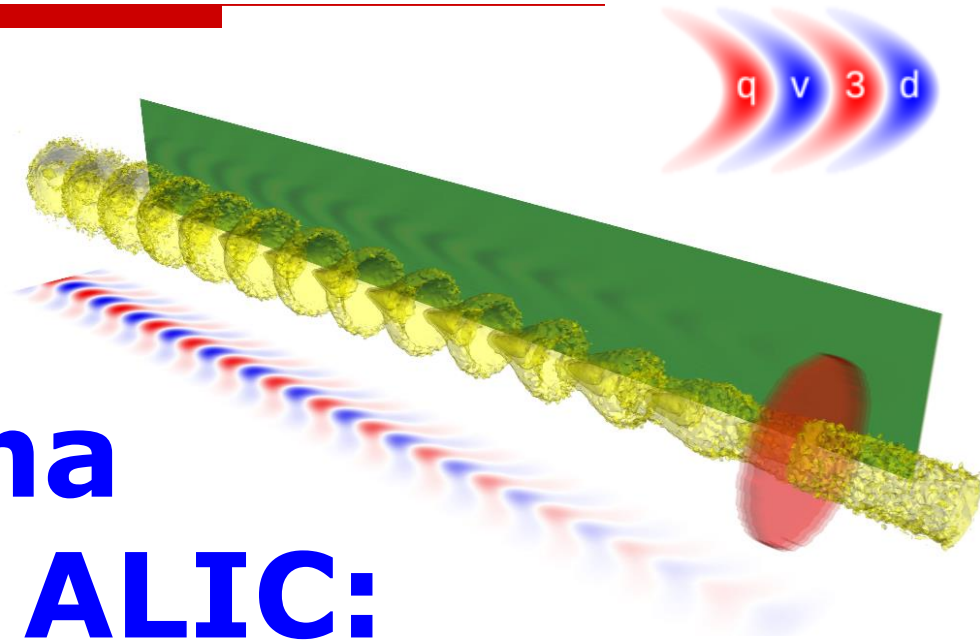


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Institute for Theoretical Physics I
University of Dusseldorf, Germany

Co-axial hollow plasma channels for ALIC: TeV acceleration



ALEGRO, CERN, 26 March 2019

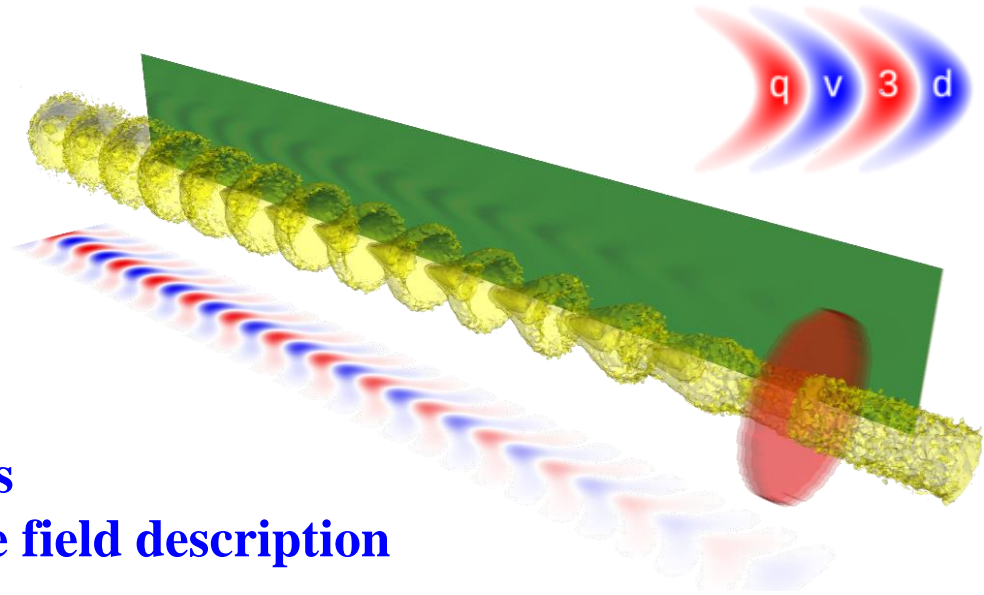
Outline

- **Hollow plasma channel:
control of hosing by a co-axial filament**
 - **Options to create the plasma structure**
 - **TeV acceleration
in a hollow plasma channel
with a hollow on-axis filament**
-

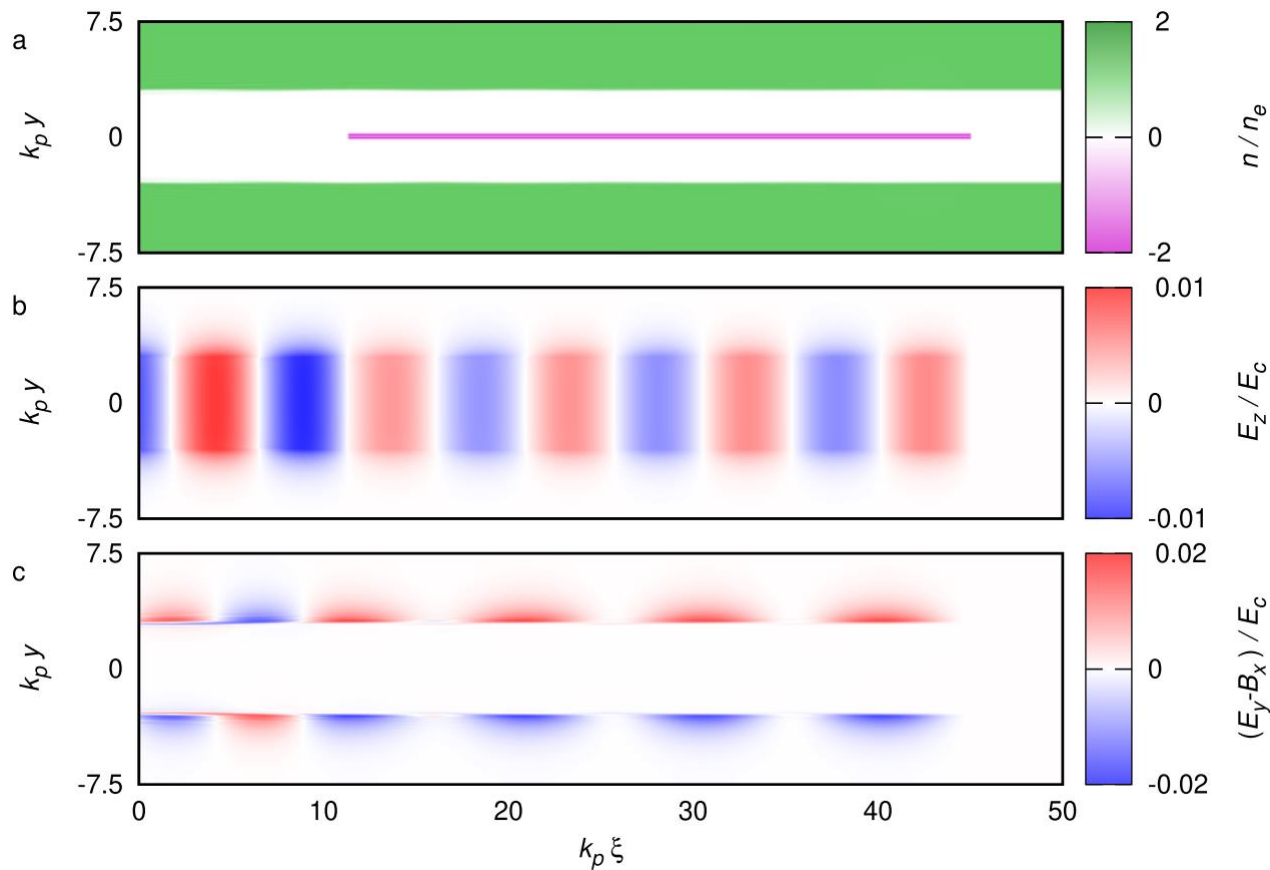
Quasi-static PIC simulations

Quasi-static 3D PIC code QV3D

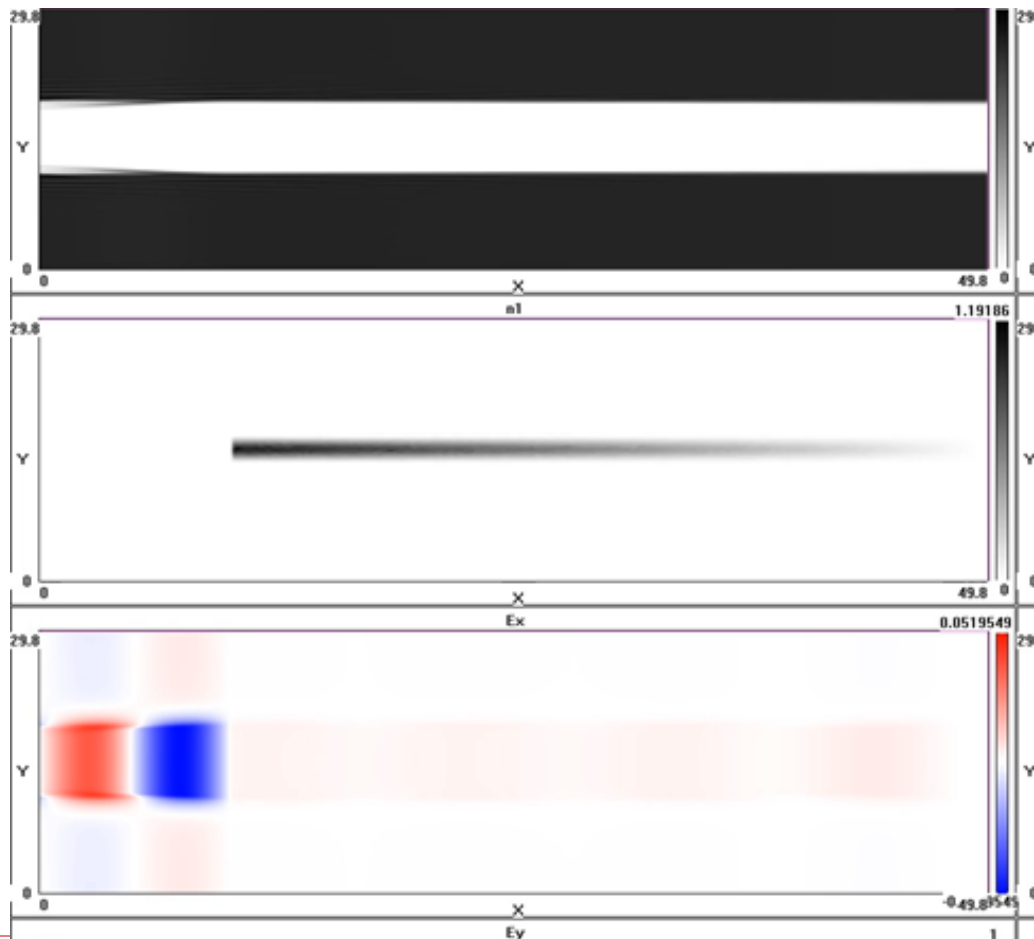
- Full 3D code, Cartesian coords
- High accuracy long term wake field description
- Emittance preserved
- Envelope laser description
- **Ionization included**
- **Betatron radiation and radiation losses included**



Perspective approach: Beam-driven wake in a Hollow Plasma Channel



Ramped bunch in a hollow channel: Potentially high transformer ratio Both for e- and e+

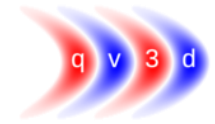


The channel

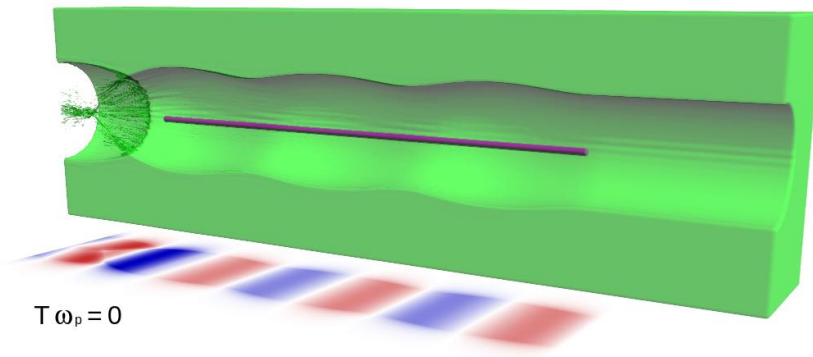
The driver

The wake

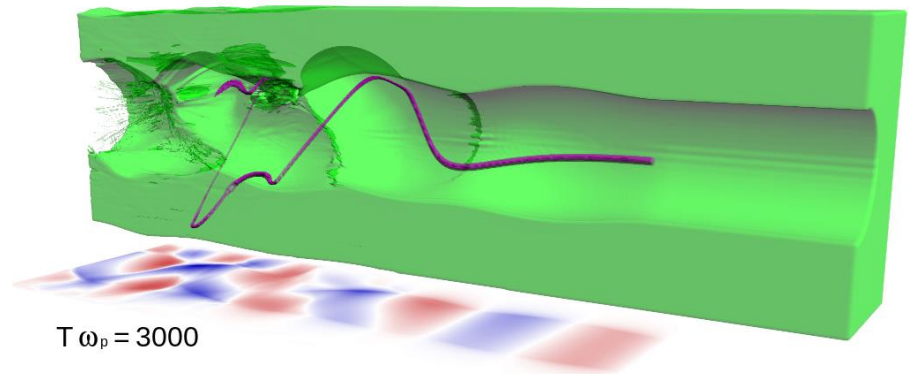
The BBU (hosing) problem

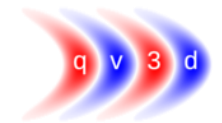
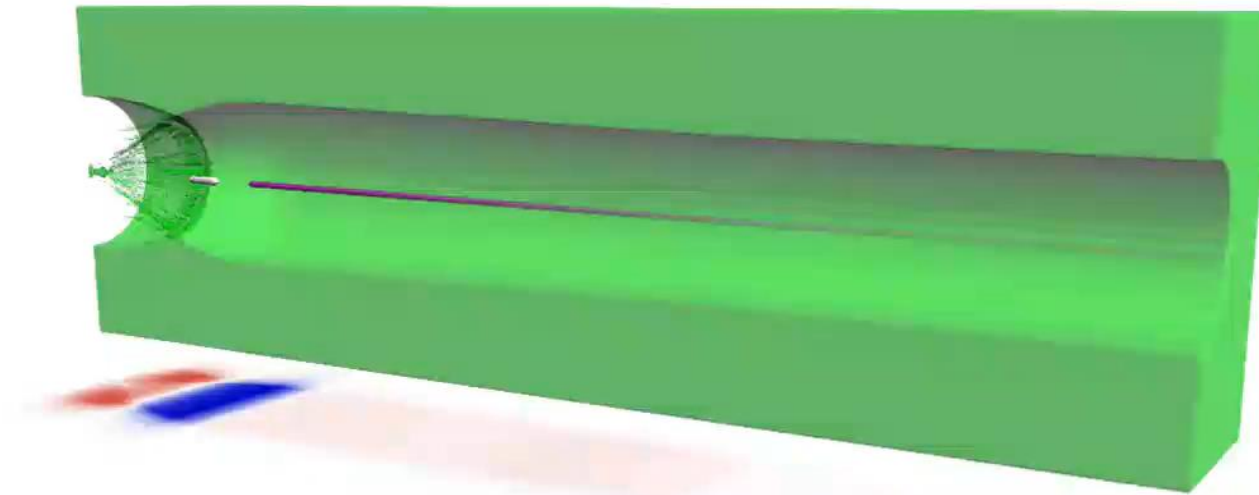


Long driver in a plasma channel...

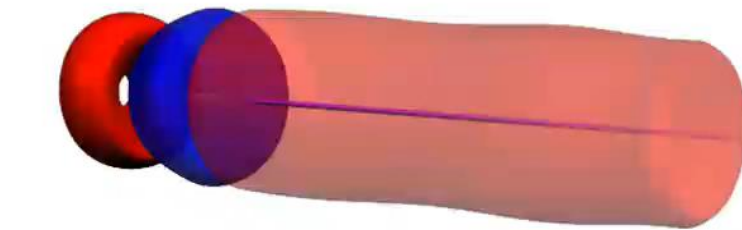


... is unstable



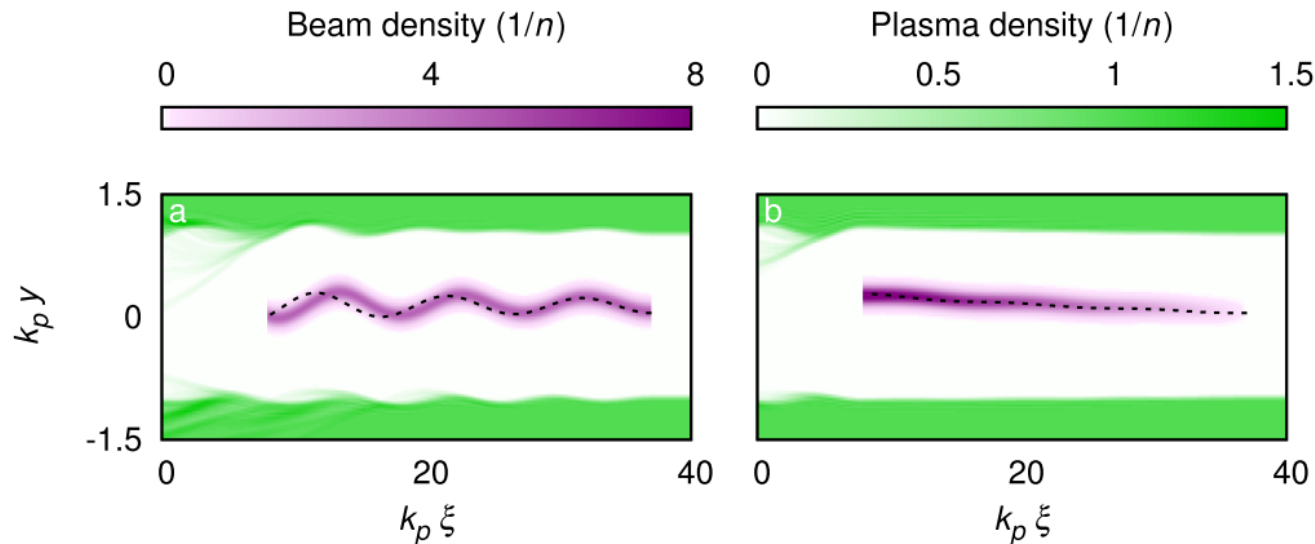


**Hollow
channel:
BBU**
The driver
is lost
before
any useful
acceleration



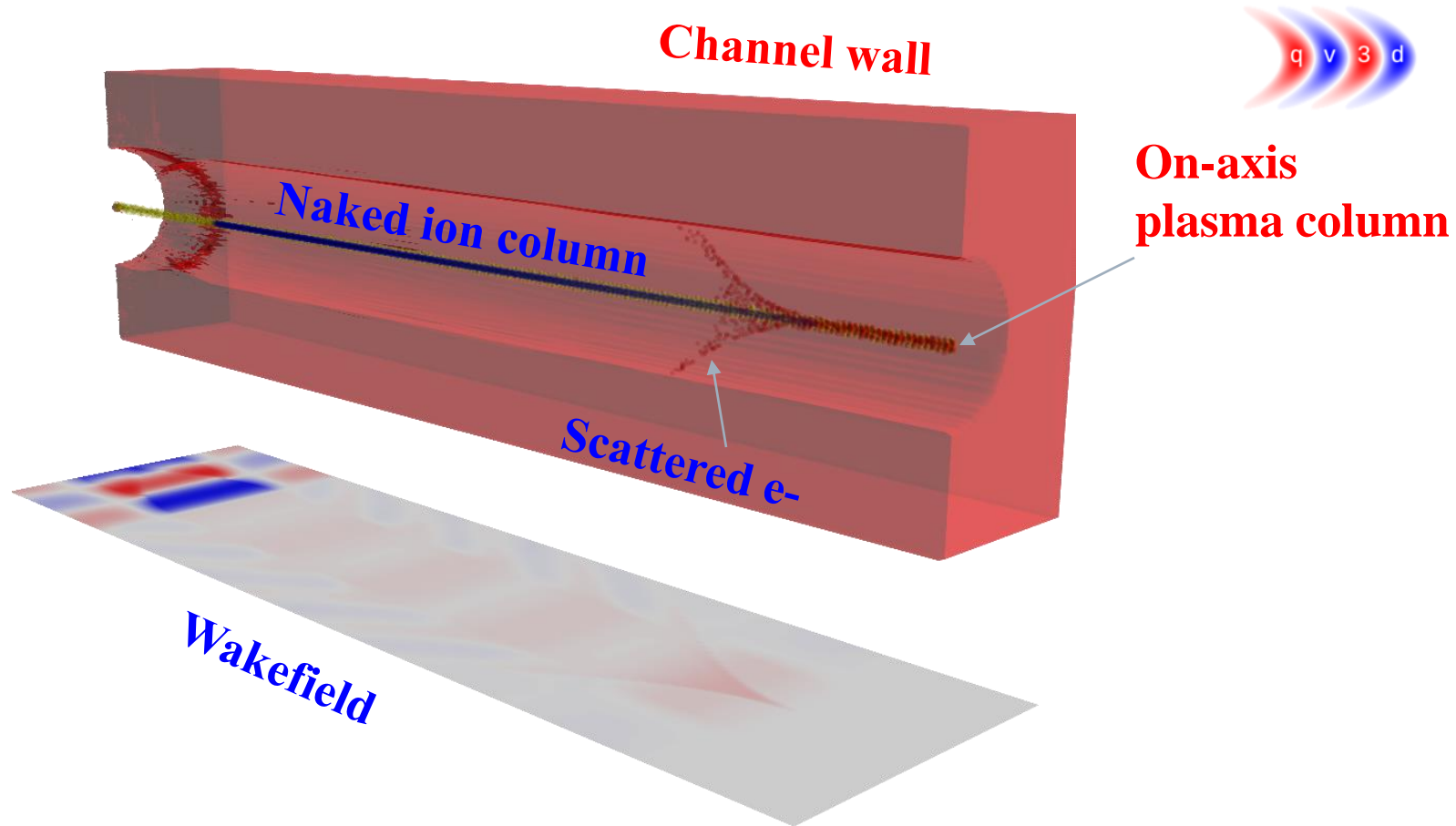
Analytical model from Scroeder *et al.* (1999) for BBU:

$$\begin{aligned}
 & (\partial_z \gamma(z) \partial_z - \gamma(z) k_\beta^2(z)) Y(z, \xi) \\
 &= \int_\xi^\infty \frac{2\kappa_1 c^2}{\omega_1 r_c^2} \frac{I(\xi')}{I_0} \sin(\omega_1 (\xi' - \xi)) Y(z, \xi') d\xi'
 \end{aligned}$$



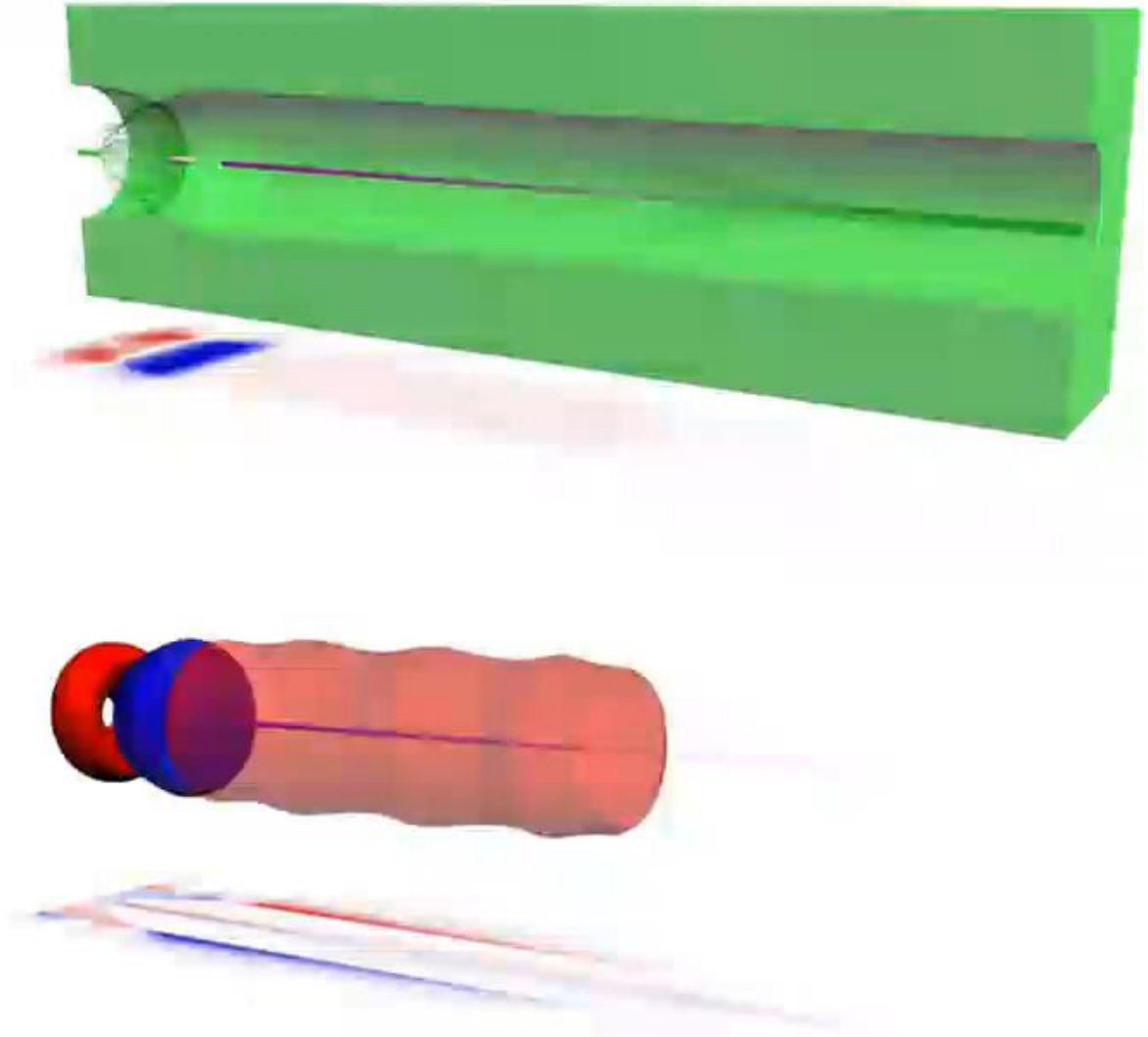
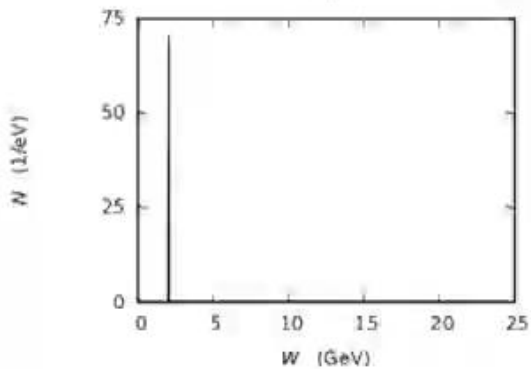
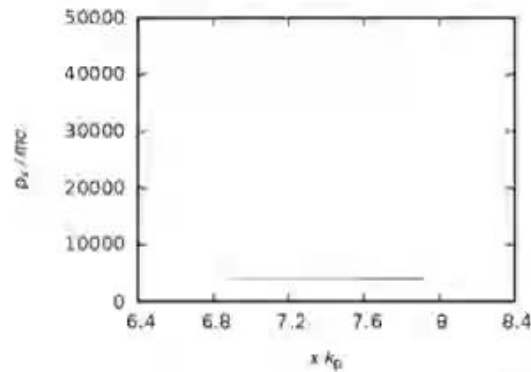
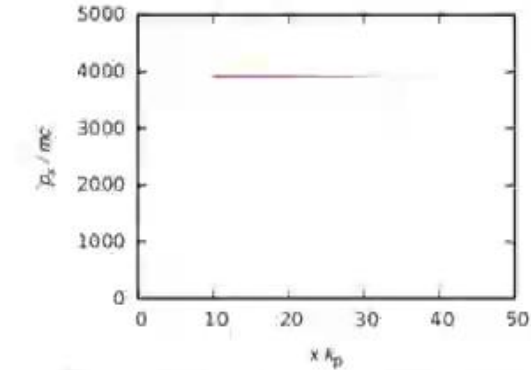
Pukhov and Farmer, PRL (2018)

The stabilization idea: Co-axial plasma channel



Stable acceleration in a co-axial plasma channel

PRL 121, 264801 (2018)



The simulation parameters

- 2 GeV electron bunch driver, 2 GeV witness bunch
- ramped driver current zero to 10 kA over 530 μm
- Plasma density $n=5.7 \times 10^{16}$ 1/cc
- Channel radius $k_p r_c = 3$
- Central filament radius $k_p r_f = 0.2$
- **Witness final energy 21 GeV**
Final energy spread **0.2% r.m.s.**
Final emittance **1.5 μm (what causes it?)**
- Accelerating gradient 2 GV/m
- Loaded transformer ratio is $R=10.5$
- 44% driver-to-witness energy efficiency

The simulation details

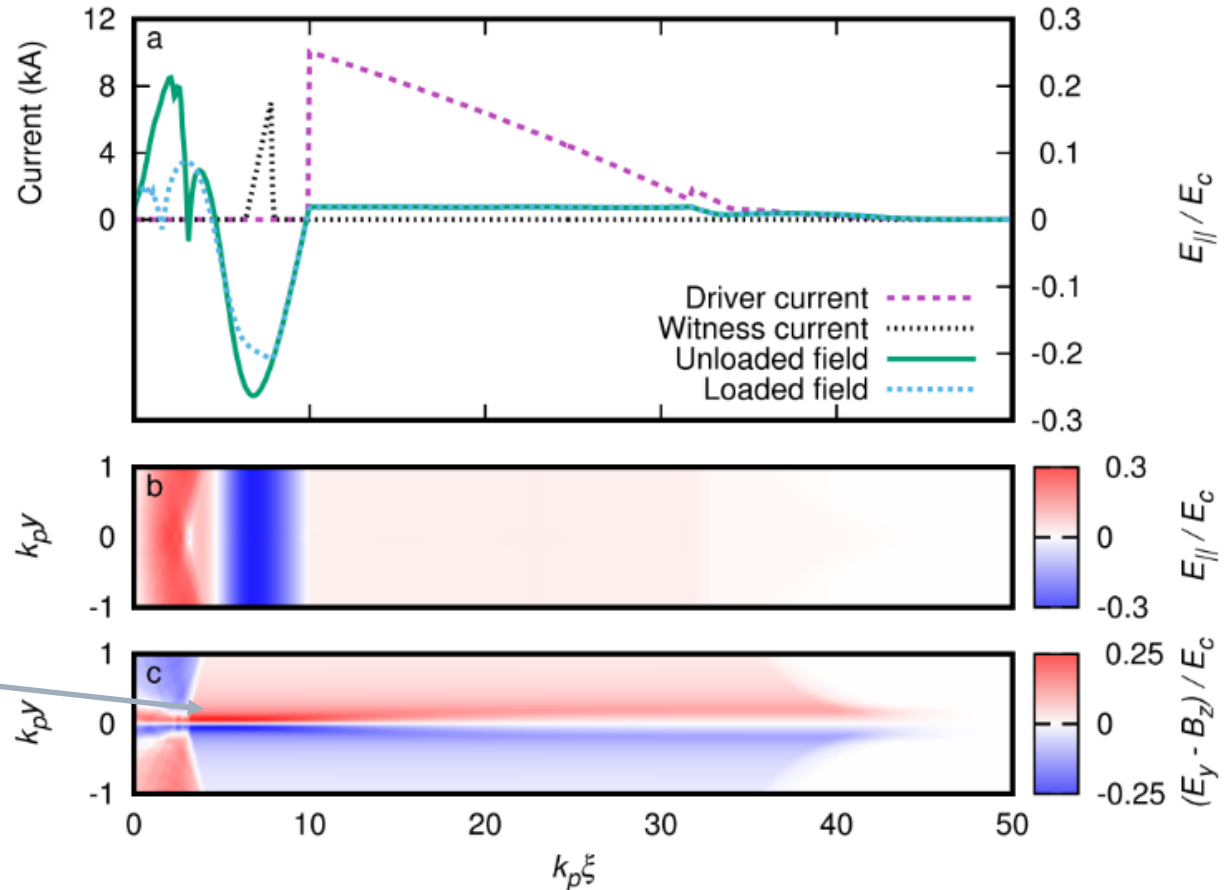
Head-to-tail chirp

in the focusing
strength

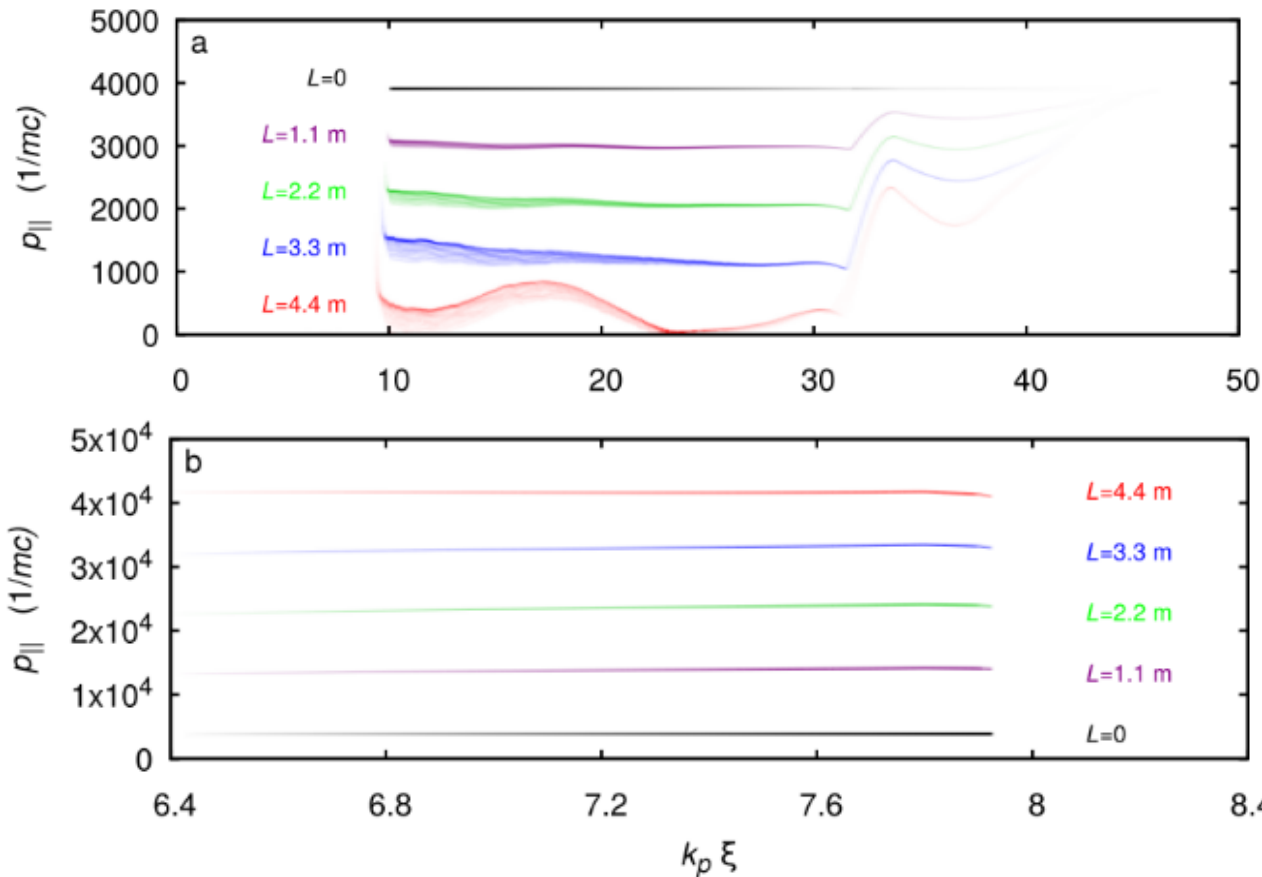
=

**betatron frequency
chirp**

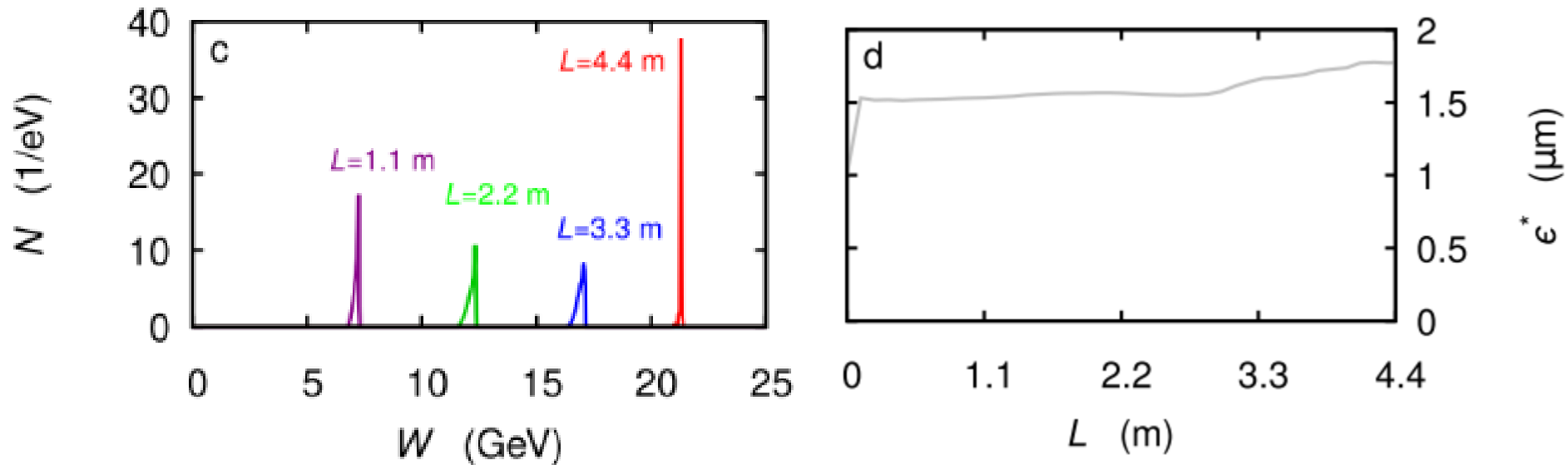
due to the ion motion



The phase space evolution



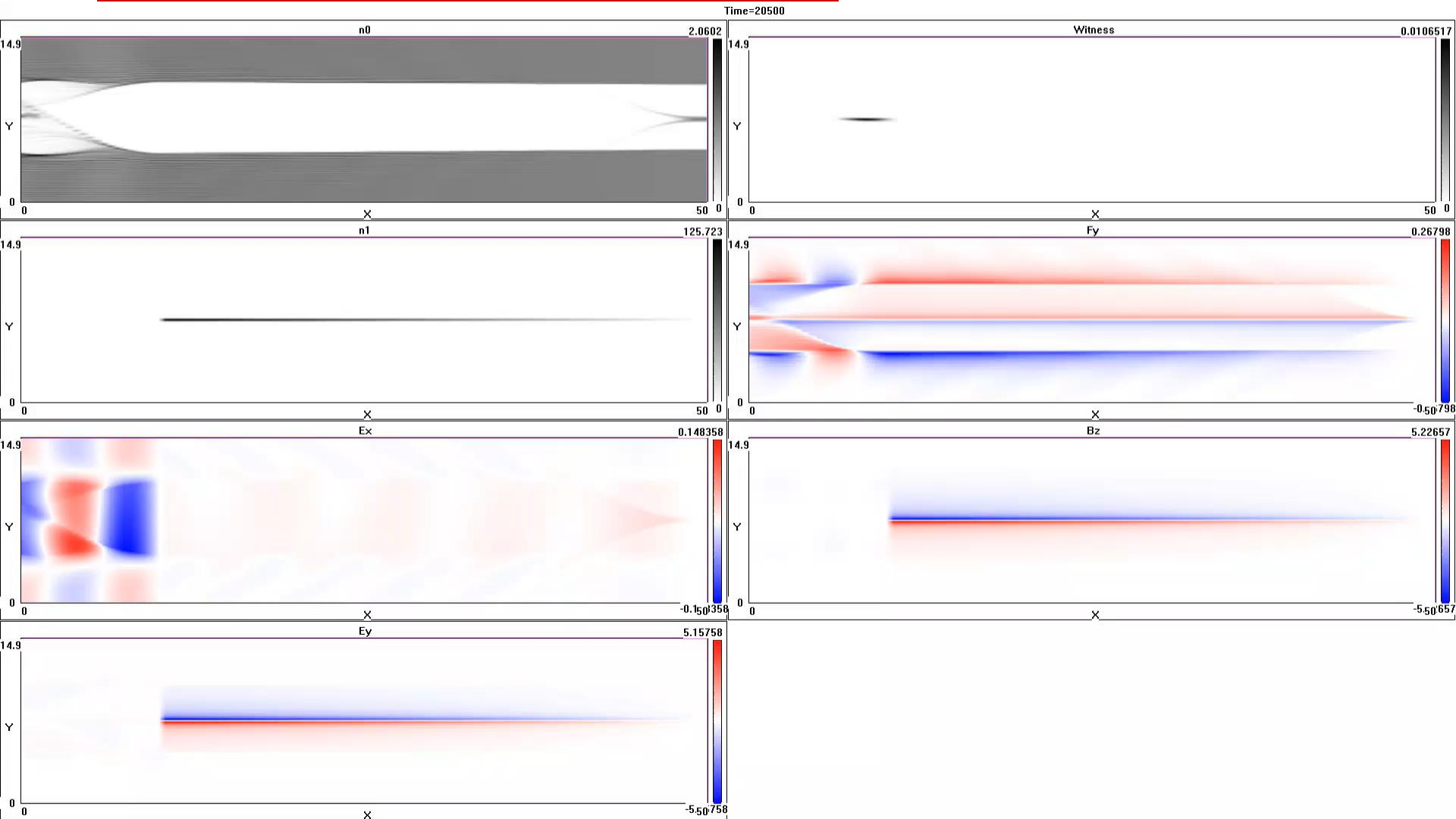
The acceleration quality



Witness energy spectrum and emittance

Stabilization in a co-axial plasma channel

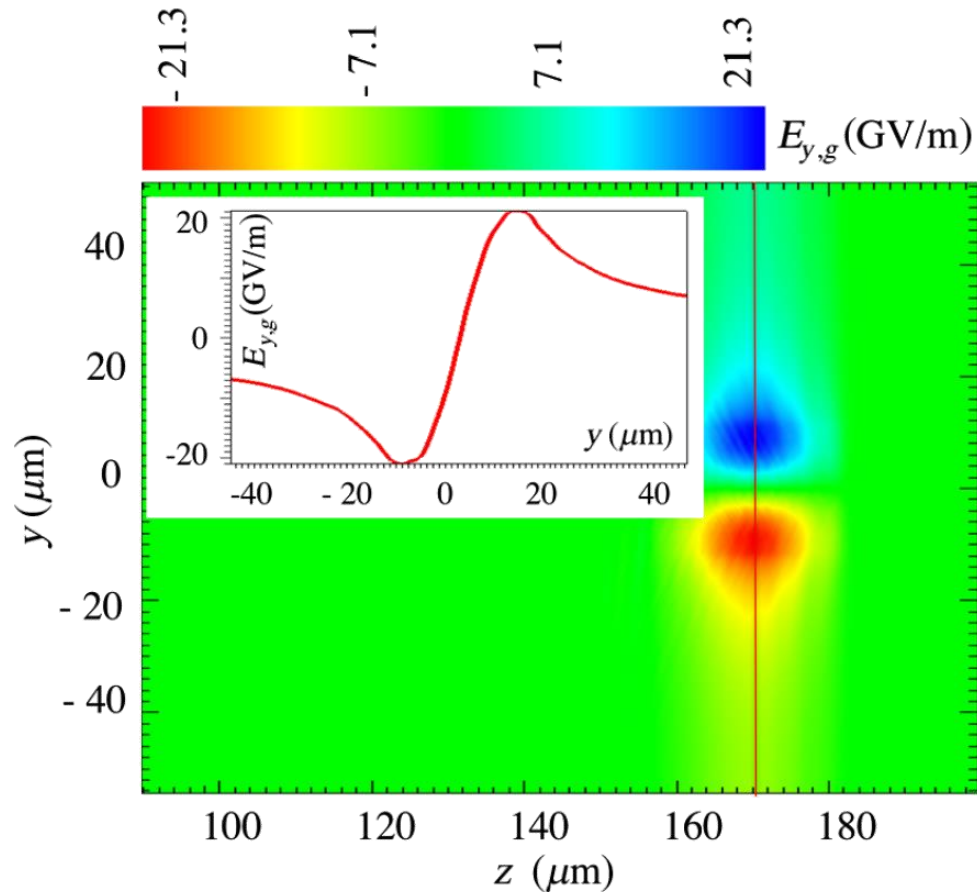
7% off-axis misalignment



Options: how to create the plasma channel with a co-axial filament?

- 3d laser printing of plasma in gas
pointing stability?
laser Rayleigh length is too short
- Gas ionization by a charged particle bunch
the bunch can be externally guided over long distances
high current bunch is required
ultra-short duration to avoid plasma self-action

Transverse bunch field



Bunch parameters required for ionization

Ionizing field

$$E_{\text{crit}} [\text{GV/m}] \sim 0.17(I_p [\text{eV}])^2$$

Bunch field

$$E_{\text{max}} [\text{GV/m}] \sim 30 I_b [\text{kA}]/a[\mu\text{m}]$$

For central plasma filament radius $a=1.5 \mu\text{m}$:

H: $I_b \sim 10 \text{ kA}$, duration 1 fs, charge 10 pC

He: $I_b \sim 40 \text{ kA}$, duration 1 fs, charge 40 pC

Li: $I_b \sim 1 \text{ kA}$, duration 1 fs, charge 1 pC

Assuming plasma density $\sim 1 \times 10^{17} \text{ 1/cm}^3$

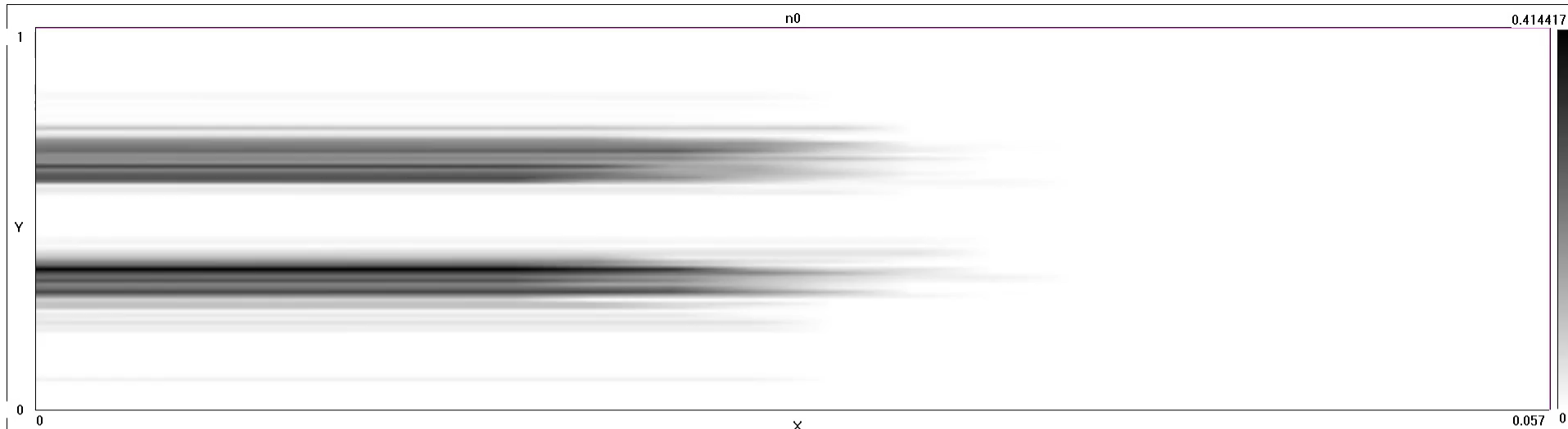
Hollow channel generation in He by charged particle bunchest

$I=40$ kA, $\tau=1$ fs, $\sigma=1.5$ mm, $W=10$ GeV, $B: 0.5$ T/mm

Time=47000

n0

0.414417

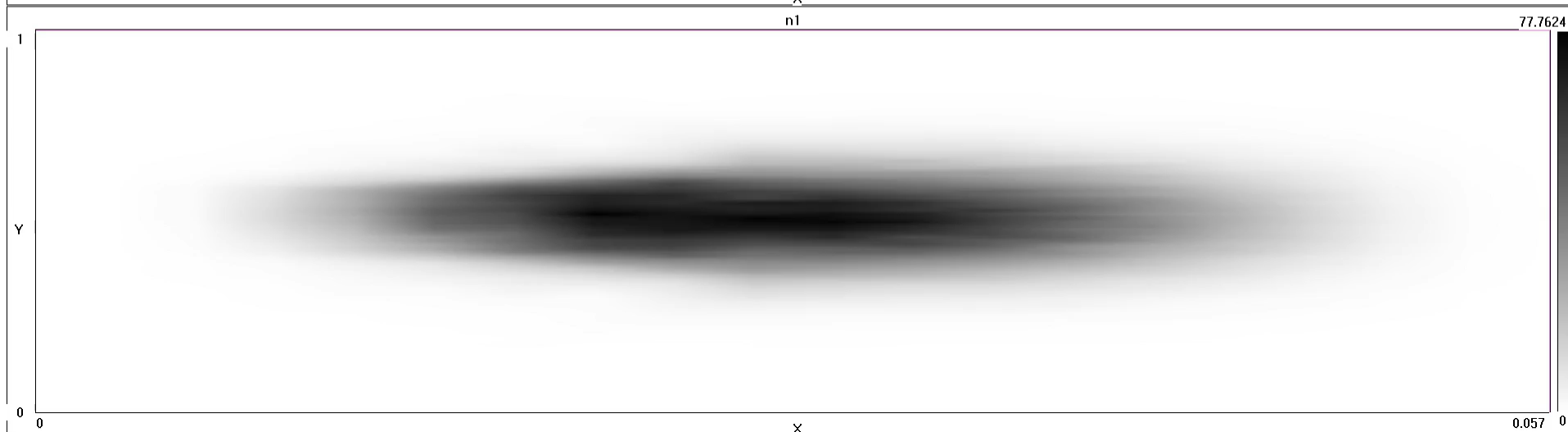


X

0.057 0

n1

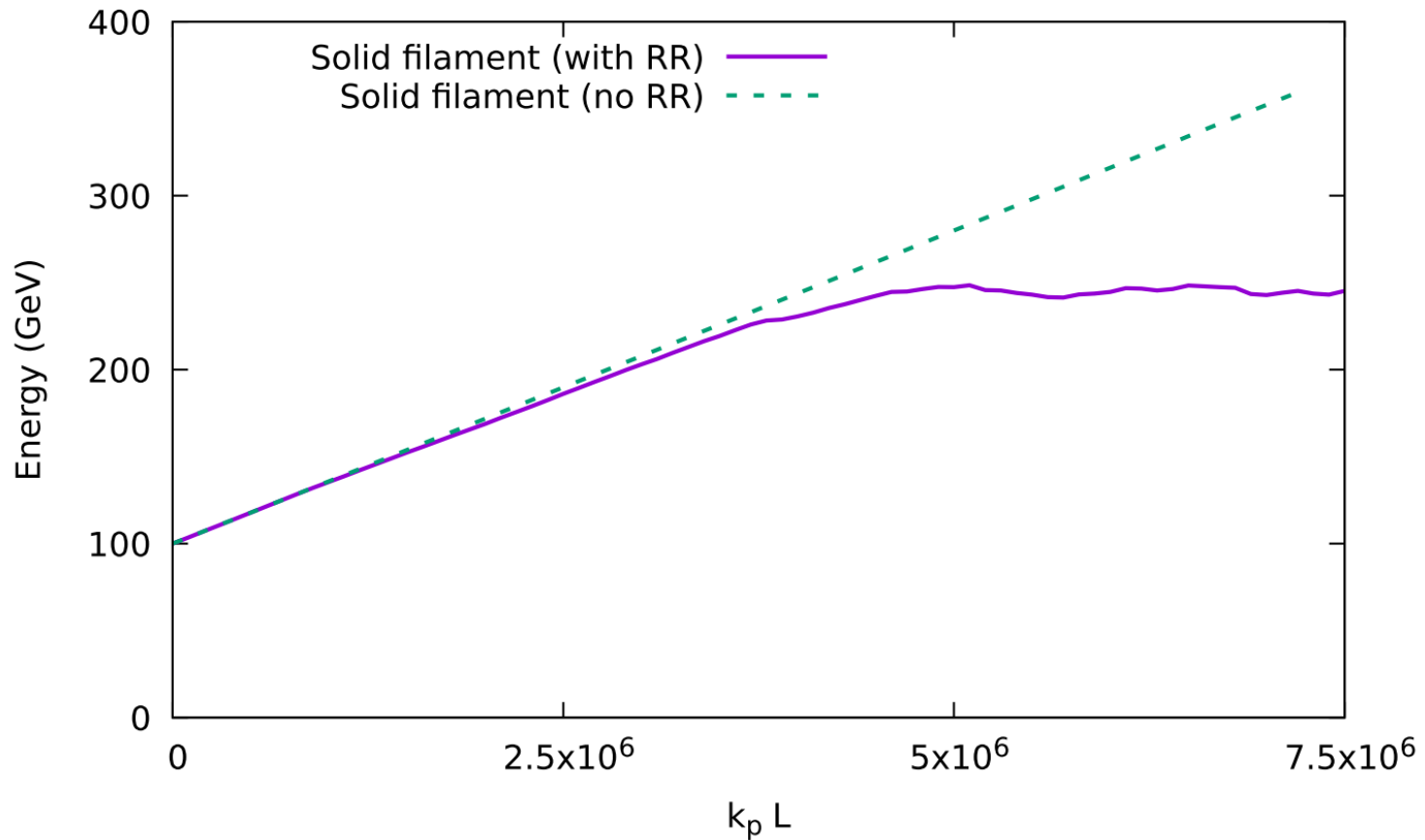
77.7624



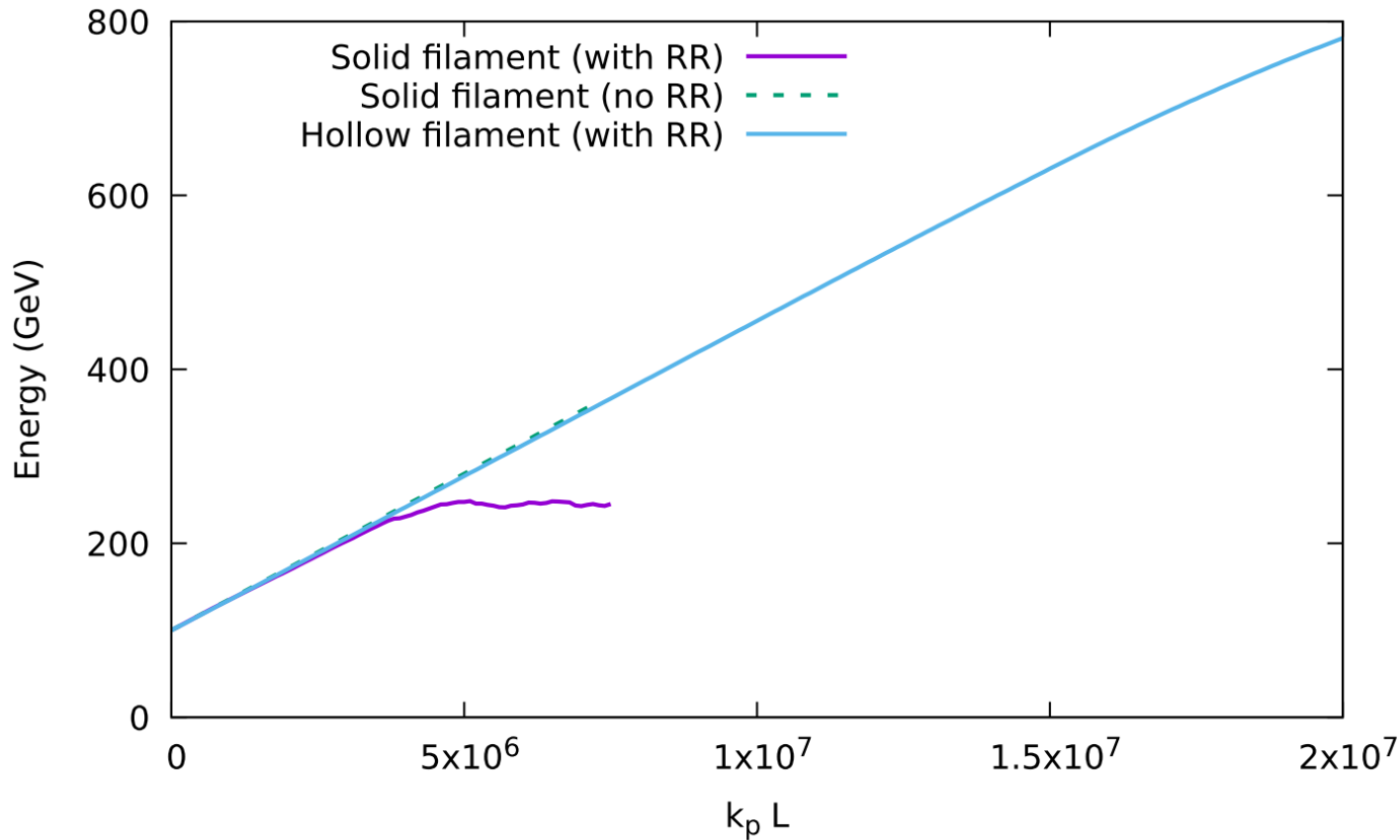
X

0.057 0

Electron acceleration in solid filament



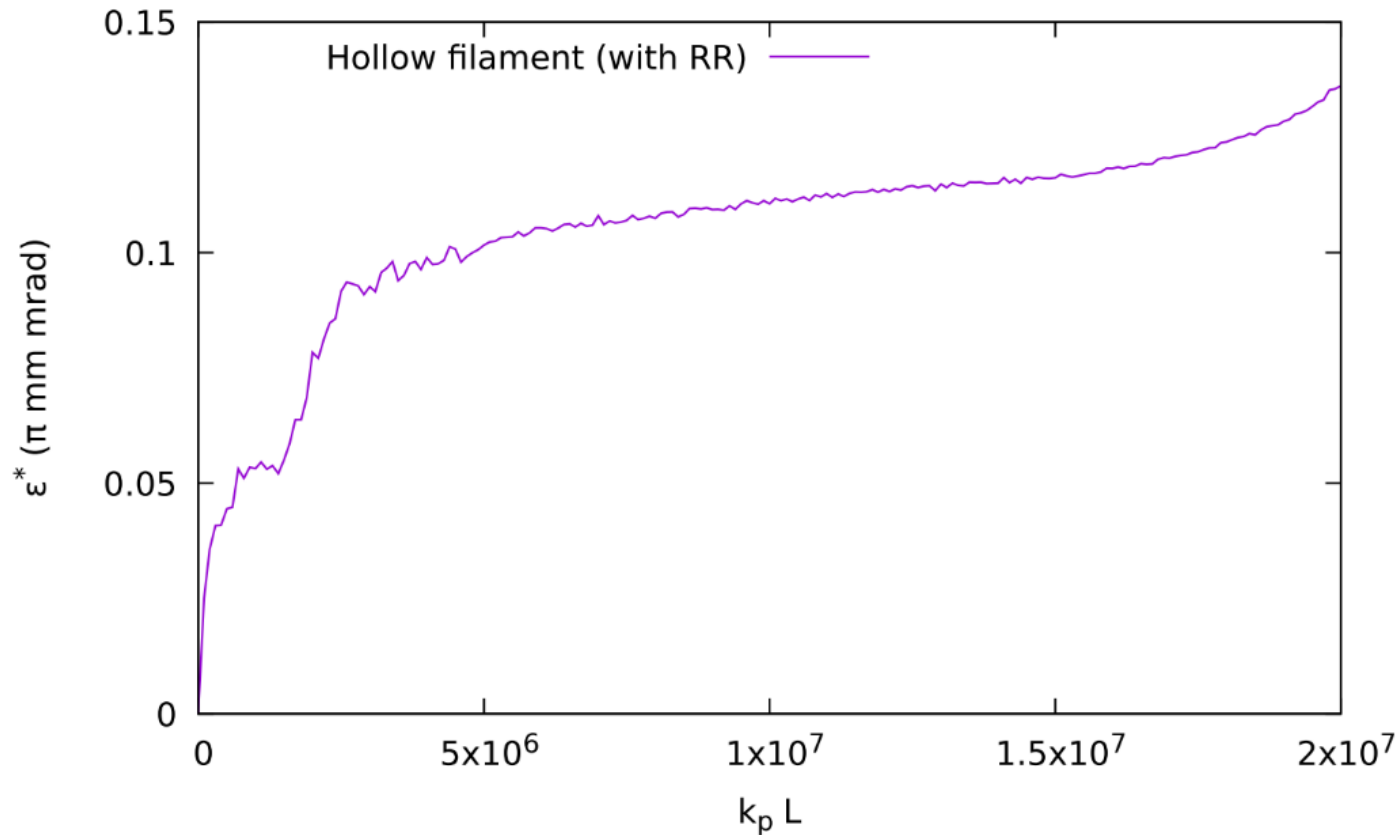
Electron acceleration in hollow filament



The TeV simulation parameters (nothing optimized at all)

- 100 GeV electron bunch driver, 100 GeV witness bunch
- 1.7 nC driver
- ramped driver current zero to 14 kA over 300 μm (1 ps)
- Plasma density $n=1.1 \times 10^{17}$ 1/cc
- Channel radius $k_p r_c = 2$
- Central filament radius $k_p r_f = 0.15$
- **Witness final energy ~ 0.8 TeV**
Final emittance ~ 0.1 μm (unmatched bunches!)

Electron acceleration in solid filament



Outlook

- **Hollow/solid plasma channels can be created by high current ultra-short particle bunches**
- **TeV acceleration in hollow plasma channels with hollow on-axis filaments is feasible**
- **Further studies towards matched bunches, final emittance reduction and positron acceleration are needed**