

Matching scalar couplings between general renormalisable theories

Johannes Braathen

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in collaboration with Mark Goodsell and Pietro Slavich

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Introduction

The need for Effective Field Theories (EFTs)

- ▶ Scale of New Physics M_{NP} is driven higher by experimental searches
 - fixed-order calculations become plagued by **large logarithmic terms** $\propto \log M_{\text{MP}}/m_{\text{EW}}$
 - accuracy of the calculation, or even perturbativity, can be spoilt when the logarithms grow!
- ▶ The perturbative expansion must be reorganised → **EFT calculation**

Effective Field Theory calculations

- ▶ **Integrate out heavy fields** at some scale $\Lambda \sim M_{\text{NP}}$ and **work in a low-energy EFT below Λ**
 - ▶ Couplings in the EFT computed by **matching** effective actions between UV theory and EFT at scale Λ → **threshold corrections**
 - ▶ Use **RGEs** to run the couplings from the high input scale, to the low scale ($< M_{\text{NP}}$) at which the calculation is performed
- ⇒ Matching + RGE running → **large logs are resummed!**

Scalar couplings and Effective Field Theories

- ▶ In the context of Higgs mass calculations in SUSY models, heavy SUSY scenarios have been extensively investigated

→ Important matching conditions: **scalar quartic couplings** needed to compute m_h in the EFT!

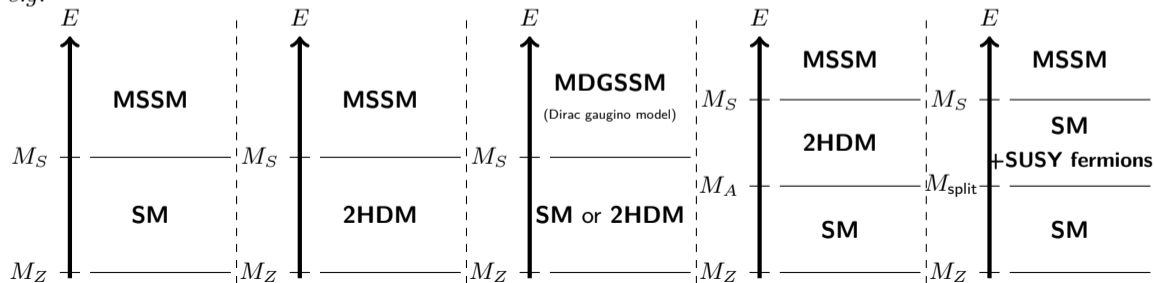
→ UV theory has usually been the MSSM, and EFT is the SM

see *e.g.* [Bernal, Djouadi, Slavich '07], [Draper, Lee, Wagner '13], [Bagnaschi, Giudice, Slavich, Strumia '14], [Pardo Vega, Villadoro '15], [Bagnaschi, Pardo Vega, Slavich '17], [Athron et al. '17], [Harlander, Klappert, Ochoa Franco, Voigt '18]

but more and more scenarios are now being investigated!

see *e.g.* [Benakli, Darmé, Goodsell, Slavich '13], [Bagnaschi, Giudice, Slavich, Strumia '14], [Lee, Wagner '15], [Benakli, Goodsell, Williamson '18], [Bahl, Hollik '18], etc.

e.g.



Matching of scalar couplings between generic theories

- ▶ Many possible scenarios → huge amount of work to compute all RGEs and matching conditions for each scenario!

⇒ **Automation**

i.e. compute RGEs and threshold corrections for general models, then apply the results to the scenario at hand.

- ▶ Two-loop RGEs are known for general QFTs, but for the thresholds, generic results have been obtained only at one-loop and mostly for the case of matching onto the SM or are difficult to implement in automated codes
 - ▶ **Our objective:** provide all necessary results to compute **threshold corrections** to scalar quartic (and Yukawa) couplings, when matching any high-energy model A onto any low-energy model B , and with the idea of going beyond one loop
- however there are challenges to address already from **one-loop order!**

[JB, Goodsell, Slavich 1810.09388]

Matching of scalar couplings in a toy model at tree-level

- Consider a simple toy model: 2 scalars, a light L and a heavy H , with a \mathbb{Z}_2 symmetry under which $L \rightarrow -L \Rightarrow$ no mixing between L and H

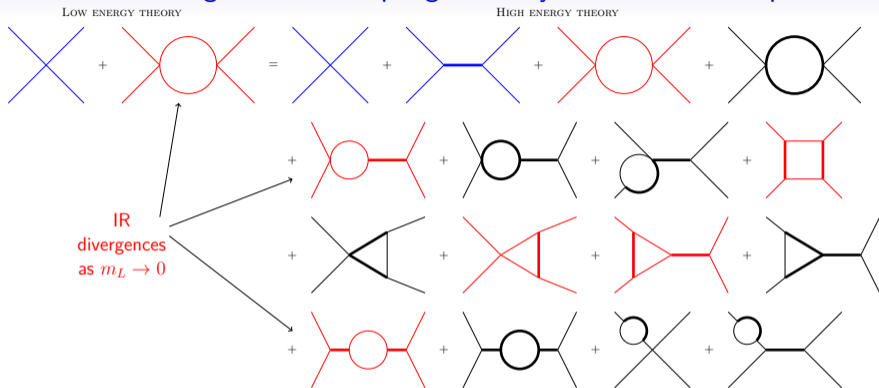
$$\begin{aligned} \text{High-energy model } \mathcal{L}_{\text{HE}} \supset & -\frac{1}{2}m_L^2 L^2 - \frac{1}{2}m_H^2 H^2 - \frac{1}{2}a_{LLH}L^2H - \frac{1}{6}a_{HHH}H^3 \\ & - \frac{1}{24}\tilde{\lambda}_{LLLL}L^4 - \frac{1}{4}\tilde{\lambda}_{LLHH}L^2H^2 - \frac{1}{24}\tilde{\lambda}_{HHHH}H^4 \\ \text{Low-energy model } \mathcal{L}_{\text{LE}} \supset & -\frac{1}{2}m_L^2 L^2 - \frac{1}{24}\lambda_{LLLL}L^4 \end{aligned}$$

- Integrating out H , one finds at **tree-level**

$$\lambda_{LLLL} = \tilde{\lambda}_{LLLL} + \frac{-3}{m_{HH}^2} a_{HLL}^2 + \text{perm.}$$

thin line: light state; thick line: heavy state

Matching of scalar couplings in a toy model at one loop

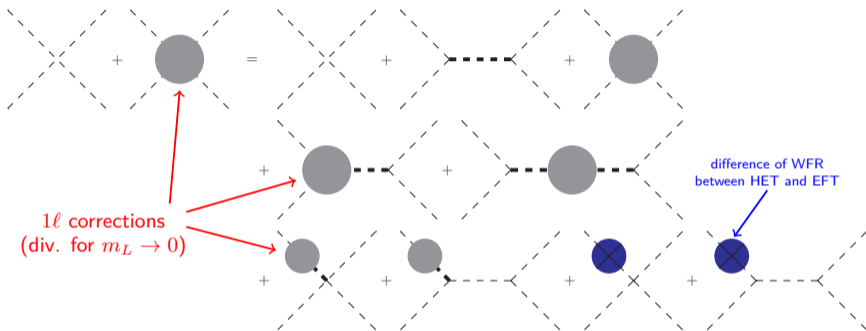


- Several diagrams are **IR divergent** in limit $m_L \rightarrow 0$, because of terms $\propto \log m_H/m_L$
 - IR parts in low and high energy theory must exactly cancel out, but because of a_{HLL} , divergent scalar diagrams are not in 1 to 1 correspondence \rightarrow **automation impossible** as is!
- \Rightarrow We have derived complete expressions for the matching of scalar couplings, at **one-loop** order, between two **generic models***, and **eliminating the IR divergent logs**

*: however without heavy gauge bosons

Matching quartic couplings between generic theories

The matching condition in the general case is

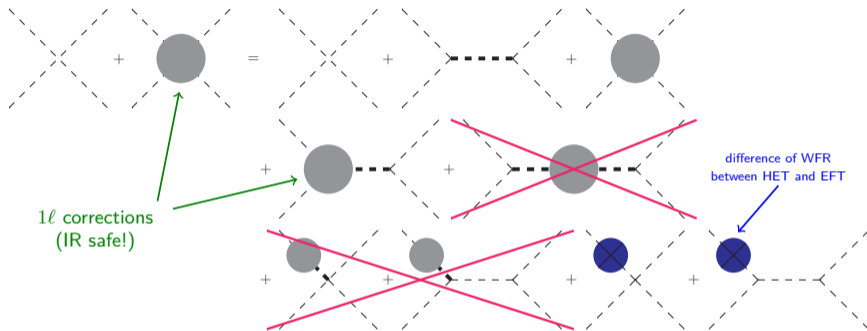


▷ Expressions can be regularised by using modified (Passarino-Veltmann) loop functions

$$B_0(0,0) \rightarrow 0, \quad C_0(0,0,X) \rightarrow -\frac{1}{X}B_0(0,X) = \frac{1}{X^2}A(X), \quad D_0(0,0,X,Y) \rightarrow -\frac{1}{X-Y} \left(\frac{1}{X^2}A(X) - \frac{1}{Y^2}A(Y) \right)$$

where $A(x) \equiv x(\log x/Q^2 - 1)$.

Matching quartic couplings between generic theories



- ▷ Expressions can be regularised by using modified (Passarino-Veltmann) loop functions
- ▷ Redefinition of (finite part of) mass counter-terms can allow eliminating δm_{KL}^2 and δm_{iK}^2 (generalises a scheme devised in [Bagnaschi, Giudice, Slavich, Strumia '14] for models with 2 doublets)
 - **mixing between heavy and light states eliminated from the matching condition!**

A simple approach to matching using two-point functions

Pole-mass matching (see e.g. [Athron et al. '16])

- ▶ Extracting the threshold corrections to λ_{SM} from

$$\underbrace{2\lambda_{\text{SM}}v_{\text{SM}}^2 + \Delta m_{\text{SM}}^2(p^2 = m_h^2)}_{\text{Higgs pole mass in EFT (SM)}} = \underbrace{(m_{\text{HET}}^2)^{\text{tree}} + \Delta m_{\text{HET}}^2(p^2 = m_h^2)}_{\text{Higgs pole mass in UV theory}}$$

$$\Rightarrow \lambda_{\text{SM}} = \frac{2}{v_{\text{HET}}^2} \left[m_{\text{HET}}^2 \left(1 + [\Pi_{hh}^{\text{HET}'}(0) - \Pi_{hh}^{\text{SM}'}(0)] \right) - \frac{m_{\text{HET}}^2}{m_Z^2} (\Pi_{ZZ}^{\text{HET}}(0) - \Pi_{ZZ}^{\text{SM}}(0)) + (\Delta m_{\text{HET}}^2(0) - \Delta m_{\text{SM}}^2(0)) \right]$$

$\Pi_{hh}(0)$, $\Pi_{ZZ}(0)$: Higgs and Z -boson self-energies at $p^2 = 0$, Δm^2 : corrections to the Higgs mass

- ▶ easier to extend beyond one-loop (as 2-point functions are easier to deal with)
- ▶ only really tractable when EFT model does not have mixing in Higgs sector
- ▶ as is, requires cancellation of large logs (as was our problem earlier)
- ▶ Formally equivalent to using the modified mass counterterms (*c.f. previous slide*)
- ▶ We obtain an efficient way to compute the threshold corrections to λ_{SM} as

$$\lambda_{\text{SM}} = \frac{2}{v_{\text{HET}}^2} \left[m_{\text{HET}}^2 \left(1 + 2 \underbrace{[\Pi_{hh}^{\text{HET}'}(0) - \Pi_{hh}^{\text{SM}'}(0)]}_{\text{w. light masses} \rightarrow 0} \right) + \underbrace{\hat{\Delta} m_{\text{HET}}^2(0)}_{\substack{\text{terms w. light masses only} \rightarrow 0 \\ \text{logs of light masses} \rightarrow 0 \\ \text{(gauge contributions)} \rightarrow 0}} \right]$$

Summary

- ▶ Use of **Effective Field Theories** becomes increasingly necessary as M_{NP} is driven higher by experimental searches
- ▶ When considering the calculation of a given observable in a wide range of scenarios or models
→ **Automation** can provide fast and accurate predictions
- ▶ **Modified loop functions and renormalisation scheme choices** now allow simple matching of scalar quartic (and Yukawa) couplings between generic theories (similar results implemented in SARAH in [[Gabelmann, Mühlleitner, Staub 1810.12326](#)])
- ▶ **Efficient approach for pole mass matching**, that will be easier to extend beyond one-loop
- ▶ *Next*: going beyond one-loop → use of modified scheme expected to become more important, consider pole-mass matching, ...

THANK YOU FOR YOUR ATTENTION!

BACKUP

Previous results for the matching of scalar couplings between generic theories

- ▶ Two-loop RGEs known for general QFTs [Machacek, Vaughn '83,'84,'85], [Luo, Wang, Xiao '02], [Schienbein, Staub, Steudner, Svirina '18], [Sperling, Stöckinger, Voigt '13].
- ▶ General results (at one loop) exist for the matching of couplings in SMEFT studies with functional methods, but difficult to implement in automated codes
see *e.g.* [Henning, Lu, Murayama '14,'16], [Drozd, Ellis, Quevillon, You '15], [Ellis, Quevillon, You, Zhang '16,'17], [Fuentes-Martin, Portoles, Ruiz-Femenia '16], [Zhang '16], [Bumm, Voigt '18]
- ▶ Efforts ongoing on the matching of a generic model onto the SM at one loop, by the FlexibleSUSY collaboration [Athron et al. '17] and in SARAH [Staub, Porod '17], via *pole mass matching* *i.e.* extracting the threshold corrections to λ_{SM} from

$$2\lambda_{\text{SM}}v_{\text{SM}}^2 + \Delta m_{\text{SM}}^2(m_h^2) = (m_{\text{HET}}^2)^{\text{tree}} + \Delta m_{\text{HET}}^2(m_h^2)$$