

# New ideas for Jet Substructure

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DESY

B2G Spring Workshop  
Open Session – May 23, 2018



- **Jet substructure** techniques play a major role in LHC physics  
**Boosted regime** → look at dynamics **inside the jet**
- Different techniques are available:
  - Shapes** constrain **soft gluon radiation**, signal is colorless and has different radiation pattern than QCD jets;  
e.g. Energy correlation, N-subjettiness.
  - Prong Finders** find **hard prongs** in the jets, usually signal has 2 symmetric prongs and QCD background has only 1;  
e.g. Y-splitter.
  - Groomers** clean **soft and large angle radiation**, often dominated by non-perturbative effects  
e.g. modified MassDrop, Soft Drop

# Example : N-subjettiness

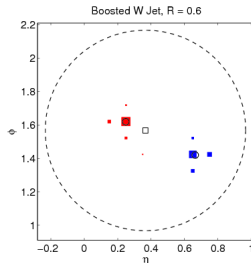
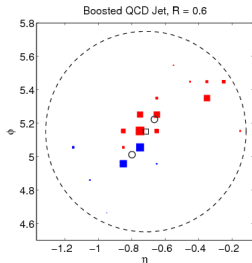
- Measures **radiation around N (pre-determined) axis**

Thaler, Tilburg (2010)

$$\tau_N = \frac{1}{R^\beta} \sum_{i \in \text{jet}} z_i \min(\theta_{ia_1}^\beta, \dots, \theta_{ia_N}^\beta),$$

$$\theta_{ij}^2 = \Delta\phi_{ij}^2 + \Delta y_{ij}^2, \quad z_i = p_{t,i}/p_{t,\text{jet}}$$

- Use the ratios  $\tau_{21} = \tau_2/\tau_1$  or  $\tau_{32} = \tau_3/\tau_2$  to find multi-prong jets



# Example : Energy correlation functions

- Basis of observables used to probe multi-pronged jets

Larkoski, Salam, Thaler (2013)

$$e_2^{(\beta)} = \sum_{1 \leq i < j \leq n_J} z_i z_j \theta_{ij}^\beta$$

$$e_3^{(\beta)} = \sum_{1 \leq i < j < k \leq n_J} z_i z_j z_k \theta_{ij}^\beta \theta_{ik}^\beta \theta_{jk}^\beta$$

- Used to **2-pronged boson discrimination** (like Z/W/H)

$$C_2^{(\beta)} = \frac{e_3^{(\beta)}}{(e_2^{(\beta)})^2}, \quad \text{or} \quad D_2^{(\beta)} = \frac{e_3^{(\beta)}}{(e_2^{(\beta)})^3}$$

- Or **top quark discrimination**

$$C_3^{(\beta)} = \frac{e_4^{(\beta)} e_2^{(\beta)}}{(e_3^{(\beta)})^2}$$

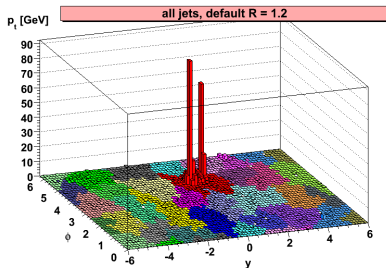
# Example : Soft Drop and modified MassDrop Tagger

- Removes **soft and large-angle radiation**;

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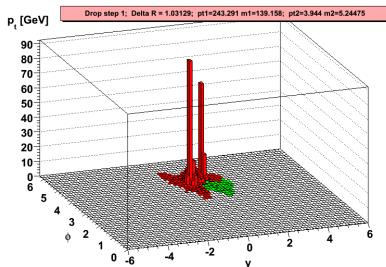
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- 1 Break jet into two  $j \rightarrow j_1 + j_2$ ;  
using C/A algorithm

- 2 Check condition  
$$\frac{\min(p_{T,1}, p_{T,2})}{(p_{T,1} + p_{T,2})} > z_{\text{cut}} \left( \frac{\theta_{12}}{R} \right)^\beta ;$$



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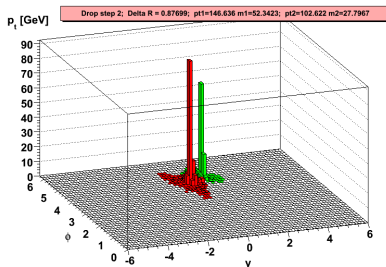
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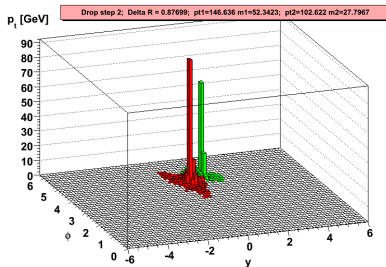
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lower  $p_T$ .
- 4 If passes, stop recursion;

mMDT is equivalent to Soft Drop with  $\beta = 0$







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  - Resummation can achieve higher accuracies
  - Results are systematically improvable
- Compute robust **uncertainty bands**
  - Correct assessment of the higher orders corrections we are neglecting

# Some recent developments

- Development of **new jet substructure tools**
  - Generalizations of energy-correlation functions
  - Dichroic observables
  - Recursive Soft Drop
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- Development of **new jet substructure tools**
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  - Dichroic observables
  - Recursive Soft Drop
  - Observables decorrelated from jet masses
- **Precision calculations** in groomed jet mass
- Studies on **fitting of the strong coupling**
- Advances in machine learning techniques  
See Larkoski, Moult, Nachman (2017) for an overview

# New angles on energy correlation functions

*Moult, Necib, Thaler (2016)*

- Generalization of the energy correlation functions

$$e_n^{(\beta)} = \sum_{1 \leq i_1 < \dots < i_n \leq n_J} z_{i_1} \dots z_{i_n} \prod_{m=1}^v \min_{s < t \in \{i_1 \dots i_n\}}^{(m)} \{\theta_{st}^\beta\}$$

- In particular, defined the series

- $M_i$  : identify jets with hard prongs, effective for groomed jets

$$M_i^{(\beta)} = \frac{1e_{i+1}^{(\beta)}}{1e_i^{(\beta)}}$$

- $N_i$  : mimics the behavior of N-subjettiness, no need for pre-defined axes

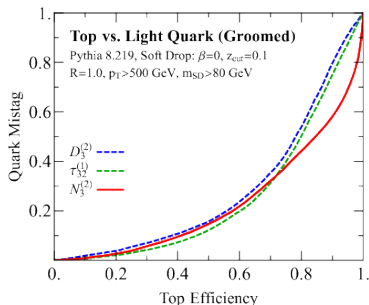
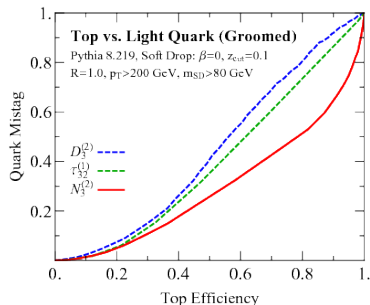
$$N_i^{(\beta)} = \frac{2e_{i+1}^{(\beta)}}{(1e_i^{(\beta)})^2}$$

- $U_i$  : probe multiple emissions within 1-pronged jets

$$U_i^{(\beta)} = 1e_{i+1}^{(\beta)}$$

# Top Tagging $N_3$

- Use the variable  $N_3 = 2e_4^{(\beta)} / (1e^{(\beta)})^2 \sim \tau_3 / \tau_2$  (for groomed jets only)

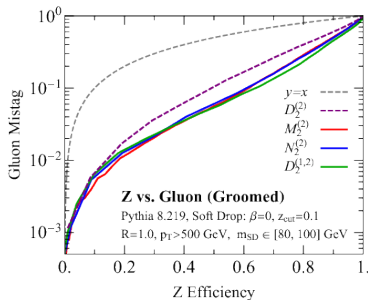
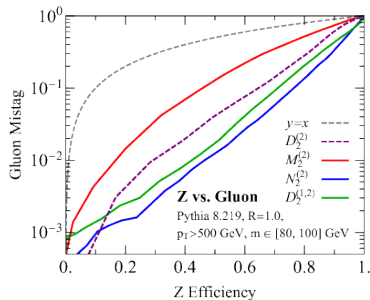


- Improved performance**, specially for higher significance efficiency



## 2-prong tagging : $N_2$ , $M_2$ and $D_2^{(\alpha,\beta)}$

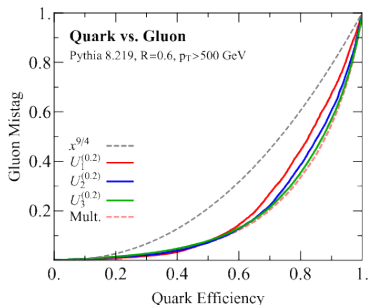
- Observables proposed:  $N_2 = 1e_3^{(\beta)} / 1e_2^{(\beta)}$ ,  $M_2 = 2e_3^{(\beta)} / (1e_2^{(\beta)})^2$  and  $D_2^{(\alpha,\beta)} = 3e_3^{(\alpha)} / (1e_2^{(\beta)})^{\frac{3\alpha}{\beta}}$
- Grooming matters, it can change considerably ROC curves



- These shapes **perform slightly better** than standard  $D_2^{(2)}$   
 (see paper for stability study in MC)

# Quark / gluon discrimination: $U_i$

- Proposed the variable  $U_i = {}_1e_{i+1}^{(\beta)}$
- Case  $U_1 = C_1$  is the standard quark/gluon discrimination variable



- Increasing  $i \rightarrow$  **increases performance** (but the effect saturates)

*Salam, LS, Soyez (2016)*

- Explore the interplay between **groomers / prong finders** and **jet shapes**;
- Example : N-subjetiness  
Usual  $\tau_{21}$  measures

$$\tau_{21} = \frac{\tau_2(\text{mMDT})}{\tau_1(\text{mMDT})} \quad \text{or} \quad \frac{\tau_2(\text{SD})}{\tau_1(\text{SD})} \quad \text{or} \quad \frac{\tau_2(\text{plain})}{\tau_1(\text{plain})}$$

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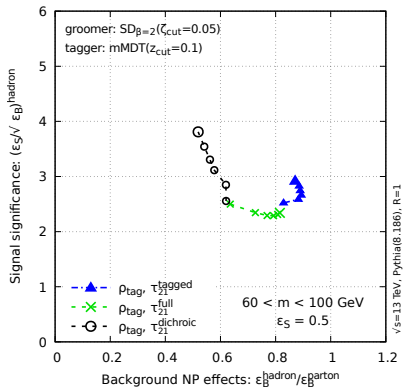
- **Dichroic** : different subjects for numerator / denominator in  $\tau_{21}$  ratios;

$$\tau_{21}^{\text{dichroic}} \equiv \frac{\tau_2^{\text{full / SD}}}{\tau_1^{\text{tagged}}}$$

- $\tau_2$  on large jet  $\rightarrow$  sensitivity to different color structures
- $\tau_1$  on small jet  $\rightarrow$  only sensitive to the invariant mass  
 $\rightarrow$  smaller influence of non-perturbative effects.

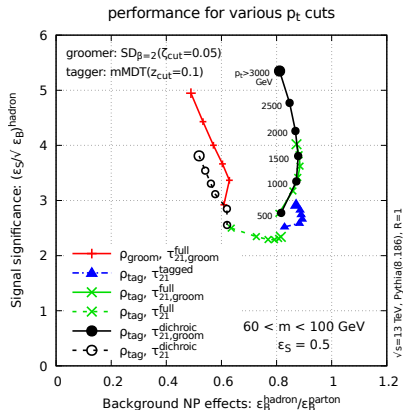
# Dichroic Jet Shapes

performance for various  $p_t$  cuts



- Dichroic  $\tau_{21}$  variation  
→ **increases discriminating power**

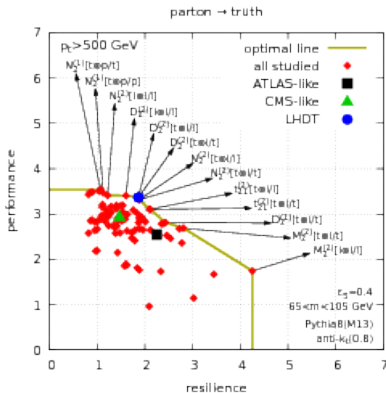
# Dichroic Jet Shapes



- Dichroic  $\tau_{21}$  variation  
→ **increases discriminating power**
- With pre-grooming step  
→ **reduction of NP effects** and still has a **better performance**
- Performance gain increases as  $p_t$  increases

# Dichroic Jet Shapes

- Comparison between a variety of jet shapes  
Les Houches 2017 SM Working Group



- Dichroic version of observables show **good performance** with relatively **low sensitivity to non-perturbative effects**

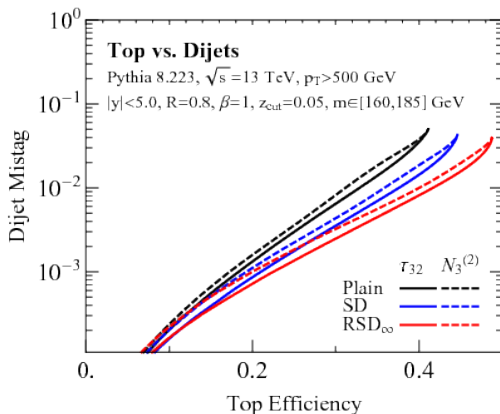
*Dreyer, Necib, Soyez, Thaler (2018)*

- Generalized version of Soft Drop algorithm
- Recursive Soft Drop algorithm:
  - 1 Uncluster the jet into 2 subjets  $j \rightarrow j_1 + j_2$
  - 2 Check the Soft Drop condition  $\frac{\min(p_{t1}, p_{t2})}{p_{t1} + p_{t2}} > z_{\text{cut}} \Delta R_{12}^\beta$
  - 3 Keep both subjets if condition is met, eliminate softer subjet if it is not
  - 4 **Iterate process until SD condition is met N times**, or until all particles are recursed through
- For  $N = 1$ , we recover the original Soft Drop



# Recursive Soft Drop

- Example : boosted top tagging
- Increases mass resolution and **improves tagging performance** (when combined to others jet shapes)

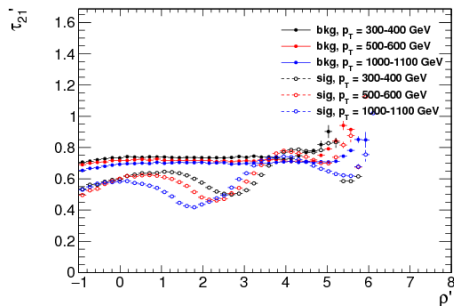


# DDT : Designing Decorrelated Taggers

*Dolen, Harris, Marzani, Rappocio, Tran (2016)*

- Observables are modified to **reduce mass correlations**  
→ practical advantages for the experimental measures
- Redefine the following quantities:

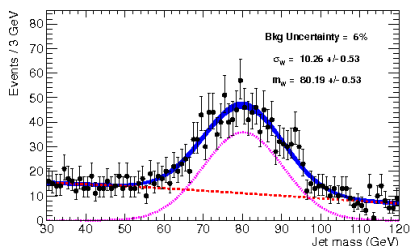
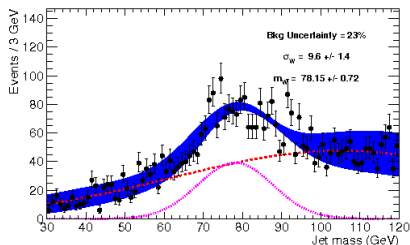
$$\rho = \log\left(\frac{m^2}{p_t^2}\right) \rightarrow \rho' = \log\left(\frac{m^2}{p_t \mu}\right), \quad \tau_{21} = \frac{\tau_2}{\tau_1} \rightarrow \tau'_{21} = \frac{\tau_2}{\tau_1} - M * \rho'$$



# Case study : Diboson background estimate

- Both selections with same background efficiency

Blue band is the background + signal fit



Cuts are  $\tau_{21} < 0.45$  in left and  $\tau'_{21} < 0.6$  in right

- We see a considerable **reduction of uncertainty bands**

*Moult, Nachman, Neil (2017)*

- Convolved SubStructure approach : use **theoretical knowledge** over observables to decorralate them and the jet mass
- Can be seen as a generalized systematical approach to DDT
- Derivate a function  $F_{CSS}$  (see systematical derivation in the paper)

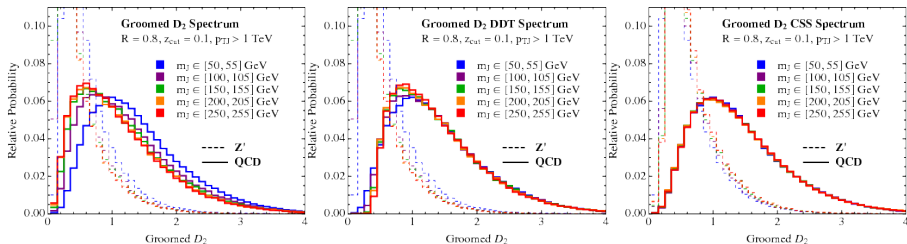
$$\frac{d\sigma^{CSS}}{dD_2} = \int_0^\infty F_{CSS}(\epsilon) \frac{d\sigma}{dD_2}(D_2 - \epsilon)$$

- $F_{CSS}$  contains both perturbative and non-perturbative information

$$F_{CSS} = F_{NP}^{-1} \otimes F_P \otimes F_{NP}$$

# Case study : $Z' \rightarrow q\bar{q}$

- $D_2$  groomed distribution for signal jets (dashed) and QCD background



- QCD background becomes decorrelated from jet mass

- Connection between measurements and calculations
- **Jet mass** is one of the simplest observables
- **Grooming** eliminates part of UE contamination
- We studied modified MassDrop Tagger and SoftDrop

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- For **boosted jets**  $p_T \gg m \rightarrow \rho \equiv m/(p_T R) \ll 1$   
 $\rightarrow$  log enhancements  $\alpha_s^n \log^{2n}(1/\rho)$

**Needs to be resummed at all orders**

- Various interesting QCD structures emerging
  - For mMDT it becomes  $[\alpha_s f(z_{\text{cut}}) \log(1/\rho)]^n$  at leading-log
  - Finite  $z_{\text{cut}}$  introduce a flavour changing matrix structure
- Compare with experiment  $\rightarrow$  needs a matching procedure:

$$\underbrace{N^k LL}_{\text{small } \rho} + \underbrace{N^m LO}_{\text{large } \rho}$$

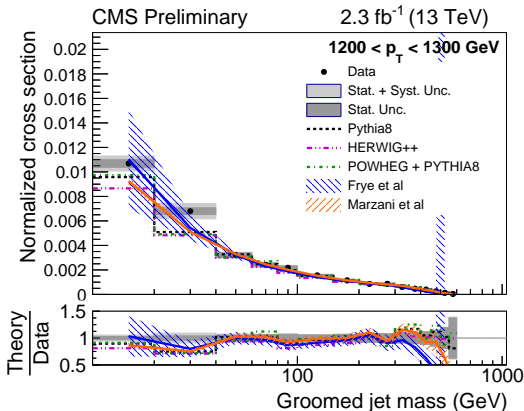
Small  $\rho \rightarrow$  **resummation** of large logarithms

Large  $\rho \rightarrow$  **fixed-order** (exact at  $\mathcal{O}(\alpha_s^m)$ )

- Calculations done with different theoretical approaches
  - NLL + LO for  $z_{\text{cut}} \ll 1$  *Frye, Larkoski, Schwartz, Yan (2016)*
  - LL + NLO for all  $z_{\text{cut}}$  *Marzani, Soyez, LS (2017)*
  - Inclusive jets version *Kang, Lee, Liu, Ringer (2018)*

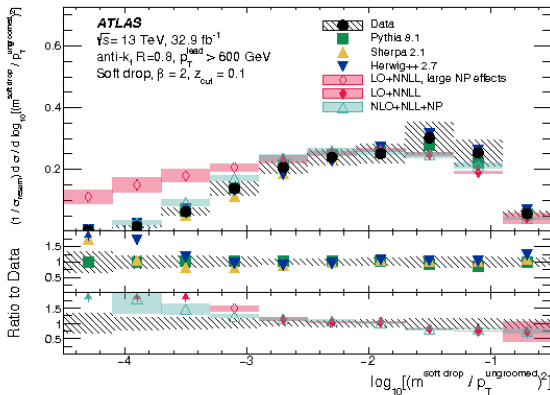


- Comparison with CMS measurements using mMDT



CMS-PAS-SMP-16-010

- Comparison with ATLAS measurements using SoftDrop ( $\beta > 0$ )



CERN-EP-2017-231

# Fitting of strong coupling

## *Les Houches 2017 SM Working Group*

- Possibility of using jet observables at the LHC to do a  $\alpha_s$  fitting
- Use of **grooming techniques** to remove undesired NP effects
- **Developments in jet shapes calculations** (now up to NNLL)
- Recent feasibility study using groomed jet mass as an example
  - With currently achievable theoretical and experimental uncertainties a  $\alpha_s$  extraction at 10% level is realistic
  - Optimistic about how developments on both sides can improve this precision

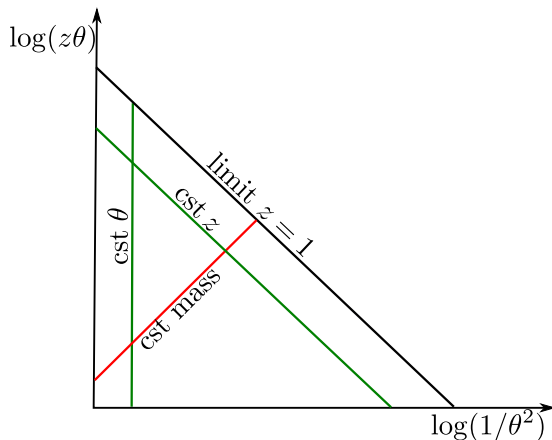
See also : use of groomed tools to improve  $\alpha_s$  fitting obtained with  $e^+e^-$  collisions  
Baron, Marzani, Theeuwes (2018), or Theeuwes's Talk at SCET18

- Jet substructure domain has a very active community, both in experiment and theory
- Analytical studies:
  - ① Better insight of existing tools
  - ② Development of new tools
  - ③ Higher accuracy results
  - ④ Robust uncertainty bands
- Increasing role as LHC reaches higher energy scales

# Backup slides

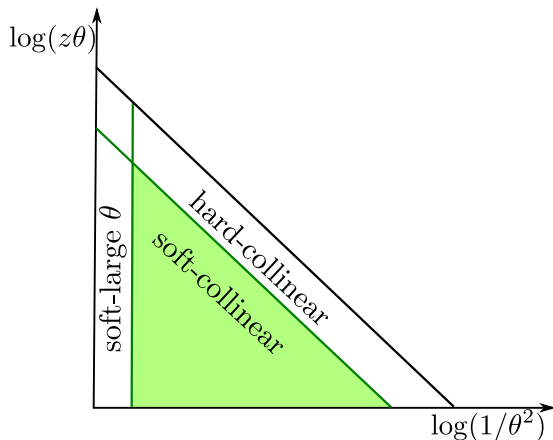
# Lund diagrams

- Lund diagram : graphical representation of the results in  $z\theta$  (transverse momentum) vs.  $1/\theta^2$  (emission angle) coordinates.

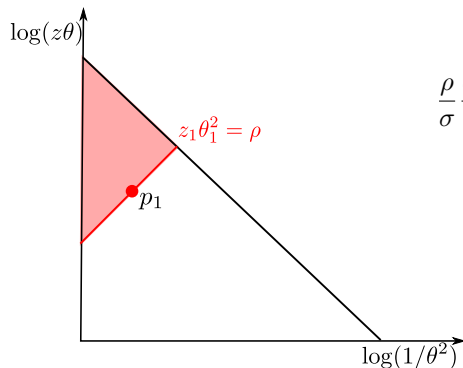


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# Calculations

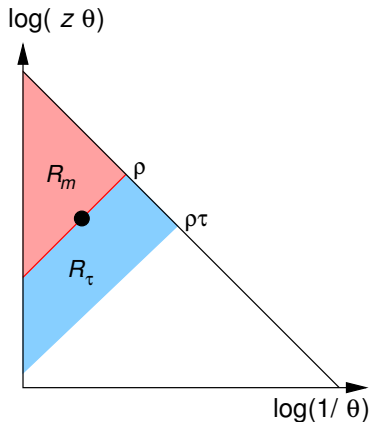


$$\frac{\rho}{\sigma} \frac{d\sigma}{d\rho} \sim \frac{C_F \alpha_s}{2\pi} R'_{\text{plain}}(\rho) \exp(-R_{\text{plain}}(\rho))$$

$$R_{\text{plain}}(\rho) \sim \frac{C_F \alpha_s}{2\pi} \int_0^1 \log(1/\rho)^2$$



# Lund diagram for $\tau_{21}$

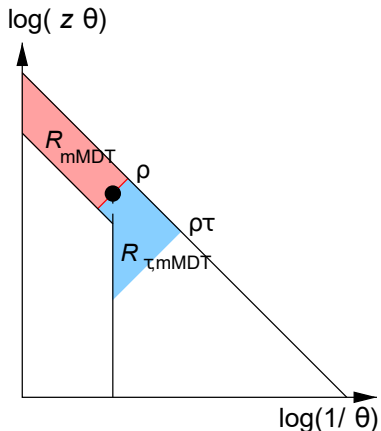


- Jet mass with cut on  $\tau_{21}$

$$\left. \frac{\rho d\sigma}{\sigma d\rho} \right|_{<v} = R'_m \exp(-R_{m+\tau})$$

	$R'_m$	$R_{m+\tau}$	NP
full	large	large	large

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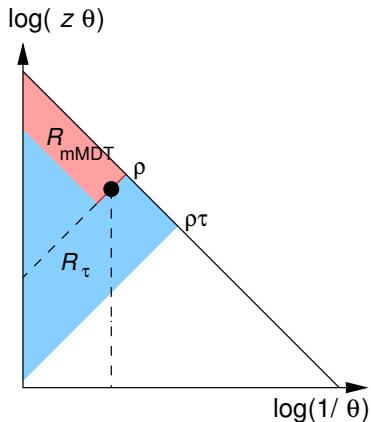


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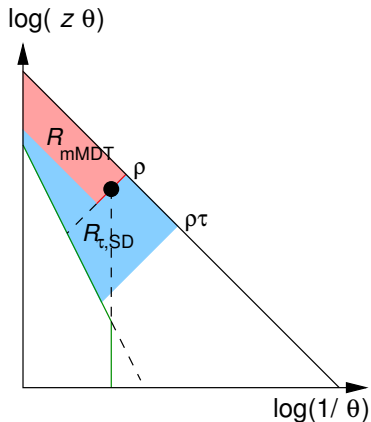


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dichroic	small	large	large

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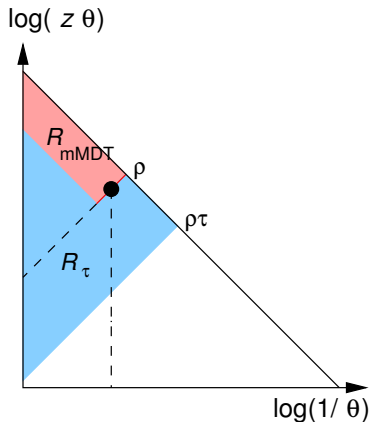


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dichroic + SD	small	large	small

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mMDT/SD	small	small	small
dichroic	small	large	large
dichroic + SD	small	large	small

$$\left. \frac{\rho}{\sigma} \frac{d\sigma}{d\rho} \right|_{\tau_{21}^{\text{dichroic}}}^{\text{LL}} \stackrel{\text{f.c.}}{=} \frac{C_F \alpha_s}{\pi} \log \frac{1}{y} \times \exp \left[ -\frac{C_F \alpha_s}{2\pi} \log^2 \frac{1}{\tau \rho} \right]$$