

# Trilinear Higgs self-coupling extraction from single Higgs measurements

Stefano Di Vita (INFN Milano)

Double Higgs Production at Colliders Workshop @ Fermilab/LPC

Sep 4, 2018

Based on

- Grojean, Panico, Riembau, Vantalón, DV [1704.01953]
- Durieux, Grojean, Gu, Liu, Panico, Riembau, Vantalón, DV [1711.03978]



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# Outline

- Testing BSM deformations with Higgs physics
- Higgs trilinear self-coupling at the HL-LHC
- Prospects at the HE-LHC and future  $e^+e^-$  colliders

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# Still missing: Higgs self-couplings

See talk by B.Di Micco

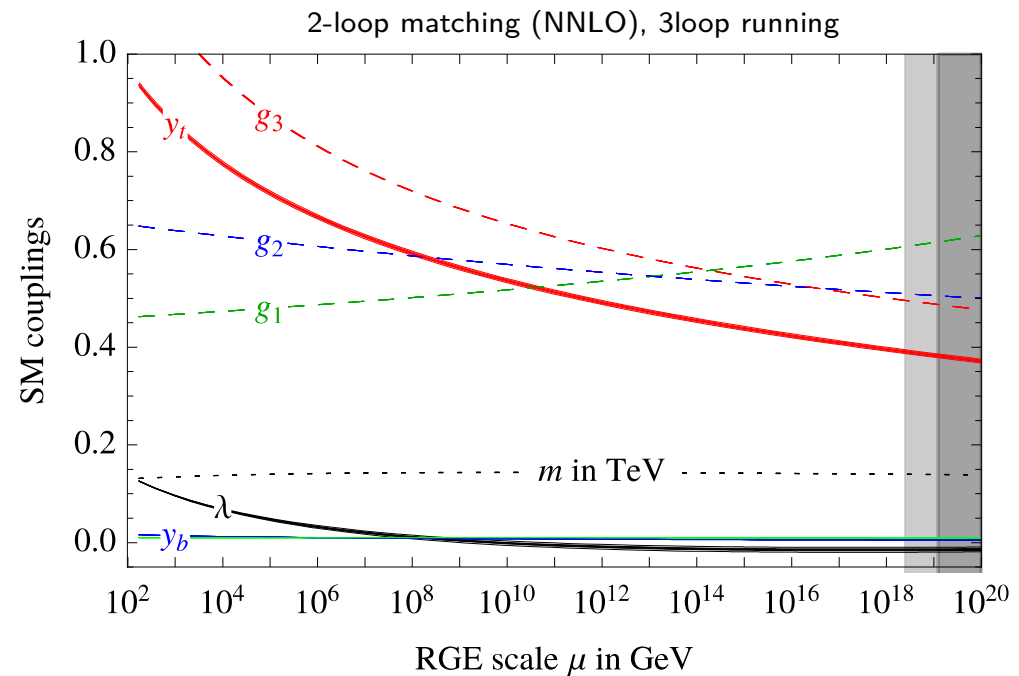
$$\left. \begin{aligned}
 V^{\text{SM}}(H^\dagger H) &= -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2 \\
 v &= \sqrt{-\mu^2/\lambda} \\
 m_h^2 &= 2\lambda v^2
 \end{aligned} \right\} \Rightarrow$$

$$\begin{aligned}
 V^{\text{SM}}(h) &= \frac{1}{2} m_h^2 h^2 + \lambda_3^{\text{SM}} v h^3 + \lambda_4^{\text{SM}} h^4 \\
 \lambda_3^{\text{SM}} &= \frac{m_h^2}{2v^2} & \lambda_4^{\text{SM}} &= \frac{m_h^2}{8v^2}
 \end{aligned}$$

(at tree level)

- SM (classical)
    - $(\lambda_3, \lambda_4) \Leftrightarrow (m_h, v) \rightarrow$  **verify it!**
  - SM (quantum)
    - $\lambda$  controls **vacuum stability** (together with  $y_t, \alpha_s$ )
    - $\lambda(\mu) = f(G_F, m_Z, m_W, m_h, m_t, \alpha_s, \dots)$
- @NNLO in the SM**

[Degrassi et al '12, Buttazzo et al '13, Bednyakov et al '15]



Within the SM, all couplings remain perturbative up to  $M_{\text{Pl}}$

# Still missing: Higgs self-couplings

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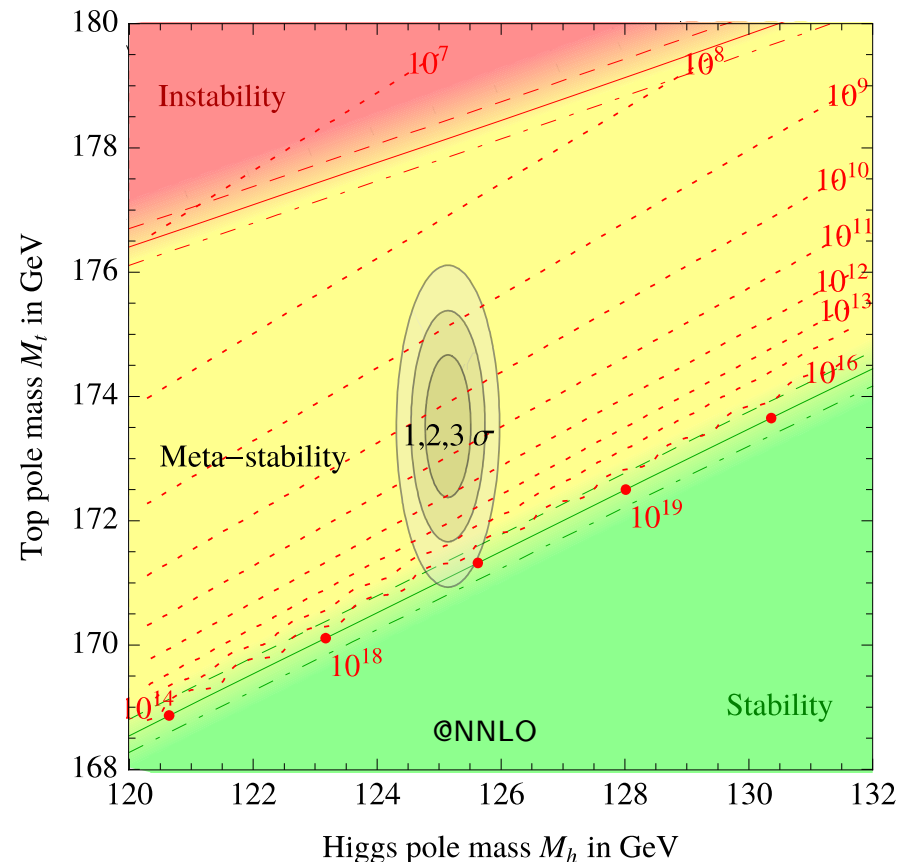
$$V^{\text{SM}}(H^\dagger H) = -\mu^2 H^\dagger H + \lambda (H^\dagger H)^2 \quad \left. \begin{array}{l} v = \sqrt{-\mu^2/\lambda} \\ m_h^2 = 2\lambda v^2 \end{array} \right\} \Rightarrow$$

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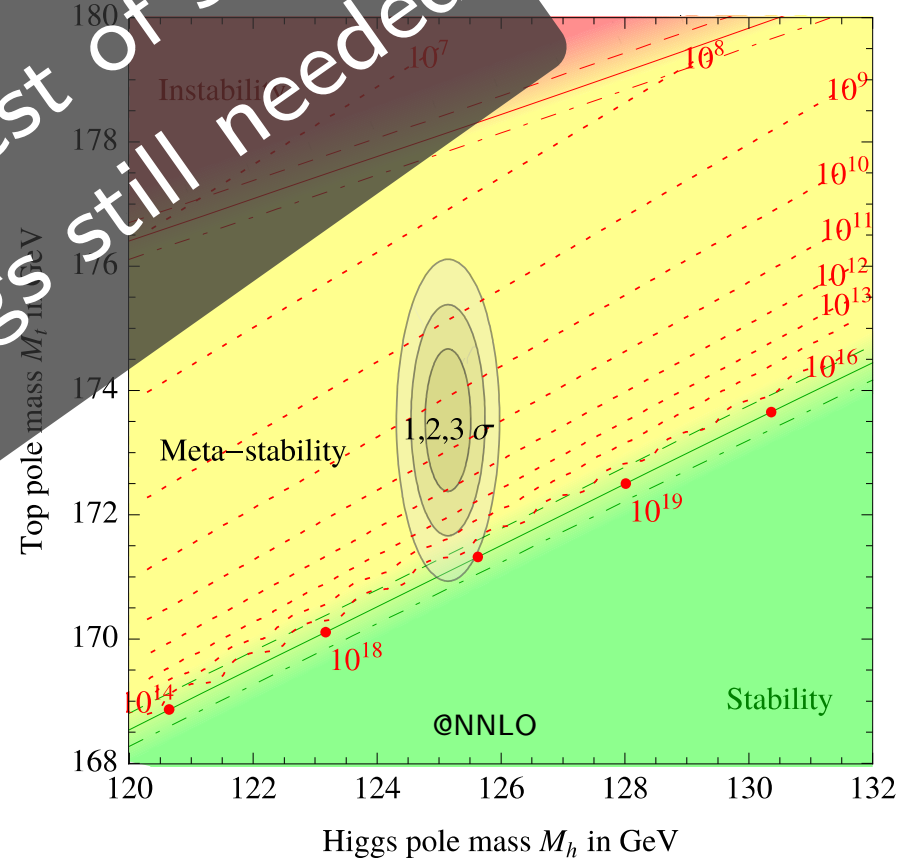
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**@NNLO in the SM**

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Direct test of self-couplings still needed



# Higgs self-couplings are interesting!

- Non-standard  $\lambda_3$  and  $\lambda_4$  affect physics in several ways
  - **hh** and **hhh** production @ **LO**
  - **h** and **hh** production @ **NLO** (EW)
  - EWPO (no h!) and **h** production @ **NNLO** (EW)

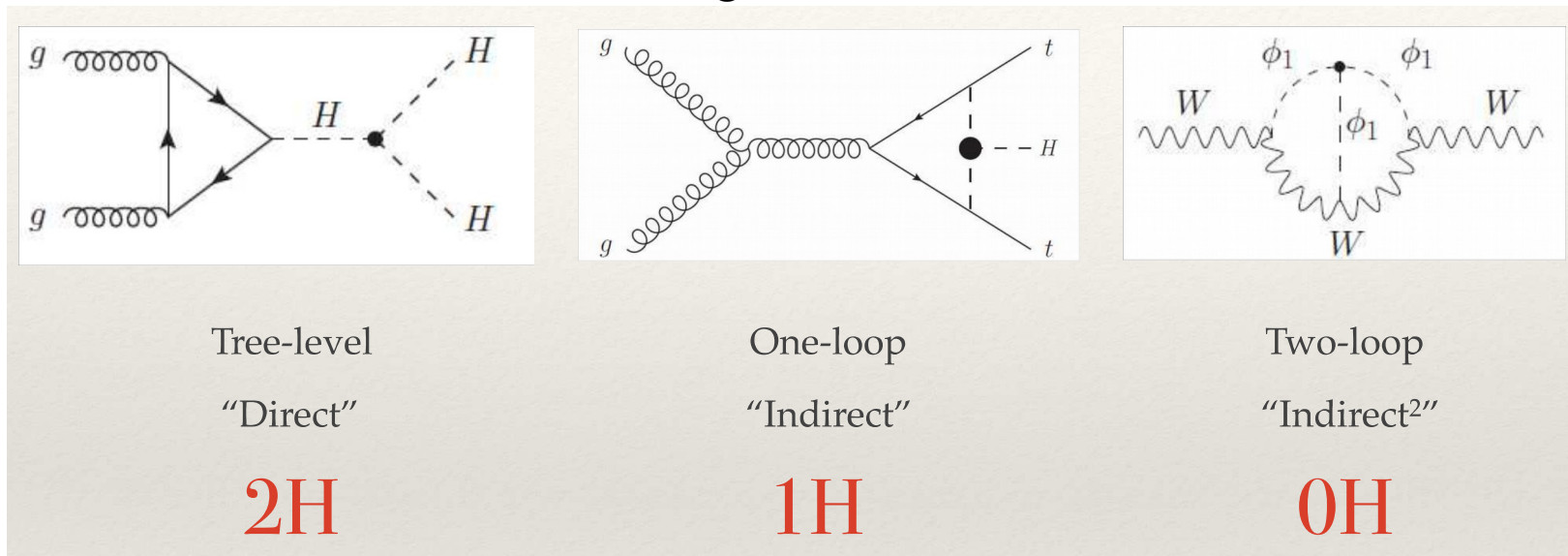
EFT ref's

Azatov et al '15  
Goertz et al '15  
Cao et al '15

McCullough '13;  
Gorbahn,Haisch '14 (+Bizon,Zanderighi '16);  
Degrassi,Giardino,Maltoni,Pagani '14

van der Bij '86;  
Degrassi,Fedele,Giardino '17;  
Kribs,Maier,Rzehak,Spannowsky,Waite '17

e.g. trilinear



from Fabio Maltoni's talk at the LHCHSWG General meeting, July 2017 @ CERN



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- Current constraints on  $\sigma_{hh}^{(SM)}$  are quite loose  $\rightarrow$  still room for BSM!
- Probe  $V(h)$  to get information on the dynamics of EW phase transition
- Interesting consequences for cosmology, e.g.
  - EW baryogenesis *see e.g. Huang, Joglekar, Li, Wagner 16; Carena, Liu, Wagner 18*
  - Primordial gravitational waves *see e.g. Huang, Long, Wang 16; Hashino, Kakizaki, Kanemura, Ko, Matsui 16*

# How to approach the self-coupling?

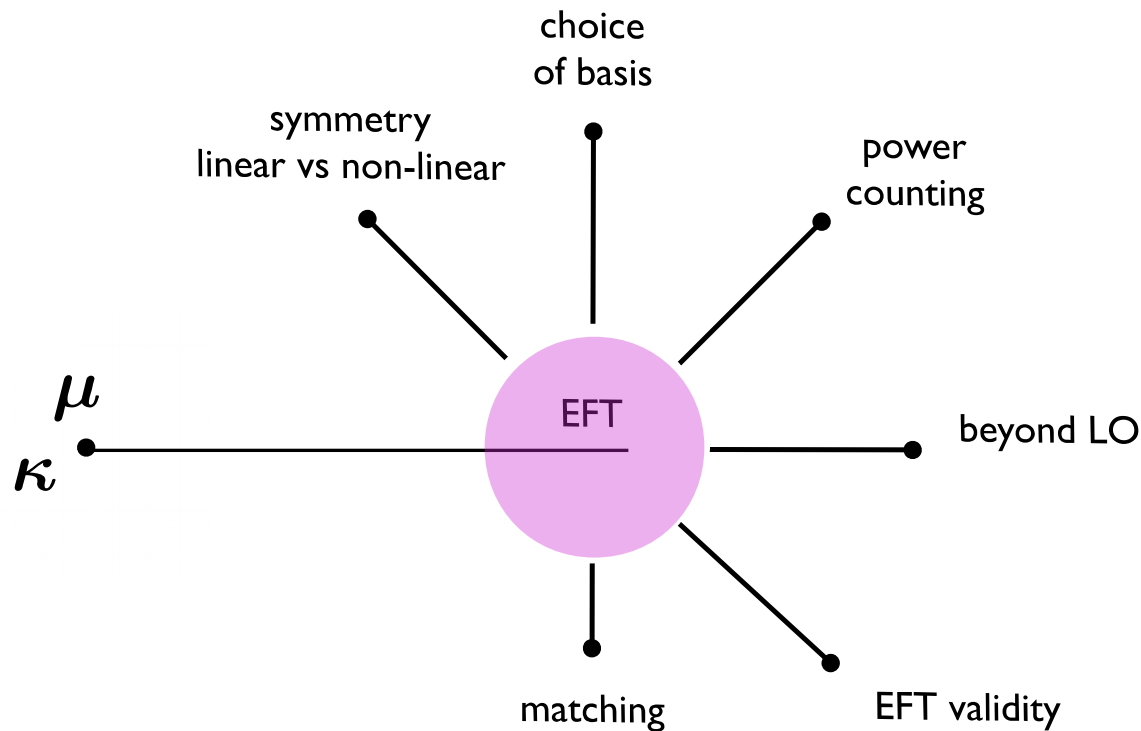
- $hVV$  &  $h\psi\psi$  tested at  $\sim 10\%$ : is it theoretically sound to **deform only  $\lambda_3$** ?
- **How large** can  $\lambda_3$  be, from the theoretical point of view?
- If  $\lambda_3$  is large, does it **spoil** the previous **single-Higgs fits**?
- Is the **bound** on  $\lambda_3$  **stable** if we allow other BSM deformations?
- Will it be **enough** to look at **inclusive rates**?
- Can we really avoid performing **global fits** for BSM?
- Can we “replace”  $pp \rightarrow hh$  with **single-Higgs observables** for  $\lambda_3$ ?



# Beyond the $\kappa$ -framework: EFT

Scale “ $\Lambda$ ” of new physics » typical energy of the process “ $E$ ”  $\Rightarrow$  EFT

Grojean @ Jeju '17



## Pros:

- ▶ correlations between different channels/observables
- ▶ combination of measurements at different energies  
e.g. EW precision data and Higgs measurements
- ▶ test of self-consistency



**unique to EFT**  
allow to focus on channels yet unconstrained and more likely to offer new discovery opportunities

# My working assumptions

- Linearly realized EW symmetry (h belongs to Higgs doublet)  $\Rightarrow$  SMEFT
- Keep operators  $O_i$  up to dimension-6
- Operators tested in processes w/o Higgs assumed to be constrained
- Work in the **Higgs basis**  $\Rightarrow$  trilinear interaction  $\lambda_3 = \kappa_\lambda \lambda_{SM} = (1 + \delta \kappa_\lambda) \lambda_{SM}$
- Further simplifying assumptions (just to limit # of  $O_i$ )
  - no CP, L, B-L, violating  $O_i$
  - no dipole  $O_i$
  - flavor universality
  - no  $\psi^4$  ( $t^4, ttqq, q^4$ )

$$\mathcal{L} \supset \boxed{\mathcal{L}_{SM}} + \cancel{\mathcal{L}_{d=5}} + \boxed{\mathcal{L}_{d=6}} + \cancel{\mathcal{L}_{d=7}} + \cancel{\mathcal{L}_{d=8}} + \dots$$


L violating
B-L violating
subleading wrt d=6

Focus on 10  $O_i$  relevant at the LHC (not just SM tensor structures! EFT  $\neq$  k-framework)  
 $\Rightarrow$  10 independent deformations of hGG, h $\psi\psi$ , hWW, hZZ, h $\gamma\gamma$ , hZ $\gamma$ , hhGG, hh $\psi\psi$ , hhh

# Higgs deformations in the Higgs basis

Pomarol '14; +Gupta,Riva '14; Falkowski '15; HXSWG YR4

$$\begin{aligned}
 \mathcal{L} \supset & \frac{h}{v} \left[ \delta c_w \frac{g^2 v^2}{2} W_\mu^+ W^{-\mu} + \delta c_z \frac{(g^2 + g'^2) v^2}{4} Z_\mu Z^\mu \right. \\
 & + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\Box} g^2 (W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.}) + \hat{c}_{\gamma\gamma} \frac{e^2}{4\pi^2} A_{\mu\nu} A^{\mu\nu} \\
 & \left. + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z^{\mu\nu} + \hat{c}_{z\gamma} \frac{e \sqrt{g^2 + g'^2}}{2\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\Box} g^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A^{\mu\nu} \right] \\
 & + \frac{g_s^2}{48\pi^2} \left( \hat{c}_{gg} \frac{h}{v} + \hat{c}_{gg}^{(2)} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu} - \sum_f \left[ m_f \left( \delta y_f \frac{h}{v} + \delta y_f^{(2)} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\
 & - (\kappa_\lambda - 1) \lambda_3^{SM} v h^3
 \end{aligned}$$


  
 $f=t,b,\tau (+ c,\mu)$

parametrize space of d=6 operators in a way more directly connected to observable quantities in Higgs physics

SM tensor structures

“SM” tensor structures

“New” tensor structures

10 Independent couplings

8 Dependent couplings

# Triple gauge couplings – Higgs interplay

Butter et al '16, Falkowski et al '16

$$\begin{aligned}
 \mathcal{L}_{\text{tgc}} = & ig s_{\theta_W} A^\mu (W^{-\nu} W_{\mu\nu}^+ - W^{+\nu} W_{\mu\nu}^-) \\
 & + ig (1 + \delta g_1^Z) c_{\theta_W} Z^\mu (W^{-\nu} W_{\mu\nu}^+ - W^{+\nu} W_{\mu\nu}^-) \\
 & + ig [(1 + \delta \kappa_Z) c_{\theta_W} Z^{\mu\nu} + (1 + \delta \kappa_\gamma) s_{\theta_W} A^{\mu\nu}] W_\mu^- W_\nu^+ \\
 & + \frac{ig}{m_W^2} (\lambda_Z c_{\theta_W} Z^{\mu\nu} + \lambda_\gamma s_{\theta_W} A^{\mu\nu}) W_\nu^{-\rho} W_{\rho\mu}^+,
 \end{aligned}$$

1 extra indep

WW $\gamma$  and WWZ data can constrain single-Higgs couplings

$$\begin{aligned}
 \delta g_{1,z} &= \frac{1}{2(g^2 - g'^2)} [c_{\gamma\gamma} e^2 g'^2 + c_{z\gamma} (g^2 - g'^2) g'^2 - c_{zz} (g^2 + g'^2) g'^2 - c_{z\Box} (g^2 + g'^2) g^2] \\
 \delta \kappa_\gamma &= -\frac{g^2}{2} \left( c_{\gamma\gamma} \frac{e^2}{g^2 + g'^2} + c_{z\gamma} \frac{g^2 - g'^2}{g^2 + g'^2} - c_{zz} \right),
 \end{aligned}$$

# Only large anomalous $\lambda_3$ ? Not really...

Remark: up to NLO, single-Higgs observables are **insensitive to  $h^4, h^5, \dots$**

- They enter only at higher loop level
- Modifications of the full  $V(h)$  could still be allowed, in principle
- At NLO,  $\kappa_\lambda$  framework = EFT w/  $O_6$

Modification of  **$h^3$  only** leads to loss perturbative unitarity at low energy scales in processes like

$$V^L V^L \rightarrow V^L V^L h^n$$

- for  $|\kappa_\lambda| < 10$  one gets  $\Lambda \sim 5\text{TeV}$

[Falkowski, Rattazzi (to appear)]

- see also Di Luzio, Gröber, Spannowsky [1704.02311]

Are there **classes** of BSM models that, in an EFT description:

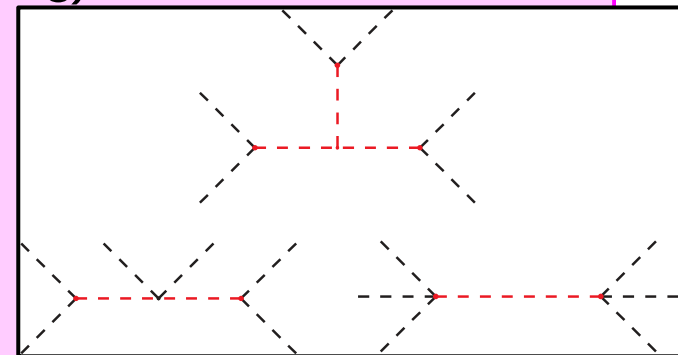
- **Either deform just Higgs self-interactions (tree-level matching)**

- e.g.  $SU(2)$  scalar quadruplets (not quite a “class”)
- still, 1-loop matching  $\rightarrow$  other single-Higgs couplings!

- **Or enhance  $\delta\kappa_\lambda$  wrt the single-Higgs couplings?**

- e.g. **tuned Higgs Portal** can get  $\delta\kappa_\lambda \sim 6$  vs other couplings  $O(0.1)$

- See also De Blas et al [1412.8480], Jiang, Trott [1612.02040], Di Luzio, Gröber, Spannowsky [1704.02311]



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Not in generic BSM scenarios

See also talk by I.Low



# Large $\lambda_3$ in tuned Higgs Portal

1 dimensionless parameter

1 coupling

1 scale

singlet

potential

dimensionless argument

$$\mathcal{L} \supset \theta g_* m_* H^\dagger H \varphi - \frac{m_*^4}{g_*^2} V(g_* \varphi / m_*)$$

Linear EFT valid if  
(expansion in  $h/v$ )

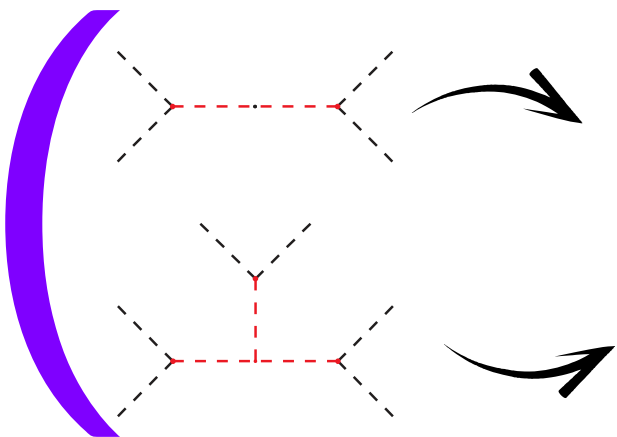
$$\varepsilon \equiv \frac{\theta g_*^2 v^2}{m_*^2} \ll 1$$

Otherwise only derivative expansion is allowed, many more couplings!!

parametrically large  $\lambda_3$   
(paying some tuning)

$$\theta \simeq 1, \quad g_* \simeq 3, \quad m_* \simeq 2.5 \text{ TeV}$$

$$\varepsilon \simeq 0.1, \quad 1/\Delta \simeq 1.5\%, \quad \delta c_z \simeq 0.1, \quad \delta \kappa_\lambda \simeq 6$$



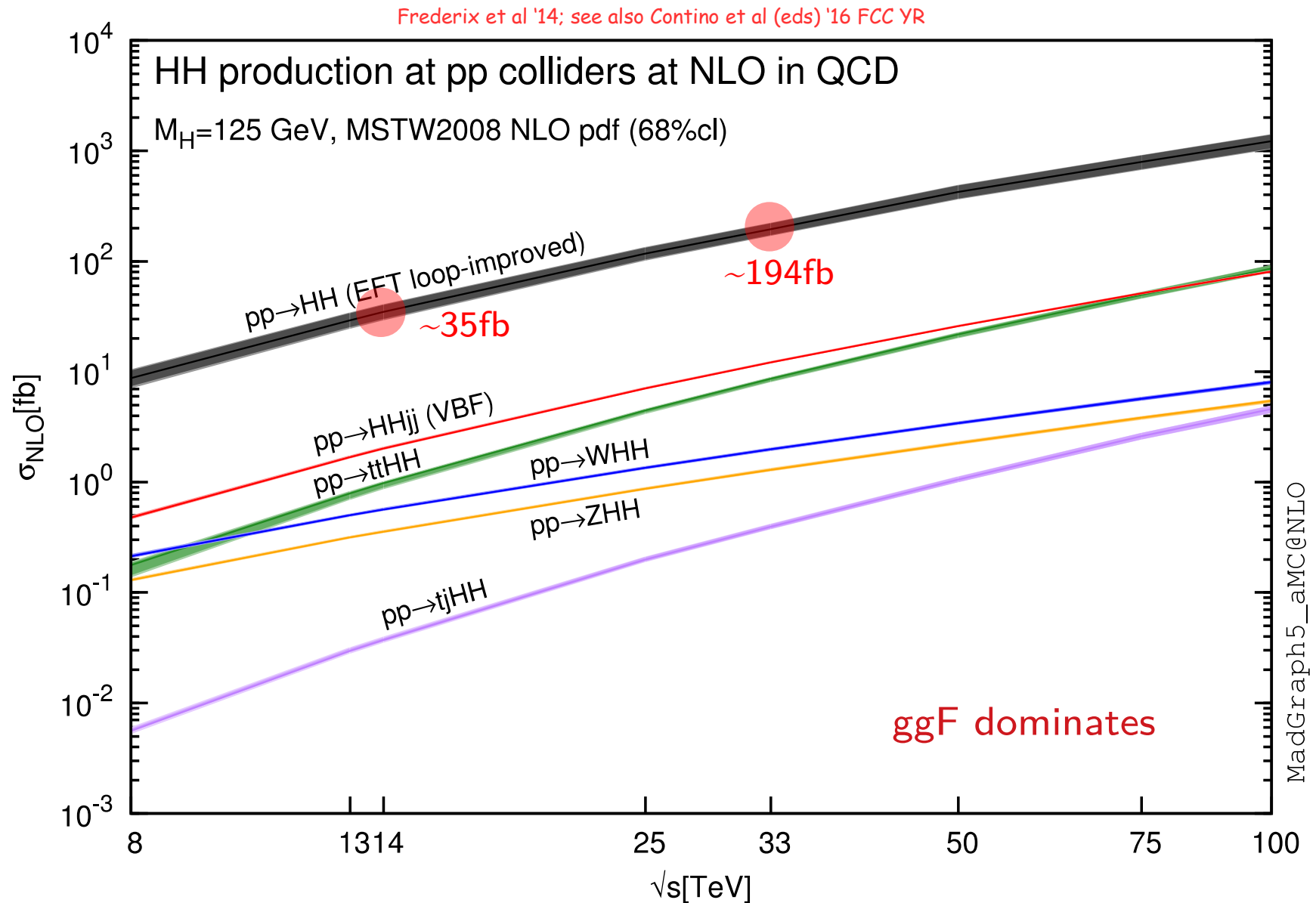
$$\left( \begin{array}{l} (H^\dagger H)^2 \quad \Rightarrow \text{tuning of quartic } \Delta \sim \frac{\theta^2 g_*^2}{\lambda_3^{\text{SM}}} \\ \partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H) \quad \Rightarrow \delta c_z \sim \theta^2 g_*^2 \frac{v^2}{m_*^2} = \theta \varepsilon \\ (H^\dagger H)^3 \quad \Rightarrow \delta \kappa_\lambda \sim \theta^3 g_*^4 \frac{1}{\lambda_3^{\text{SM}}} \frac{v^2}{m_*^2} = \varepsilon \Delta \end{array} \right)$$

DV, Grojean, Panico, Riemann, Vantalon [1704.01953]

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- Testing BSM deformations with Higgs physics
- **Higgs trilinear self-coupling at the HL-LHC**
- Prospects at the HE-LHC and future  $e^+e^-$  colliders

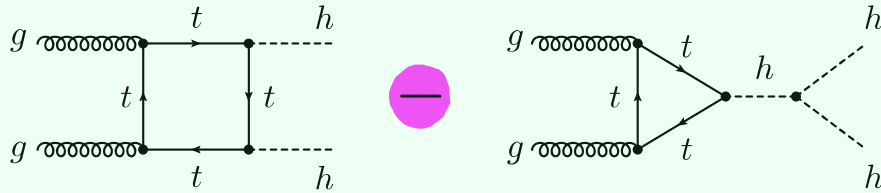
# Obviously: double-Higgs production



# Double-Higgs deformation(s) [ggF]

U. Haisch@MoriondEW2017

## Anatomy of hh production



$$R = \frac{\sigma(pp \rightarrow hh)}{\sigma(pp \rightarrow hh)_{\text{SM}}} = 2.1 - 10.8\lambda + 17.2\lambda^2$$

$$R = 1 \implies \lambda_{1,2} = \{\lambda_{\text{SM}}, 3.8\lambda_{\text{SM}}\}$$

## Limits on $\lambda$ from hh production

LHC Run I, 20.3 fb<sup>-1</sup>  $\longrightarrow$   $\frac{\lambda}{\lambda_{\text{SM}}} \in [-14.5, 19.1]$   
2y2b, 1406.5053;  
 4b, 1506.00285;  
 2b2t, 2y2W, 1509.04670

LHC Run II, 13.3 fb<sup>-1</sup>  $\longrightarrow$   $\frac{\lambda}{\lambda_{\text{SM}}} \in [-8.4, 13.4]$   
4b, ATLAS-CONF-2016-049

HL-LHC, 3 ab<sup>-1</sup>  $\longrightarrow$   $\frac{\lambda}{\lambda_{\text{SM}}} \in [-0.8, 7.7]$   
2y2b, ATL-PHYS-PUB-2017-001

1-param

$$\lambda = \kappa_\lambda \lambda_3^{\text{SM}}$$

EFT dim-6

$$\begin{aligned} \frac{\sigma(pp \rightarrow hh)}{\sigma_{\text{SM}}(pp \rightarrow hh)} = & A_1 (1 + \delta y_t)^4 + A_2 (\delta y_t^{(2)})^2 + A_3 \kappa_\lambda^2 (1 + \delta y_t)^2 + A_4 \kappa_\lambda^2 \hat{c}_{gg}^2 \\ & + A_5 (\hat{c}_{gg}^{(2)})^2 + A_6 (1 + \delta y_t)^2 \delta y_t^{(2)} + A_7 \kappa_\lambda (1 + \delta y_t)^3 \\ & + A_8 \kappa_\lambda (1 + \delta y_t) \delta y_t^{(2)} + A_9 \kappa_\lambda \hat{c}_{gg} \delta y_t^{(2)} + A_{10} \hat{c}_{gg}^{(2)} \delta y_t^{(2)} \\ & + A_{11} \kappa_\lambda \hat{c}_{gg} (1 + \delta y_t)^2 + A_{12} \hat{c}_{gg}^{(2)} (1 + \delta y_t)^2 + A_{13} \kappa_\lambda^2 \hat{c}_{gg} (1 + \delta y_t) \\ & + A_{14} \kappa_\lambda \hat{c}_{gg}^{(2)} (1 + \delta y_t) + A_{15} \kappa_\lambda \hat{c}_{gg} \hat{c}_{gg}^{(2)} \end{aligned}$$

Azatov et al '15

Goertz et al '15

Cao et al '15

# Self-coupling & single-Higgs @NLO

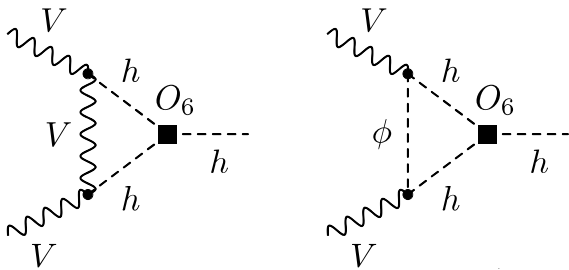
Idea: trilinear coupling affects also single-Higgs rates, but @NLO. Still, if  $\lambda_3$  is large ...

McCullough '13

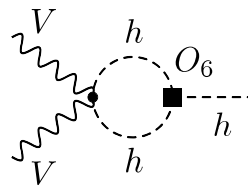
$$\sigma_{Zh} = \left| \begin{array}{c} e \\ \uparrow \\ \text{---} \\ \uparrow \\ e \end{array} \right. \left. \begin{array}{c} Z \\ \uparrow \\ \text{---} \\ \uparrow \\ h \end{array} \right| + 2 \operatorname{Re} \left[ \begin{array}{c} \text{---} \\ \uparrow \\ Z \\ \uparrow \\ \text{---} \\ \uparrow \\ h \end{array} \cdot \left( \begin{array}{c} e^+ \\ \uparrow \\ \text{---} \\ \uparrow \\ e^- \end{array} \right) + \begin{array}{c} e^+ \\ \uparrow \\ \text{---} \\ \uparrow \\ e^- \end{array} \right]$$

$$\delta_\sigma^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

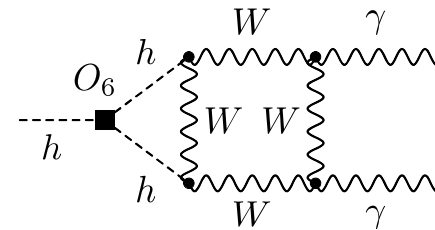
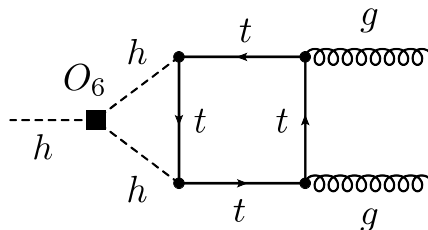
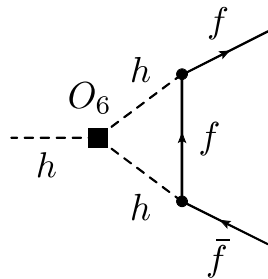
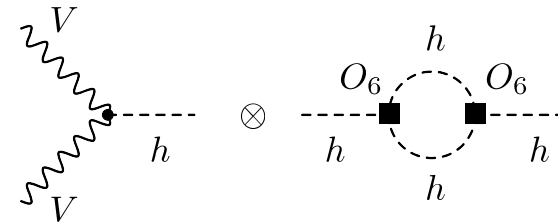
Gorbahn, Haisch '16



Degrassi, Giardino, Maltoni, Pagani '16



Bizon, Gorbahn, Haisch, Zanderighi '16



# Single-Higgs at the HL-LHC

End of LHC Run 3  $\rightarrow 300 \text{ fb}^{-1} @ 14 \text{ TeV}$



End of HL-LHC  $\rightarrow 3000 \text{ fb}^{-1} @ 14 \text{ TeV}$



Process	Combination	Theory	Experimental
$H \rightarrow \gamma\gamma$	ggF	0.07	0.05
	VBF	0.22	0.16
	$t\bar{t}H$	0.17	0.12
	WH	0.19	0.08
	ZH	0.28	0.07
$H \rightarrow ZZ$	ggF	0.06	0.05
	VBF	0.17	0.10
	$t\bar{t}H$	0.20	0.12
	ZH	0.21	0.08
$H \rightarrow WW$	ggF	0.07	0.05
	VBF	0.15	0.12
$H \rightarrow Z\gamma$	incl.	0.30	0.13
$H \rightarrow b\bar{b}$	WH	0.37	0.09
	ZH	0.14	0.05
$H \rightarrow \tau^+\tau^-$	VBF	0.19	0.12

- Good sensitivity on 16 channels, O(5-10-20)%
- Estimated relative uncertainties on signal strengths  $\mu$ , with pile-up 140 events/bunch crossing
- Large luminosity allows for good statistics in bins of differential measurements  $\rightarrow$  exploit!

ATL-PHYS-PUB-2014-016 + ATL-PHYS-PUB-2016-008 + ggF N<sup>3</sup>LO uncertainty+ VH (H $\rightarrow$ ZZ) split in WH,ZH

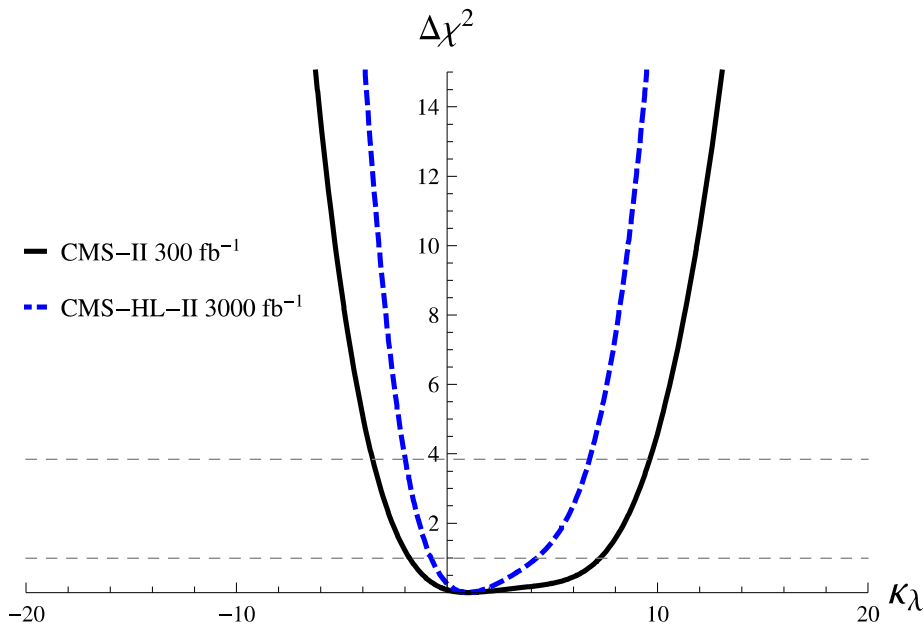
# Only an anomalous $\lambda_3 = \kappa_\lambda \lambda_{SM}$

Use only indirect constraint from single-Higgs

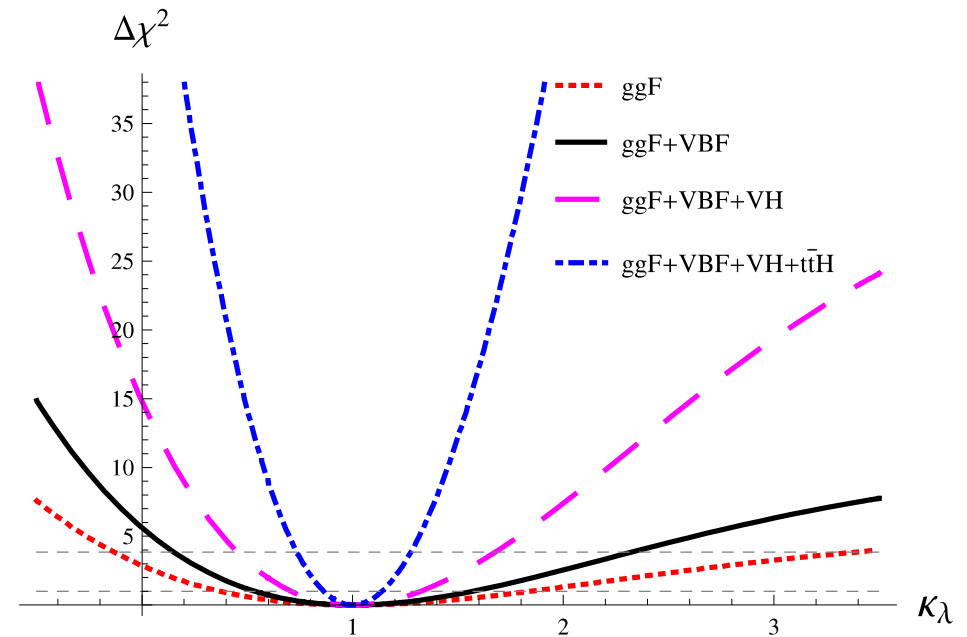
[first sensitivity study by Degraasi et al '16]

Optimistic CMS projections for HL-LHC

Exercise: assume 1% combined th/exp uncert



$$\kappa_\lambda^{1\sigma} \in [-0.7, 4.2] \quad \kappa_\lambda^{2\sigma} \in [-2.0, 6.8]$$



$$\kappa_\lambda^{1\sigma} \in [0.86, 1.14] \quad \kappa_\lambda^{2\sigma} \in [0.74, 1.28]$$

↻ a bit worse than ATLAS HL-LHC HH projection (less optimistic assumptions)

$$\kappa_\lambda^{2\sigma} \in [-0.8, 7.7]$$

# A global view on the Higgs self-coupling

Grojean, Panico, Riembau, Vantalon, DV [1704.01953]

**HL-LHC** prospects on  $\delta\kappa_\lambda$  with ATLAS projections ( $\sim$  CMS “Scenario 1”)  
14TeV, 3/ab, pile-up  $\mu=140$

ATL-PHYS-PUB-2014-016 + ATL-PHYS-PUB-2016-008 + ggF N<sup>3</sup>LO uncertainty HXSWG YR4 + VH (H $\rightarrow$ ZZ) split in WH,ZH

Keep only interference SM-BSM  
Allow for NLO corrections due to  $\kappa_\lambda$   
With my assumptions, **10 parameters**  
Perform  $\chi^2$  fit with SM signal ( $\mu_i^f=1$ )

**Signal strength** measurements  
 $\mu_i^f = \sigma_i \times BR^f / (\sigma_i \times BR^f)_{SM} \sim 1 + \delta\sigma_i + \delta BR^f$   
Production channels: ggF, WH, ZH, VBF, ttH  
Decay modes:  $\gamma\gamma, WW, ZZ, bb, \tau\tau$

A fit of the “usual” inclusive rates is insensitive to simultaneous global shift

$$\sigma_i \rightarrow \sigma_i + \Delta \quad \& \quad BR^f \rightarrow BR^f - \Delta$$

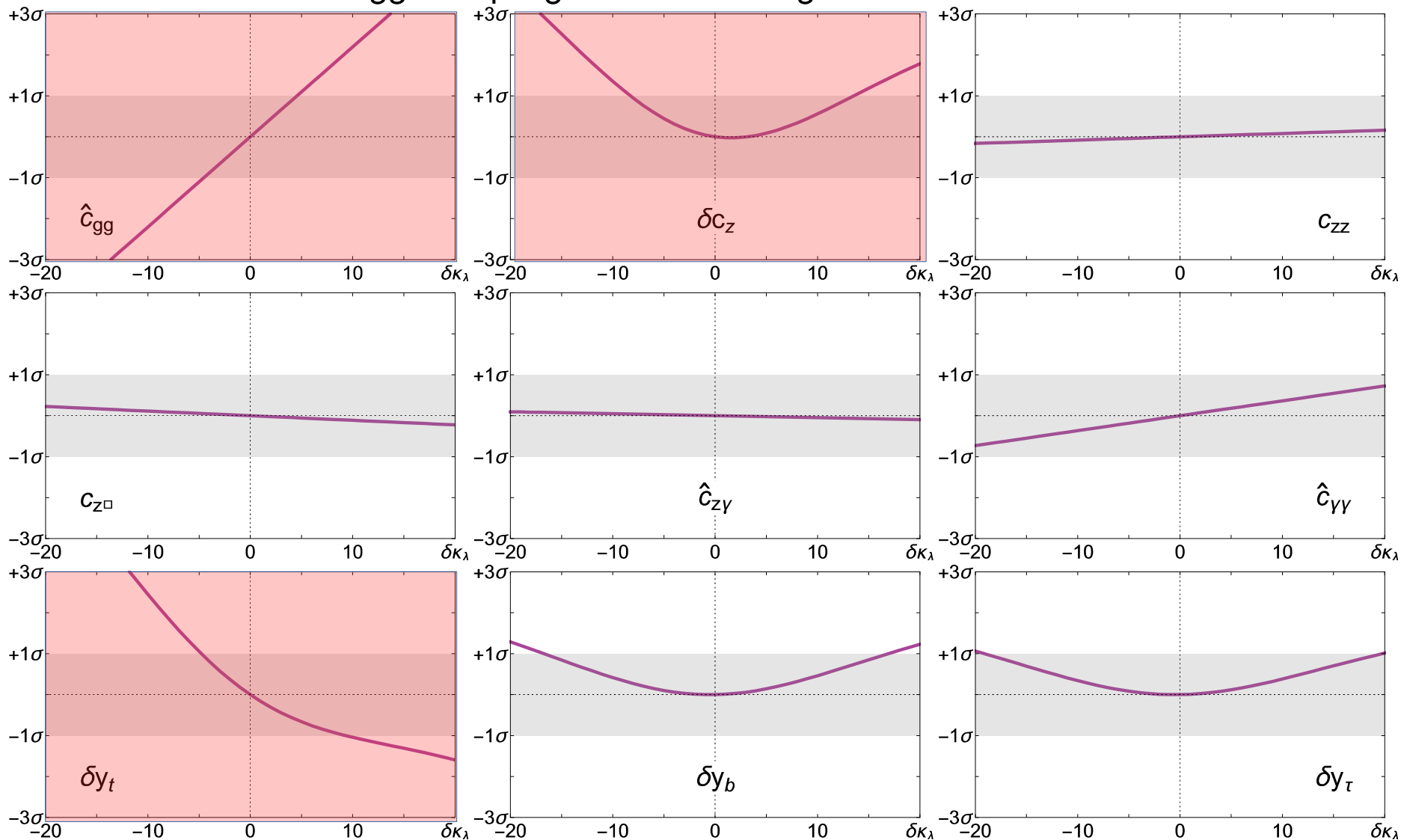
In principle have  $5 \times 5 = 25$  observables, in fact only 9 directions are independent  
 $\Rightarrow$  **we expect 1 exact flat direction in a 10 parameters fit**

Sorry: including Triple Gauge Couplings constraints,  $BR(h \rightarrow Z\gamma)$ ,  $BR(h \rightarrow \mu\mu)$  does not really help :(  
Also: Higgs width (on-shell vs off-shell) has no impact (moreover EFT interpretation problematic)

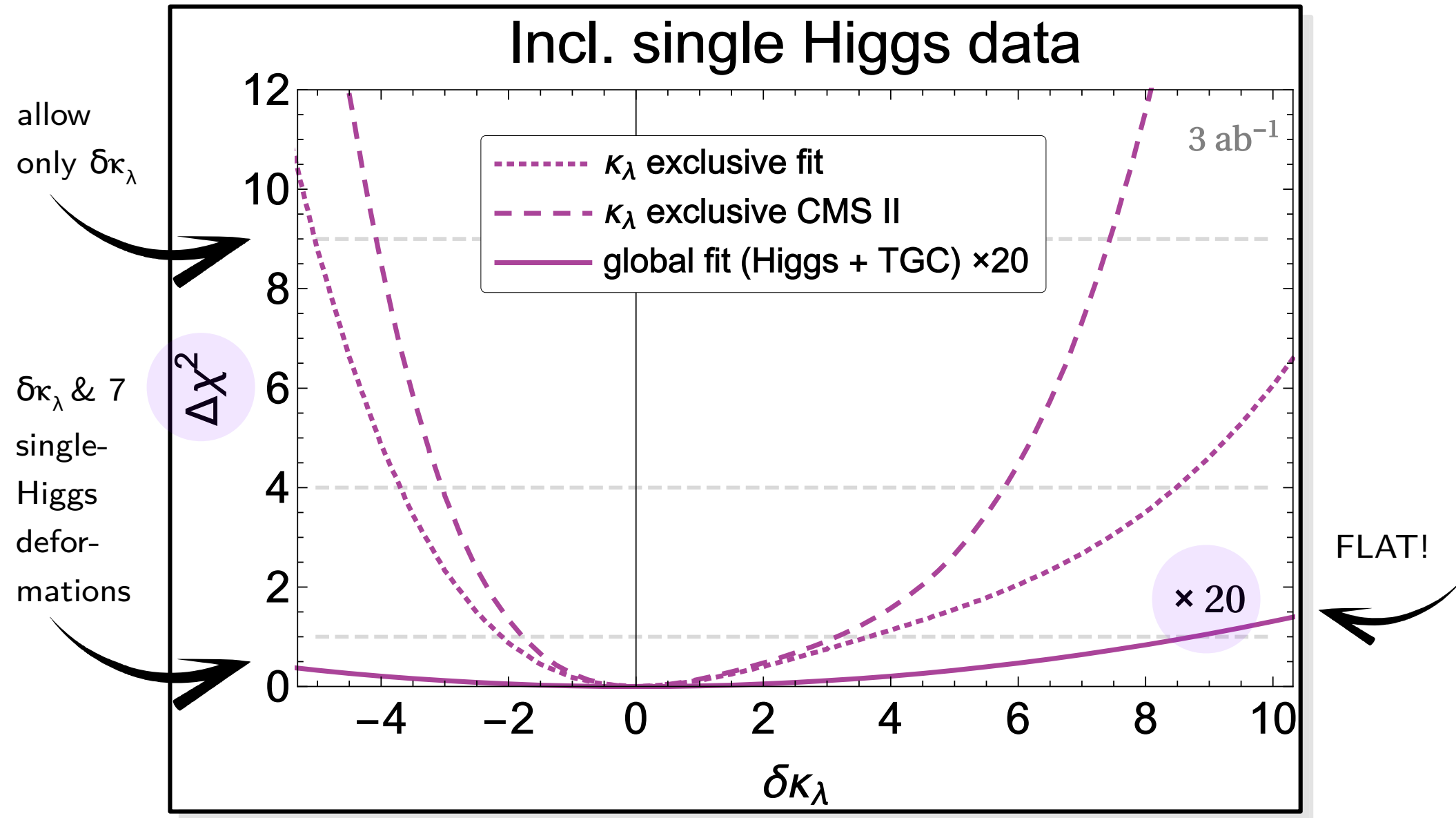


# Exact flat direction in the global fit

Higgs couplings variation along the flat direction



# Bound on $\delta\kappa_\lambda$ from inclusive rates

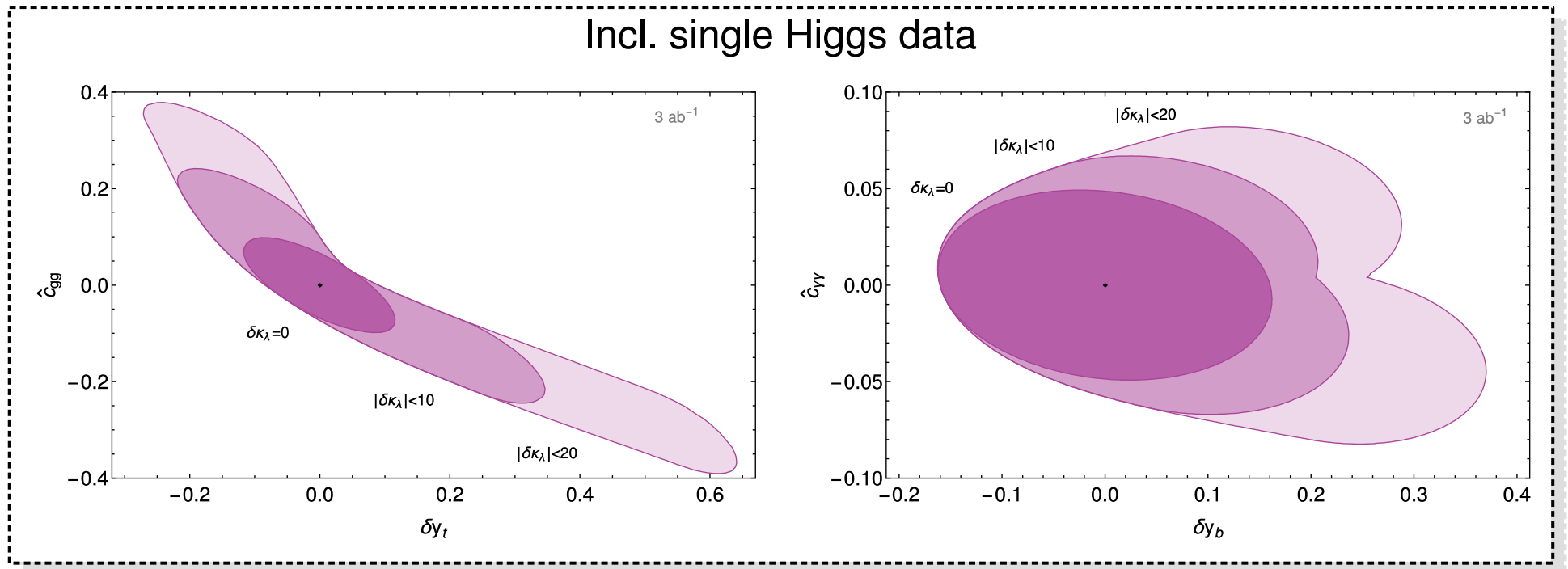


the flat direction is rather insensitive to the TGC constraint

# Single-Higgs couplings fit w/ $\kappa_\lambda$ @NLO

$$(\delta y_t, \hat{c}_{gg})$$

$$(\delta y_b, \hat{c}_{\gamma\gamma})$$

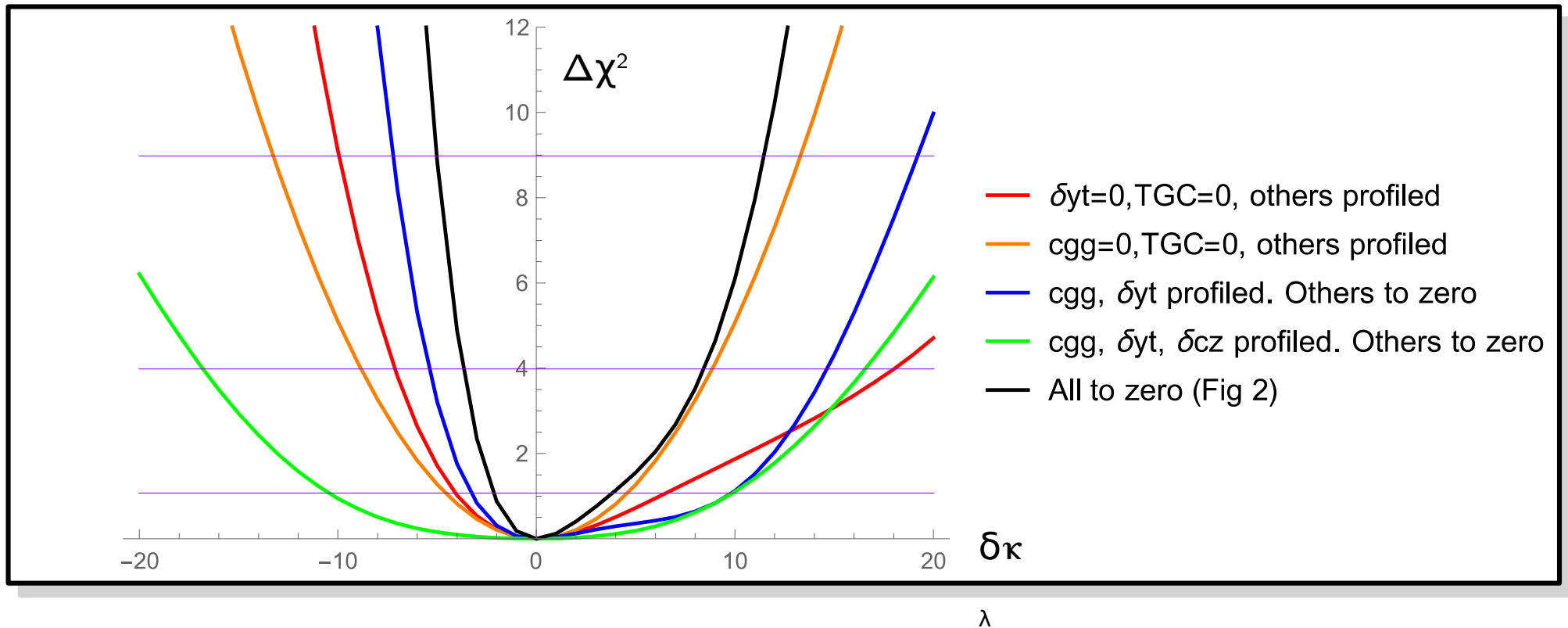


$\Delta\chi^2=2.3$  contours (68% CL in the gaussian limit)  
[other 8 couplings profiled]

If large  $\kappa_\lambda$  is allowed, it feeds back into single-Higgs couplings fits

# Constrained “intermediate” scenarios

A game: let's pretend we have scenarios with some of  $(\delta y_{t,c_{gg}}, \delta c_z)$  switched off

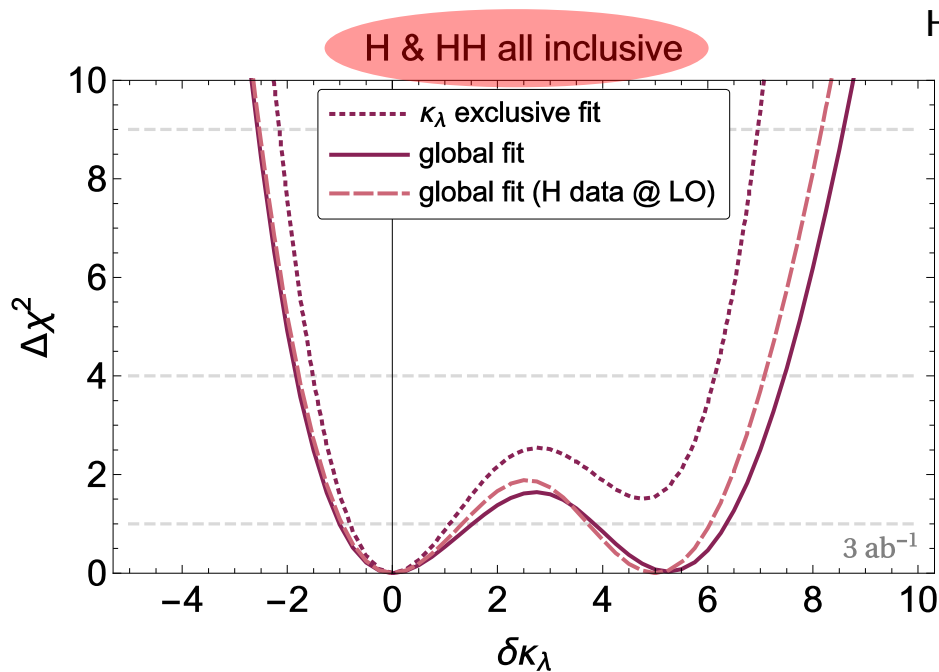


As expected, constraining “by hand” the coefficients that control the flat direction, the bound on  $\kappa_\lambda$  shrinks

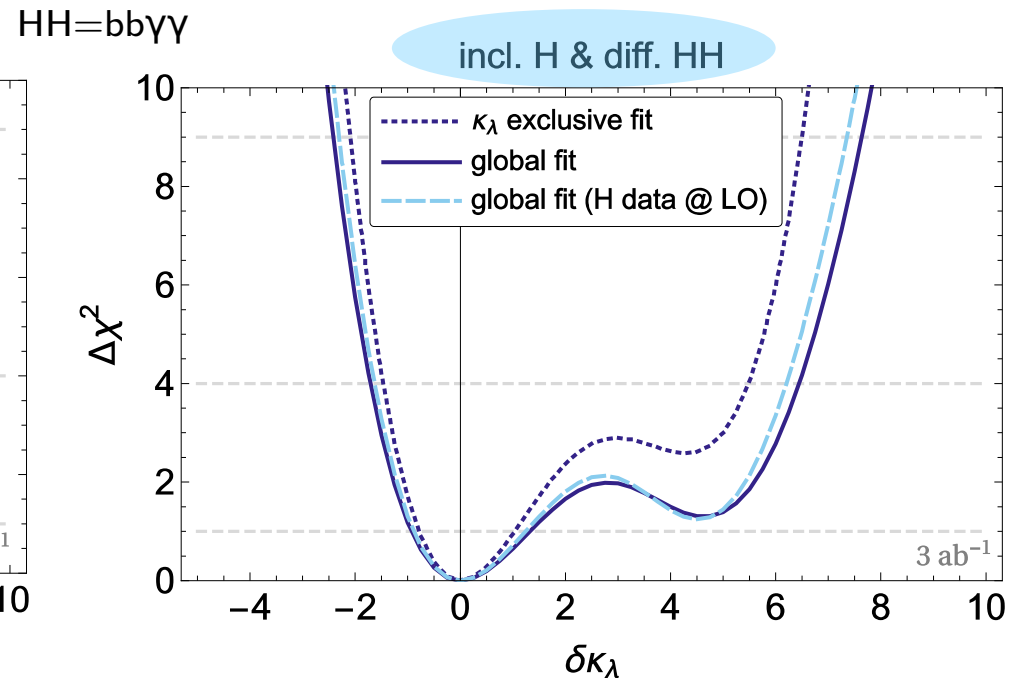


Any model builder willing to explore how motivated such scenarios are?

# Compare & combine w/ double-Higgs



**Double-Higgs drives the bound on  $\kappa_\lambda$**   
 while, single-Higgs observables are essential in order to constrain the other coefficients deforming  $\sigma(hh)$



Differential ( $m_{hh}$ ) double-Higgs removes degeneracy due to second minimum

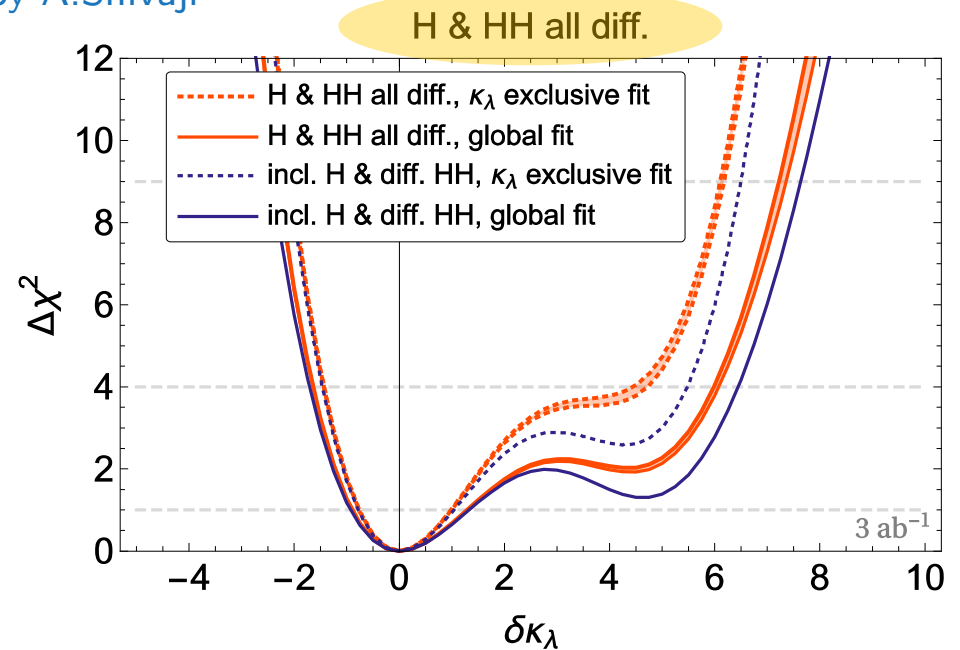
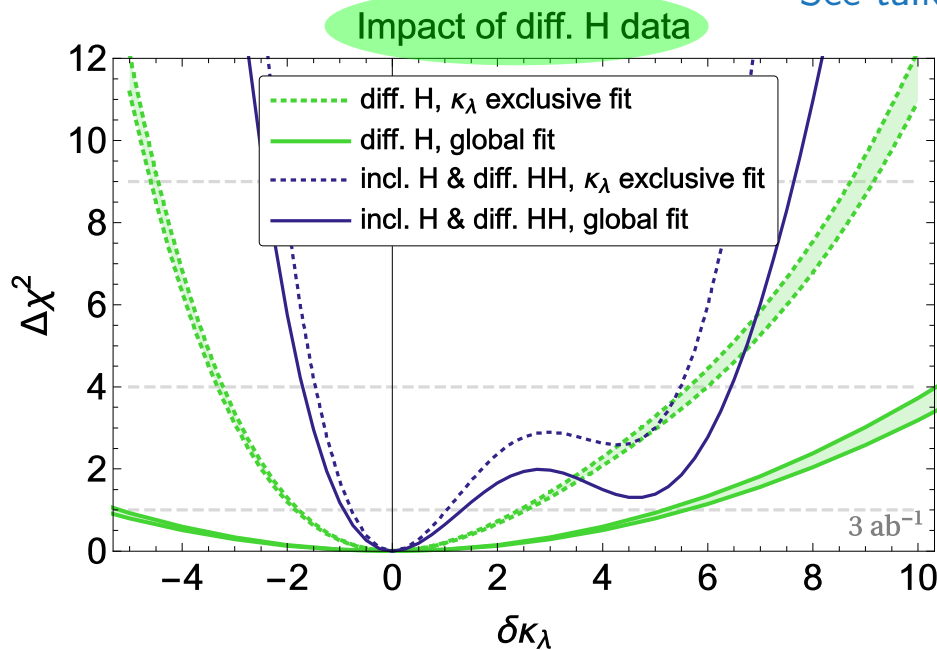
“Exclusive”  $\kappa_\lambda$  fits benefit from NLO single-Higgs, global don’t

Warning: here the assumption is that of linearly realized EW symmetry.

Non-linear EFT  $\Rightarrow \{1, h, h^2\}XY$  couplings unrelated  $\Rightarrow$  more parameters, global fit w/ EWPO!

# Impact of differential VH and ttH

See talk by A. Shivaji



Inclusion of differential data ( $d\sigma/dm_{\text{inv}}$ ) for single-Higgs observables seems promising, but more detailed estimates of the experimental systematics are required, as well as more refined analyses.

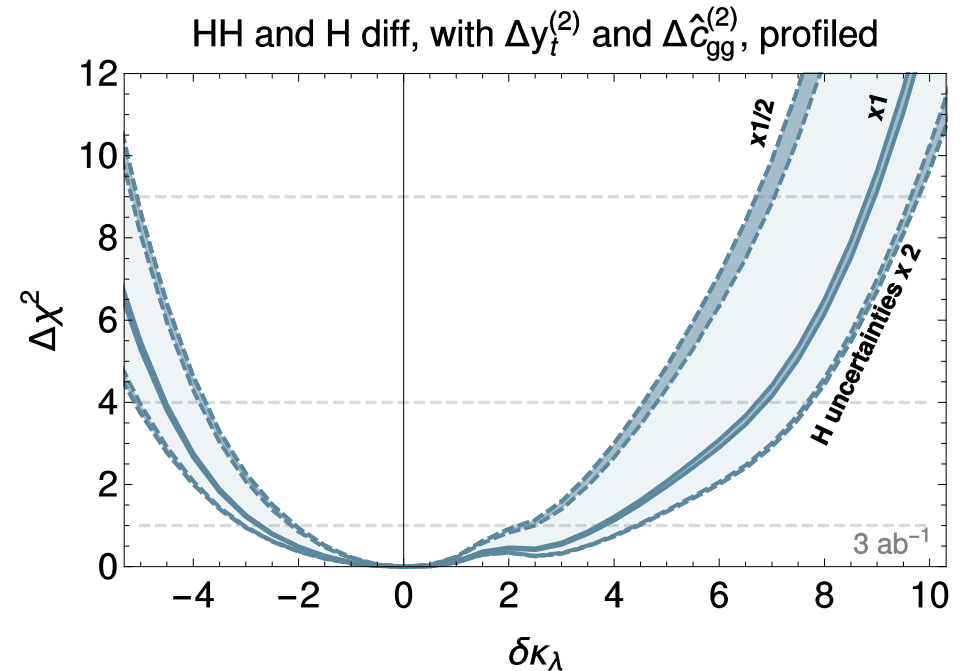
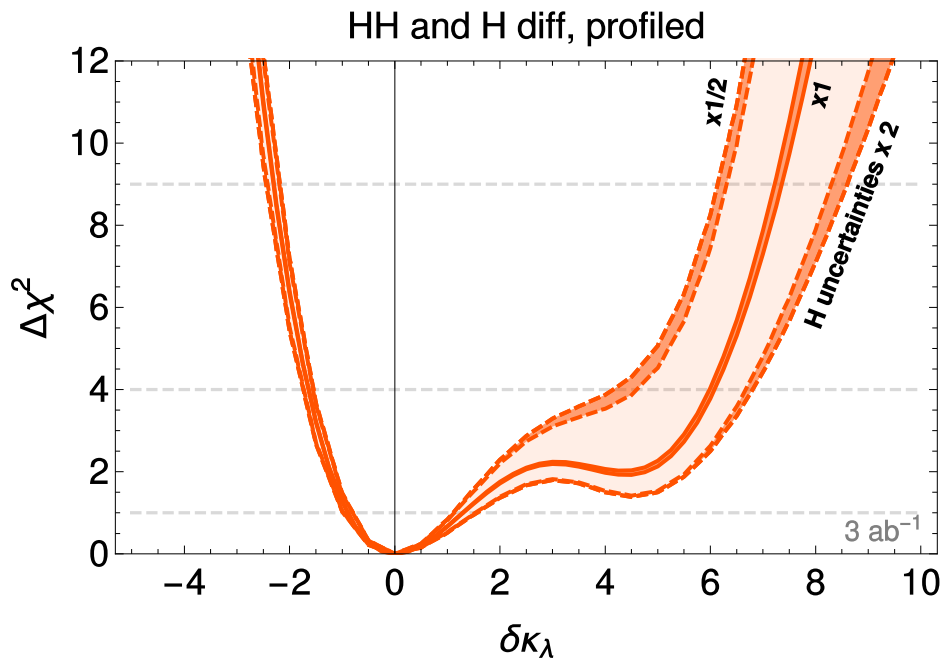
See Maltoni, Pagani, Shivaji, Zhao [1709.08649] for the impact of  $\delta\kappa_\lambda$  on single-Higgs differential distributions and for a simplified  $\kappa$ -framework analysis  
 \* see backup a couple of their plots

Combining differential data from single- and double-Higgs, the minimum at large  $\delta\kappa_\lambda$  is further lifted. Synergy!

Bound from single-H not competitive but has totally different systematics  
 $\Rightarrow$  complementary to HH

# Some simple robustness checks

(HH=bbγγ)



simple global rescaling of  
single-Higgs uncertainties  
doesn't impact too much

relaxing the assumption of  
linear EFT for double-Higgs  
weakens the bound  
→ also, more operators have  
to be considered

# Outline

- Testing BSM deformations with Higgs physics
- Higgs trilinear self-coupling at the HL-LHC
- Prospects at the HE-LHC and future  $e^+e^-$  colliders

See also talks by [A.Canepa](#) and [P.Roloff](#)



# Higgs self-coupling @ HE-LHC

Stay tuned for the  
HL/HE-LHC YR  
See talk by S.Gori

## HL-LHC

14 TeV, 3/ab  
 $\sigma(\text{hh,ggF}) \sim 35\text{fb}$

Grojean, Panico, Riembau, Vantalon, DV [1704.01953]

- Inclusive single-Higgs rates can't constrain  $\delta\kappa_\lambda$  (w/ NLO effects) in generic BSM scenarios
- Double-Higgs production drives the bound (single-Higgs LO crucial for other deformations)
- Differential measurements of both h and hh help eliminate the extra minimum  $\delta\kappa_\lambda \sim 5$
- HL-LHC is **the machine** for accurate differential Higgs measurements → explore prospects!

## HE-LHC

33 TeV, 10/ab  
 $\sigma(\text{hh,ggF}) \sim 194\text{fb}$

- HE here is just naive extrapolation! (FCC=100TeV)
- Old machine parameters, just for illustrative purposes

$\delta\kappa_\lambda$ bound / scenario	68%	95%
HL: h incl, hh incl	[-1, 1.5] U [3.9, 6.4]	[-1.8, 7.5]
HL: h incl, hh diff	[-1.1, 1.3]	[-1.7, 6.5]
HE: h incl, hh incl	[-0.3, 0.3] U [5.0, 6.0]	[-0.5, 0.7] U [4.5, 6.7]
HL + HE	[-0.3, 0.3]	[-0.5, 0.6] U [4.8, 6.0]
FCC 100 TeV 30/ab h incl, hh diff	[-0.03, 0.03]	[-0.06, 0.06]

- Uncertainties on single-H  $\mu$ 's: naively extrapolated from HL-LHC
- Double-H EFT: interpolation between HL-LHC and FCC of Azatov et al '15
- NLO  $\delta\kappa_\lambda$  effect on single-H: courtesy of D.Pagani

- Both high E and high lumi
- Probe BSM in distrib's tails
- Exploit non-SM tensor structures to disentangle flat directions in BSM fits
- Also VBF channel *See e.g. Contino et al '10, '12*
- Work to be done!

# The lepton collider option

## Hadron

- High-energy  $\rightarrow$  discovery?
- No direct handle on partonic c.o.m. energy  $\rightarrow$  pdf's
- Large QCD backgrounds
- Sensitivity to couplings to quarks

## Lepton

- Lower energies but clean environment  $\rightarrow$  Higgs factories
- Lower energies achievable
- Beam polarization (extra handle)
- Sensitivity to EW couplings

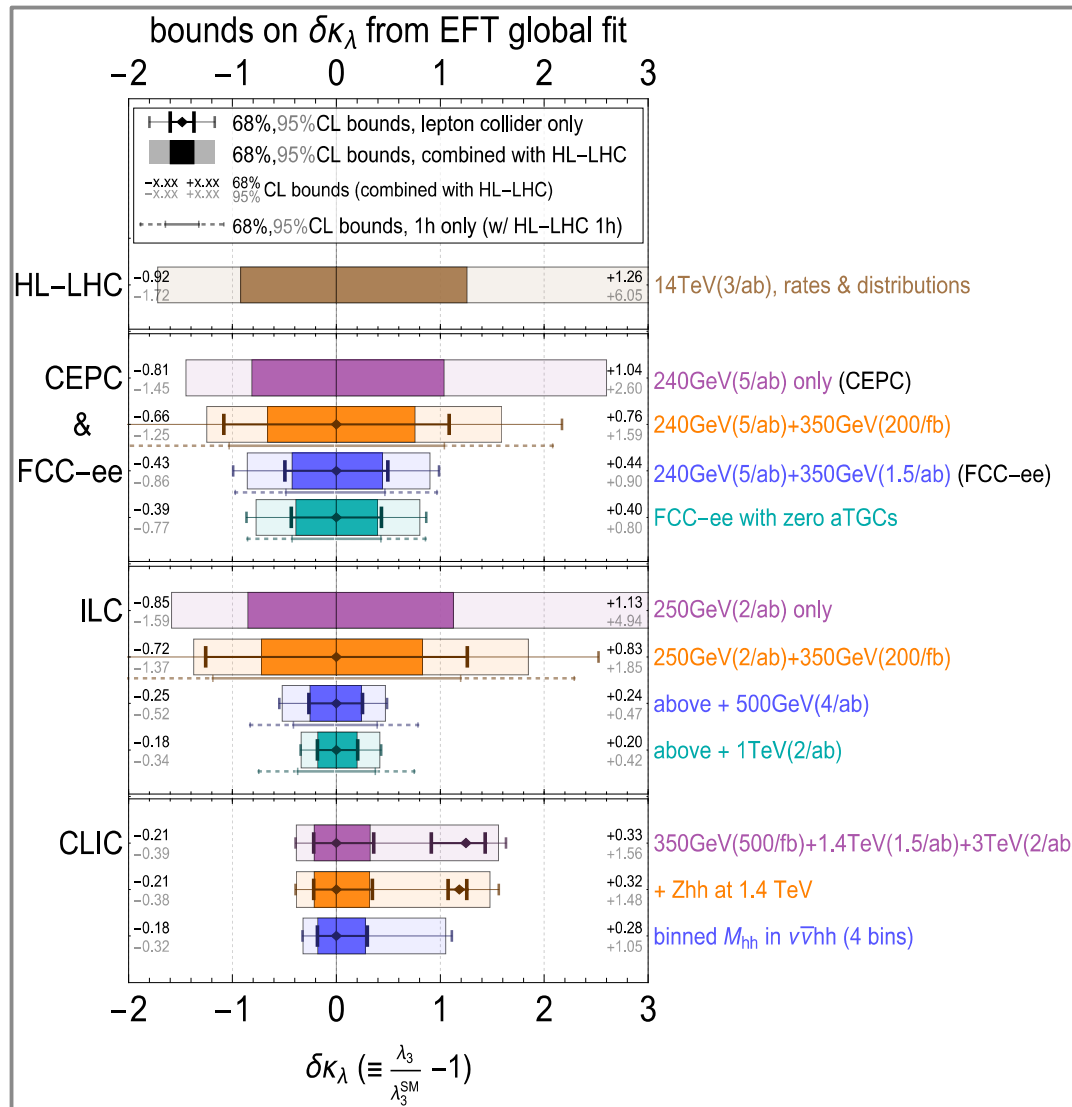
## Circular

- Energy limited by synchrotron radiation
- Higher luminosity
- Several interaction points
- Precise determination of beam energy

## Linear

- Allows for staged development (gradual energy increase)
- Easier to control beam polarization
- Bremsstrahlung

# Comparison of future colliders reach



- HL/HE-LHC
  - HL will be able to put only  $O(1)$  bound, **driven by hh production**
  - HE with cross-section and lumi increase  $\rightarrow$  factor 10 better
- Low energy  $e^+e^-$ 
  - only a 240GeV circular collider is not enough: need to combine with HL-LHC or run at other energy
  - 40% precision from **indirect bound (h)**, provided runs at both 240/250 GeV and 350 GeV are available ( $\sim$ few  $ab^{-1}$  lumi)
- High-energy  $e^+e^-$ 
  - **direct bound (hh) dominates**
  - ILC maximizes sensitivity (Zh, WBF)
  - CLIC loses access to Zh  $\rightarrow$  residual minimum for  $\delta\kappa_\lambda \sim 1$

Durieux, Grojean, Gu, Liu, Panico, Riemann, Vantalon, DV [1711.03978]

# Items for discussion at the LHC

- Keep up with the hard work in measuring inclusive & diff rates
- Use simplified scenarios (e.g.  $\kappa_\lambda$  or  $\kappa_\lambda\text{-}\kappa_t$ ) just as a training ground
- Bounds on  $\kappa_\lambda$  from simplified fits have a physical interpretation only in very non-generic scenarios
  - ⇒ they are **not** model-independent statements on the Higgs self-coupling!

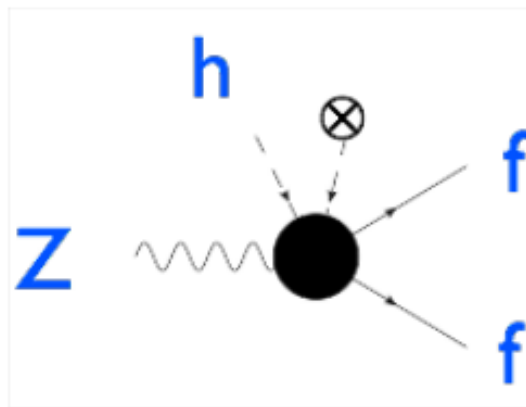
- Bounds on  $\kappa_\lambda$  from single-H can't compete with HH
  - ⇒ but somehow complementary
- Come up with optimized observables (e.g. best differential distrib's)
- Include new channels to resolve flat directions (e.g.  $h+j$ ,  $h+\gamma$ )

- More/updated HL-LHC projections (incl. and diff) very welcome!
- Is it reasonable to neglect the other operators in these extrapolations?
- Are there BSM scenarios that can be tested today? ⇒ Model building effort

# Backup

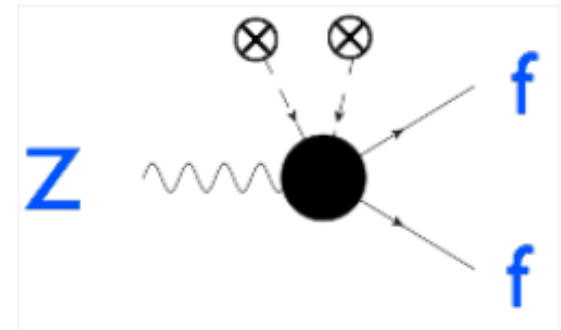
# BSM deformations and Higgs physics

Potentially new BSM-effects in  $h$  physics could have been already tested in the vacuum



$$H^\dagger D_\mu H \bar{f} \gamma^\mu f$$

$$= \frac{1}{2v} \times$$



(assuming that the Higgs boson is part of a doublet)

Modifications in  $h \rightarrow Z f \bar{f}$  related to  $Z \rightarrow f \bar{f}$

already constrained at LEP




# BSM deformations and Higgs physics

There are others deformations away from the SM that are harmless in the vacuum and need a Higgs field to be probed

e.g. 
$$\frac{1}{g_s^2} G_{\mu\nu}^2 + \frac{|H|^2}{\Lambda^2} G_{\mu\nu}^2 \rightarrow \left( \frac{1}{g_s^2} + \frac{v^2}{\Lambda^2} \right) G_{\mu\nu}^2$$

operator not visible in the vacuum  
(redefinition of input parameter)



But can affect h physics:



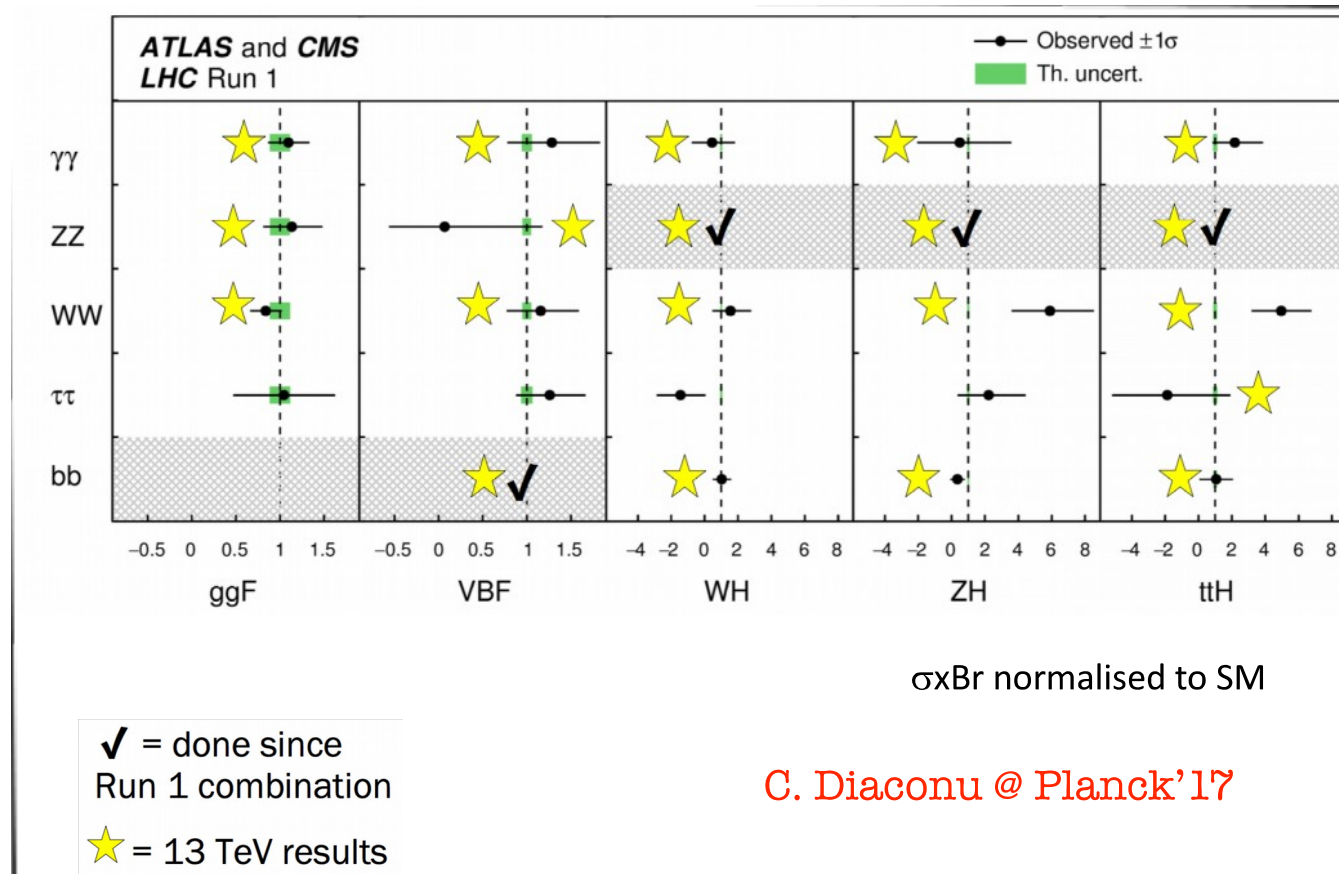
# Single-Higgs couplings at the LHC today

signal strengths  $\mu_i \times \mu^f = \mathbf{inclusive}$  rates ( $\sigma_i \times BR_f$ ) relative to SM prediction

$$\mu_i = \frac{\sigma[i \rightarrow h]}{(\sigma[i \rightarrow h])_{SM}}$$

$$\mu_f = \frac{BR[h \rightarrow f]}{(BR[h \rightarrow f])_{SM}}$$

decay  
↙



↘ production

C. Diaconu @ Planck'17

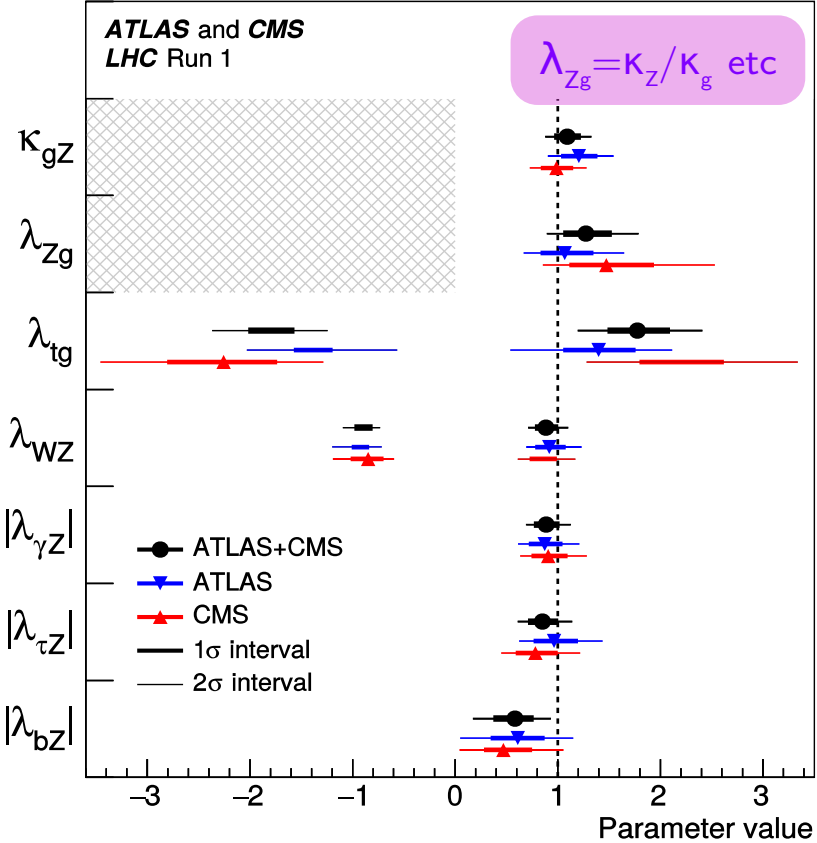
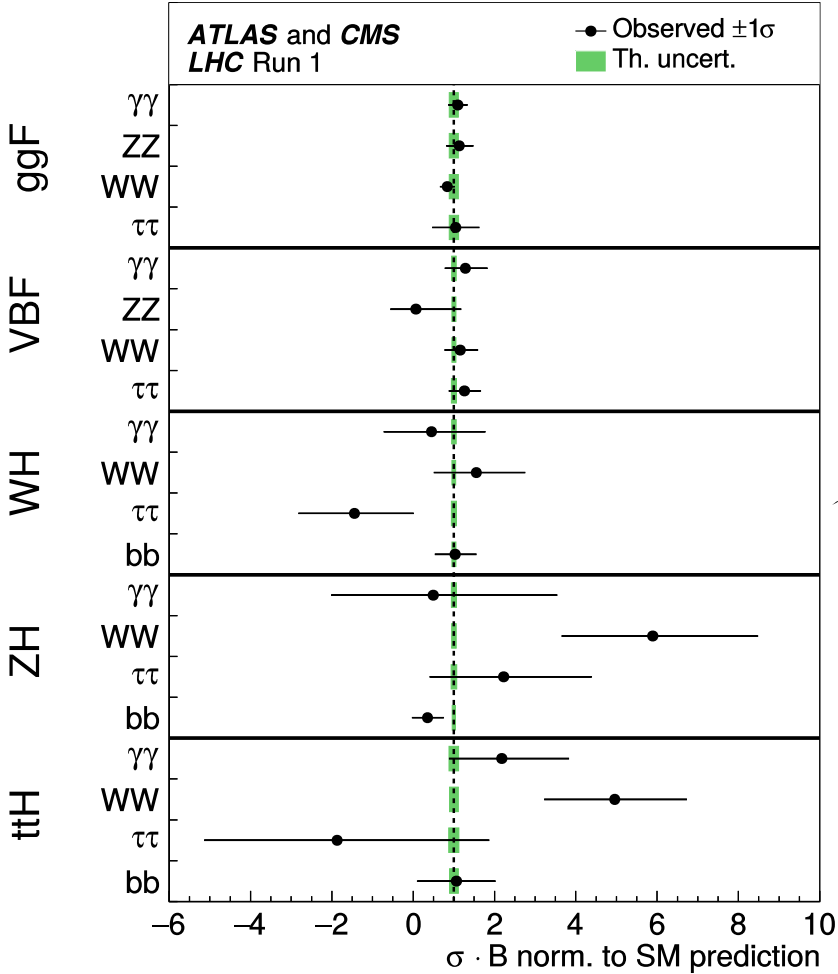


# A (too) simple interpretation: $\kappa$ -framework

(ideally)  $5^2 \mu_i \times \mu^f$

7-parameters “ $\kappa$ -framework”

ATLAS+CMS [1606.02266]



- Only total rates modified
- No new tensor structures allowed

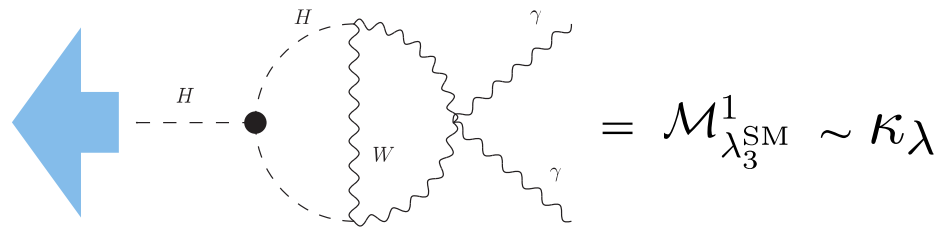
$$(\sigma \cdot \text{BR})(gg \rightarrow H \rightarrow \gamma\gamma) = \sigma_{\text{SM}}(gg \rightarrow H) \cdot \text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma) \cdot \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

# Self-coupling & single-Higgs @NLO

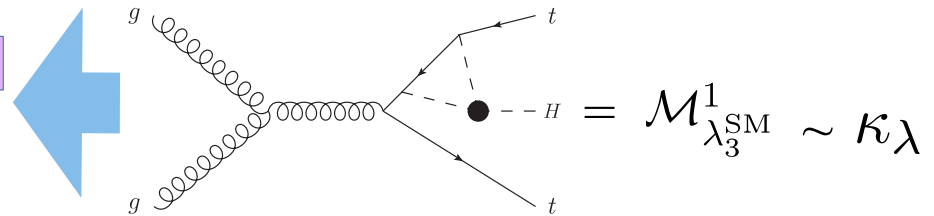
LO can include  
QCD corrections

$$\Sigma_{\text{NLO}} = Z_H \Sigma_{\text{LO}} (1 + \kappa_\lambda C_1)$$

$$C_1^\Gamma = \frac{\int d\Phi \, 2\Re(\mathcal{M}^{0*} \mathcal{M}_{\lambda_3^{\text{SM}}}^1)}{\int d\Phi \, |\mathcal{M}^0|^2}$$



$$C_1^\sigma = \frac{\sum_{i,j} \int dx_1 dx_2 f_i(x_1) f_j(x_2) \, 2\Re(\mathcal{M}_{ij}^{0*} \mathcal{M}_{\lambda_3^{\text{SM},ij}}^1) \, d\Phi}{\sum_{i,j} \int dx_1 dx_2 f_i(x_1) f_j(x_2) \, |\mathcal{M}_{ij}^0|^2 \, d\Phi}$$



$d\Phi$  inclusive or differential

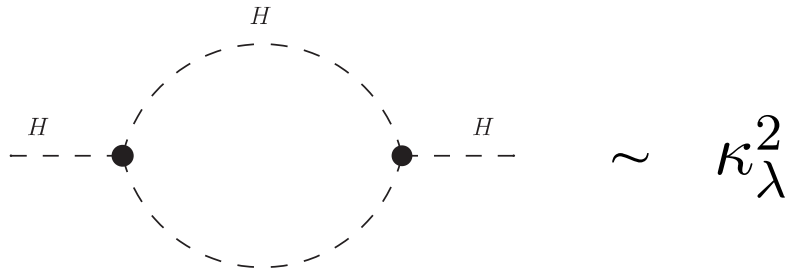
Courtesy of D. Pagani @ Turin '17

# Self-coupling & single-Higgs @NLO

$$\Sigma_{\text{NLO}} = \boxed{Z_H} \Sigma_{\text{LO}} (1 + \kappa_\lambda C_1)$$

$$Z_H = \frac{1}{1 - \kappa_\lambda^2 \delta Z_H}$$

$$\delta Z_H = -\frac{9}{16} \frac{2(\lambda_3^{\text{SM}})^2}{m_H^2 \pi^2} \left( \frac{2\pi}{3\sqrt{3}} - 1 \right)$$



$$\kappa_\lambda^2 \delta Z_H \lesssim 1 \quad \rightarrow \quad |\kappa_\lambda| \lesssim 25$$

The wave-function normalization receives corrections that depend quadratically on  $\lambda_3$ . For large  $\kappa_\lambda$ , the result cannot be linearized and must be resummed.

For a sensible resummation

20

Courtesy of D. Pagani @ Turin '17

# Self-coupling & single-Higgs @NLO

$$\Sigma_{\text{NLO}} = Z_H \Sigma_{\text{LO}} (1 + \kappa_\lambda C_1)$$

$$\Sigma_{\text{NLO}}^{\text{SM}} = \Sigma_{\text{LO}} (1 + C_1 + \delta Z_H)$$



$$\delta\Sigma_{\lambda_3} \equiv \frac{\Sigma_{\text{NLO}} - \Sigma_{\text{NLO}}^{\text{SM}}}{\Sigma_{\text{LO}}} = \underbrace{(\kappa_\lambda - 1)C_1}_{\text{universal}} + \underbrace{(\kappa_\lambda^2 - 1)C_2}_{\text{universal}} + \mathcal{O}(\kappa_\lambda^3 \alpha^2)$$

Process and kinetic dependent

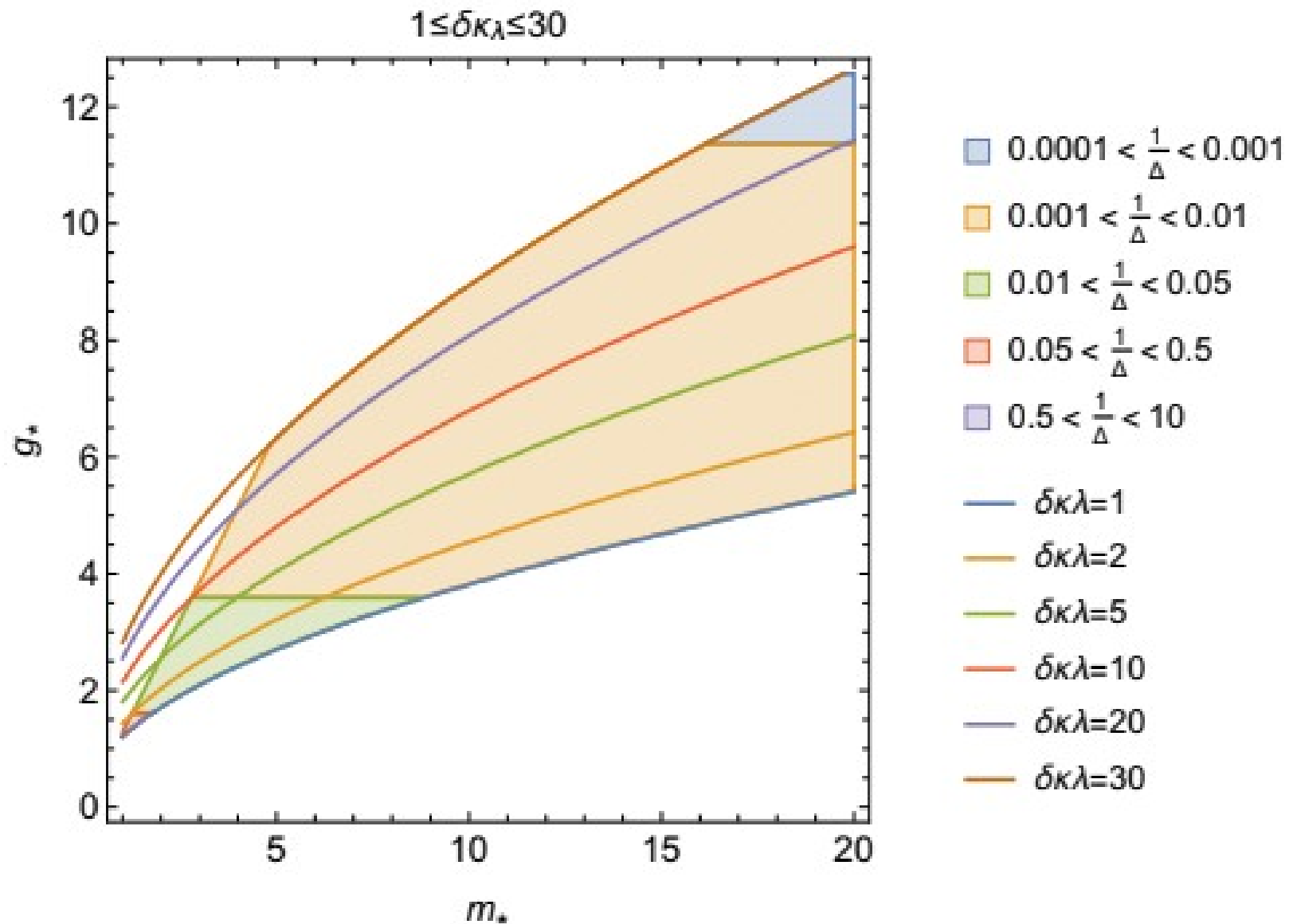
(inclusive or differential in  $m_{\text{inv}}$  and  $p_T^H$ )

$$C_2 = \frac{\delta Z_H}{(1 - \kappa_\lambda^2 \delta Z_H)}$$

$$\mathcal{O}(\kappa_\lambda^3 \alpha^2) \simeq \kappa_\lambda^3 C_1 \delta Z_H \lesssim 10\% \quad \rightarrow \quad |\kappa_\lambda| \lesssim 20$$

Courtesy of D. Pagani @ Turin '17

# Large $\lambda_3$ in tuned Higgs Portal



# How large can $\lambda_3$ be?

Think in terms of model classes

?

No analysis is truly model independent!

>

NLO w/ dominant  $h^3$

=

LO w/ subdominant other h

<

Minimal Composite Higgs

SILH

$$\xi = \frac{v^2}{f^2} \ll 1$$

$$\frac{1}{f^2} (\partial_\mu |H|^2)^2$$

$$\kappa_V \equiv \frac{g_{hVV}^{\text{SM}}}{g_{hVV}} = 1 + \xi$$

$$\frac{\lambda_4}{f^2} |H|^6$$

$$\kappa_3 \equiv \frac{g_{hhh}^{\text{SM}}}{g_{hhh}} = 1 + \xi$$

NLO  $h^3$   
irrelevant

Partly Composite Higgs

$$\xi = \frac{v^2}{f^2} \ll 1$$

$$\frac{\varepsilon^4}{f^2} (\partial_\mu |H|^2)^2$$

$$\kappa_V \equiv \frac{g_{hVV}^{\text{SM}}}{g_{hVV}} = 1 + \varepsilon^4 \xi$$

$$\frac{\varepsilon^6}{f^2} |H|^6$$

$$\kappa_3 \equiv \frac{g_{hhh}^{\text{SM}}}{g_{hhh}} = 1 + \varepsilon^2 \frac{g_*^2 v^2}{m_h^2} \varepsilon^4 \xi$$

NLO  $h^3$   
could be relevant

Bosonic Technicolor

Induced EWSB

$$\varepsilon = \frac{f}{v} \ll 1$$

$$\frac{\varepsilon^4}{f^2} (\partial_\mu |H|^2)^2$$

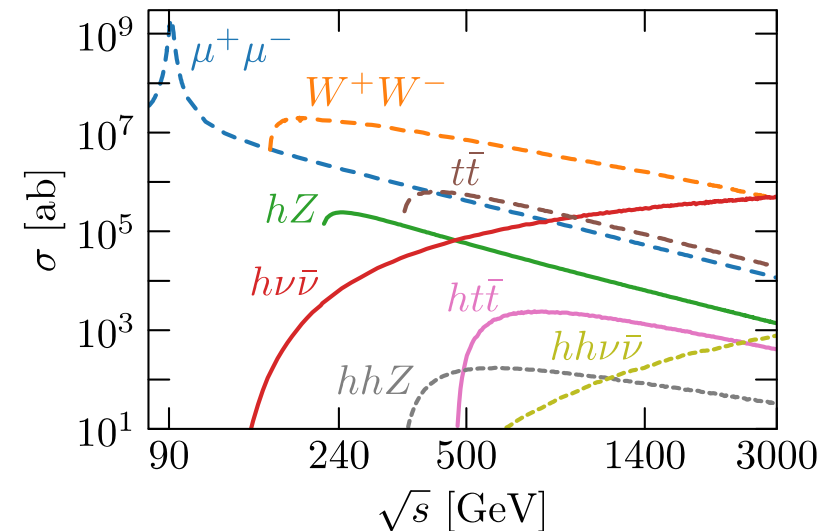
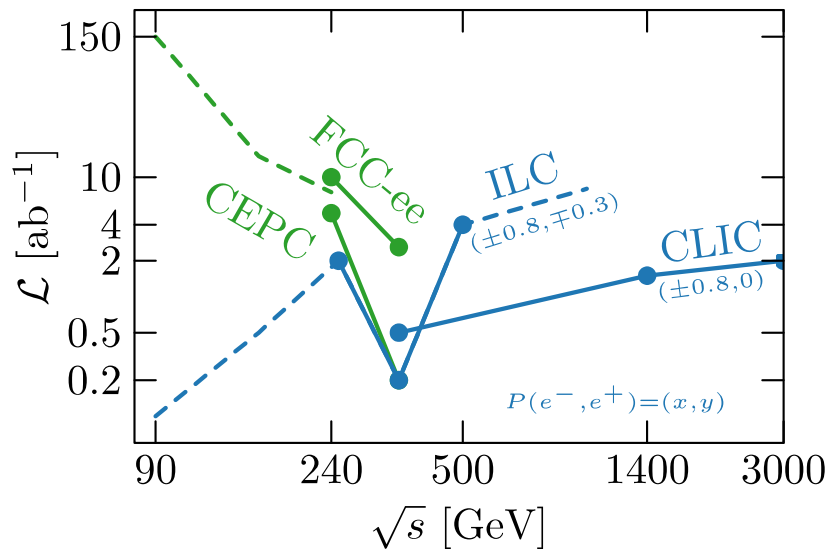
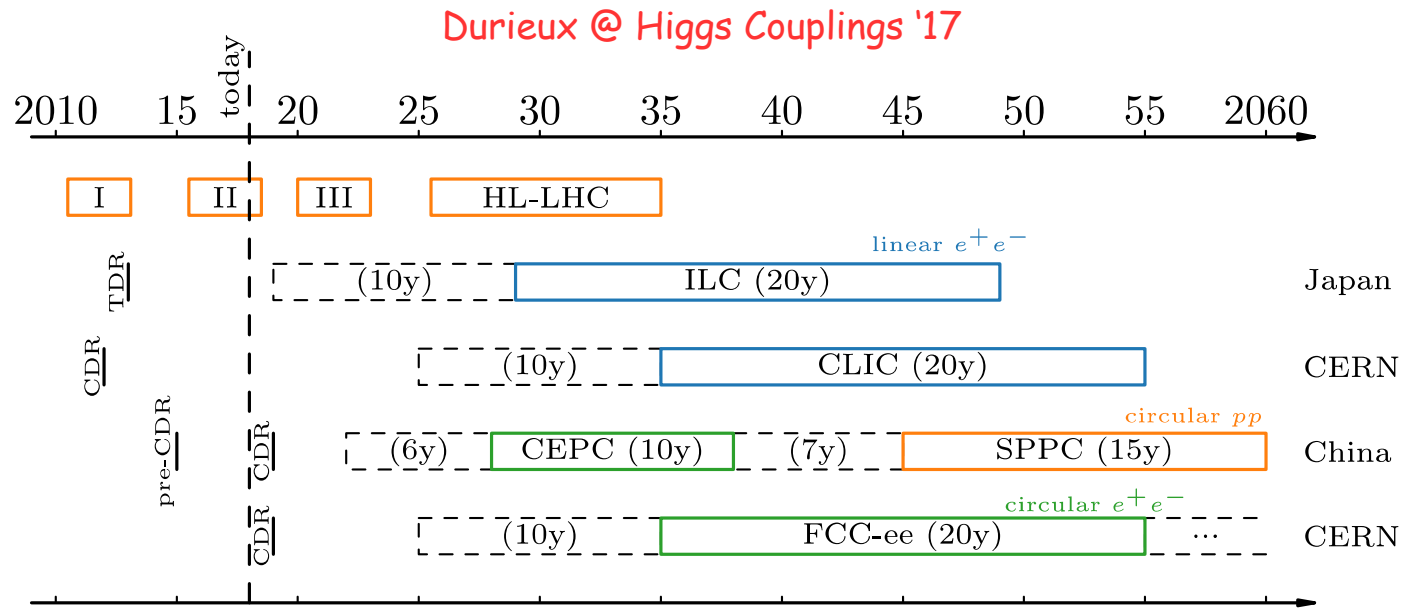
$$\kappa_V \equiv \frac{g_{hVV}^{\text{SM}}}{g_{hVV}} = 1 + \varepsilon^2$$

$$\frac{\varepsilon^6}{f^2} |H|^6$$

$$\kappa_3 \equiv \frac{g_{hhh}^{\text{SM}}}{g_{hhh}} = 1 + \mathcal{O}(1)$$

NLO  $h^3$   
a priori relevant

# A future history of lepton colliders

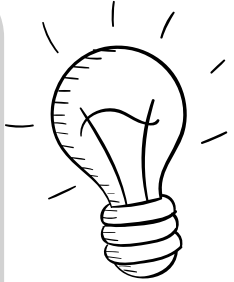


# Will further constraints help?

- Triple Gauge Couplings

- currently WWZ and WW $\gamma$  tested at 5%  $\rightarrow$  expect 1%
- can be converted in constraints on 2 linear combinations of

$$\hat{c}_{\gamma\gamma}, \hat{c}_{z\gamma}, c_{zz}, c_{z\Box}$$



- BR(h $\rightarrow$ Z $\gamma$ )

- Will be measured w/ 30% accuracy
- Can be used to constrain  $c_{z\gamma}$   $\rightarrow$  not relevant for  $\kappa_\lambda$ !

- BR(h $\rightarrow$  $\mu\mu$ )

- Either one extra parameter  $\delta y_\mu$
- Or (w/ flavor universality) just helps to better bound  $\delta y_e$



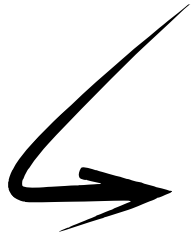


# Gauge invariant operators in the Higgs basis

$$\begin{aligned}
 O_{\delta\lambda_3} &= -\frac{1}{v^2}(H^\dagger H)^3, \\
 O_{c_{gg}} &= \frac{g_s^2}{4v^2} H^\dagger H G_{\mu\nu}^a G_{\mu\nu}^a \\
 O_{\delta c_z} &= -\frac{1}{v^2} \left[ \partial_\mu (H^\dagger H) \right]^2 + \frac{3\lambda}{v^2} (H^\dagger H)^3 + \left( \sum_f \frac{\sqrt{2}m_{f_i}}{v^3} H^\dagger H \bar{f}_{L,i} H f_{R,i} + \text{h.c.} \right), \\
 O_{c_{z\Box}} &= \frac{ig^3}{v^2(g^2 - g'^2)} \left( H^\dagger \sigma^i \overleftrightarrow{D}_\mu H \right) D_\nu W_{\mu\nu}^i - \frac{ig^2 g'}{v^2(g^2 - g'^2)} \left( H^\dagger \overleftrightarrow{D}_\mu H \right) \partial_\nu B_{\mu\nu}, \\
 O_{c_{zz}} &= \frac{ig(g^2 + g'^2)}{2v^2(g^2 - g'^2)} \left( H^\dagger \sigma^i \overleftrightarrow{D}_\mu H \right) D_\nu W_{\mu\nu}^i - \frac{ig'(g^2 + g'^2)}{2v^2(g^2 - g'^2)} \left( H^\dagger \overleftrightarrow{D}_\mu H \right) \partial_\nu B_{\mu\nu} \\
 &\quad - \frac{ig}{v^2} \left( D_\mu H^\dagger \sigma^i D_\nu H \right) W_{\mu\nu}^i - \frac{ig'}{v^2} \left( D_\mu H^\dagger D_\nu H \right) B_{\mu\nu}, \\
 O_{c_{z\gamma}} &= -\frac{2igg'^2}{v^2(g^2 + g'^2)} \left( D_\mu H^\dagger \sigma^i D_\nu H \right) W_{\mu\nu}^i + \frac{2ig'g^2}{v^2(g^2 + g'^2)} \left( D_\mu H^\dagger D_\nu H \right) B_{\mu\nu}, \\
 O_{c_{\gamma\gamma}} &= -\frac{igg'^4}{2v^2(g^4 - g'^4)} \left( H^\dagger \sigma^i \overleftrightarrow{D}_\mu H \right) D_\nu W_{\mu\nu}^i + \frac{ig'^5}{2v^2(g^4 - g'^4)} \left( H^\dagger \overleftrightarrow{D}_\mu H \right) \partial_\nu B_{\mu\nu} \\
 &\quad - \frac{igg'^4}{v^2(g^2 + g'^2)^2} \left( D_\mu H^\dagger \sigma^i D_\nu H \right) W_{\mu\nu}^i + \frac{ig'^3(2g^2 + g'^2)}{(g^2 + g'^2)^2 v^2} \left( D_\mu H^\dagger D_\nu H \right) B_{\mu\nu} + \frac{g'^2}{4v^2} H^\dagger H B_{\mu\nu} B_{\mu\nu}, \\
 [O_{\delta y_f}]_{ij} &= -\frac{\sqrt{2}m_{f_i} m_{f_j}}{v^3} H^\dagger H \bar{f}_{L,i} H f_{R,j} + \text{h.c.},
 \end{aligned}$$

# Estimated precision @ circular colliders

O(1%) on  
most channels



	CEPC				FCC-ee			
	[240 GeV, 5 ab <sup>-1</sup> ]		[350 GeV, 200 fb <sup>-1</sup> ]		[240 GeV, 10 ab <sup>-1</sup> ]		[350 GeV, 2.6 ab <sup>-1</sup> ]	
production	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$
$\sigma$	0.50%	—	2.4%	—	0.40%	—	0.67%	—
	$\sigma \times \text{BR}$				$\sigma \times \text{BR}$			
$h \rightarrow b\bar{b}$	0.21%★	0.39%◇	2.0%	2.6%	0.20%	0.28%◇	0.54%	0.71%
$h \rightarrow c\bar{c}$	2.5%	—	15%	26%	1.2%	—	4.1%	7.1%
$h \rightarrow gg$	1.2%	—	11%	17%	1.4%	—	3.1%	4.7%
$h \rightarrow \tau\tau$	1.0%	—	5.3%	37%	0.7%	—	1.5%	10%
$h \rightarrow WW^*$	1.0%	—	10%	9.8%	0.9%	—	2.8%	2.7%
$h \rightarrow ZZ^*$	4.3%	—	33%	33%	3.1%	—	9.2%	9.3%
$h \rightarrow \gamma\gamma$	9.0%	—	51%	77%	3.0%	—	14%	21%
$h \rightarrow \mu\mu$	12%	—	115%	275%	13%	—	32%	76%
$h \rightarrow Z\gamma$	25%	—	144%	—	18%	—	40%	—

**Table 2.** The estimated precision of CEPC and FCC-ee Higgs measurements. We gather the available estimations from refs. [1, 2, 86], while the missing ones (highlighted in green) are obtained from scaling with luminosity. See appendix B for more details. For  $\sigma(e^+e^- \rightarrow \nu\bar{\nu}h)$ , the precisions marked with a diamond ◇ are normalized to the cross section of the inclusive channel which includes both the  $WW$  fusion and  $e^+e^- \rightarrow hZ, Z \rightarrow \nu\bar{\nu}$ , while the unmarked precisions are normalized to the  $WW$  fusion process only. For the CEPC, the precision of the  $\sigma(hZ) \times \text{BR}(h \rightarrow b\bar{b})$  measurement (marked by a star ★) reduces to 0.24% if one excludes the contribution from  $e^+e^- \rightarrow hZ, Z \rightarrow \nu\bar{\nu}, h \rightarrow b\bar{b}$  to avoid double counting with  $e^+e^- \rightarrow \nu\bar{\nu}h, h \rightarrow b\bar{b}$ . The corresponding information is not available for the FCC-ee.

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# Estimated precision @ linear colliders: ILC

ILC											
	[250 GeV, 2 ab <sup>-1</sup> ]		[350 GeV, 200 fb <sup>-1</sup> ]		[500 GeV, 4 ab <sup>-1</sup> ]			[1 TeV, 1 ab <sup>-1</sup> ]		[1 TeV, 2.5 ab <sup>-1</sup> ]	
production	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}h$	$t\bar{t}h$
$\sigma$	0.71%	—	2.1%	—	1.1%	—	—	—	—	—	—
	$\sigma \times \text{BR}$										
$h \rightarrow b\bar{b}$	0.42%	3.7%	1.7%	1.7%	0.64%	0.25%	9.9%	0.5%	6.0%	0.3%	3.8%
$h \rightarrow c\bar{c}$	2.9%	—	13%	17%	4.6%	2.2%	—	3.1%	—	2.0%	—
$h \rightarrow gg$	2.5%	—	9.4%	11%	3.9%	1.4%	—	2.3%	—	1.4%	—
$h \rightarrow \tau\tau$	1.1%	—	4.5%	24%	1.9%	3.2%	—	1.6%	—	1.0%	—
$h \rightarrow WW^*$	2.3%	—	8.7%	6.4%	3.3%	0.85%	—	3.1%	—	2.0%	—
$h \rightarrow ZZ^*$	6.7%	—	28%	22%	8.8%	2.9%	—	4.1%	—	2.6%	—
$h \rightarrow \gamma\gamma$	12%	—	44%	50%	12%	6.7%	—	8.5%	—	5.4%	—
$h \rightarrow \mu\mu$	25%	—	98%	180%	31%	25%	—	31%	—	20%	—
$h \rightarrow Z\gamma$	34%	—	145%	—	49%	—	—	—	—	—	—

**Table 3.** The estimated precision of ILC Higgs measurements. For the 250 GeV, 350 GeV and 500 GeV runs, all numbers are scaled from ref. [58] (table 13), except for  $\sigma(hZ) \times \text{BR}(h \rightarrow Z\gamma)$  which is scaled from the CEPC estimation. A beam polarization of  $P(e^-, e^+) = (-0.8, +0.3)$  is assumed. The 1 TeV run is only included in figure 17 of appendix C, while the estimations are taken from ref. [59] which assumes a polarization of  $P(e^-, e^+) = (-0.8, +0.2)$ .

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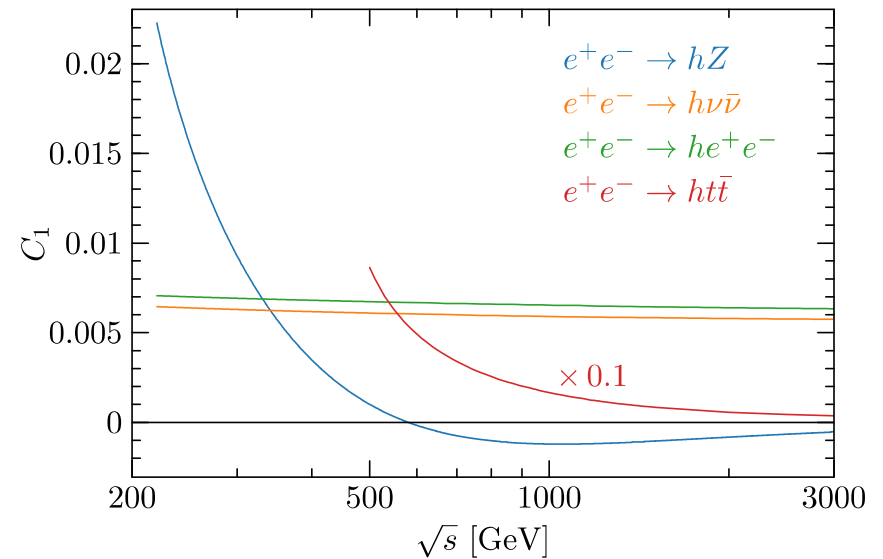
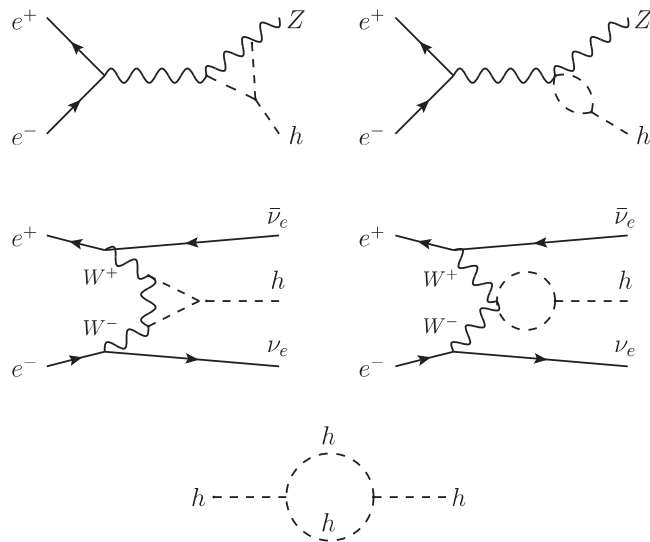
# Estimated precision @ linear colliders: CLIC

CLIC					
	[350 GeV, 500 fb <sup>-1</sup> ]		[1.4 TeV, 1.5 ab <sup>-1</sup> ]		[3 TeV, 2 ab <sup>-1</sup> ]
production	$Zh$	$\nu\bar{\nu}h$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}h$
$\sigma$	1.6%	—	—	—	—
	$\sigma \times \text{BR}$				
$h \rightarrow b\bar{b}$	0.84%	1.9%	0.4%	8.4%	0.3%
$h \rightarrow c\bar{c}$	10.3%	14.3%	6.1%	—	6.9%
$h \rightarrow gg$	4.5%	5.7%	5.0%	—	4.3%
$h \rightarrow \tau\tau$	6.2%	—	4.2%	—	4.4%
$h \rightarrow WW^*$	5.1%	—	1.0%	—	0.7%
$h \rightarrow ZZ^*$	—	—	5.6%	—	3.9%
$h \rightarrow \gamma\gamma$	—	—	15%	—	10%
$h \rightarrow \mu\mu$	—	—	38%	—	25%
$h \rightarrow Z\gamma$	—	—	42%	—	30%

**Table 4.** The estimated precision of CLIC Higgs measurements taken from ref. [60], which assumes unpolarized beams and considers only statistical uncertainties. In addition, we also include the estimations for  $\sigma(hZ) \times \text{BR}(h \rightarrow b\bar{b})$  at high energies in ref. [35], which are 3.3% (6.8%) at 1.4 TeV (3 TeV). We find the inclusion of the  $ZZ$  fusion ( $e^+e^- \rightarrow e^+e^-h$ ) measurements to have little impact in our analysis.

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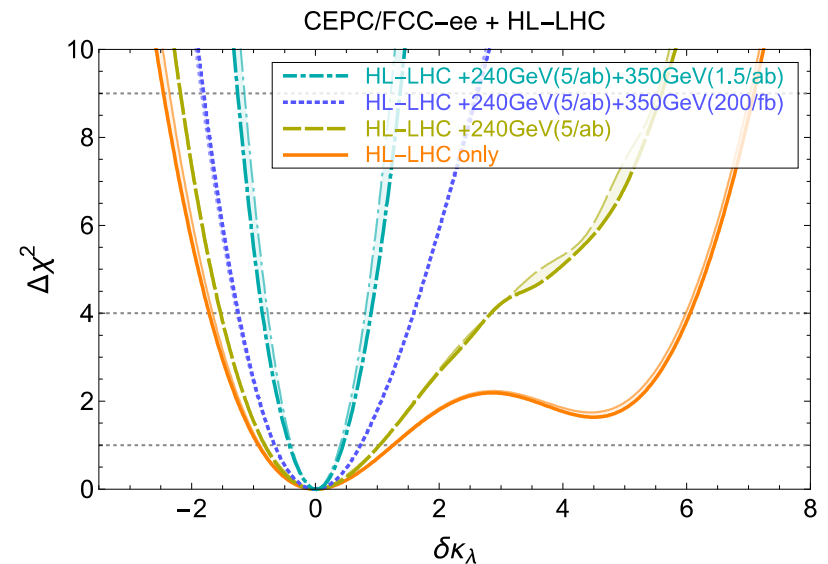
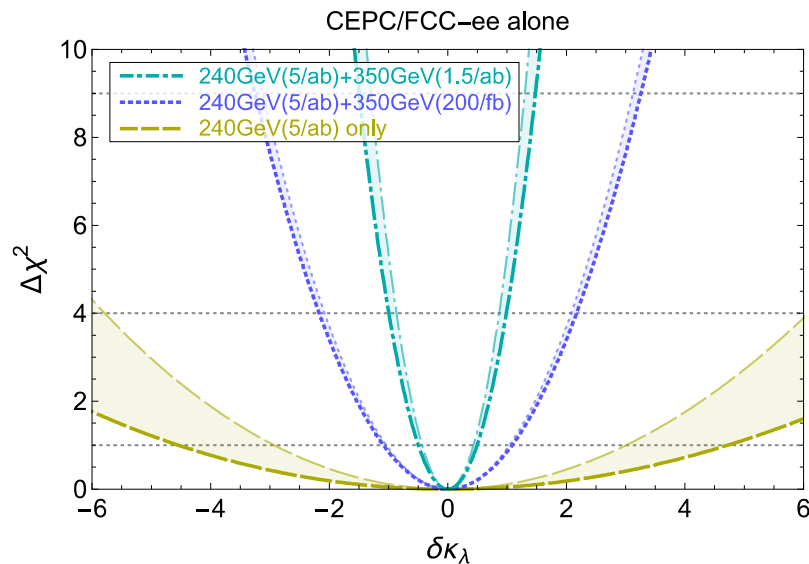
# Low-energy lepton colliders



- 2 main production modes
- 4 angular distributions in Zh
- 2 beam polarization runs ( $\pm 80\%$ ,  $\mp 30\%$ )
- 7+2 decay modes ZZ, WW,  $\gamma\gamma$ ,  $Z\gamma$ ,  $\tau\tau$ , bb, gg, (cc,  $\mu\mu$ )
- no flat direction expected

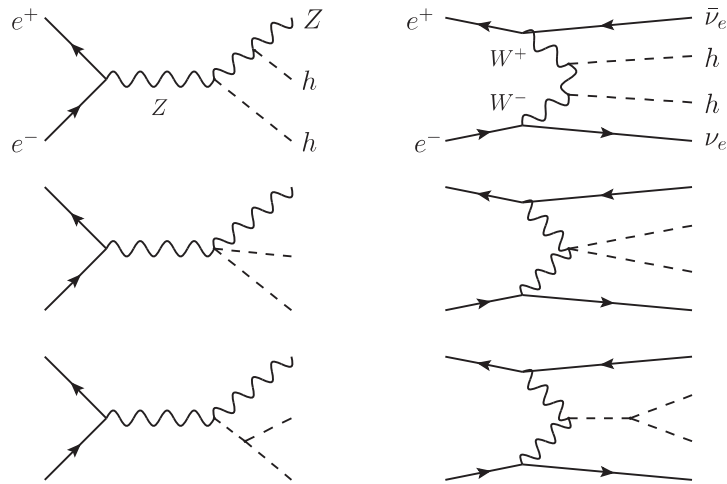
Durieux, Grojean, Gu, Liu, Panico, Riembau, Vantalon, DV [1711.03978]

# Low-energy lepton colliders

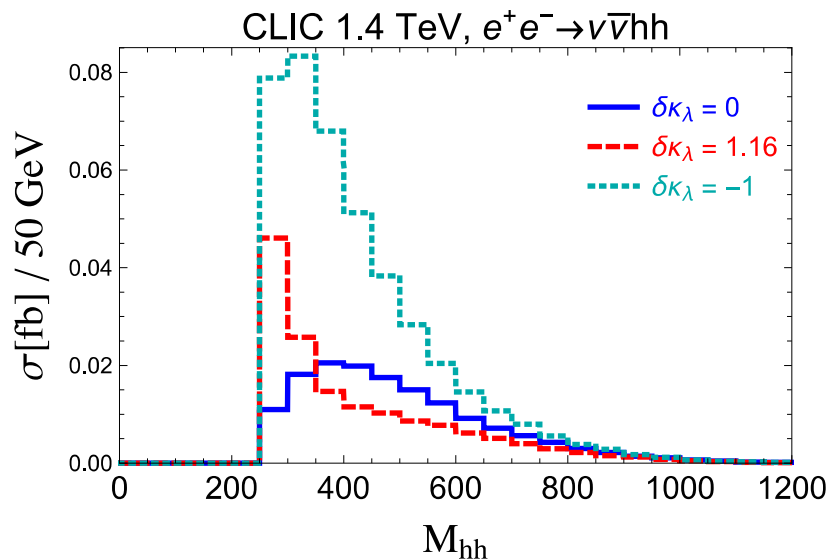
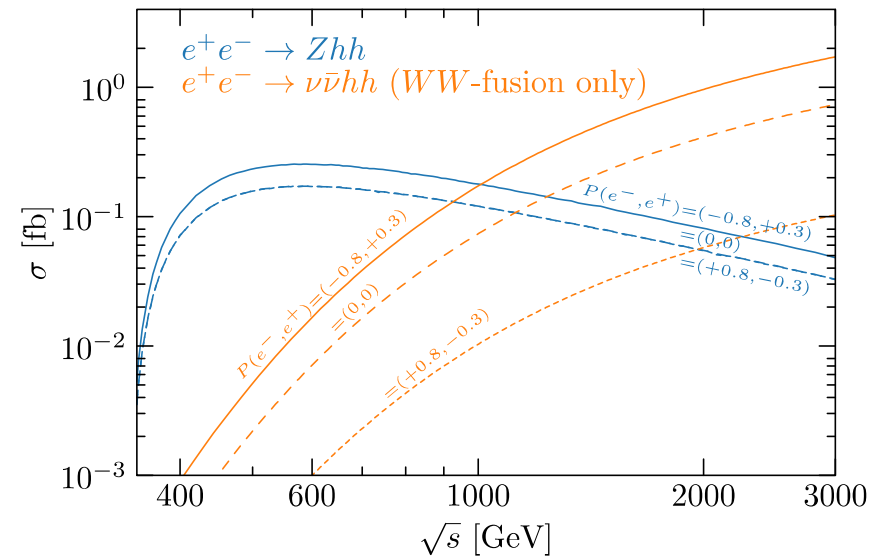


- shaded band reflects different assumptions on TGCs → large impact! global analysis needed to constrain single-Higgs deformations
- low-energy circular collider needs either combination with HL-LHC or 2 energy runs to set meaningful bounds

# High-energy lepton colliders



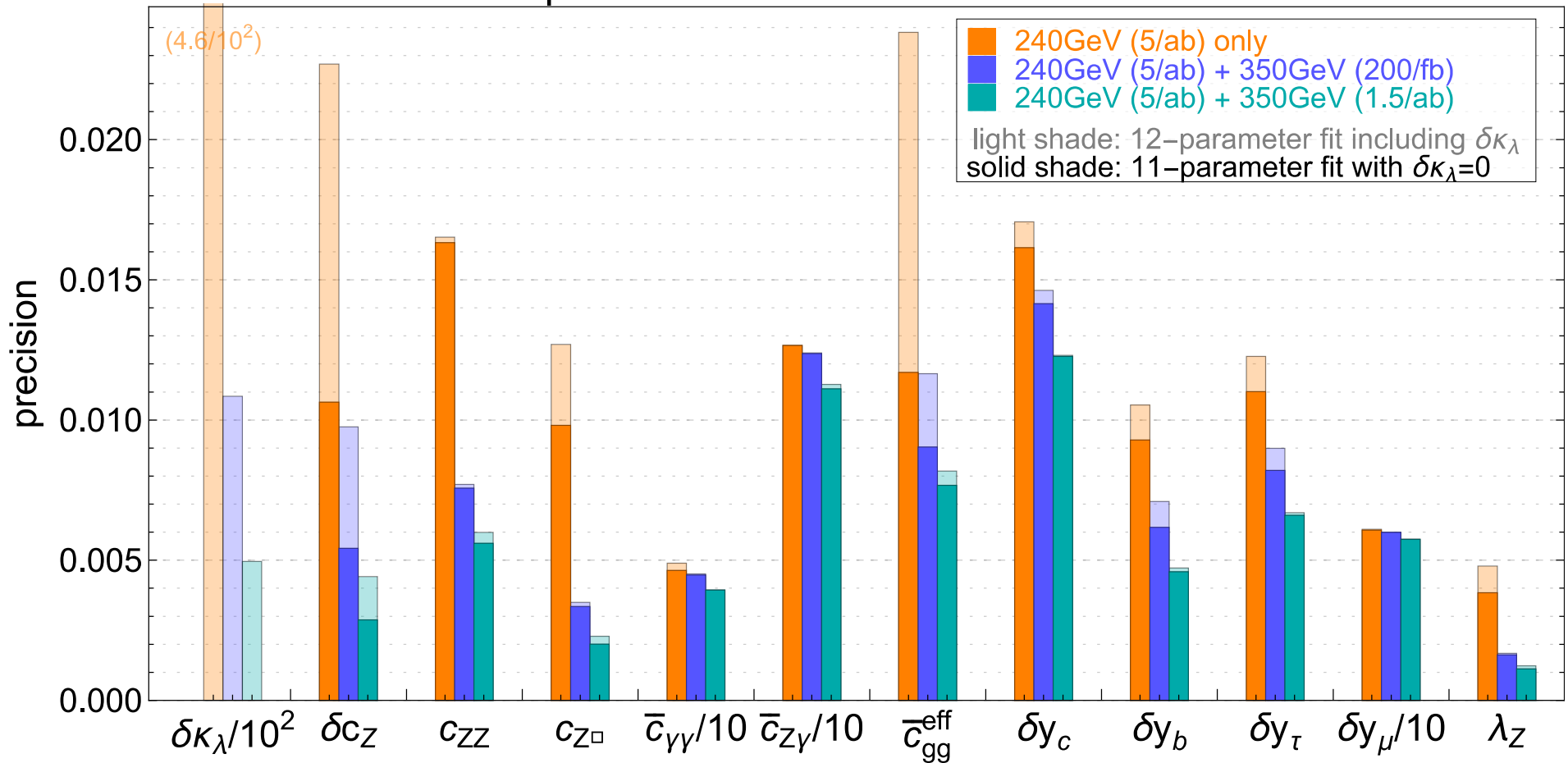
more sensitive to  $\delta\kappa_\lambda > 0$     more sensitive to  $\delta\kappa_\lambda < 0$



- access to double-Higgs production, ZHH / WBF complementary
- differential data in  $m_{hh}$  add useful info
- exploit impact of polarization at ILC
- dependence on  $\delta\kappa_\lambda$  stronger at low energy  $\rightarrow$  ILC runs at 500GeV and 1TeV maximize sensitivity

# Impact on the other couplings

precision reach at CEPC/FCC-ee





# Impact on the other couplings

precision reach at CEPC/FCC-ee (combined with HL-LHC)

