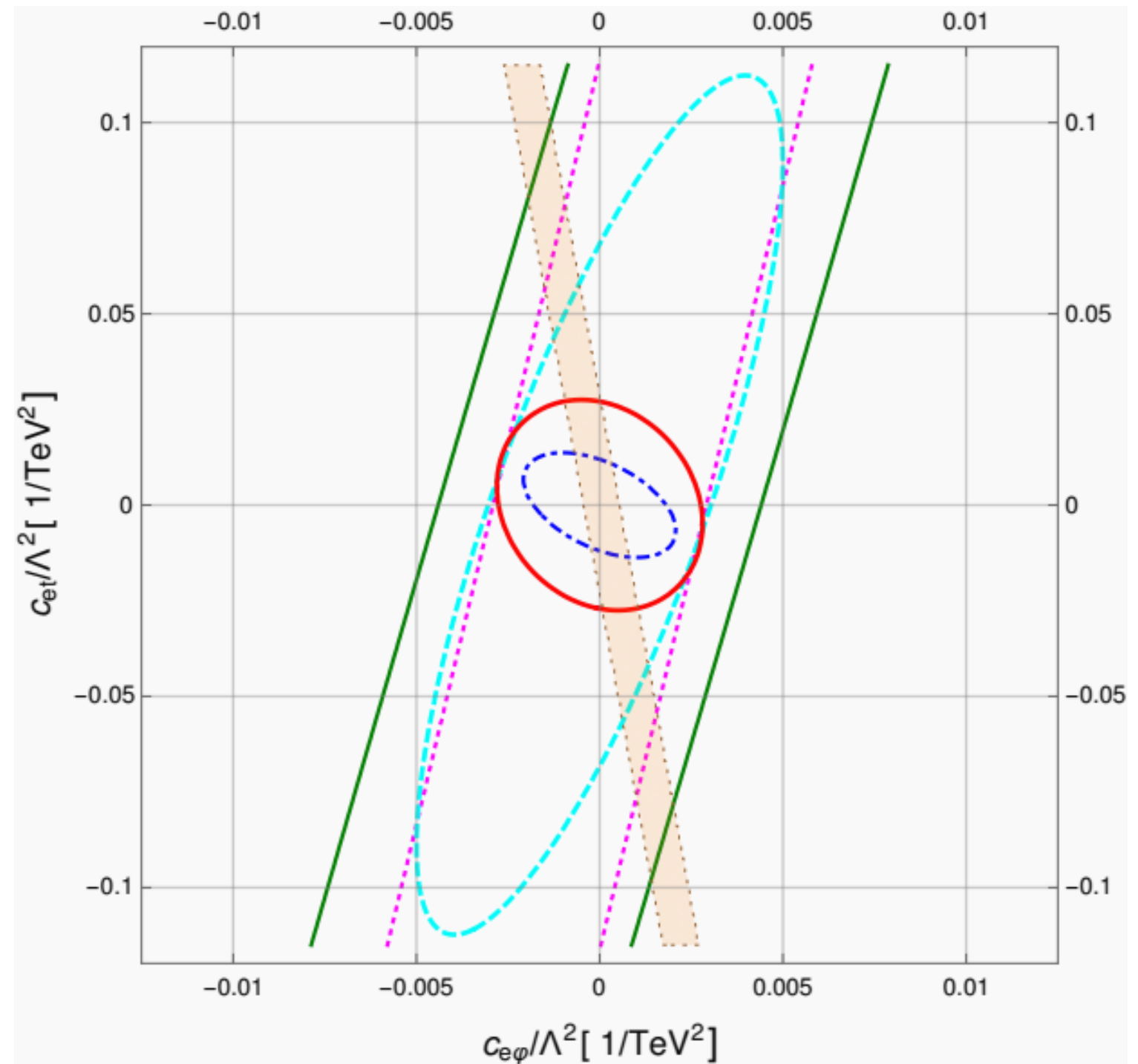
bottom decay

$$k = \text{BR}(h \rightarrow f_1 \bar{f}_1) \times \text{BR}(h \rightarrow f_2 \bar{f}_2)$$

# Results for future colliders

Benchmark	Experiment	$\sqrt{s}$ (GeV)	$L$ ( $\text{ab}^{-1}$ )
1	FCC-ee	350	2.6
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95%CL,  $k=1$



Other constraints

# Other constraints

Higgs coupling to electron (will improve)

$$\left| -\frac{m_e}{v} + \frac{c_{e\varphi}(\mu)v^2}{\Lambda^2\sqrt{2}} - \frac{3}{(4\pi)^2} \frac{y_t}{\sqrt{2}} \frac{c_{et}}{\Lambda^2} (4m_t^2 - m_h^2) \left[ f(m_h^2, m_t^2) + \log \frac{\mu^2}{m_t^2} \right] \right| \lesssim 600 \frac{m_e}{v}$$

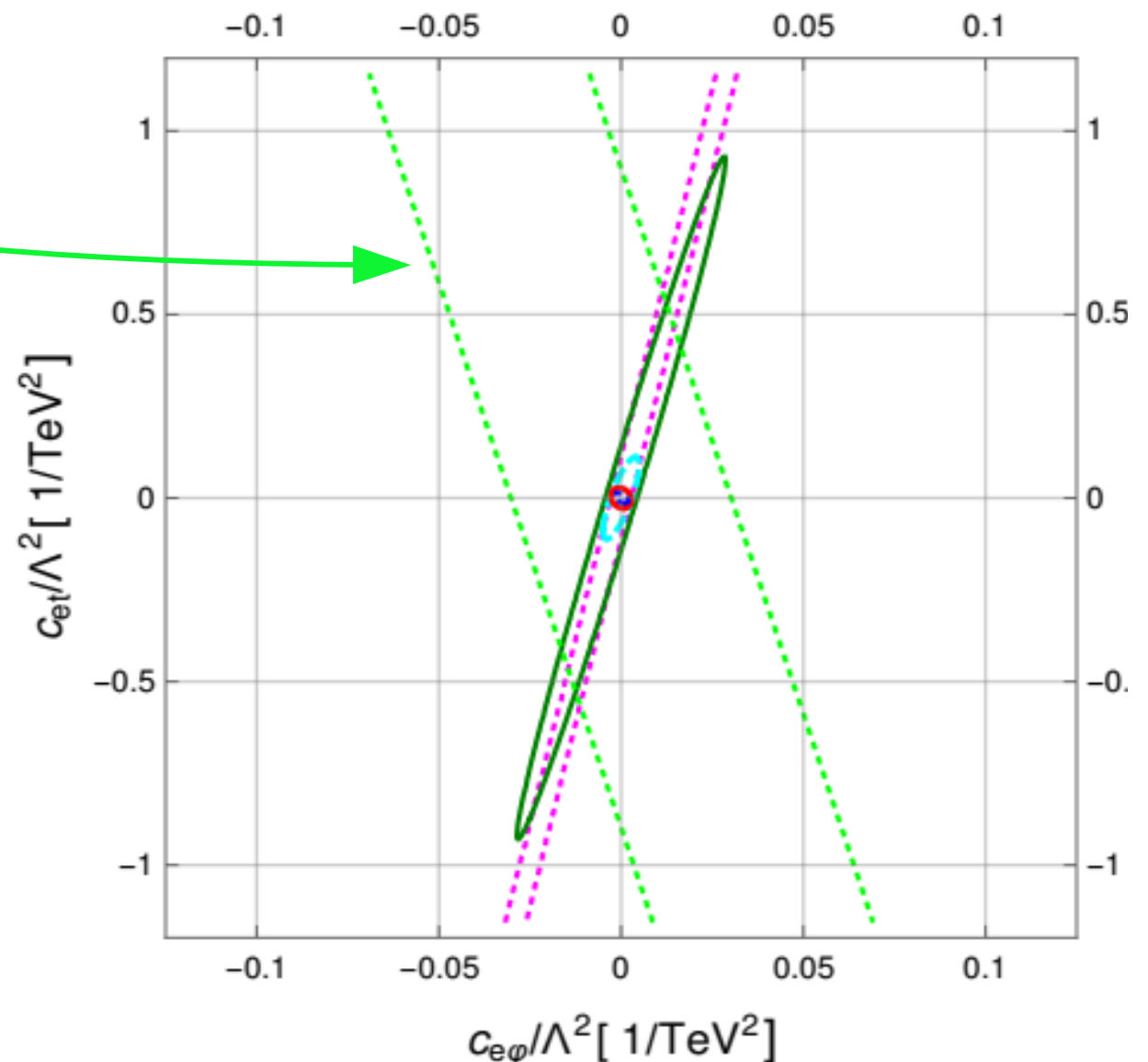
Fine tuning of the mass

$$|\delta m_e| \lesssim m_e$$

$$\left| \frac{c_{et}}{\Lambda^2} \right| \lesssim \frac{8\pi^2}{3} \frac{m_e}{m_t^3} \simeq 2 \times 10^{-3} \text{TeV}^{-2}$$

Top pair production

$$\frac{c_{et}}{\Lambda} \lesssim 10^{-2} - 10^{-3} \text{TeV}^{-2}$$





# Summary

# Summary

- HH production is small in the SM
- 2 operators are relevant for  $ee > HH$
- HH at lepton colliders:  $\frac{c_{e\varphi}}{\Lambda^2} \lesssim 10^{-3} \text{TeV}^{-2}$      $\frac{c_{et}}{\Lambda^2} \lesssim 10^{-1} - 10^{-2} \text{TeV}^{-2}$
- They will be further constrained by  $t\bar{t}b\bar{b}$ , H