



# FCC WEEK 2019

BRUSSELS, BELGIUM  
24 - 28 JUNE 2019  
Crowne Plaza Brussels  
Le Palace

## Electro-mechanical properties of Nb<sub>3</sub>Sn conductors for application to high-field magnets

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### WRITING the FUTURE

<http://fccweek2019.web.cern.ch/>





# Outline



- Introduction
- Critical Current Measurements of Cables under Transverse Load
- Computational Modeling
- Conclusions



# Introduction

## Strain dependence of Nb<sub>3</sub>Sn



- Superconducting **performance** of Nb<sub>3</sub>Sn are strongly **dependent** on the superconductor **strain state**
- In the case of **applied axial strain**, with a good approximation we can write

$B_{c2}(T, \epsilon) = B_{c2}(T, 0) s(\epsilon)$       Where  $s(\epsilon)$  is the *strain function* that ranges between 0 and 1

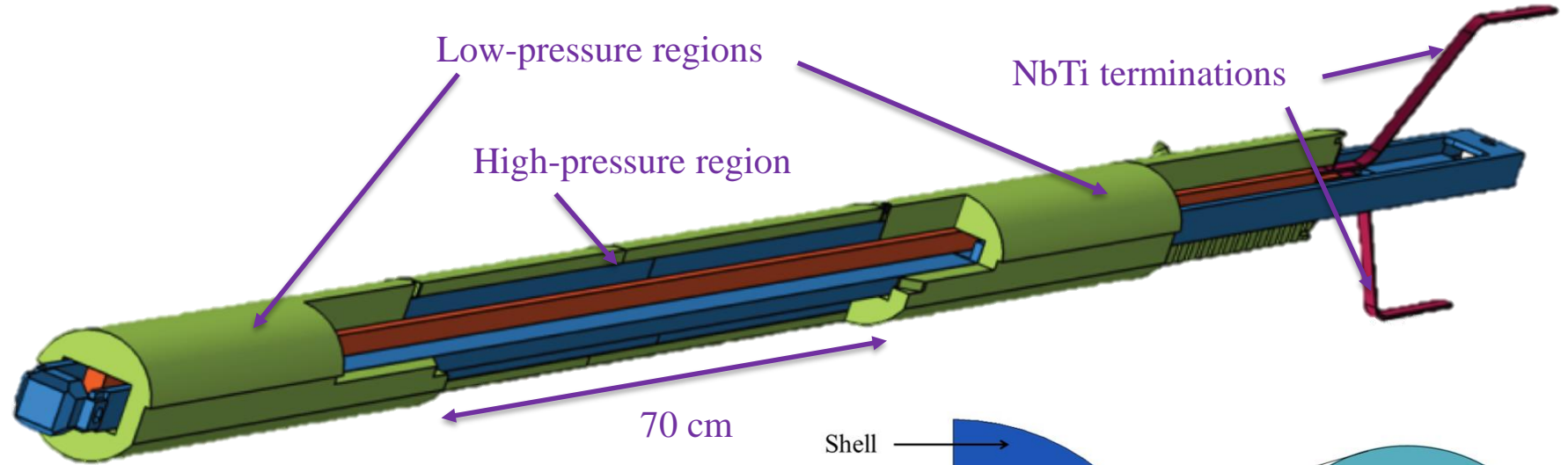
$$J_c(B, T, \epsilon) = C(T) b^{-0.5} (1-b)^2 \quad \text{Where: } b = \frac{B}{B_{c2}(T, \epsilon)}$$

- **Before cracking the filaments**, the same equation proved to be **valid** also in the case of **transverse loads**

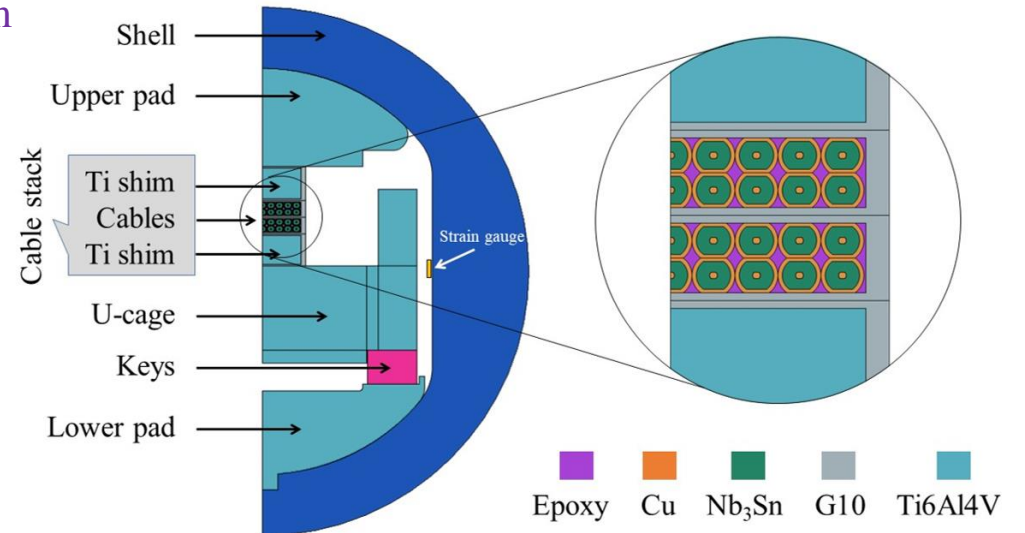
## CERN cable sample holder



Max transverse force: 1750 kN



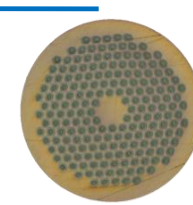
- Pro: very representative of the conductor behavior in a magnet
- Contra: long test campaigns, only narrow cables (~10 mm) can reach up to 250 MPa



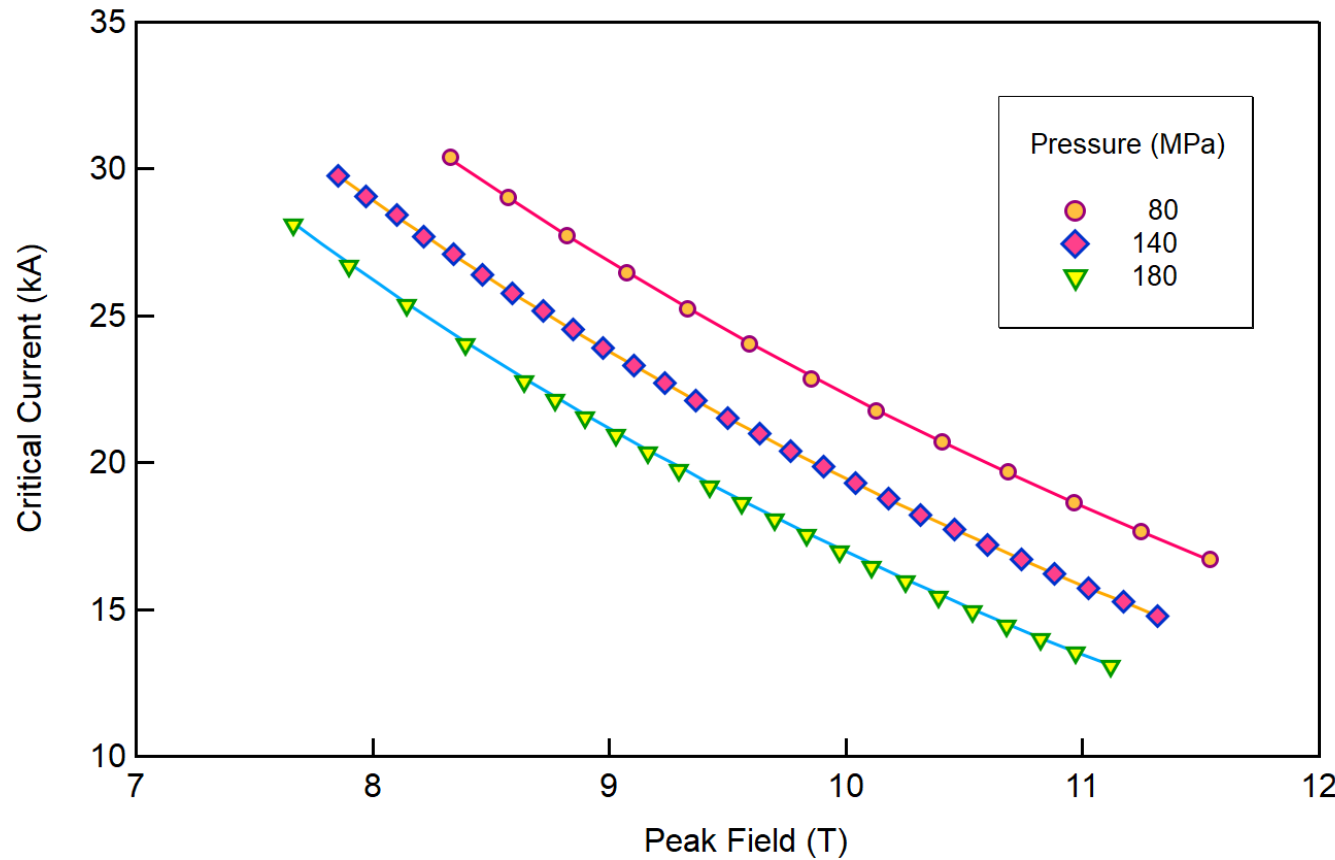


# PIT cable based on 1-mm wires

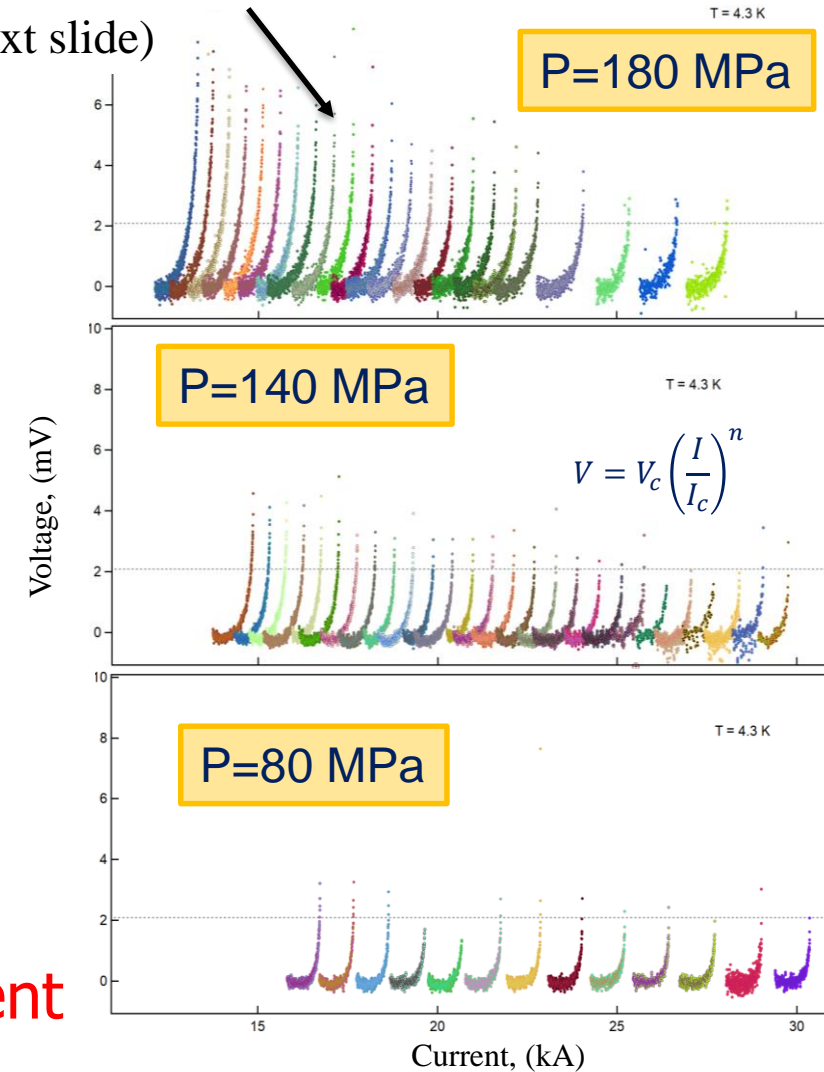
## Voltage-Current Measurements



Typical results for a PIT Cable measured at CERN at 4.3 K (full test sequence in next slide)



Different Curves at different applied magnetic fields



● **Significant Reversible Reduction** of the critical current

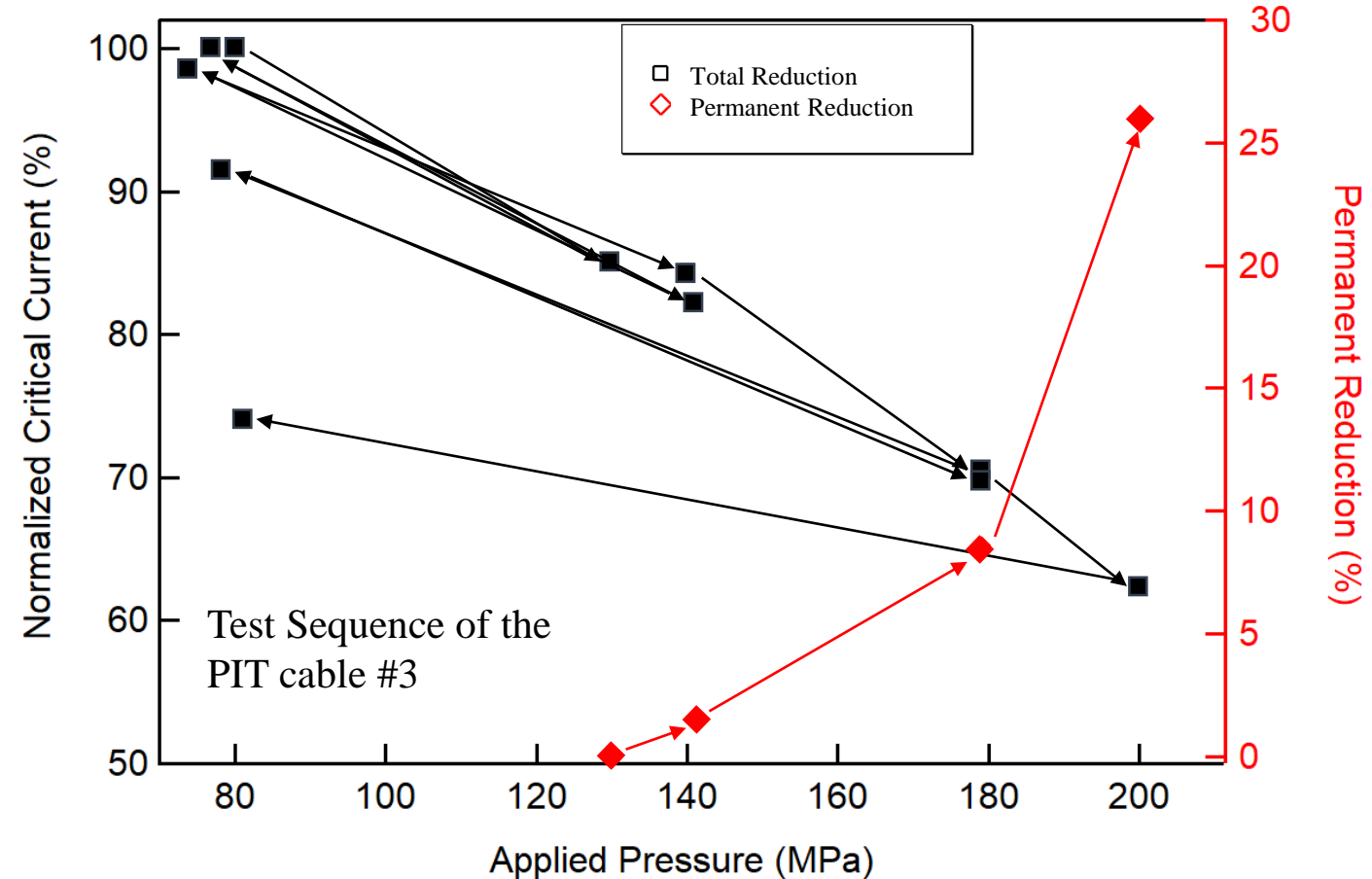
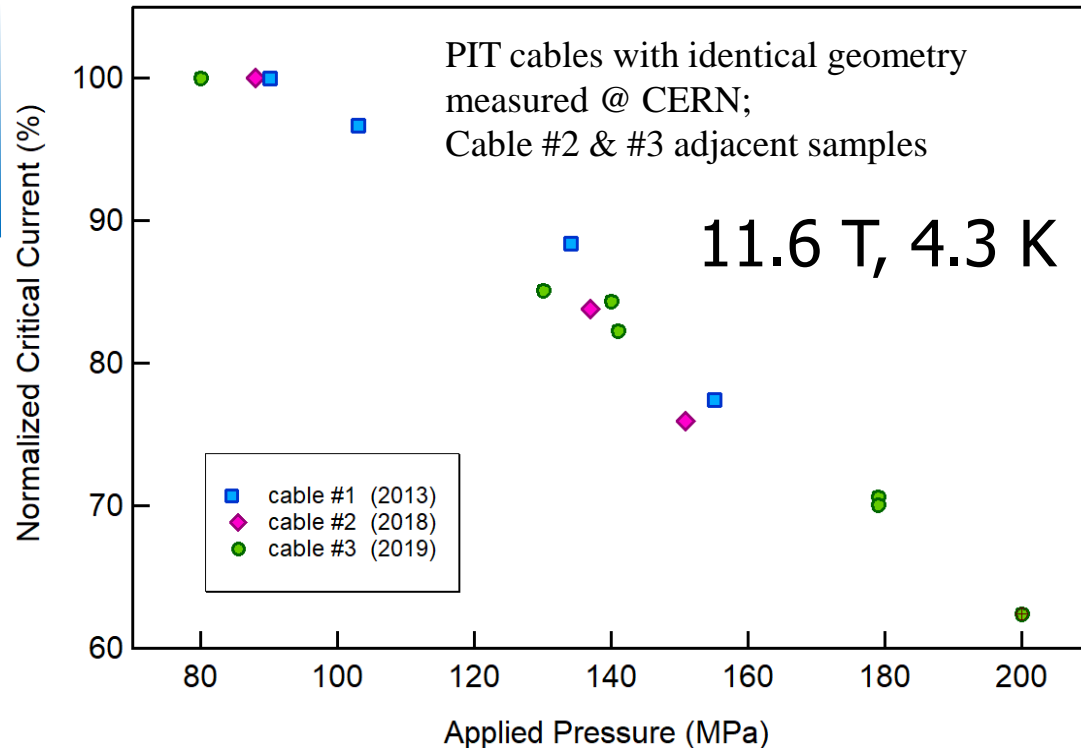


# PIT cable based on 1-mm wires



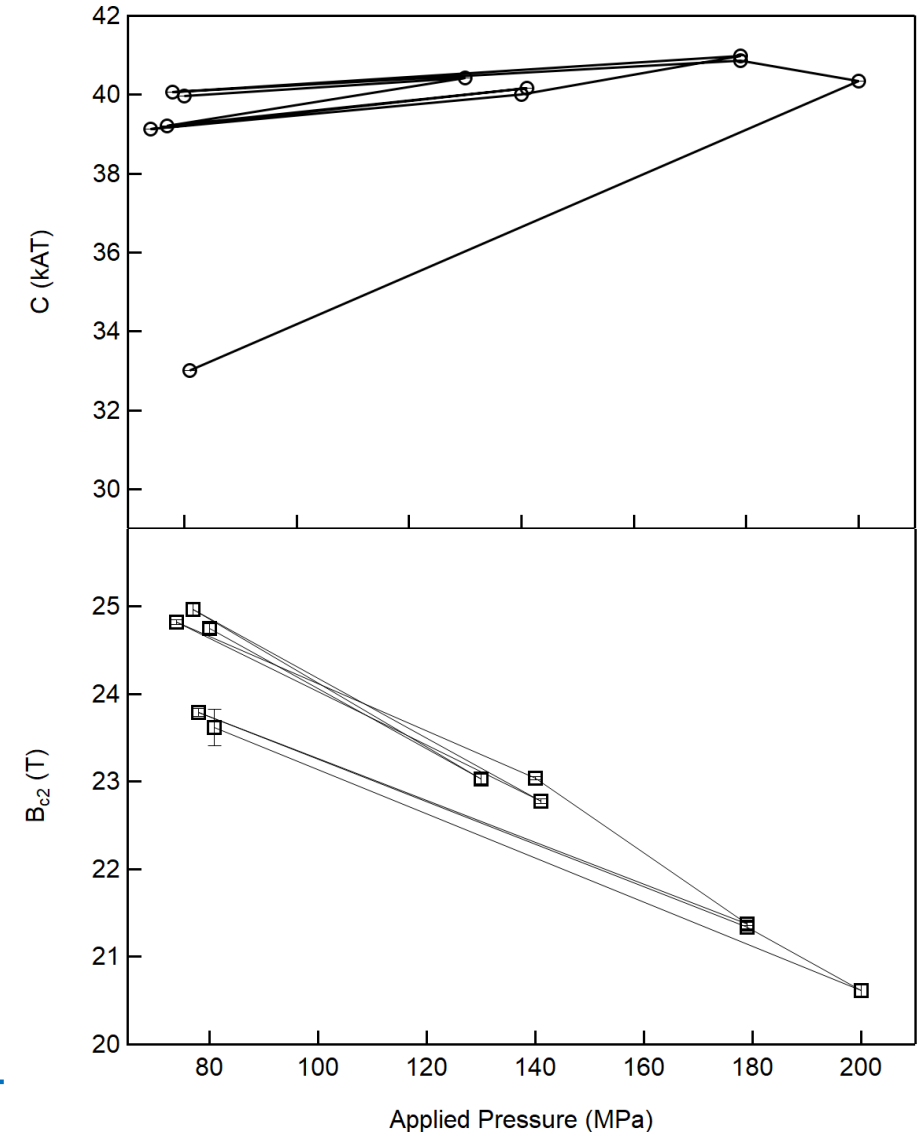
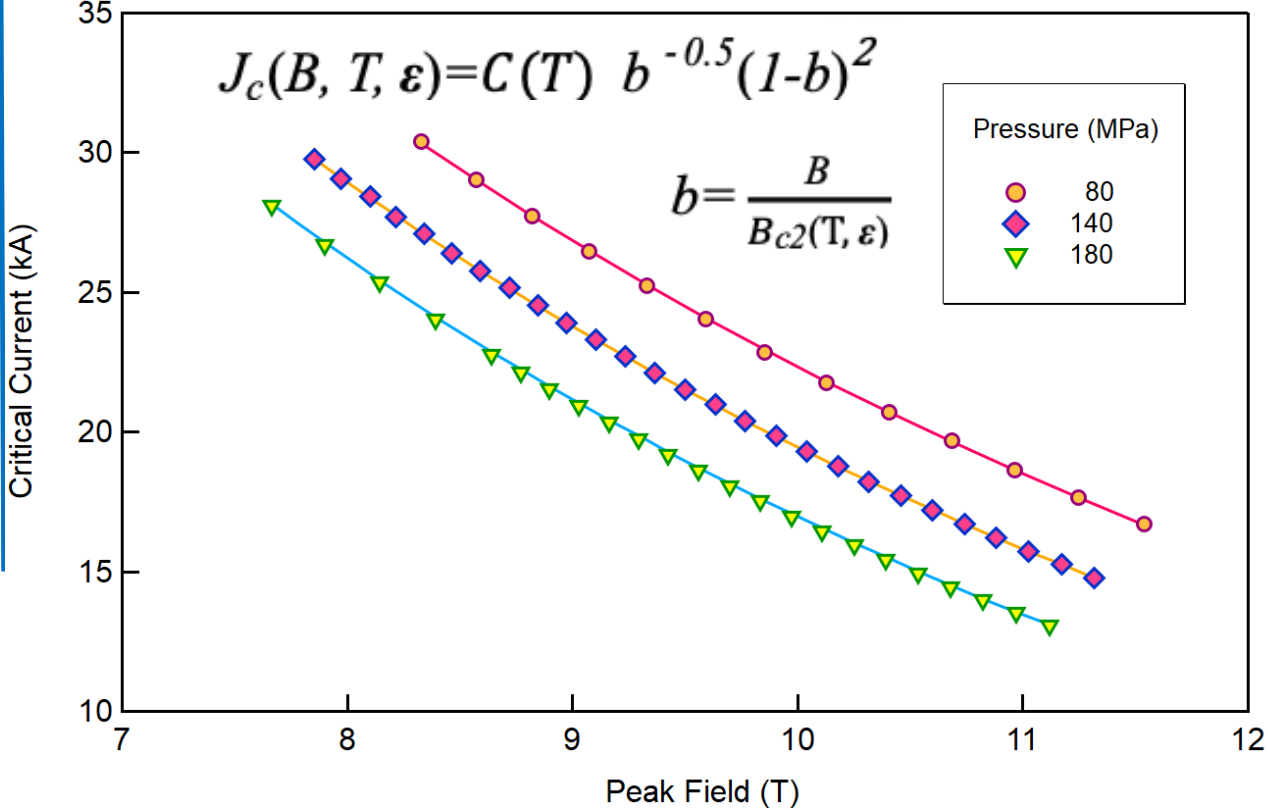
## Measurement Reproducibility & Permanent Reduction

New measurements at CERN and Twente **confirmed** and **consolidated** the results observed in 2013; furthermore they allowed **extending** our **understanding**



**Onset permanent** reduction **~130 MPa**, up to **~180 MPa** most likely due to **plasticization of copper afterwards**, to **cracks in the filaments**

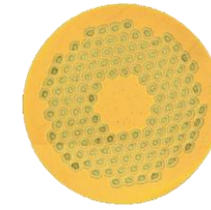
## Scaling the $I_c$ Reduction



- $I_c$  reduction mainly due to the decrease of the upper critical field  $B_{c2} \rightarrow$  larger  $I_c$  reduction at larger fields: at **150 MPa and 1.9 K**  $\sim 20\%$  at 12 T and  $\sim 45\%$  at 19 T



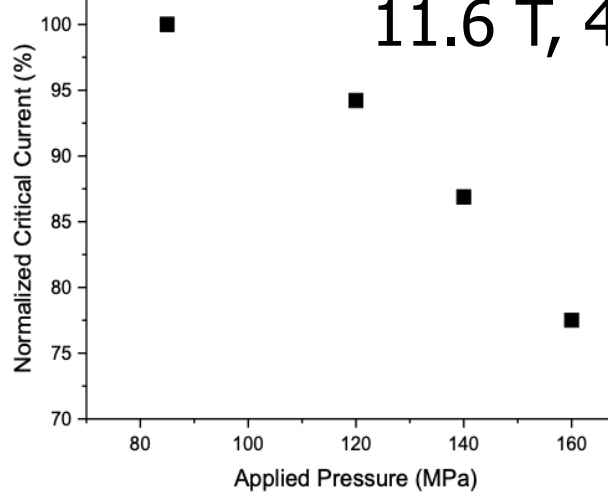
# RRP Cable based on 1-mm wires



## Critical Current Reduction

Test at CERN

11.6 T, 4.3 K



● The **RRP** cable has still the **same behavior** of the **PIT** cable but it is **less sensitive** to transverse load

➤ Onset **permanent**  $I_c$  reduction

1. PIT: ~130 MPa

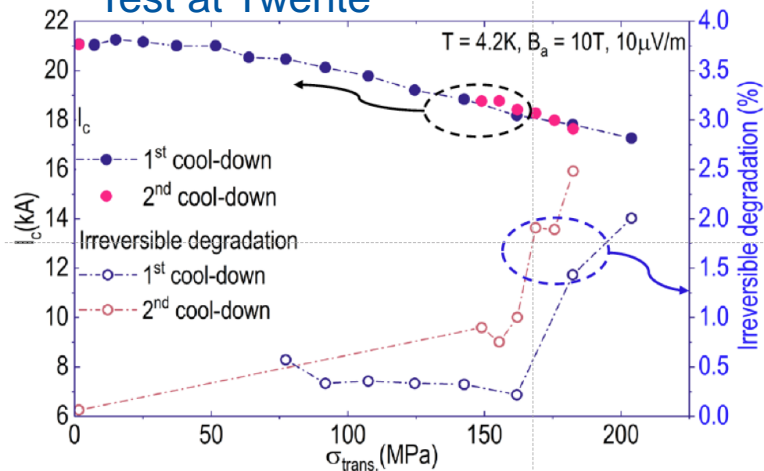
2. RRP: ~170 MPa

➤ **Total**  $I_c$  reduction at 11.6 T and **150 MPa**

1. PIT: ~ 20 %

2. RRP: ~ 15 %

Test at Twente\*



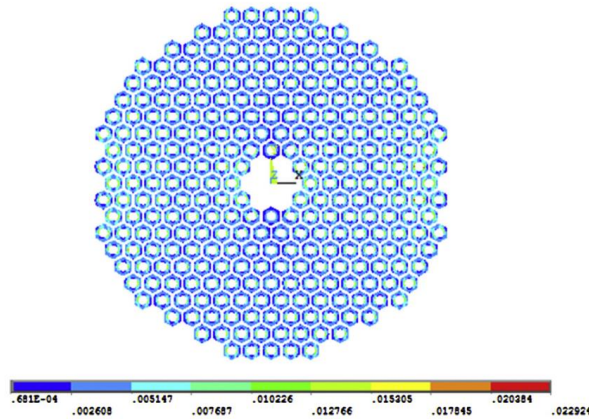
\*Courtesy of M. Dhalle



# Computational Modeling

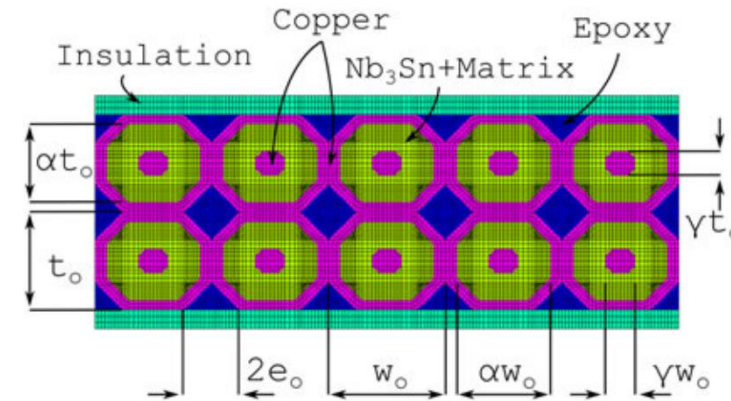
## Introduction – Previous Studies

Wang – wire, UniGe



T. Wang, L. Chiesa, M. Takayasu, and B. Bordini, *Cryogenics (Guildf.)*, vol. 63, pp. 275–281, 2014.

Vallone – cable, FRESKA



G. Vallone, B. Bordini, and P. Ferracin, *IEEE Trans. Appl. Supercond.*, vol. 28, no. 4, 2018.

### General Idea

- 2D mechanical FEM  $\rightarrow$  strain field  $\boldsymbol{\varepsilon} \rightarrow$  scaling law  $J_c(s(\boldsymbol{\varepsilon}))$
- $s(\boldsymbol{\varepsilon}) = s(I_1, J_2)$  [5] where  $I_1$  is the **first invariant** of the **strain tensor** and  $J_2$  is the **second invariant** of the **deviatoric strain tensor**

[5] B. Bordini, P. Alknes, L. Bottura, L. Rossi, and D. Valentini, " *Supercond. Sci. Technol.*, vol. 26, no. 7, p. 075014, 2013.



# Computational Modeling

## Introduction – Aims of this work

Both models were quite successful in reproducing the experimental results however, they rely on some **assumptions** that deserve to be further investigated

### Aim

Study these assumptions to enhance the understanding of the physical phenomena involved. Most relevant **assumptions**:

- 1) longitudinal strains/stresses (**plane strain** [6] and the **plane stress** [7])
- 2) the necessary strain amplification factor when the wire layout is simplified and the material properties are **homogenized** [7]
- 3) no **current redistribution**

### How?

A 3D FEM model with no geometrical and material assumptions and no hypothesis on the longitudinal strain

Add, in the future, an electric 3D model to simulate the possible current redistribution

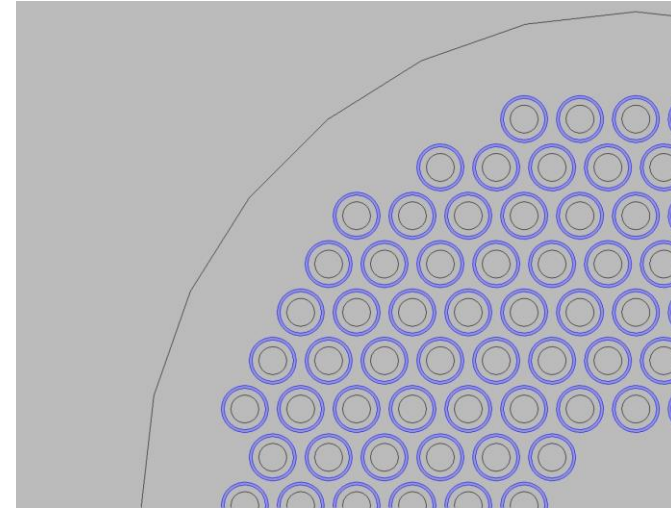
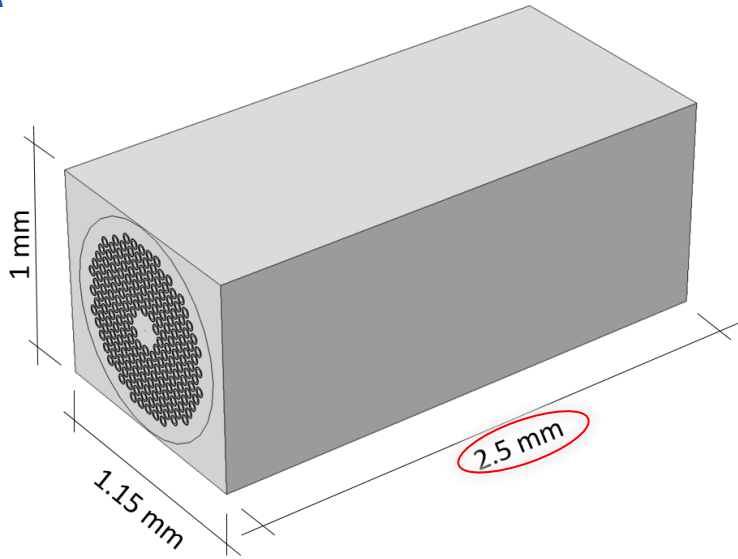
[6] T. Wang, L. Chiesa, M. Takayasu, and B. Bordini, "Cryogenics (Guildf).", vol. 63, pp. 275–281, 2014.

[7] G. Vallone, B. Bordini, and P. Ferracin, IEEE Trans. Appl. Supercond., vol. 28, no. 4, 2018.

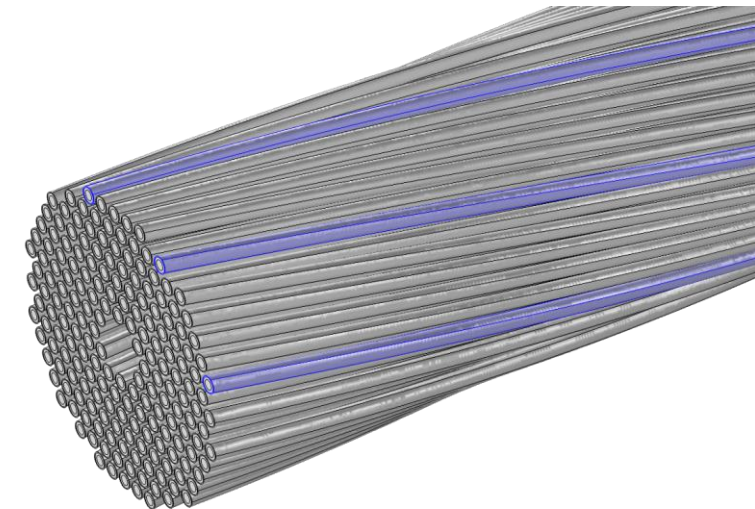


# Computational Modeling

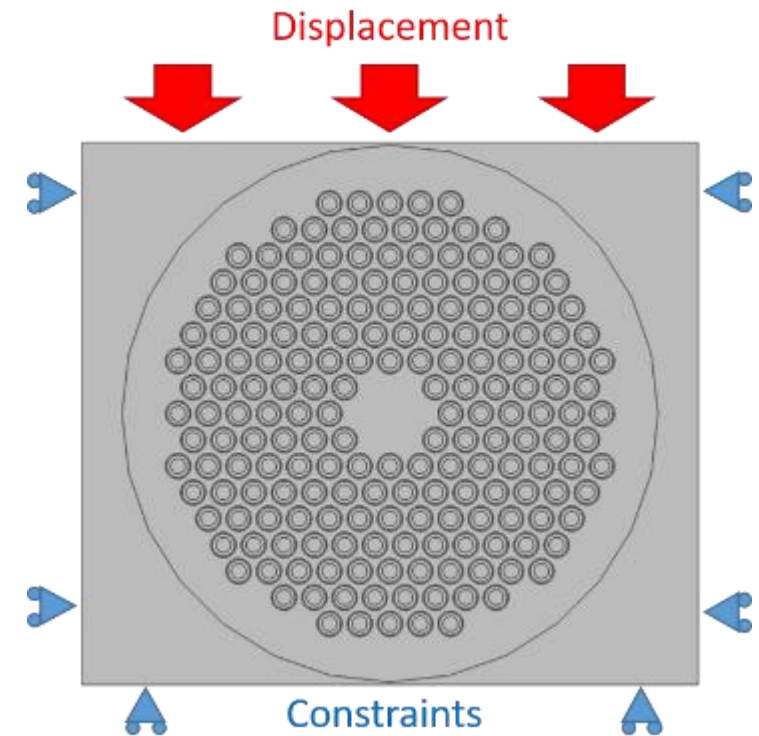
## Model Geometry



- High computational costs: smallest representative segment = **2.5 mm** long
- **No homogenizations**: All the 192 filaments are modeled
- The strand is **twisted** (15 mm)

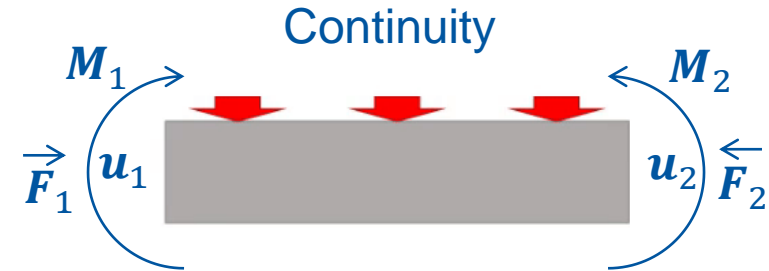


- Groove and anvil are treated as rigid bodies: modeled as boundary constraints
  - Lateral and bottom faces are free to slide on their respective planes
  - Progressive, compressive displacement on the top face



Two possible set of boundary conditions on the strand ends to study the extreme cases:

**Clamped** and symmetric by translation:  
continuity  $u_1 = u_2$



**Free to elongate** and symmetric by translation:  
 $u_1 - u_2 = [q \ 0 \ 0]'$  with  $q$   
such that forces and couples are null:

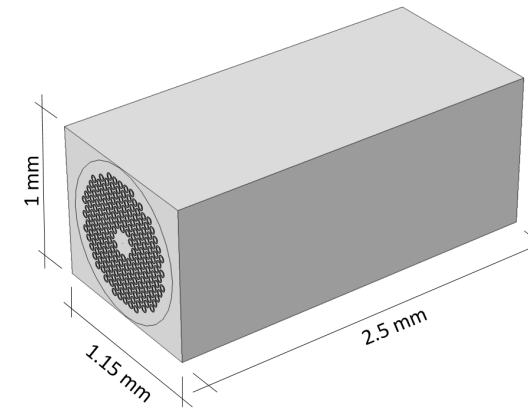
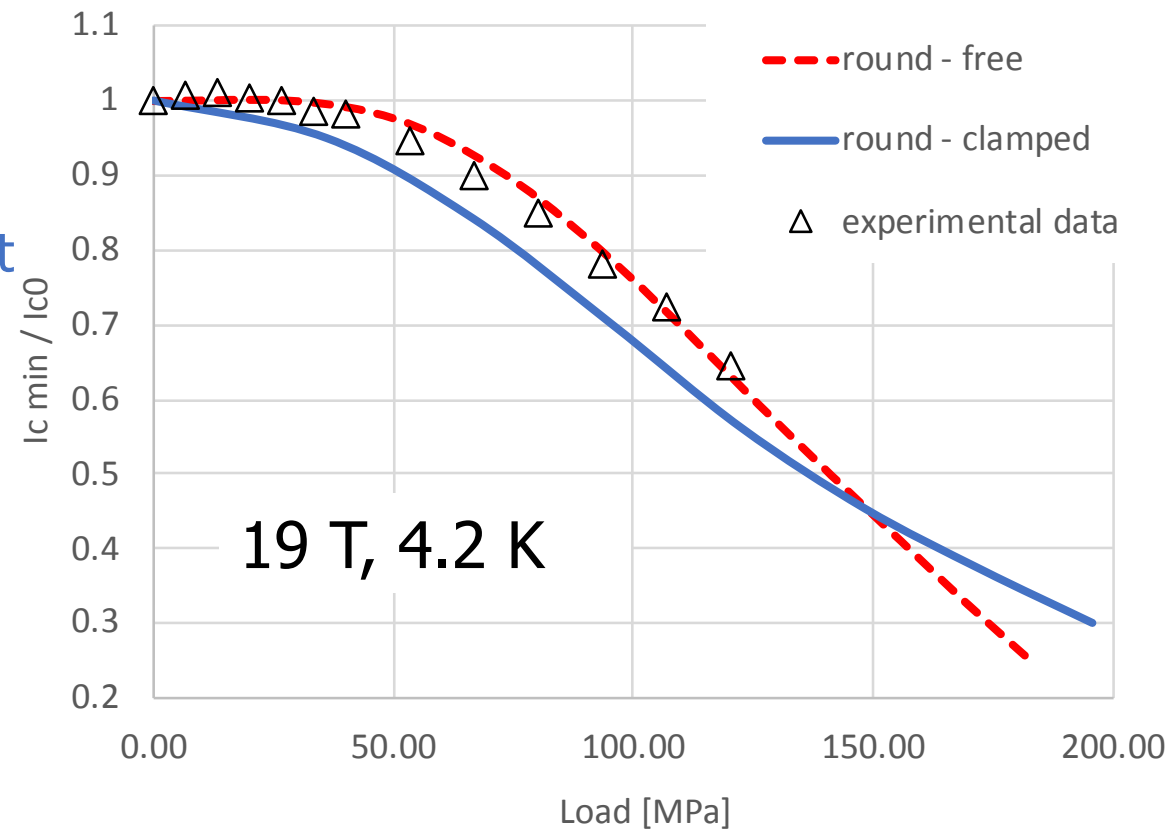
$$F_1 = F_2 = M_1 = M_2 = 0$$



- Hypothesis: **no current redistribution**

➤  $I_c$  dictated by the most strained filament

- **Good agreement with experimental data [4]**



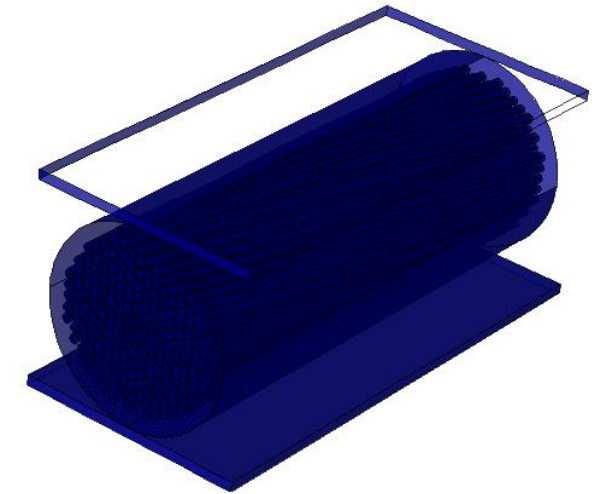
$$\text{Load} = \frac{1}{A} \int_A \sigma_{zz} dA$$

$$A = 1.15 \text{ mm} * 2.5 \text{ mm}$$

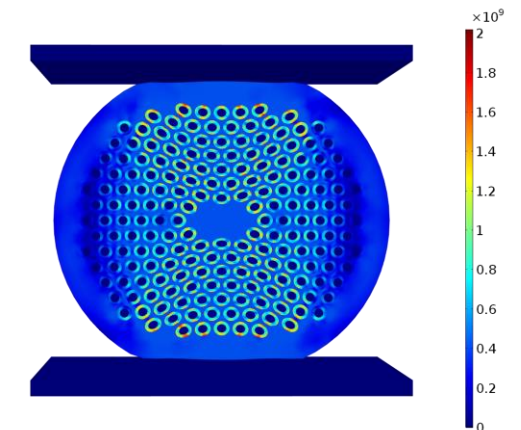
[4] C. Calzolaio *et al.*, *Supercond. Sci. Technol.*, vol. 28, no. 5, pp. 1–11, 2015.

## Rolled strand: deformed configuration

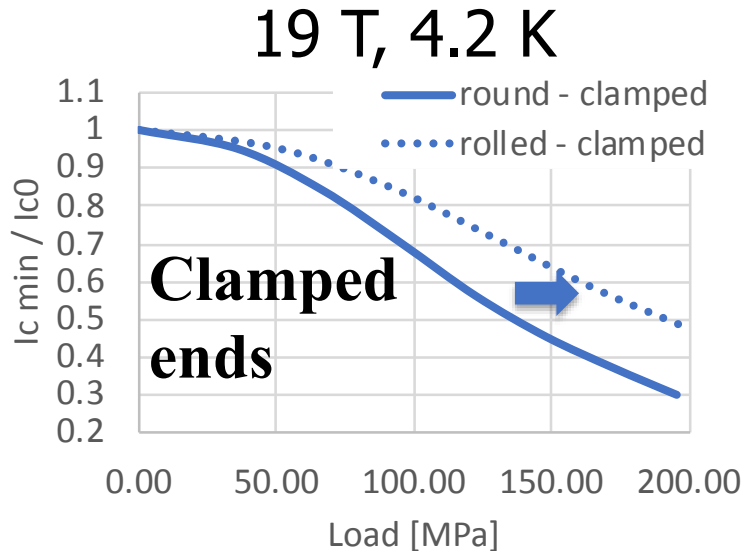
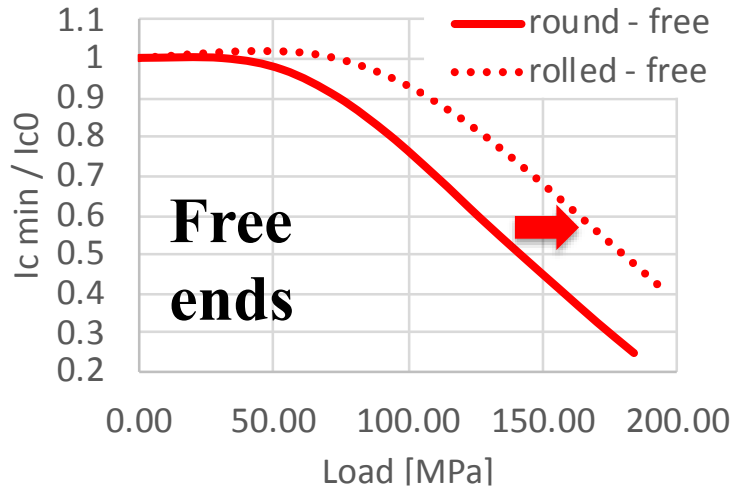
- Rolled strand (15% def.) are more representative of the geometry of the strand in a Rutherford cable
- In order to study this case, the deformed configuration is required
- An additional simulation of rolling is performed: the strand is deformed plastically between 2 rigid plates



Rolling



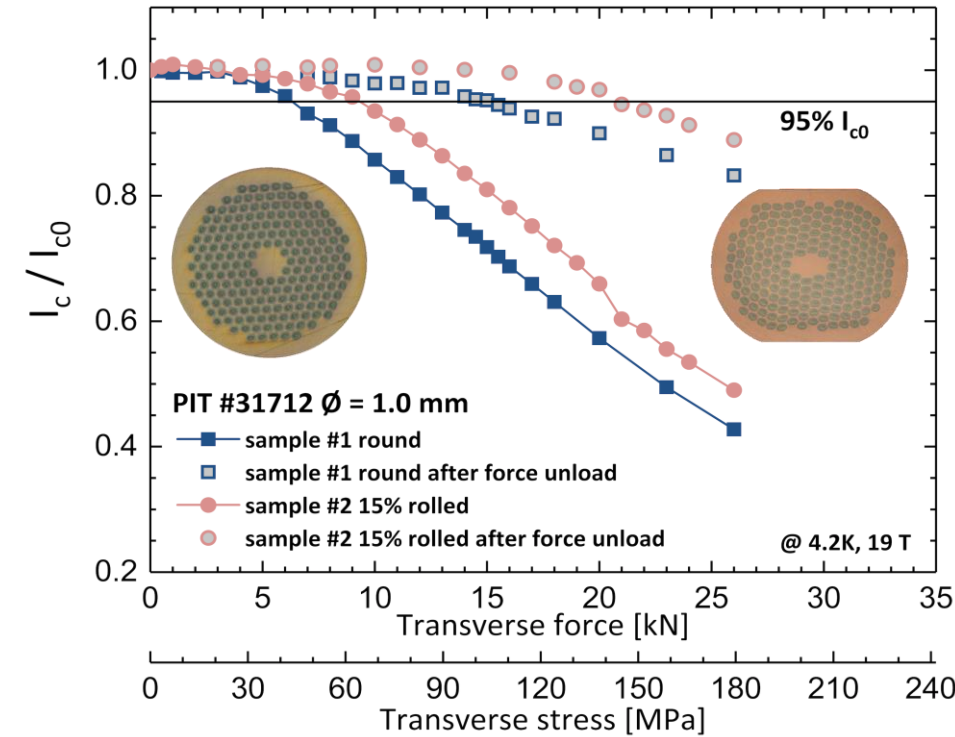
## Results $I_c$ reduction PIT wires: Round vs 15% Rolled



- The model reproduces the lower sensitivity of 15% rolled samples with respect to round wire samples

- The same performance reduction is obtained at **40 MPa larger** loads

- The model is in good agreement with the experimental data from the University of Geneva



Courtesy of C. Senatore



# Conclusions

- The **effect** of the **transverse load** on the **superconducting performance** of Nb<sub>3</sub>Sn cables is **relevant** already at **150 MPa** and has to be taken into account in the **design** of high field accelerator **magnets**
- **Before cracking** the filaments (at least up to 180 MPa), the **critical current reduction**:
  - is mainly due to a **decrease** of the **upper critical field** and can be **described** with the well established **scaling laws** developed for the case of applied axial strain  $I_c(B, T, \varepsilon) = I_c(B, T, s(\varepsilon))$  - where  $s$  is the *strain-function*
  - can be **estimated** with mechanical Finite Element Method models coupled with the **exponential strain-function** developed at CERN



Future Circular Collider Conference

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