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EFT approach to searches for new physics at the LHC

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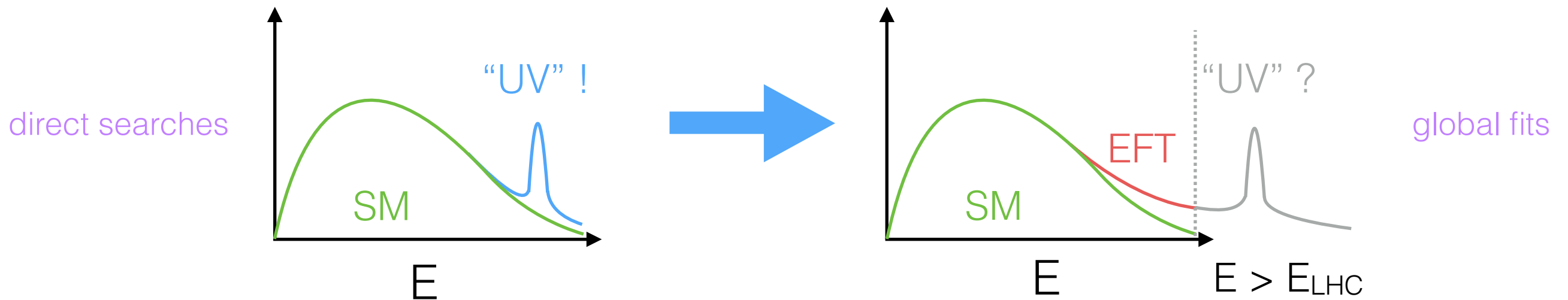
Be.HEP summer solstice meeting 2018

21st June 2018

Introduction

- The LHC is entering a **precision era**
 - No clear evidence for new physics from **direct searches**
 - We are approaching the **limits of the 'energy frontier'**
 - Higgs boson discovery has all but completed the picture of the Standard Model (SM) Electroweak (EW) sector
 - Properties consistent with SM expectations
 - Complementary approach: searches for **deviations in SM processes**
- Many channels are becoming **systematics dominated**
 - Requires **high precision** theory input including higher order corrections
 - Fixed order (FO) & interfaced with parton shower (PS)
 - Both for SM and BSM effects

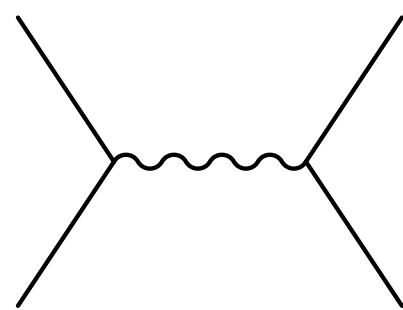
From bumps to tails



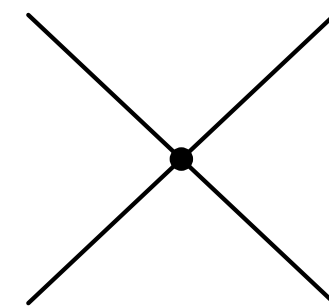
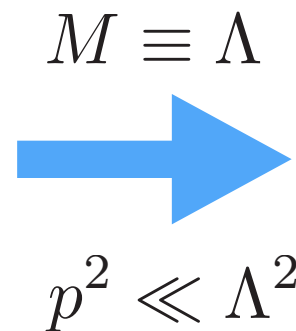
- Possibility that new states exist (just) beyond the energy reach of the LHC
 - We may still observe *indirect* effects of such particles in the kinematic *tails* of distributions, e.g., LEP limits on $\sim \text{TeV } Z'$
 - Intrinsically *small effects* that require precise theoretical control on signal and background predictions
- Framework: SM effective field theory (**SMEFT**)
 - Theoretically consistent, 'model independent' approach to *deviations* of interactions between SM fields

SMEFT

- Operator expansion: $\mathcal{L}_{\text{eff}} = \sum_i \frac{c_i \mathcal{O}_i^D}{\Lambda^{D-4}}$ more: fields
derivatives
- Heavy states are integrated out
 - Leaving only local operators built from SM fields
 - We are sensitive to these via large momentum flows through effective vertices (i.e. tails of energy distributions)
 - Truncated at dimension 6 (leading B & L preserving interactions)



$$\frac{g^2}{p^2 - M^2}$$



cf. Fermi Theory

'Matching'

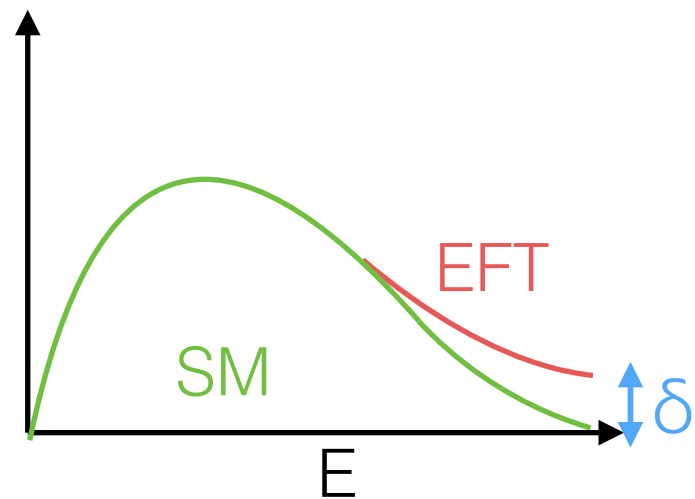
D=6

$$-\frac{g^2}{\Lambda^2} \left[1 + \frac{p^2}{\Lambda^2} + \frac{p^4}{\Lambda^4} + \dots \right]$$

SMEFT: the new SM

- Wilsonian approach: our world is a low energy EFT
 - SM: all possible **relevant** & **marginal** operators
 - SMEFT: tower of **irrelevant** operators
- $SU(3)_C \times SU(2)_L \times U(1)_Y$ gauge invariant operator set
 - **Linear** realisation of EW symmetry breaking: Higgs field is an $SU(2)$ **doublet**
- Order-by-order: self-consistent, renormalisable QFT
 - Unlike an ‘**Anomalous Couplings**’ approach
 - It is a **theory**, applicable within a finite energy range $< \Lambda$
- Can be **matched** to UV theories of new physics
 - Each theory predicts specific Wilson coefficients
 - **Patterns/correlations** among them

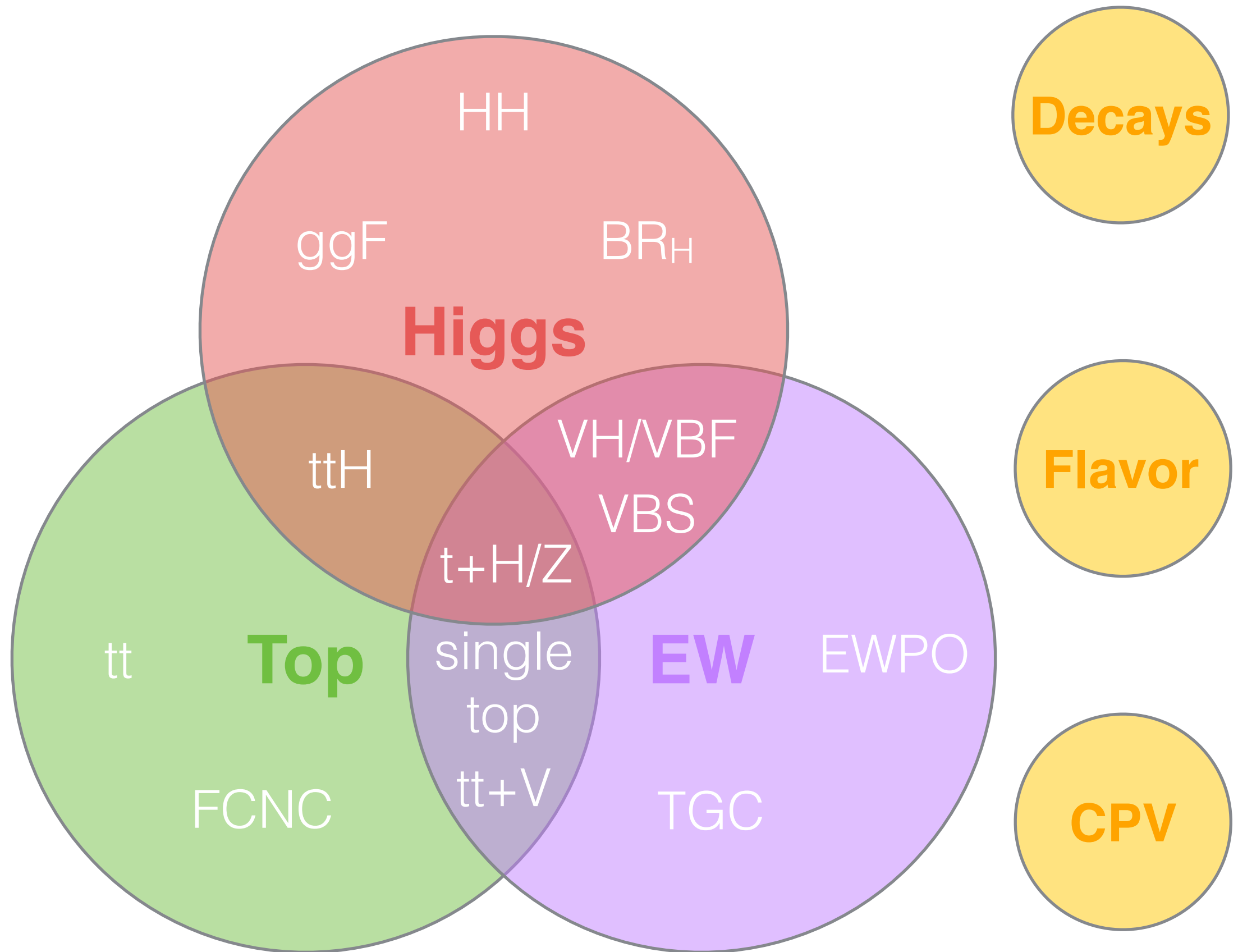
SMEFT at the LHC



Higgs/gauge interactions
Precision top physics
EW production processes
Blind directions from low energy experiments (LEP,...)

- We have a great theory, lets test it!
 - How? by measuring SM processes at **inclusive & differential** level
 - And then? like for the SM at LEP, perform a **global fit**
- The LHC is a great high-energy machine to do this
 - Countless SM measurements & even a few **dedicated** EFT interpretations
- What do we need?
 - Precise MC tools for signal generation
 - Well designed analyses/measurements with control over **energy scale**

SMEFT at the LHC: key players



General strategy

- Process that gets contributions from SMEFT operator(s)
- Step 1: sensitivity
 - Process → sensitive observable(s)
 - Determine functional dependence of observable on Wilson coefficients

MC implementations



$$\sigma(\mu_0) = \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i(\mu_0) \sigma_i(\mu_0) + \sum_{i,j} \frac{1\text{TeV}^4}{\Lambda^4} C_i(\mu_0) C_j(\mu_0) \sigma_{ij}(\mu_0)$$

- One at a time → all together
- Step 2: LHC study
 - Observable in fiducial detector volume
 - Unfolded detector effects but not to full phase space (model dependent)
 - Never sensitive to deviations outside the fiducial region

General strategy

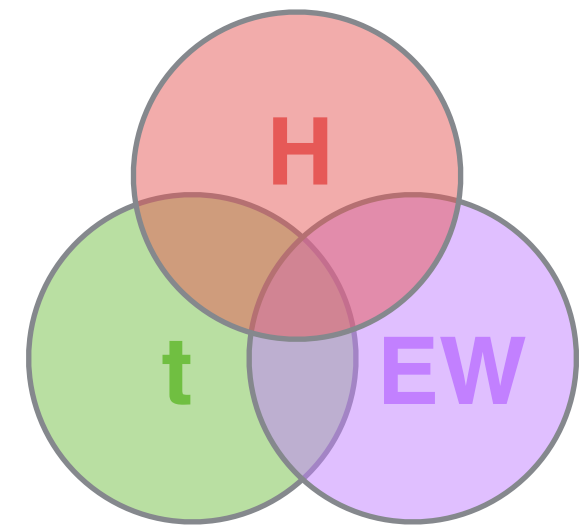
- Step 3: LHC **measurement**
 - If unfolded to particle level → reinterpretation without full/fast-sim
 - If MVA used: more complicated but not a showstopper
 - **Reproducible** event selection & background rejection
 - Easy to include in global fit
 - Dedicated EFT interpretation possible here
 - **Control energy scale**, binned observables or variable upper cuts
- Step 4: Input to **global fit**
 - Combine many such observables & perform statistical interpretation
 - Validity (energy scale vs cut-off) assessment **a posteriori**
 - Compare to **UV models**

Tools for SMEFT

- Ultimate goal: a **precision** global fit to all available data including LHC measurements
 - Need precise theoretical predictions for the full SMEFT
- Higher order (NLO) predictions
 - Control over scale and PDF **uncertainties**
 - Also scale uncertainty due to running of Wilson coefficients
 - Operators mix under renormalisation group running
 - **New operators** can enter at loop-level
- So far, existing global fits are performed
 - At leading order in perturbation theory
 - Separately for the Higgs/EW and top quark sectors

Need for a public, comprehensive implementation of SMEFT at NLO in QCD for the LHC

Top/Higgs/EW SMEFT

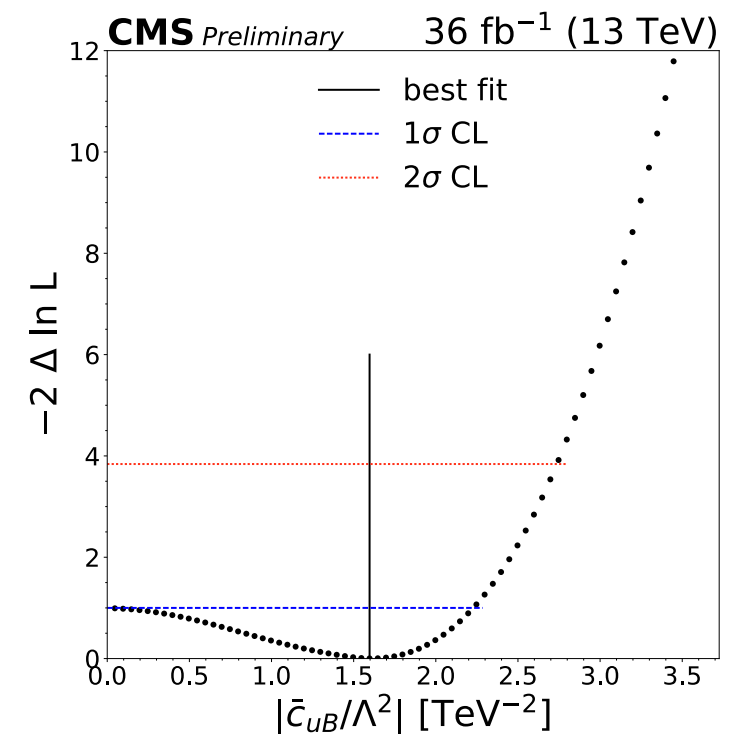
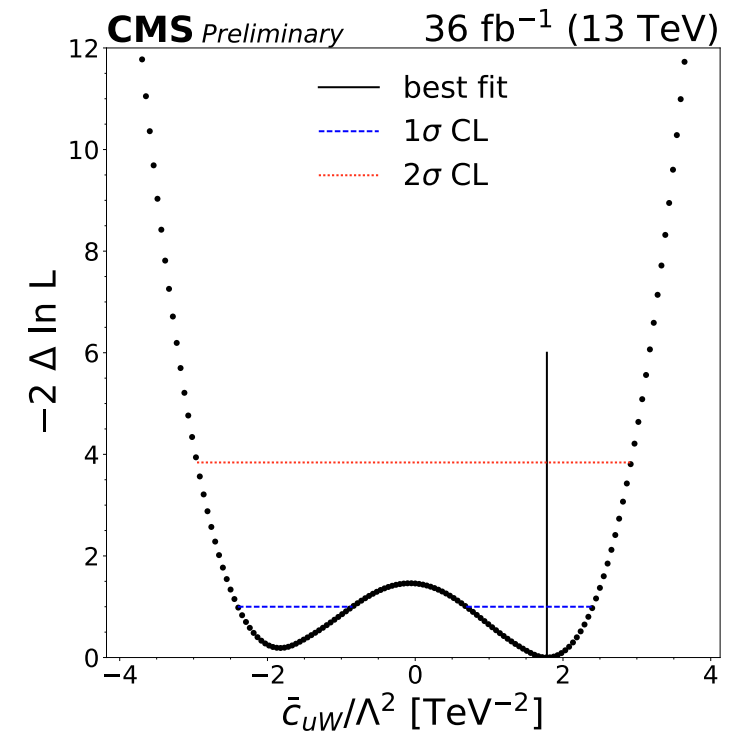
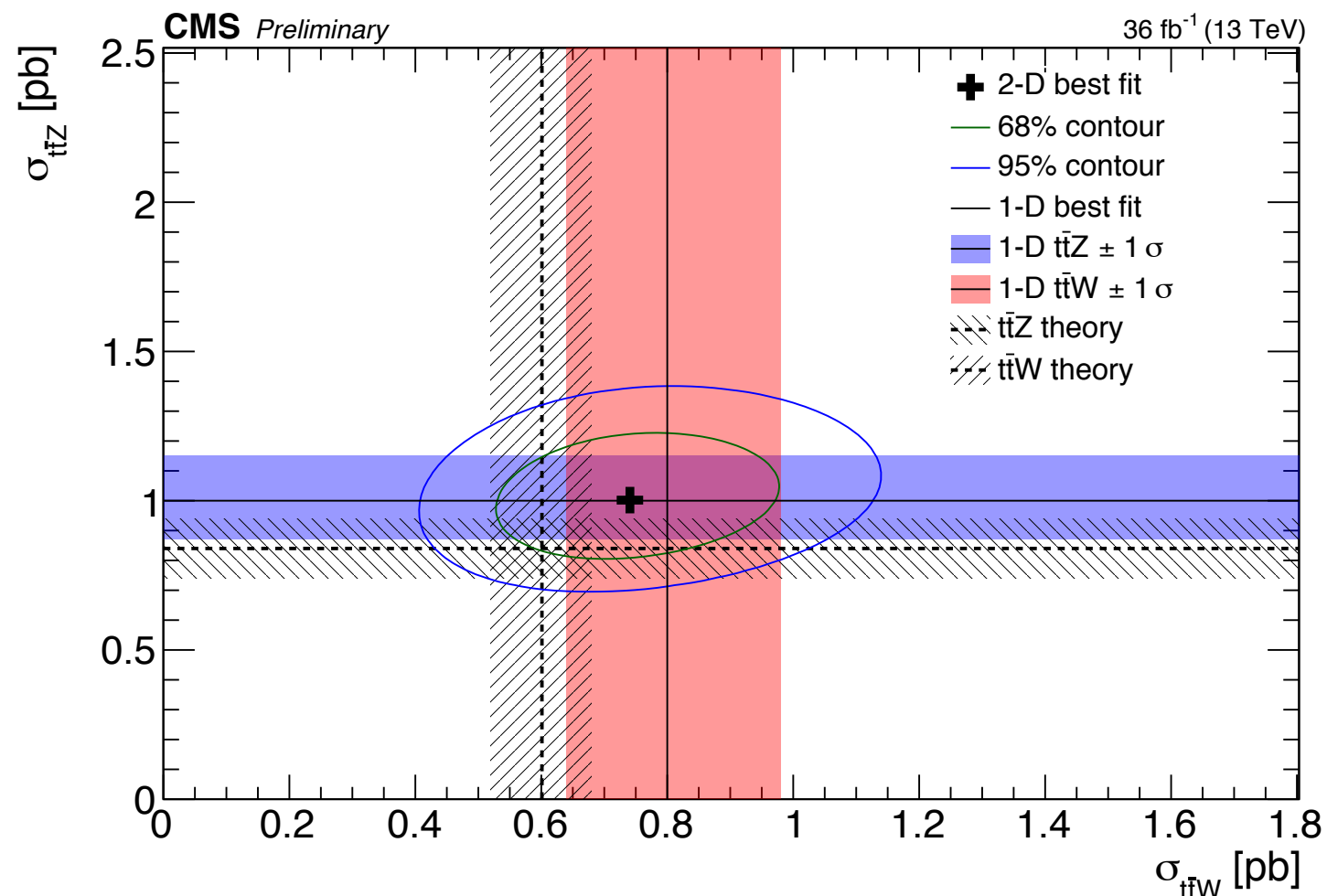


- Explore the origin of EW symmetry breaking
 - Precisely measure the interactions of the Higgs boson
 - Continue to probe EW gauge boson sector post-LEP
- **Top quark** is also a crucial ingredient in the story
 - Top-Higgs-W/Z couplings/masses are related in SM: **unitarity cancellations**
 - May reveal hints about the underlying nature of EWSB
 - **Coloured** particle, strongly coupled to the Higgs
 - QCD corrections relevant & interesting
- Many measurements at the LHC (total/differential/boosted)
 - Also **rare** processes *e.g.* $tt+Z/W/\gamma$, ttH (**NEW!**), tZj (**NEW!**)
 - Possibility to simultaneously probe all three sectors

Top/Higgs/EW EFT @ LHC

- CMS $t\bar{t}W$ & $t\bar{t}Z$ cross section measurement with EFT interpretation
- Backgrounds: $t\bar{t}H$, $t\bar{t}Zj$, $t\bar{t}Hj$, ...

Are also modified by EFT!



SMEFT@NLO

- Unified MC implementation for top/Higgs/EW sector
 - All processes at NLO QCD accuracy with, e.g. MadGraph5_aMC@NLO
 - Flavour symmetry assumptions to reduce 2499-dim. parameter space
 - Single out top interactions in a controlled way
- Based on a body of previous work concerning NLO SMEFT predictions for top processes and EW Higgs production

VH & VBF

[KM, Sanz & Williams.; JHEP 1608 (2016) 039]

[Degrande, Fuks, Mawatari, KM & Sanz; EPJC 77 (2017) 4, 262]

ttH, ttZ, ttγ

[Maltoni, Vryonidou & Zhang; JHEP 1610 (2016) 123]

[Bylund et al.; JHEP 1605 (2016) 052]

tt & Single top

[Zhang; PRL 116 (2016) 162002]

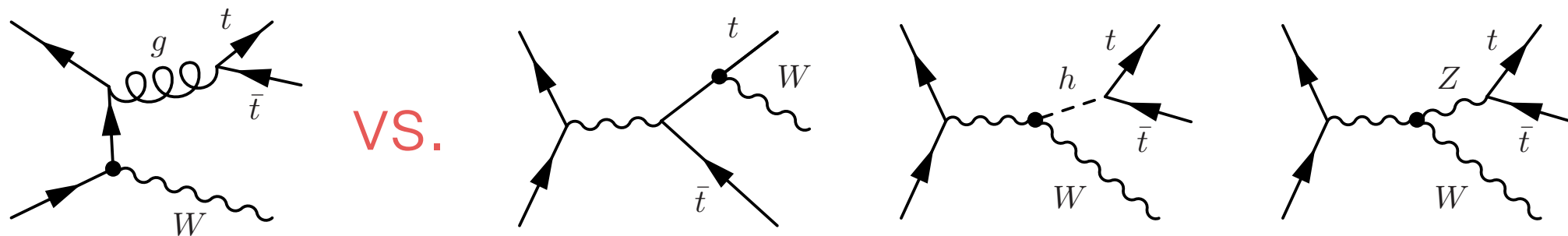
[Degrande et al.; PRD 91 (2015) 034024]

top FCNC

[Durieux, Maltoni & Zhang; PRD 91 (2015) 074017]

Case study: tZj/tHj

- Processes involving top+Higgs/W/Z
 - Interesting set of LHC-accessible processes to study EW sector + top
 - **Unitarity cancellations** \leftrightarrow top **mass generation** mechanism
- Previous $tt+X$ EFT studies considered QCD contributions
 - In the SM, pure EW contributions 2 orders of magnitude smaller
 - EFT effects can strongly enhance these due to **unitarity-violating** behaviour



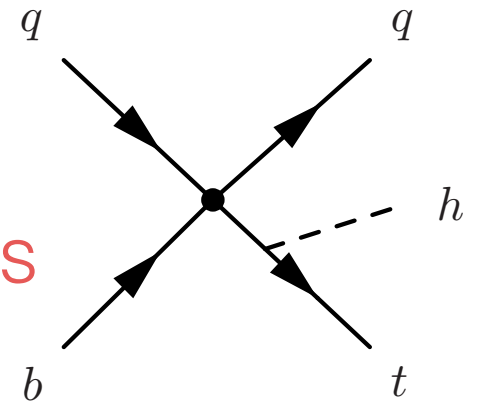
- SMEFT interpretation different from anomalous couplings
 - Quantitative power counting/expansion for **high energy** behaviour

Case study: tZj/tHj

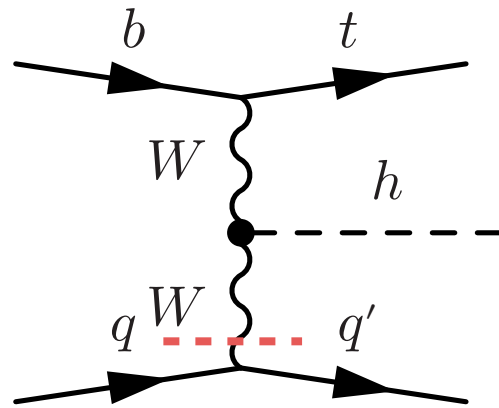
- Alternative to $tt+X$: require a **single top** quark
 - Eliminates dominant QCD contribution
- Single top rate at 13 TeV LHC ~ 200 pb (1/4 of QCD tt)
 - Sensitive to **2 four-fermion** and **3 top/EW** operators that modify tbW vertex
- Require the presence of an additional **Z** or **Higgs**
 - Possibility of probing large set of top/Higgs/EW operators at once
 - Processes at the heart of EWSB sector
 - **Higher thresholds** may enhance EFT effects
- Recent LHC measurement of tZj cross section at 4.2σ
[ATLAS; arXiv:1710.03659], [CMS-PAS-TOP-16-020 & arXiv:1712.02825]
- Timely moment to perform EFT sensitivity study in this pair of challenging processes & showcase model implementation

Anatomy of tHj/tZj

Single-top
4f operators



tHj (tZj = h → Z)

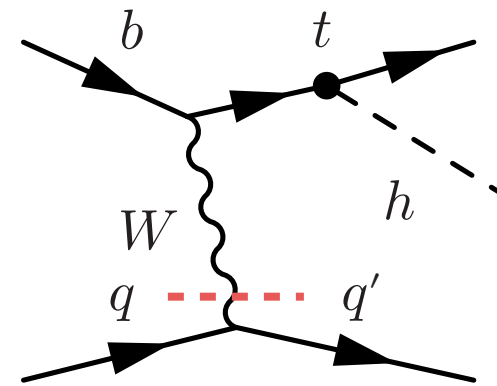


$$\mathcal{O}_{\varphi W} : \varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$$

HWW

TGC

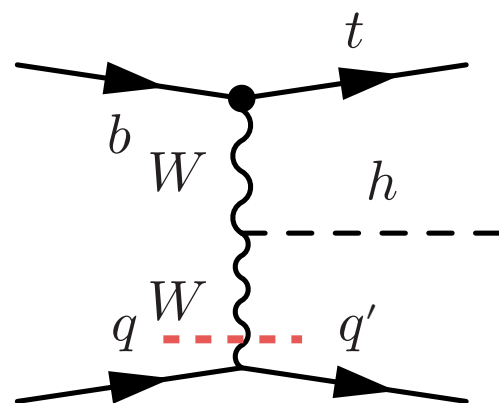
$$\mathcal{O}_W : \epsilon^{ijk} W_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^\mu$$



$$\mathcal{O}_{t\varphi}$$

top Yukawa
ttZ coupling

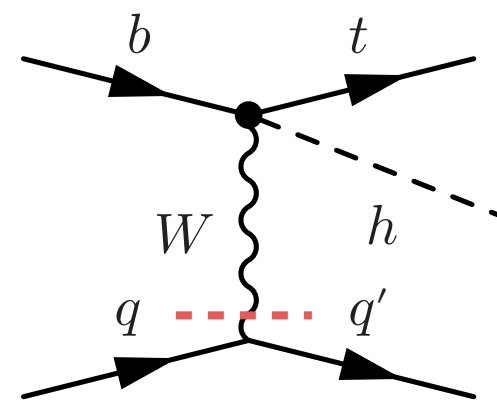
$$\mathcal{O}_{\varphi t}$$



$$\mathcal{O}_{\varphi Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi)(\bar{Q}\gamma^\mu \sigma_i Q)$$

Wtb vertex

$$\mathcal{O}_{\varphi tb} : i(\tilde{\varphi} D_\mu \varphi)(\bar{b}\gamma^\mu t)$$



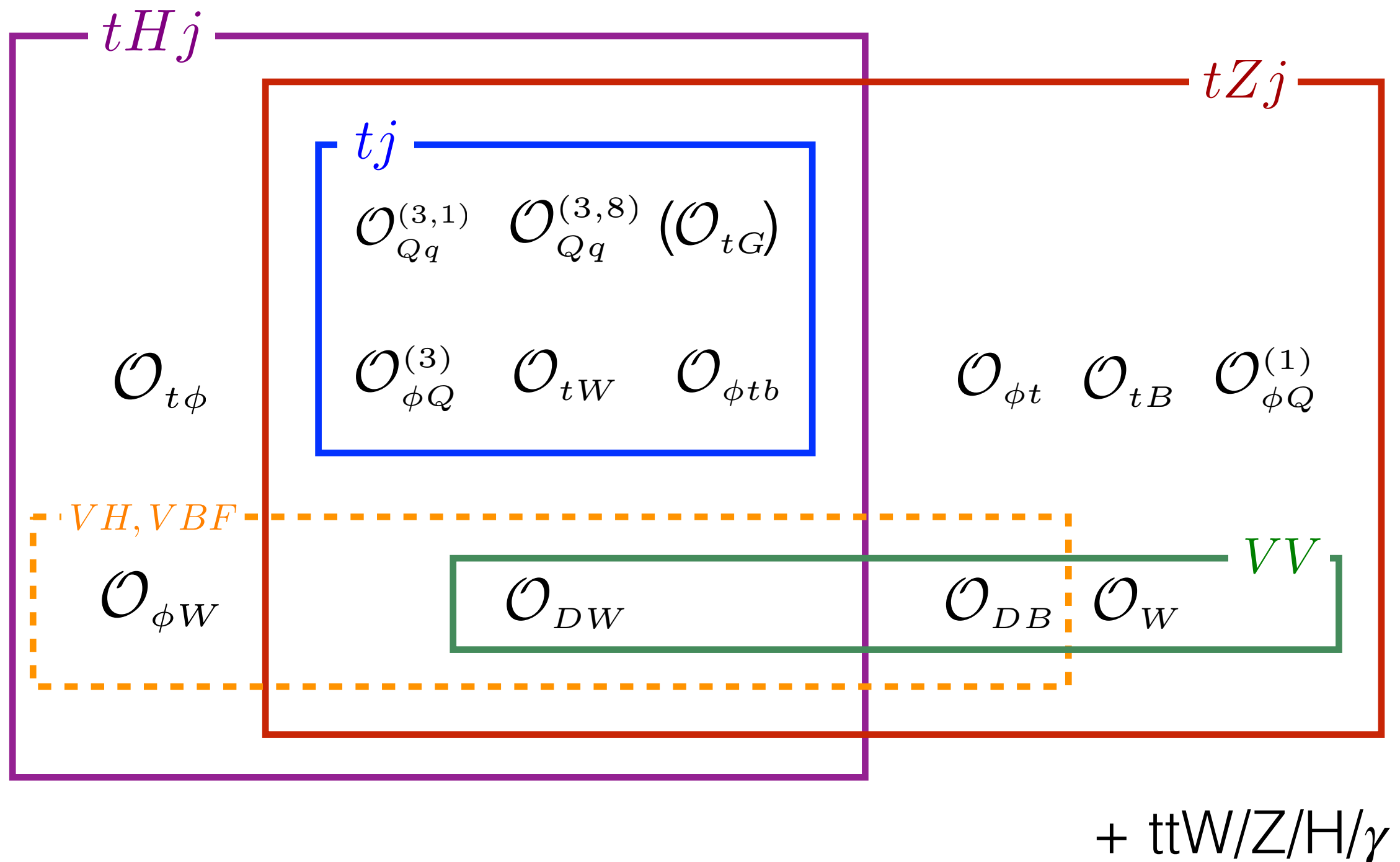
$$\mathcal{O}_{\varphi Q}^{(3)}$$

Contact terms

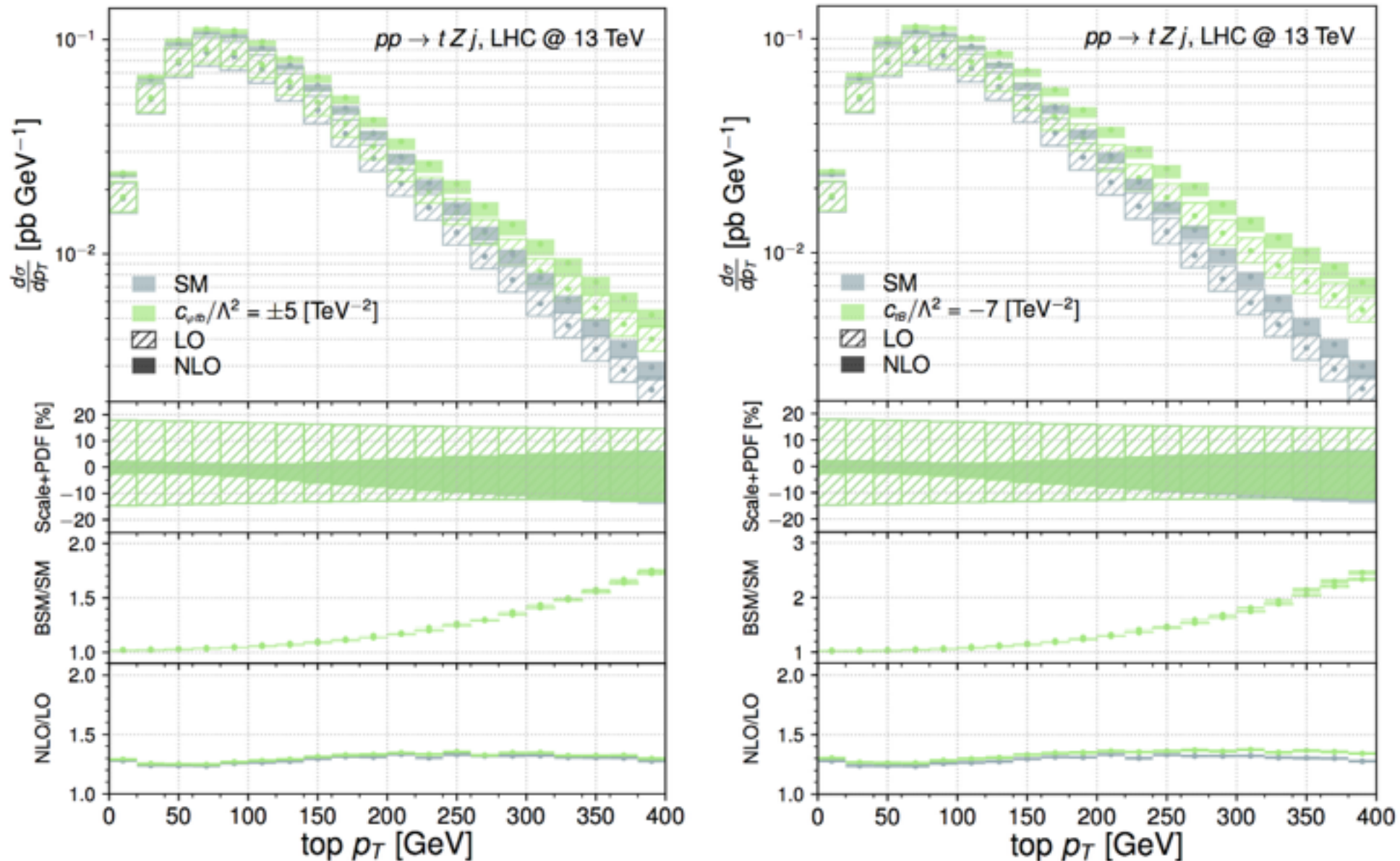
$$\mathcal{O}_{tB}$$

- Accessing the $bW \rightarrow tH$ & $bW \rightarrow tZ$ sub-amplitudes
 - Rich interplay between EFT operators from different sectors
 - Different energy growth and interference patterns with the SM

Interplay



LHC sensitivity



Potentially large deviations in the tails (saturating current limits)
 tHj process is very rare, differential results not likely at LHC

LHC sensitivity

Usual EFT story: looking at **high energy tails** increases sensitivity
 Important to put into context **w.r.t single top** which has a much larger rate

$r = \sigma_i / \sigma_{SM}$	tj	tj	tZj	tZj	tHj
		$(p_T^t > 350 \text{ GeV})$		$(p_T^t > 250 \text{ GeV})$	
σ_{SM}	224 pb	880 fb	839 fb	69 fb	75.9 fb
r_{tW}	0.0275	0.024	0.016	0.010	0.292
$r_{tW,tW}$	0.0162	0.35	0.095	0.67	0.940
$r_{\varphi Q^{(3)}}$	0.121	0.121	0.192	0.172	-0.132
$r_{\varphi Q^{(3)},\varphi Q^{(3)}}$	0.0037	0.0037	0.029	0.114	0.21
$r_{\varphi tb,\varphi tb}$	0.00090	0.0008	0.0050	0.027	0.050
r_{tG}	0.0003	-0.01	0.00053	-0.0048	-0.0055
$r_{tG,tG}$	0.00062	0.045	0.0027	0.022	0.025
$r_{Qq^{(3,1)}}$	-0.353	-4.4	-0.59	-2.22	-0.39
$r_{Qq^{(3,1)},Qq^{(3,1)}}$	0.126	11.5	0.65	5.1	1.21
$r_{Qq^{(3,8)},Qq^{(3,8)}}$	0.0308	2.73	0.133	1.01	1.08

Increased sensitivity for **certain operators**

Consistent with $2 \rightarrow 2$ subamplitude analysis

New energy growths w.r.t single top

Single top should eventually outperform tHj/tZj for **four fermion operators**

High p_T tZj : end of run II/HL-LHC
 tHj : HL-LHC ?

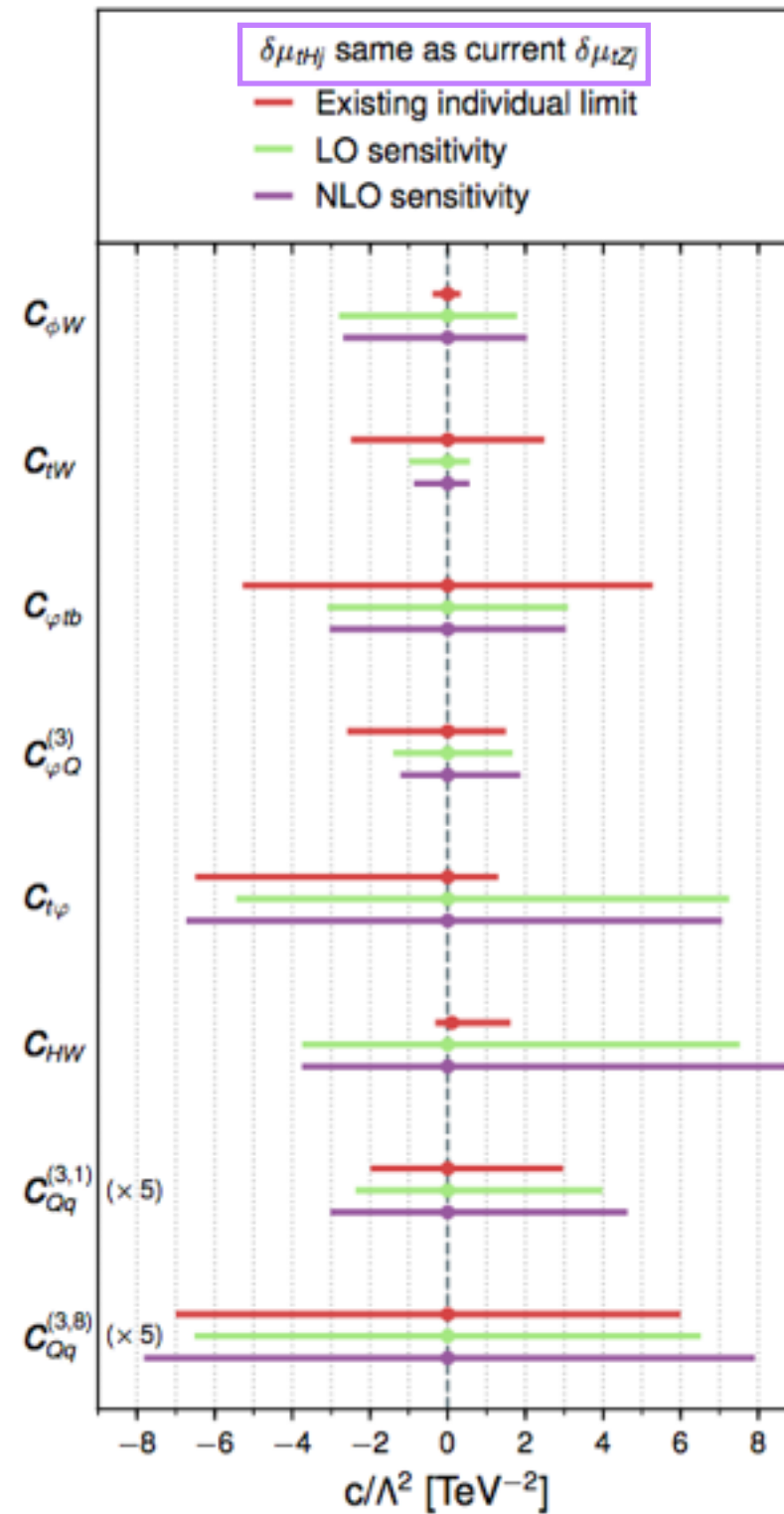
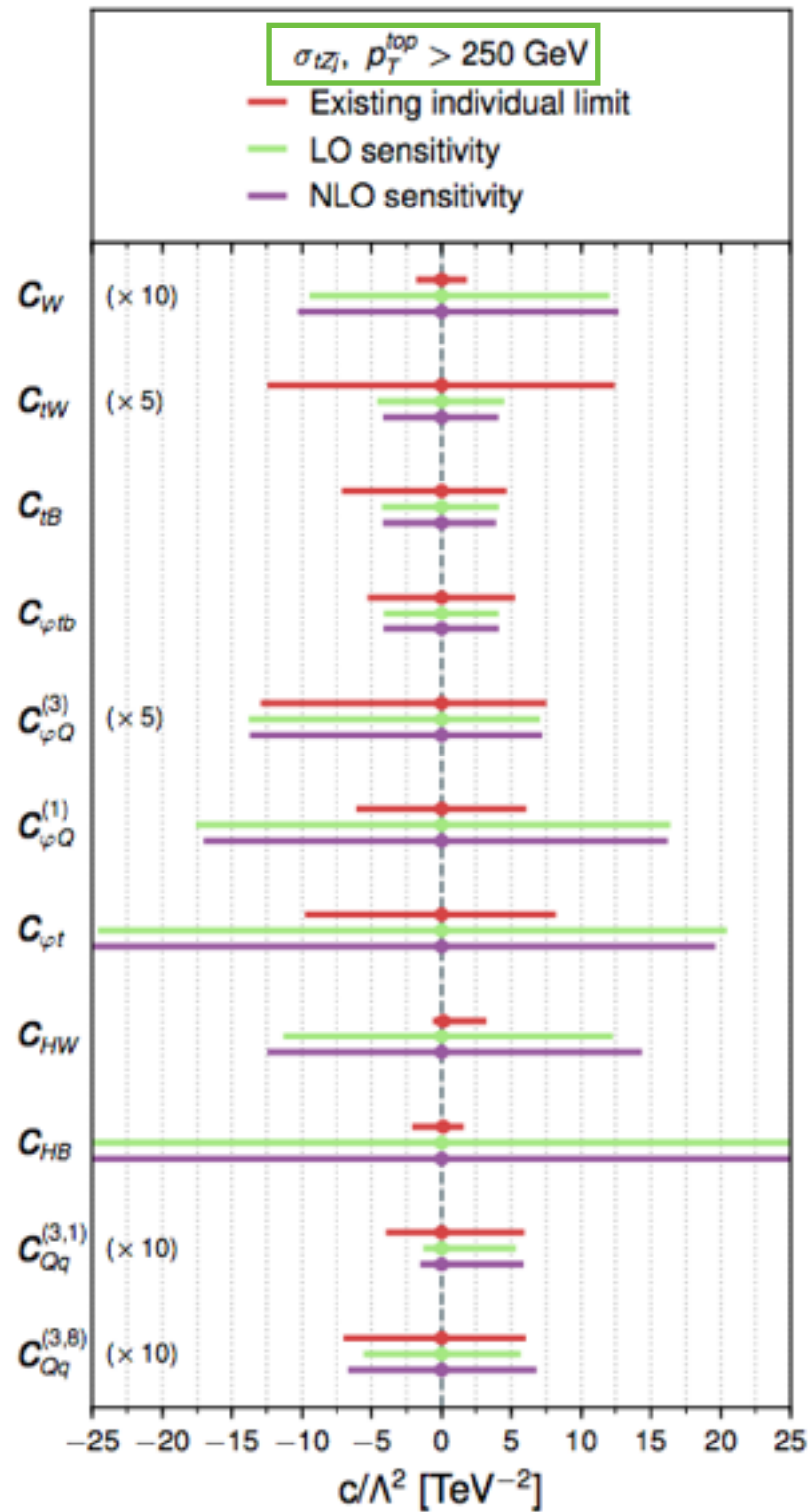
Future sensitivity

tZj

tHj

TGC
 Dipoles
 RHCC
 Currents
 LEP
 orthogonal
 4-fermion

Gauge-Higgs
 Dipole
 RHCC
 Currents
 LEP
 orthogonal
 4-fermion



Top 4F operators @ LHC

- Generated by heavy, new physics coupling to **3rd generation**
 - Top mass generation
 - Z'/Composite dynamics?
- Contain tttt, ttbb and bbbb interactions
 - Colour singlet & triplet
 - Vector & scalar currents
- One way to constrain them is by measuring **four top production**
 - Only a **subset** of operators

$$O_{QQ}^1 = (\bar{Q} \gamma_\mu Q) (\bar{Q} \gamma^\mu Q),$$

- $O_{QQ}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{Q} \gamma^\mu T^A Q),$
- $O_{tt}^1 = (\bar{t} \gamma_\mu t) (\bar{t} \gamma^\mu t),$
 $O_{tb}^1 = (\bar{t} \gamma_\mu t) (\bar{b} \gamma_\mu b),$
 $O_{tb}^8 = (\bar{t} \gamma_\mu T^A t) (\bar{b} \gamma_\mu T^A b),$
- $O_{Qt}^1 = (\bar{Q} \gamma_\mu Q) (\bar{t} \gamma^\mu t),$
- $O_{Qt}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{t} \gamma^\mu T^A t),$
 $O_{Qb}^1 = (\bar{Q} \gamma_\mu Q) (\bar{b} \gamma^\mu b),$
 $O_{Qb}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{b} \gamma^\mu T^A b),$
 $O_{QtQb}^1 = (\bar{Q} t) \varepsilon (\bar{Q} b),$
 $O_{QtQb}^8 = (\bar{Q} T^A t) \varepsilon (\bar{Q} T^A b)$

Four top production

- Very **rare** process at the LHC ~ 9 fb
 - Best effort at the LHC about 4.6 times the SM *[ATLAS-EXOT-2016-13]*
 - Not a precision measurement *[CMS; EPJC 78 (2018) 2, 140]*
- Not a precision measurement *[Zhang; Chin. Phys. C42 (2018) 023104]*
 - Sensitive to four heavy quark & 2 heavy + 2 light quark operators
 - High threshold ~ 700 GeV

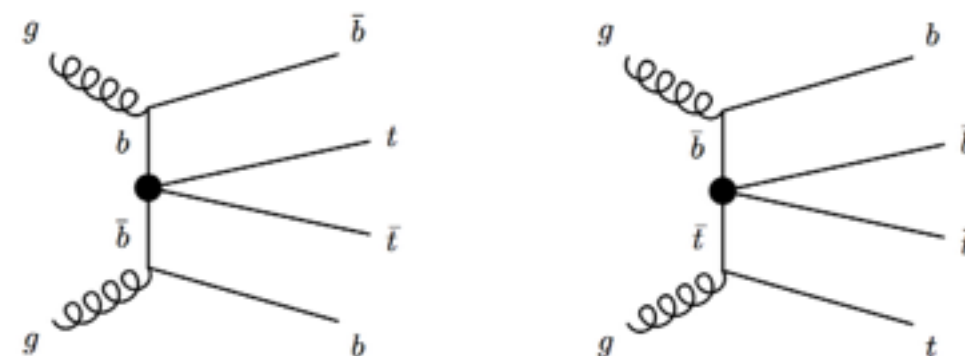
$$\begin{array}{l}
 [\text{TeV}^{-2}] \quad c_{Qt}^1 \quad [-4.97, 4.90] \quad (E_{cut} = 3 \text{ TeV}) \\
 \quad \quad \quad c_{Qt}^8 \quad [-10.3, 9.33] \quad (E_{cut} = 3 \text{ TeV}) \\
 \quad \quad \quad c_{tt}^1 \quad [-2.92, 2.80] \quad (E_{cut} = 3 \text{ TeV})
 \end{array}$$

3 out of 14 relevant
degrees of freedom

↑
Best limit: dedicated
ATLAS EFT interpretation!

[Aguilar-Saavedra et al.; arXiv:1802.07237]

ttbb production



- Less rare process at the LHC ~ 3 pb
 - Measured at the LHC with $\sim 30\%$ accuracy [CMS; PLB 776 (2018) 355-378]
 - Major background for ttH(bb) search
 - Turn it around into a new physics signature!
- Affected by all but one of the 14 operators [Degrande et al.; JHEP 03 (2011) 125]
 - Some of which have never been bounded before
- Sensitivity study of ttbb to four heavy operators
 - New limits on 3rd generations four-quark operators
 - Future projections of dedicated analyses optimised to EFT kinematics
 - Experimented with multivariate classification techniques
 - Sensitivity may exceed that of 4 top for operators common to both

General strategy

ttbb

✓ Process that gets contributions from SMEFT operator(s)

✓ Step 1: sensitivity

M_{4b} & NN discriminant

✓ Process → sensitive observable(s)

✓ Determine functional dependence of observable on Wilson coefficients

$$\sigma(\mu_0) = \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i(\mu_0) \sigma_i(\mu_0) + \sum_{i,j} \frac{1\text{TeV}^4}{\Lambda^4} C_i(\mu_0) C_j(\mu_0) \sigma_{ij}(\mu_0)$$

✓ One at a time → all together

✓ Step 2: LHC study

MG5_aMC@NLO + Pythia8 + Delphes

✓ Observable in fiducial detector volume

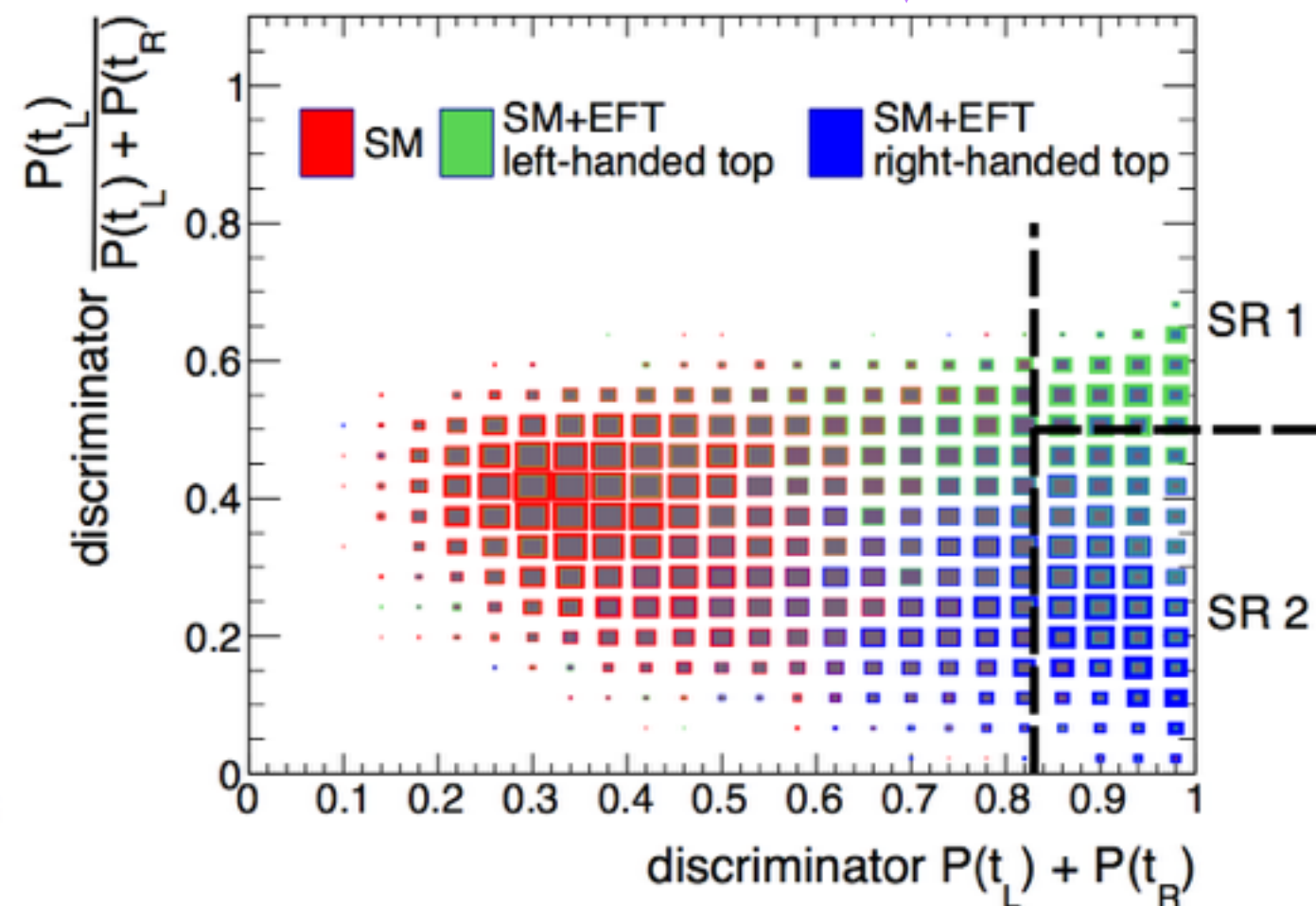
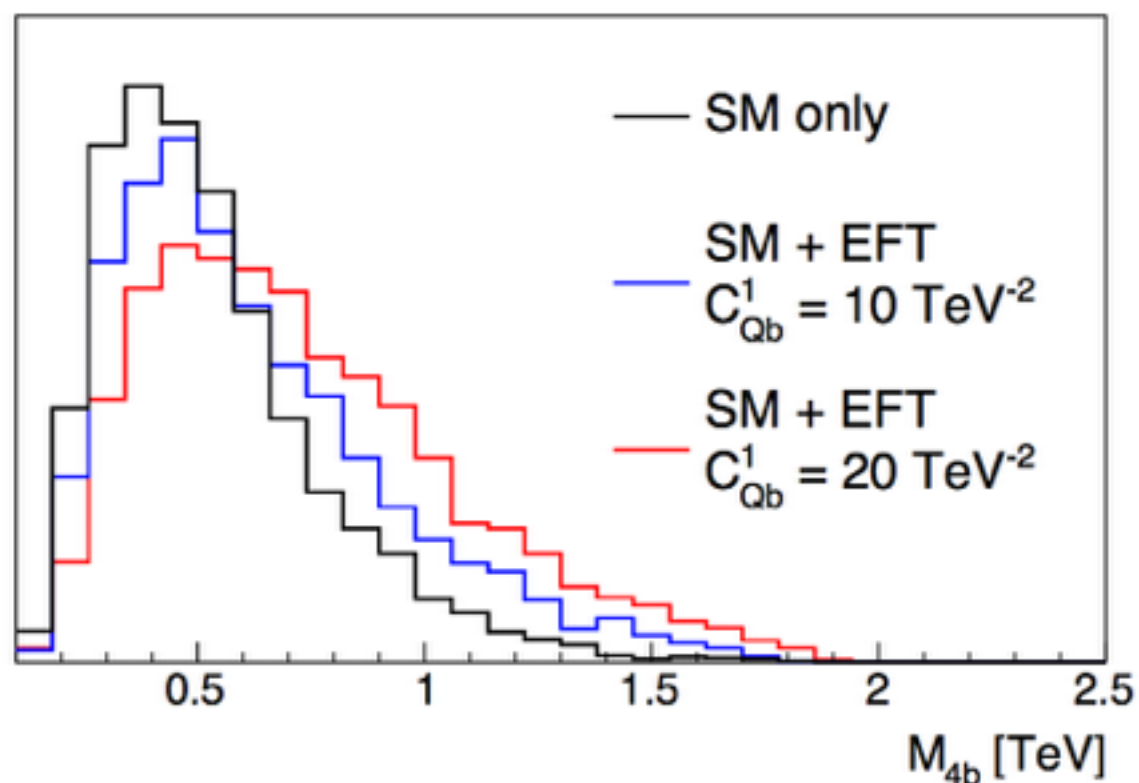
✓ Unfolded detector effects but not to full phase space (model dependent)

✓ Never sensitive to deviations outside the fiducial region

Observables

- “High energy” kinematic variable M_{4b}
 - Bulk of sensitivity to 4F operators
 - Sensitivity comes from events below 1.5 TeV $\rightarrow M_{\text{cut}} = 2$ TeV
- Multi(3) class NN discriminant
 - SM vs t_L operators vs t_R operators

Cut on discriminant
vs.
template fit



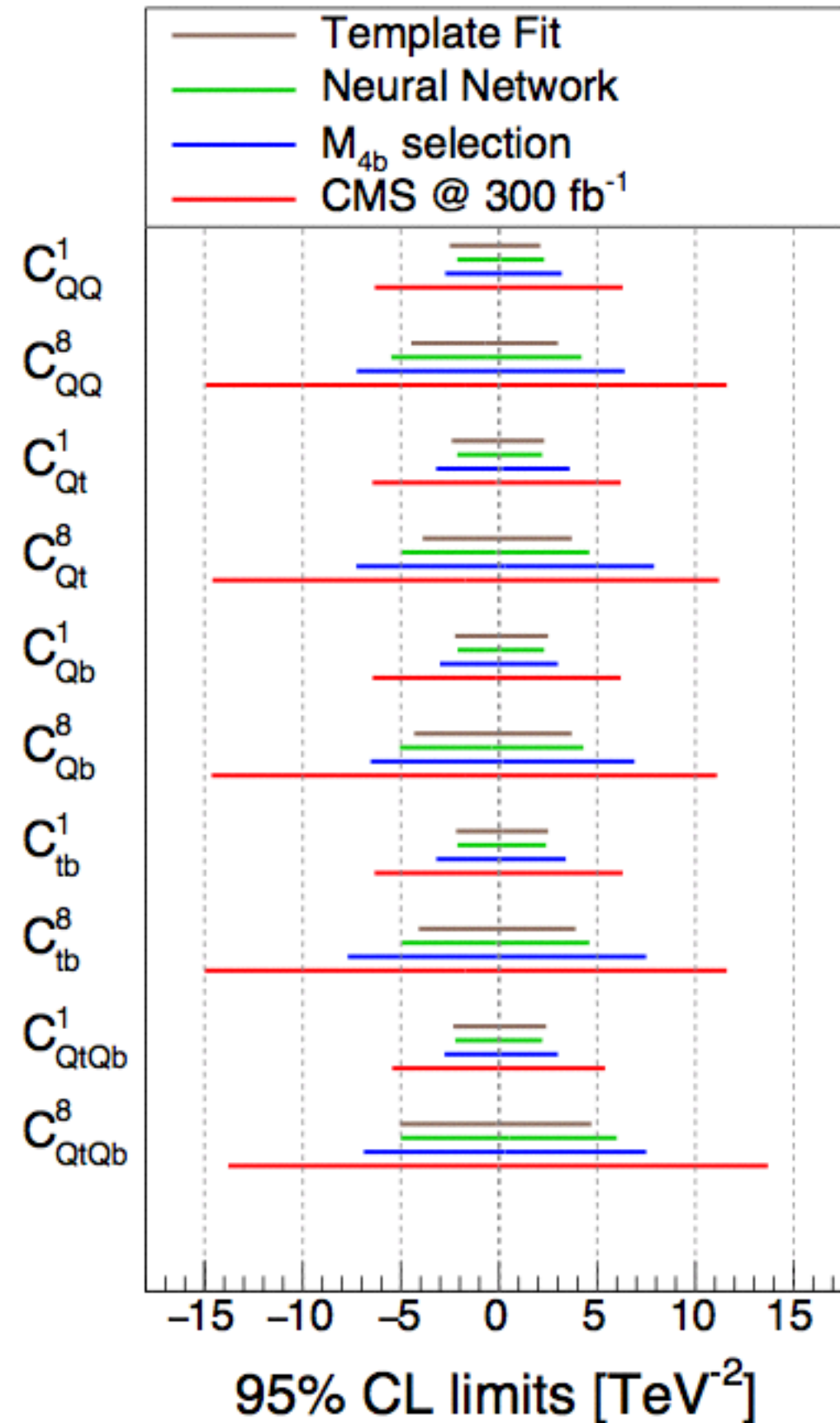
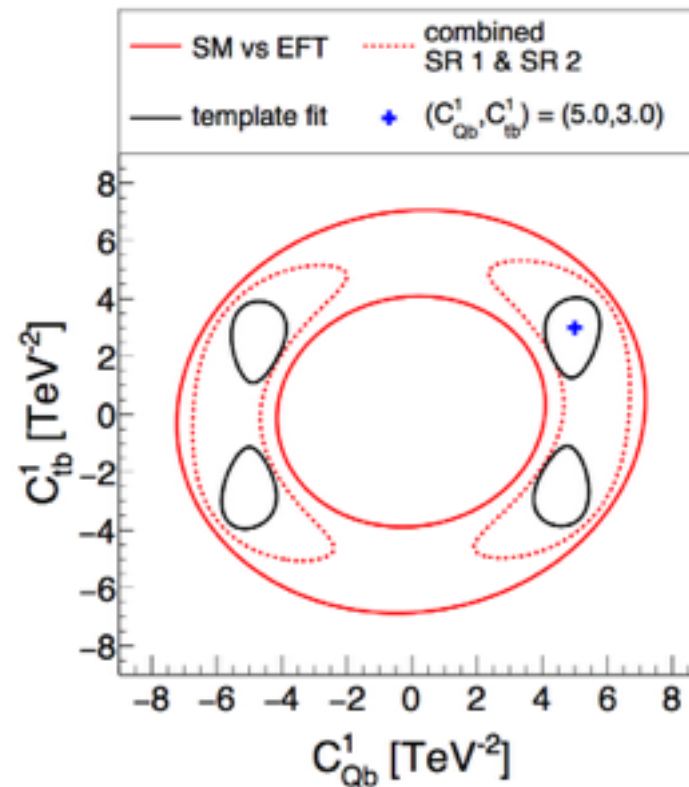
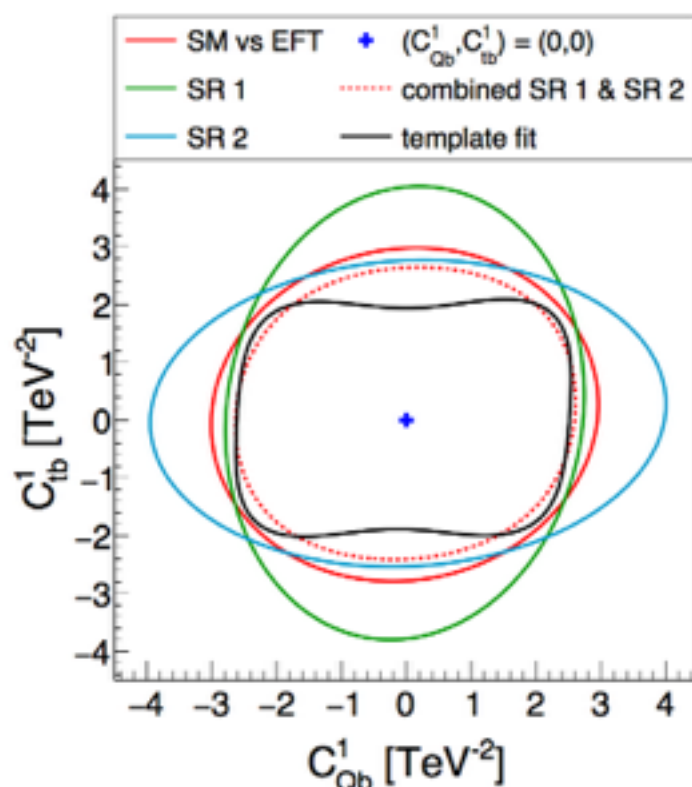
LHC sensitivity

1) Assuming SM observation

- Improve on inclusive measurement
- Template fit to NN similar to M_{4b}

2) EFT signal injection

- NN focuses in on preferred parameters



Conclusion

- The LHC has entered an **EFT era**
- **SMEFT**: consistent framework to go beyond the SM
 - Theory consensus for global description & MC implementation
 - Extended to top/Higgs/EW sector & NLO in QCD
- **Global** view of top/Higgs/EW measurements
 - Blurring the line between **signal** & **background**
 - Different approach needed?
 - Ensure measurements can be interpreted by a global SMEFT fit
- Many **unexplored** processes
 - New sensitivity studies ripe for the picking!
 - Single MC tool for all top/Higgs/EW processes at the LHC

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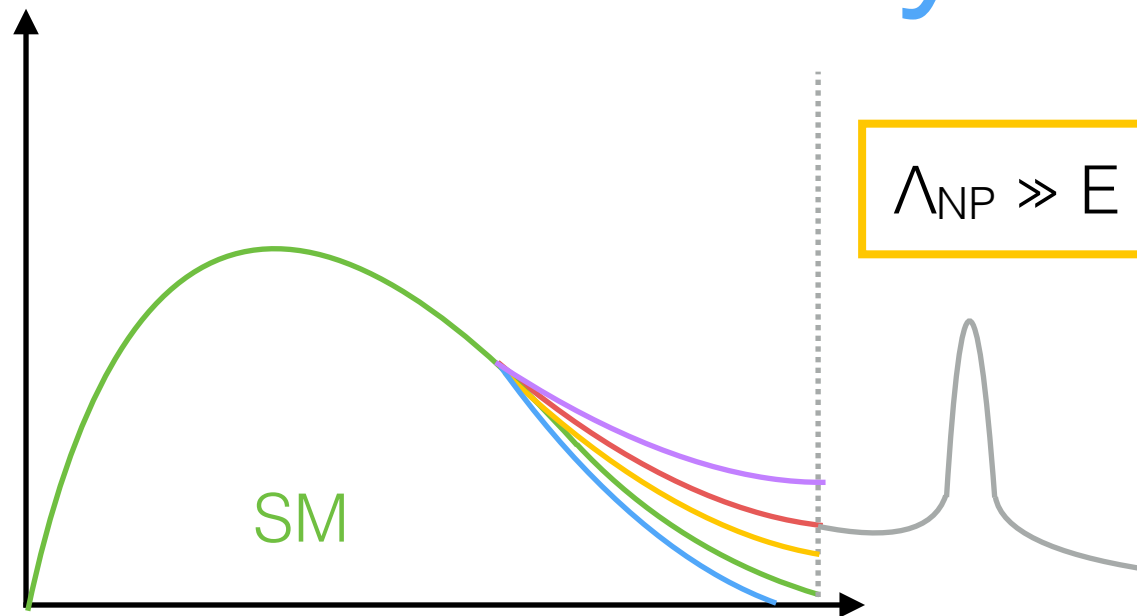
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Thank you

Interpretation

- Global likelihood in SMEFT parameter space
- **Individual** & **marginalised** confidence intervals
 - Individual limits are useful to quantify degree of sensitivity to given coeff.
 - Marginalised intervals reveal degeneracies/blind directions
- Impact of including or not squared EFT terms
- Constraints as a function of cuts
 - Allow a wider range of model interpretations (different NP mass scales)
 - Perturbativity in Wilson coefficients
- Matching to UV models
 - Correlated Wilson coefficients → better limits
 - Validity & perturbativity in NP couplings

EFT validity



Q: How well does my EFT approximate full theory?
 A: Depends on the theory!
 Q: But I thought EFT was model independent....

- Two “expansions” occur
- Lagrangian level, (E/Λ_{NP}) , truncated at operator dimension
 - Golden rule: cannot probe energies beyond Λ_{NP}

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

- Observable level, $(c_i E/\Lambda_{NP})$ truncated at... ?

$$\sigma = \sigma_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \sigma_i^{(6)} + \sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\Lambda^4} \sigma_{ij}^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \sigma_i^{(8)} + \dots$$

EFT expansion

- Practically:
$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

- Observable:
$$\sigma = \sigma_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \sigma_i^{(6)} + \sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\Lambda^4} \sigma_{ij}^{(6)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \sigma_i^{(8)} + \dots$$

- To square or not to square...
 - Formally, **D=6 squared** part is of the same order as **D=8 interference**
 - D=8 part, in general, is unknown and/or not feasible
- Is the EFT invalid if **(D=6 squared) > (D=6 interference)**?
 - Depends on $c^{(6)}_i$, $c^{(6)}_{ij}$, $c^{(8)}_i$ and $\sigma^{(6)}_i$, $\sigma^{(6)}_{ij}$, $\sigma^{(8)}_i \rightarrow$ **model dependence**
 - At most, the σ scale with energy as: $\sigma^{(6)}_i \sim E^2$, $\sigma^{(6)}_{ij} \sim E^4$, $\sigma^{(8)}_i \sim E^4$

Large coefficients

- If c is **large** e.g. Wilson coefficient is poorly constrained
- $(D=6)^2$ terms **could** be important without invalidating EFT

$$\frac{E^2}{\Lambda^2} < 1 < c_i^{(6)} \frac{E^2}{\Lambda^2} < c_i^{(6)} c_j^{(6)} \frac{E^4}{\Lambda^4}$$

- Truncating L at $D=6$, σ is not really a series expansion

$$\sigma = \sigma_{SM} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \sigma_i^{(6)} + \sum_{i < j} \frac{c_i^{(6)} c_j^{(6)}}{\Lambda^4} \sigma_{ij}^{(6)} + \text{nothing}$$

- Dropping the squared terms $\rightarrow \sigma$ **not positive-definite**
- If $(D=6)^2$ are relevant, UV interpretations lean towards strongly coupled models (large c 's)
 - Most model independent approach: assume nothing about the size of c 's

Non-interference

- Alternatively, one may have $\sigma^{(6)}_i < \sigma^{(6)}_{ij}$
 - **Non-interference** by e.g. helicity selection rules in the high energy limit

[Cheung & Shen; PRL 115 (2015) 071601]

[Azatov, Contino & Riva; PRD 95 (2017) 065014]

- High energy theorem

- Many $2 \rightarrow 2$ amplitudes involving **at least one transverse gauge boson** mediated by D=6 operators do not interfere with the SM

Total Helicity

Interference?

A_4	$ h(A_4^{\text{SM}}) $	$ h(A_4^{\text{BSM}}) $
VVVV	0	4,2
VV $\phi\phi$	0	2
VV $\psi\psi$	0	2
V $\psi\psi\phi$	0	2
$\psi\psi\psi\psi$	2,0	2,0
$\psi\psi\phi\phi$	0	0
$\phi\phi\phi\phi$	0	0

X

✓

V = Transverse vector

ϕ = Longitudinal vector or Higgs

ψ = Fermion

$p p \rightarrow ZH, WH, WW, WZ$

Interference can be recovered considering **finite mass effects** or **higher order corrections (2 \rightarrow 3,4)**

[Panico, Riva & Wulzer; CERN-TH-2017-85]

[Azatov, et al. LHEP 1710 (2017) 027]

EFT “expansion”

- To square or not to square...

- Model & process dependent

- Better calculate both and check the effect of including or not the square

SM x EFT



- Relation to the validity question

- Depends on the sensitivity of each measurement/process

- We can only constrain (c/Λ) & Λ an arbitrary scale w.r.t to unknown Λ_{NP}

- Validity assessment is an *a posteriori* check at interpretation stage on a process-by-process basis

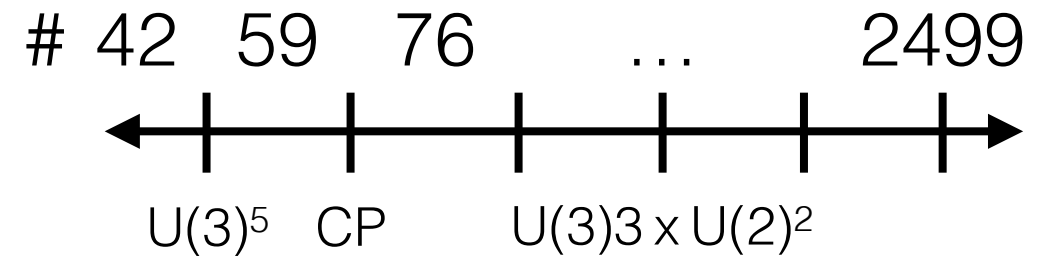
- Publish limits as a function of experimental energy

[Contino et al.; JHEP 1607 (2016) 144]

- Realistically can't include $D=8$ without sufficient motivation

- If $c^{(6)}_i=0$ e.g. for neutral triple gauge boson couplings

Flavor symmetry



- SM fermion sector q^i, u^i, d^i, l^i, e^i
 - 5 SU(3) x SU(2) x U(1) representations → U(3)⁵ flavor symmetry
 - Only **broken** by Yukawa interactions
- Some SMEFT operators also break it
 - Chirality flipping F_Lf_R structures (Yukawa-like)
 - Flavor violating (off diagonal/non-universal) entries
- Starting point: **flavor symmetric**
 - No chirality flipping & diagonal, universal structure
- Controlled departures
 - Minimal for top physics: U(3)³ x U(2)², single out q³, u³
 - Similarly MFV: expansion in Yukawa couplings

Going NLO

- Ultimate goal: a **precision global fit** of SMEFT to LHC observables at HL-LHC
- Step 1: **NLO QCD(+PS)** predictions
 - K-factors/shapes & control over PDF + scale uncertainties
- **NLO EW** corrections
 - Potentially important but much harder
 - Automation on the way with SHERPA, Madgraph5_aMC@NLO
- **RG-improved** predictions & **operator mixing**
 - Very helpful for cross checking NLO implementations
 - Compare to full NLO calculations, assess the importance of finite terms
[Alonso, Jenkins, Manohar & Trott; JHEP 1310 (2013) 087, JHEP 1401 (2014) 035 & JHEP 1404 (2014) 159*]*

ttH in SMEFT

$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu) \quad \gamma = \begin{pmatrix} -2 & 16 & 8 \\ 0 & -7/2 & 1/2 \\ 0 & 0 & 1/3 \end{pmatrix}$$

$$O_{t\phi} = (\varphi^\dagger \varphi) (\bar{Q}_L \tilde{\varphi} t_R)$$

$$O_{\phi G} = (\varphi^\dagger \varphi) G_{\mu\nu}^A G_A^{\mu\nu}$$

$$O_{tG} = (\bar{Q}_L \sigma_{\mu\nu} T^A t_R) \tilde{\varphi} G_A^{\mu\nu}$$

- Operators involving the **top/Higgs/gluon**
 - $gg \rightarrow H$ & tt production partly constrain the Wilson coefficient space
 - ttH is the only direct probe of the Top-Higgs interaction
 - In principle 3-gluon O_G and 4 fermion operators also contribute but turn out to be better constrained by tt and multi-jet measurements
- **Different K-factors** among SM/dim-6 operators
- **Large Λ^{-4} effects** in both shape & normalisation
 - Scenarios where “EFT-squared” terms are large but energy is below cutoff

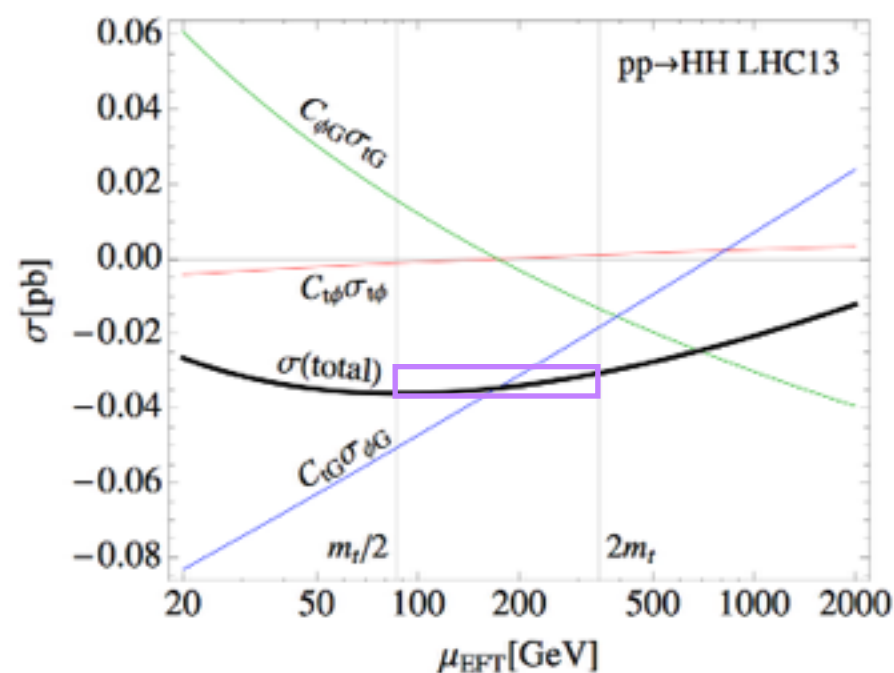
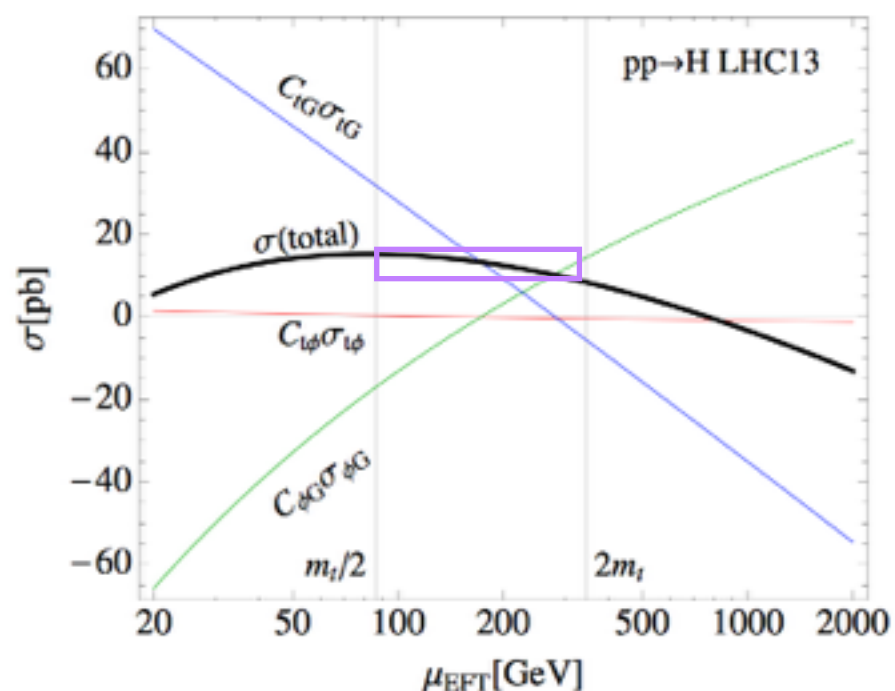
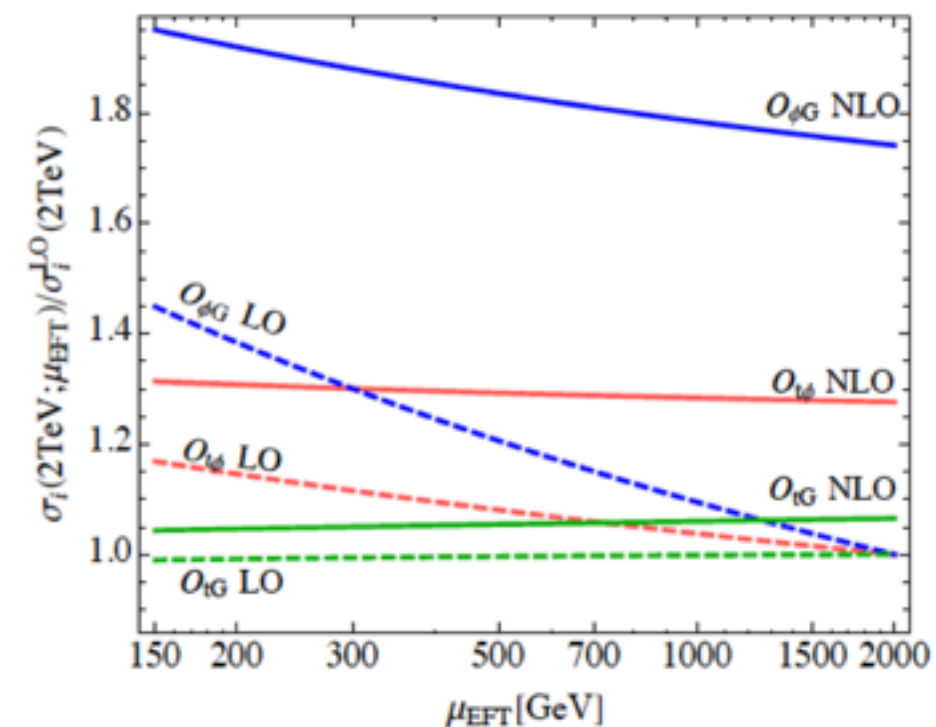
$$\frac{E^2}{\Lambda^2} < 1 < c_i^{(6)} \frac{E^2}{\Lambda^2} < c_i^{(6)} c_j^{(6)} \frac{E^4}{\Lambda^4}$$

ttH in SMEFT

Update from ttH
signal strengths

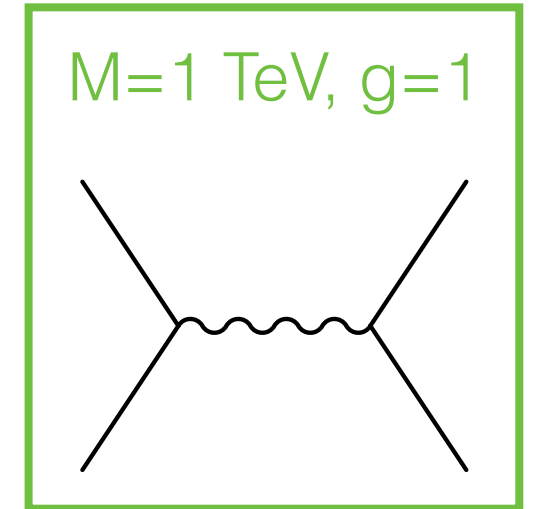
$$C_{t\varphi} \subset [-6.5, 1.3] \text{ TeV}^{-2}$$

- Full NLO stable under scale variation
- Large **finite** terms: RG improved underestimates NLO
- EFT scale uncertainty estimate
 - Take c_i defined at scales $2\mu_0$ & $\mu_0/2$ and run back to the central scale



$\delta\mu_{\text{EFT}}$:
Does not cancel in
e.g. cross section
ratios

TopFitter

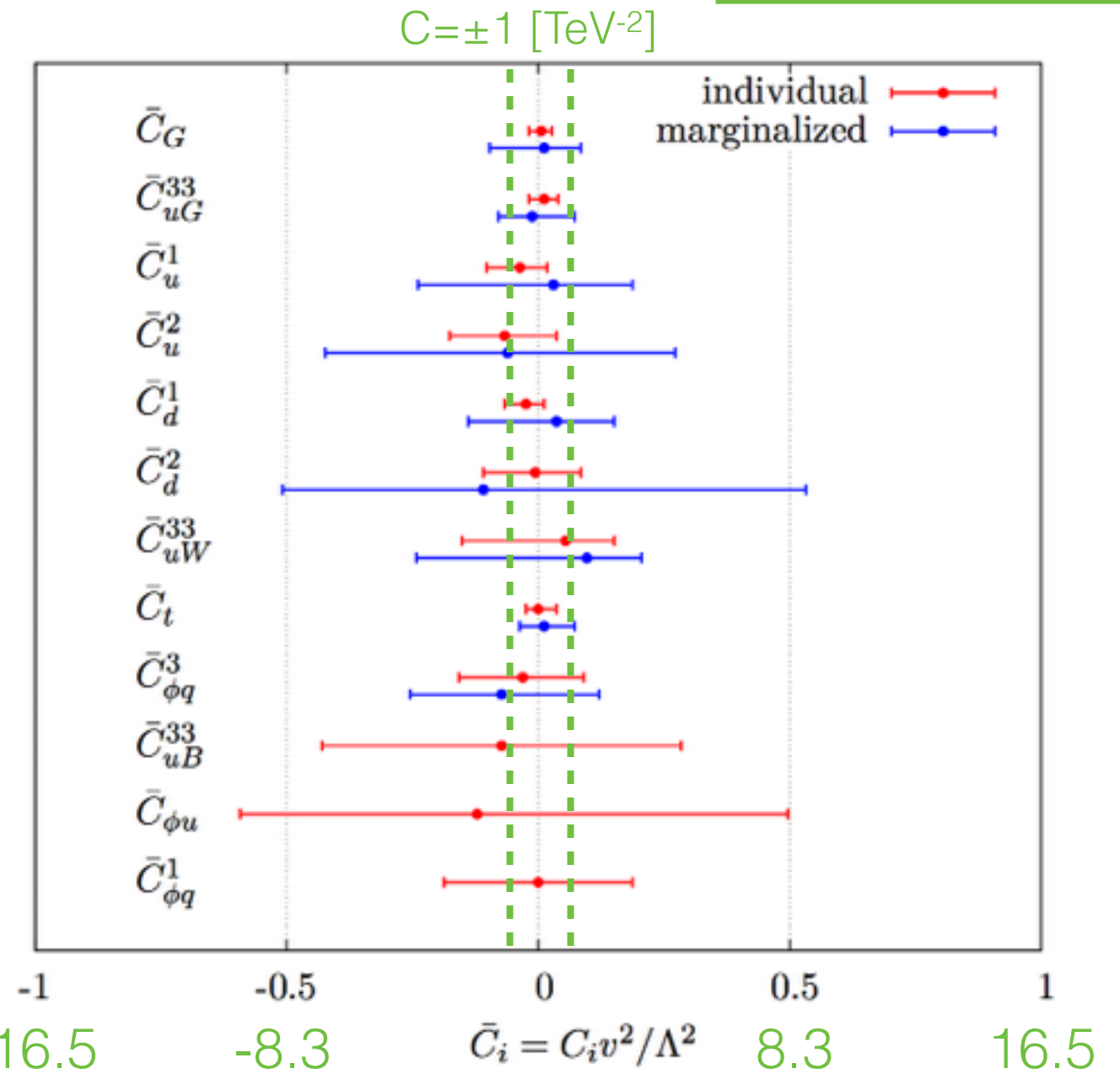


- Constrained a set of 12 operators at LO

- tt, single-top & tt+Z/γ
- Helicity fractions, A_{FB} & A_C

- Selected operators that interfere with SM

- ttg, tbW, ttZ, ggg + linear combinations of 4F operators
- EFT² dependence included in observables
- Impact is significant
- **Validity** assessment necessary



dim6top

[Aguilar-Saavedra et al.; arXiv:1802.07237]

Interpreting top-quark LHC measurements
in the standard-model effective field theory

J. A. Aguilar Saavedra,¹ C. Degrande,² G. Durieux,³
F. Maltoni,⁴ E. Vryonidou,² C. Zhang⁵ (editors),
D. Barducci,⁶ I. Brivio,⁷ V. Cirigliano,⁸ W. Dekens,^{8,9} J. de Vries,¹⁰ C. Englert,¹¹
M. Fabbrichesi,¹² C. Grojean,^{3,13} U. Haisch,^{2,14} Y. Jiang,⁷ J. Kamenik,^{15,16}
M. Mangano,² D. Marzocca,¹² E. Mereghetti,⁸ K. Mimasu,⁴ L. Moore,⁴ G. Perez,¹⁷
T. Plehn,¹⁸ F. Riva,² M. Russell,¹⁸ J. Santiago,¹⁹ M. Schulze,¹³ Y. Soreq,²⁰
A. Tonerio,²¹ M. Trott,⁷ S. Westhoff,¹⁸ C. White,²² A. Wulzer,^{2,23,24} J. Zupan.²⁵

- Consensus from the LHC top WG on SMEFT description for top physics
 - Classification of the relevant degrees of freedom (independent operators)
 - Prescription for staged implementation of flavor assumptions
 - Very nice overview & bigger picture discussion
- dim6top: FeynRules/UFO model provided
 - Useful to have a ‘unified’ & community validated tool
 - Avoid confusion of results presented in different bases, normalisations etc.
 - LO predictions only

All operators
previously
described
(including 4F)

<http://feynrules.irmp.ucl.ac.be/wiki/dim6top>

Anatomy of tHj

- LO helicity amplitudes

- High energy limit: $s \sim -t \gg v^2$

- Maximum energy growth

- SU(2) triplet current
- Interferes with leading SM
- RH Charged Current
- Weak dipole

- Fields strengths source transverse gauge bosons
- Not captured by Goldstone equiv.

- Subleading energy growth

- $\propto m_t$ & interferes with sub-leading SM amplitude \rightarrow no growth

bW \rightarrow tH (bW \rightarrow tZ in backup)

$\lambda_b, \lambda_W, \lambda_t$	SM	$\mathcal{O}_{t\varphi}$	$\mathcal{O}_{\varphi Q}^{(3)}$	$\mathcal{O}_{\varphi W}$	\mathcal{O}_{tW}	\mathcal{O}_{HW}
$-, 0, -$	s^0	s^0	$\sqrt{s(s+t)}$	s^0	s^0	$\sqrt{s(s+t)}$
$-, 0, +$	$\frac{1}{\sqrt{s}}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W s}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$
$-, -, -$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$	$m_W\sqrt{-t}$	$\frac{m_W s}{\sqrt{-t}}$	$m_t\sqrt{-t}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, -, +$	$\frac{1}{s}$	s^0	s^0	—	$\sqrt{s(s+t)}$	$\frac{1}{s}$
$-, +, -$	$\frac{1}{\sqrt{s}}$	—	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, +, +$	s^0	—	s^0	s^0	s^0	$\frac{1}{s}$

$\mathcal{O}_{\varphi tb}, \lambda_b = +$

$\lambda_t \backslash \lambda_W$	0	+	-
+	$\sqrt{s(s+t)}$	$m_W\sqrt{-t}$	$\frac{1}{\sqrt{s}}$
-	$m_t\sqrt{-t}$	s^0	s^0

Consistent with non-interference theorem in $2 \rightarrow 2$

[Cheung & Shen; PRL 115 (2015) 071601]
 [Azatov, Contino & Riva; PRD 95 (2017) 065014]

Anatomy of tZj

$bW \rightarrow tZ$

$\lambda_b, \lambda_W, \lambda_t, \lambda_Z$	SM	$\mathcal{O}_{\varphi Q}^{(3)}$	$\mathcal{O}_{\varphi Q}^{(1)}$	$\mathcal{O}_{\varphi t}$	\mathcal{O}_{tB}	\mathcal{O}_{tW}	\mathcal{O}_W	\mathcal{O}_{HW}	\mathcal{O}_{HB}
$-, 0, -, 0$	s^0	$\sqrt{s(s+t)}$	-	-	-	s^0	s^0	$\sqrt{s(s+t)}$	s^0
$-, 0, +, 0$	$\frac{1}{\sqrt{s}}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_Z \sqrt{-t}$	$\frac{m_W(2s+3t)}{\sqrt{-t}}$	-	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
$-, -, -, 0$	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	-	-	-	-	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$m_W \sqrt{-t}$	$\frac{1}{\sqrt{s}}$
$-, -, +, 0$	$\frac{1}{s}$	s^0	s^0	s^0	s^0	$\sqrt{s(s+t)}$	s^0	s^0	$\frac{1}{\sqrt{s}}$
$-, 0, -, -$	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	-	-	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$\frac{m_W(ss_W^2+2t)}{\sqrt{-t}}$	$\frac{m_W s}{\sqrt{-t}}$
$-, 0, -, +$	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, 0, +, -$	s^0	s^0	s^0	-	-	s^0	s^0	s^0	s^0
$-, 0, +, +$	$\frac{1}{s}$	s^0	s^0	s^0	$\sqrt{s(s+t)}$	$\sqrt{s(s+t)}$	-	s^0	s^0
$-, +, -, 0$	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
$-, +, +, 0$	s^0	s^0	-	-	-	s^0	-	s^0	$\frac{1}{s}$
$-, -, -, -$	s^0	s^0	s^0	-	s^0	s^0	s^0	s^0	s^0
$-, -, -, +$	$\frac{1}{s}$	-	-	-	-	-	$\sqrt{s(s+t)}$	s^0	s^0
$-, -, +, -$	$\frac{1}{\sqrt{s}}$	-	-	-	-	$\frac{m_Z(s_W^2 t - 3c_W^2(2s+t))}{\sqrt{-t}}$	-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
$-, -, +, +$	-	-	-	-	$m_W \sqrt{-t}$	$m_Z \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
$-, +, -, -$	$\frac{1}{s}$	-	-	-	-	-	$\sqrt{s(s+t)}$	s^0	s^0
$-, +, -, +$	s^0	s^0	s^0	-	-	-	-	s^0	s^0
$-, +, +, -$	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
$-, +, +, +$	$\frac{1}{\sqrt{s}}$	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$

$\mathcal{O}_{\varphi tb}, \lambda_b, \lambda_t = +, +$

$\lambda_Z \backslash \lambda_W$	0	+	-
0	$\sqrt{s(s+t)}$	$m_W \sqrt{-t}$	-
+	$m_Z \sqrt{-t}$	s^0	-
-	-	-	s^0

$\mathcal{O}_{\varphi tb}, \lambda_b, \lambda_t = +, -$

$\lambda_Z \backslash \lambda_W$	0	+	-
0	-	-	s^0
+	s^0	-	-
-	s^0	-	-

Consistent with non-interference theorem in $2 \rightarrow 2$

[Cheung & Shen; PRL 115 (2015) 071601]
 [Azatov, Contino & Riva; PRD 95 (2017) 065014]

Existing limits

[TeV⁻²]

Op.	TF (I)	TF (M)	RHCC (I) tree/loop	SFitter (I)	PEWM ²
\mathcal{O}_W				[-0.18,0.18]	
\mathcal{O}_{HW}				[-0.32,1.62]	
\mathcal{O}_{HB}				[-2.11,1.57]	
$\mathcal{O}_{\varphi W}$				[-0.39,0.33]	
$\mathcal{O}_{\varphi tb}$			[-5.28,5.28]/[-0.046,0.040]		
$\mathcal{O}_{\varphi Q}^{(3)}$	[-2.59,1.50]	[-4.19,2.00]			-1.0 ± 2.7 ³
$\mathcal{O}_{\varphi Q}^{(1)}$	[-3.10,3.10]				1.0 ± 2.7
$\mathcal{O}_{\varphi t}$	[-9.78,8.18]				1.8 ± 3.8
\mathcal{O}_{tW}	[-2.49,2.49]	[-3.99,3.40]			-0.4 ± 2.4
\mathcal{O}_{tB}	[-7.09,4.68]				4.8 ± 10.6
\mathcal{O}_{tG}	[-0.24,0.53]	[-1.07,0.99]			
$\mathcal{O}_{t\varphi}$				[-18.2,6.30]	
$\mathcal{O}_{Qq}^{(3,1)}$	[-0.40,0.60]	[0.66,1.24]			
$\mathcal{O}_{Qq}^{(3,8)}$	[-4.90,3.70]	[6.06,6.73]			

$$c_{t\varphi} \subset [-6.5, 1.3]$$

Combination of ttH @ 13 TeV

[CMS; CMS-PAS-HIG-17-003]

[CMS; CMS-PAS-HIG-17-004]

[ATLAS; CERN-EP-2017-281]

$$c_{Qq}^{(3,8)} \subset [-1.40, 1.20]$$

Combination of LHC single-top

[CMS; JHEP 12 (2012) 035]

[ATLAS; PRD 90 (2014) 11, 112006]

[CMS; JHEP 09 (2016) 027]

[ATLAS; JHEP 04 (2017) 086]

[ATLAS; EPJC 77 (2017) 8, 531]

[ATLAS; PLB 756 (2016) 228-246] SMEFT @ the LHC

$$pp \rightarrow t(\bar{t}) H j$$

$$c/\Lambda = 1 [\text{TeV}^{-2}]$$

Inclusive results: tHj

LHC@13 TeV

σ [fb]	LO	NLO	K-factor
σ_{SM}	$57.56(4)^{+11.2\%}_{-7.4\%} \pm 10.2\%$	$75.87(4)^{+2.2\%}_{-6.4\%} \pm 1.2\%$	1.32
$\sigma_{\varphi W}$	$8.12(2)^{+13.1\%}_{-9.3\%} \pm 9.3\%$	$7.76(2)^{+7.0\%}_{-6.3\%} \pm 1.0\%$	0.96
$\sigma_{\varphi W, \varphi W}$	$5.212(7)^{+10.6\%}_{-6.8\%} \pm 10.2\%$	$6.263(7)^{+2.6\%}_{-7.8\%} \pm 1.3\%$	1.20
$\sigma_{t\varphi}$	$-1.203(6)^{+12.0\%}_{-15.6\%} \pm 8.9\%$	$-0.246(6)^{+144.5[31.4]\%}_{-157.8[19.0]\%} \pm 2.1\%$	0.20
$\sigma_{t\varphi, t\varphi}$	$0.6682(9)^{+12.7\%}_{-8.9\%} \pm 9.6\%$	$0.7306(8)^{+4.6[0.6]\%}_{-7.3[0.2]\%} \pm 1.0\%$	1.09
σ_{tW}	$19.38(6)^{+13.0\%}_{-9.3\%} \pm 9.4\%$	$22.18(6)^{+3.8[0.4]\%}_{-6.8[0.9]\%} \pm 1.0\%$	1.14
$\sigma_{tW, tW}$	$46.40(8)^{+9.3\%}_{-5.5\%} \pm 11.1\%$	$71.24(8)^{+7.4[1.5]\%}_{-14.0[6.9]\%} \pm 1.9\%$	1.54
$\sigma_{\varphi Q^{(3)}}$	$-3.03(3)^{+0.0\%}_{-2.2\%} \pm 15.4\%$	$-10.04(4)^{+11.1\%}_{-8.9\%} \pm 1.8\%$	3.31
$\sigma_{\varphi Q^{(3)}, \varphi Q^{(3)}}$	$11.23(2)^{+9.4\%}_{-5.6\%} \pm 11.2\%$	$15.28(2)^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.36
$\sigma_{\varphi tb}$	0	0	—
$\sigma_{\varphi tb, \varphi tb}$	$2.752(4)^{+9.4\%}_{-5.5\%} \pm 11.3\%$	$3.768(4)^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.54
σ_{HW}	$-3.526(4)^{+5.6\%}_{-9.5\%} \pm 10.9\%$	$-5.27(1)^{+6.5\%}_{-2.9\%} \pm 1.5\%$	1.50
$\sigma_{HW, HW}$	$0.9356(4)^{+7.9\%}_{-4.0\%} \pm 12.3\%$	$1.058(1)^{+4.8\%}_{-11.9\%} \pm 2.3\%$	1.13
σ_{tG}		$-0.418(5)^{+12.3\%}_{-9.8\%} \pm 1.1\%$	—
$\sigma_{tG, tG}$		$1.413(1)^{+21.3\%}_{-30.6\%} \pm 2.5\%$	—
$\sigma_{Q\varphi^{(3,1)}}$	$-22.50(5)^{+8.0\%}_{-11.8\%} \pm 9.7\%$	$-20.10(5)^{+13.8\%}_{-13.3\%} \pm 1.1\%$	0.89
$\sigma_{Q\varphi^{(3,1)}, Q\varphi^{(3,1)}}$	$69.78(3)^{+8.0\%}_{-4.1\%} \pm 12.1\%$	$62.20(3)^{+11.5\%}_{-15.9\%} \pm 2.3\%$	0.89
$\sigma_{Q\varphi^{(3,8)}}$	—	$0.25(3)^{+25.4\%}_{-27.1\%} \pm 4.7\%$	—
$\sigma_{Q\varphi^{(3,8)}, Q\varphi^{(3,8)}}$	$15.53(2)^{+8.0\%}_{-4.1\%} \pm 12.1\%$	$14.07(2)^{+11.0\%}_{-15.7\%} \pm 2.1\%$	0.91

K-factors **not universal**

Reduction of QCD scale/PDF uncertainties

EFT scale uncertainty **subdominant**

Some very **strong dependence** on EFT operators

O(> 1) deviations within current bounds

σ [fb]	LO	NLO	K-factor
σ_{SM}	660.8(4) $^{+13.7\%}_{-9.6\%} \pm 9.7\%$	839.1(5) $^{+1.1\%}_{-5.1\%} \pm 1.0\%$	1.27
σ_W	-7.87(7) $^{+8.4\%}_{-12.6\%} \pm 9.7\%$	-8.77(8) $^{+8.5\%}_{-4.3\%} \pm 1.1\%$	1.12
$\sigma_{W,W}$	34.58(3) $^{+8.2\%}_{-3.9\%} \pm 13.0\%$	43.80(4) $^{+6.6\%}_{-15.1\%} \pm 2.8\%$	1.27
σ_{tB}	2.23(2) $^{+14.7[0.9]\%}_{-10.7[1.0]\%} \pm 9.4\%$	2.94(2) $^{+2.3[0.4]\%}_{-3.0[0.7]\%} \pm 1.1\%$	1.32
$\sigma_{tB,tB}$	2.833(2) $^{+10.5[1.7]\%}_{-6.3[1.9]\%} \pm 11.1\%$	4.155(3) $^{+4.7[0.9]\%}_{-10.1[1.4]\%} \pm 1.7\%$	1.47
σ_{tW}	2.66(4) $^{+18.8[0.9]\%}_{-15.3[1.0]\%} \pm 11.4\%$	13.0(1) $^{+15.8[2.1]\%}_{-22.8[0.0]\%} \pm 1.2\%$	4.90
$\sigma_{tW,tW}$	48.16(4) $^{+10.0[1.7]\%}_{-5.8[1.9]\%} \pm 11.3\%$	80.00(4) $^{+7.9[1.3]\%}_{-14.7[1.6]\%} \pm 1.9\%$	1.66
$\sigma_{\varphi dtR}$	4.20(1) $^{+14.9\%}_{-10.9\%} \pm 9.3\%$	4.94(2) $^{+3.4\%}_{-6.7\%} \pm 1.0\%$	1.18
$\sigma_{\varphi dtR,\varphi dtR}$	0.3326(3) $^{+13.6\%}_{-9.5\%} \pm 9.6\%$	0.4402(5) $^{+3.7\%}_{-9.3\%} \pm 1.0\%$	1.32
$\sigma_{\varphi Q}$	14.98(2) $^{+14.5\%}_{-10.5\%} \pm 9.4\%$	18.07(3) $^{+2.3\%}_{-1.6\%} \pm 1.0\%$	1.21
$\sigma_{\varphi Q,\varphi Q}$	0.7442(7) $^{+14.1\%}_{-10.0\%} \pm 9.5\%$	1.028(1) $^{+2.8\%}_{-7.3\%} \pm 1.0\%$	1.38
$\sigma_{\varphi Q(3)}$	130.04(8) $^{+13.8\%}_{-9.8\%} \pm 9.5\%$	161.4(1) $^{+0.9\%}_{-4.8\%} \pm 1.0\%$	1.24
$\sigma_{\varphi Q(3),\varphi Q(3)}$	17.82(2) $^{+11.7\%}_{-7.5\%} \pm 10.5\%$	23.98(2) $^{+3.7\%}_{-9.3\%} \pm 1.4\%$	1.35
$\sigma_{\varphi tb}$	0	0	-
$\sigma_{\varphi tb,\varphi tb}$	2.949(2) $^{+10.5\%}_{-6.2\%} \pm 11.1\%$	4.154(4) $^{+5.1\%}_{-11.2\%} \pm 1.8\%$	1.41
σ_{HW}	-5.16(6) $^{+7.8\%}_{-12.0\%} \pm 10.5\%$	-6.88(8) $^{+6.4\%}_{-2.0\%} \pm 1.4\%$	1.33
$\sigma_{HW,HW}$	0.912(2) $^{+9.4\%}_{-5.2\%} \pm 12.0\%$	1.048(2) $^{+5.2\%}_{-12.8\%} \pm 2.1\%$	1.15
σ_{HB}	-3.015(9) $^{+9.9\%}_{-13.9\%} \pm 9.5\%$	-3.76(1) $^{+5.2\%}_{-1.0\%} \pm 1.0\%$	1.25
$\sigma_{HB,HB}$	0.02324(6) $^{+12.7\%}_{-8.5\%} \pm 9.9\%$	0.02893(6) $^{+2.3\%}_{-7.5\%} \pm 1.1\%$	1.24
σ_{tG}		0.45(2) $^{+93.0\%}_{-148.8\%} \pm 4.9\%$	-
$\sigma_{tG,tG}$		2.251(4) $^{+20.9\%}_{-30.0\%} \pm 2.5\%$	-
$\sigma_{Qq(3,1)}$	-393.5(5) $^{+8.1\%}_{-12.3\%} \pm 10.0\%$	-498(1) $^{+8.9\%}_{-3.2\%} \pm 1.2\%$	1.26
$\sigma_{Qq(3,1),Qq(3,1)}$	462.25(3) $^{+8.4\%}_{-4.1\%} \pm 12.7\%$	545.50(5) $^{+7.4\%}_{-17.4\%} \pm 2.9\%$	1.18
$\sigma_{Qq(3,8)}$	0	-0.9(3) $^{+23.3\%}_{-26.3\%} \pm 19.2\%$	-
$\sigma_{Qq(3,8),Qq(3,8)}$	102.73(5) $^{+8.4\%}_{-4.1\%} \pm 12.7\%$	111.18(5) $^{+9.3\%}_{-18.4\%} \pm 2.8\%$	1.08

tZj ~ 10 times bigger than tHj

NLO corrections: similar features to tHj

EFT contributions smaller relative to SM

Higgs always radiated from top/EW gauge boson
 Z boson can also come from light quark leg

Dimension 8 in ttbb

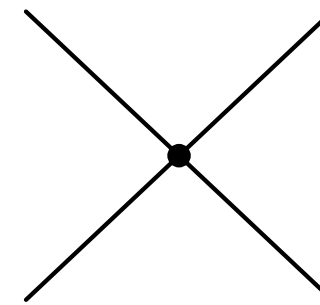
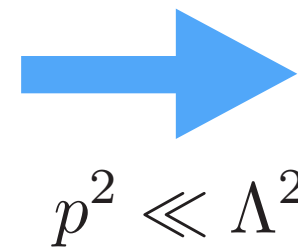
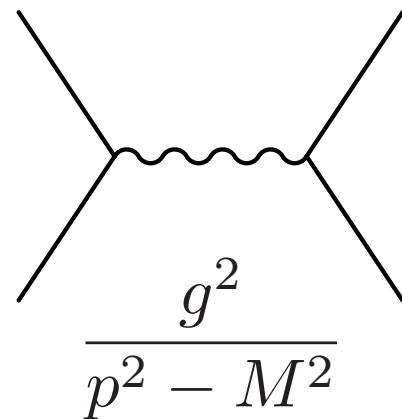
- Sensitivity dominated by EFT squared ($1/\Lambda^4$) terms
 - Non-interference due to colour
 - Large Wilson coefficients \sim strong coupling regime $\frac{C^{(6)}E^2}{\Lambda^2} \gtrsim 1$
- Are higher dimension operators relevant?
- As long as $E < \Lambda$
 - 6 fermion operators: at least dim-10 $\sim (E/\Lambda)^6$
 - Dim-8 four fermion operators $\sim (E/\Lambda)^4$

schematically: $ffffD_\mu D_\nu$ & $ffffG_{\mu\nu}$

one coupling & one scale power counting:

$$\mathcal{L}_{\text{EFT}} = \frac{\Lambda_{NP}^4}{g_*^2} \mathcal{L} \left(\frac{D_\mu}{\Lambda_{NP}}, \frac{g_* H}{\Lambda_{NP}}, \frac{g_* f_{L,R}}{\Lambda_{NP}^{3/2}}, \frac{g F_{\mu\nu}}{\Lambda_{NP}^2} \right)$$

Power counting



$$-\frac{g^2}{\Lambda^2} \left[1 + \frac{p^2}{\Lambda^2} + \frac{p^4}{\Lambda^4} + \dots \right]$$

D=6

D=8

$$\frac{C_{4F}^{(6)}}{\Lambda^2} \sim \frac{C_{4F}^{(8)}}{\Lambda^2} \sim \frac{g_*^2}{M^2}$$

dim-6 interference: $\frac{g_s^6 g_*^2 E^2}{\Lambda_{NP}^2}$

dim-6 quadratic term: $\frac{g_s^4 g_*^4 E^4}{\Lambda_{NP}^4}$

$$(g_*/g_s)^2 E^2 / \Lambda_{NP}^2 \approx 1. \rightarrow \text{SQ} \sim \text{INT}$$

$ffff D_\mu D_\nu$ $\frac{C_i^{(8)}}{\Lambda^2} \sim \frac{g_*^2}{M^2}$

$ffff G_{\mu\nu}$ $\frac{C_i^{(8)}}{\Lambda^2} \sim \frac{g_*^2 g_s}{M^2}$

ttbb operator + 2 derivatives

gttbb contact term

ggttbb contact term

dim-8 interference: $\frac{g_s^6 g_*^2 E^4}{\Lambda_{NP}^4}$

no g^* enhancement