

More BSM ideas with or without present flavor anomalies

- Motivation
- Lessons
- LNU 2018 +
- Uncharted territory: mapping out $|\Delta c| = |\Delta u| = 1$

based on works with Stefan de Boer, Martin Schmaltz, Ivo de Medeiros Varzielas, Dennis Loose, Kay Schönwald and Ivan Nisandzic

Gudrun Hiller, TU Dortmund

We'd like to understand

1. the borders of the SM (test the SM and look for BSM physics) and
2. "flavor" (Pattern of fermion masses and mixings).

To do so, besides improving theory precision, we invoke model-independent analyses (fits to Wilson coefficients C_i), study (and design) null test observables and aim at leaving no stone unturned (diverse searches, synergy with collider and dark matter searches).

top 10 observables beyond $\mathcal{B}(b \rightarrow s\gamma)$

1. CP asymmetry $a_{CP}(b \rightarrow s\gamma)$; in SM direct CP violation in $b \rightarrow s$ is small: $a_{CP} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} \propto \alpha_s(m_b) \text{Im} \frac{V_{ub} V_{us}^*}{V_{tb} V_{ts}^*} \sim \alpha_s(m_b) \lambda^2 \lesssim \mathcal{O}(1\%)$
 $a_{CP} = (-0.079 \pm 0.108 \pm 0.022)(1 \pm 0.03)$ CLEO hep-ex/0010075
2. search for wrong helicity $\bar{s}_R \sigma_{\mu\nu} b_L$ in $b \rightarrow s\gamma$; in SM small
 $C'_7 = m_s/m_b C_7$ e.g. with polarization studies in $\Lambda_b \rightarrow \Lambda \gamma$ at Tevatron, LHC, GigaZ hep-ph/0108074
3. $|\sin 2\beta_{(J/\Psi K)} - \sin 2\beta_{(\Phi K)}|$ is $\lesssim \mathcal{O}(\lambda^2)$ in SM; direct CPX in $b \rightarrow s\bar{s}s$
 $\mathcal{B}(B \rightarrow \Phi K_0)_{ave} = 8.8^{+2.7}_{-2.3} \cdot 10^{-6}$ Belle, Babar preliminary
 $\sigma_{\Phi K_s}(stat) = 0.56, 0.18$ with $0.1, 1ab^{-1}$ hep-ph/0112312
4. precision study in inclusive $b \rightarrow s\ell^+\ell^-$ branching ratio at NNLO for low dilepton inv mass below $c\bar{c}$ threshold hep-ph/0112300

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beach 2002

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top 10 observables beyond $\mathcal{B}(b \rightarrow s\gamma)$

5. For-Back-asymmetry $A_{FB}(B \rightarrow (X_s, K^*)\ell^+\ell^-)$ sign/shape
6. if it exists, what is the position of the A_{FB} zero in low q^2
7. Forward-Back-CP asymmetry $A_{FB}^{CP} \equiv \frac{A_{FB} + \bar{A}_{FB}}{A_{FB} - \bar{A}_{FB}} \sim \frac{\text{Im}(C_{10})}{\text{Re}(C_{10})}$ probes non-SM CP phase in sZb vertex; in SM $A_{FB}^{CP} < 10^{-3}$ hep-ph/0006136
8. $B_s - \bar{B}_s$ mixing, Z-penguins
9. $\mathcal{B}(B_{d,s} \rightarrow \mu^+\mu^-)$, sensitive to neutral higgs exchange
10. nEDMs, strong CP problem $\bar{\Theta} < 10^{-10}$, $\delta_{CKM} \sim \mathcal{O}(1)$? sensitive to flavor blind CP violation if PQ-axion solution, if spontaneously broken CP tight constraints on flavor structure hep-ph/0201251

top 100: $b \rightarrow s\nu\bar{\nu}$, $K \rightarrow \pi\nu\bar{\nu}$, $D_0 - \bar{D}_0$, leptons, neutrinos

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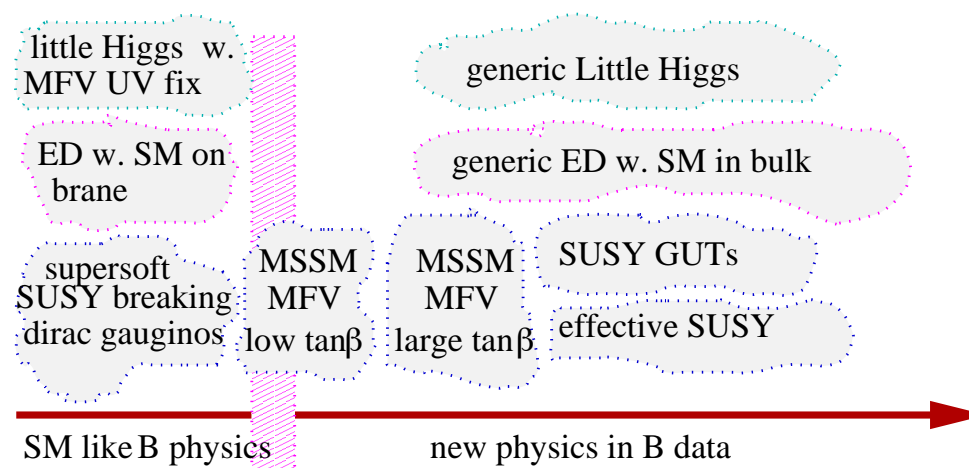
beach 2002

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Key topics 2002: CP, observation of rare B -decays, start of $b \rightarrow s\ell\ell$ angular analysis, $C_7, C'_7, C_{10}, C_P \dots$ and K, D physics

Key themes now: precision, CP, lepton nonuniversality ... and K, D

plot from hep-ph/0207121



2002: top-down models

2018: $U(1)$ -extensions, leptoquarks,...

We are seeing $\sim 2.6\sigma$ hints of new physics in $b \rightarrow sll$, LNU between e 's and μ 's in each observable R_K and R_{K^*} , both < 1 , [LHCb '14, '17](#),

$$R_H = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{H} \mu \mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{H} e e)}, \text{ same cuts } e \text{ and } \mu, \quad H = K, K^*, X_s, \dots$$

Lepton-universal models (incl. SM): $R_H = 1 + \text{tiny}$ [GH, Krüger, hep-ph/0310219, PRD](#)

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More model-independent analysis of $b \rightarrow s$ processes

Gudrun Hiller*

Ludwig-Maximilians-Universität München, Sektion Physik, Theresienstraße 37, D-80333 München, Germany

Frank Krüger†

Physik Department, Technische Universität München, D-85748 Garching, Germany

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We study model-independently the implications of nonstandard scalar and pseudoscalar interactions for the decays $b \rightarrow s \gamma$, $b \rightarrow s g$, $b \rightarrow s \ell^+ \ell^-$ ($\ell = e, \mu$) and $B_s \rightarrow \mu^+ \mu^-$. We find sizable renormalization effects from scalar and pseudoscalar four-quark operators in the radiative decays and at $O(\alpha_s)$ in hadronic b decays. Constraints on the Wilson coefficients of an extended operator basis are worked out. Further, the ratios $R_H = \mathcal{B}(B \rightarrow H \mu^+ \mu^-) / \mathcal{B}(B \rightarrow H e^+ e^-)$, for $H = K^{(*)}, X_s$, and their correlations with the $B_s \rightarrow \mu^+ \mu^-$ decay are investigated. We show that the standard model prediction for these ratios defined with the same cut on the dilepton mass for electron and muon modes, $R_H = 1 + O(m_\mu^2/m_b^2)$, has a much smaller theoretical uncertainty ($\leq 1\%$) than the one for the individual branching fractions. The present experimental limit $R_K \leq 1.2$ puts constraints on scalar and pseudoscalar couplings, which are similar to the ones from current data on $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$. We find that new physics corrections to R_{K^*} and R_{X_s} can reach 13% and 10%, respectively.

R_{K,K^*} situation needs to be consolidated/deciphered/understood

1. Correlations among R_H Predictions: 1411.4773

$$R_K \simeq R_\eta \simeq R_{K_1(1270,1400)}, \quad R_{K^*} \simeq R_\Phi \simeq R_{K_0(1430)}$$

All R_H equal if no V+A currents present.

$$R_{X_s} \simeq 0.73 \pm 0.07 \text{ inclusive decays } 1704.05444 \text{ Belle II}$$

2. BSM in electrons, or muons, or in both? Lepton-specific measurements $B \rightarrow K^* ee$ angular distribution Belle '17

Global fits presently suggest that it suffices to have BSM in

$b \rightarrow s\mu\mu$ only. several fit groups: Silvestrini et al, Bobeth, van Dyk et al, Descotes-Genon, Matias et al,

Altmannshofer, Straub et al Good fit: $C_9^\mu = -C_{10}^\mu \simeq -0.6$ vs $C_9^{\text{SM}} \simeq -C_{10}^{\text{SM}} \simeq 4$

$\sim 15\%$ BSM contribution to $O_{LL} = \bar{s}_L \gamma_\mu b_L \bar{\mu}_L \gamma^\mu \mu_L$. just the right size on FCNC amplitude (suppressed by GIM,CKM,loop in SM).

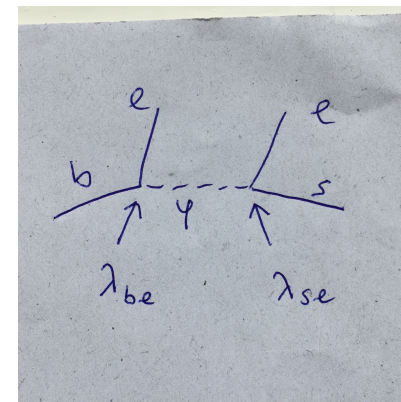
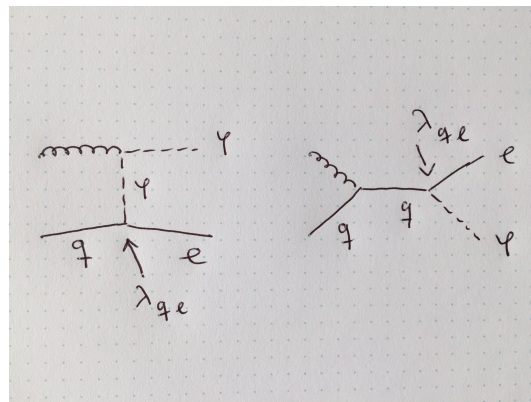
3. Side effects from flavor: LFV, τ 's, by $SU(2)$ ν 's [1411.0565,1412.7164,1503.01084](#)

LQ coupling patterns rows: quarks, columns: leptons **red**: K , D -physics

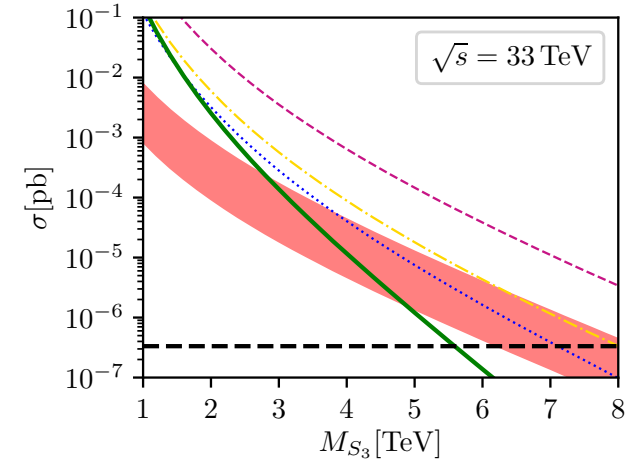
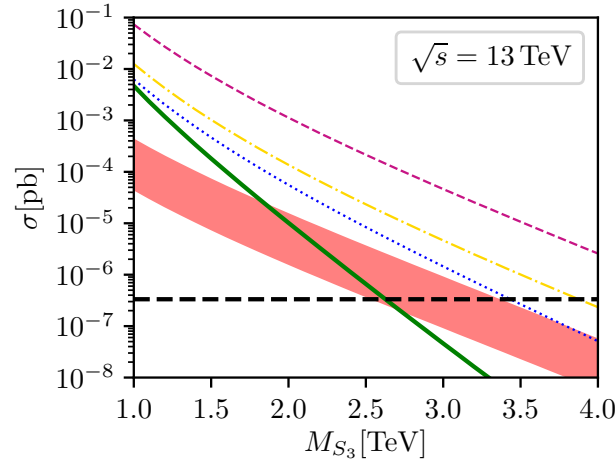
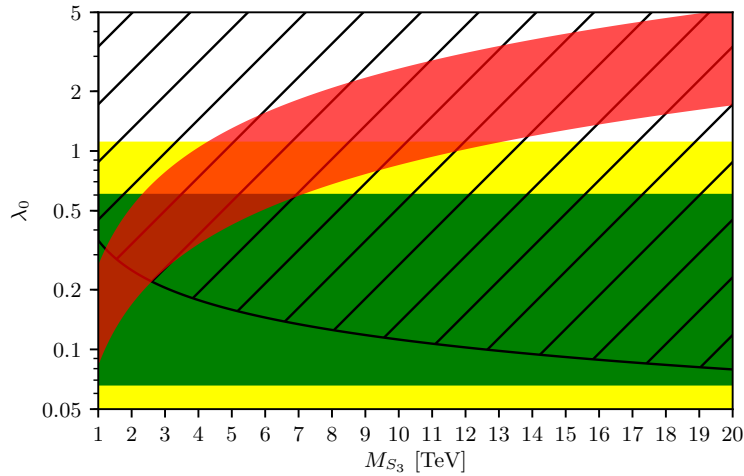
$$\lambda_{q\ell} = \begin{pmatrix} \lambda_{q1e} & \lambda_{q1\mu} & \lambda_{q1\tau} \\ \lambda_{q2e} & \lambda_{q2\mu} & \lambda_{q2\tau} \\ \lambda_{q3e} & \lambda_{q3\mu} & \lambda_{q3\tau} \end{pmatrix}, \begin{pmatrix} * & * & * \\ \lambda_{q2e} & \lambda_{q2\mu} & * \\ \lambda_{q3e} & \lambda_{q3\mu} & * \end{pmatrix} + \text{Occam's razor} : \begin{pmatrix} * & * & * \\ * & \lambda_{q2\mu} & * \\ * & \lambda_{q3\mu} & * \end{pmatrix}.$$

4. Collider implications (leptoquarks!) $\frac{\lambda_{b\mu}\lambda_{s\mu}^* - \lambda_{be}\lambda_{se}^*}{M^2} \simeq \frac{1.1}{(35 \text{ TeV})^2}$

Single leptoquark production from b -anomalies [1801.09399](#) in association with a lepton $\sigma(pp \rightarrow \varphi\ell) \propto |\lambda_{q\ell}|^2 \alpha_s$ depends on flavor



Producing leptoquarks at the LHC



red band: R_{K,K^*} -data $M/11.6 \text{ TeV} \lesssim \lambda_{b\ell} \lesssim M/3.9 \text{ TeV}$ using flavor hierarchy $\lambda_{s\ell} \sim m_s/m_b \lambda_{b\ell}$

left plot: green: flavor model prediction points to multi-TeV mass; yellow: $\Gamma/M \lesssim 5\%$

other plots: magenta, yellow, blue: $\lambda_{d\mu} = 1, \lambda_{s\mu} = 1, \lambda_{b\mu} = 1$, black: no-loss reach with 3 ab^{-1}

green curve: pair production (LO Madgraph) [1801.09399](#)

– Beauty wins over PDF if λ_{ql} follow quark mass hierarchies. Inverted hierarchies $\lambda_{sl} > \lambda_{bl}$ would be surprising from a symmetry-based flavor perspective and suggests means beyond.

LNU anomalies in B -decays will be sorted out.

Irrespective of this, it is a truly flavor-type question whether BSM in $b \rightarrow s$ -FCNC decays has implications for $c \rightarrow u$ decays.

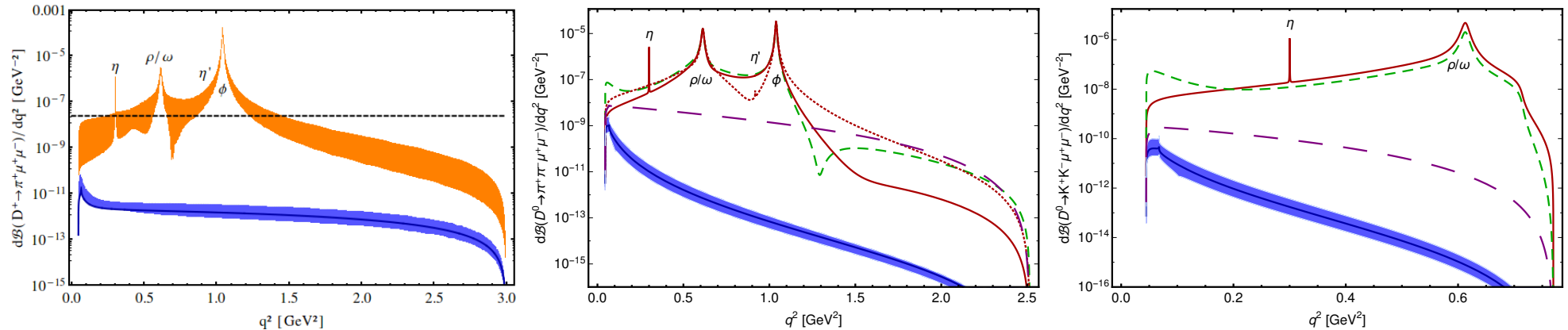
What do we know about $|\Delta c| = |\Delta u| = 1$ couplings anyway? – genuine probe of flavor in the up-quark sector. Consider

rare charm decays

Bigi, Burdman, d'Ambrosio, Cata, Fajfer, Feldmann, Golowich, Hewett, Kosnic, Pakvasa, Seidel, Singer, Zwicky, de Boer, GH

1510.00311 on $D \rightarrow \pi ll$, 1701.06392 on Br and A_{CP} in radiative D -decays, 1802.02769 on photon polarization from TDA or up-down asymmetry; measure SM BGD 1805.08516 on $D \rightarrow P_1 P_2 ll$, $P_{1,2} = \pi, K$

Resonance contributions vs BSM



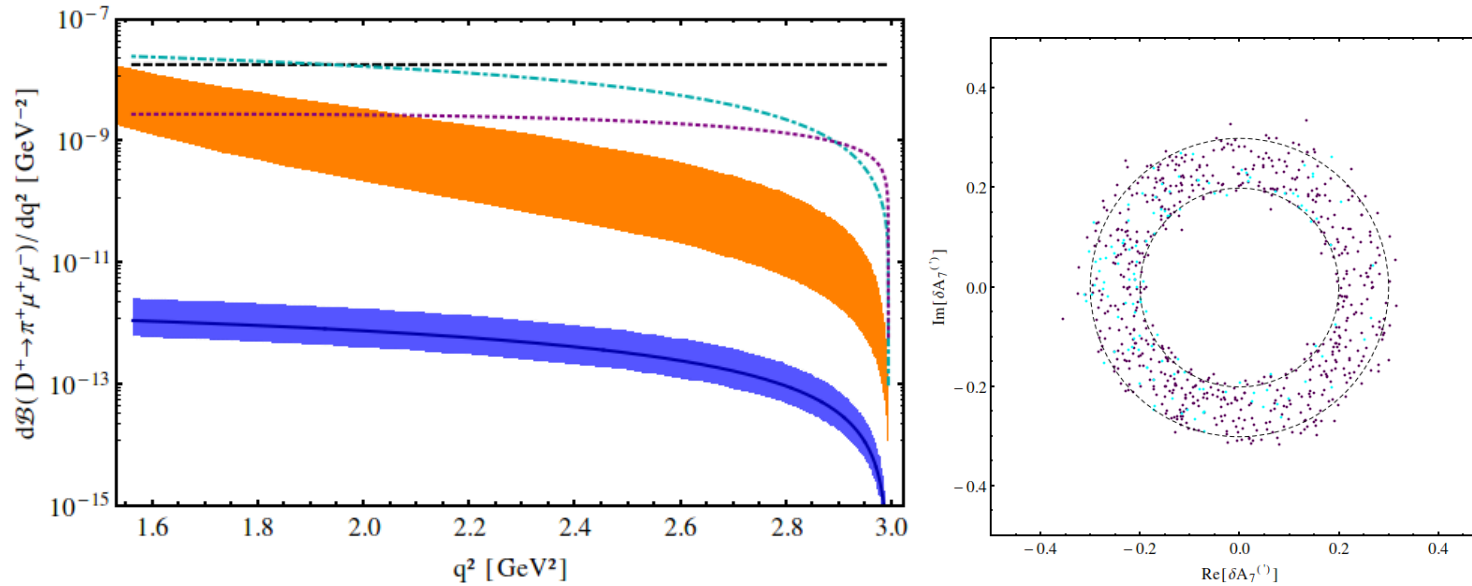
BSM windows in branching ratios only in $D \rightarrow \pi \mu^+ \mu^-$ (left) at high q^2 [1510.00311](#); $D \rightarrow \pi^+ \pi^- \mu \mu$ (mid), $D \rightarrow K^+ K^- \mu \mu$ (right), [1805.08516](#), [1705.05891](#)

$c \rightarrow u$ amplitudes are strongly GIM-suppressed:

$$\mathcal{A}_{c \rightarrow u} \simeq \sin \Theta_C [f(m_s^2/m_W^2) - f(m_d^2/m_W^2)] + O(\sin^5 \Theta_C)$$

To observe BSM in rare charm either i) BSM is an obvious excess in rates, ii) SM BDG can be measured, e.g. $D \rightarrow V \gamma$, or iii) contributes to SM null tests related to (approx.) symmetries of the SM.

Model-independent constraints on $|\Delta c| = |\Delta u| = 1$



$(\bar{u}\Gamma c)(\bar{\mu}\Gamma\mu)$: $|C_{9,10}^{(\prime)}| \lesssim 1$, $|C_{T,T5}| \lesssim 1$, $|C_{S,P}^{(\prime)}| \lesssim 0.1$, $|C_7^{(\prime)}| \lesssim 0.3$.

vs $|C_9^{\text{effSM}}| \lesssim 0.01$, $C_{10}^{\text{SM}} = 0$, $C'^{\text{SM}}, C_{S,P,T,T5}^{\text{SM}} = 0$, $|C_7^{\text{effSM}}| = \mathcal{O}(0.001)$.

$(\bar{u}\Gamma c)(\bar{e}\Gamma e)$: constraints $(2-4) \times$ weaker (data) than muon constraints.

$(\bar{u}\Gamma c)(\bar{\mu}\Gamma e)$, $(\bar{e}\Gamma\mu)$: $(6-7) \times$ weaker than muon constraints.

Predictions for charm decays

	$\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)$	$\mathcal{B}(D^0 \rightarrow \mu^+ \mu^-)$	$\mathcal{B}(D^+ \rightarrow \pi^+ e^\pm \mu^\mp)$	$\mathcal{B}(D^0 \rightarrow \mu^\pm e^\mp)$	$\mathcal{B}(D^+ \rightarrow \pi^+ \nu \bar{\nu})$
i)	SM-like	SM-like	$\lesssim 2 \cdot 10^{-13}$	$\lesssim 7 \cdot 10^{-15}$	$\lesssim 3 \cdot 10^{-13}$
ii.1)	$\lesssim 7 \cdot 10^{-8}$ ($2 \cdot 10^{-8}$)	$\lesssim 3 \cdot 10^{-9}$	0	0	$\lesssim 8 \cdot 10^{-8}$
ii.2)	SM-like	$\lesssim 4 \cdot 10^{-13}$	0	0	$\lesssim 4 \cdot 10^{-12}$
iii.1)	SM-like	SM-like	$\lesssim 2 \cdot 10^{-6}$	$\lesssim 4 \cdot 10^{-8}$	$\lesssim 2 \cdot 10^{-6}$
iii.2)	SM-like	SM-like	$\lesssim 8 \cdot 10^{-15}$	$\lesssim 2 \cdot 10^{-16}$	$\lesssim 9 \cdot 10^{-15}$

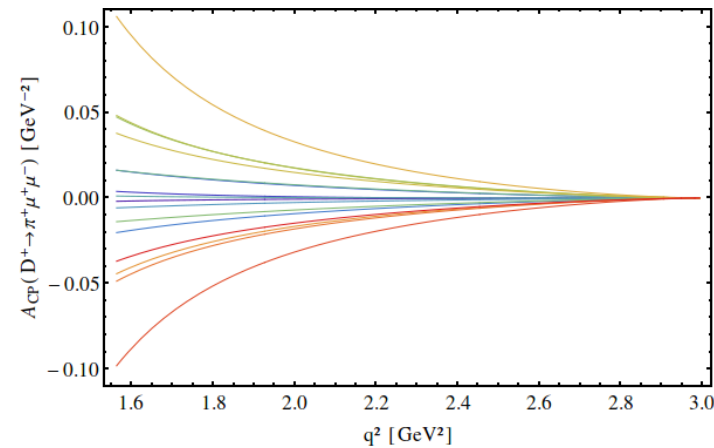
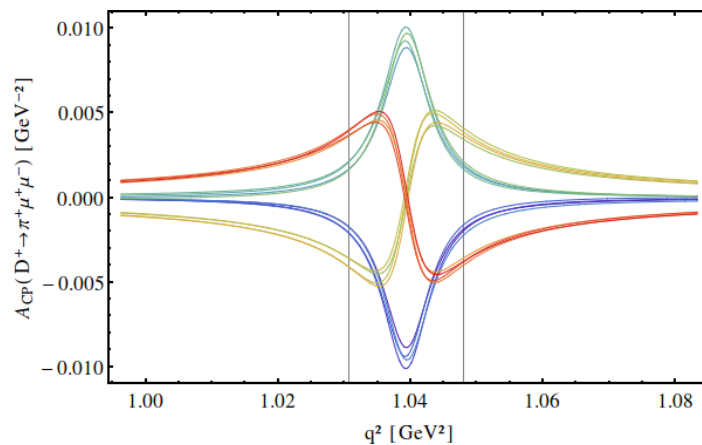
Table 1: Branching fractions for the full q^2 -region (high q^2 -region) for different classes of leptoquark couplings. Summation of neutrino flavors is understood. "SM-like" denotes a branching ratio which is dominated by resonances or is of similar size as the resonance-induced one. All $c \rightarrow ue^+e^-$ branching ratios are "SM-like" in the models considered. Note that in the SM $\mathcal{B}(D^0 \rightarrow \mu\mu) \sim 10^{-13}$.

LHCb: arXiv:1512.00322 [hep-ex] $\mathcal{B}(D^0 \rightarrow e^\pm \mu^\mp) < 1.3 \cdot 10^{-8}$ at 90 % CL

i): hierarchy, ii) muons only iii) skewed, 1) no kaon bounds 2) kaon bounds apply for $SU(2)_L$ -doublets $Q = (c, s)$ 1510.00311

Probing even small couplings: $A_{CP}(D \rightarrow \pi ll)$

GIM-suppression can be eased by the resonances, which are less $SU(3)_F$ -symmetric than the nr- contributions. also "resonance-catalyzed CP", Fajfer et al '13



Large uncertainties, however, large BSM signals possible ($|A_{CP}^{\text{SM}}| \lesssim \text{few} 10^{-3}$) even independent of strong phases around Φ .

Opportunity to probe SM-like lorentz-structure $C_{V,A}$ even in presence of $SU(2)$ -link to K-physics – links between **charm and b-physics**

Null tests of the SM based on

1. CP & GIM
2. angular distributions
3. LNU
4. LFV
5.

Full $D \rightarrow P_1 P_2 l^+ l^-$ angular distribution

Learn, e.g., from B -physics literature [1406.6681](#), earlier works in charm [1209.4235](#)

$$d^5\Gamma = \frac{1}{2\pi} \left[\sum c_i(\vartheta_l, \varphi) I_i(q^2, p^2, \cos \vartheta_{P_1}) \right] dq^2 dp^2 d \cos \vartheta_{P_1} d \cos \vartheta_l d\varphi ,$$

L, R : lepton current handedness

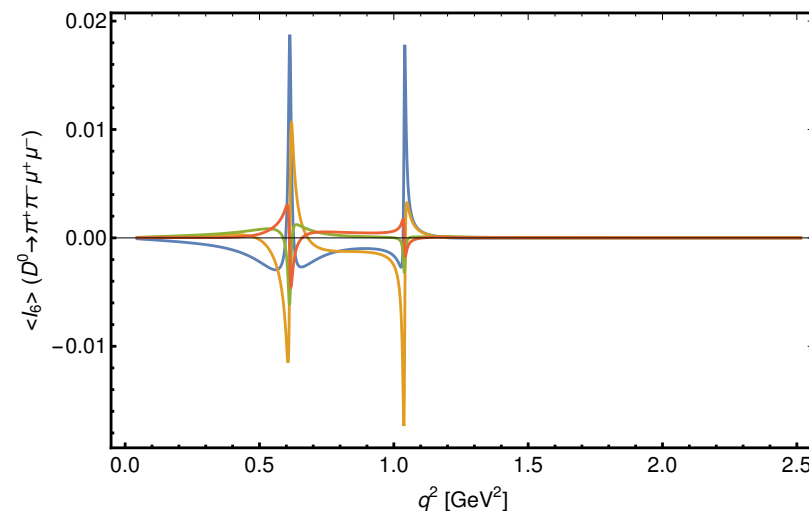
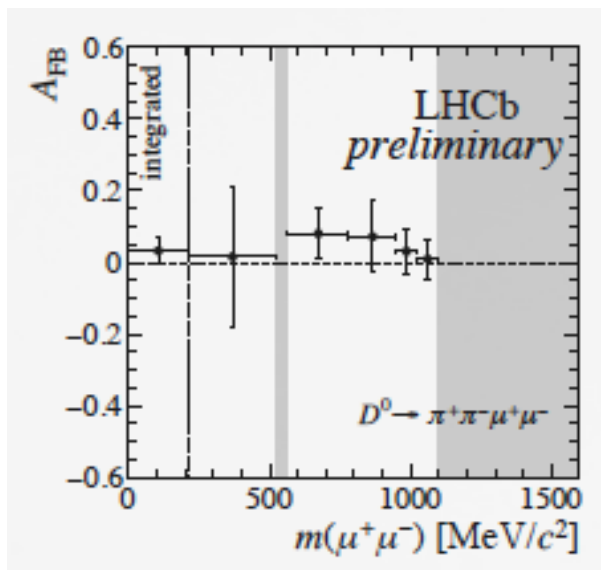
$$\begin{aligned} I_1 &= \frac{1}{16} \left[|H_0^L|^2 + (L \rightarrow R) + \frac{3}{2} \sin^2 \vartheta_{P_1} \{ |H_\perp^L|^2 + |H_\parallel^L|^2 + (L \rightarrow R) \} \right] , \\ I_2 &= -\frac{1}{16} \left[|H_0^L|^2 + (L \rightarrow R) - \frac{1}{2} \sin^2 \vartheta_{P_1} \{ |H_\perp^L|^2 + |H_\parallel^L|^2 + (L \rightarrow R) \} \right] , \\ I_3 &= \frac{1}{16} \left[|H_\perp^L|^2 - |H_\parallel^L|^2 + (L \rightarrow R) \right] \sin^2 \vartheta_{P_1} , \\ I_4 &= -\frac{1}{8} \left[\text{Re}(H_0^L H_\parallel^{L*}) + (L \rightarrow R) \right] \sin \vartheta_{P_1} , \\ I_5 &= -\frac{1}{4} \left[\text{Re}(H_0^L H_\perp^{L*}) - (L \rightarrow R) \right] \sin \vartheta_{P_1} , \\ I_6 &= \frac{1}{4} \left[\text{Re}(H_\parallel^L H_\perp^{L*}) - (L \rightarrow R) \right] \sin^2 \vartheta_{P_1} , \\ I_7 &= -\frac{1}{4} \left[\text{Im}(H_0^L H_\parallel^{L*}) - (L \rightarrow R) \right] \sin \vartheta_{P_1} , \\ I_8 &= -\frac{1}{8} \left[\text{Im}(H_0^L H_\perp^{L*}) + (L \rightarrow R) \right] \sin \vartheta_{P_1} , \\ I_9 &= \frac{1}{8} \left[\text{Im}(H_\parallel^{L*} H_\perp^L) + (L \rightarrow R) \right] \sin^2 \vartheta_{P_1} . \end{aligned} \tag{1}$$

Full $D \rightarrow P_1 P_2 l^+ l^-$ angular distribution

In charm, due to GIM, dynamics dominated by $SU(3)_C \times U(1)_{em}$: all vector-like: $I_{5,6,7}^{SM} = 0$ (proportional to $C_{10}^{(\prime)}$) 1805.08516

Things are simpler than in B -decays because of the resonances

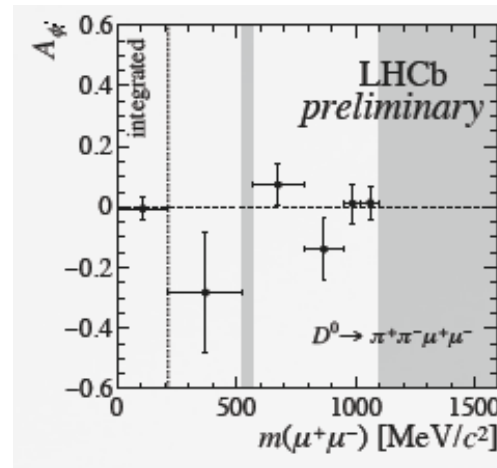
$I_6 \propto A_{FB}$ already measured LHCb talk by D.Mitzel at CHARM 2018 (grey: NS) model-independent BSM effects up to few %



Full $D \rightarrow P_1 P_2 l^+ l^-$ angular distribution: untagged CP

Angular coefficients $I_{5,6,8,9}$ are CP-odd and allow to measure CP-asymmetries without tagging. $A_k = 2 \frac{I_k - \bar{I}_k}{\Gamma + \bar{\Gamma}} = \frac{I_k - \bar{I}_k}{\Gamma_{ave}}$;
 $\langle A_k^{\text{SM}} \rangle$ below permille. With BSM: 1805.08516

$q_{\min}^2 = (1.1 \text{ GeV})^2$	$C_9 = -C_{10} = \pm 0.5i$	$C'_9 = -C'_{10} = \pm 0.5i$
$\langle A_5 \rangle$	$[-0.04, 0.04]$	$[-0.03, 0.03]$
$\langle A_6 \rangle$	$[-0.06, 0.05]$	$[-0.06, 0.06]$
$\langle A_8 \rangle$	$[-0.02, 0.02]$	$[-0.02, 0.02]$
$\langle A_9 \rangle$	$[-0.03, 0.03]$	$[-0.03, 0.03]$



A_Φ related to A_9

branching ratio	$D^0 \rightarrow \pi^+ \pi^- \mu^+ \mu^-$	$D^0 \rightarrow K^+ K^- \mu^+ \mu^-$	$D^0 \rightarrow \pi^+ \pi^- e^+ e^-$	$D^0 \rightarrow K^+ K^- e^+ e^-$
LHCb 17	$(9.64 \pm 1.20) \times 10^{-7}$	$(1.54 \pm 0.33) \times 10^{-7}$	–	–
BESIII 18	–	–	$< 0.7 \times 10^{-5}$	$< 1.1 \times 10^{-5}$
resonant	$\sim 1 \times 10^{-6}$	$\sim 1 \times 10^{-7}$	$\sim 10^{-6}$	$\sim 10^{-7}$
non-resonant	$10^{-10} - 10^{-9}$	$\mathcal{O}(10^{-10})$	$10^{-10} - 10^{-9}$	$\mathcal{O}(10^{-10})$

$$R_{P_1 P_2}^D = \frac{\int_{q_{\min}^2}^{q_{\max}^2} d\mathcal{B}/dq^2(D \rightarrow P_1 P_2 \mu^+ \mu^-)}{\int_{q_{\min}^2}^{q_{\max}^2} d\mathcal{B}/dq^2(D \rightarrow P_1 P_2 e^+ e^-)} \quad \text{with same cuts } q_{\min}^2 \geq 4m_\mu^2$$

full q^2	SM	BSM	LQ	hi q^2 SM	LQs	lo q^2 SM	BSM
$R_{\pi\pi}^D$	$1.00 \pm \mathcal{O}(\%)$	0.85 ...0.99	SM-like	$1.00 \pm \mathcal{O}(\%)$	0.7 ...4.4		
R_{KK}^D	$1.00 \pm \mathcal{O}(\%)$	SM-like	SM-like	NA	NA	$0.83 \pm \mathcal{O}(\%)$	0.60..0.87

O(1)BSM effects in $R_{\pi\pi}^D$ above Φ ; small BSM effects in R_{KK}^D below η .

Naive ratios $\bar{R}_{\pi^+\pi^-}^{D\,exp} \gtrsim 0.1$, $\bar{R}_{K^+K^-}^{D\,exp} \gtrsim 0.01$ based on different cuts and about one order of magnitude away from SM, are model-dependent.

Photon polarization in $c \rightarrow u\gamma$ from untagged TDA

Time-dependent analysis $D^0, \bar{D}^0 \rightarrow V\gamma$, $V = \rho^0, \Phi, \bar{K}^{*0}$ (decays to CP eigenstate with CP eigenvalue ξ) [1210.6546](#), [1802.02769](#)

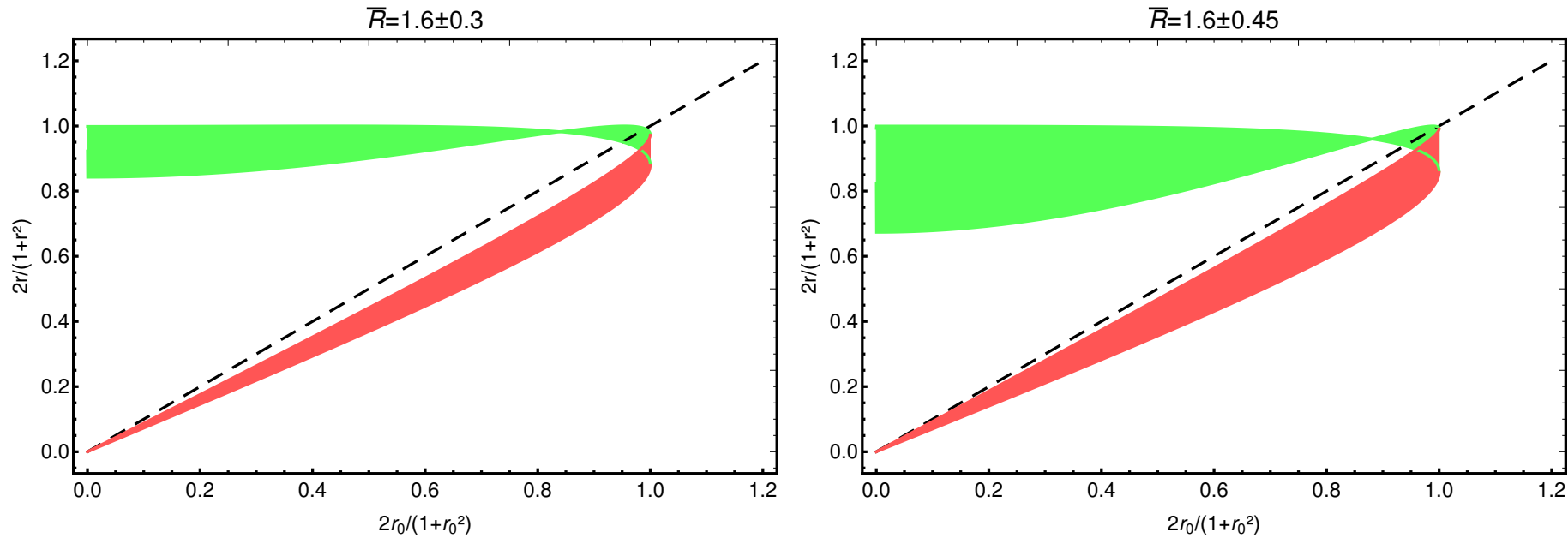
$$\Gamma(t) = \mathcal{N}e^{-\Gamma t} (\cosh[\Delta\Gamma t/2] + A^\Delta \sinh[\Delta\Gamma t/2] + \zeta C \cos[\Delta m t] - \zeta S \sin[\Delta m t])$$

$A^\Delta(D^0 \rightarrow \bar{K}^{*0}\gamma) \simeq \frac{4\xi_{\bar{K}^{*0}} \left| \frac{q}{p} \right| \cos\varphi}{\left(1 + \left| \frac{q}{p} \right|^2\right)} \frac{r_0}{1+r_0^2}$ Here, r_0 is ratio of wrong-chirality (RH) to LH-photons in SM-like process $D^0 \rightarrow \bar{K}^{*0}\gamma$.

Up to $SU(3)$ -breaking: $r(D^0 \rightarrow \Phi\gamma) = r_0$, $r(D^0 \rightarrow \rho\gamma) = r_0$;
perturbative $r = C'_7/C_7$, in SUSY, r unconstrained.

Br's	$D^0 \rightarrow \rho^0\gamma$	$D^0 \rightarrow \omega\gamma$	$D^0 \rightarrow \Phi\gamma$	$D^0 \rightarrow \bar{K}^{*0}\gamma$
Belle 2016	$(1.77 \pm 0.31) \times 10^{-5}$	–	$(2.76 \pm 0.21) \times 10^{-5}$	$(4.66 \pm 0.30) \times 10^{-4}$
BaBar 2008	–	–	$(2.81 \pm 0.41) \times 10^{-5}$	$(3.31 \pm 0.34) \times 10^{-4}$
CLEO 1998	–	$< 2.4 \times 10^{-4}$	–	–

Photon polarization in $c \rightarrow u\gamma$ from untagged TDA



$2r/(1 + r^2)$ as a function of $2r_0/(1 + r_0^2)$ (plots to the right), in the cases a) (SM case) $C_7, C_7' \simeq 0$ (black, dashed curve), c) $C_7 \simeq 0$ (green, upper band) and d) $C_7' \simeq 0$ (red, lower band). The upper (lower) plots correspond to $\bar{R}_{ave} = 1.6 \pm 0.3$ ($\bar{R} = 1.6 \pm 0.45$ from 50% inflated uncertainty).

$$\bar{R} = 1/f^2 \frac{|V_{cs}|^2}{|V_{cd}|^2} \frac{\mathcal{B}(D^0 \rightarrow \rho\gamma)}{\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\gamma)} \text{ with leading U-spin breaking removed } f = m_\rho f_\rho / (m_{K^{*0}} f_{K^{*0}})$$

Photon polarization from up-down asymmetry

Method 2: probe the photon polarization with an up-down asymmetry in $D^0 \rightarrow \bar{K}_1(\rightarrow \bar{K}\pi\pi)\gamma$ (a la $B \rightarrow K_1\gamma$ (Gronau, Pirjol, Grossman, Kou))

$$\frac{d\Gamma}{ds_{13} ds_{23} d\cos\vartheta} \propto |\mathbf{J}|^2(1 + \cos^2\vartheta) + \lambda_\gamma 2 \operatorname{Im}[\mathbf{n} \cdot (\mathbf{J} \times \mathbf{J}^*)] \cos\vartheta, \quad \lambda_\gamma = -\frac{1-r_0^2(\bar{K}_1)}{1+r_0^2(\bar{K}_1)}$$

The corresponding BSM-sensitive mode is $D_s \rightarrow \bar{K}_1(\rightarrow \bar{K}\pi\pi)\gamma$.

Method requires D -tagging but unlike TDA, does not depend on strong phases between LH and RH amplitude.

$K_1(1270)$ dominant in charm as $K(1400)$ family phase space suppressed by about factor of 2.

Constraints on up-sector FCNCs are at the level of b -physics in the last millenium. $c \rightarrow u\mu\mu, \gamma$: $|C_{9,10}^{(\prime)}| \lesssim 1$, $|C_7^{(\prime)}| \lesssim 0.3$, $|C_{T,T5}| \lesssim 1$, $|C_{S,P}^{(\prime)}| \lesssim 0.1$.

versus $|C_7^{\text{effSM}}| = \mathcal{O}(0.001)$, $|C_9^{\text{effSM}}| \lesssim 0.01$, $C_{10}^{\text{SM}} = 0$, (GIM !) $C'^{\text{SM}}, C_{S,P,T,T5}^{\text{SM}} = 0$

Charm decays into leptons are plagued by resonance contributions, and $1/m_c$ not ideal 1705.05891. BSM physics can be seen in rates only if very large (still possible!), or in SM null tests, several of which we discussed. SM BGD in $c \rightarrow u$ photon polarization can be measured using U-spin. – Great prospects to test the SM and look for BSM physics in semileptonic and radiative rare D decays, complementary to K, B -decays.

clean = clean enough

Plenty of opportunities for BaBar, BESIII, Belle, Belle II and LHCb

Unique information on flavor in the up-sector

- Current anomalies $R_{K^{(*)}}, R_{D^{(*)}}$ in semileptonic B -meson decays hint at violation of lepton-universality – and breakdown of SM. The April 2017 release of R_{K^*} by LHCb has strengthened the hints and allowed to pin down the Dirac structure: predominantly $V - A$ -type.
- Future data – LNU updates and other observables $R_\Phi, R_{X_s}, \dots, B \rightarrow K^* ee$ – from LHCb and in the nearer future from Belle II are eagerly awaited.
- What makes these LNU-anomalies – iff true – so important? Because they are theoretically clean and intimately linked to "flavor": Look for imprints in other sectors: D, K physics, LFV. [see talks](#)
- In addition, new BSM model-building has been triggered that deserves attention in direct searches at ATLAS and CMS and future colliders.

[Leptoquarks are flavorful and can be in reach of the LHC, where they can provide complementary information to rare decays:](#) $\lambda_{s\ell}, \lambda_{b\ell}, M$ vs $\lambda_{b\ell} \lambda_{s\ell}^*/M^2 \simeq 1/(35 \text{ TeV})^2$
Model-independent upper limit by B_s -mixing $\propto (\lambda_{b\ell} \lambda_{s\ell})^2/M^2$ at $\sim 40 \text{ TeV}$.
bulk of parameter space outside of LHC.

BACK-UP

$c \rightarrow u$ amplitudes are strongly GIM-suppressed:

$$\mathcal{A}_{c \rightarrow u} \simeq \sin \Theta_C [f(m_s^2/m_W^2) - f(m_d^2/m_W^2)] + O(\sin^5 \Theta_C)$$

Resulting (non-resonant) SM branching ratios are $10^{-12} - 10^{-13}$:

q^2 -bin	$\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)_{\text{nr}}^{\text{SM}}$	90% CL limit LHCb'13
full q^2 :	$3.7 \cdot 10^{-12} (\pm 1, \pm 3, {}^{+16}_{-15}, \pm 1, {}^{+4}_{-1}, {}^{+158}_{-1}, {}^{+16}_{-12})$	$7.3 \cdot 10^{-8}$
low q^2 :	$7.4 \cdot 10^{-13} (\pm 1, \pm 4, {}^{+23}_{-21}, {}^{+10}_{-11}, {}^{+11}_{-1}, {}^{+238}_{-23}, {}^{+6}_{-5})$	$2.0 \cdot 10^{-8}$
high q^2 :	$7.5 \cdot 10^{-13} (\pm 1, \pm 6, {}^{+15}_{-14}, \pm 6, {}^{+2}_{-1}, {}^{+136}_{-45}, {}^{+27}_{-20})$	$2.6 \cdot 10^{-8}$

Table 2: Non-negligible uncertainties correspond to (normalization, m_c , m_s , μ_W , μ_b , μ_c , f_+), respectively, given in percent [arXiv:1510.00311](#), see PhD

[thesis of S de Boer \(2017\)](#) for 2-loop effects

Largest uncertainty: μ_c -scale dependence $m_c/\sqrt{2} < \mu_c \leq \sqrt{2}m_c$.

Θ : angle between negatively charged lepton and D in dilepton cms

$$\frac{d\Gamma(D \rightarrow \pi l^+ l^-)}{d \cos \Theta} = \frac{3}{4}(1 - F_H)(1 - \cos^2 \Theta) + A_{FB} \cos \Theta + F_H/2 \quad \text{Bobeth et al '07}$$

SM: $A_{FB}, F_H \simeq 0$ by lorentz-structure and small lepton masses. Both require S,P- and or tensor operators.

Model-independently, striking BSM signals possible (high q^2):

$$|A_{FB}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)| \lesssim 0.6, |A_{FB}(D^+ \rightarrow \pi^+ e^+ e^-)| \lesssim 0.8 \text{ and } F_H(D^+ \rightarrow \pi^+ l^+ l^-) \lesssim 2 \text{ for } l = e, \mu.$$

LFV-rates and dineutrino modes which vanish in SM can be just around the corner (model-independently).

Flavor patterns of leptoquark coupling matrix λ (rows=quark flavor, columns=lepton flavor):

$$\lambda_{ql} \sim \begin{pmatrix} \rho_d \kappa & \rho_d & \rho_d \\ \rho \kappa & \rho & \rho \\ \kappa & 1 & 1 \end{pmatrix}, \quad \begin{pmatrix} 0 & * & 0 \\ 0 & * & 0 \\ 0 & * & 0 \end{pmatrix}, \quad \begin{pmatrix} * & 0 & 0 \\ 0 & * & 0 \\ 0 & * & 0 \end{pmatrix}, \dots$$

LQs make interesting link between quark (hierarchy) and lepton (anarchy? non-abelian discrete?) flavor [1503.01084](#).