



**Universität
Zürich**^{UZH}

Theoretical status of the **Flavor Anomalies**

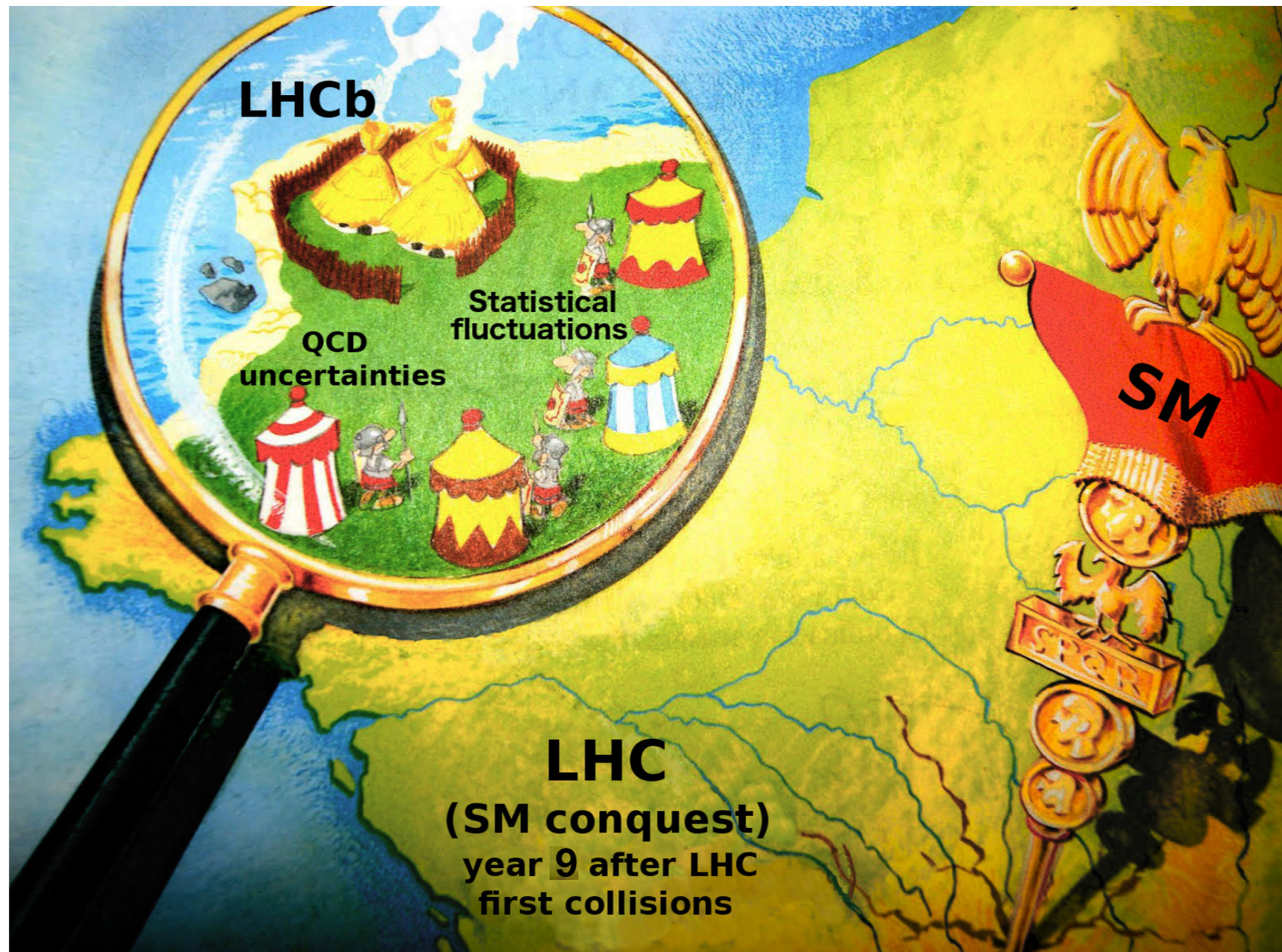
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University of Zurich (UZH)

Based on **arXiv:1712.01368**, **arXiv:1805.09328**, **arXiv:1808.00942**,
and ongoing work

DISCRETE 2018, 6th Symposium on Prospects in the Physics of Discrete Symmetries

The LHC landscape

The year is 9 after the LHC first collisions. Experimental data is entirely SM-like. Well, not entirely! The LHCb Collaboration still holds out against the SM. And life is not easy for the SM there...

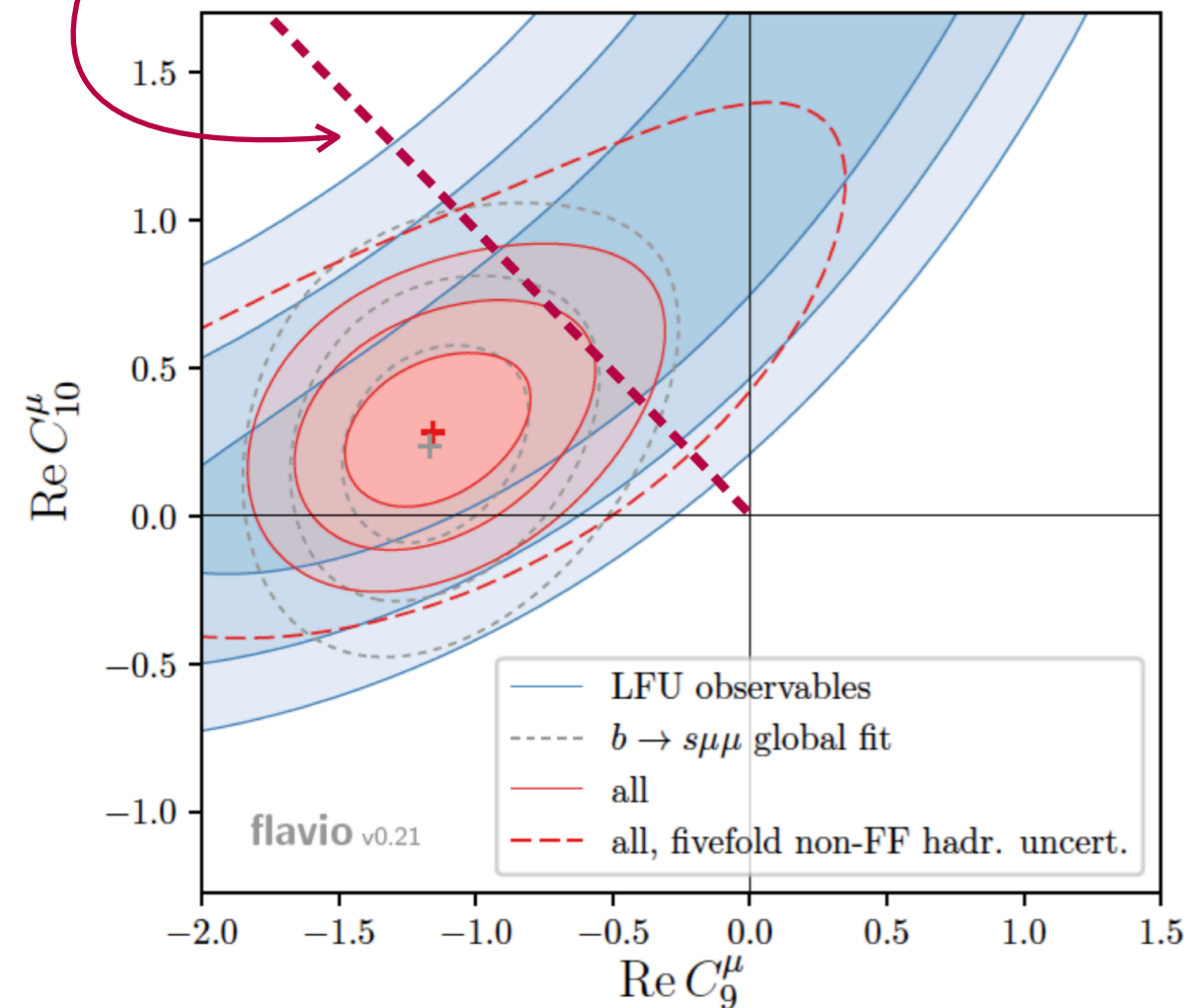


The $b \rightarrow s\ell\ell$ anomalies

See Annarita Buonaura's talk for an experimental insight!

$$\text{Re } C_9^\mu = -\text{Re } C_{10}^\mu \quad (\text{V} - \text{A solution})$$

Altmannshofer, Stangl, Straub '17



$$\mathcal{O}_9^\mu = (\bar{s}\gamma_\alpha P_L b)(\bar{\mu}\gamma^\alpha \mu)$$

$$\mathcal{O}_{10}^\mu = (\bar{s}\gamma_\alpha P_L b)(\bar{\mu}\gamma^\alpha \gamma_5 \mu)$$

Several anomalies observed in $b \rightarrow s\ell\ell$ ($\ell = e, \mu$) transitions [$\sim 5\sigma$ from the SM]

★ Various observables involved [$R_K, R_{K^*}, P'_5, b \rightarrow s\mu\mu$ branching fractions...]

★ “Clean” Lepton Flavor Universality ratios alone give a (combined) 4σ deviation from the SM

$$R(K^{(*)}) = \frac{\mathcal{B}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\mathcal{B}(B \rightarrow K^{(*)}e^+e^-)}$$

★ Results compatible with no NP in electrons (or subleading effects)

★ Left-handed quark helicity largely favored; situation less clear in the lepton sector

★ Mostly driven by LHCb

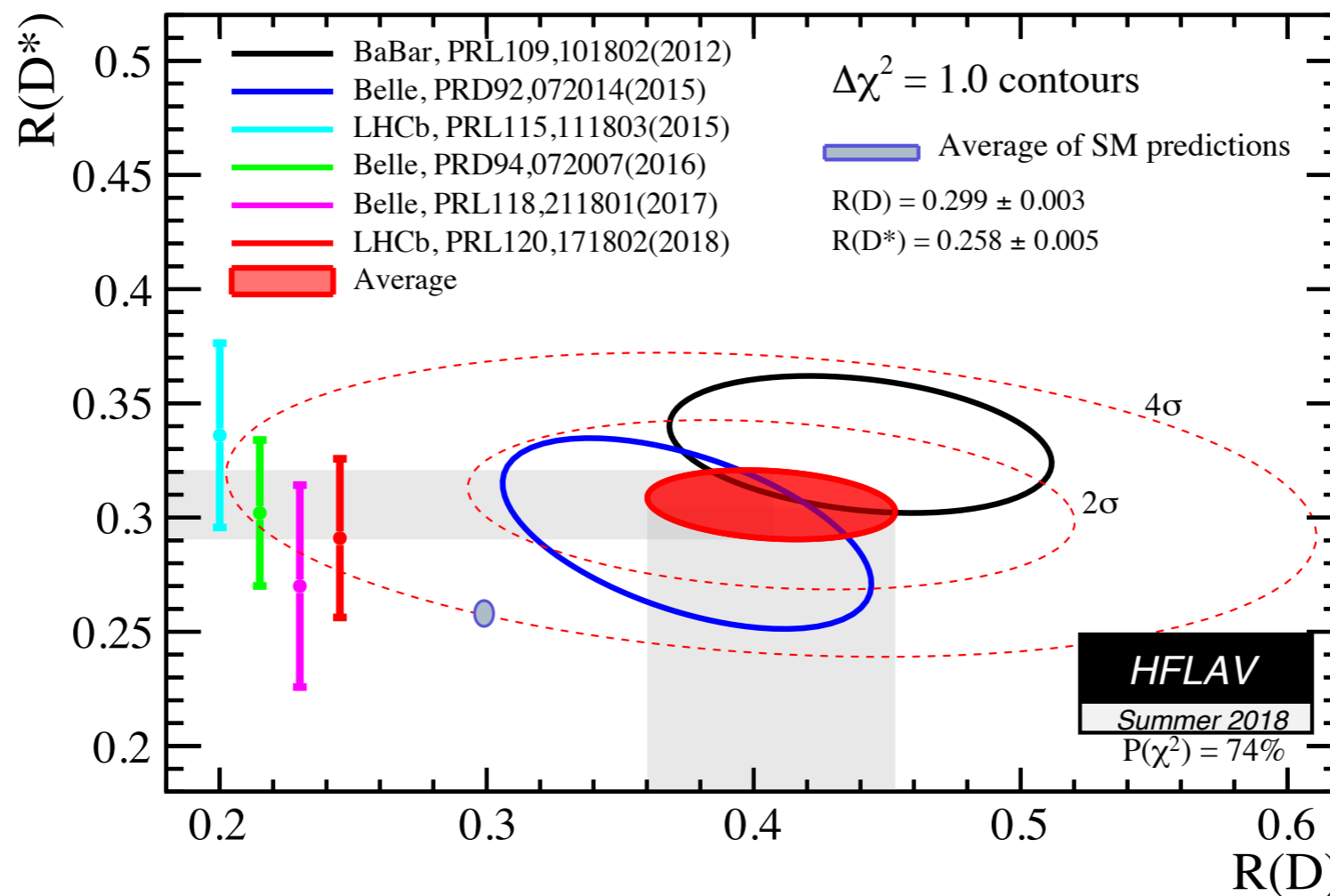
The $R(D^{(*)})$ anomalies

See Annarita Buonaura's talk for an experimental insight!

Experimental measurements disagree by almost 4σ with the SM in $b \rightarrow c\tau\nu$ transitions...

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)}$$

$(\ell = \mu \text{ or } e + \mu)$



Preliminary hints for deviations in $B_c \rightarrow J/\psi\tau\nu$: $R(J/\psi) = 0.71 \pm 0.17 \pm 0.18$

[LHCb Collaboration 1711.05623]

What are the anomalies telling us?

See Paulina Rocha's talk for a model for $b \rightarrow s\ell\ell$ alone

The B anomalies are possibly the **largest coherent set** of deviations from the SM we have ever seen...

... So let us assume that the anomalies (both!) are genuine hints of NP and that they are both connected. Can we conclude something meaningful?

Intriguingly, they follow a very peculiar structure



The only source of **Lepton Flavor Universality Violation** in the SM (Yukawas) follow a similar trend: $y_e \ll y_\mu \ll y_\tau \dots$. Are the anomalies related to them?

What are the anomalies telling us?

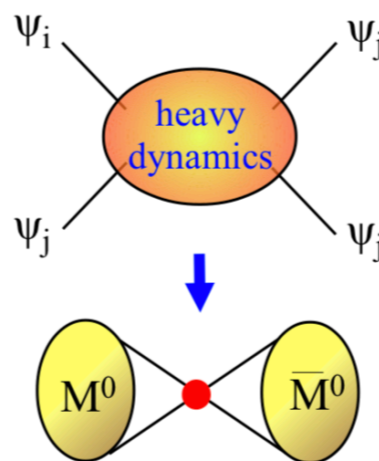
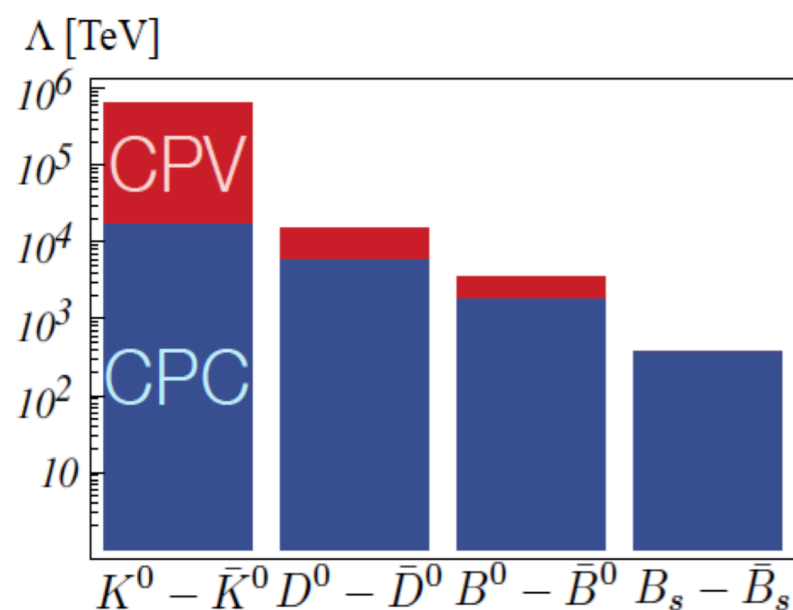
A combined explanation calls for NP: (*)

★ Coupled dominantly to the **3rd generation**

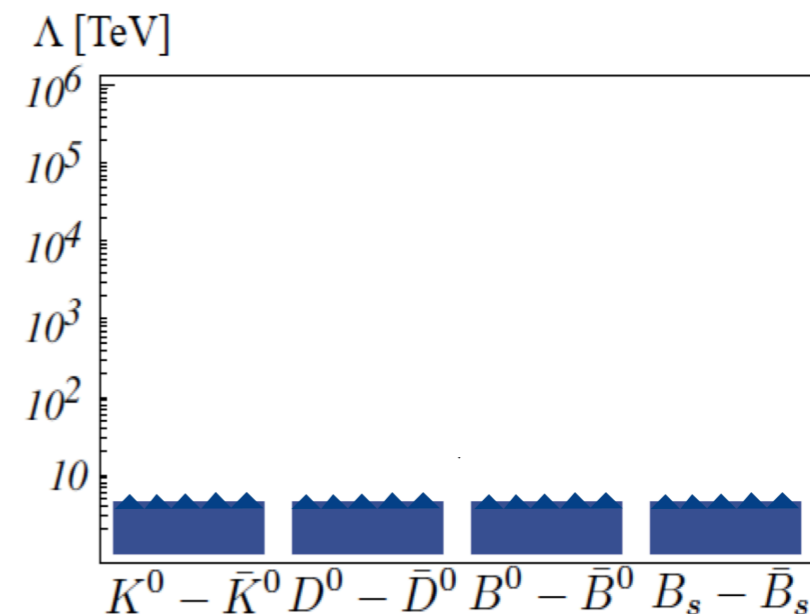
★ $\Lambda_{\text{NP}} \sim \mathcal{O}(1 \text{ TeV})$

(*) N.B.: conclusions driven (mostly) by $R(D^{(*)})$

Anarchical couplings



Hierarchical couplings



Severe constraints on generic new (BSM) flavor breaking sources
(mis)interpreted as indication of a high flavor scale

U(2) flavor symmetry as a guiding principle

The SM Yukawas respect an approximate U(2) symmetry

[Barbieri et al. 1105.2296]

$$M_{u,d} \sim \begin{array}{|c|c|} \hline \text{light} & \text{light} \\ \hline \text{light} & \text{heavy} \\ \hline \text{light} & \text{heavy} \\ \hline \end{array}$$

$$V_{\text{CKM}} \sim \begin{array}{|c|c|c|} \hline \text{heavy} & \text{light} & \text{light} \\ \hline \text{light} & \text{heavy} & \text{light} \\ \hline \text{light} & \text{light} & \text{heavy} \\ \hline \end{array}$$

$$U(2)_q \times U(2)_u \times U(2)_d$$

$$\psi = (\psi_1 \ \psi_2 \ \psi_3)$$

$$Y_{u,d} = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$$

Unbroken symmetry

$$\begin{pmatrix} 0 & V \\ 0 & 1 \end{pmatrix}$$

Leading breaking

$$\begin{pmatrix} \Delta & V \\ 0 & 1 \end{pmatrix}$$

Final breaking

$$\begin{aligned} |V| &\sim |V_{ts}| \\ |\Delta| &\sim y_c \end{aligned}$$

- ✓ Assuming a single leading breaking ensures an effective protection of FCNCs
[SM-like mixing among light & 3rd generations \longrightarrow consistent with CKM fits]
- ✓ Large NP effects in 3rd generation, light-generation effects controlled by the breaking
- Compatibility between high- p_T data and $R(D^{(*)})$ require largish 32 couplings

The general approach

We can follow three theoretical approaches to describe the anomalies:

I. EFT

Starting point

[test of low energy observables & flavor symmetries]

II. Simplified models

Essential to test high-pT observables

III. UV complete models

Essential to test the consistency of the solution

[new correlations among observables, particles...]

Each step is important and complementary to each other

[**any serious theoretical attempt follows epicycles around the three...**]

EFT-type considerations

The $SU(2)_L$ triplet operator is a natural starting point for explaining $R(D^{(*)}) + b \rightarrow s\ell\ell$

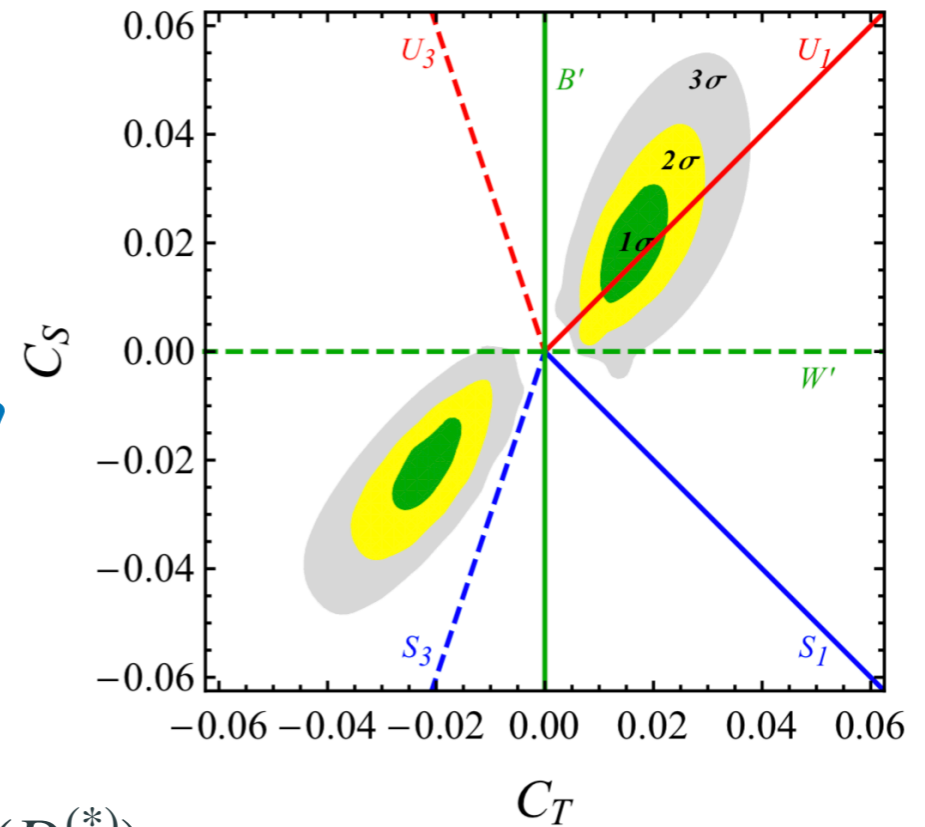
$$-\frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell C_T (\bar{q}_L^i \gamma^\mu \tau^a b_L) (\ell_L^\alpha \gamma_\mu \tau^a \ell_L^\beta) \supset \frac{1}{\Lambda_{R_D^{(*)}}^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\tau}_L \gamma_\mu \nu_L) + \frac{1}{\Lambda_{R_K^{(*)}}^2} (\bar{s}_L \gamma_\mu b_L) (\bar{\mu}_L \gamma^\mu \mu_L)$$

... but other operators are also needed or useful

★ Singlet operator necessary to avoid too large $b \rightarrow s\nu\nu$

$$-\frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell [C_T (\bar{q}_L^i \gamma^\mu \tau^a b_L) (\ell_L^\alpha \gamma_\mu \tau^a \ell_L^\beta) + C_S (\bar{q}_L^i \gamma^\mu b_L) (\ell_L^\alpha \gamma_\mu \ell_L^\beta)]$$

$$\supset \frac{1}{\Lambda_{R_D^{(*)}}^2} (C_T - C_S) (\bar{s}_L \gamma^\mu b_L) (\bar{\nu}_L \gamma_\mu \nu_L)$$



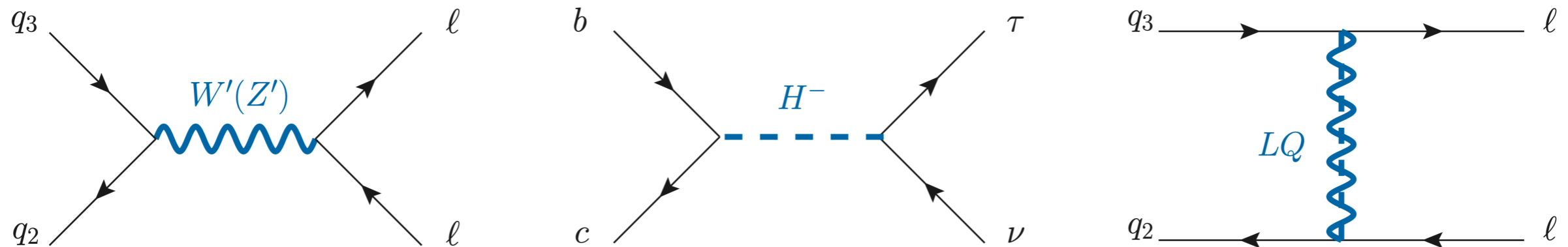
★ Right-handed, scalar and/or tensor operators helpful for $R(D^{(*)})$

[Buttazzo et al. 1706.07808]

Solutions based on an **approximate $U(2)$ flavor symmetry** are viable

Simplified models, which mediator?

Only few possibilities are available to “UV-complete” the EFT...



Long story short...

- ★ **Charged Higgs** solutions are excluded by measurements of τ_{B_c}
[Contributions to $\mathcal{B}(B_c \rightarrow \tau\nu)$ are **scalar enhanced and huge**] [Alonso et al. 1611.06676]
- ★ **Minimal W'/Z' models** in **large tension with high- p_T data** [Faroughy et al. 1609.07138]
 W' + light ν_R in better shape but still in tension with $pp \rightarrow \tau\nu$
[Greljo et al. 1811.07920]
- ★ **Scalars** and **vector leptoquarks** are the **best candidates so far**

Simplified dynamical models: the main suspects

Faroughi @ CKM18

	Model	$R_{K(*)}$	$R_{D(*)}$	$R_{K(*)}$ & $R_{D(*)}$
Scalars	$S_1 = (\mathbf{3}, \mathbf{1})_{-1/3}$	✗	✓	✗
	$R_2 = (\mathbf{3}, \mathbf{2})_{7/6}$	✗	✓	✗
	$\tilde{R}_2 = (\mathbf{3}, \mathbf{2})_{1/6}$	✗	✗	✗
	$S_3 = (\mathbf{3}, \mathbf{3})_{-1/3}$	✓	✗	✗
Vector	$U_1 = (\mathbf{3}, \mathbf{1})_{2/3}$	✓	✓	✓
	$U_3 = (\mathbf{3}, \mathbf{3})_{2/3}$	✓	✗	✗

Angelescu, Becirevic, DAF, Sumensari [1808.08179]

Three viable options in the market^(*):

★ $U_1 + \text{UV completion}$

[di Luzio, Greljo, Nardecchia 1708.08450;
Calibbi, Crivellin, Li 1709.00692;
Bordone, Cornella, JF, Isidori 1712.01368;
Barbieri, Tesi, 1712.06844...]

★ $S_1 + S_3$

[Crivellin, Muller, Ota 1703.09226;
Buttazzo et al. 1706.07808;
Marzocca 1803.10972]

★ $S_3 + R_2$

[Bečirević et al., 1806.05689]

(*) Assuming no light ν_R

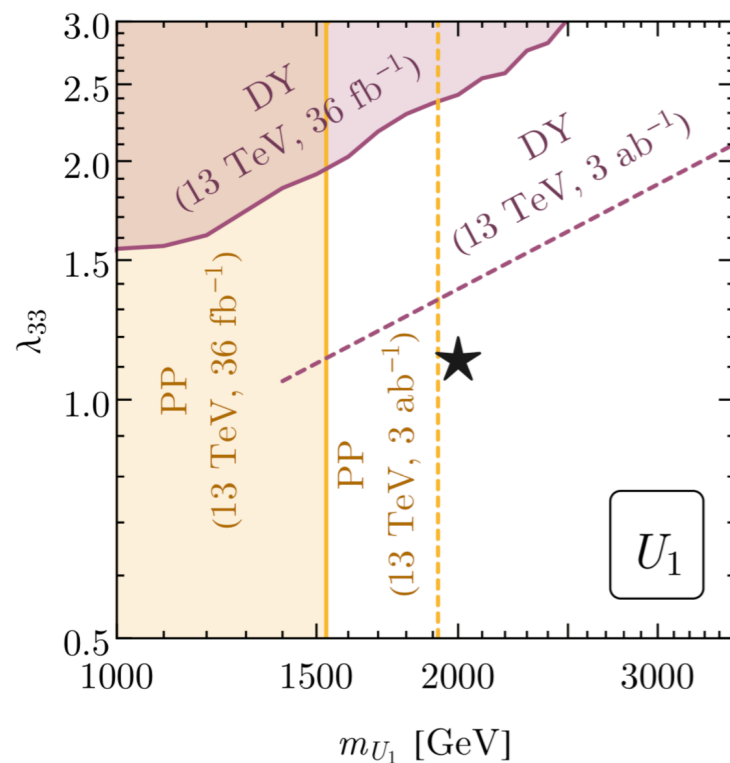
Only one single-mediator possibility... that needs to be UV completed
[two scalar leptoquarks can also do the job...]

The U_1 leptoquark: the pure LH case

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[\beta_{i\alpha}^L (\bar{q}_{L}^i \gamma_\mu \ell_L^\alpha) + \beta_{i\alpha}^R (\bar{d}_{R}^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.}$$

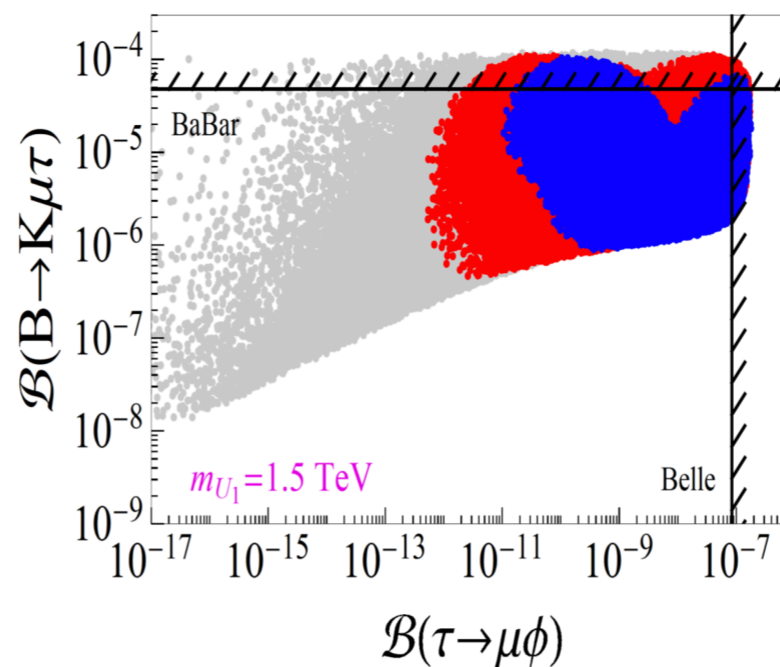
Pure LH U_1 (i.e. $\beta_{i\alpha}^R = 0$) extensively analyzed in the literature...

Safe from high-pT



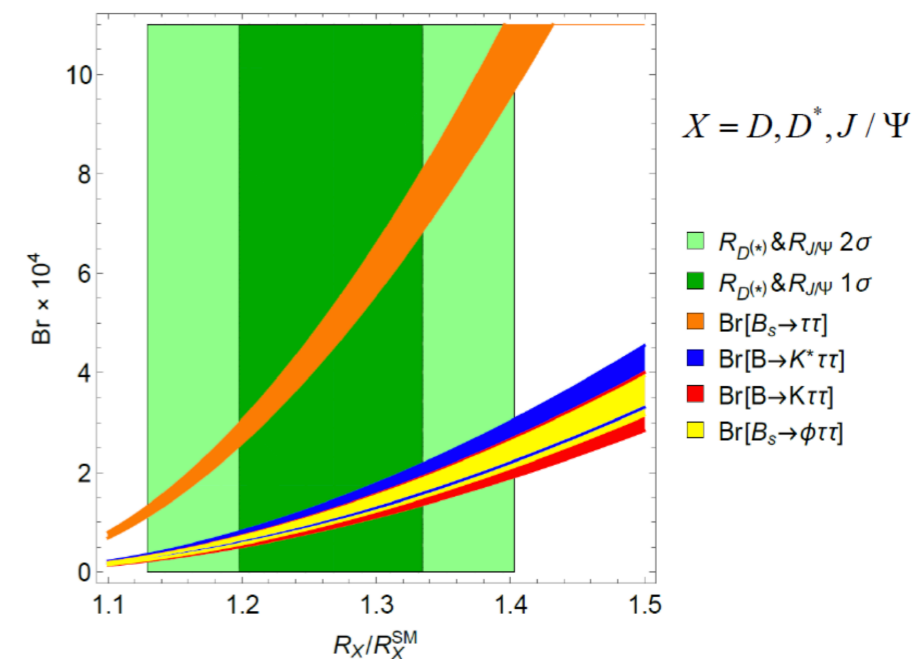
[Schmaltz, Zhong, 1810.10017]
(see also 1808.08179, 1609.07138)

LFV around the corner



[Angelescu et al., 1808.08179]

Huge effects in $b \rightarrow s \tau \tau$



[Capdevila et al., 1712.01919]

The U_1 leptoquark: all in

$$\mathcal{L} \supset \frac{g_U}{\sqrt{2}} U_1^\mu \left[\beta_{i\alpha}^L (\bar{q}_L^i \gamma_\mu \ell_L^\alpha) + \beta_{i\alpha}^R (\bar{d}_R^i \gamma_\mu e_R^\alpha) \right] + \text{h.c.}$$

Pure LH U_1 (i.e. $\beta_{i\alpha}^R = 0$) extensively analyzed in the literature...

... RH U_1 coupling usually ignored. Important pheno implications!

Flavor assumptions:

$$\beta^L = \begin{bmatrix} 0 & 0 & \beta_{d\tau}^L \\ 0 & \beta_{s\mu}^L & \beta_{s\tau}^L \\ 0 & \beta_{b\mu}^L & \beta_{b\tau}^L \end{bmatrix}$$

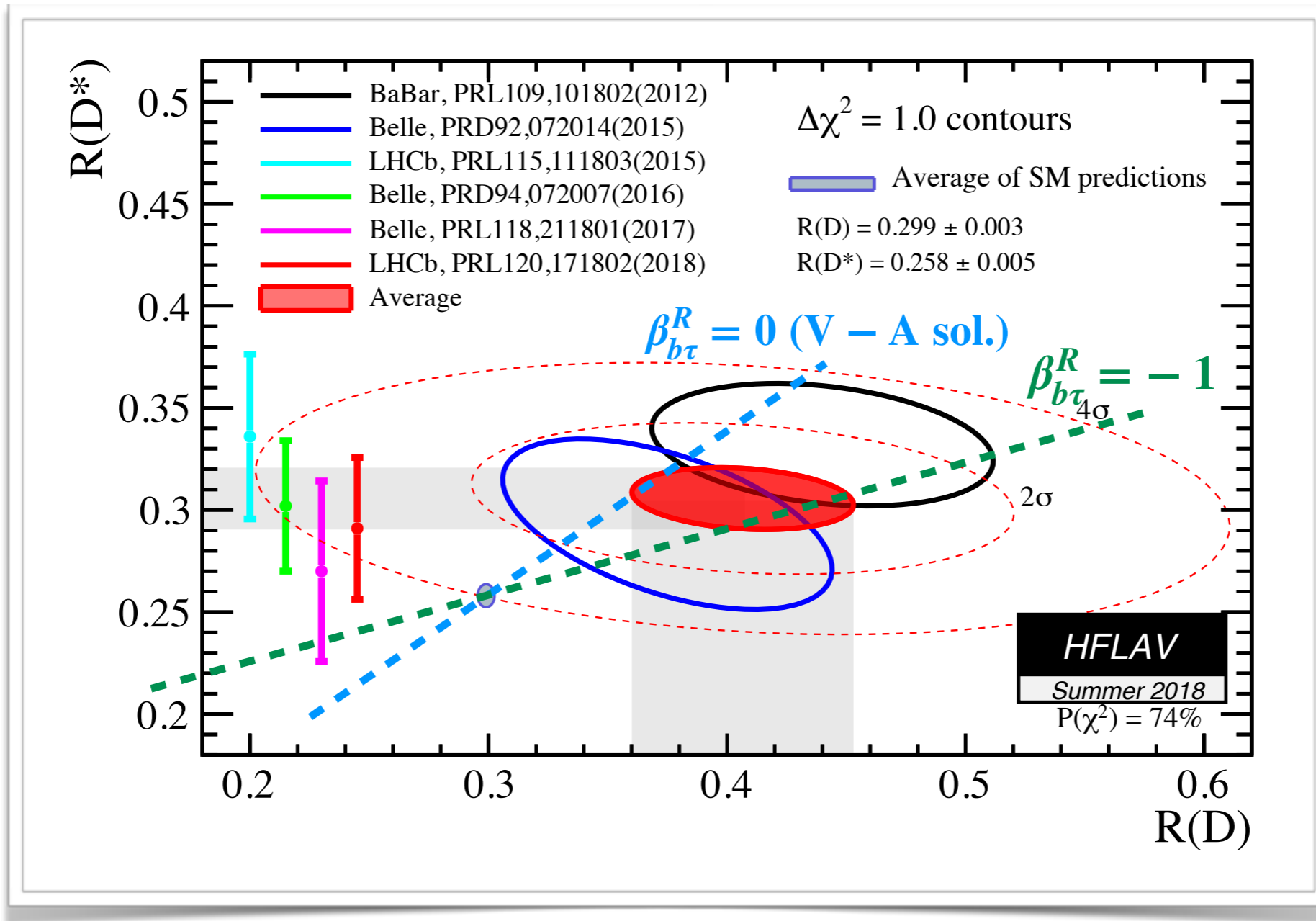
$$\beta^R = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \beta_{b\tau}^R \end{bmatrix}$$

$$C_{V_L} = (\bar{c}_L \gamma_\mu b_L) (\bar{\ell}_L \gamma^\mu \nu_L)$$

$$C_{S_R} = (\bar{c}_L b_R) (\bar{\ell}_R \nu_L)$$

(RGE enhanced)

The U_1 leptoquark: $R(D^{(*)})$ projections



Differential distributions, polarizations,... could also be different from the SM
 [Essential to test at future facilities like Belle II]

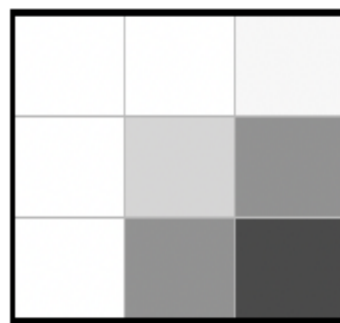
Low energy implications of the U_1 leptoquark

$$\Delta R_K, \Delta R_{K^*}$$

$$B_s \rightarrow \mu\mu$$

chiral-enhanced scalar contribution if $\beta_{b\mu}^R \neq 0$

$$\beta^L = \begin{bmatrix} 0 & 0 & \beta_{d\tau} \\ 0 & \beta_{s\mu} & \beta_{s\tau} \\ 0 & \beta_{b\mu} & \beta_{b\tau} \end{bmatrix}$$



$$\beta^R = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$\Delta R_{D^{(*)}}$ • scalar contr. RGE enhanced
• non universal (~~V-A~~*~~V-A~~)

$B_s \rightarrow \tau\tau$ chiral enhanced
→ close to exp. limit

$B \rightarrow \tau\nu$ chiral enhanced
[alleviated by $\beta_{d\tau}$]

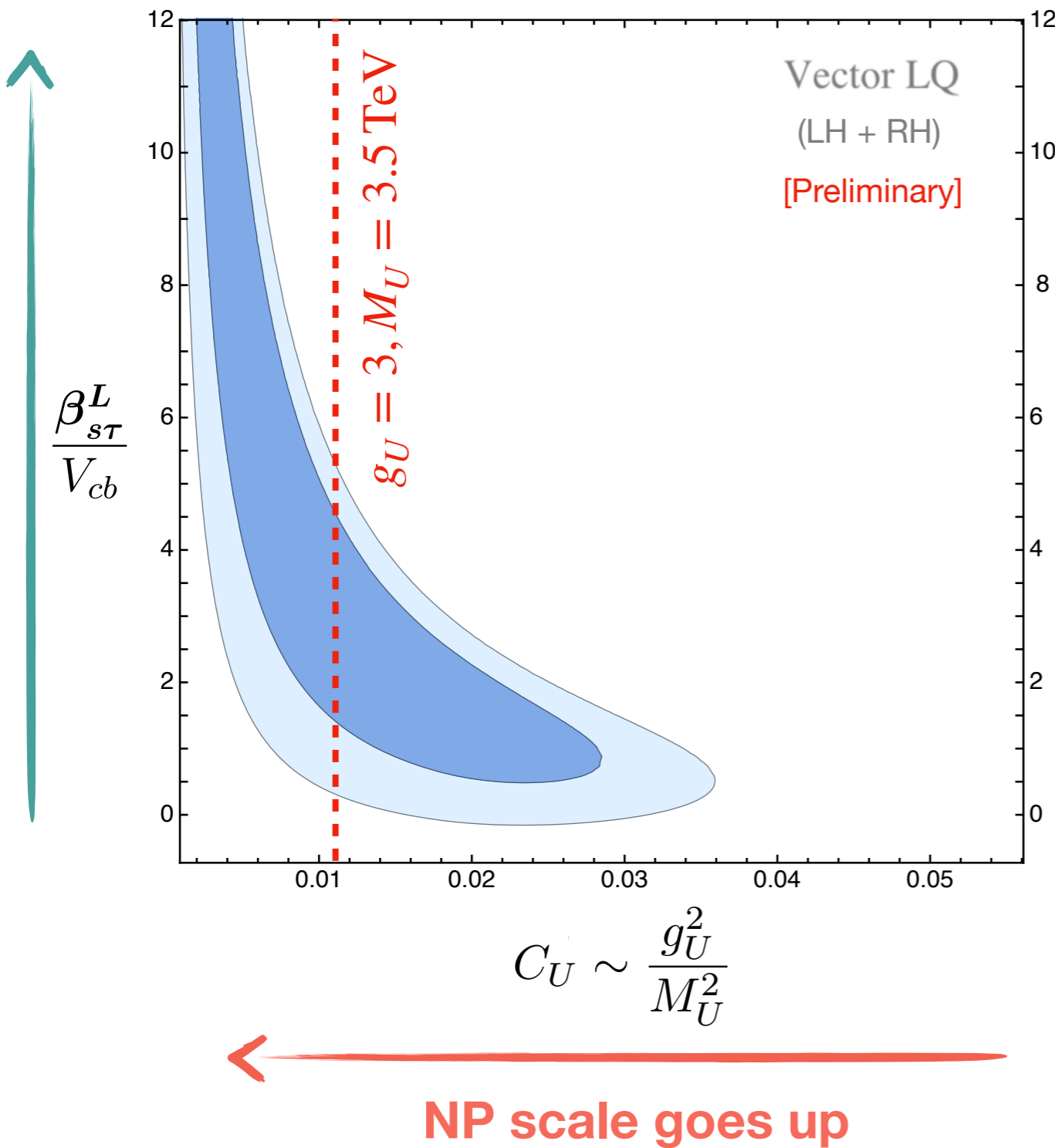
LFV in $\tau \rightarrow \mu$ transitions

$$\tau \rightarrow \mu\phi \quad \tau \rightarrow \mu\gamma$$

$$B \rightarrow K^* \tau^+ \mu^-$$

$B_s \rightarrow \tau^+ \mu^-$ Chiral enhanced
[**soon new result**
from LHCb]

Low-energy vs high-pT



In contrast to the chiral (pure LH) U_1 , limits on $pp \rightarrow \tau^+\tau^-$ are **around the corner** in the LH + RH solution...

... e.g. for $g_U = 3.0$

$M_U \gtrsim 3.5 \text{ TeV}$ [LH + RH]

$M_U \gtrsim 2 \text{ TeV}$ [LH only]

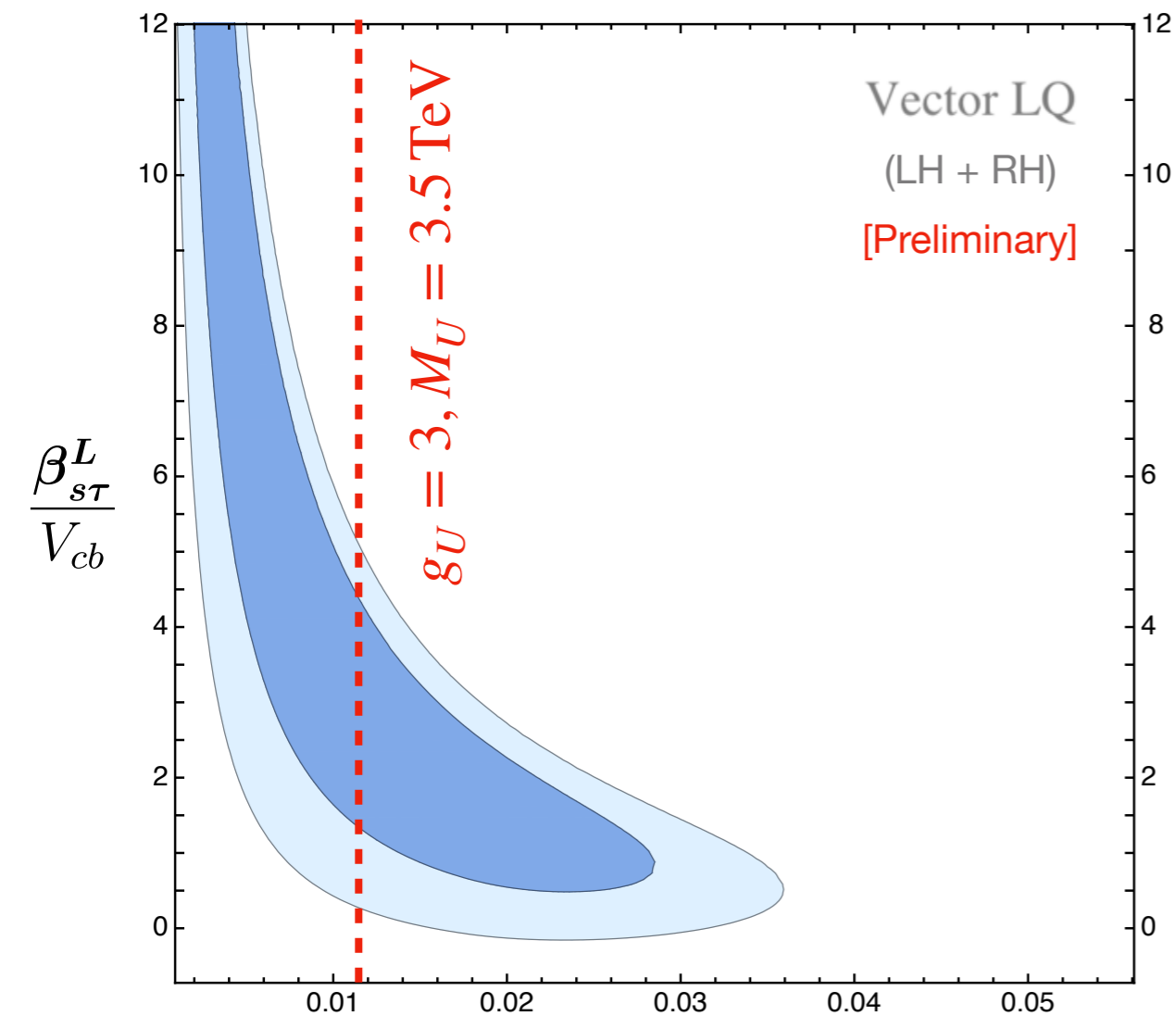
[Baker, JFM, Isidori, König, in preparation]

$\beta_{s\tau} \sim \text{few } V_{cb}$

[Non-trivial but possible in specific UV models]

[JFM, Cornella, Isidori, in preparation]

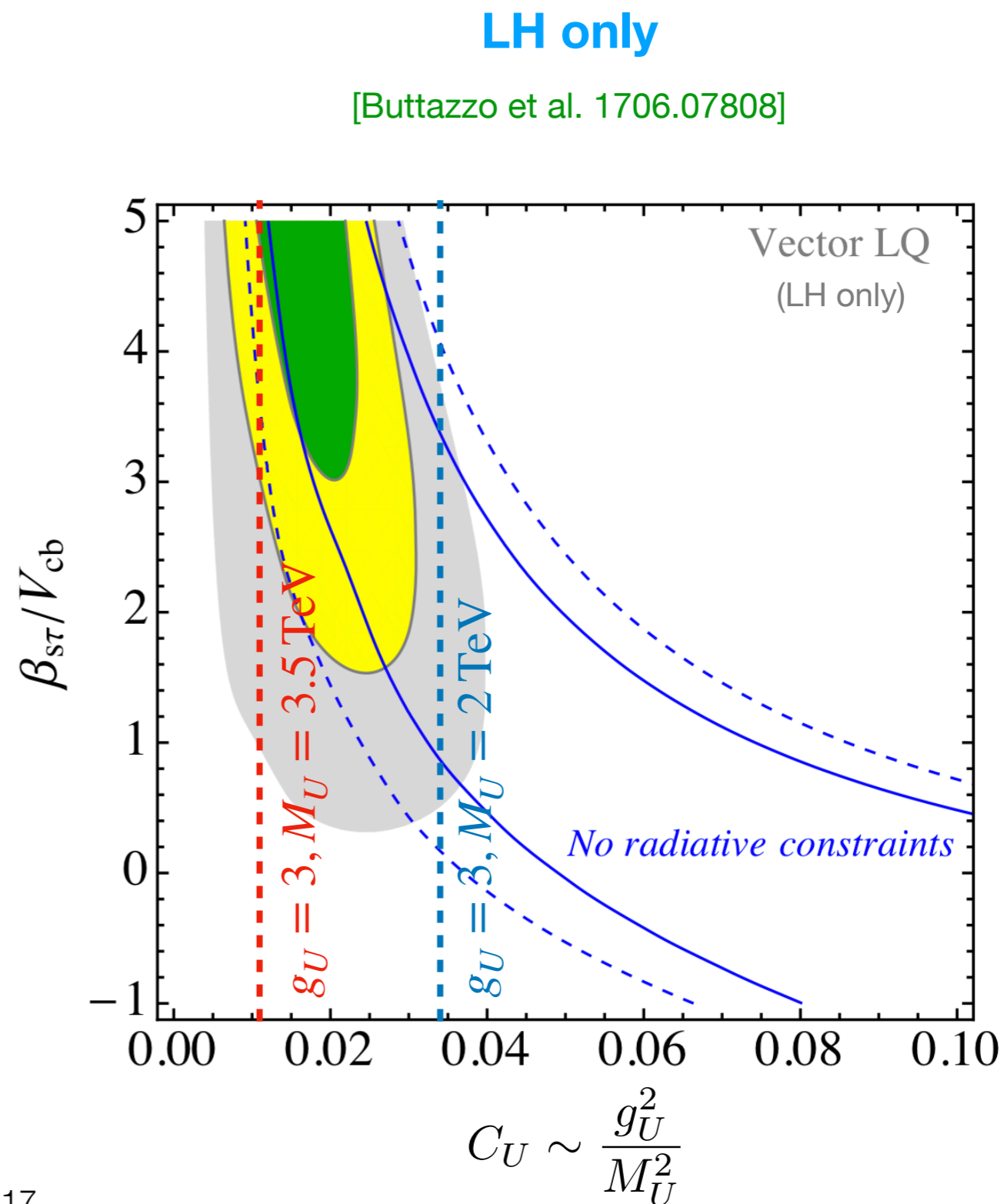
Comparison among U_1 solutions



$$C_U \sim \frac{g_U^2}{M_U^2}$$

LH + RH

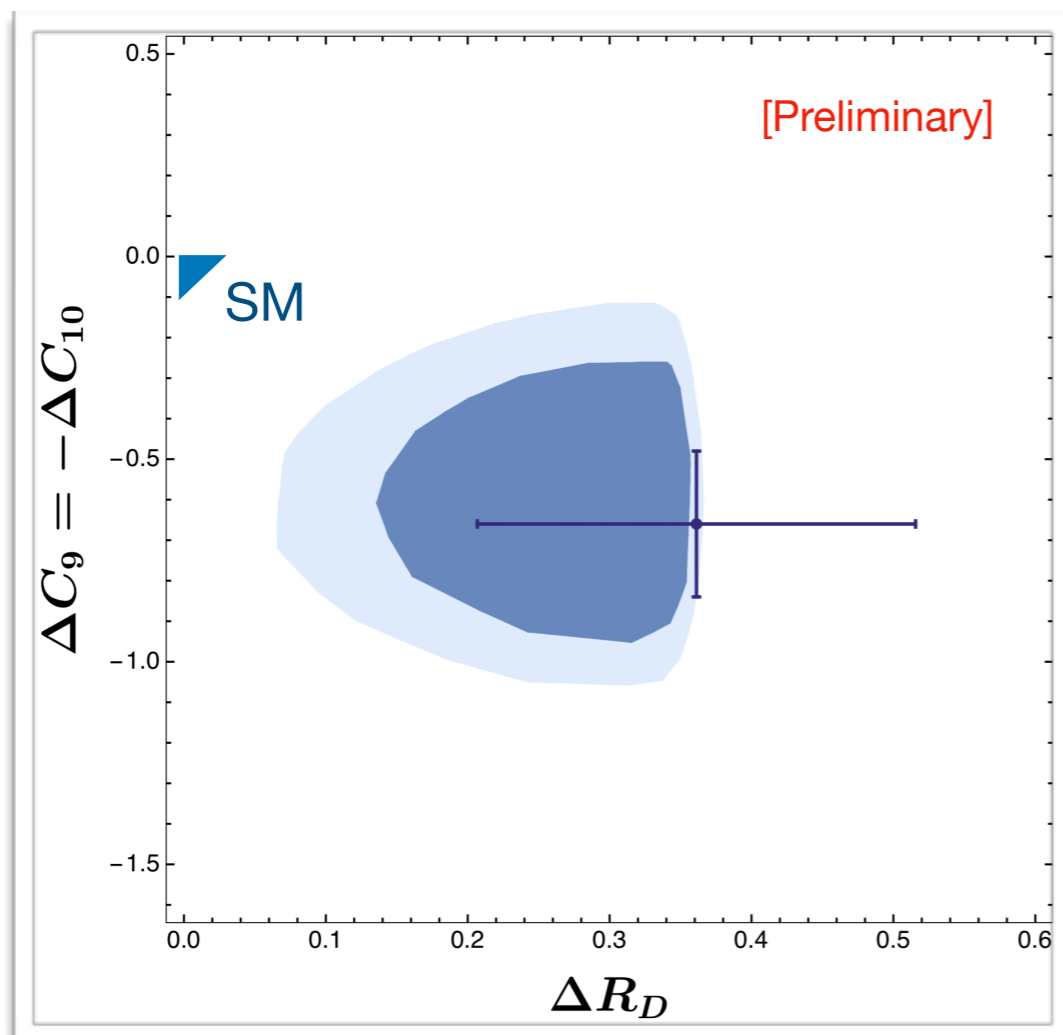
[JFM, Cornella, Isidori, in preparation]



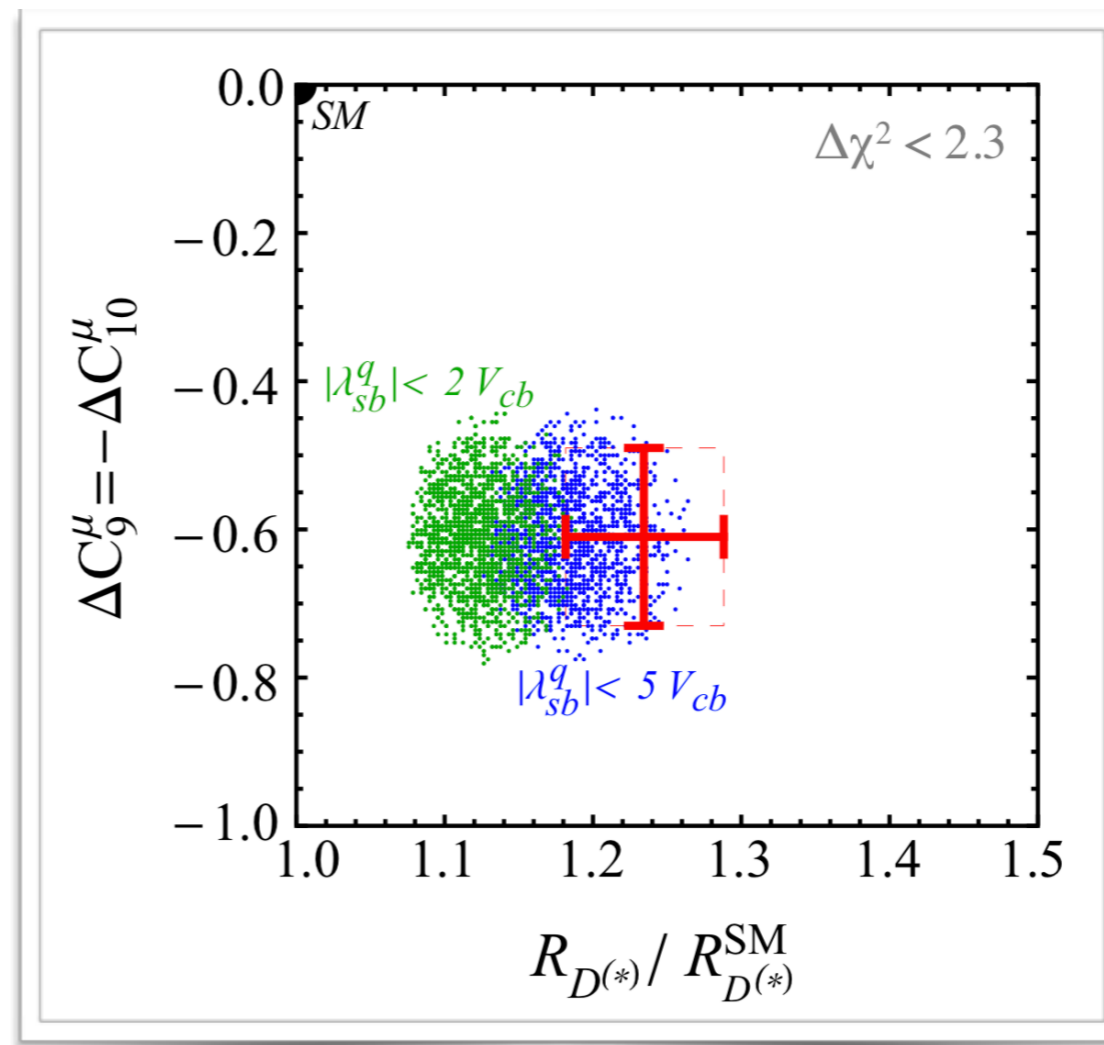
Fitting the anomalies with a U_1 leptoquark

In both solutions the fit to low-energy data is very good

LH + RH



LH only



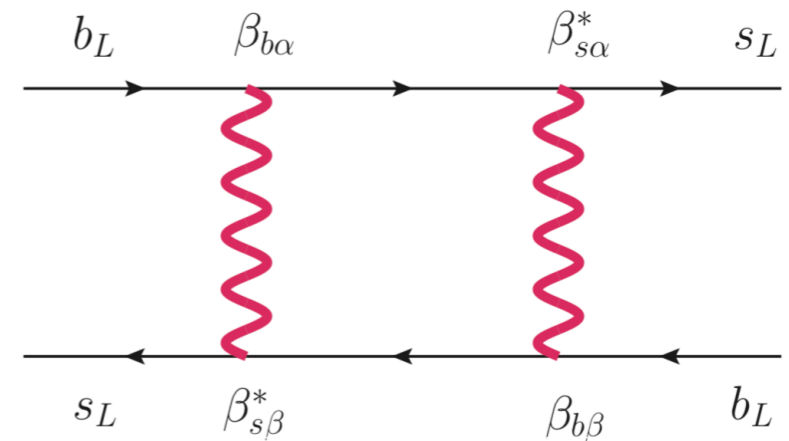
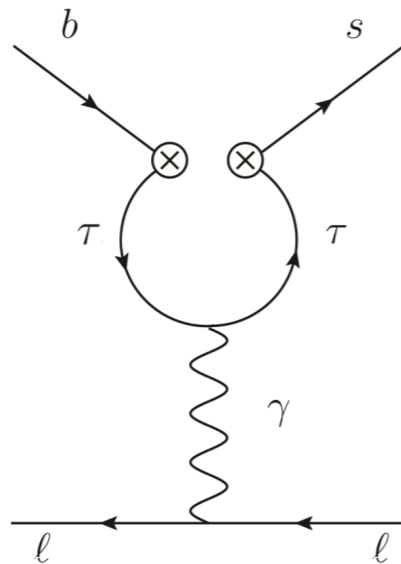
[JFM, Cornella, Isidori, in preparation]

[Buttazzo et al. 1706.07808]

The need for a UV-complete U_1

Loop effects are crucial...

For some loops the dominant effect is captured in the EFT...



Others, like $\Delta F = 2$ observables, are not calculable without a UV-completion

Important (universal) contributions to

$$\Delta C_9^\ell = \Delta C_{10}^\ell$$

The need for a UV-completion of the vector leptiquark is unavoidable

[Bobeth, Haisch, 1109.1826
Crivellin, et al., 1807.02068]

Why not the Pati Salam model?

The vector-leptoquark solution points to Pati-Salam unification

$$\mathbf{PS} \equiv \mathbf{SU}(4) \times \mathbf{SU}(2)_L \times \mathbf{SU}(2)_R$$

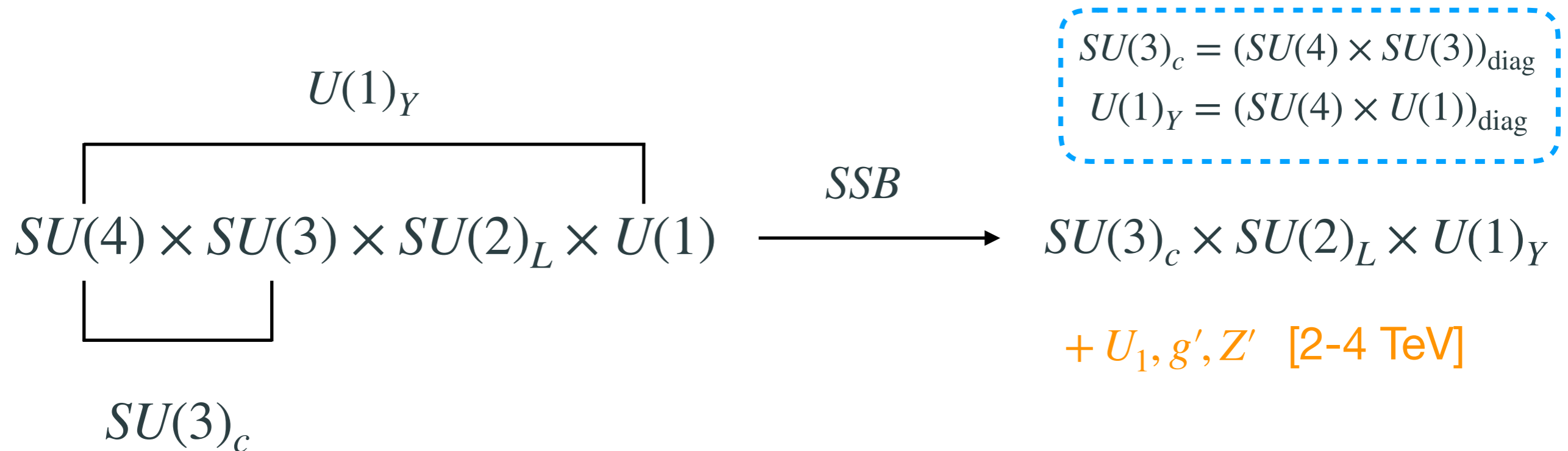
[Pati, Salam, Phys. Rev. D10 (1974) 275]

$$\Psi_{L,R} = \begin{pmatrix} Q_{L,R}^1 \\ Q_{L,R}^2 \\ Q_{L,R}^3 \\ L_{L,R} \end{pmatrix}$$

[Lepton number as the 4th “color”]

- ✓ $\mathbf{SU}(4)$ is the smallest group containing the required vector LQ [$U_1 \sim (\mathbf{3}, \mathbf{1})_{2/3}$]
- ✓ No proton decay (protected by symmetry)
- ✗ The (flavor blind) Pati-Salam model cannot work
 - The bounds from $K_L \rightarrow \mu e$ and $D - \bar{D}$ lift the LQ mass to 100 TeV
- ✗ The associated Z' would be excessively produced at LHC
 - $M_U \sim M_{Z'} \sim \mathcal{O}(\text{TeV})$ & $\mathcal{O}(g_s)$ Z' couplings to valence quarks

The 4321 model(s)



Why an additional $SU(3)$?

✗ The extra $SU(3)$ gives a g' (**coloron**), apart from the Z' already present in PS

✓ It allows to **decorrelate** the $SU(4)$ from the SM color group. In the limit

$g_4 \gg g_{3,1}$, this “solves” the high- p_T problem

→ $\mathcal{O}(g_3/g_4)$ and $\mathcal{O}(g_1/g_4)$ g' and Z' couplings to valence quarks

[Very interesting collider signatures!]

The 4321 model(s)

$$\begin{array}{ccc}
 & U(1)_Y & \\
 & \overbrace{\hspace{15em}} & \\
 SU(4) \times SU(3) \times SU(2)_L \times U(1) & \xrightarrow{SSB} & SU(3)_c \times SU(2)_L \times U(1)_Y \\
 \underbrace{\hspace{10em}} & & + U_1, g', Z' \quad [2-4 \text{ TeV}] \\
 SU(3)_c & &
 \end{array}$$

Different fermion embeddings give two distinct solutions:

- ★ The “original” 4321 [U_1 LH couplings only]
 [di Luzio, Greljo, Nardecchia 1708.08450; Diaz, Schmaltz, Zhong 1706.05033;
 di Luzio, JFM, Greljo, Nardecchia, Renner, 1808.00942]
- ★ “Flavored” 4321 (“natural” low-energy limit of PS^3) [U_1 LH + RH couplings]
 [Bordone, Cornella, JFM, Isidori 1712.01368, 1805.09328; Greljo, Stefanek, 1802.04274]

$$\begin{array}{c}
 \boxed{\phantom{SU(4)_3 \times SU(3)_{1+2} \times SU(2)_L \times U(1)}} \\
 SU(4)_3 \times SU(3)_{1+2} \times SU(2)_L \times U(1) \xrightarrow{\langle \Omega_{1,3,15} \rangle} SU(3)_c \times SU(2)_L \times U(1)_Y \\
 \boxed{} \\
 SU(3)_c
 \end{array}
 + U_1, g', Z' \quad [2-4 \text{ TeV}]$$

	Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
1st & 2nd families	q_L^i	1	3	2	1/6
	u_R^i	1	3	1	2/3
	d_R^i	1	3	1	-1/3
	ℓ_L^i	1	1	2	-1/2
	e_R^i	1	1	1	-1
3rd family	ψ_L^3	4	1	2	0
	$\psi_{R_{u,d}}^3$	4	1	1	$\pm 1/2$
$n_{\text{VL}} = 2$	χ_L^i	4	1	2	0
	χ_R^i	4	1	2	0
	$H_{1,15}$	1, 15	1	2	1/2
	Ω_1	$\bar{4}$	1	1	-1/2
	Ω_3	$\bar{4}$	3	1	1/6
	Ω_{15}	15	1	1	0

“Flavoring” of the gauge group has interesting implications

✓ U(2)-like Yukawa textures
(explanation to the SM flavor hierarchies)

✓ Couplings to 3rd family naturally big

Smaller effects in 1st & 2nd families through SM-Vector-like mixing

Gauge anomaly cancellation implies large U_1 couplings also to RH fields

Concluding remarks

Current data is still inconclusive and the overall picture might change but...

... it is still possible to find interesting solutions to the current B anomalies while remaining consistent with other low- and high-energy data

Connection to the SM Yukawa structure, based on a U(2) structure still viable

Going beyond simplified dynamical models is important

Lesson from 4321: unexpected experimental signatures (g' , Z' , VL fermions,...)

If the anomalies are really pointing to NP, **new experimental indications** (both in high- p_T and at low energies) should show up soon in several observables

... However this conclusion is strongly driven by $R(D^{(*)})$

Thank you!

Backup slides

The 4321 model(s)

$$\begin{array}{c}
 \overbrace{SU(4)_3 \times SU(3)_{1+2} \times SU(2)_L \times U(1)}^{U(1)_Y} \\
 \underbrace{\hspace{10em}}_{SU(3)_c} \xrightarrow{\langle \Omega_{1,3,15} \rangle} SU(3)_c \times SU(2)_L \times U(1)_Y
 \end{array}$$

The “original” 4321

Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
χ_L^i	4	1	2	0
χ_R^i	4	1	2	0
H	1	1	2	1/2
Ω_1	$\bar{4}$	1	1	-1/2
Ω_3	$\bar{4}$	3	1	1/6
Ω_{15}	15	1	1	0

$n_{\text{SM-like}} = 3$

$n_{\text{VL}} = 3$

“Flavored” 4321

Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$
q_L^i	1	3	2	1/6
u_R^i	1	3	1	2/3
d_R^i	1	3	1	-1/3
ℓ_L^i	1	1	2	-1/2
e_R^i	1	1	1	-1
ψ_L^3	4	1	2	0
$\psi_{R,u,d}^3$	4	1	1	$\pm 1/2$
χ_L^i	4	1	2	0
χ_R^i	4	1	2	0
$H_{1,15}$	1, 15	1	2	1/2
Ω_1	$\bar{4}$	1	1	-1/2
Ω_3	$\bar{4}$	3	1	1/6
Ω_{15}	15	1	1	0

1st & 2nd families

3rd family

$n_{\text{VL}} = 2$

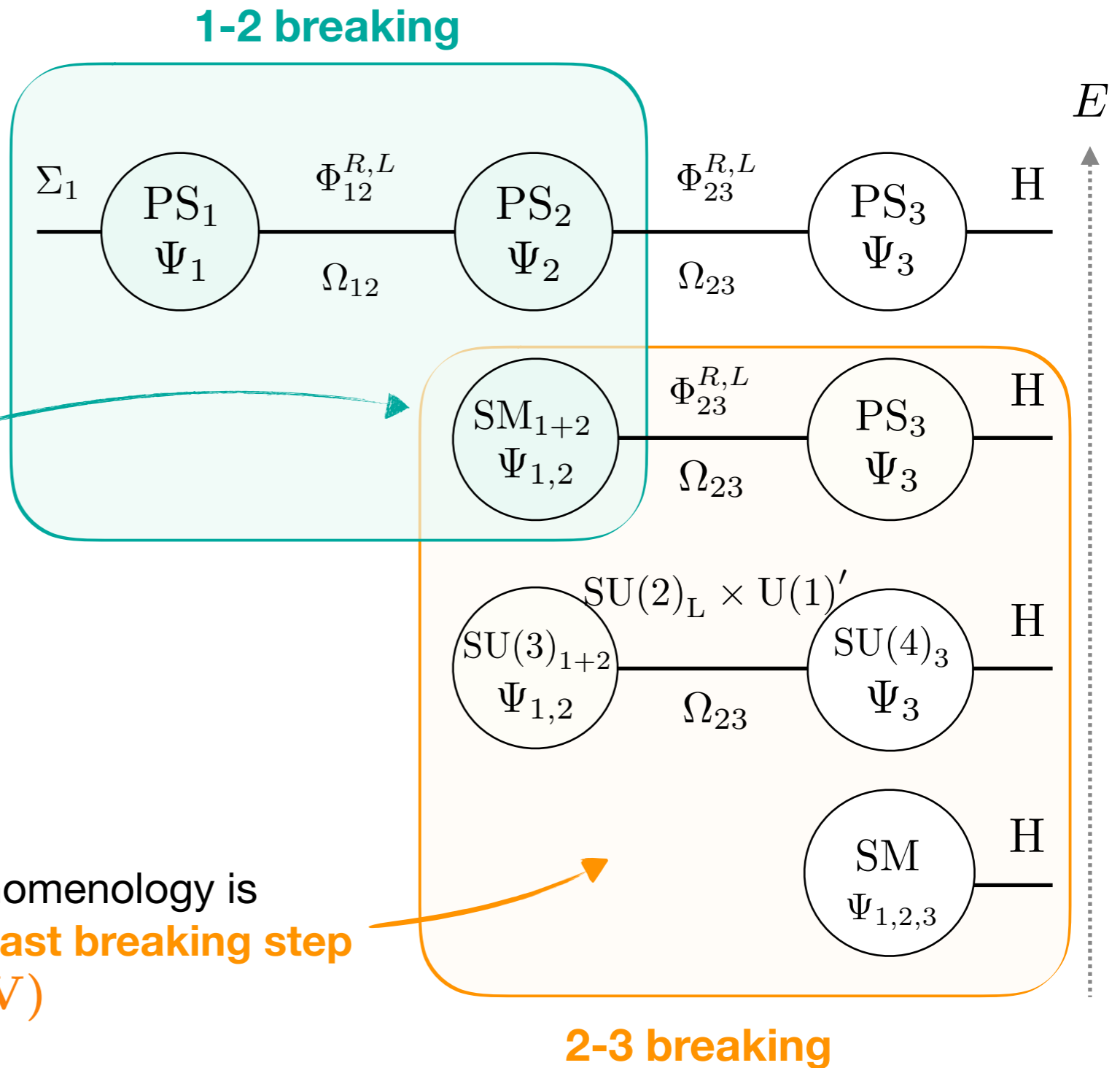
PS³ symmetry breaking pattern

lower limit on 1-2 scale
set by FC processes
involving light generations

$$> 10^3 \text{ TeV}$$

accidental $U(2)^5$ flavour symmetry
In the gauge sector

all low energy phenomenology is
determined by the very **last breaking step**
 $\sim \mathcal{O}(\text{TeV})$



PS³ flavor structure

Yukawa hierarchies from a **flavored gauge structure** + **NP scale hierarchies**

[Bordone, Cornella, JF, Isidori 1712.01368]

SM Yukawas: $\mathcal{L}_Y^{\text{ren}} \supset y_u \bar{\psi}_L^3 \tilde{H} \psi_{R_u}^3 + y_d \bar{\psi}_L^3 H \psi_{R_d}^3$

$|\Delta| \sim \frac{\langle \Phi_{\ell 3}^L \rangle \langle \Phi_{\ell 3}^R \rangle}{\Lambda^2} \sim y_c$

At the NP scale I'm discussing this would be $d = 4$

$$Y_f \sim \begin{bmatrix} \Delta & V \\ 0 & 1 \end{bmatrix}$$

$|V| \sim \frac{\langle \Omega_{1,3} \rangle}{M_\chi} \sim |V_{ts}|$

[see also Greljo, Stefaneke, 1802.04274]

$y_b \approx y_\tau$ ✓

$y_t \approx y_{\nu_3}$ → Requires low-scale seesaw

PS³ flavor structure

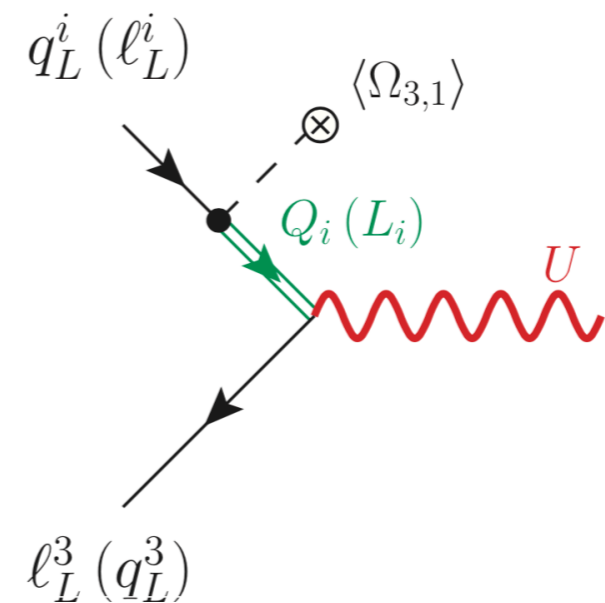
Yukawa hierarchies from a **flavored gauge structure** + **NP scale hierarchies**

SM-VL mixing: $\mathcal{L}_\Psi \supset \lambda_\ell \bar{\ell}'_L \Omega_1 \chi_R + \lambda_q \bar{q}'_L \Omega_3 \chi_R + \lambda_{15} \bar{\chi}_L \Omega_{15} \chi_R + M \bar{\chi}_L \chi_R$

Ω_{15} is a new a source of flavor:

$$\lambda'_{15} \bar{\psi}_L^3 \Omega_{15} \chi_R$$

[Cornella, JF, Isidori, in preparation]



Large 2-3 misalignment
only in LQ transitions!