

# *Heavy-quark Hadron Production in Nuclear Collisions*

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- *Introduction*
- *Correlation between Strangeness and Charm*
- *Correlation between Strangeness and Baryon Density*
- *Sequential Coalescence*
- *$D_s/D^0$  ( $\Lambda_c/D^0$ ) Enhancement (Suppression)*
- *Summary*

*work by Jiaxing Zhao, Shuzhe Shi, Nu Xu and PZ*

# Hadronization

- *Hadronization in vacuum*

*a non-perturbative process, unsolved problem in physics*

- *Hadronization at finite temperature* (such as in heavy ion collisions)

*statistics should play an important role in hadronization of quark matter.*

*statistical distribution at freeze-out:*

*P.Braun-Munzinger, J.Stachel, J.Wessels and N.Xu, PLB344, 43(1995)*

*coalescence (recombination) models:*

*V.Greco, C.Ko and P.Levai, PRL90, 202302(2003)*

*R.Hwa and C.Yang, PRC70, 024905(2004)*

$$N_{meson} \sim \int d\sigma^\mu p_\mu W(x, p) f_q(x_1, p_1) f_{\bar{q}}(x_2, p_2)$$

*hydro, dynamics, statistics*

- *Two assumptions*

*1) the coalescence probability (Wigner function)*

$$W(x, p) \sim e^{-\frac{x^2}{\langle x \rangle^2}} e^{-\frac{p^2}{\langle p \rangle^2}} \text{ with parameters } \langle x \rangle \text{ and } \langle p \rangle$$

*2) all the hadrons (light- and heavy-quark hadrons) are created at the same surface (time).*

## Limit: Quarkonia

- Quarkonia in vacuum

non-relativistic potential model with Cornell potential:

C.Quigg and J.Rosner, *Phys. Rep.* 56, 167(1979)

- Quarkonia at finite temperature (such as in heavy ion collisions)

non-relativistic potential model with lattice simulated potential:

H.Satz, *J.Phys.* G32, R25(2006)

→ 1) sequential suppression, the dissociation temperature

$$T_{J/\psi} > T_{\psi'} \simeq T_{\chi_c}$$

$J/\psi$  is produced earlier than  $\psi'$  and  $\chi_c$ .

Heavy-quark hadrons are sequentially produced.

→ 2) calculable Wigner function

$$W(x, p) = \int d^4y e^{-ipy} \psi(x + \frac{y}{2}) \psi^*(x - \frac{y}{2})$$

- Quarkonium regeneration:

P.Braun-Munzinger and J.Stachel, *PLB*490, 196(2000)

R.Thews, M.Schroedter and J.Rafelski, *PRC*63, 054905(2001)

L.Grandchamp and R.Rapp, *NPA*709, 415(2002)

L.Yan, N.Xu and PZ, *PRL*97, 232301(2006)



Langevin equation for heavy quarks with attractive force between correlated  $c$  and  $\bar{c}$ ,

C.Young and E.Shuryak, *PRC*79, 034907(2009)

$$\frac{d\vec{p}}{dt} = -\gamma\vec{p} + \vec{\eta} - \vec{\nabla}V$$

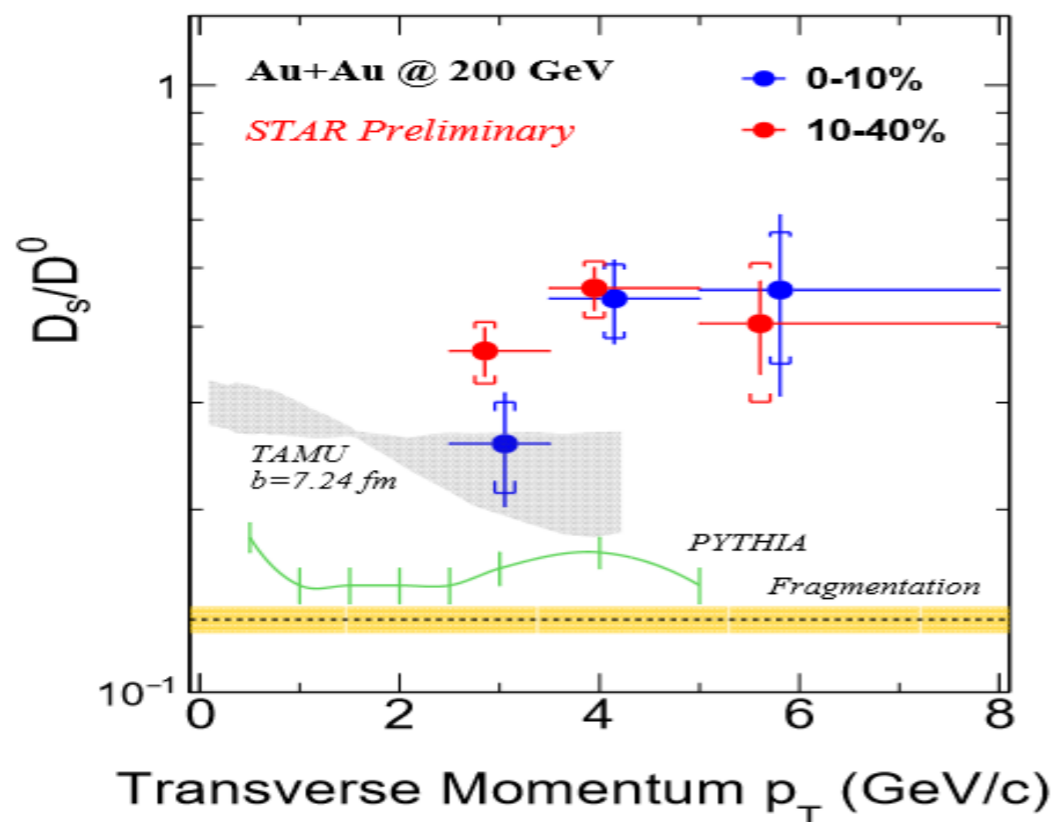
→ increasing charmonium surviving probability.

# Strangeness Enhancement

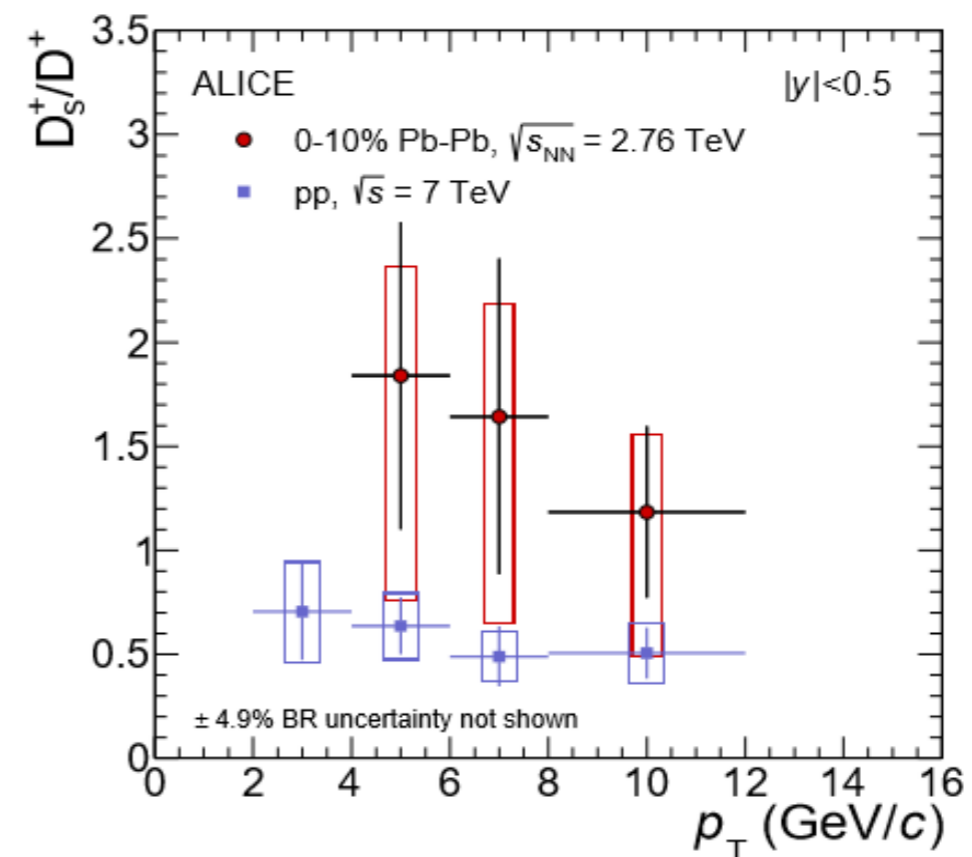
- Well-known strangeness enhancement due to thermal production in QGP, supported by experimental data in heavy ion collisions.

*P.Koch, B.Muller and J.Rafelski, Phys. Rept. 142, 167(1986)*

- Strong  $D_s/D^0$  enhancement at RHIC and LHC



*L.Zhou [STAR], NPA967, 620(2017)*



*J.Adam et. al. [ALICE], JHEP 1603, 082(2016)*

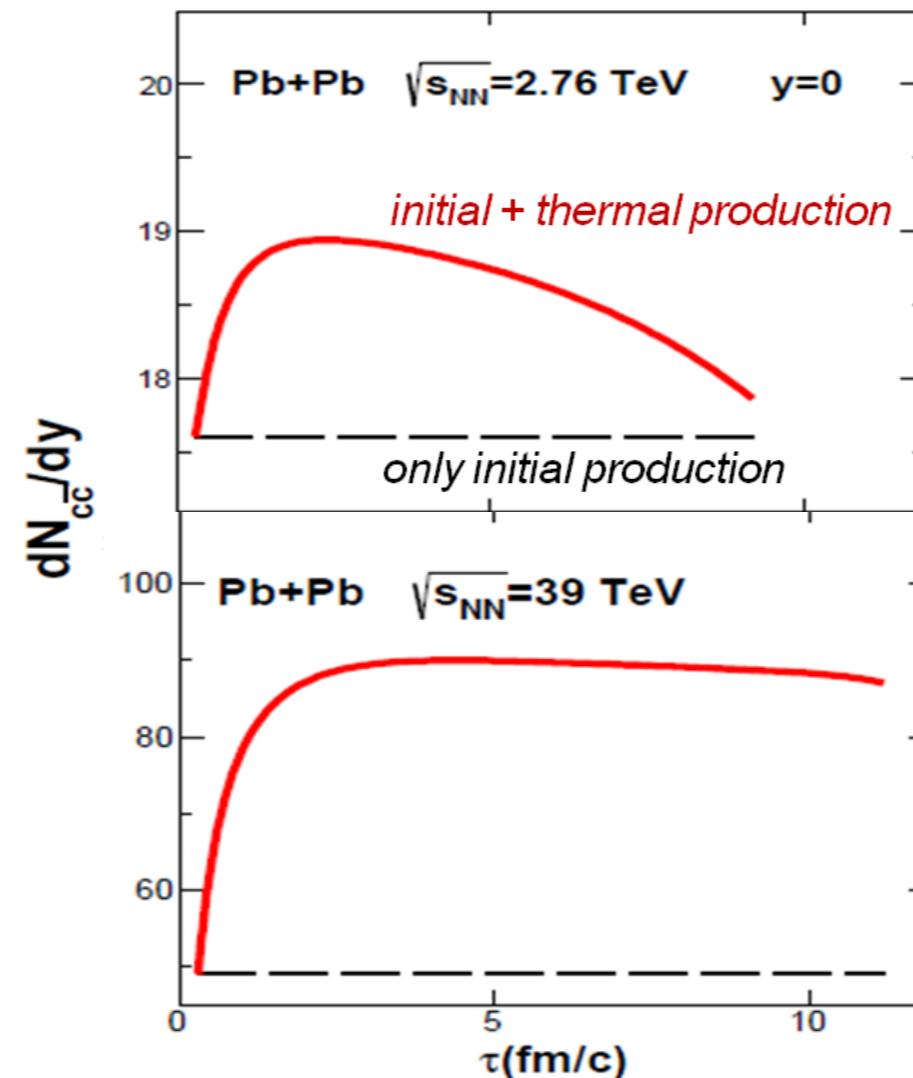
- $D_s$  enhancement via strangeness enhancement

*M.He, R.Fries and R.Rapp, PRL110, 112301(2013)*

*there is still a sizeable difference between strangeness enhancement and data.*

## Charm Conservation

### ■ Charm quark thermal production in QGP



*K.Zhou, Z.Chen, C.Greiner and PZ,. PLB758, 434(2016)*

■ Even at LHC energy, heavy quark production is controlled by the initial hard process, the thermal production in QGP can be safely neglected.

→ Charm quark number is conserved during the evolution of HIC.

## Correlation between Strangeness and Charm

### ■ Charm conservation in heavy ion collisions

*P.Braun-Munzinger and J.Stachel, PLB490, 196(2000)*

*M.Gorenstein, A.Kostyuk, H.Stoecker and W.Greiner, PLB509, 277(2001)*

*Y.Oh, C.Ko, S.Lee and S.Yasui, PRC79, 044905(2009)*

*S.Plumari, V.Minissale, S.Das and V.Greco, EPJC78, 348(2018)*

*If all charmed hadrons are simultaneously produced, the constraint of charm conservation is introduced via a normalization constant  $g_c$ ,*

*# of any singly charmed hadron  $\sim g_c$*

*→ no effect on the ratio  $D_s/D^0$  and  $\Lambda_c/D^0$  !*

■ *If charmed hadrons are sequentially produced, more charm quarks are involved in the earlier production and less in the later production, due to charm conservation.*

*→ different charm conservation effect on different hadrons !*

### ■ Correlation between strangeness and charm:

*When  $D_s$  is produced earlier than  $D^0$ ,*

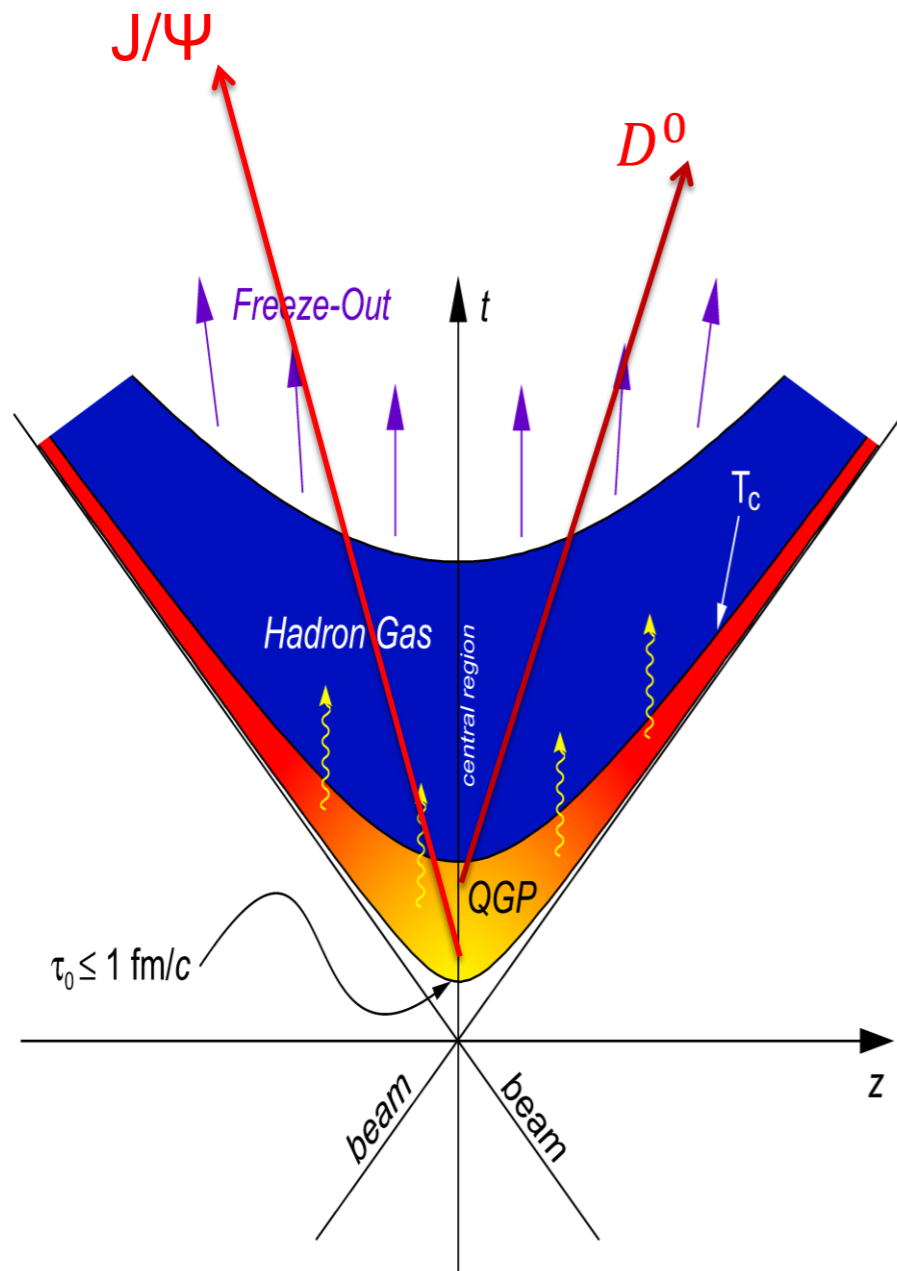
*$D_s$  enhancement by strangeness enhancement*

*→  $D_0$  suppression by charm conservation*

*→ an extra  $D_s/D^0$  enhancement !*

# Sequential Coalescence Model

J.Zhao, S.Shi, N.Xu and PZ, arXiv: 1805.10858



- **Step 1: Sequential production temperature from 2-body (3-body) Dirac equations for  $c\bar{q}$  ( $q = u, d, s, c$ ),**

→ 1) binding energy  $\varepsilon(T)$ ,  
production (dissociation) temperature  
 $\varepsilon(T_D) = 0$

2) wave function  $\psi(x|T)$   
coalescence probability

$$W(x, p|T) = \int d^4y e^{-ipy} \psi(x + \frac{y}{2}|T) \psi^*(x - \frac{y}{2}|T)$$

- **Step 2: Sequential production time from hydrodynamics for QGP evolution**

→ production time  $t(\vec{x}, T_D)$

- **Step 3: Sequential coalescence with charm conservation**

$$N \sim \int d\sigma^\mu p_\mu W(x, p) f_q(x_1, p_1) f_{\bar{q}}(x_2, p_2)$$

total charm quark number:  $N_c$

total charm quark number in the sequential coalescence process:

$$N_c - \sum (\text{all used charm quarks})$$



## Step 1: Sequential Production Temperature from 2-body Dirac Equations

$T = 0$ : H.Crater, J.Yoon and C.Wong, *PRD79*, 034011(2009)

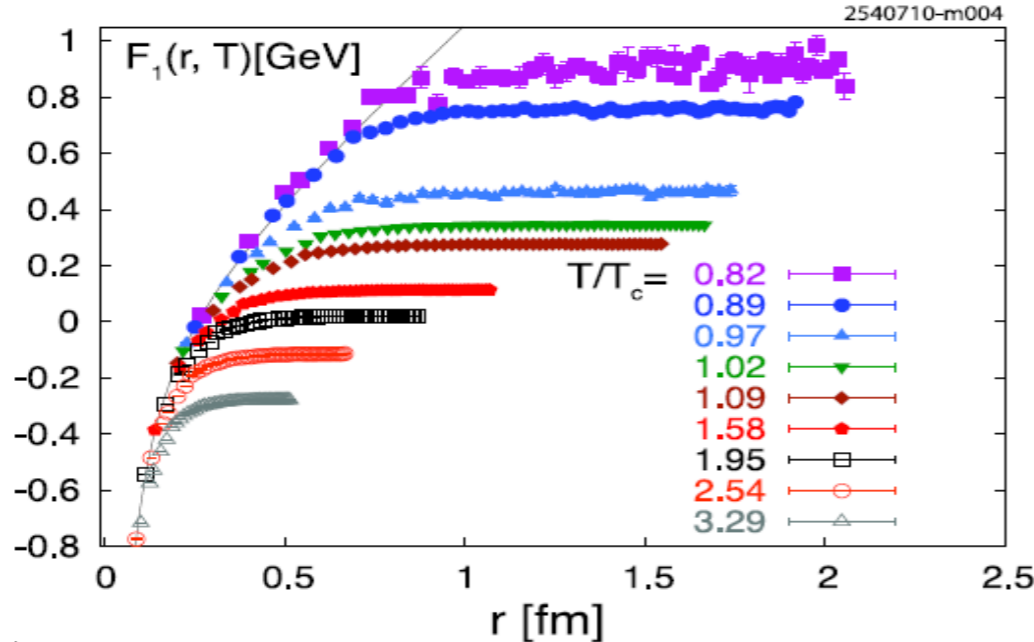
$T \neq 0$ : S.Shi, X.Guo and PZ, *PRD88*, 014021(2013)

$$\begin{aligned} & \left[ -\frac{d^2}{dr^2} + \frac{j(j+1)}{r^2} + 2m_w B + B^2 + 2\epsilon_w A - A^2 + \Phi_D - 3\Phi_{SS} \right] u_0 + 2\sqrt{j(j+1)} (\Phi_{SOD} - \Phi_{SOX}) u_1^0 = b^2 u_0, \\ & \left[ -\frac{d^2}{dr^2} + \frac{j(j+1)}{r^2} + 2m_w B + B^2 + 2\epsilon_w A - A^2 + \Phi_D - 2\Phi_{SO} + \Phi_{SS} + 2\Phi_T - 2\Phi_{SOT} \right] u_1^0 \\ & + 2\sqrt{j(j+1)} (\Phi_{SOD} + \Phi_{SOX}) u_0 = b^2 u_1^0, \\ & \left[ -\frac{d^2}{dr^2} + \frac{j(j-1)}{r^2} + 2m_w B + B^2 + 2\epsilon_w A - A^2 + \Phi_D + 2(j-1)\Phi_{SO} + \Phi_{SS} + \frac{2(j-1)}{2j+1} (\Phi_{SOT} - \Phi_T) \right] u_1^+ \\ & + \frac{2\sqrt{j(j+1)}}{2j+1} (3\Phi_T - 2(j+2)\Phi_{SOT}) u_1^- = b^2 u_1^+, \\ & \left[ -\frac{d^2}{dr^2} + \frac{(j+1)(j+2)}{r^2} + 2m_w B + B^2 + 2\epsilon_w A - A^2 + \Phi_D - 2(j+2)\Phi_{SO} + \Phi_{SS} + \frac{2(j+2)}{2j+1} (\Phi_{SOT} - \Phi_T) \right] u_1^- \\ & + \frac{2\sqrt{j(j+1)}}{2j+1} (3\Phi_T + 2(j-1)\Phi_{SOT}) u_1^+ = b^2 u_1^- \end{aligned} \quad (2)$$

$$\begin{aligned} \Phi_D &= M + F'^2 + K'^2 - \nabla^2 F + 2K'P - 2\left(F' + \frac{1}{r}\right)Q, \\ \Phi_T &= \frac{1}{3} \left[ N + 2F'K' - \nabla^2 K + \left(3F' - K' + \frac{3}{r}\right)P + \left(F' - 3K' + \frac{1}{r}\right)Q \right] \\ \Phi_{SO} &= -\frac{F'}{r} + K'P - \left(F' + \frac{1}{r}\right)Q, \\ \Phi_{SS} &= O + \frac{2}{3}F'K' - \frac{1}{3}\nabla^2 K + \frac{2}{3}K'P - 2\left(F' + \frac{1}{3r}\right)Q, \\ \Phi_{SOT} &= -\frac{K'}{r} + \left(F' + \frac{1}{r}\right)P - K'Q, \\ F &= \frac{1}{2}L - \frac{3}{2}G, \\ G &= -\frac{1}{2} \ln \left( 1 - 2\frac{A}{m_m} \right), \\ K &= \frac{1}{2}L + \frac{1}{2}G, \\ L &= \ln \sqrt{1 + \frac{2m_w B + B^2}{m_Q^2 (1 - 2A/m_m)}}, \\ M &= -\frac{1}{2}\nabla^2 G + \frac{3}{4}G'^2 + G'F' - K'^2, \\ N &= \frac{1}{3} \left[ \nabla^2 K - \frac{1}{2}\nabla^2 G + \frac{3}{2}\frac{G' - 2K'}{r} + F'(G' - 2K') \right] \\ O &= \frac{1}{3}\nabla^2 (K + G) - \frac{1}{3}F'(G' + K') - \frac{1}{2}G'^2, \\ P &= \frac{\sinh 2K}{r}, \\ Q &= \frac{\cosh 2K - 1}{r} \end{aligned}$$

$$b^2 = \frac{1}{4} \left[ m_m^2 - 2(m_{q1}^2 + m_{q2}^2) + (m_{q1}^2 - m_{q2}^2)^2 / m_m^2 \right]$$

O.Kaczmarek, *EPJC* 61, 811(2009)





## Step 2: Sequential Production Time from Hydrodynamic Equations

### ■ Sequential production temperature

TABLE I. Meson masses in vacuum and the comparison with the experimental data [19].

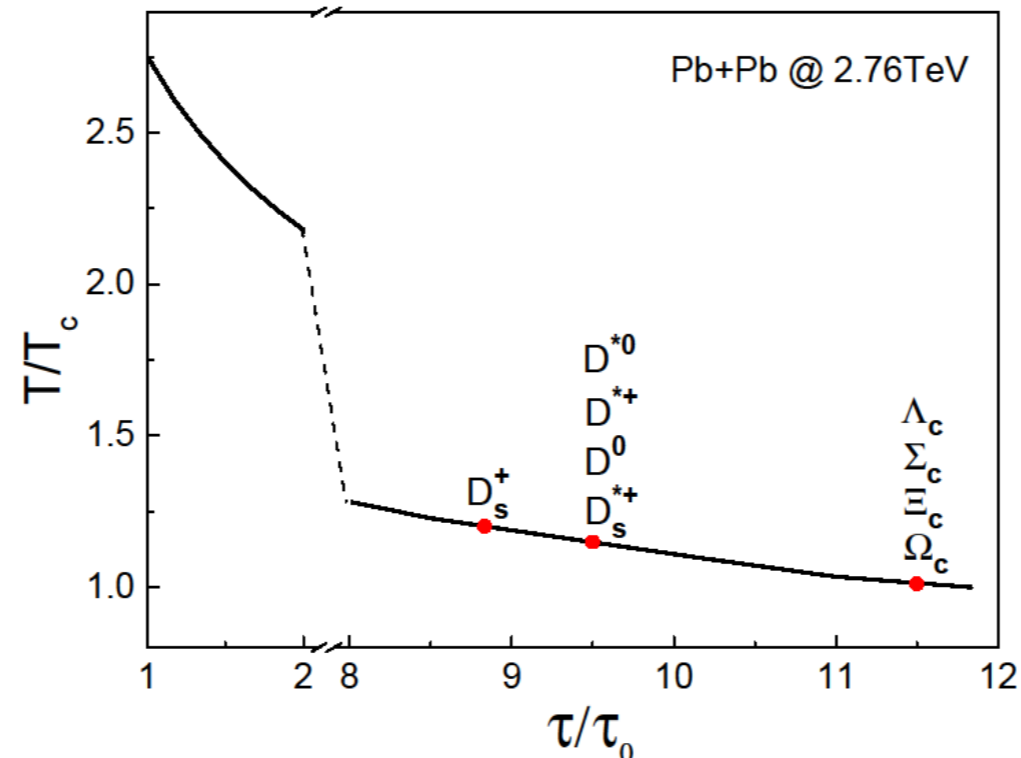
| Meson             | $n^{2s+1}l_j$     | Experiment (GeV) | Theoretical (GeV) |
|-------------------|-------------------|------------------|-------------------|
| $\phi:s\bar{s}$   | $1^3S_1 + 1^3D_1$ | 1.019            | 1.096             |
| $D:c\bar{u}$      | $1^1S_0$          | 1.865            | 1.929             |
| $D^*:c\bar{u}$    | $1^3S_1 + 1^3D_1$ | 2.010            | 1.989             |
| $D_s:c\bar{s}$    | $1^1S_0$          | 1.968            | 1.978             |
| $D_s^*:c\bar{s}$  | $1^3S_1 + 1^3D_1$ | 2.112            | 2.037             |
| $J/\psi:c\bar{c}$ | $1^3S_1 + 1^3D_1$ | 3.097            | 3.045             |
| $\psi':c\bar{c}$  | $2^3S_1 + 1^3D_1$ | 3.686            | 3.609             |
| $\chi_1:c\bar{c}$ | $1^3P_1$          | 3.511            | 3.395             |

$$V = F$$

$$T_D/T_c \simeq \begin{cases} 1.20 & D_s \\ 1.15 & D^0 \\ 1 & \Lambda_c \end{cases}$$

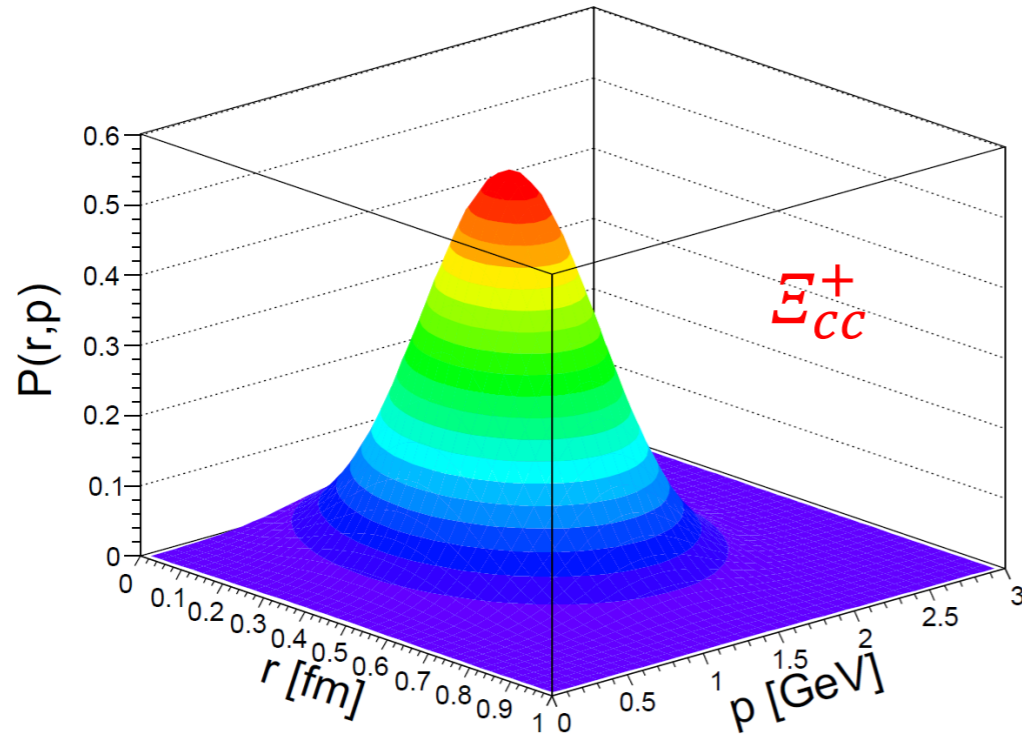
### ■ Sequential production time

ideal hydrodynamics:  $\partial^\mu T_{\mu\nu} = 0 + \partial^\mu n_\mu = 0 \rightarrow \tau(\vec{x}|T_D)$

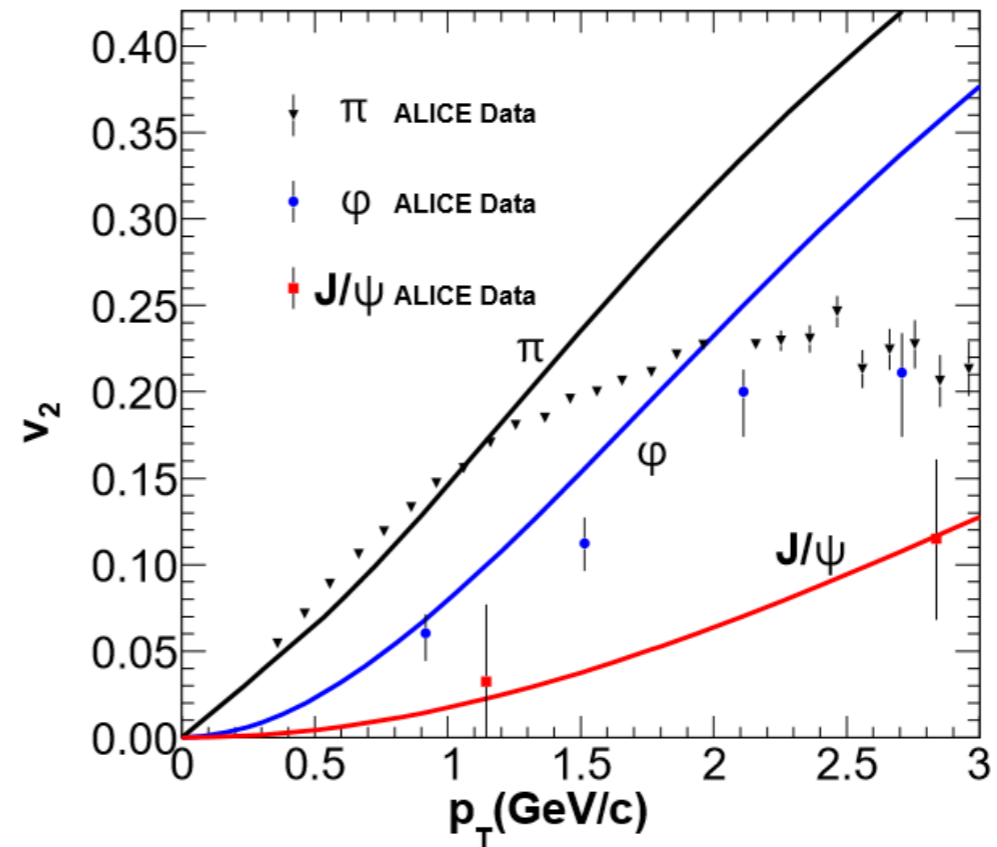
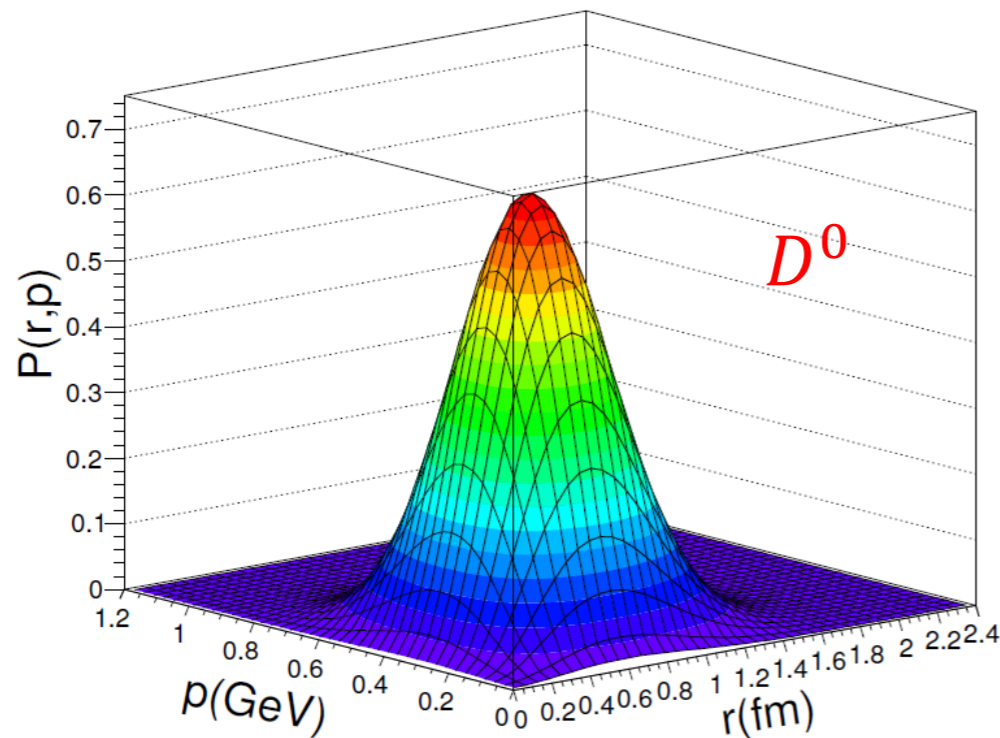


## Step 3: Sequential Coalescence

$$\frac{dN}{d^2P_T d\eta} = C \int \frac{P^\mu d\sigma_{\mu\nu}(R)}{(2\pi)^3} \frac{d^4r d^4p}{(2\pi)^3} f_c(r_1, p_1) f_{\bar{q}}(r_2, p_2) W(r, p)$$



*J.Zhao, H.He and PZ, PLB771, 349(2017)*



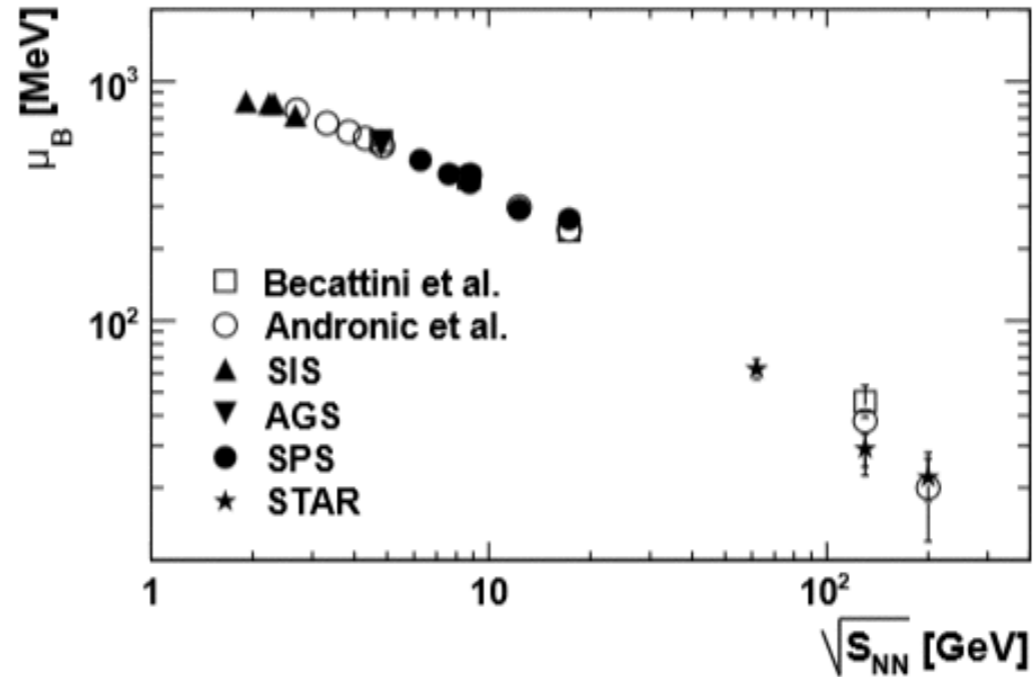
*S.Shi, X.Guo and PZ, PRD88, 014021(2013)*

# Light & Strange Quark Distributions

- **light quarks  $u$  and  $d$ :**  
equilibrium distribution

$$f_q = \frac{N_q}{e^{(u^\mu p_\mu - \mu_q)/T} + 1}$$

STAR Collaboration. *Phys. Rev. C* 79,034909(2009)

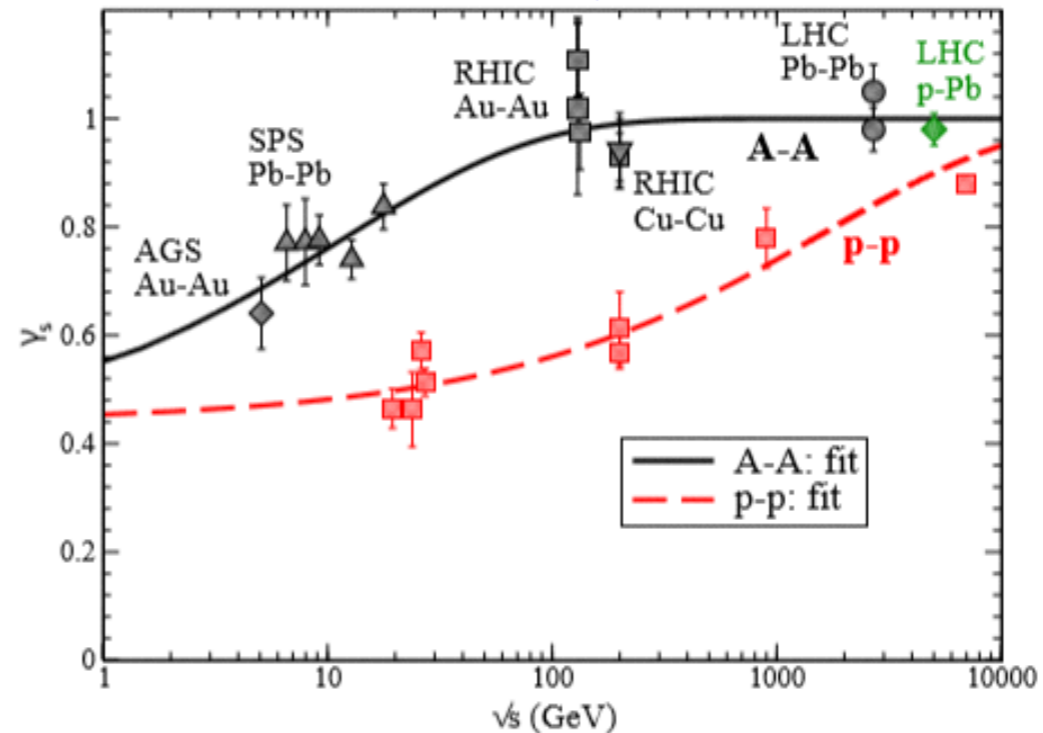


- **strange quark  $s$ :**  
equilibrium distribution with strangeness fugacity

$$f_s = \frac{N_s \lambda_s}{e^{u^\mu p_\mu / T} + 1}$$

$$\lambda_s = \begin{cases} 0.85 & \text{at RHIC} \\ 1 & \text{at LHC} \end{cases}$$

H. Satz et al. *Int. J. Mod. Phys. E* 26, 1750081(2017)



# Charm Quark Distribution

- **Partial thermalization:**  $f_c = r_c \rho_c(x) [\alpha f_{th}(p) + \beta f_{pp}(p)]$

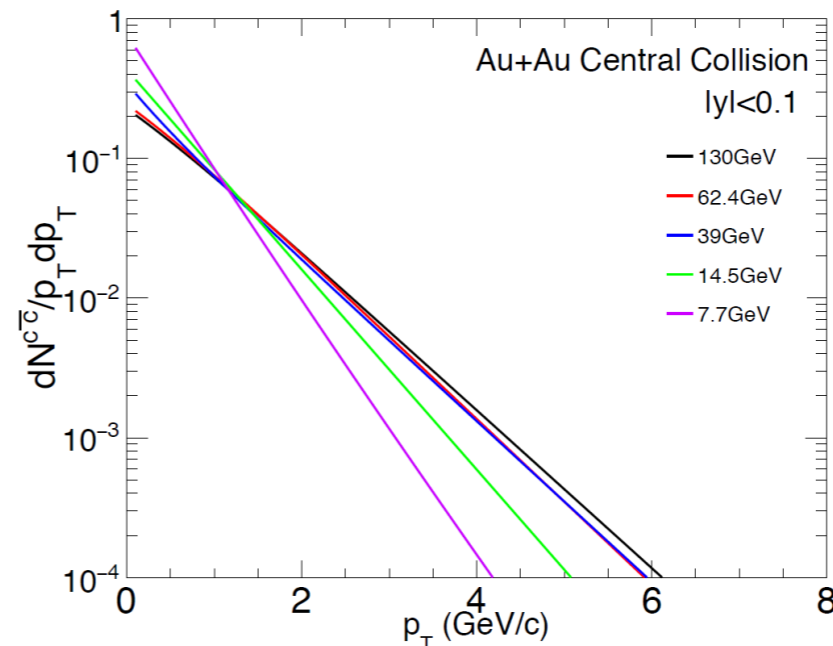
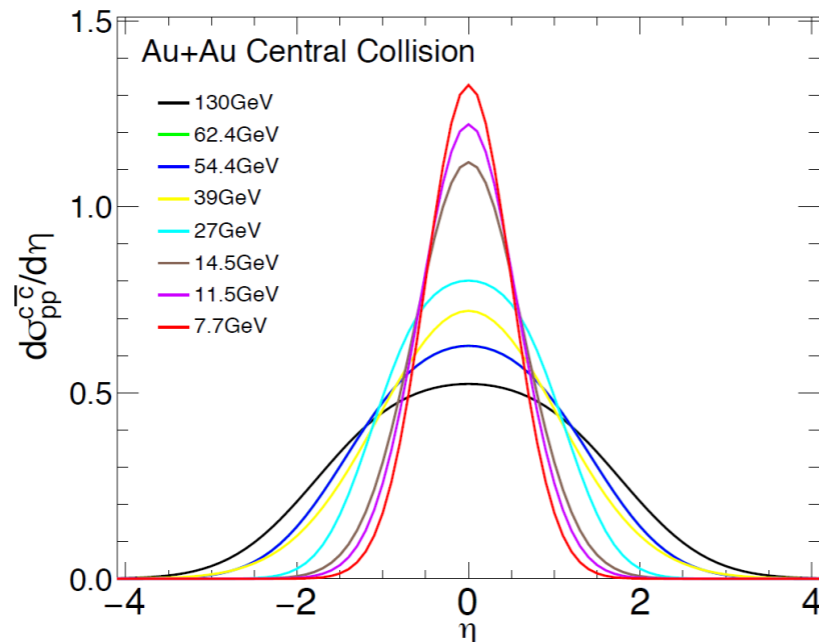
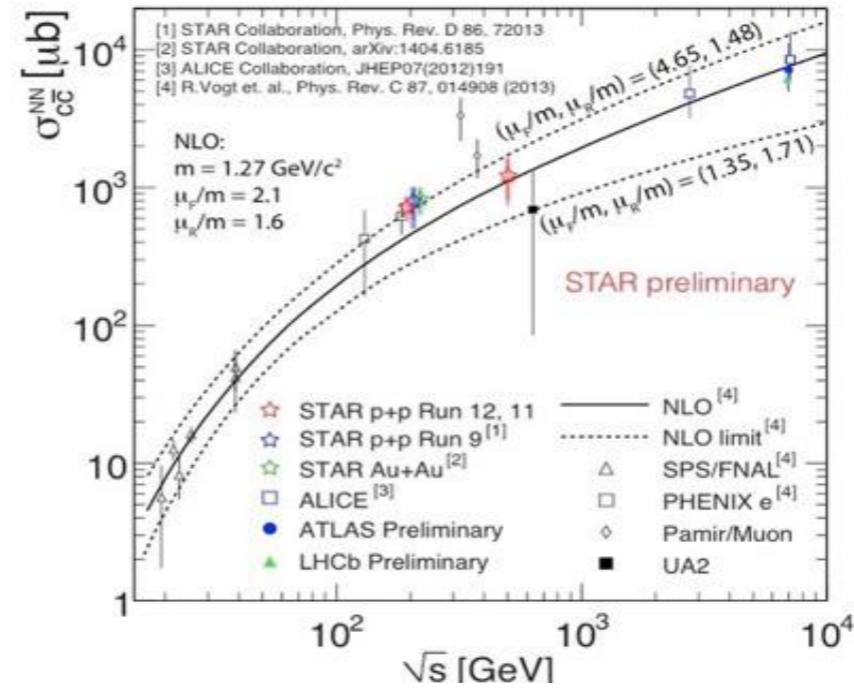
$$\rho_c(x) = T_A(x_T) T_B(x_T - b) \frac{\cosh \eta}{\tau} \frac{d\sigma_{pp}^{c\bar{c}}}{d\eta}$$

- **Sequential thermalization:**

$$(\alpha, \beta) = \begin{cases} (0.4, 0.6) & D_s \\ (0.5, 0.5) & D^0 \\ (0.6, 0.4) & \Lambda_c \end{cases}$$

- **Charm conservation:**

$$r_c = \begin{cases} 1 & D_s \\ 1 - N_{D_s}/N_c (\sim 90\%) & D^0 \\ 1 - N_D/N_c (\sim 60\%) & \Lambda_c \end{cases}$$



Normalized rapidity and transverse momentum distributions with PYTHIA8

## *Hadron Decay after Coalescence*

*Decay from excited states to ground state (from PDG book)*

*to  $D^0$ : 100% of  $D^{*0}$  and 68% of  $D^{*+}$*

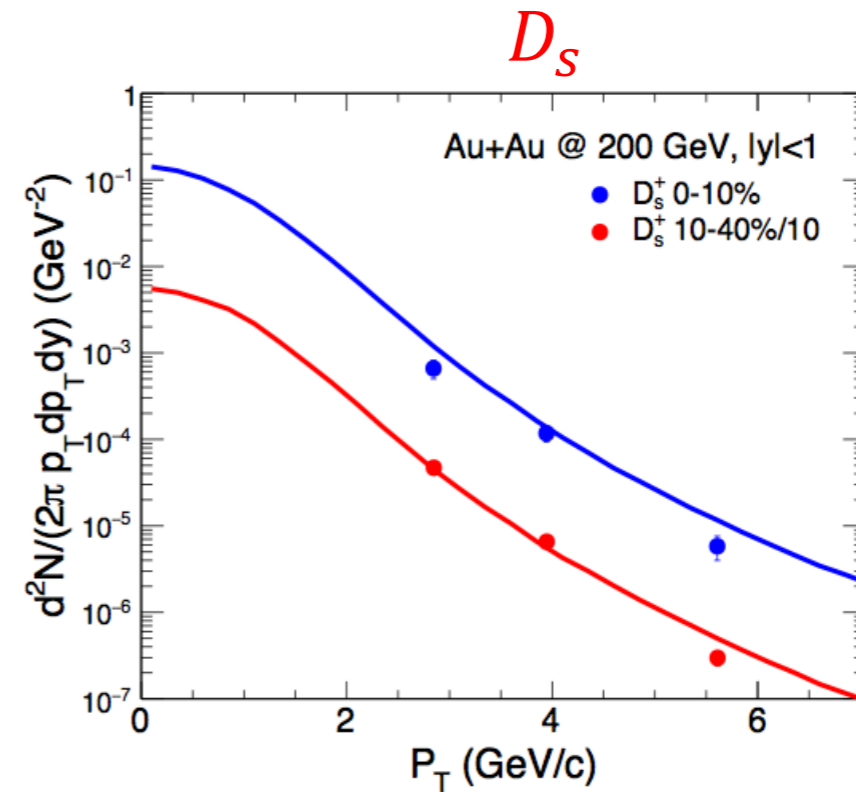
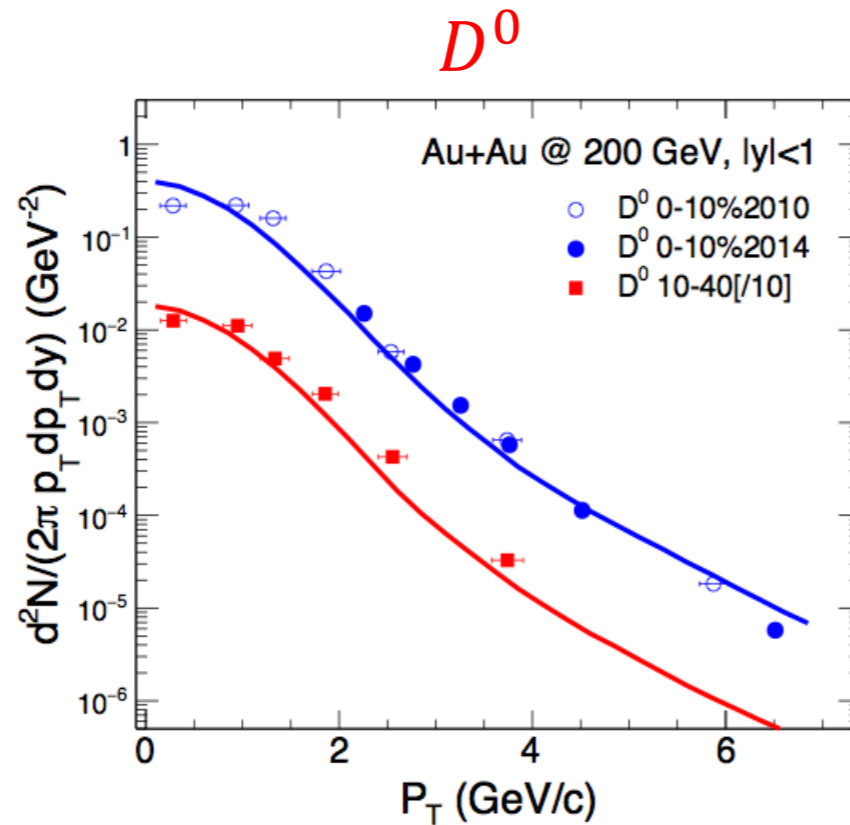
*to  $D_s^+$ : 100% of  $D_s^{*+}$*

*92% of  $\Lambda_c$  is from the excited state decay*

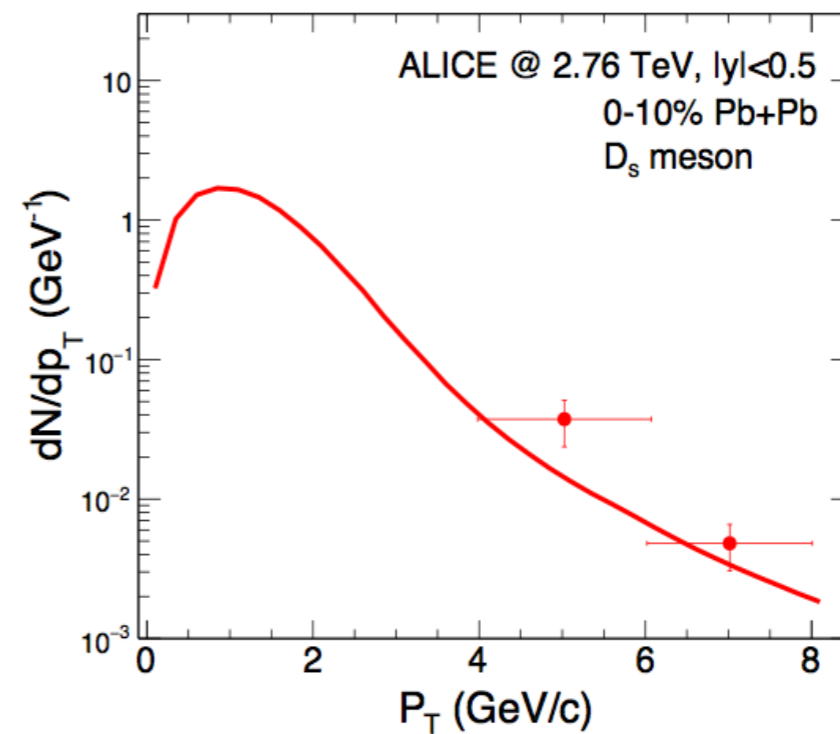
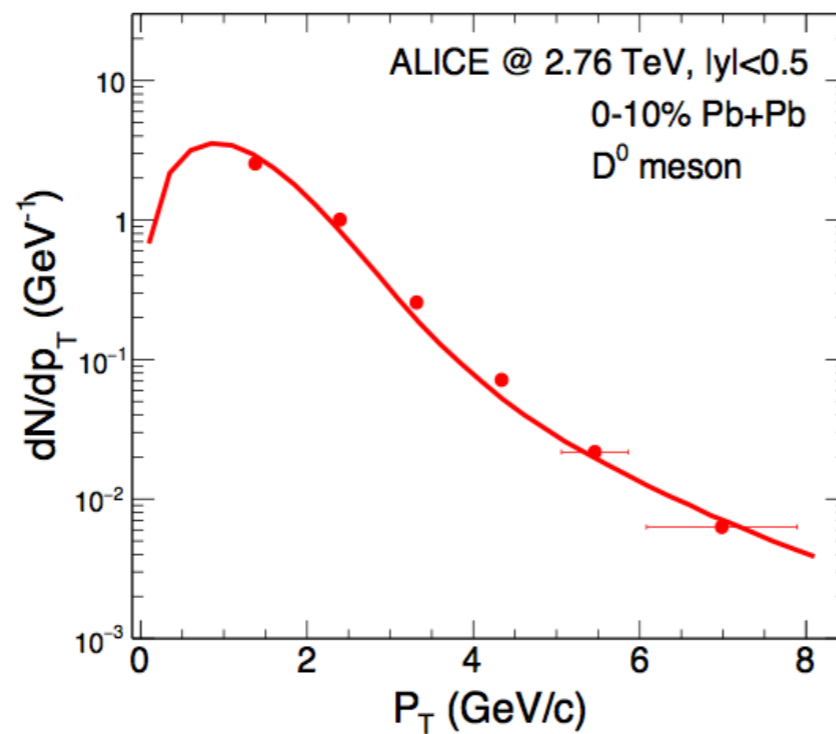
# Charmed Hadron $P_T$ Distribution

J.Zhao, S.Shi, N.Xu and PZ, arXiv: 1805.10858

RHIC



LHC

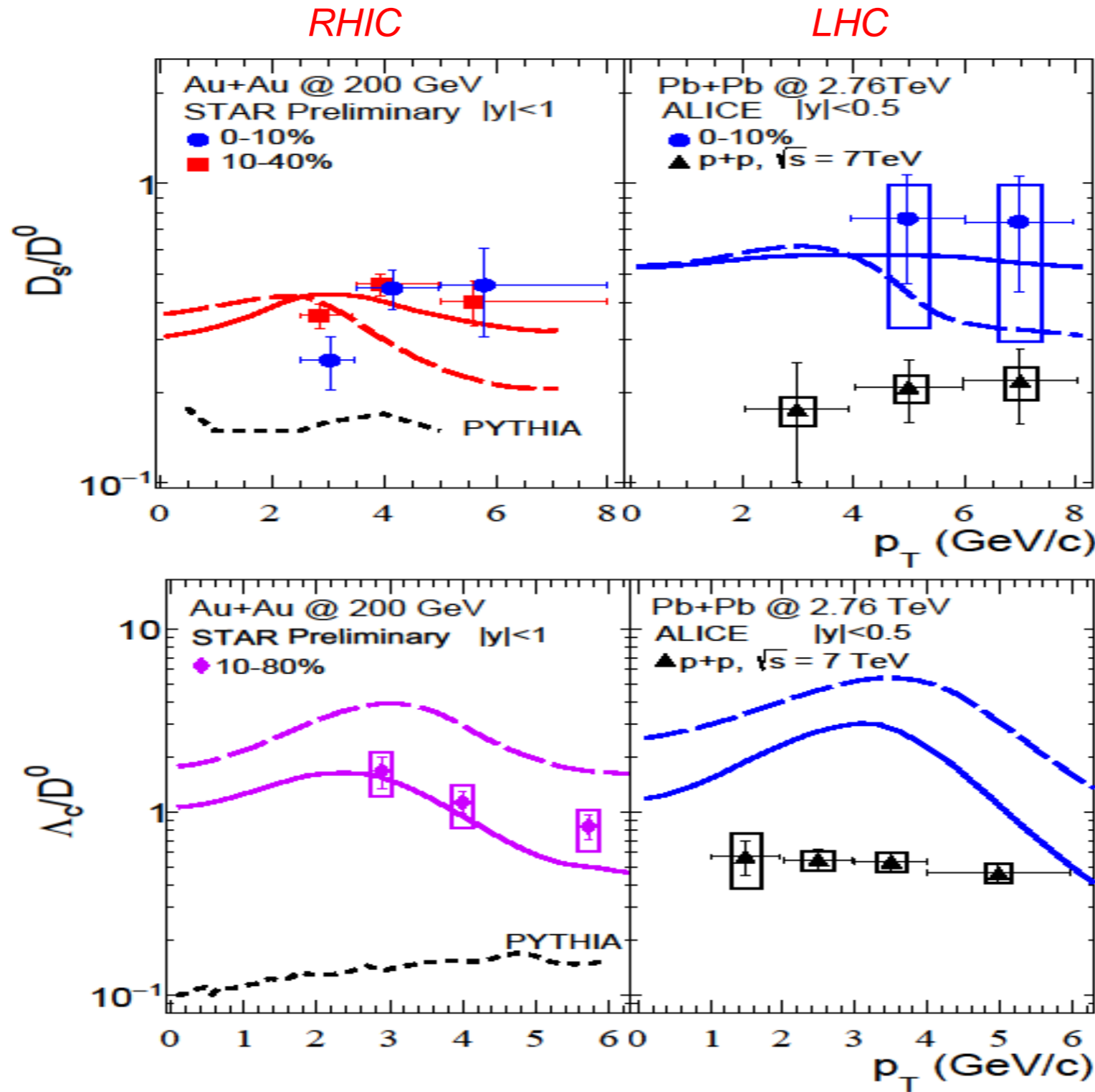


*the shape is controlled by charm quark thermalization, namely the value of  $\alpha$ .*



# Yield Ratios

J.Zhao, S.Shi, N.Xu and PZ, arXiv: 1805.10858



Solid lines:  
with charm conservation

Dashed lines:  
without charm conservation

Charm conservation increases the ratio  $D_s/D^0$ ,  
but sequential thermalization decreases the ratio at low  $p_T$  and increases the ratio at high  $p_T$ .

# Correlation between Strangeness and Baryon Density

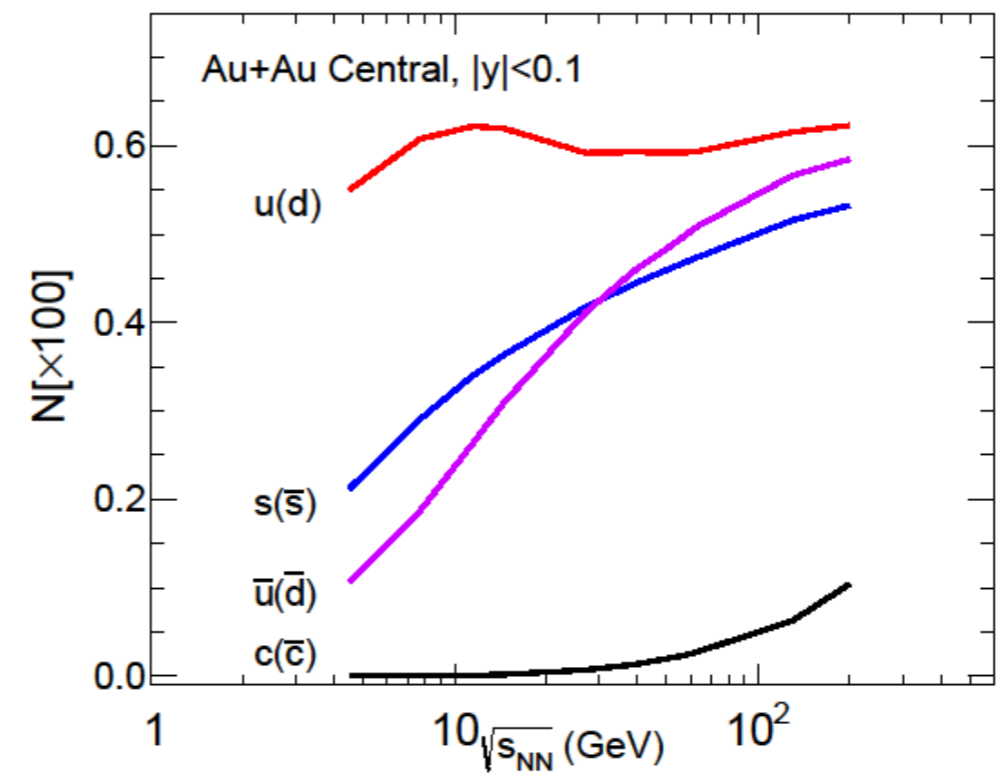
## ■ Baryon density effect

$$f_{u,d} = \frac{N_{u,d}}{e^{(u^\mu p_\mu - \mu_B/3)/T} + 1}$$

$$f_s = \frac{N_s \lambda_s}{e^{u^\mu p_\mu/T} + 1}$$

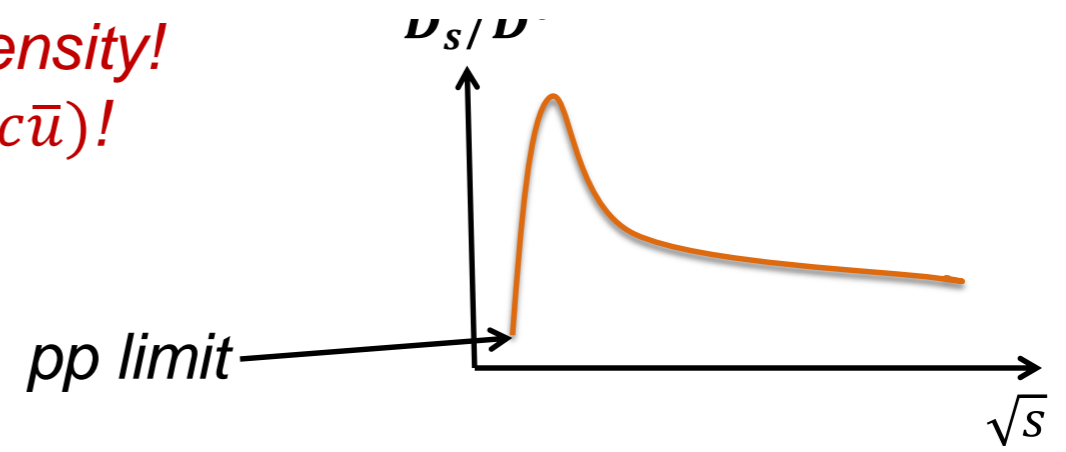
At high baryon density, more  $u$  and  $d$  quarks, less  $\bar{u}$  and  $\bar{d}$  quarks, and probably  $n_{\bar{u}} < n_{\bar{s}}$  !

Quark number density at  $\vec{r} = 0$ :

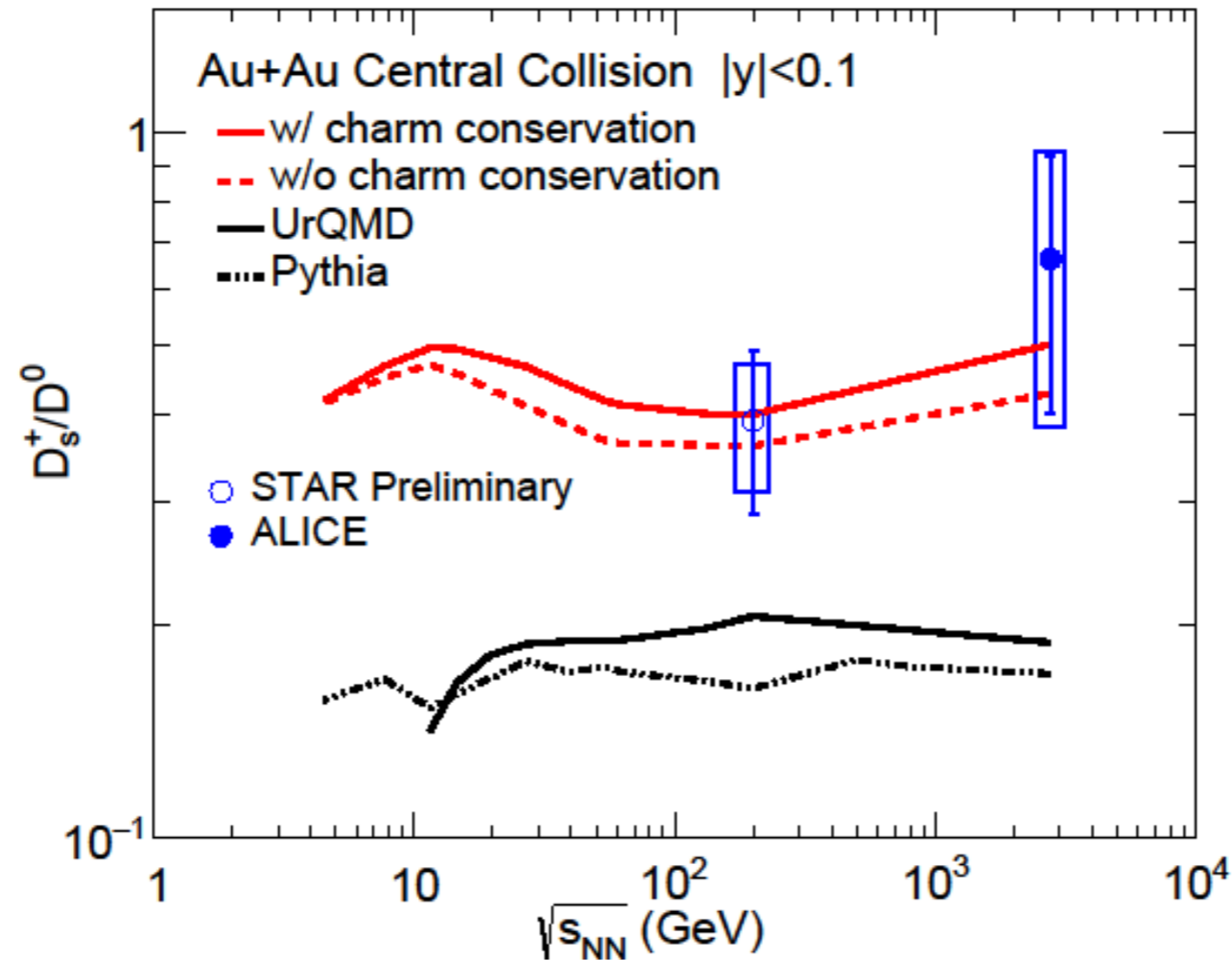


## ■ Strangeness enhancement at high baryon density!

$D_s(c\bar{s})$  enhancement in comparison with  $D^0(c\bar{u})$ !

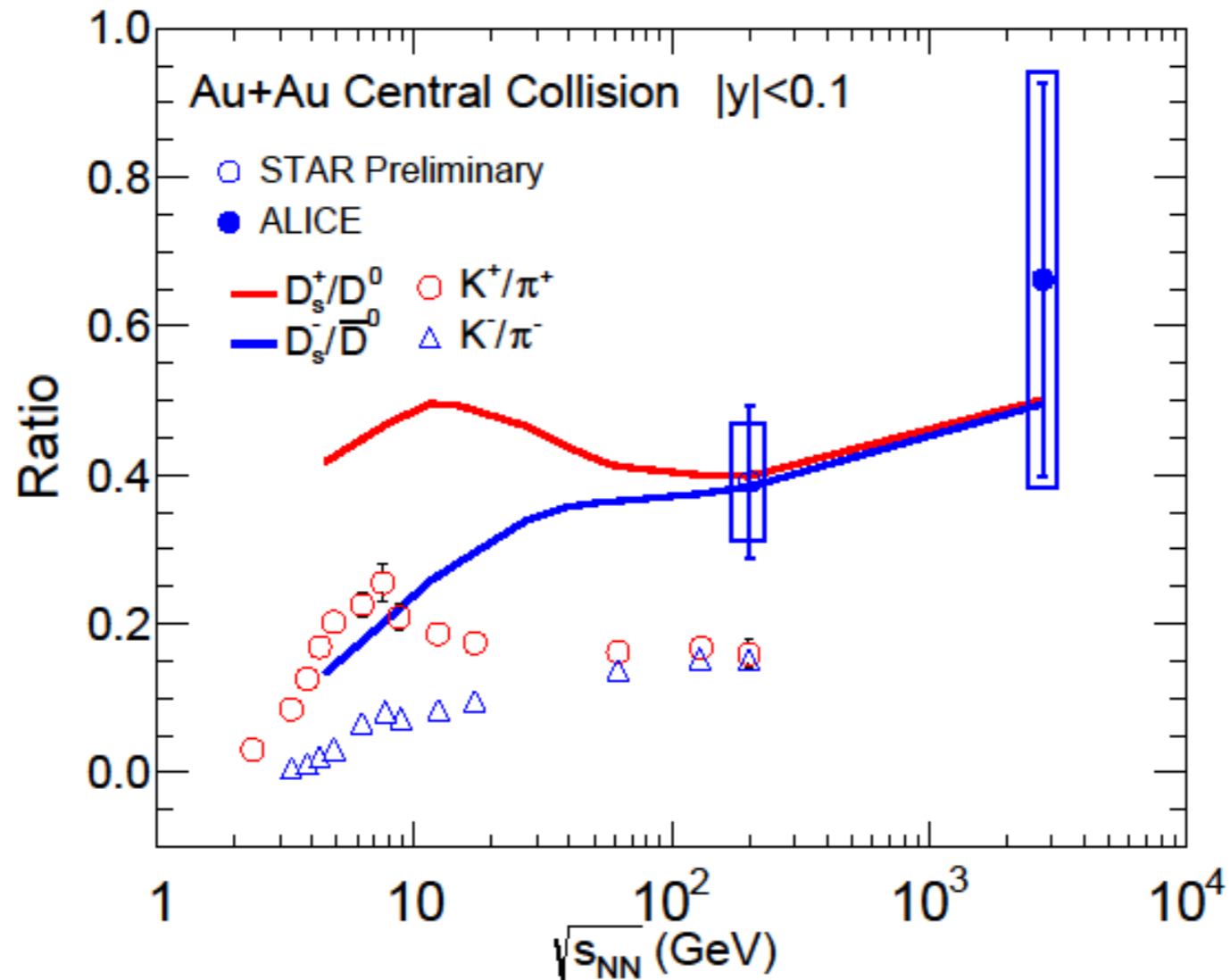


$$D_s/D^0(\sqrt{s})$$



- *Very strong  $D_s/D^0$  enhancement at about  $\sqrt{s} = 10$  GeV where the baryon density is the largest.*
- *The decreasing ratio at very low  $\sqrt{s}$  is due to the disappearance of  $s$ -quark thermal production, or the disappearance of the QGP fireball.*

## Comparison with $K/\pi$



- *The behavior of  $D_s^+/D^0$  ( $D_s^-/\bar{D}^0$ ) is similar to  $K^+/\pi^+$  ( $K^-/\pi^-$ ).*
- *The two peaks locate at the largest baryon density.*

## Summary

- *We developed a sequential coalescence model with charm conservation and continuous charm thermalization.*
- *The charm conservation significantly enhances (suppresses) the ratio  $D_s/D^0$  ( $\Lambda_c/D^0$ ).*
- *The peak of  $D_s/D^0(\sqrt{s})$  in the energy region of FAIR/NICA/HIAF can be considered as a signal of QGP phase transition.*



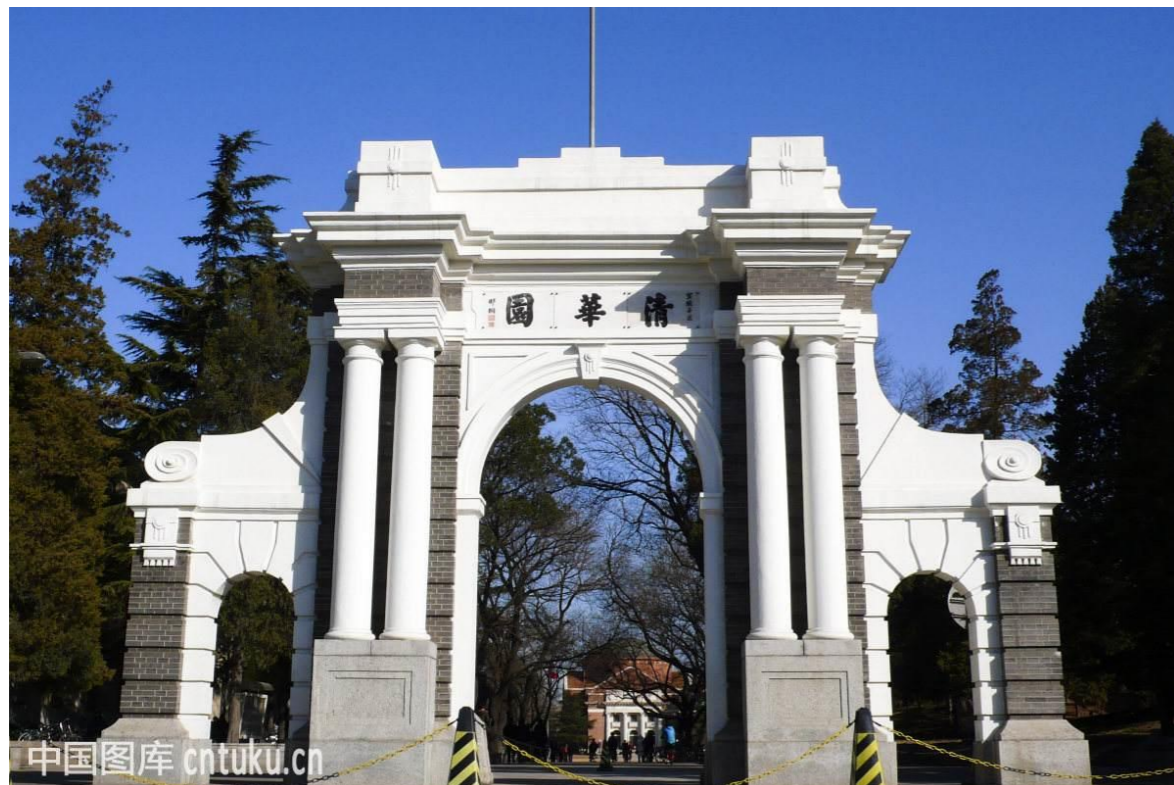
## *Chirality Workshop 2019*

*The 5<sup>th</sup> Workshop on Chirality, Vorticity and Magnetic Field  
in Heavy Ion Collisions*

*The 1<sup>st</sup> (2015), 2<sup>nd</sup> (2016), and 3<sup>rd</sup> (2017) workshops at UCLA*

*The 4<sup>th</sup> workshop at Florence*

- *Place: Tsinghua University, Beijing*
- *Date: April 8-12, 2019*



*You are welcome to join the workshop!*