

Uploaded after the meeting:

→ Corrections on some formulas p10

Signal uncertainties in STXS stage 1 for VH(bb)

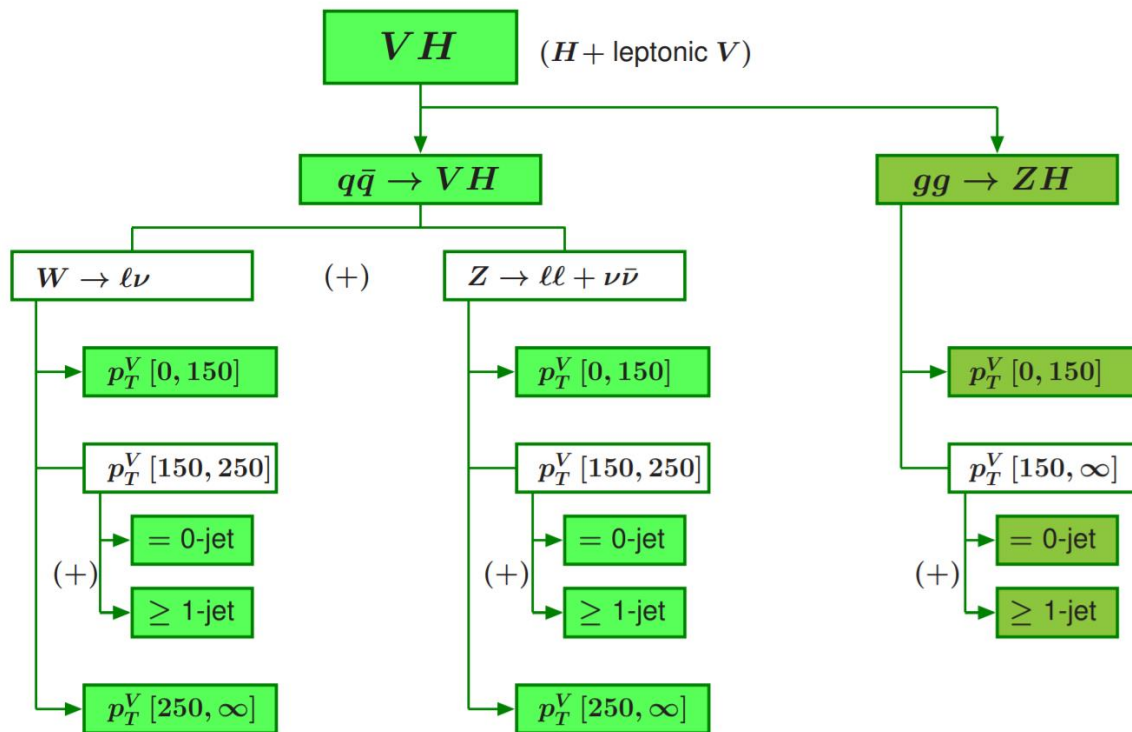
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*Fiducial/STXS subgroup meeting
May 17th, 2018*



Introduction: STXS binning

- Stage 1: truth binning based on VH(bb) analysis categories
 - Reduce impact of theory on the measurement (no acceptance, ...)



Split production mode:

- qq/gg initiated
- different calculations

Split with variables used for analysis categorization:

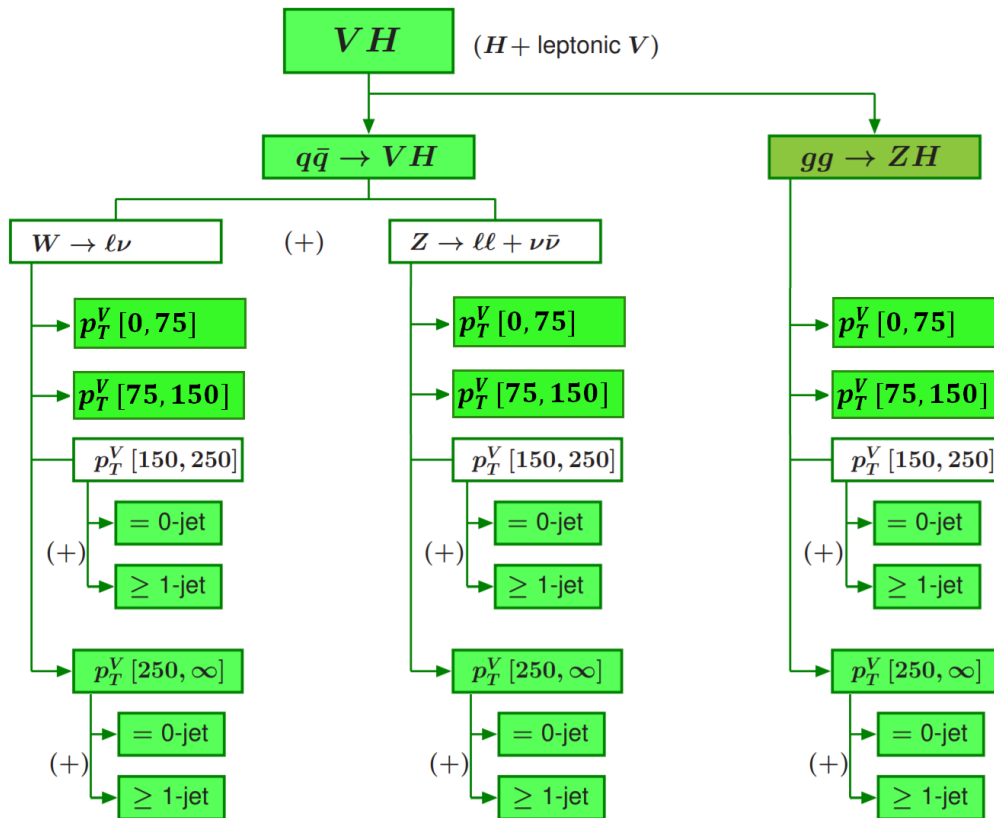
- W/Z, $p_T(V)$, N(jets) not from Higgs

Original plan: [LHC report 4 \(click me\)](#)



Introduction: STXS binning

- Stage 1: truth binning based on VH(bb) analysis categories
 - Reduce impact of theory on the measurement (no acceptance, ...)



Analysis already use finer categorization

Implement stage 1+:

- Get closer to analysis bins
- Left figure with split Z to $\ell\ell/\nu\nu$

Consider a finer “stage 1++”:

- Towards stage 2:
 - Split at $p_T(V) = 400 \text{ GeV}$
- For analysis unc. estimation:
 - More N(add jet) bins (≥ 2)
 - N(add jet) also for low $p_T(V)$?

Goal: derive uncertainties for stage 1++ and merge where needed

3 signal uncertainty sets to discuss:

-> **Scale**

-> **PDF**

-> **PS / UE**



Scale Variations: The Big Guys

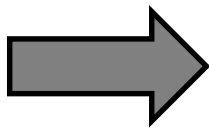
- Problematic: how to deal with bin migration/correlation
- 2 bins (a and b) case: the generic parametrization

Uncertainty matrix = correlated + anti-correlated components

$$C(\{\sigma_a, \sigma_b\}) = \begin{pmatrix} (\Delta_a^y)^2 & \Delta_a^y \Delta_b^y \\ \Delta_a^y \Delta_b^y & (\Delta_b^y)^2 \end{pmatrix} + \begin{pmatrix} \Delta_{a/b}^2 & -\Delta_{a/b}^2 \\ -\Delta_{a/b}^2 & \Delta_{a/b}^2 \end{pmatrix}$$

1 bin case

$$\begin{array}{l} \text{XSec} = \sigma_{ab} \\ \text{Unc } \Delta_{ab}^y \end{array}$$



2 bin case: a + b = 1 (event fractions)

Overall unc:
Impact of Δ_{ab}^y
in the two bins

$$\begin{array}{l} \text{XSec} = \sigma_a \\ \text{Unc } \Delta_a^y + \Delta_{a/b} \end{array}$$

$$\begin{array}{l} \text{XSec} = \sigma_b \\ \text{Unc } \Delta_b^y - \Delta_{a/b} \end{array}$$

Migration unc
induced by a/b
cut

[LHC report 4 \(click me\)](#) for more details



Scale Variations: The Big Guys

➤ Parametrization in the VH(bb) stage 1 case

➤ Showing WH here, in stage 1 same table for ZH (from [Les Houches 2017, click me](#))

$q\bar{q}' \rightarrow W$	QCD uncertainties			
	Δ_{WH}^y	Δ_{150}^{WH}	Δ_{250}^{WH}	$\Delta_{0/1}^{WH}$
$p_T^V [0,150]$	x_1	-1	-y	
$p_T^V [150,250]$	x_2	+1 - y	-(1 - y)	0
= 0-jet	$x_2 z$	+(1 - y)z	-(1 - y)z	+1
≥ 1-jet	$x_2(1 - z)$	+(1 - y)(1 - z)	-(1 - y)(1 - z)	-1
$p_T^V [250,\infty]$	x_3	y	+1	

$$unc_{[0,150]} = x_1 \Delta_{WH}^y - \Delta_{150}^{WH} - y_2 \Delta_{250}^{WH}$$

$$unc_{[150,250]} = x_2 \Delta_{WH}^y + (1 - y_1) \Delta_{150}^{WH} - y_2 \Delta_{250}^{WH}$$

Sign: keep track of correlation
Actual unc size: squared sum

$$unc_{[250,\infty]} = x_3 \Delta_{WH}^y + y_1 \Delta_{150}^{WH} + \Delta_{250}^{WH}$$

➤ How to compute all parameters ?

Original proposal: $x_{[250,\infty]} = \Delta_{[250,\infty]}^y / \Delta^y$

$$\Delta_{250}^y \sim \Delta_{[250,\infty]}^y$$

❖ Over-enhancement issue:

$$unc_{[250,\infty]} = (\Delta_{250}^y / \Delta^y) \Delta^y + y_1 \Delta_{150} + \Delta_{250}$$

Can new scheme solve this ?



Parameter Calculation Proposal

➤ Calculating the $x_i/y/z$:

	Δ	Δ_{75}	Δ_{150}	Δ_{250}	Δ_{150J}	Δ_{250J}
0-75	$\frac{Y_{[0,75]}}{Y_{Total}}$	-1	$-\frac{Y_{[0,75]}}{Y_{[0,150]}}$	$-\frac{Y_{[0,75]}}{Y_{[0,250]}}$		
75-150	$\frac{Y_{[75,150]}}{Y_{Total}}$	$\frac{Y_{[75,150]}}{Y_{[75,\infty]}}$	$-\frac{Y_{[75,150]}}{Y_{[0,150]}}$	$-\frac{Y_{[75,150]}}{Y_{[0,250]}}$		
150-250 0J	$\frac{Y_{[150,250]+0J}}{Y_{Total}}$	$\frac{Y_{[150,250]+0J}}{Y_{[75,\infty]}}$	$\frac{Y_{[150,250]+0J}}{Y_{[150,\infty]}}$	$-\frac{Y_{[150,250]+0J}}{Y_{[0,250]}}$	-1	
150-250 1J+	$\frac{Y_{[150,250]+1J+}}{Y_{Total}}$	$\frac{Y_{[150,250]+1J+}}{Y_{[75,\infty]}}$	$\frac{Y_{[150,250]+1J+}}{Y_{[150,\infty]}}$	$-\frac{Y_{[150,250]+1J+}}{Y_{[0,250]}}$	1	
250+ 0J	$\frac{Y_{[250,\infty]+0J}}{Y_{Total}}$	$\frac{Y_{[250,\infty]+0J}}{Y_{[75,\infty]}}$	$\frac{Y_{[250,\infty]+0J}}{Y_{[150,\infty]}}$	$\frac{Y_{[250,\infty]+0J}}{Y_{[250,\infty]}}$		-1
250+ 1J+	$\frac{Y_{[250,\infty]+1J+}}{Y_{Total}}$	$\frac{Y_{[250,\infty]+1J+}}{Y_{[75,\infty]}}$	$\frac{Y_{[250,\infty]+1J+}}{Y_{[150,\infty]}}$	$\frac{Y_{[250,\infty]+1J+}}{Y_{[250,\infty]}}$		1

Sum to 1 0 0 0 0 0

Replace:

“relative unc fraction”
 $x_{[250,\infty]} = \Delta_{[250,\infty]}^y / \Delta^y$



“yields fractions (bin acceptance)”

$$x_{[250,\infty]} = y_{[250,\infty]} / y_{[0,\infty]}$$

In the $[250, \infty[$ (without considering N(jet) split)

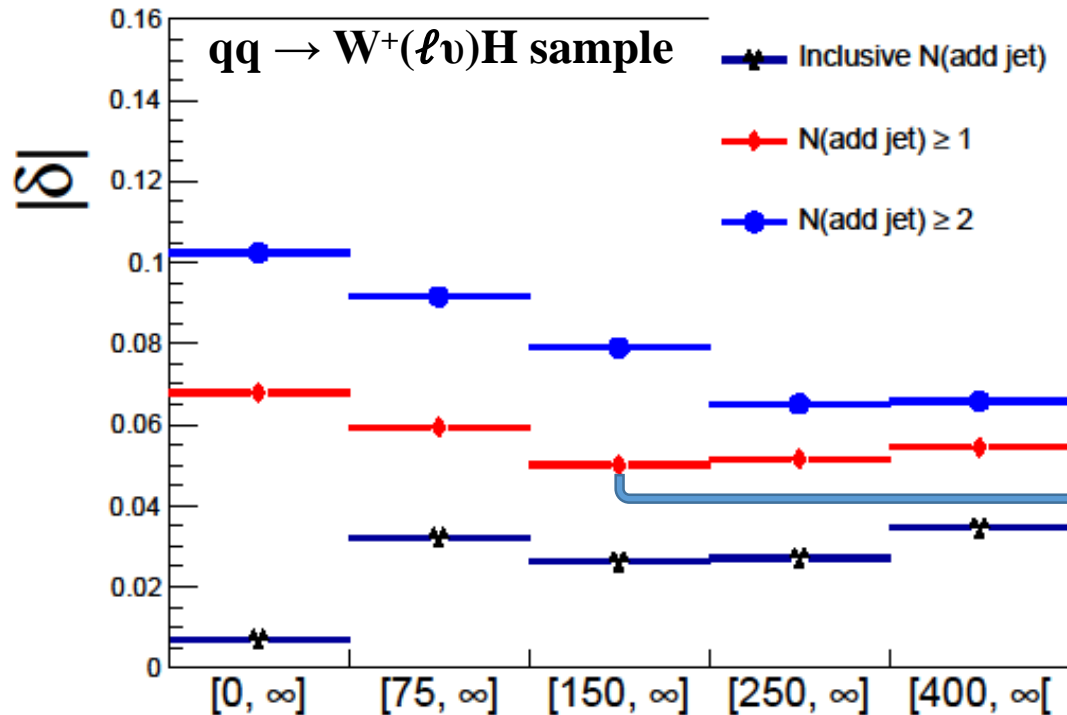
$$unc_{[250,\infty]} = \Delta * \frac{y_{[250,\infty[}}{y_{[0,\infty[}} + \Delta_{75} \frac{y_{[250,\infty[}}{y_{[75,\infty[}} + \Delta_{150} \frac{y_{[250,\infty[}}{y_{[150,\infty[}} + \Delta_{250}$$



Estimations of Δ_S

➤ Available ingredients:

- Overall relative unc. δ from NNLO QCD cross-section in YR4
- Relative uncertainties $\delta_{[a,b]}$ on $y_{[a,b]}$ from Powheg+MINLO with non-diagonal scale variation by a factor of 2



Read as:

For $p_T(V) > 150$ GeV (bin 3)
and $N(\text{add jets}) \geq 1$ (red points)

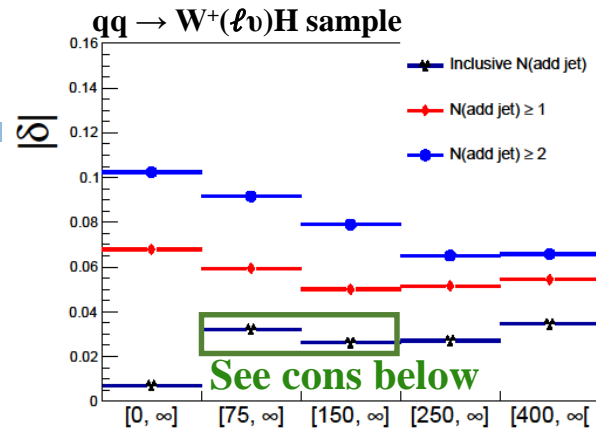
Rel unc: $\delta_{[250, \infty[\cup [1jet]} = 5.01\%$



Estimations of Δ_s

➤ Available ingredients:

- Overall relative unc. δ from YR4
- Relative uncertainties $\delta_{[a,b]}$ on $y_{[a,b]}$ from Powheg+MINLO



➤ Proposal for Δ_s :

→ In our same example:

$$y_{[250,\infty[} * \delta_{[250,\infty[} = \Delta * \frac{y_{[250,\infty[}}{y_{[0,\infty[}} + \Delta_{75} \frac{y_{[250,\infty[}}{y_{[75,\infty[}} + \Delta_{150} \frac{y_{[250,\infty[}}{y_{[150,\infty[}} + \Delta_{250}$$

→ When solving the equations (with approximations):

$$\begin{aligned} \Delta &= y_{tot} \cdot \delta \\ \Delta_{75} &= y_{[75,\infty[} \cdot (\delta_{[75,\infty[} \ominus \delta) \\ \Delta_{150} &= y_{[150,\infty[} \cdot (\delta_{[150,\infty[} \ominus \delta_{[75,\infty[}) \\ \Delta_{250} &= y_{[250,\infty[} \cdot (\delta_{[250,\infty[} \ominus \delta_{[150,\infty[}) \\ \Delta_{150J} &= y_{[150,250[\cup [\geq 1jet]} \\ &\quad \cdot (\delta_{[150,250[\cup [\geq 1jet]} \ominus \delta_{[150,\infty[}) \\ \Delta_{250J} &= y_{[250,\infty[\cup [\geq 1jet]} \\ &\quad \cdot (\delta_{[250,\infty[\cup [\geq 1jet]} \ominus \delta_{[250,\infty[}) \end{aligned}$$

Pro

Quadrature subtraction naturally remove some double-counting

Cons

Ill defined if relative uncertainty reduce with $p_T(V)$ or $N(\text{add jet})$
 Δ_{150} for us



Estimations of Δ s

- Frank's proposal: if ill defined use 0.5*relative variation
 - Applied also to sub-sequent Δ 's
 - Also consider applying it only to ill defined Δ 's
 - Which error propagation is the more correct ?

$$\begin{aligned}\Delta &= y_{tot} \cdot \delta \\ \Delta_{75} &= y_{[75,\infty[} \cdot (\delta_{[75,\infty[} \ominus \delta) \\ \Delta_{150} &= y_{[150,\infty[} \cdot (\delta_{[150,\infty[} \ominus \delta_{[75,\infty[}) \\ \Delta_{250} &= y_{[250,\infty[} \cdot (\delta_{[250,\infty[} \ominus \delta_{[150,\infty[}) \\ \Delta_{150J} &= y_{[150,250[\cup [\geq 1jet]} \\ &\quad \cdot (\delta_{[150,250[\cup [\geq 1jet]} \ominus \delta_{[150,\infty[}) \\ \Delta_{250J} &= y_{[250,\infty[\cup [\geq 1jet]} \\ &\quad \cdot (\delta_{[250,\infty[\cup [\geq 1jet]} \ominus \delta_{[250,\infty[})\end{aligned}$$

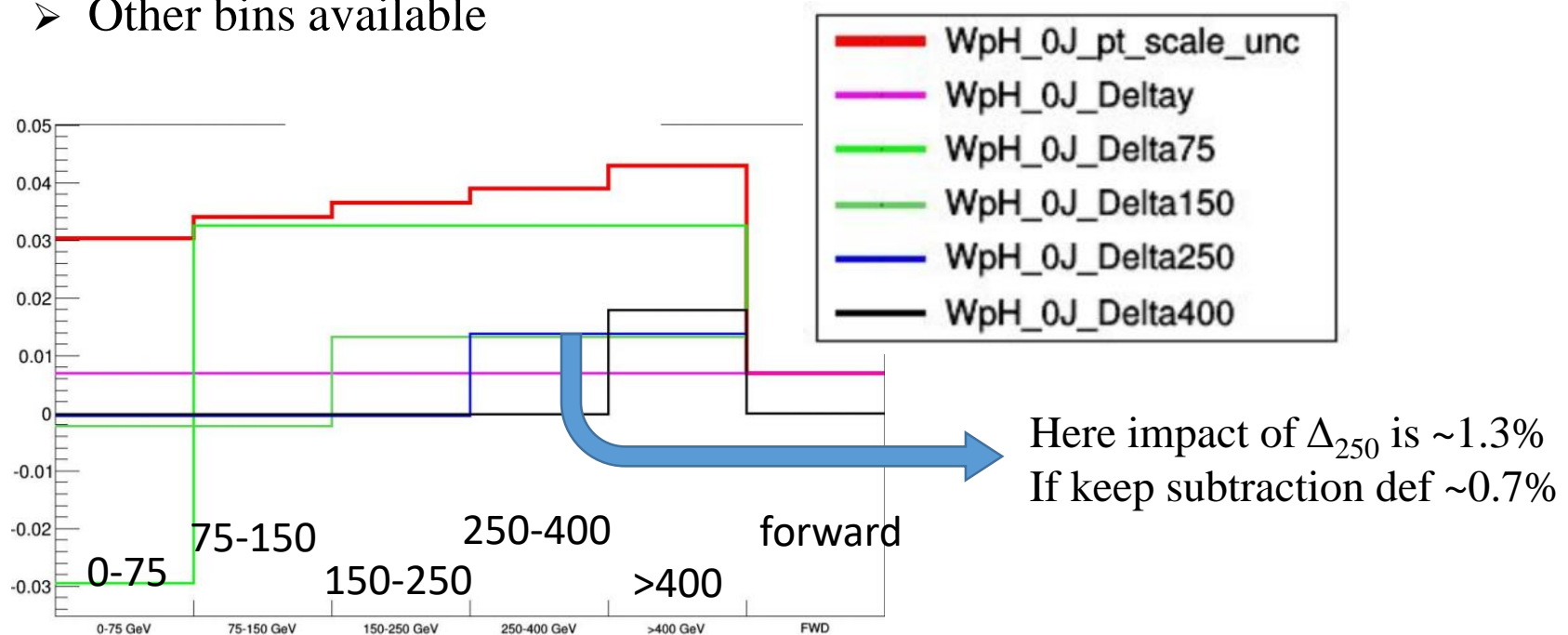


$$\begin{aligned}\Delta &= y_{tot} \cdot \delta \\ \Delta_{75} &= y_{[75,\infty[} \cdot \delta_{[75,\infty[} \\ \Delta_{150} &= y_{[150,\infty[} \cdot (0.5) \cdot \delta_{[150,\infty[} \\ \Delta_{250} &= y_{[250,\infty[} \cdot (0.5) \cdot \delta_{[250,\infty[} \\ \Delta_{150J} &= y_{[150,250[\cup [\geq 1jet]} \\ &\quad \cdot \delta_{[150,250[\cup [\geq 1jet]} \\ \Delta_{250J} &= y_{[250,\infty[\cup [\geq 1jet]} \\ &\quad \cdot \delta_{[250,\infty[\cup [\geq 1jet]}\end{aligned}$$



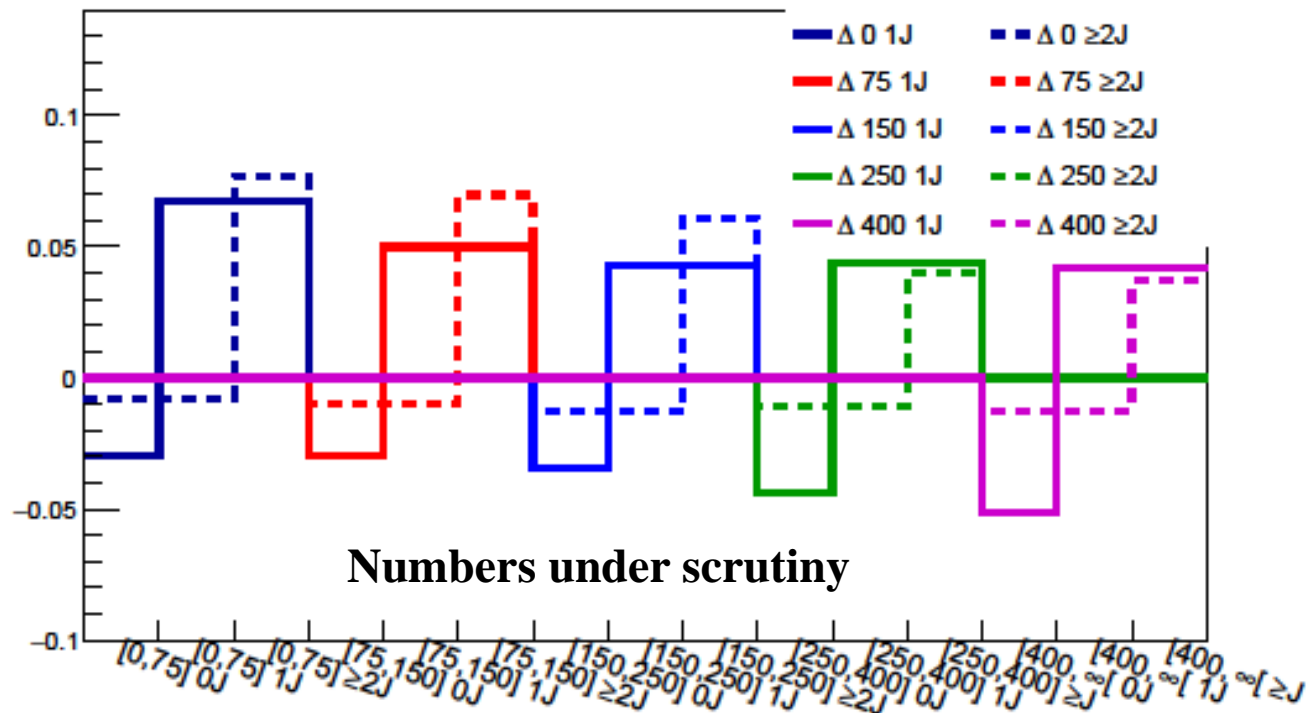
Result for the Δ s

- Frank's proposal: if ill defined use $0.5 \times$ relative variation
 - Applied also to sub-sequent Δ 's
- Impact of Δ 's in the stage1++ bins:
 - Showing here no add jet bin for $qq \rightarrow W^+(\ell\nu)H$
 - Other bins available



Result for the Δ s

- Frank's proposal: if ill defined use $0.5 \times$ relative variation
 - Applied also to sub-subsequent Δ 's
- Impact of Δ 's in the stage1++ bins:
 - Showing here no add jet bin for $qq \rightarrow W^+(\ell\nu)H$
 - Other bins available



2 signal uncertainty sets left to discuss:

~~→ Scale~~

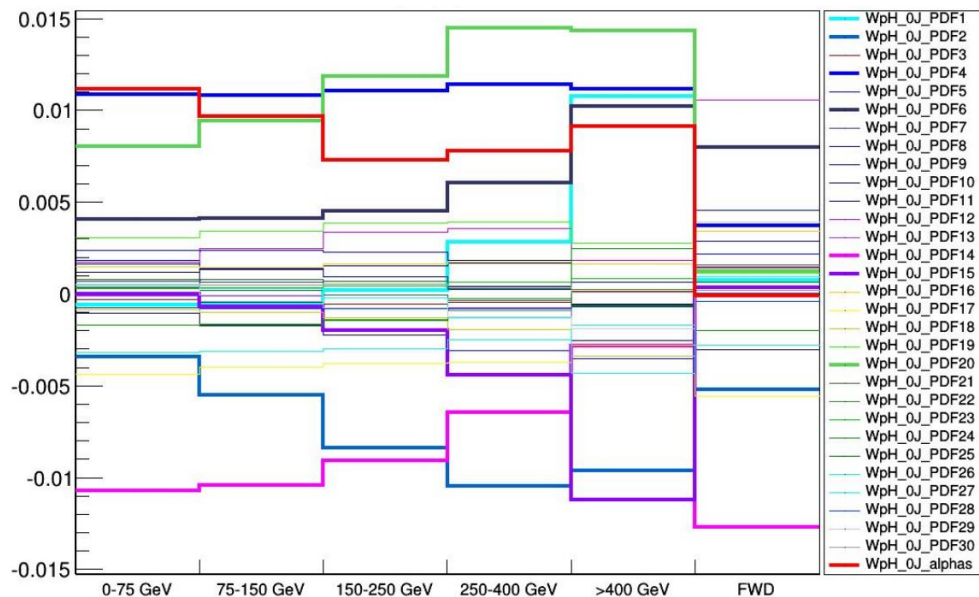
→ PDF

→ PS / UE



PDF uncertainties

- Want to use the relative PDF variation in each stage1++ bin:
 - Use PDF4LHC_nlo_30_pdfas ([click me](#)) set
 - Compute variation w.r.t first weight
 - Use yields per in each bin: $var[i] = \frac{y_{pdf}[i] - y_{pdf}[0]}{y_{pdf}[0]} \quad \forall i \in [1,30]$
- α_s uncertainty as average of up/down relative uncertainties on yields.



Only few variations $> 0.5\%$
→ Can merge small variations
→ Maximum impact 1.5%



1 signal uncertainty set left to discuss:

~~→ Scale~~

~~→ PDF~~

→ PS / UE

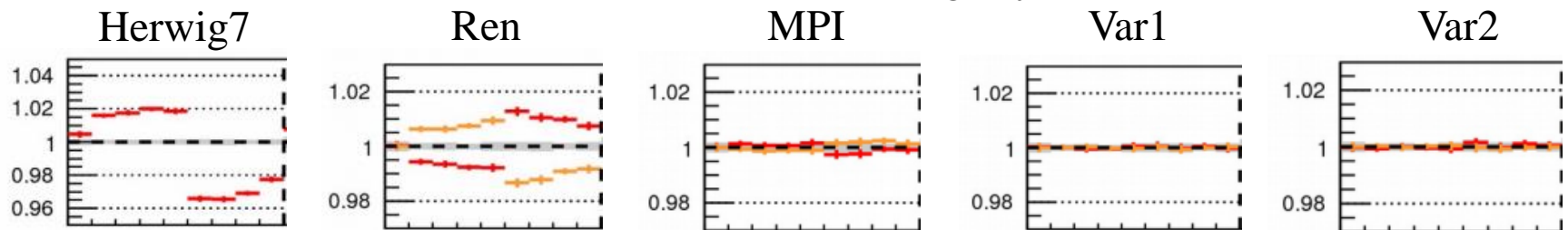


Parton Shower / UE uncertainties

- Important source of uncertainty for EPS:
 - Acceptance uncertainty
- Estimated comparing different samples across STXS bins:
 - Powheg+Pythia8 (nom), Powheg+Herwig7, MPI up/down, Ren up/down, Var1 and Var2 up/down (primordial-kT and ISR-cutoff variations).

$qq \rightarrow W(\ell\nu)H$ sample

Relative variation over Powheg+Pythia8:



Binning: [forward] – [N(add jets)=0]x([0, 75] [75, 150] [150, 250] [250, ∞])
– [N(add jets)≥1]x([0, 75] [75, 150] [150, 250] [250, ∞])

Now talking of only 2-4% effects

→ Main effect on N(jets)

Note: expect bigger impact from shape/acceptance

Conclusion



Conclusion

- First implementation of the stage 1++ scale uncertainties
~ready to go:
 - Calculation based on inclusive bin acceptances (y 's) and their associated relative uncertainties (δ 's)
 - Still some tunable items: “ δ -subtraction” and “ $\delta*0.5$ ”
 - Final uncertainties Δ 's showing ~ 1 to 4% effects
- PDFs/ α_S based on standard approach:
 - Relative uncertainties on yields following recommendations
 - Unc < 1.5% with $p_T(V)$ and $N(\text{jet})$ trends.
- PS/UE uncertainties:
 - Sample differences across the STXS bins
 - $\sim 2/4\%$ with $N(\text{jet slope})$
 - Still stage 1+ (don't expect new conclusions with 1++)



Thank you for your attention

