Development of Start-to-End Simulation for ILC positron sources

KEK    M. Fukuda
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• Simulation test on the undulator scheme using Geant4
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The purpose of development of simulation for ILC positron source

• I will develop start-to-end simulation codes for ILC positron source.
  • Positron generation of target: Geant4
  • Target to Capture section: Geant4 or GPT
  • Booster section to DR: SAD

• The purpose is to compare the yield calculation of positron generation for both undulator scheme and e-driven scheme under the same condition.

• I am developing the simulation program from the positron generation to the end of the capture section.
  • Code: Geant4.10
  • The program is based on the example program of B4.
Simulation of a positron source for undulator method

I am making the simulation code for a positron source by using Geant4.10. The tracking of positrons up to the exit of Capture section (125MeV) can be simulated now.

The tracking of positrons after the capture section is simulated by T. Okugi.

Positron generation at a target --- Capture section (125MeV): calculated by M. Fukuda
Tracking of positrons after Capture section: T. Okugi
Positron generation

Gamma-rays data from Undulators was calculated by CAIN (Yokoya’s calculation)

**Number of Gamma-rays:** 4.03e6 (4,025,930).

There are generated from 10,000 electrons with the energy of 125GeV.

**Target:** Ti6Al4V, thickness 7mm

**Number of generated positrons:** 4.43e4

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**Gamma-rays from Undulator**

**Ti6Al4V 7mm**

**Generated positrons**

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<table>
<thead>
<tr>
<th>Energy [MeV]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Entries</td>
</tr>
<tr>
<td>Mean</td>
</tr>
<tr>
<td>RMS</td>
</tr>
</tbody>
</table>

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Magnetic field of QWT and Solenoid

The magnetic field data was calculated by POISSON. This 2D map data of magnetic field is used in the simulation. QWT (Peak 1.04T) + 0.5T (capture section) After z = 444.5mm, Bz = const. (~0.51T), Br = 0

 Designed by Wanming Liu
 Recalculated by Fukuda
Accelerating electric field of standing wave tube

I consider only the accelerating electric field $E_z$.

$$E_z = E_0 \cdot 2 \cdot \sin(\text{omegaspace} \cdot (z-z_{\text{front RF}})) \cdot \cos(\text{omegatime} \cdot t + \text{Ephase})$$

$$\text{omegaspace} = k = \frac{2\pi}{\lambda}$$

$$\text{omegatime} = \omega = \frac{2\pi f}{c} = \frac{2\pi}{\lambda}$$

$$\lambda = 230.60958\text{mm} \ (L\text{-band})$$

$E_{\text{acc}}: 15.2\text{MV/m}$

1.27m (11 cells)

Aperture ($2a$): 60mm

Table 1: Parameters of SW structure.

<table>
<thead>
<tr>
<th>Structure Type</th>
<th>Simple $\pi$ Mode</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell Number</td>
<td>11</td>
</tr>
<tr>
<td>Aperture 2a</td>
<td>60 mm</td>
</tr>
<tr>
<td>$Q$</td>
<td>29700</td>
</tr>
<tr>
<td>Shunt impedance $r$</td>
<td>34.3 M$\Omega$/m</td>
</tr>
<tr>
<td>$E_0$ (8.6 MW input)</td>
<td>15.2 MV/m</td>
</tr>
</tbody>
</table>

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Accelerating electric field of traveling wave tube

I consider only the accelerating electric field $E_z$.

$$E_z = E_0*\sin(\text{omegaspace}*(z-z\text{-frontRF}) - \text{omegatime}*t - E\text{phase})$$

$\text{omegaspace} = k = 2\pi/\lambda$  
$\text{omegatime} = \omega = 2\pi f = 2\pi c/\lambda$

$\lambda = 230.60958\text{mm (L-band)}$  
$E_{acc}: 7.2\text{MV/m}$

Table 2. Parameters of TW structure

<table>
<thead>
<tr>
<th>Structure Type</th>
<th>TW 3π/4 Mode</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell Number</td>
<td>50</td>
</tr>
<tr>
<td>Aperture 2a</td>
<td>46 mm</td>
</tr>
<tr>
<td>Attenuation $\tau$</td>
<td>0.98</td>
</tr>
<tr>
<td>$Q$</td>
<td>24842 - 21676</td>
</tr>
<tr>
<td>Group velocity $V_g/c$</td>
<td>0.62% – 0.14%</td>
</tr>
<tr>
<td>Shunt impedance $r$</td>
<td>48.60 – 39.45 MΩ/m</td>
</tr>
<tr>
<td>Filling time $T_f$</td>
<td>5.3 μs</td>
</tr>
<tr>
<td>Power Dissipation</td>
<td>8.2 kW/m</td>
</tr>
<tr>
<td>$E_0$ (8.6 MW input)</td>
<td>8.0 MV/m</td>
</tr>
</tbody>
</table>

Figure 4. Profiles of the first, middle and last cell for 4.3m 3π/4 Mode TW structures,

J. W. Wang  SLAC-PUB-12412
Placement of the QWT and an accelerator

Target – QWT: 11.5mm
QWT – ACC: 50mm
Arrangement of acceleration tube

I adjusted the space between the accelerating tubes so that the accelerating tubes would have the same acceleration phase. The distance between accelerating tubes is an integral multiple of the wavelength.

**Standing wave tube**

- $5.5\lambda = 11\text{cells}$
- $7\lambda$
- $1.5\lambda = 3\text{cells}$

**Traveling wave tube:**

- $20\lambda$
- $18.75\lambda = 50\text{cells}$
- $1.25\lambda$
- $18.75\lambda = 50\text{cells}$
Parameters of the simulation up to the capture section for undulator scheme

Input: Gamma-rays from Undulators calculated by CAIN (Yokoya’s calculation)

**Number of Gamma-rays is 4,025,930** which are generated from 10000 electrons with 125GeV.

Target: Ti6Al4V, 7mm

OMD: **QWT (Peak 1.04T) + 0.5T (capture section)**
The magnetic filed was calculated by POISSON.

**Accelerating tube**: SWx2 + TWx3

Standing wave tube: **Eacc: 15.2MV/m**, L-band (1.3GHz) 11cell (1.268m)
Traveling wave tube: **Eacc: 7.2MV/m**, L-band (1.3GHz) 50cell (4.324m)

→ Positrons are accelerated to about 125MeV.
Phase scan of accelerators

The phase of the accelerator was optimized so that the number of positrons within +/- 7 mm in the longitudinal position distribution was maximized.

Positrons within +/-7mm in the longitudinal position distribution are captured in DR.

The phases of all the accelerating tubes were simultaneously moved.

All particles
Captured

Analyzed by T. Okugi
Number of positrons after capture section (125MeV)
Energy, z position and time distribution of positrons

Phase 160deg

Phase 180deg
Tracking Simulations

simulated by Andriy Ushakov

Used parameters are:
* 126.5 GeV e-beam
* 231 m undulator with $K = 0.85$
* 401 m distance between the middle of undulator and the target
* 7 mm target thickness (Ti6Al4V)
* QWT with 1.04 T field solenoid downstream the target
* Deceleration E-field downstream QWT

simulated by M. Fukuda

Target: Ti alloy (Ti-6Al-4V), 7mm
QWT: 1.04T
ACC SOL: 0.5T
ACC SWx2: Eacc 15.2MV/m
ACC TWx3: Eacc 7.2MV/m

Analyzed by T. Okugi
**Comparison of 2 simulations**

Transverse momentum ($P_t$) distribution in the low energy region is totally different.

After tracking 400MeV, the upper limit of transverse momentum is the same.
Transverse momentum when the aperture(2a) of TW is 60mm

I calculated positrons distribution after capture section when the aperture(2a) of TW tube was changed from 46mm to 60mm.
In this case, the maximum of Pt became 2.5 MeV/c. However, the distribution around 1MeV/c is different yet.

Aperture(2a) of TW tube: 46 → 60mm
Comparison of positron distributions at the exit of a target

In the region of large angle, the distribution is different.

The effect is caused by the magnetic field on the target.

If the magnetic field is zero, The distribution is almost same.

I thank Ushakov-san for sending me the data of positron simulation.

Analyzed by T. Okugi
I tracked the positrons using the Ushakov-san’s positron data at the exit of a target. However, the transverse momentum distribution of positrons was not changed. I could not reproduce the result he calculated.

**Number of e+ at the exit of a target**
- 4.5e4 (M. Fukuda)
- 4.7e4 (A. Ushakov)

**Target**: Ti6Al4V, 7mm  
**OMD**: QWT (Peak 1.04T)  
**Solenoid**: 0.5T (capture section)  

**Accelerating tube**: SWx2 + TWx3  
**SW**: Eacc: 15.2MV/m  
**TW**: Eacc: 7.3MV/m

Transverse momentum distribution of positrons at 125MeV
Summary

• The tracking simulation up to the exit of Capture section (125MeV)
  • The yield of positrons in my simulation is different from the Ushakov-san result.
  • Positron yield(e+/e-): 1.3 (Ushakov), 0.8 (Fukuda)
  • Transverse momentum distribution is different.
  • It has not been clarified why the difference is occurring.
  • To investigate the reason, I am preparing the positron tracking simulation by using GPT code.

• Development of the simulation for positron source
  • The simulation of positron source for e-driven scheme (ILC and SuperKEKB)