

# Indirect search for CP-violation in the Higgs sector by the precision test of Higgs couplings

---

Mitsunori KUBOTA  
Osaka University

[arXiv: 1808.08770]

Collaborators: M. Aoki<sup>1</sup>, K. Hashino<sup>2,3</sup>, D. Kaneko<sup>1</sup>, S. Kanemura<sup>2</sup>

1: Univ. of Kanazawa, 2: Osaka Univ., 3: Univ. of Toyama

# Introduction

- ◆ Discovered Higgs boson looks like the SM one.
- ◆ CP-violating Higgs sector is motivated by the baryon number asymmetry of the Universe.
- ◆ Until now, there are no sign of non-SM particles.

We focus on the precision test of the discovered Higgs boson to explore the CP-violation in the Higgs sector.

# In this talk,...

- ◆ We consider the two Higgs doublet model (2HDM) with softly broken  $Z_2$ .

2HDM:

- Simple extension of the SM.
- CP-violation can be introduced.

$Z_2$  sym. : To avoid FCNC at tree level.

[S. L. Glashow and S. Weinberg, PRD15, 1958 (1977)]

$$\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2$$

FCNC: Flavor Changing Neutral Current

- ◆ We analyze the Higgs coupling constants (for  $hVV$ ,  $h\tau\tau$ ,  $hbb$ ,  $hcc$ ) in the CP-conserving (CPC) 2HDM and the CP-violating (CPV) 2HDM.

- ◆ We then compare these results to show whether we can distinguish CPV 2HDM and CPC 2HDM.

# CPV parameter in this model

$$\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2 \text{ under } Z_2.$$

## ◆ Potential of 2HDM (with softly broken $Z_2$ sym.)

$$V = \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\Phi_2|^2 - \{ \mu_3^2 (\Phi_1^\dagger \Phi_2) + h.c. \} \\ + \frac{1}{2} \lambda_1 |\Phi_1|^4 + \frac{1}{2} \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + h.c. \right\}$$

## ◆ Vacuum expectation value

$$\Phi_j = \begin{pmatrix} w_j^+ \\ \frac{1}{\sqrt{2}} (v_j + h_j + iz_j) \end{pmatrix} e^{i\theta_j} \quad (j = 1, 2)$$

$$v^2 \equiv v_1^2 + v_2^2 = (246 \text{ GeV})^2$$

The redefinition of the phases can get  $\theta_j$  to disappear.

Stationary condition

$$\left. \frac{\partial V}{\partial h_1} \right|_0 = 0, \quad \left. \frac{\partial V}{\partial h_2} \right|_0 = 0, \quad \left. \frac{\partial V}{\partial z_1} \right|_0 = 0$$

$$\begin{cases} \mu_1^2 = \frac{v_2}{v_1} \text{Re}(\mu_3^2) - \frac{1}{2} (\lambda_1 v_1^2 + \lambda_{345} v_2^2) \\ \mu_2^2 = \frac{v_1}{v_2} \text{Re}(\mu_3^2) - \frac{1}{2} (\lambda_2 v_2^2 + \lambda_{345} v_1^2) \\ \underline{2 \text{Im}(\mu_3^2) = v_1 v_2 \text{Im}(\lambda_5)} \end{cases}$$

## ◆ Parameters in this model

$$v_1, v_2, \text{Re}(\mu_3^2), \lambda_1, \lambda_2, \lambda_3, \lambda_4, \text{Re}(\lambda_5), \text{Im}(\lambda_5)$$

$$\lambda_{345} \equiv \lambda_3 + \lambda_4 + \text{Re}(\lambda_5)$$

# CP mixing between the neutral scalars

Higgs basis

[Davidson and Haber, PRD72, 035004 (2005)]

$$\begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix} = \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \Phi_1 \\ \Phi_2 \end{pmatrix} \quad \tan \beta = \frac{v_2}{v_1}$$

$$\phi_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + h'_1 + iG^0) \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(h'_2 + ih'_3) \end{pmatrix}$$

◆ Mass matrix:  $\mathcal{M}_{ij}^2 \equiv \partial^2 V / \partial h'_i \partial h'_j |_0$  ( $i, j = 1-3$ )

$$m_{H_1} = 125 \text{ GeV}$$

$$\mathcal{M}^2 = \begin{pmatrix} \mathcal{M}_{11}^2 & \mathcal{M}_{12}^2 & \mathcal{M}_{13}^2 \\ \mathcal{M}_{12}^2 & \mathcal{M}_{22}^2 & \mathcal{M}_{23}^2 \\ \mathcal{M}_{13}^2 & \mathcal{M}_{23}^2 & \mathcal{M}_{33}^2 \end{pmatrix}$$

$$\mathcal{M}_{13}^2, \mathcal{M}_{23}^2 \propto \text{Im}(\lambda_5)$$

$$R^T \mathcal{M}^2 R = \text{diag}(m_{H_1}^2, m_{H_2}^2, m_{H_3}^2)$$

$$\begin{pmatrix} h'_1 \\ h'_2 \\ h'_3 \end{pmatrix} = \begin{pmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{pmatrix} \begin{pmatrix} H_1 \\ H_2 \\ H_3 \end{pmatrix}$$

$h'_1, h'_2$ : CP even,  $h'_3$ : CP odd

$\text{Im}(\lambda_5) \neq 0 \Rightarrow$  CP mixing

# Higgs couplings

$Z_2$  charge assignment in each Type

## ◆ Types of 2HDM

$$\begin{aligned}
 -\mathcal{L}_{Yukawa} = & Y_u \bar{Q}_L (i\sigma_2 \Phi_u^*) u_R \\
 & + Y_d \bar{Q}_L \Phi_d d_R \\
 & + Y_e \bar{L}_L \Phi_e e_R + h.c.
 \end{aligned}$$

	$\Phi_1$	$\Phi_2$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$
Type-I	+	-	+	+	-	-	-
Type-II	+	-	+	+	-	+	+
Type-X	+	-	+	+	-	-	+
Type-Y	+	-	+	+	-	+	-

[Barger, Hewett and Phillips, PRD41, 3421 (1990)]

[Aoki, Kanemura, Tsumura and Yagyu, PRD80, 015017 (2009)]

## ◆ Higgs couplings

$$\mathcal{L}_{H_1 V V}^{2HDM} = \underline{R_{11}} g_{hVV}^{SM} V_\mu V^\mu H_1$$

$$\mathcal{L}_{H_1 f f}^{2HDM} = -g_{hff}^{SM} \bar{\psi}_f (\underline{c_f^s} + i\gamma_5 c_f^p) \psi_f H_1$$

$H_1$ : 125 GeV Higgs  
 $V$ :  $W$  and  $Z$   
 $f$ :  $u$ ,  $d$  and  $e$

$$c_f^s = R_{11} + R_{21} \xi_f$$

$$c_f^p = (-2I_f) R_{31} \xi_f$$

$$I_u = 1/2, I_d = I_e = -1/2$$

	$\xi_u$	$\xi_d$	$\xi_e$
Type-I	$+\cot\beta$	$+\cot\beta$	$+\cot\beta$
Type-II	$+\cot\beta$	$-\tan\beta$	$-\tan\beta$
Type-X	$+\cot\beta$	$+\cot\beta$	$-\tan\beta$
Type-Y	$+\cot\beta$	$-\tan\beta$	$+\cot\beta$

# Numerical analysis

◆ We calculate following values.

$$\triangleright \kappa_V = \frac{g_{H_1 VV}^{2\text{HDM}}}{g_{hVV}^{\text{SM}}} = R_{11}$$

$$\triangleright \frac{\Gamma_{2\text{HDM}}(H_1 \rightarrow f\bar{f})}{\Gamma_{\text{SM}}(h \rightarrow f\bar{f})} \simeq (c_f^s)^2 + (c_f^p)^2$$

◆ Parameters

These are independent of  $m_{H^\pm}, \text{Re}[\mu_3^2]$  at the tree level.

$$\underline{v, m_{H_1}, \tilde{m}_H, \tilde{m}_A, m_{H^\pm}, \text{Re}[\mu_3^2], \kappa_V, \tan \beta, \text{Im}[\lambda_5]}$$

$v$	$= 246 \text{ GeV}$
$m_{H_1}$	$= 125 \text{ GeV}$
$\tilde{m}_H$	$= 200 \text{ GeV}$
$\tilde{m}_A$	$= 250 \text{ GeV}$

$\kappa_V, \tan \beta, \text{Im}[\lambda_5]$  are treated as variables.

$\tilde{m}_H, \tilde{m}_A$  ( $\text{Im}(\lambda_5) \rightarrow 0$ )

$\rightarrow$  Mass eigenvalues of  $H_2, H_3$

[Keus, King, Moretti and Yagyu, JHEP 04, 048 (2016)]

# Result

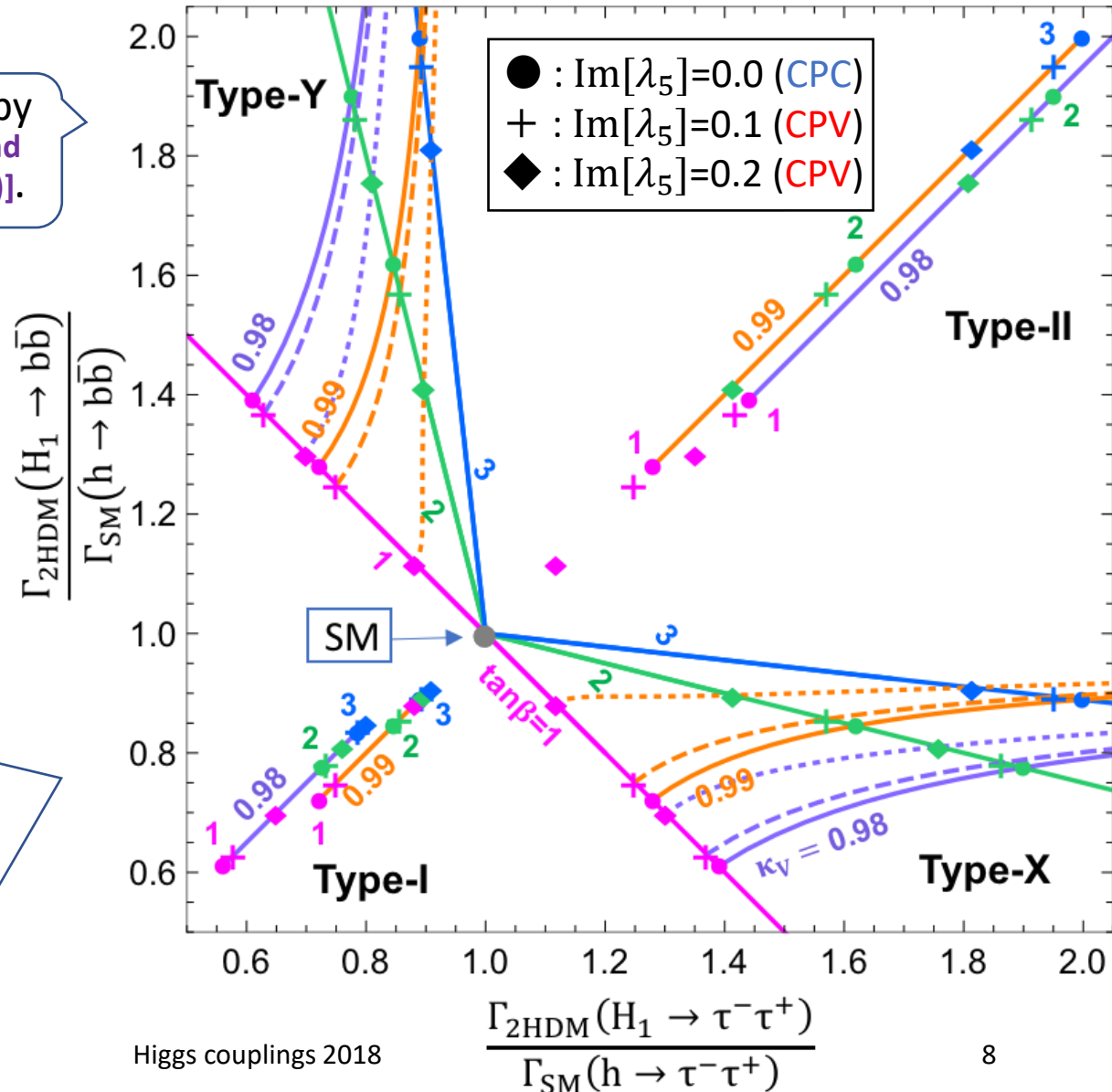
[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

$$R_{21} \leq 0$$

CP-conserving case is plotted by  
[Kanemura, Tsumura, Yagyu and  
Yokoya, PRD90, 075001 (2014)].

In our parameter set,  
Type-II and Y are  
disfavored by  $b \rightarrow s\gamma$ ,  
and EDM constraint  
for Type-I is stricter  
than one for Type-X.

[Aoki, Kanemura, Tsumura  
and Yagyu, PRD80, 015017]  
[Cheung, Lee, Senaha and  
Tseng, JHEP 06, 149 (2014)]



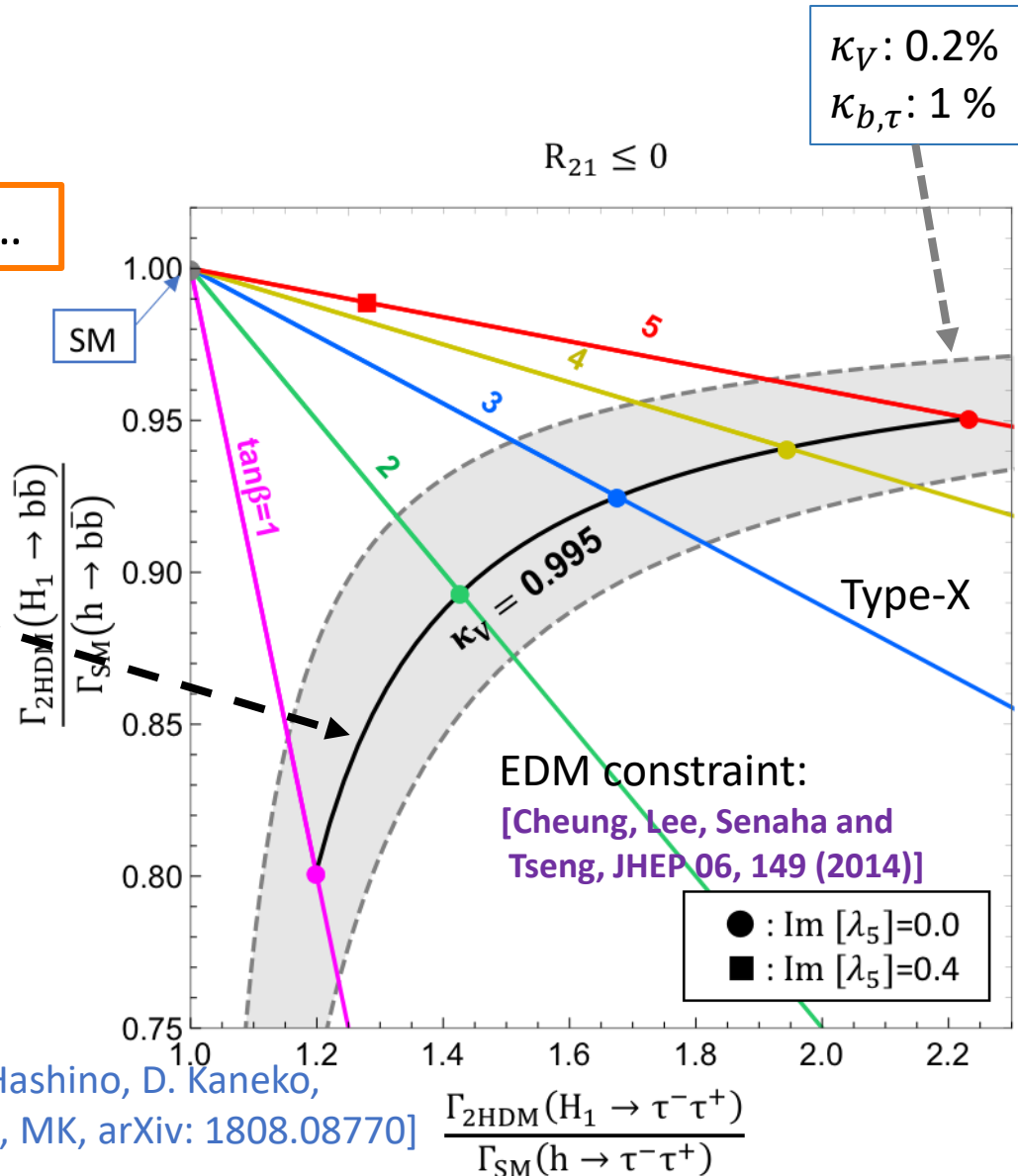


# Result

For instance, if  $\kappa_V$  measures 0.995, ...

- In the CP-conserving 2HDM, the ratio of decay rate for the fermion should be on the black curve.

$\text{Im}[\lambda_5] = 0$



[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

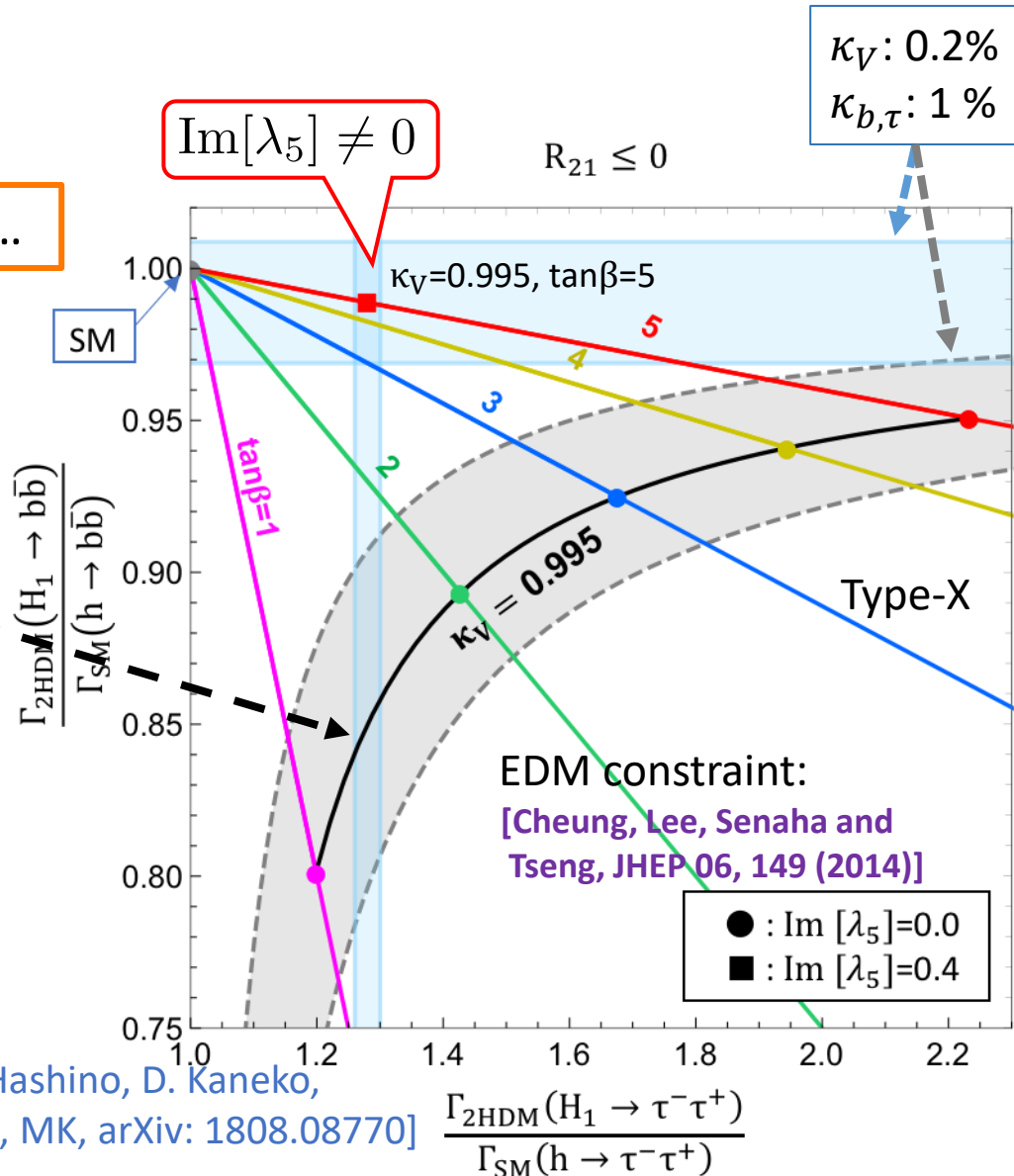
# Result

For instance, if  $\kappa_V$  measures 0.995, ...

- In the CP-conserving 2HDM, the ratio of decay rate for the fermion should be on the black curve.

$\text{Im}[\lambda_5] = 0$

$\text{Im}[\lambda_5] \neq 0$



[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

# Result

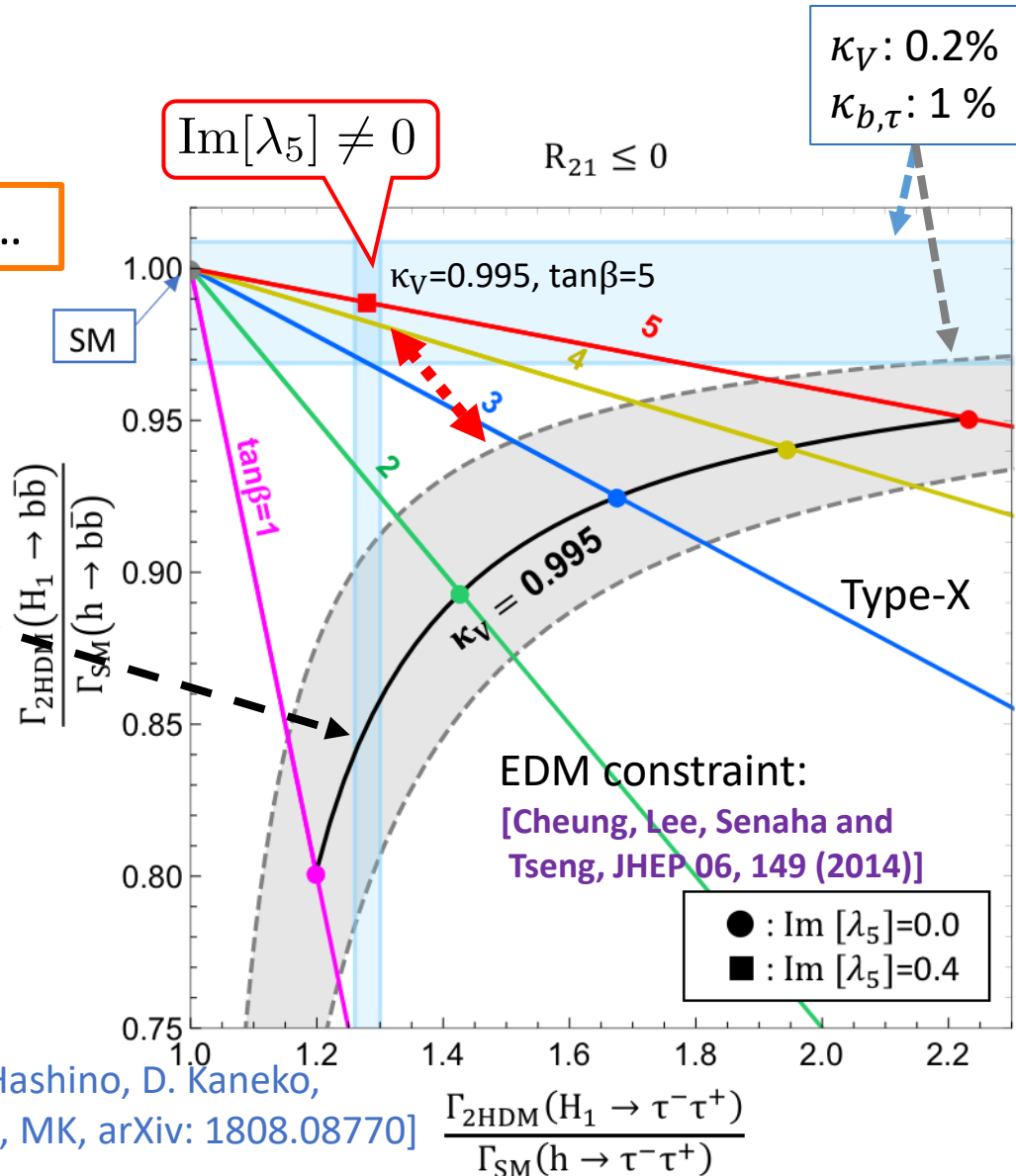
For instance, if  $\kappa_V$  measures 0.995, ...

- In the CP-conserving 2HDM, the ratio of decay rate for the fermion should be on the black curve.

$$\text{Im}[\lambda_5] = 0$$

The deviation from the black curve is indirect effect of CP-violation.

[M. Aoki, K. Hashino, D. Kaneko, S. Kanemura, MK, arXiv: 1808.08770]



# Result

ILC250 ( $2ab^{-1}$ )  $\kappa_Z: 0.38\%$   
 [K. Fujii, et al., arXiv: 1710.07621]  $\kappa_b: 1.8\%$   
 $\kappa_\tau: 1.9\%$

$8ab^{-1}$   
 $\kappa_V: 0.2\%$   
 $\kappa_{b,\tau}: 1\%$

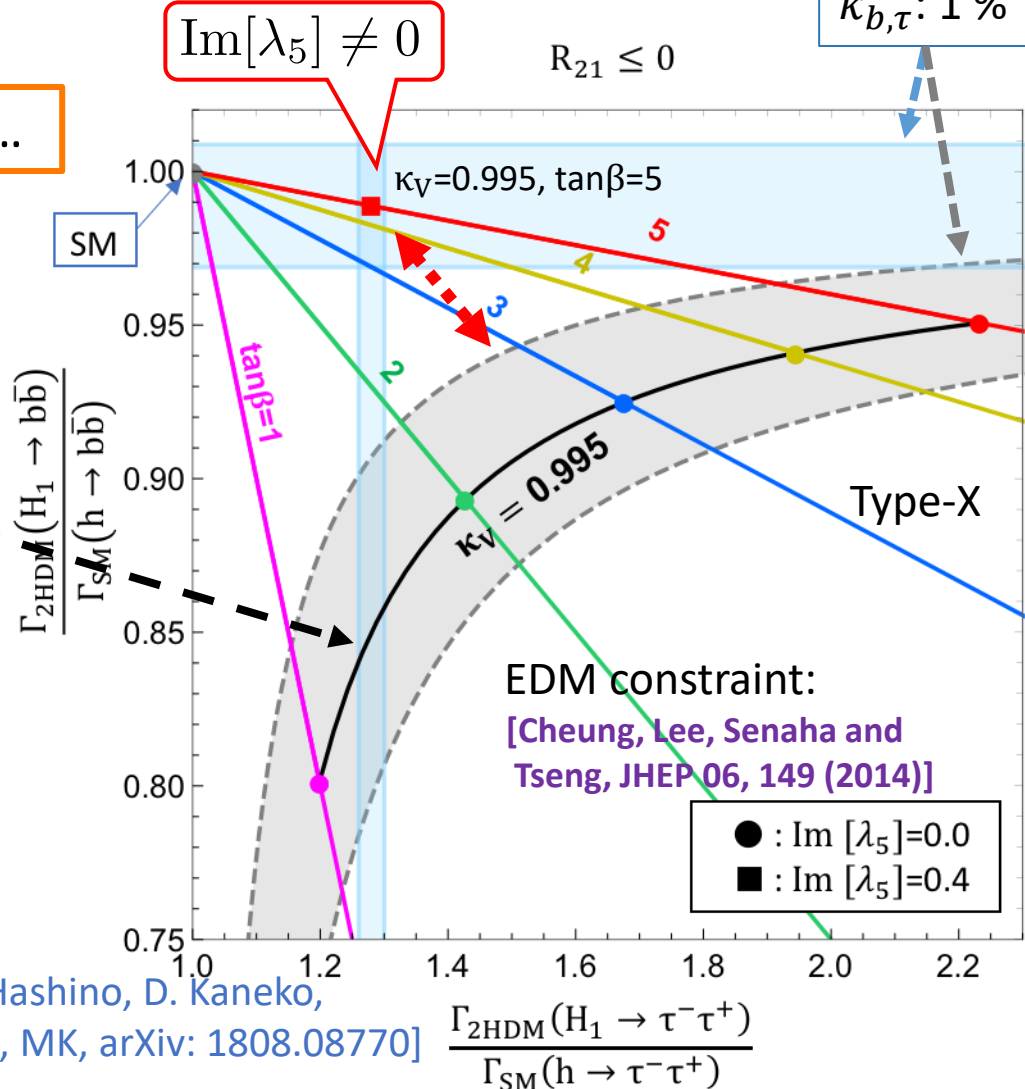
For instance, if  $\kappa_V$  measures 0.995, ...

➤ In the CP-conserving 2HDM, the ratio of decay rate for the fermion should be on the black curve.

$\text{Im}[\lambda_5] = 0$

The deviation from the black curve is indirect effect of CP-violation.

[M. Aoki, K. Hashino, D. Kaneko, S. Kanemura, MK, arXiv: 1808.08770]



# Summary

- ◆ In this talk, we analyze the CP-violating effect on the Higgs coupling constants in the 2HDM from the viewpoint of indirect search.
- ◆ The prediction of the Higgs couplings in the CP-violating 2HDM can be certainly deviated from the CP-conserving one.
- ◆ By measuring the Higgs couplings very precisely we are able to extract the information of the CP-violation in the scalar sector.

# Back up

# Current data

[ATLAS-CONF-2018-031]

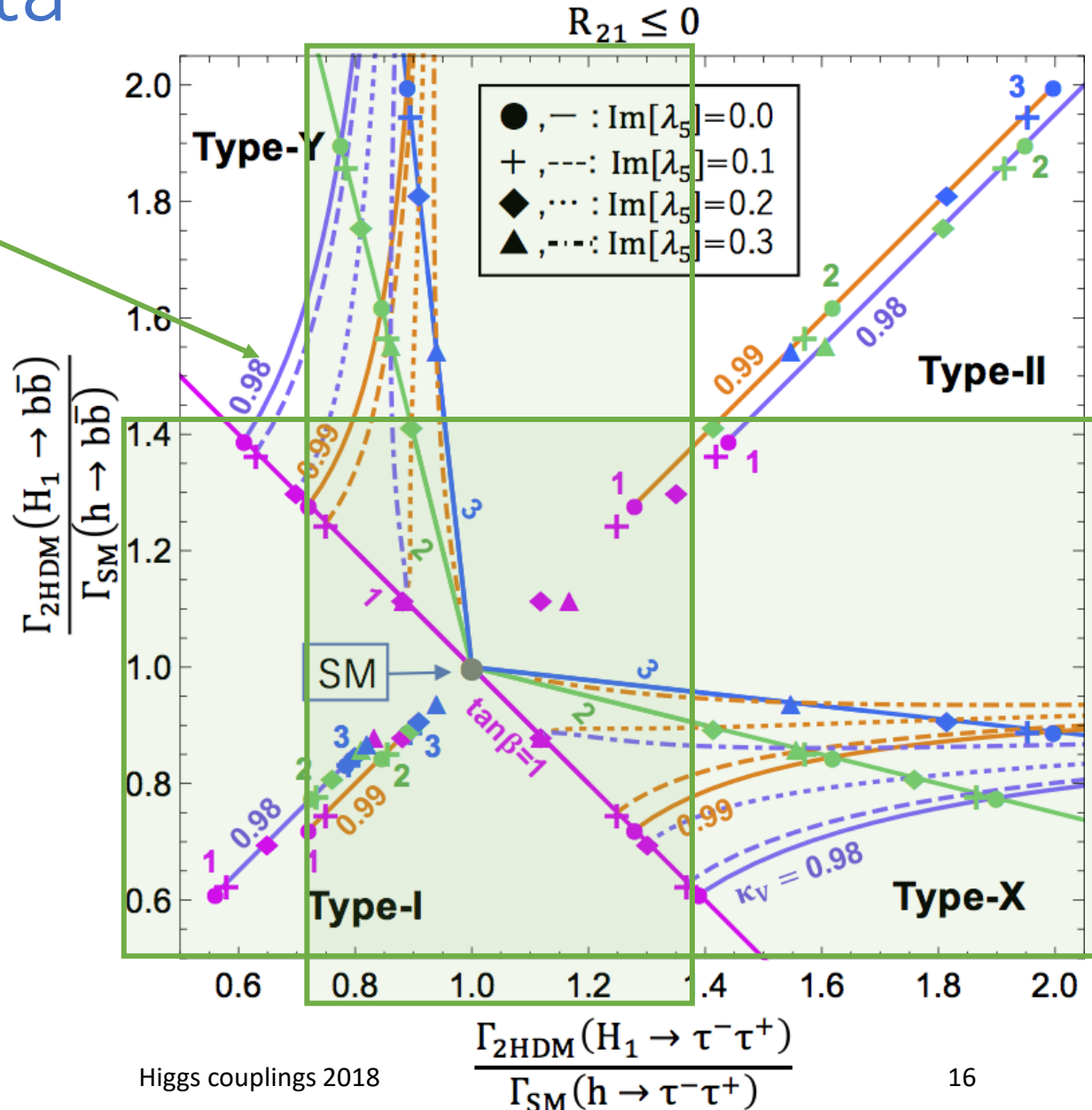
Parameter	(a) no BSM	(b) with BSM
$\kappa_Z$	$1.07 \pm 0.10$	restricted to $\kappa_Z \leq 1$
$\kappa_W$	$1.07 \pm 0.11$	restricted to $\kappa_W \leq 1$
$\kappa_b$	$0.97^{+0.24}_{-0.22}$	$0.85^{+0.13}_{-0.14}$
$\kappa_t$	$1.09^{+0.15}_{-0.14}$	$1.05^{+0.14}_{-0.13}$
$\kappa_\tau$	$1.02^{+0.17}_{-0.16}$	$0.95 \pm 0.13$
$\kappa_\gamma$	$1.02^{+0.09}_{-0.12}$	$0.98^{+0.05}_{-0.08}$
$\kappa_g$	$1.00^{+0.12}_{-0.11}$	$0.97^{+0.10}_{-0.09}$
$B_{\text{BSM}}$	-	$< 0.26$ at 95% CL

# Current data

[M. Aoki, K. Hashino, D. Kaneko, S. Kanemura, MK, arXiv: 1808.08770]

[ATLAS-CONF-2018-031]

Parameter	(a) no BSM
$\kappa_Z$	$1.07 \pm 0.10$
$\kappa_W$	$1.07 \pm 0.11$
$\kappa_b$	$0.97^{+0.24}_{-0.22}$
$\kappa_t$	$1.09^{+0.15}_{-0.14}$
$\kappa_\tau$	$1.02^{+0.17}_{-0.16}$
$\kappa_\gamma$	$1.02^{+0.09}_{-0.12}$
$\kappa_g$	$1.00^{+0.12}_{-0.11}$
$B_{\text{BSM}}$	-





# Current data

[CMS-PAS-HIG-17-031]

$BR_{inv.} = 0$				$BR_{inv.} > 0, \kappa_V < 1$					
Parameter	Best fit	Uncertainty		Parameter	Best fit	Uncertainty			
		Stat.	Syst.			Stat.	Syst.		
$\kappa_Z$	0.99	$+0.11$ $-0.11$ (+0.11) (-0.11)	$+0.09$ $-0.09$ (+0.09) (-0.09)	$+0.06$ $-0.06$ (+0.06) (-0.06)	$\kappa_Z$	0.89	$+0.09$ $-0.08$ (+0.00) (-0.11)	$+0.07$ $-0.07$ (+0.00) (-0.09)	$+0.05$ $-0.04$ (+0.00) (-0.06)
$\kappa_W$	1.12	$+0.13$ $-0.19$ (+0.12) (-0.12)	$+0.10$ $-0.18$ (+0.09) (-0.09)	$+0.08$ $-0.07$ (+0.07) (-0.07)	$\kappa_W$	1.00	$+0.00$ $-0.05$ (+0.00) (-0.12)	$+0.00$ $-0.04$ (+0.00) (-0.09)	$+0.00$ $-0.02$ (+0.00) (-0.07)
$\kappa_t$	1.09	$+0.14$ $-0.14$ (+0.14) (-0.15)	$+0.08$ $-0.08$ (+0.08) (-0.09)	$+0.12$ $-0.12$ (+0.12) (-0.12)	$\kappa_t$	1.12	$+0.17$ $-0.16$ (+0.18) (-0.15)	$+0.09$ $-0.09$ (+0.13) (-0.09)	$+0.14$ $-0.13$ (+0.12) (-0.12)
$\kappa_\tau$	1.01	$+0.17$ $-0.18$ (+0.16) (-0.15)	$+0.11$ $-0.15$ (+0.11) (-0.11)	$+0.12$ $-0.09$ (+0.11) (-0.11)	$\kappa_\tau$	0.91	$+0.13$ $-0.13$ (+0.14) (-0.15)	$+0.08$ $-0.08$ (+0.09) (-0.11)	$+0.11$ $-0.10$ (+0.11) (-0.11)
$\kappa_b$	1.10	$+0.27$ $-0.33$ (+0.25) (-0.23)	$+0.19$ $-0.30$ (+0.19) (-0.17)	$+0.19$ $-0.14$ (+0.17) (-0.15)	$\kappa_b$	0.91	$+0.19$ $-0.16$ (+0.18) (-0.23)	$+0.12$ $-0.11$ (+0.13) (-0.17)	$+0.14$ $-0.11$ (+0.13) (-0.15)
$\kappa_g$	1.14	$+0.15$ $-0.13$ (+0.14) (-0.12)	$+0.10$ $-0.09$ (+0.10) (-0.09)	$+0.11$ $-0.09$ (+0.10) (-0.09)	$\kappa_g$	1.17	$+0.18$ $-0.14$ (+0.17) (-0.12)	$+0.11$ $-0.10$ (+0.13) (-0.09)	$+0.14$ $-0.11$ (+0.10) (-0.09)
$\kappa_\gamma$	1.07	$+0.15$ $-0.18$ (+0.12) (-0.12)	$+0.10$ $-0.17$ (+0.10) (-0.10)	$+0.11$ $-0.07$ (+0.07) (-0.07)	$\kappa_\gamma$	0.96	$+0.09$ $-0.08$ (+0.08) (-0.12)	$+0.06$ $-0.06$ (+0.07) (-0.09)	$+0.07$ $-0.05$ (+0.05) (-0.07)
					$BR_{inv.}$	0.04	$+0.09$ $+0.00$ (+0.08) (+0.00)	$+0.03$ $-0.03$ (+0.04) (-0.00)	$+0.08$ $-0.00$ (+0.07) (-0.00)
					$BR_{undet.}$	0.00	$+0.09$ $+0.00$ (+0.20) (+0.00)	$+0.08$ $-0.00$ (+0.17) (-0.00)	$+0.03$ $-0.00$ (+0.11) (-0.00)

# In this talk,...

- ◆ We consider the 2HDM with softly broken  $Z_2$ .

## 2HDM

- Simple extension of the SM.
  - CP-violation can be introduced.
- ◆ We analyze the Higgs coupling constants ( $hVV, h\tau\tau, hbb, hcc$ ) in the CP-conserving 2HDM and the CP-violating 2HDM.
  - ◆ We then compare these results.

$Z_2$  sym. : To avoid FCNC at tree level.

[S. L. Glashow and S. Weinberg, PRD15, 1958 (1977)]

## 2HDM with CPV

[T. D. Lee, PRD8, 1226 (1973)]

[J. F. Gunion and H. E Haber, PRD72, 095002 (2005)]

[I. F. Ginzburg and M. Krawczyk, PRD72, 115013 (2005)]

[G. C. Branco, P. M. Ferreira, L. Lavoura, M. N. Rebelo, M. Sher and J. P. Silva, PR516, 1 (2012)]

[B. Grzadkowski, O. M. Ogreid and P. Osland, JHEP 11, 084 (2014)]

[D. Fontes, M. Mühlleitner, J. C. Romão, R. Santos, J. P. Silva and J. Wittbrodt, JHEP 02, 073 (2018)]

and so on.

# 2HDM with softly broken $Z_2$

## ◆ Ratio of decay rate

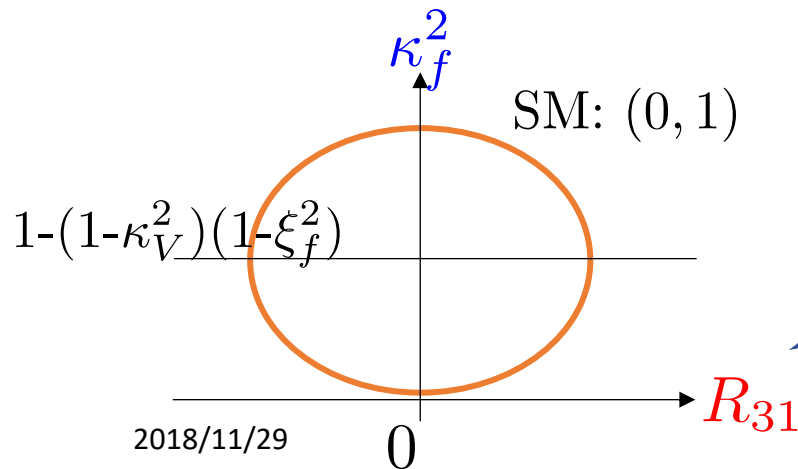
$$\kappa_f^2 \equiv \frac{\Gamma_{2HDM}(h \rightarrow f\bar{f})}{\Gamma_{SM}(h \rightarrow f\bar{f})} \simeq (c_f^s)^2 + (c_f^p)^2$$

$$\kappa_V \equiv R_{11}$$

$$R_{11}^2 + R_{21}^2 + R_{31}^2 = 1$$

$$= (R_{11} + R_{21}\xi_f)^2 + (R_{31}\xi_f)^2$$

$$\Rightarrow \frac{\left(\kappa_f^2 - 1 + (1 - \kappa_V^2)(1 - \xi_f^2)\right)^2}{4\kappa_V^2 \xi_f^2 (1 - \kappa_V^2)} + \frac{R_{31}^2}{1 - \kappa_V^2} = 1 \text{ : Ellipse}$$



$\text{Im}(\lambda_5)$  increase

$\rightarrow |R_{31}|$  increase

# 2HDM with softly broken $Z_2$

$$\hat{\phi}_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + h'_1 + iG^0) \end{pmatrix}, \quad \hat{\phi}_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(h'_2 + ih'_3) \end{pmatrix} \quad \begin{pmatrix} h'_1 \\ h'_2 \\ h'_3 \end{pmatrix} = R \begin{pmatrix} H_1 \\ H_2 \\ H_3 \end{pmatrix}$$

- CP conserving case (  $\text{Im}(\lambda_5) = 0$  ), for the mixing states  $(h'_1, h'_2, h'_3)$ ,

$$\mathcal{M}_{CPC}^2 = \begin{pmatrix} m_h^2 s_{\beta-\alpha}^2 + m_H^2 c_{\beta-\alpha}^2 & \frac{1}{2}(m_h^2 - m_H^2) s_{2(\beta-\alpha)} & 0 \\ \frac{1}{2}(m_h^2 - m_H^2) s_{2(\beta-\alpha)} & m_h^2 c_{\beta-\alpha}^2 + m_H^2 s_{\beta-\alpha}^2 & 0 \\ 0 & 0 & m_A^2 \end{pmatrix}$$

mass eigenstates

- CP violating case (  $\text{Im}(\lambda_5) \neq 0$  ),

↓ tilde

$$\mathcal{M}^2 = \begin{pmatrix} \tilde{m}_h^2 s_{\beta-\tilde{\alpha}}^2 + \tilde{m}_H^2 c_{\beta-\tilde{\alpha}}^2 & \frac{1}{2}(\tilde{m}_h^2 - \tilde{m}_H^2) s_{2(\beta-\tilde{\alpha})} & -\frac{1}{2}v^2 \text{Im}(\lambda_5) s_{2\beta} \\ \frac{1}{2}(\tilde{m}_h^2 - \tilde{m}_H^2) s_{2(\beta-\tilde{\alpha})} & \tilde{m}_h^2 c_{\beta-\tilde{\alpha}}^2 + \tilde{m}_H^2 s_{\beta-\tilde{\alpha}}^2 & -\frac{1}{2}v^2 \text{Im}(\lambda_5) c_{2\beta} \\ -\frac{1}{2}v^2 \text{Im}(\lambda_5) s_{2\beta} & -\frac{1}{2}v^2 \text{Im}(\lambda_5) c_{2\beta} & \tilde{m}_A^2 \end{pmatrix}$$

- Parameters in this model

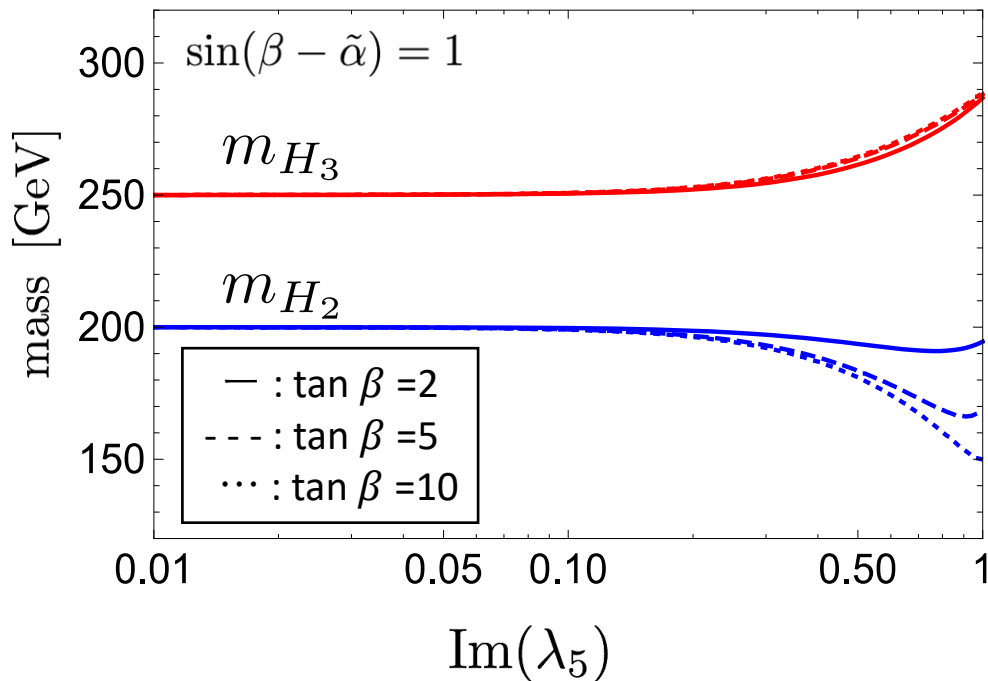
[Kanemura and Yagyu, Phys.Lett. B751 (2015) 289-296]

[Keus, King, Moretti and Yagyu, JHEP 04, 048 (2016)]

$$v(= 246 \text{ GeV}), m_{H_1}(= 125 \text{ GeV}), M, m_{H^\pm}, \tilde{m}_H, \tilde{m}_A, \kappa_V, \tan \beta, \text{Im}(\lambda_5)$$

# 2HDM with softly broken $Z_2$

◆ Mass dimensional parameters  $\tilde{m}_H, \tilde{m}_A$



$v$	$= 246 \text{ GeV},$
$m_h$	$= 125 \text{ GeV},$
$\tilde{m}_H$	$= 200 \text{ GeV},$
$\tilde{m}_A$	$= 250 \text{ GeV}$

When  $\text{Im}(\lambda_5)$  is small,  
 $\tilde{m}_H \approx m_{H_2}, \tilde{m}_A \approx m_{H_3}$

Mass eigenvalue

$\tilde{m}_H, \tilde{m}_A (\text{Im}(\lambda_5) \rightarrow 0)$   
 $\rightarrow$  Mass eigenvalues

# Result

## ◆ Input parameters

$$\begin{aligned}
 v &= 246 \text{ GeV}, \\
 m_{H_1} &= 125 \text{ GeV}, \\
 \tilde{m}_H &= 200 \text{ GeV}, \\
 \tilde{m}_A &= 250 \text{ GeV}
 \end{aligned}$$

$\tilde{m}_H, \tilde{m}_A$  ( $\text{Im}(\lambda_5) \rightarrow 0$ )  
 $\rightarrow$  Mass eigenvalues of  $H_2, H_3$   
 [Keus, King, Moretti and Yagyu, JHEP 04, 048 (2016)]

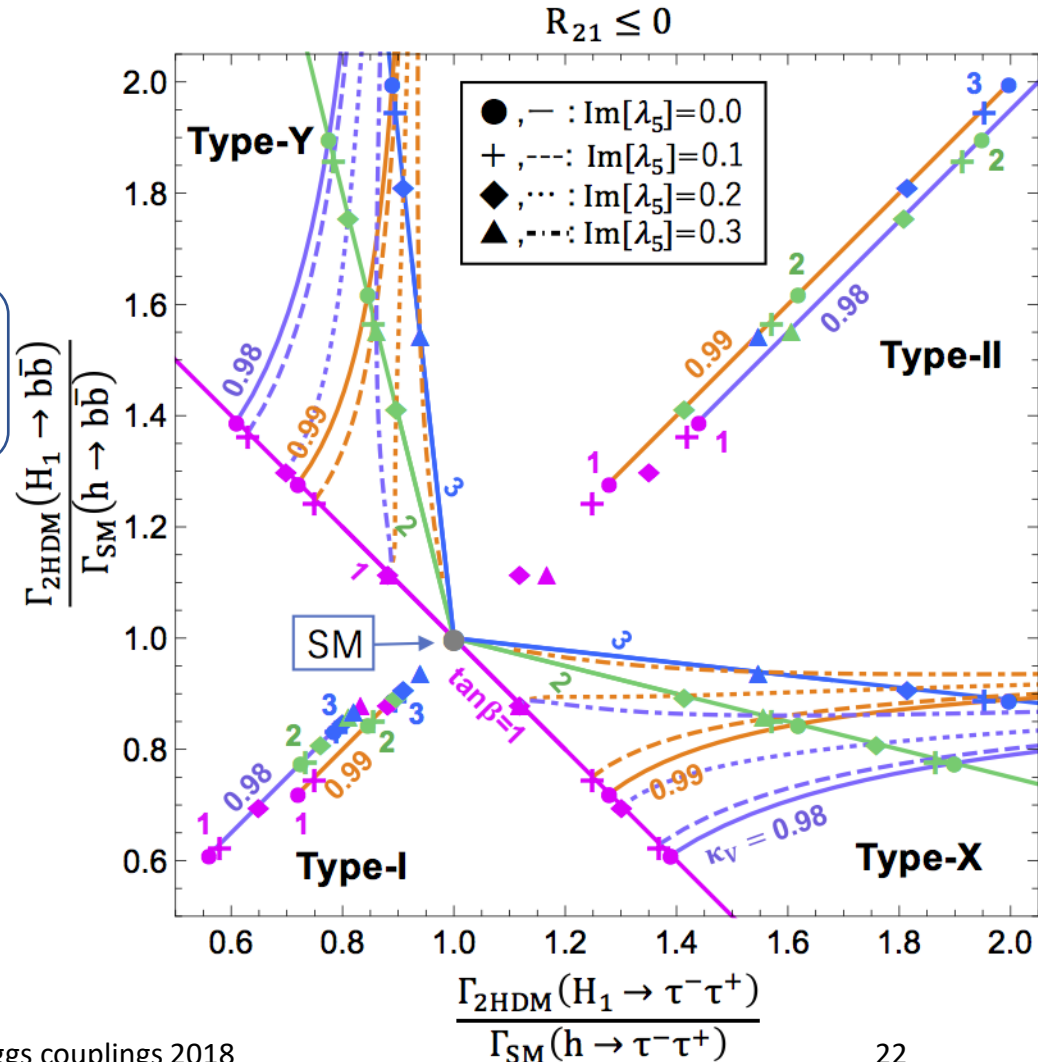
$\kappa_V, \tan \beta, \text{Im}[\lambda_5]$   
 are variables.

They are independent of  
 $\text{Re}(\mu_3^2), m_{H^\pm}$  at the tree level

CP-conserving case is plotted by  
 [Kanemura, Tsumura, Yagyu and Yokoya, PRD90, 075001 (2014)]

2018/11/29

$$\begin{aligned}
 \triangleright \kappa_V &= \frac{g_{H_1 VV}^{2\text{HDM}}}{g_{hVV}^{\text{SM}}} = R_{11} \\
 \triangleright \frac{\Gamma_{2\text{HDM}}(H_1 \rightarrow f\bar{f})}{\Gamma_{\text{SM}}(h \rightarrow f\bar{f})} &\simeq (c_f^s)^2 + (c_f^p)^2
 \end{aligned}$$



Higgs couplings 2018

22

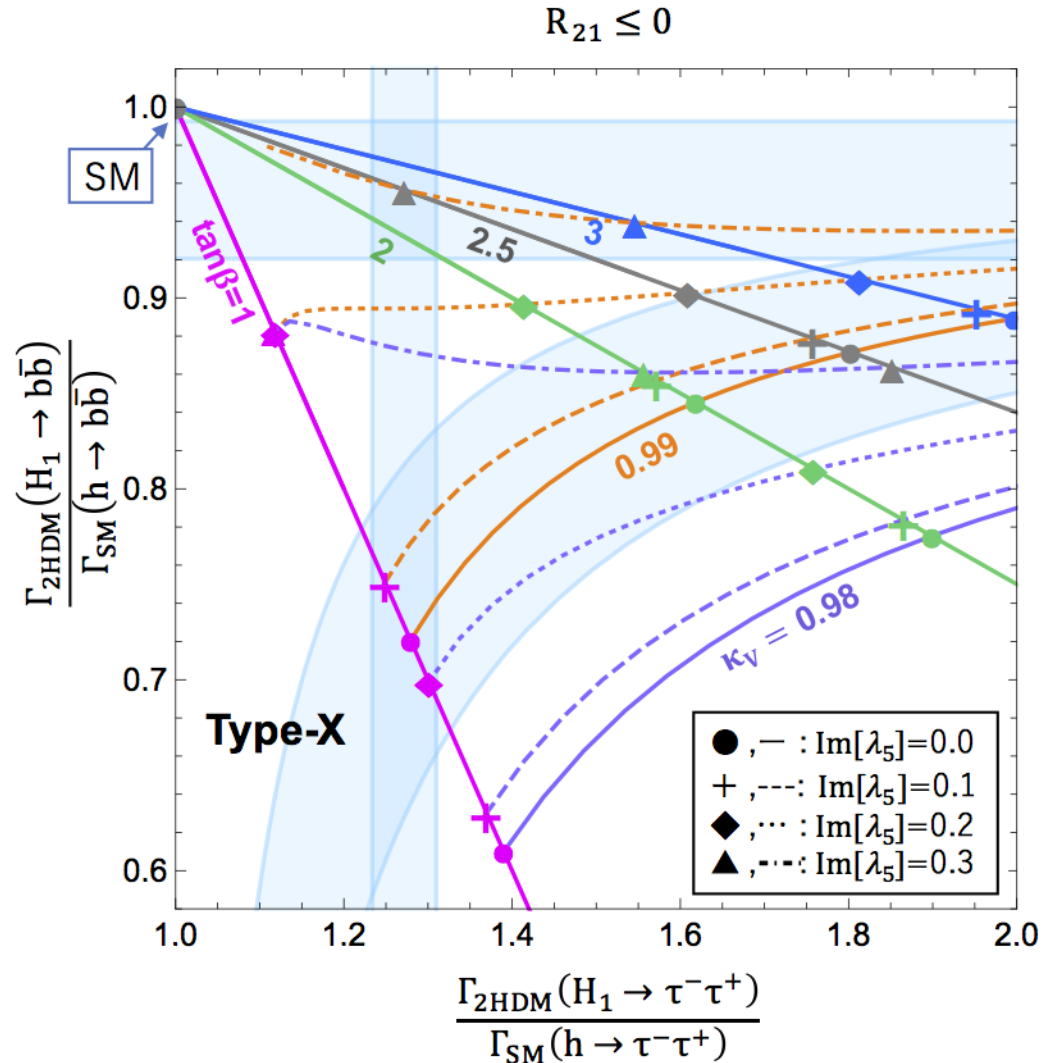
# Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

## ◆ ILC prospect

[K. Fujii, et al., arXiv: 1710.07621]

	ILC250	+ILC500
	$\kappa$ fit	$\kappa$ fit
$g(hbb)$	1.8	0.60
$g(hcc)$	2.4	1.2
$g(hgg)$	2.2	0.97
$g(hWW)$	1.8	0.40
$g(h\tau\tau)$	1.9	0.80
$g(hZZ)$	0.38	0.30
$g(h\gamma\gamma)$	1.1	1.0
$g(h\mu\mu)$	5.6	5.1
$g(h\gamma Z)$	16	16

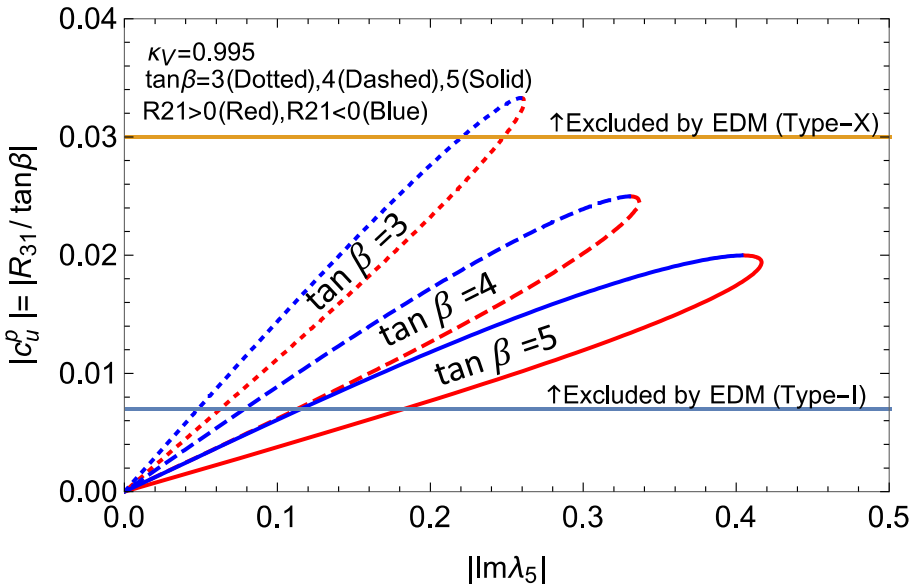


# Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

Sensitivity:  $\kappa_V: 0.2\%$   
 $\kappa_f: 1\%$

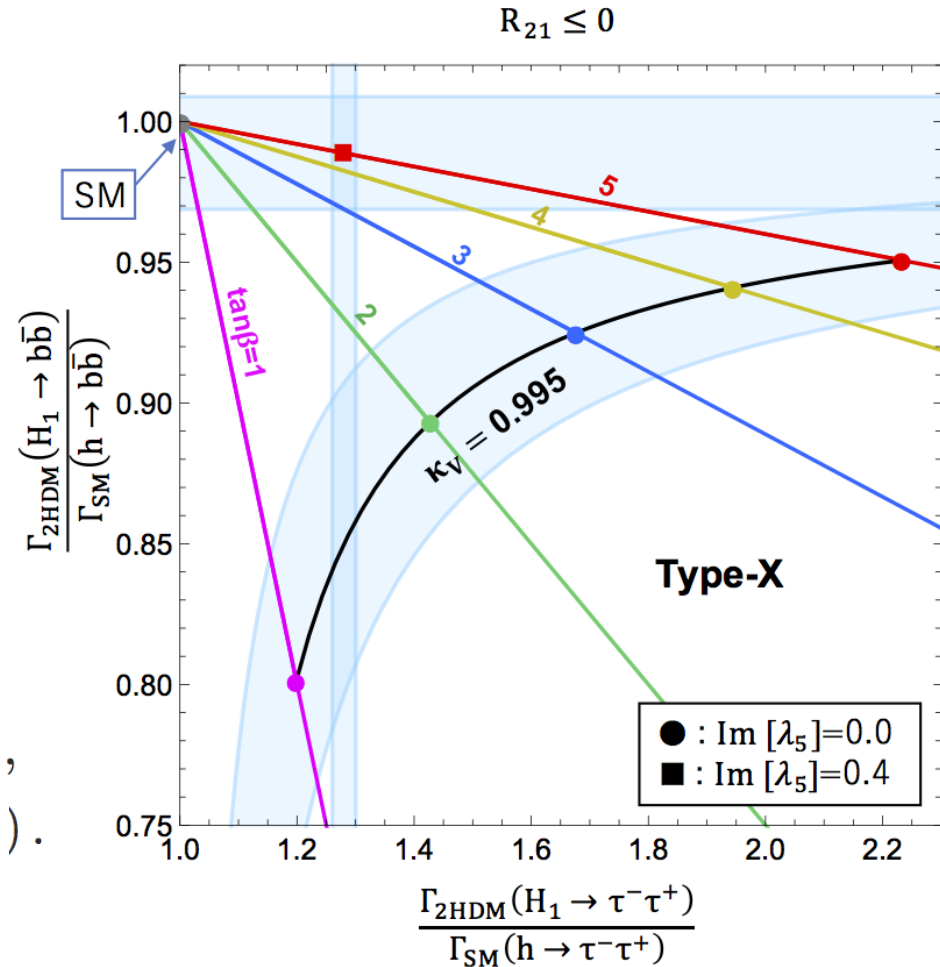
## ◆ EDM constraint (Type-X ( $R_{21} \leq 0$ ))



$$|C_u^P| \lesssim \begin{matrix} 7 \times 10^{-3} \text{ (I)}, & 2 \times 10^{-2} \text{ (II)}, \\ 3 \times 10^{-2} \text{ (X)}, & 6 \times 10^{-3} \text{ (Y)}. \end{matrix}$$

[Cheung, Lee, Senaha and Tseng, JHEP 06, 149 (2014)]

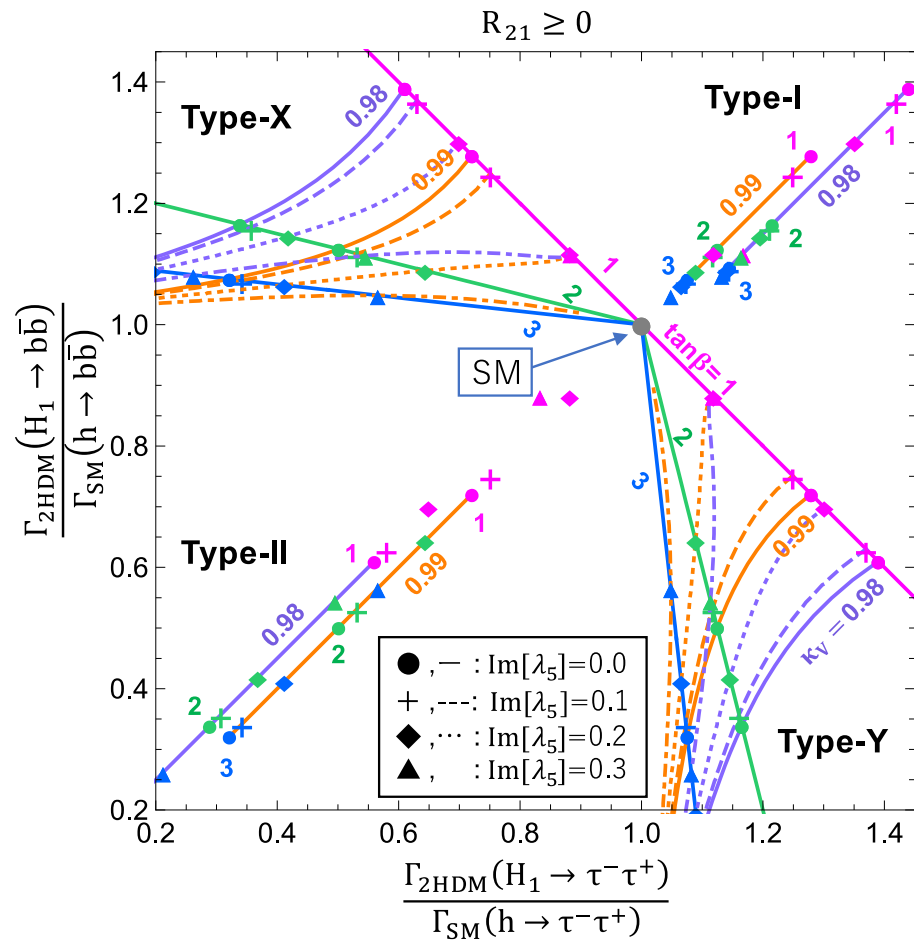
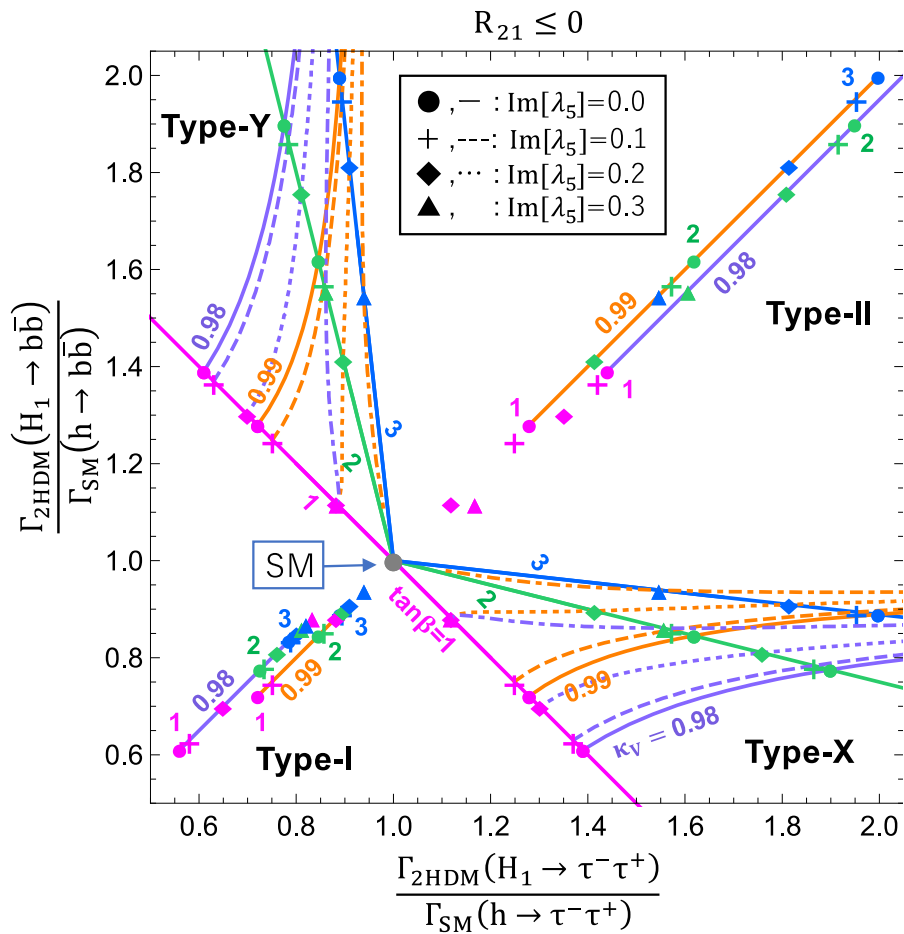
[Keus, King, Moretti and Yagyu, JHEP 04, 048 (2016)]





# Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]



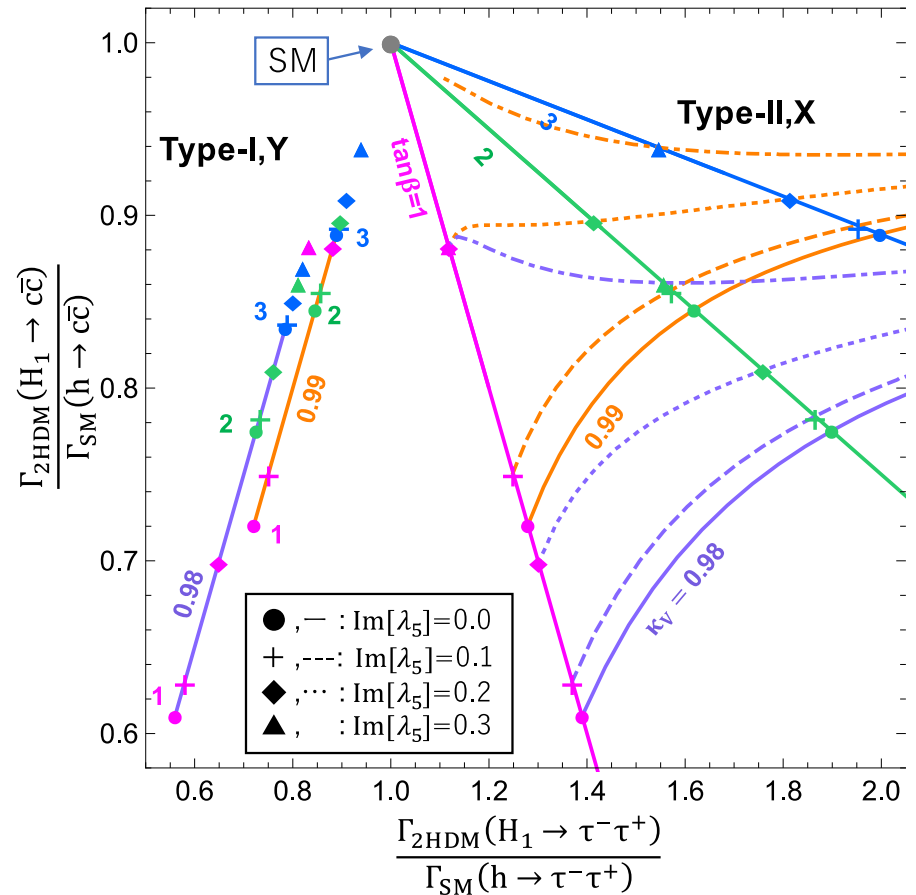
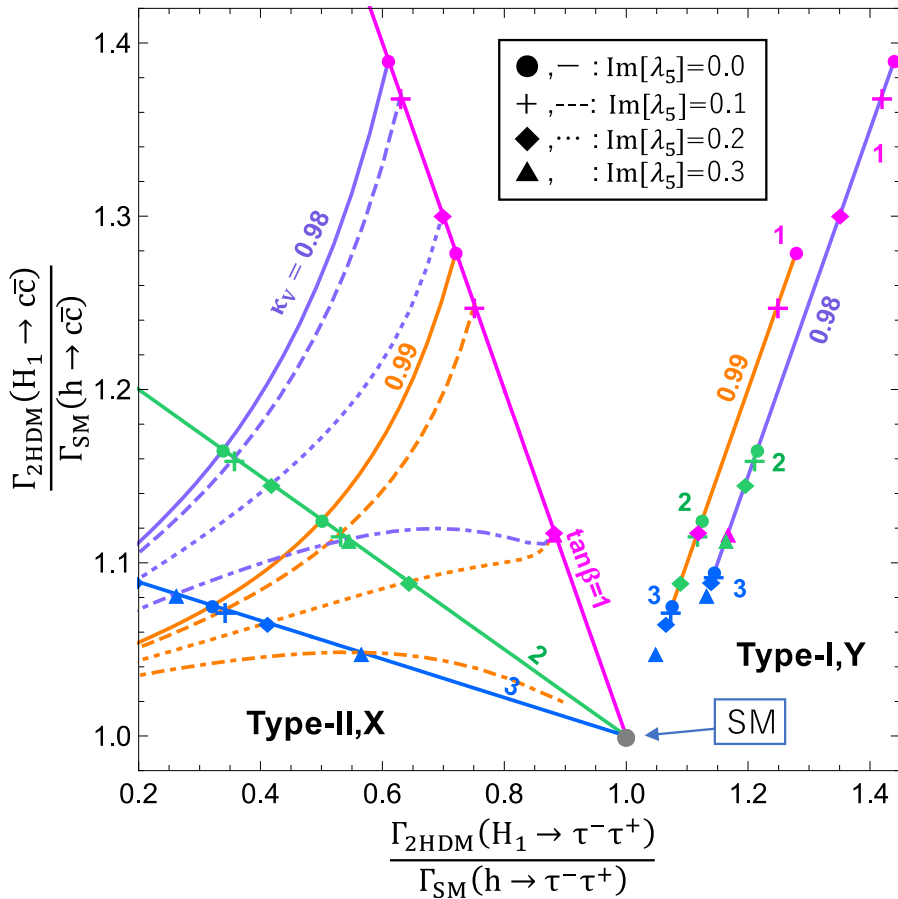
$hb\bar{b}-h\tau\tau$

# Result

[M. Aoki, K. Hashino, D. Kaneko, S. Kanemura, MK, arXiv: 1808.08770]

$R_{21} \geq 0$

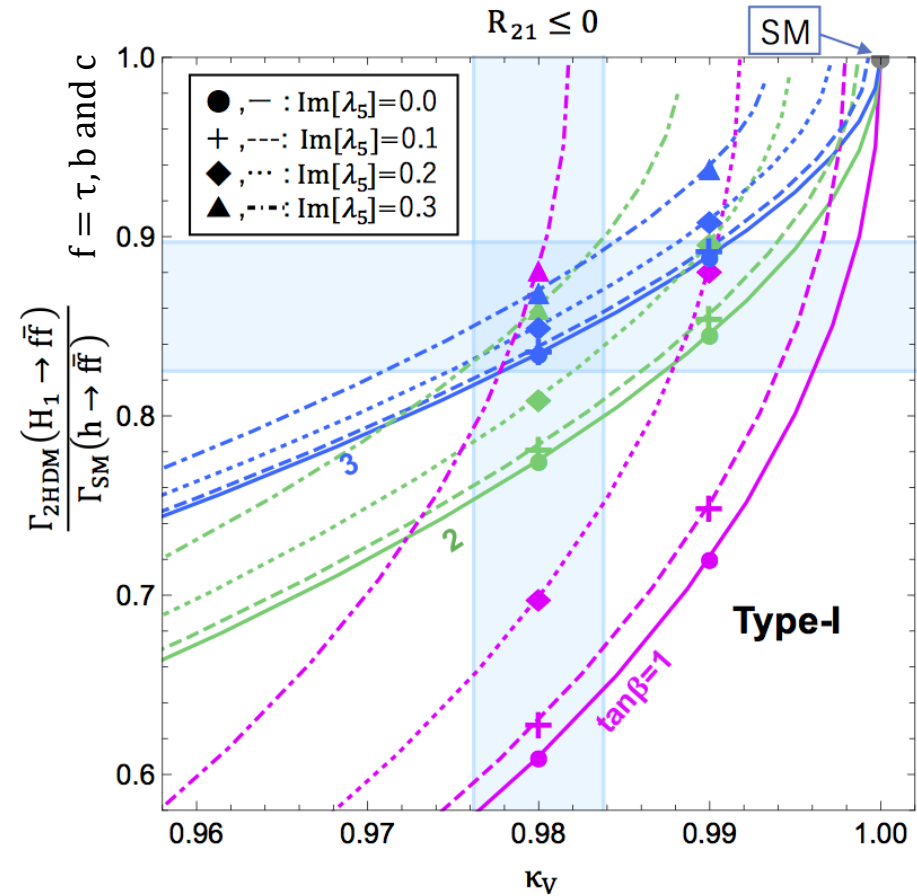
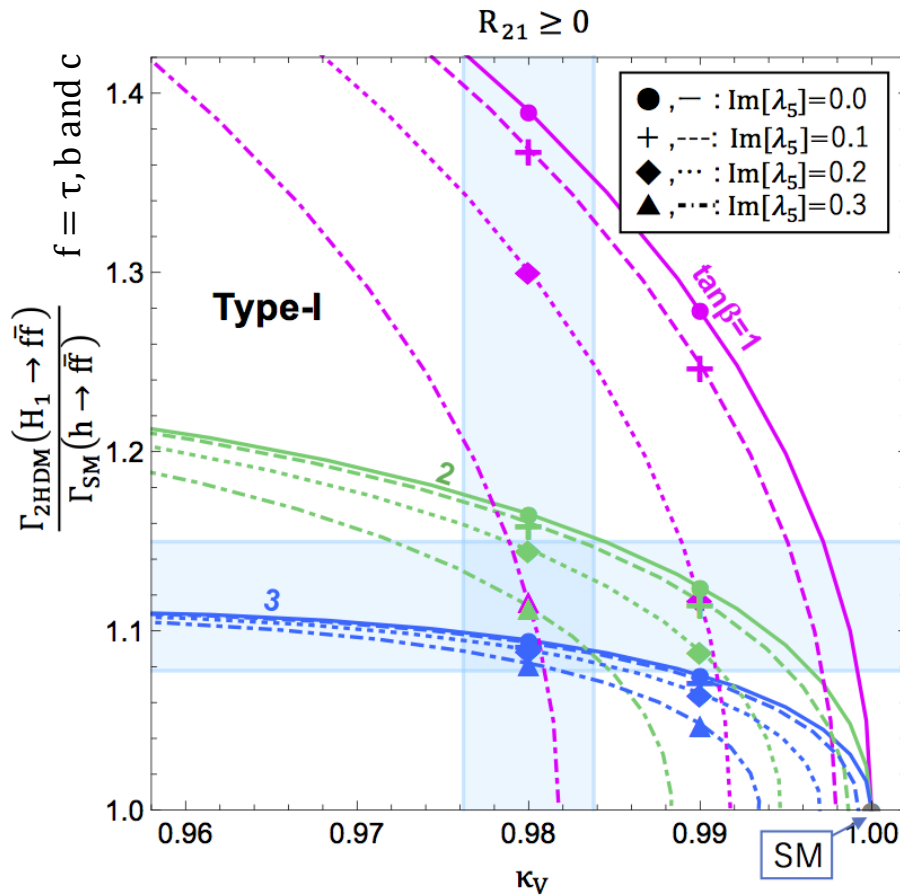
$R_{21} \leq 0$



$hcc-h\tau\tau$

# Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

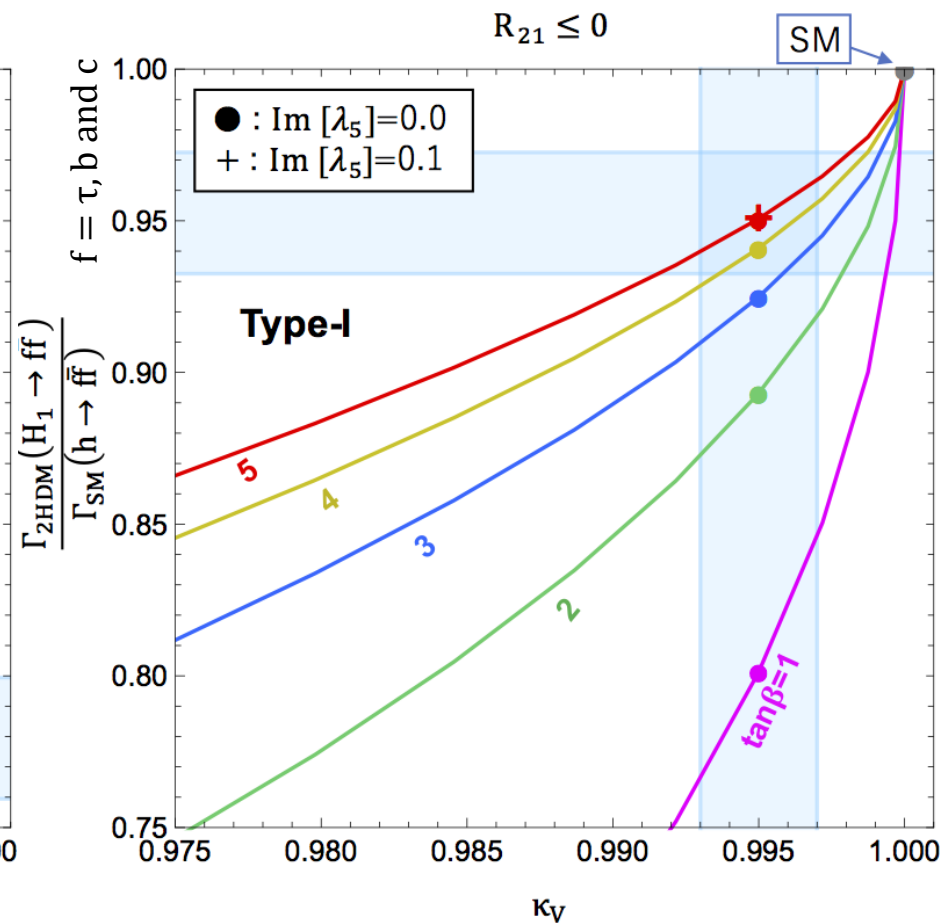
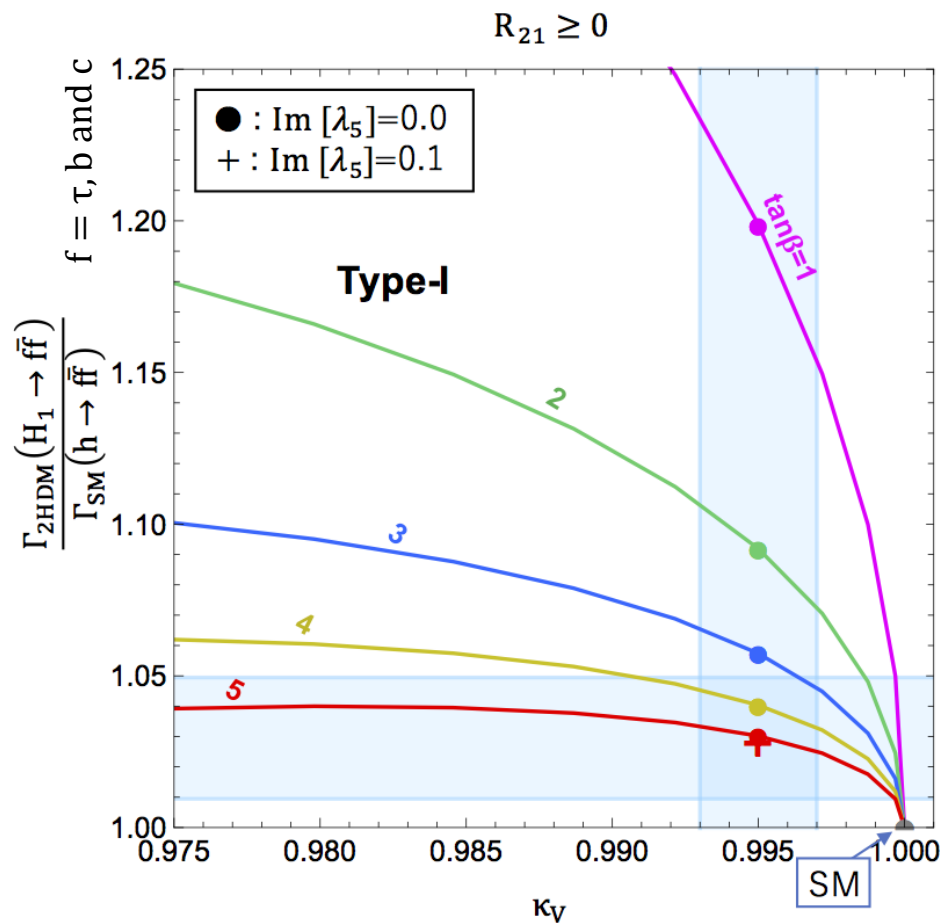


Type-I

# Result

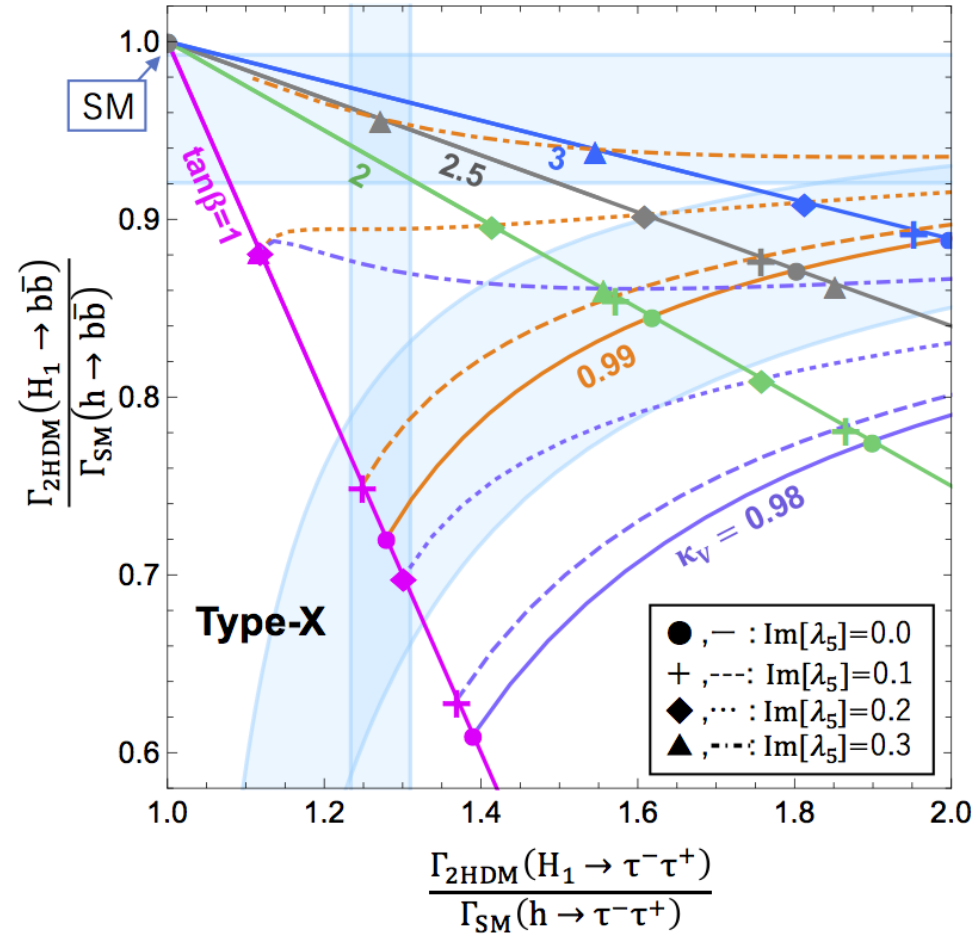
[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

$\kappa_V$ : 0.2%  
 $\kappa_{b,\tau}$ : 1%

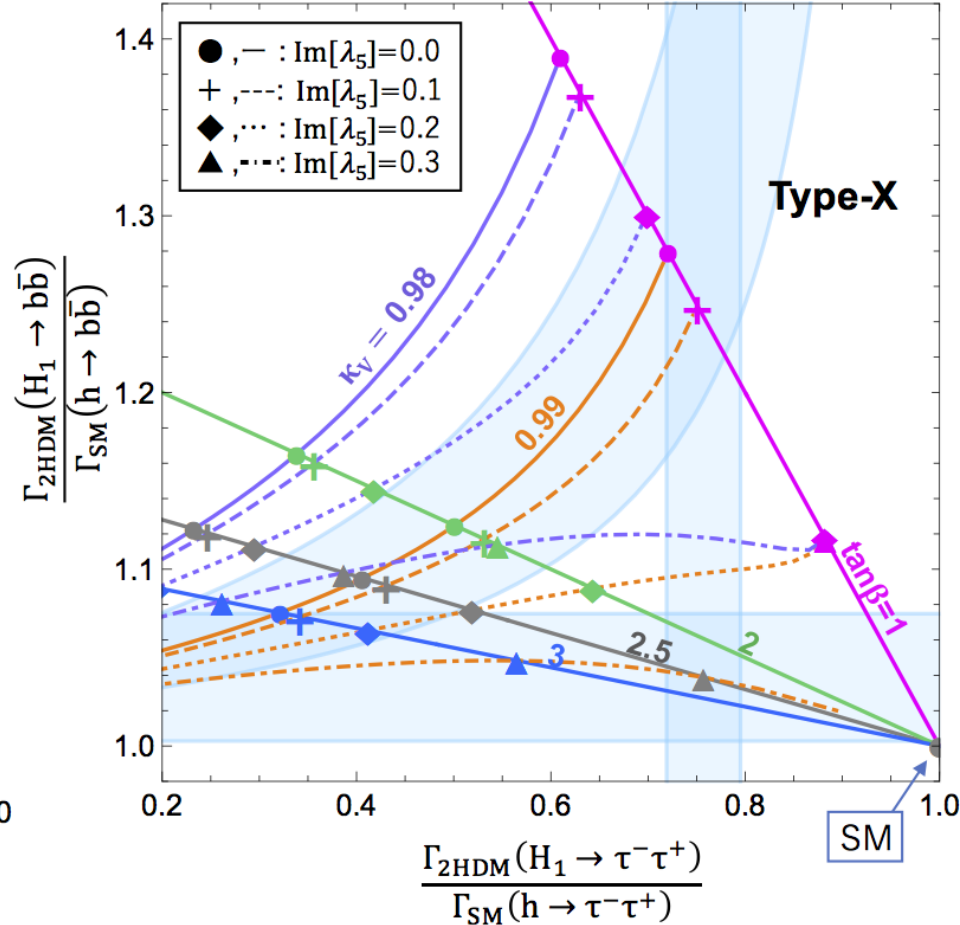


Type-I

## Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]ILC250 ( $2ab^{-1}$ ) $R_{21} \leq 0$  $R_{21} \geq 0$ 

Type-X



Type-X

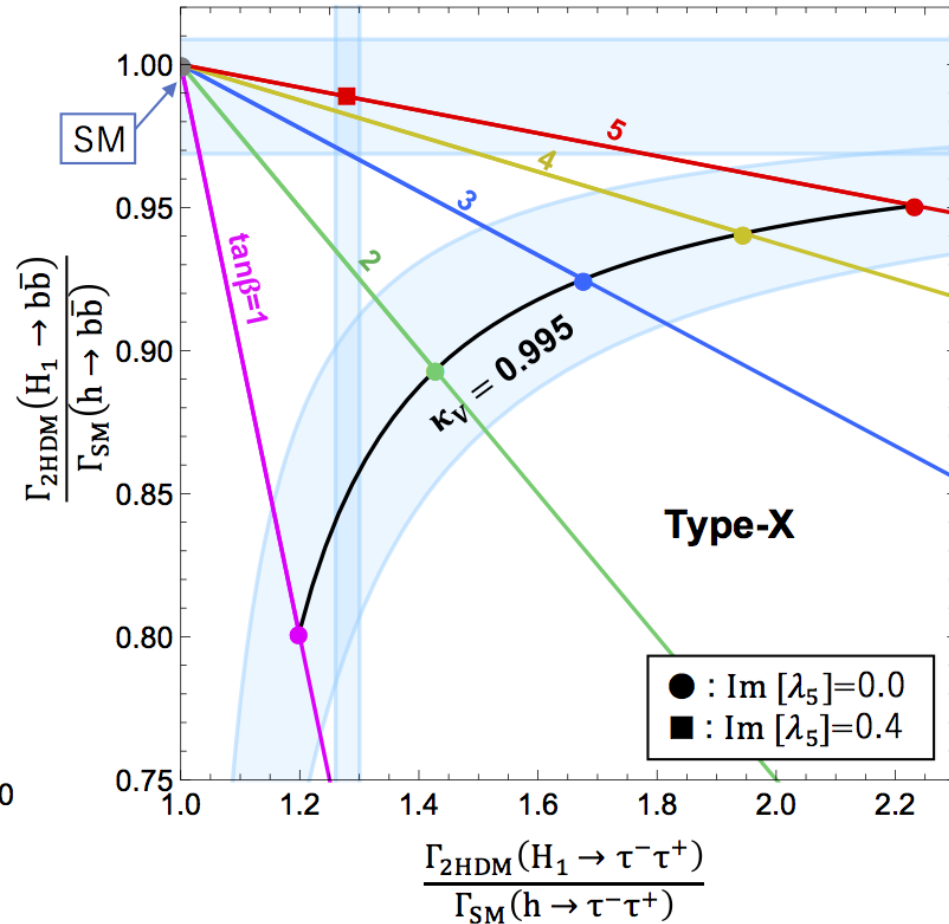
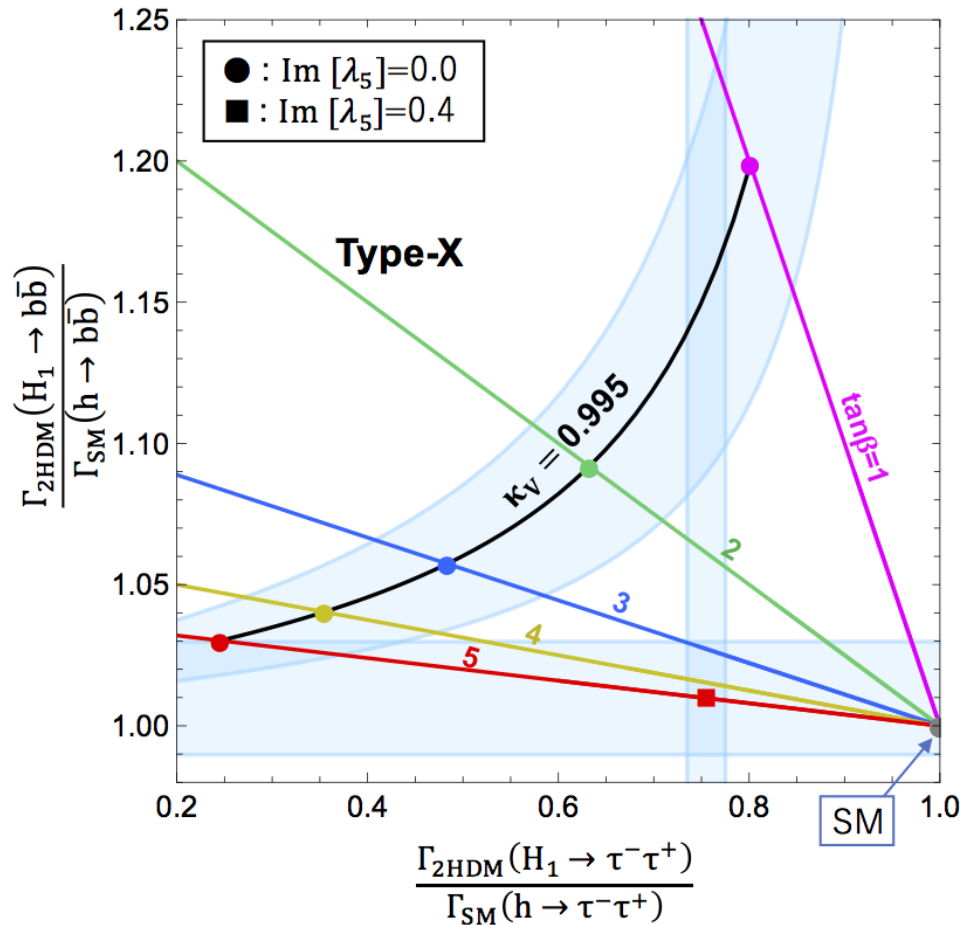
# Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

$\kappa_V$ : 0.2%  
 $\kappa_{b,\tau}$ : 1%

$R_{21} \geq 0$

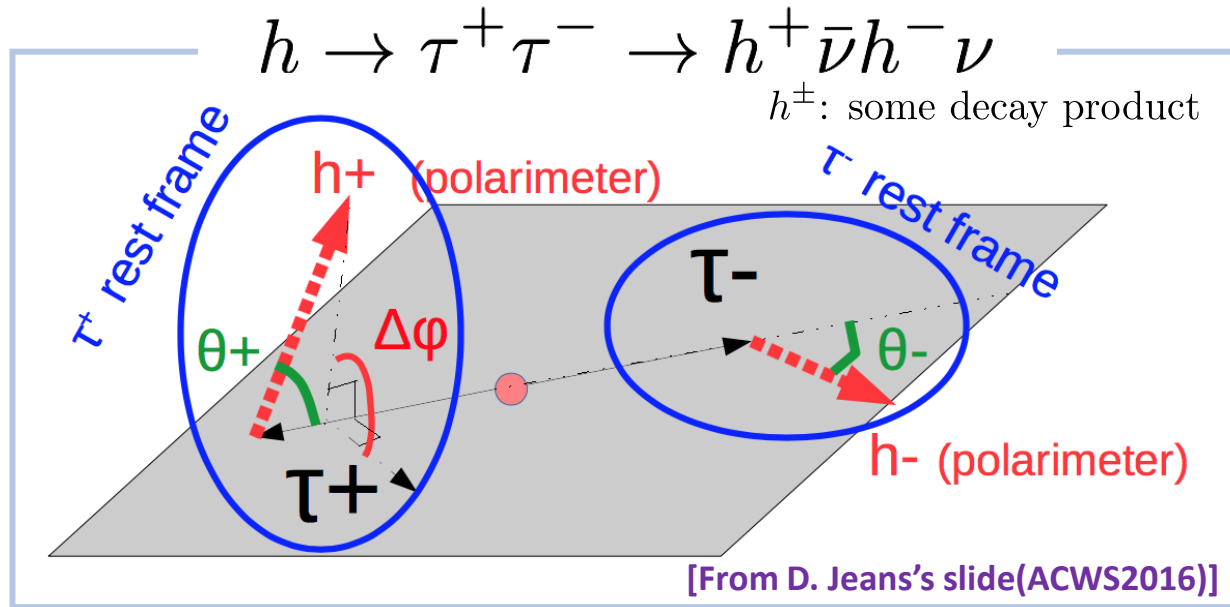
$R_{21} \leq 0$



Type-X

# Angular distribution of $h \rightarrow \tau\tau$

Yukawa coupling:  $\mathcal{L}_{h\tau\tau} = g\bar{\tau}(\cos\psi_{CP} + i\underline{\gamma_5 \sin\psi_{CP}})\tau h$



$$dN/(d \cos \theta^+ d \cos \theta^- d \phi^+ d \phi^-) \propto (1 + \underline{\cos \theta^+ \cos \theta^-}) - \underline{\sin \theta^+ \sin \theta^- \cos(\Delta \phi - 2\underline{\psi_{CP}})}.$$

$\text{ILC250, } 2ab^{-1} : \Delta\psi_{CP} = 4.3^\circ$

[Jeans and Wilson, PRD98, 013007 (2018)]

# Result

[M. Aoki, K. Hashino, D. Kaneko,  
S. Kanemura, MK, arXiv: 1808.08770]

ILC250,  $2ab^{-1} : \Delta\psi_{CP}=4.3^\circ$

[Jeans and Wilson, PRD98, 013007 (2018)]

## ◆ Angular distribution of $h \rightarrow \tau\tau$

For  $\kappa_V = 0.995, \tan\beta = 5,$

$R_{21} \geq 0$

$(\text{Im}\lambda_5, \psi_{CP}) = (0.0, 0^\circ),$

$$\tan\psi_{CP} \equiv c_\tau^p / c_\tau^s$$

$(0.4, -26^\circ)$  for  $R_{21} \leq 0,$   
 $(0.4, -30^\circ)$  for  $R_{21} \geq 0.$

$R_{21} \leq 0$

