



# MSSM4G<sup>📶</sup> scenario and vectorlike lepton @ LHC

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Based on [[1608.00283](#)] in collaboration with  
**M. Abdullah, J. L. Feng, and B. Lillard** (UC Irvine)

chiral: $\mathcal{L} \ni y \langle H \rangle \bar{\psi}_R \psi_L$ vector-like: $\mathcal{L} \ni m \bar{\psi}_R \psi_L$
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■ Chiral  $q_4$  ... disfavored by  
 $\sigma(gg \rightarrow h)$

■ Vectorlike  $q_4$

- Motivated by MSSM Higgs mass enhancement
- Searched for at the LHC:  $pp \rightarrow q_4 \bar{q}_4 \rightarrow 2q + 2 \text{ bosons}$

■ Chiral  $e_4$  ... ??? (at least GUT incompatible?)

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- Motivated by MSSM4G model (and more)
- Search-able at the (HL-)LHC



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## ■ Vectorlike $e_4$ **2**

- Motivated by MSSM4G model (and more)
- Search-able at the (HL-)LHC **3**

# ■ SUSY = solution to Naturalness

old-days expectation :

Papucci, Ruderman, Weiler [[1110.6926](https://arxiv.org/abs/1110.6926)]

$$|\mu| \lesssim 200 \text{ GeV} \left( \frac{\Delta^{-1}}{20\%} \right)^{-1/2}$$

$$\sqrt{m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2} \lesssim 600 \text{ GeV} \frac{\sin \beta}{\sqrt{1 + \alpha^2}} \left( \frac{\log(\Lambda/\text{TeV})}{3} \right)^{-1/2} \left( \frac{\Delta^{-1}}{20\%} \right)^{-1/2}$$

$$m_{\tilde{g}} \lesssim 900 \text{ GeV} \cdot \sin \beta \left( \frac{\log(\Lambda/\text{TeV})}{3} \right)^{-1/2} \left( \frac{\Delta^{-1}}{20\%} \right)^{-1/2}$$

difficulties:

- LHC bounds
- radiative Higgs mass

$\Delta$  : “naturalness”

$\alpha = A_t/m_{\tilde{t}}$  (stop mixing parameter)

$\Lambda$  : SUSY-breaking scale

# ■ SUSY = solution

old-days expectation :

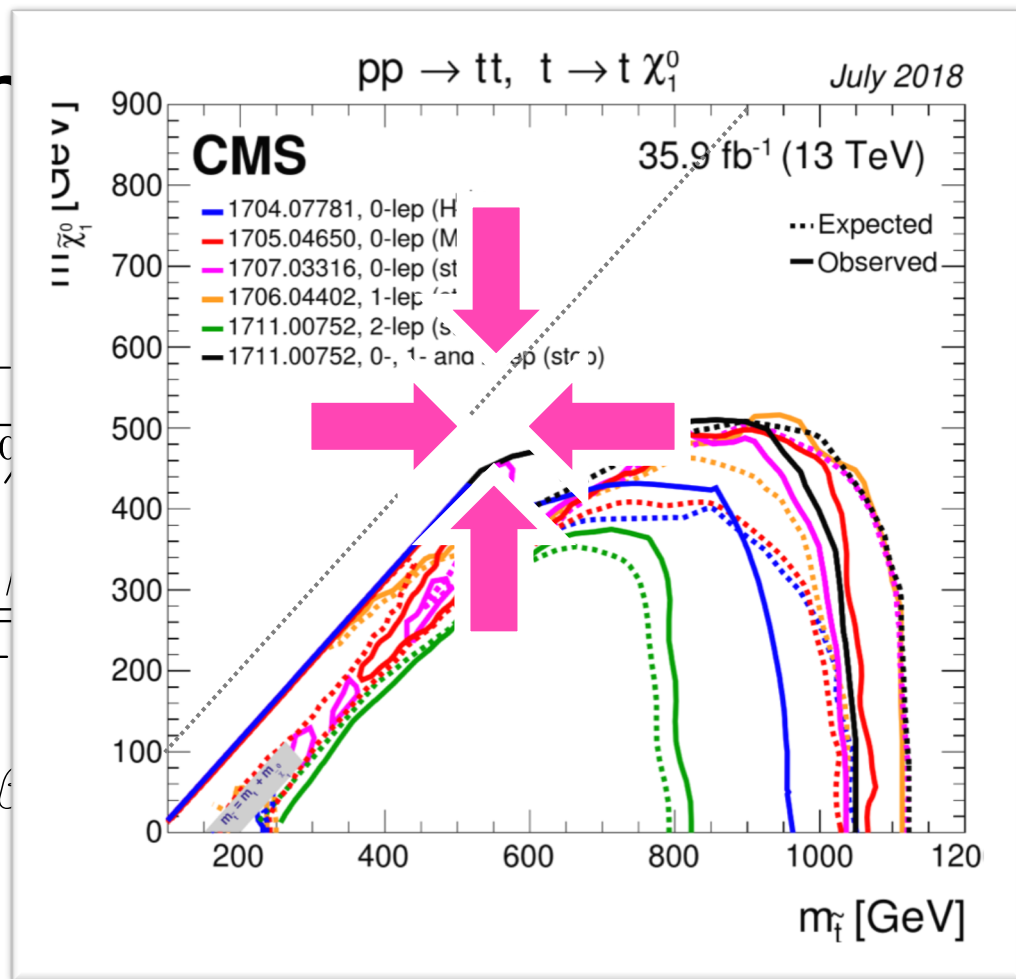
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difficulties:

- LHC bounds ... "avoidable"
- radiative Higgs mass



Δ : "naturalness"

a = A<sub>t</sub>/m<sub>tilde\_t</sub> (stop mixing parameter)

Λ : SUSY-breaking scale

## ■ MSSM prediction

$$m_h^2 \approx m_Z^2 \cos^2(2\beta) + \frac{3y_t^2 \sin^2 \beta}{4\pi^2} m_t^2 \left[ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \alpha^2 \left( 1 - \frac{\alpha^2}{12} \right) \right]$$

$(125\text{GeV})^2$      $(91\text{GeV})^2$     SUSY-breaking effect from  $W \ni \underline{y_t H_u q_3 \bar{u}_3}$

$$\implies m_{\tilde{t}} \gtrsim 1 \text{ TeV}$$

cf. Hall, Pinner, Ruderman [[1112.2703](#)] etc.

## ■ To relax this constraint

- add a scalar particle ("NMSSM")
- add "another top" ... MSSM + vectorlike quark

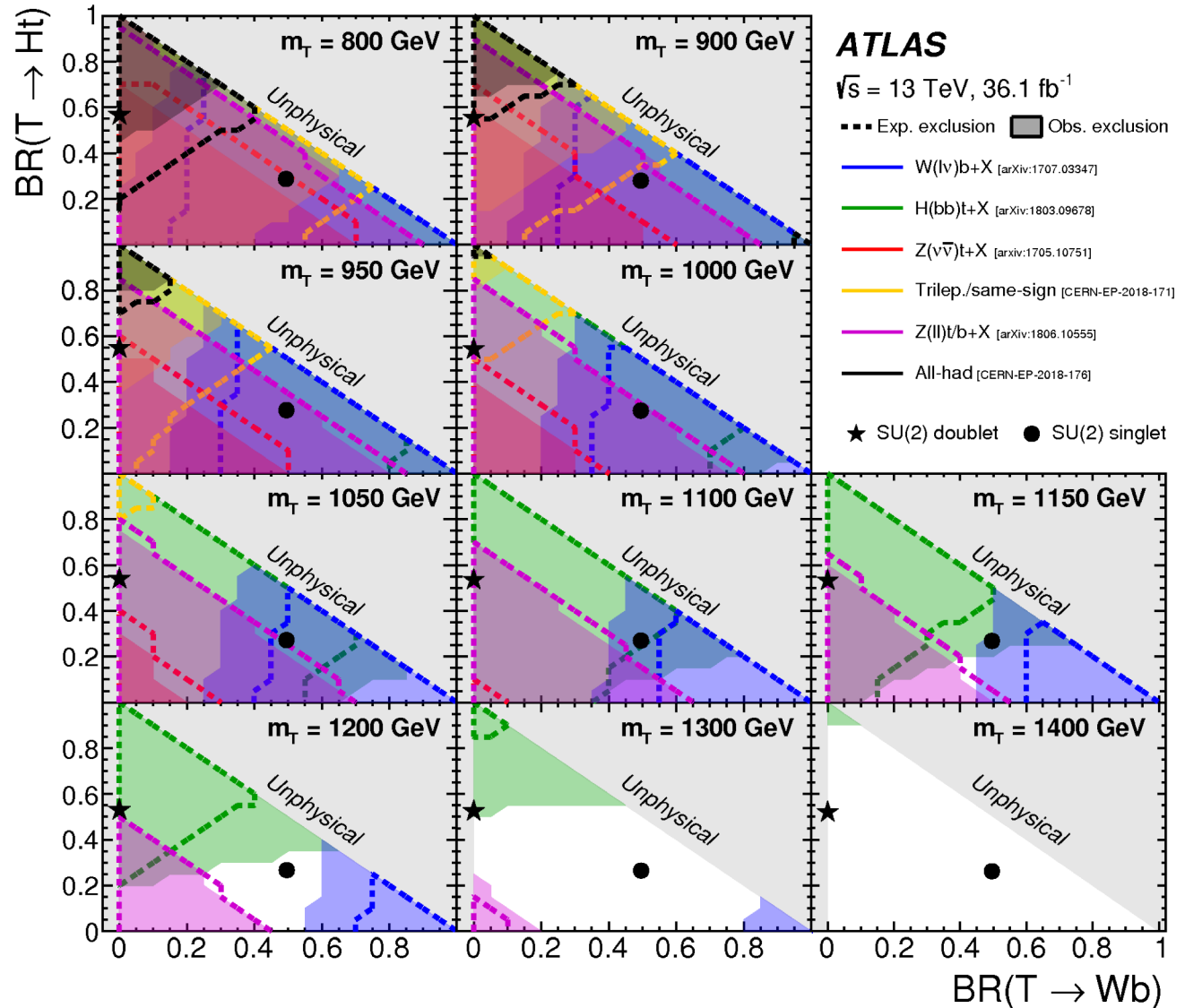
e.g. MSSM +  $q_4 + \bar{u}_4 + \bar{q}_4 + u_4$ :

$$W_{\text{VLQ}} = \underline{y' H_u q_4 \bar{u}_4} + \underline{M_{q_4} q_4 \bar{q}_4} + \underline{M_{u_4} u_4 \bar{u}_4}$$

vectorlike mass terms

assuming  $T \rightarrow Wb$  or  $Ht$  or  $Zt$ ,

$m_T < 1100$  GeV is excluded for any decay patterns (BRs).



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e.g. MSSM +  $q_4 + \bar{u}_4 + \bar{q}_4 + u_4$ : GUT compatibility?

$$W_{\text{VLQ}} = y' H_u q_4 \bar{u}_4 + M_{q_4} q_4$$

$$5 = q + \bar{u} + \bar{e} \text{ in SU(5)-GUT}$$

- MSSM4G scenario

= use this  $e_4$  to solve "bino overabundance"

Abdullah, Feng [1510.06089]

If dark matter is  $\tilde{\chi}^0$  and it is pure-Bino  $\tilde{B}$ ,  
it would give larger DM density than observed.

$\tilde{\chi}^0$ : lightest neutralino

$$\tilde{\chi}^0 = \tilde{B} \oplus \tilde{W}^0 \oplus \tilde{H}_d^0 \oplus \tilde{H}_u^0$$



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1) In early Universe with  $T > m_{\tilde{B}}$  → DM "equilibrium"

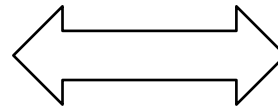
pair creation ( $f\bar{f} \rightarrow \tilde{B}\tilde{B}$ )



pair annihilation ( $\tilde{B}\tilde{B} \rightarrow f\bar{f}$ )



equilibrium



kinetic energy  $\sim T$  ( $> m_{\tilde{B}}$ )

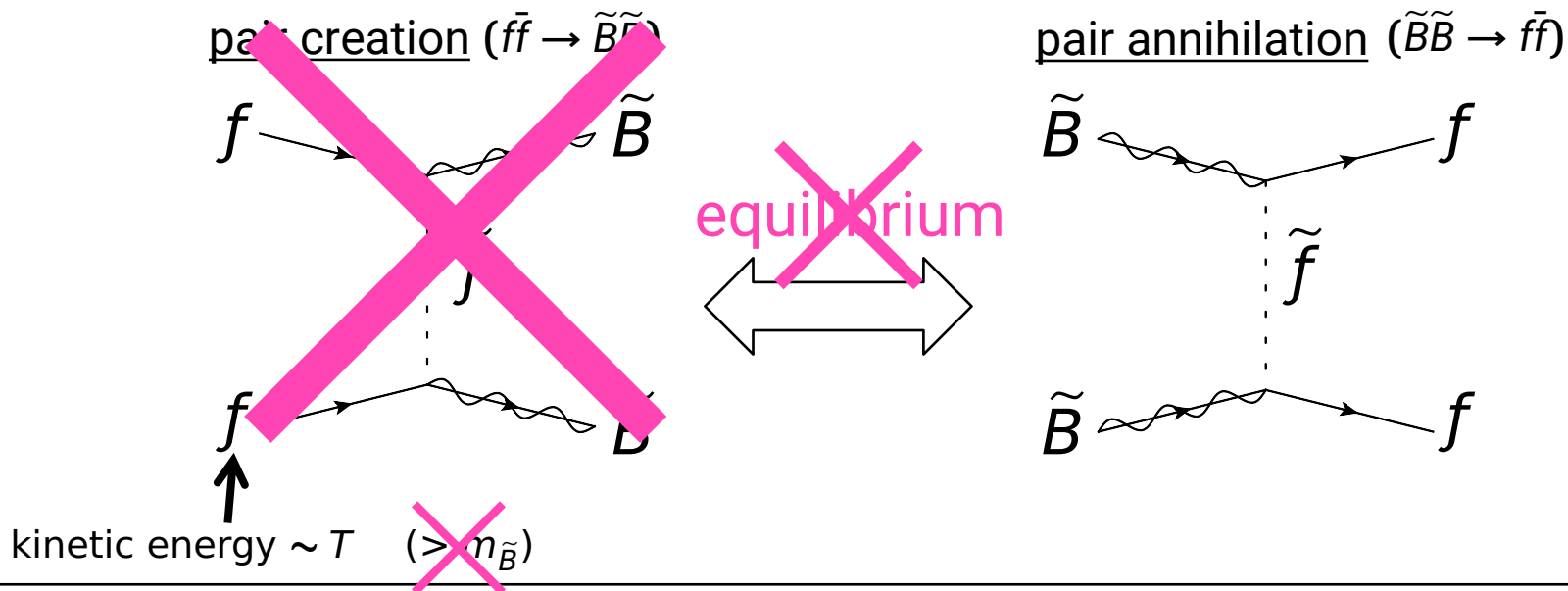
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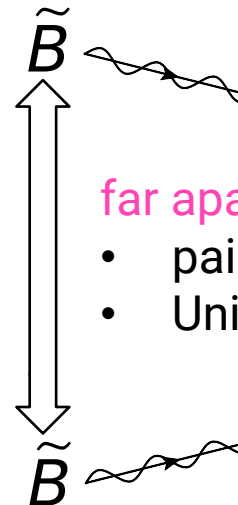
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3) after  $T < m_{\tilde{B}}/20 \rightarrow$  DM **frozen-out**

pair annihilation ( $\tilde{B}\tilde{B} \rightarrow f\bar{f}$ )



- far apart due to
- pair annihilation
  - Universe's expansion

## ■ MSSM4G scenario

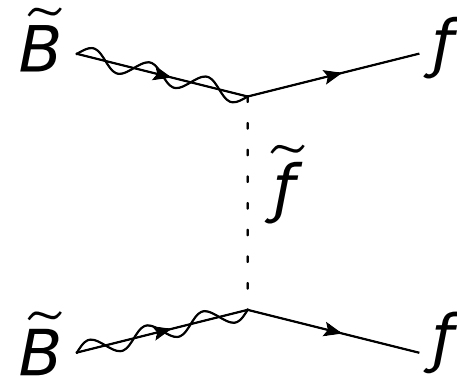
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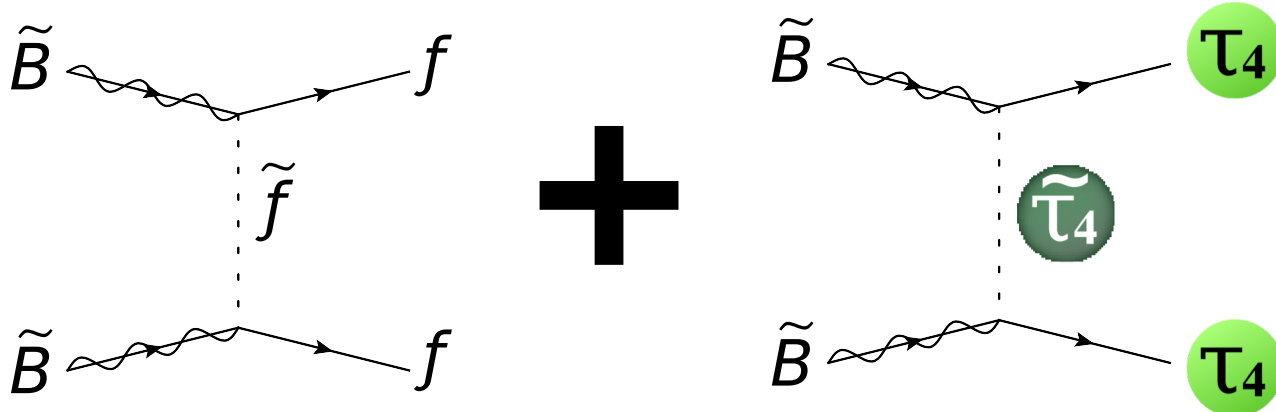


$\tilde{B}$ : smaller cross section  
 $\rightarrow$  "overabundant problem"  
 of Bino thermal relic DM

■ MSSM4G scenario

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extra annihilation channel

if  $\tau_4 \approx \tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$

→ abundance reduced

$$\langle \sigma v \rangle = \frac{g_Y^4 Y_L^2 Y_R^2}{2\pi} \frac{m_f^2}{m_{\tilde{B}}} \frac{\sqrt{m_{\tilde{B}}^2 - m_f^2}}{(m_{\tilde{B}}^2 + m_{\tilde{f}}^2 - m_f^2)^2}$$

■ MSSM4G scenario

= use this  $e_4$  to solve "bino over

$Q : (\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{Q} : (\bar{\mathbf{3}}, \mathbf{2}, -1/6)$
$\bar{U} : (\bar{\mathbf{3}}, \mathbf{1}, -2/3)$	$U : (\mathbf{3}, \mathbf{1}, 2/3)$
$\bar{D} : (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$D : (\mathbf{3}, \mathbf{1}, -1/3)$
$\bar{E} : (\mathbf{1}, \mathbf{1}, 1)$ (same as SM)	$E : (\mathbf{1}, \mathbf{1}, -1)$ (vectorlike partners)

■ QUE model : MSSM +  $Q\bar{Q}U\bar{U}E\bar{E}$

✓ gauge coupling unification

✓ SU(5) GUT

➤ extra  $H_u Q_4 \bar{U}_4$  interaction  $\rightarrow m_h$  

■ QDEE model : MSSM +  $Q\bar{Q}D\bar{D}E\bar{E}E\bar{E}$

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~~✗ SU(5) GUT~~

➤ extra  $H_d Q_4 \bar{D}_4$  coupling  $\rightarrow m_h$  slightly 

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vectorlike mass terms

$$W_{\text{QUE}} = y' H_u Q_4 \bar{U}_4 - y'' H_d \bar{Q}_4 U_4 + \overbrace{M_Q Q_4 \bar{Q}_4 + M_U U_4 \bar{U}_4 + M_E E_4 \bar{E}_4}^{\text{vectorlike mass terms}}$$

$$+ \underbrace{\epsilon_i H_u Q_i \bar{U}_4 + \epsilon'_i H_u Q_4 \bar{U}_i - \epsilon''_i H_d L_i \bar{E}_4}_{\text{SM-Vectorlike mixings}}$$

SM-Vectorlike mixings

- **dangerous** : induce flavor violations
- **necessary** : let VLF decay

... we need an approximate

**DISCRETE  $Z_2$**

(SM: even, VLF: odd)



CASAM  
INVESTICAO



DISCRETE18



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$$W_{QDEE} = y' H_u \bar{Q}_4 D_4 - y'' H_d Q_4 \bar{D}_4 + M_Q Q_4 \bar{Q}_4 + M_D D_4 \bar{D}_4 + M_E E_4 \bar{E}_4 + M'_E E_5 \bar{E}_5$$

$$- \epsilon_i H_d Q_i \bar{D}_4 - \epsilon'_i H_d Q_4 \bar{D}_i - \epsilon''_i H_d L_i \bar{E}_4 - \epsilon'''_i H_d L_i \bar{E}_5$$

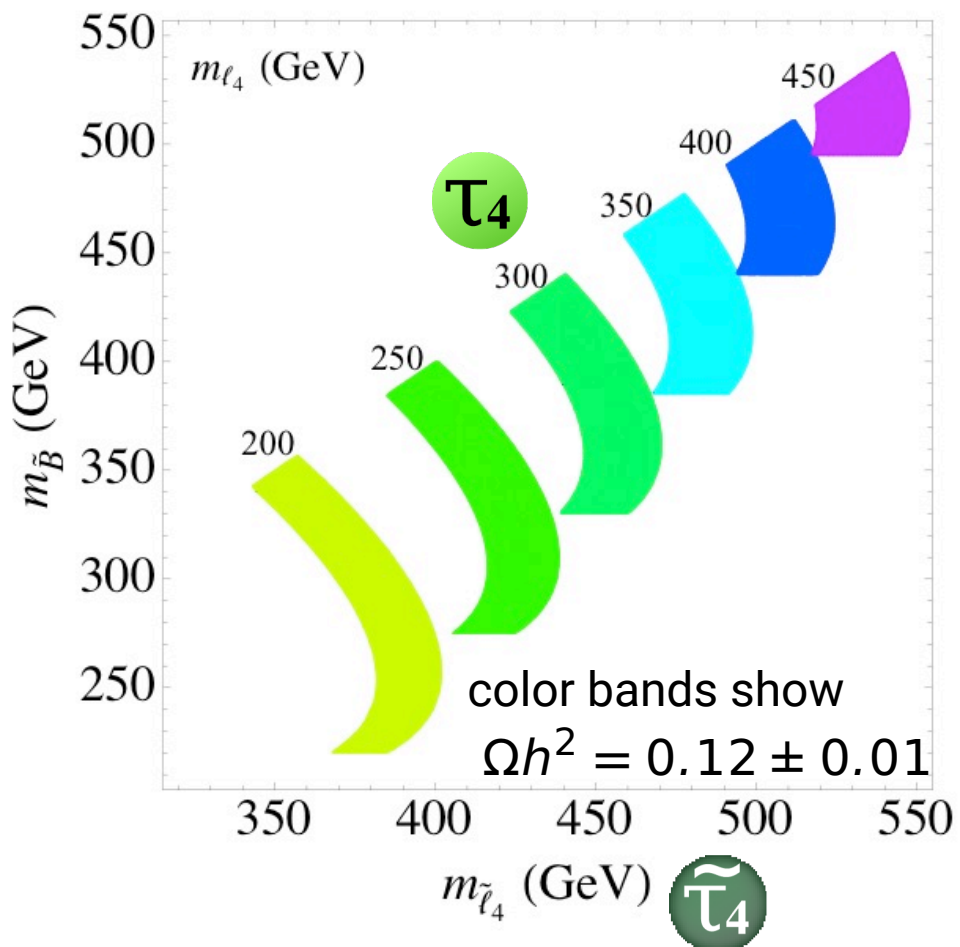
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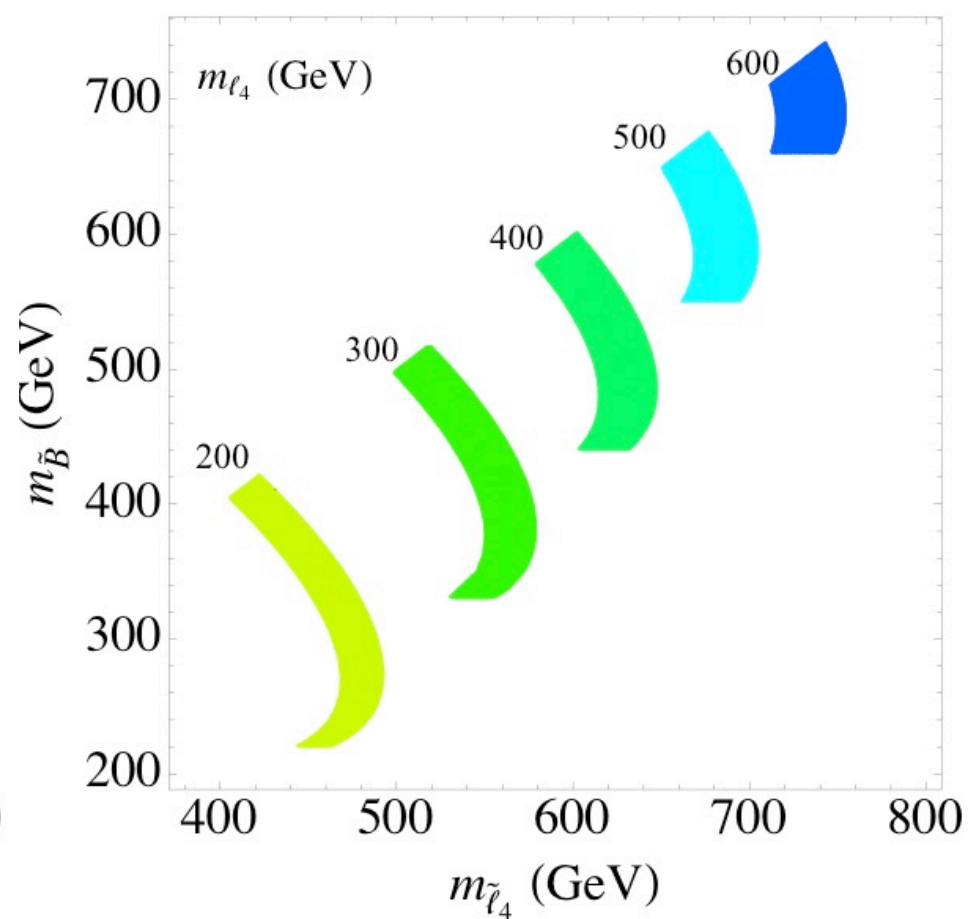
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### QUE model

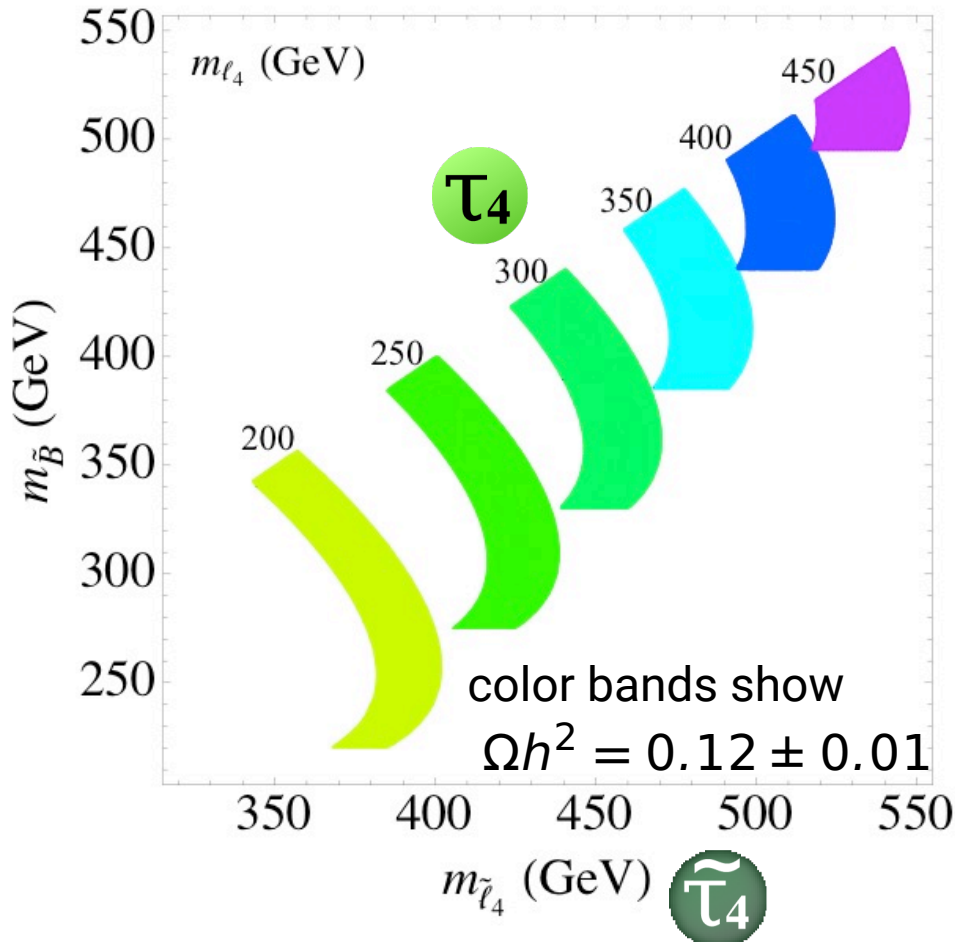


### QDEE model



$$\tilde{\tau}_4 \gtrsim \tilde{B} > \tau_4$$

### QUE model



### ■ LHC searches

- Searches for VL-slepton  $\tilde{\tau}_4$ 
  - 2 lepton + mET search
- Searches for VLL  $\tau_4$

### ■ Gamma-ray observation

- from  $\tau$ -leptons coming from
  - (DM)+(DM) →  $\tau_4 \tilde{\tau}_4$
  - $(Z\tau)(Z\bar{\tau})$

### ■ (DM direct detection)

- LZ, DARWIN, ...

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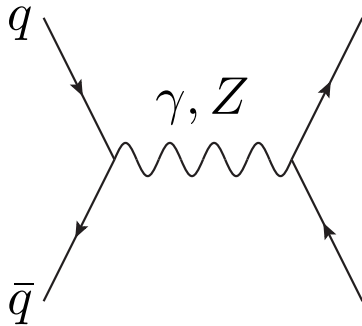
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## ■ Vector-like lepton $\tau_4$

- Lagrangian  $\mathcal{L}_{\text{extra}} = \epsilon_i H L_i \bar{\tau}_4 + m \bar{\tau}_4 \tau_4 + (\text{kinetic})$
- production & decay:

$$pp \rightarrow \tau_4 \bar{\tau}_4, \quad \tau_4 \rightarrow W^- \nu_i, \quad Z l_i^-, \quad h l_i^-$$

"Drell-Yan" production



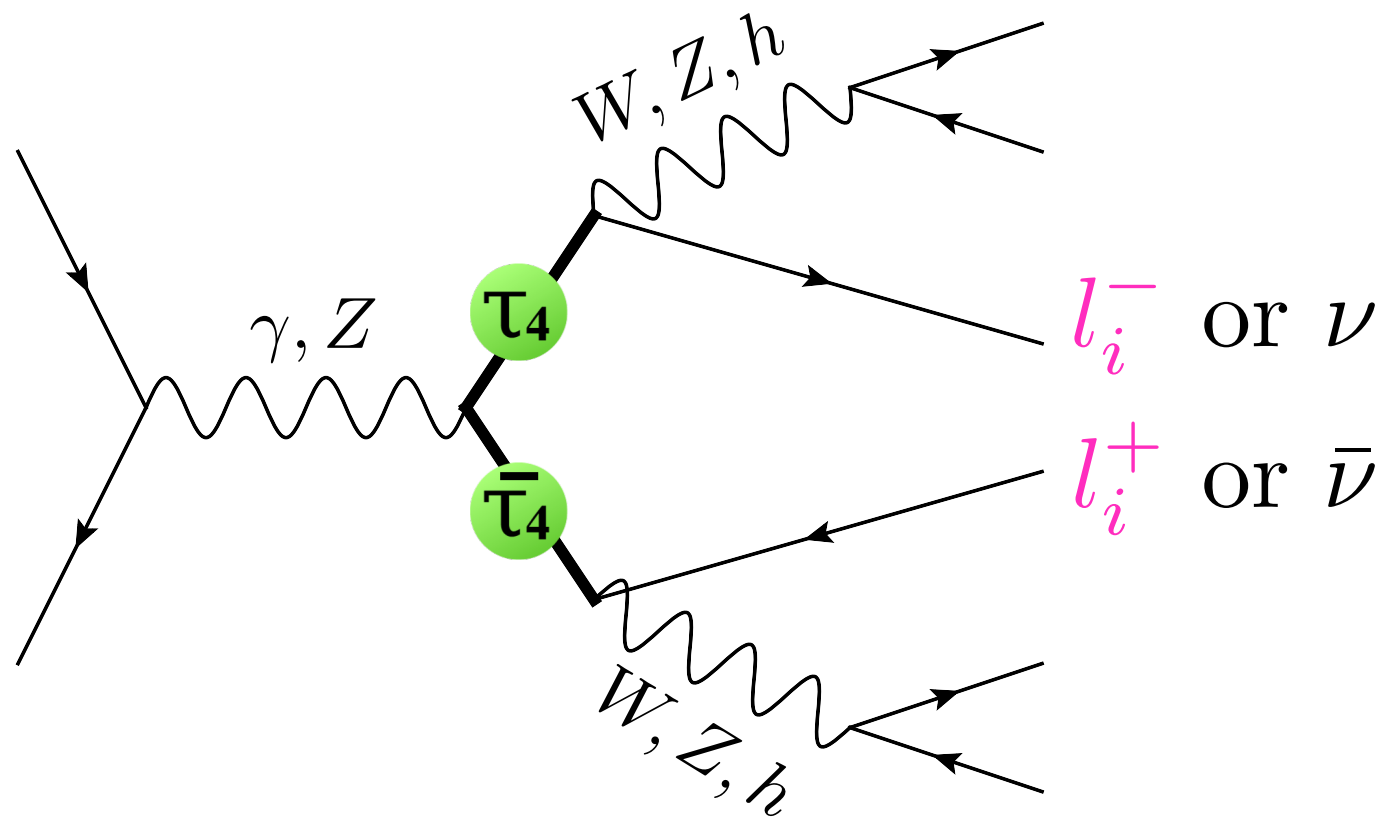
Decay through "SM-4G mixing"

- 3 benchmark scenarios assuming hierarchical  $\epsilon_i$   
(if not  $\rightarrow$  flavor-violation constraints)

- $\text{Br}(\tau_4 \rightarrow e \text{ or } \nu_e) \approx 100\%$
- $\text{Br}(\tau_4 \rightarrow \mu \text{ or } \nu_\mu) \approx 100\%$
- $\text{Br}(\tau_4 \rightarrow \tau \text{ or } \nu_\tau) \approx 100\%$

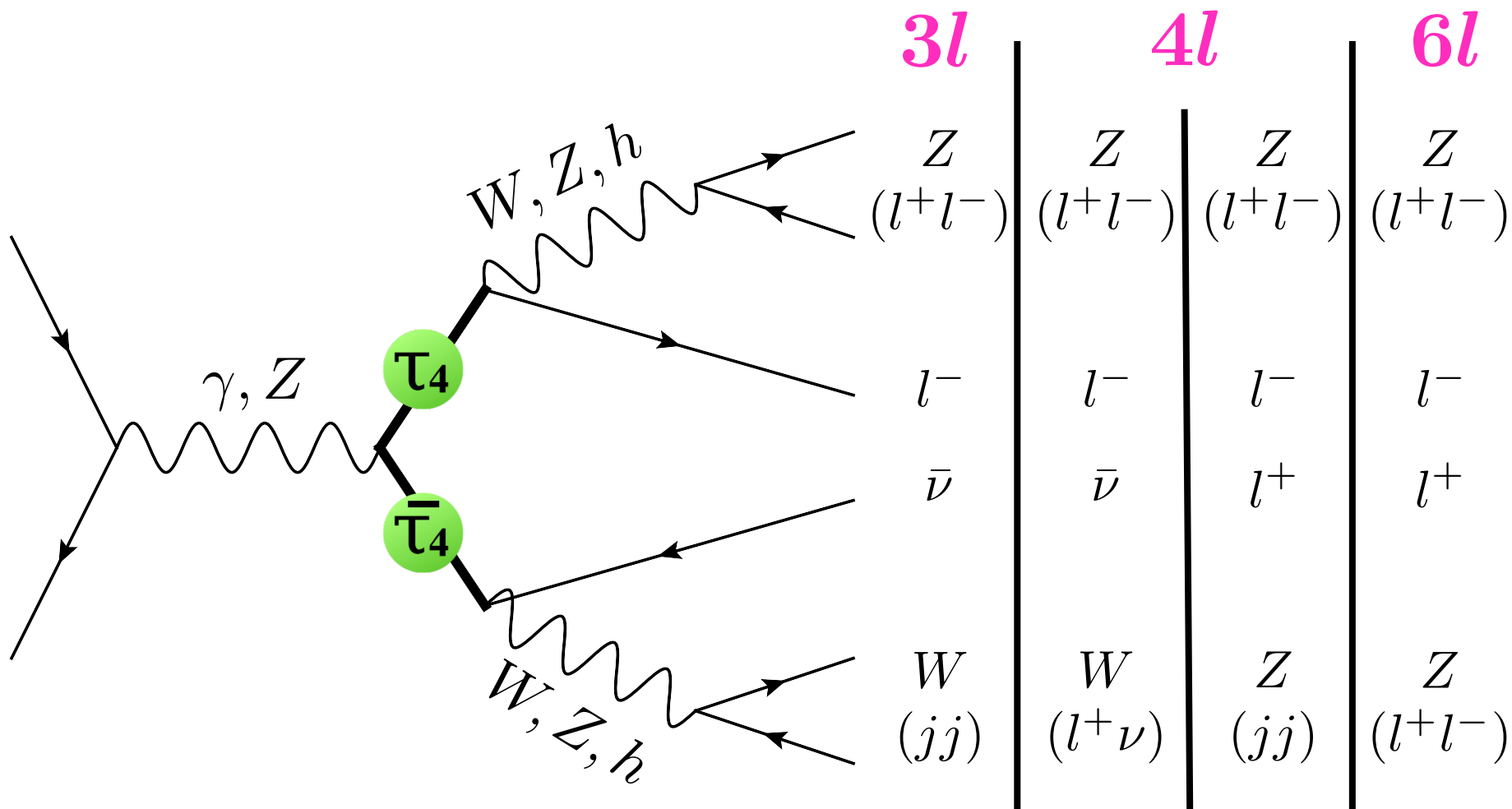
cf.  $\text{Br}(W) : \text{Br}(Z) : \text{Br}(h) \approx 2 : 1 : 1$

- Vector-like lepton :  $pp \rightarrow \tau_4 \bar{\tau}_4$       $\tau_4 \rightarrow Z l_i^-, W^- \nu_i, h l_i^-$



How do you capture this signature?

■ Vector-like lepton :  $pp \rightarrow \tau_4 \bar{\tau}_4$       $\tau_4 \rightarrow Z l_i^-, W^- \nu_i, h l_i^-$



■ Vector-like lepton :  $pp \rightarrow \tau_4 \bar{\tau}_4 \quad \tau_4 \longrightarrow Z l_i^-, W^- \nu_i, h l_i^-$

➤ Our "most basic" approach: **multi- $\ell^\pm$  (3–5 $\ell^\pm$ ) search**

➔ HL-LHC may exclude  $m_{\tau_4} < 350$  GeV  
**if VLL decays to e or  $\mu$ .**  
 (= "mixes with")

details for experts

	$WZ(j)$	$WZ(\ell)$	$ZZ(j)$	$ZZ(\ell)$	
$N_\ell$	$\geq 3$	$\geq 4$	$\geq 4$	$\geq 5$	
$N_j$	$\geq 2$	$< 2$	$\geq 2$	—	
$ m_{jj} - m_W $	$< 20$ GeV	—	—	—	
$ m_{jj} - m_Z $	—	—	$< 40$ GeV	—	←W/Z-like jet pair
$\cancel{E}_T$	$> 60$ GeV	$> 100$ GeV	—	—	←Large mET from $\nu$ &W
$N_{Z(\ell\ell)}$	—	—	$\geq 1$	$\geq 1$	←Z-like lepton pair

- Snowmass BKG set is used.
  - MG5–Pythia–Delphes + NLO K-factor
  - di-boson +  $tt$  dominated
- Signal by FR–MG5aMC–Pythia–Delphes (LO)

- PT cut:  $(\ell_1, \ell_2, \ell_i) > (120, 60, 20)$  GeV,  $(j) > 20$  GeV.
- **tau-tag / b-tag not used (avoided)**
- Uncertainties = stat. + 20% syst.

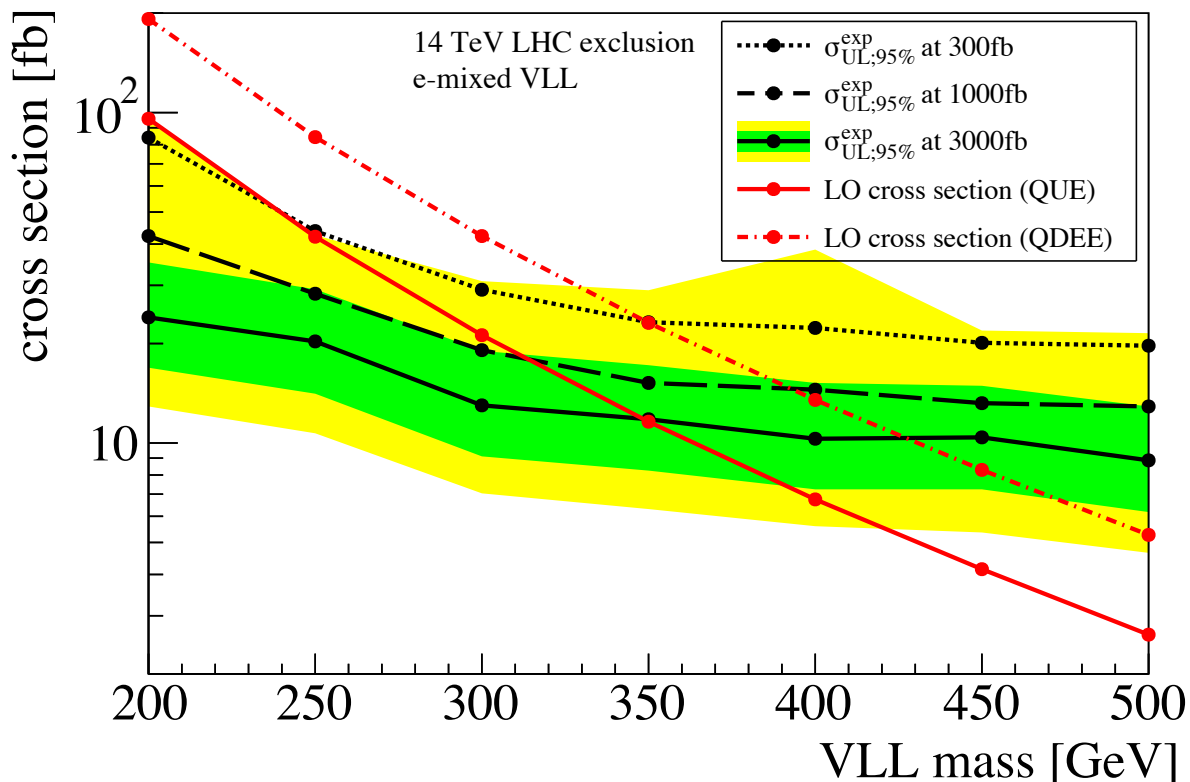


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■ Possible (by expm. physicists) improvements

➤ **This bound is for "right-handed" VLL.**

→ stronger bound expected for left-handed VLL.

➤ Use  $\tau$ -tagging to capture VLL mixed with  $\tau$ .

➤ Use Higgs-tagging to capture VLL decays to  $h$ .

### ■ Vectorlike $q_4$

- $m_h$  (MSSM) <sup>UP</sup> ↗ ; excluded up to 1.1TeV

### ■ Vectorlike $e_4$

$$\mathcal{L}_{\text{extra}} = \epsilon_i H L_i \bar{\tau}_4 + m \bar{\tau}_4 \tau_4 + (\text{kinetic})$$

- MSSM4G model: solves Bino-overabundance
- HL-LHC expectation : **350 GeV** if "right-handed" & mixed with  $e$  or  $\mu$

## What I skipped

- MSSM4G is testable also by **DM-direct** and **Gamma-ray**.

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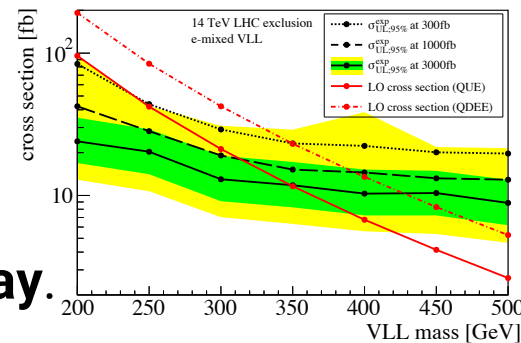
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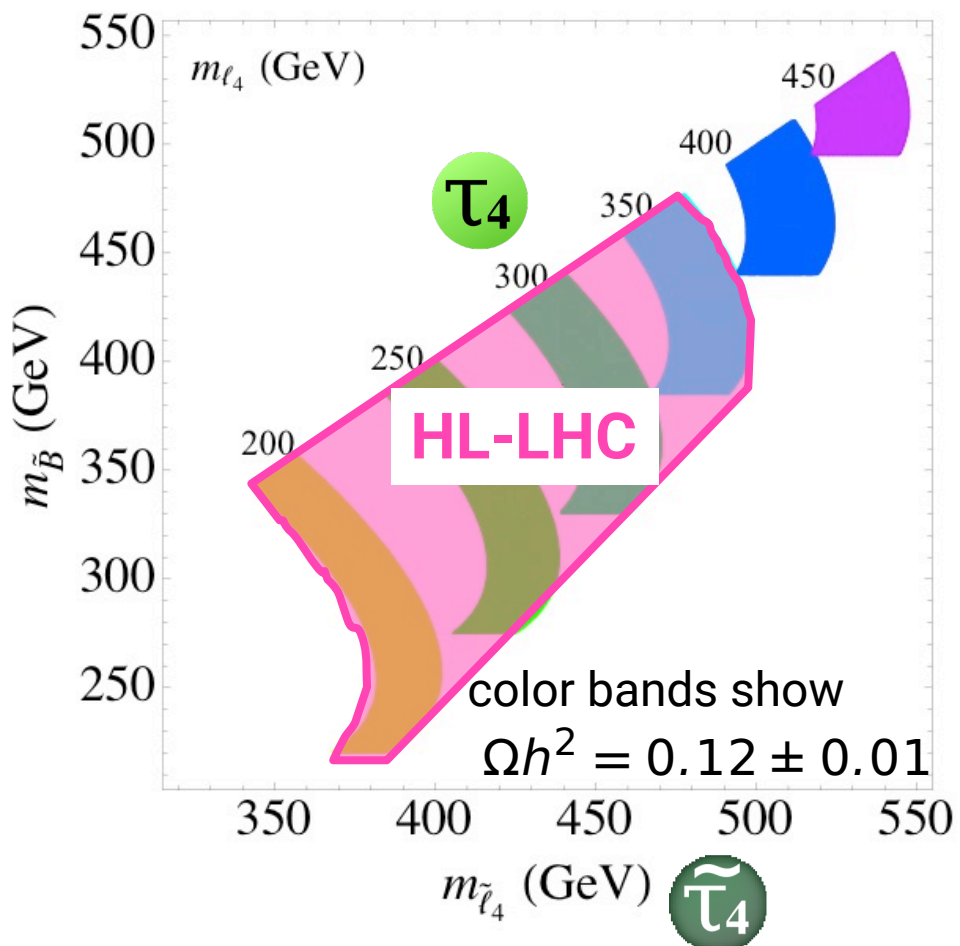
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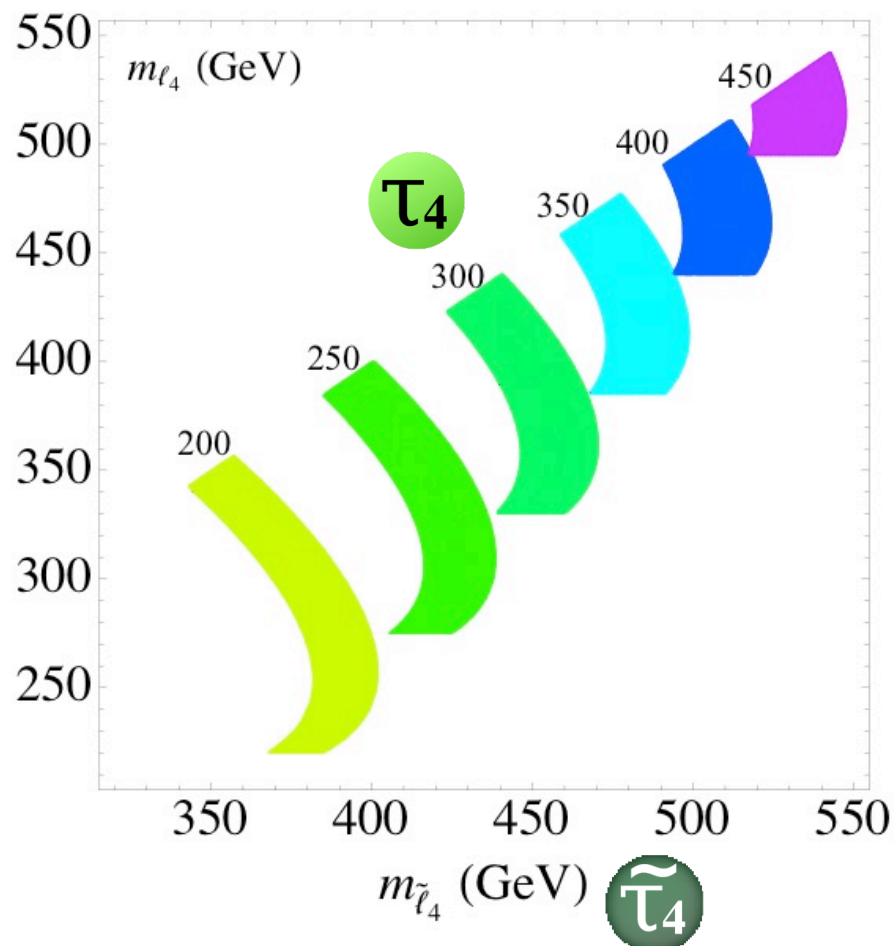
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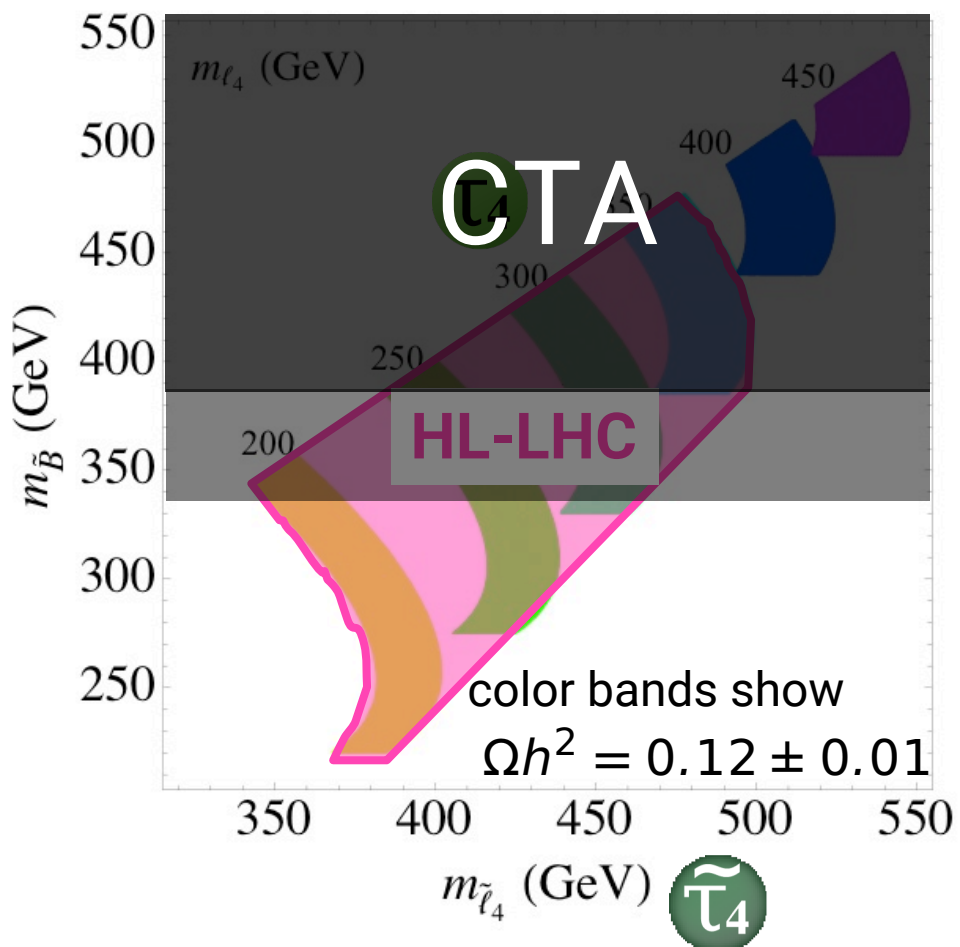
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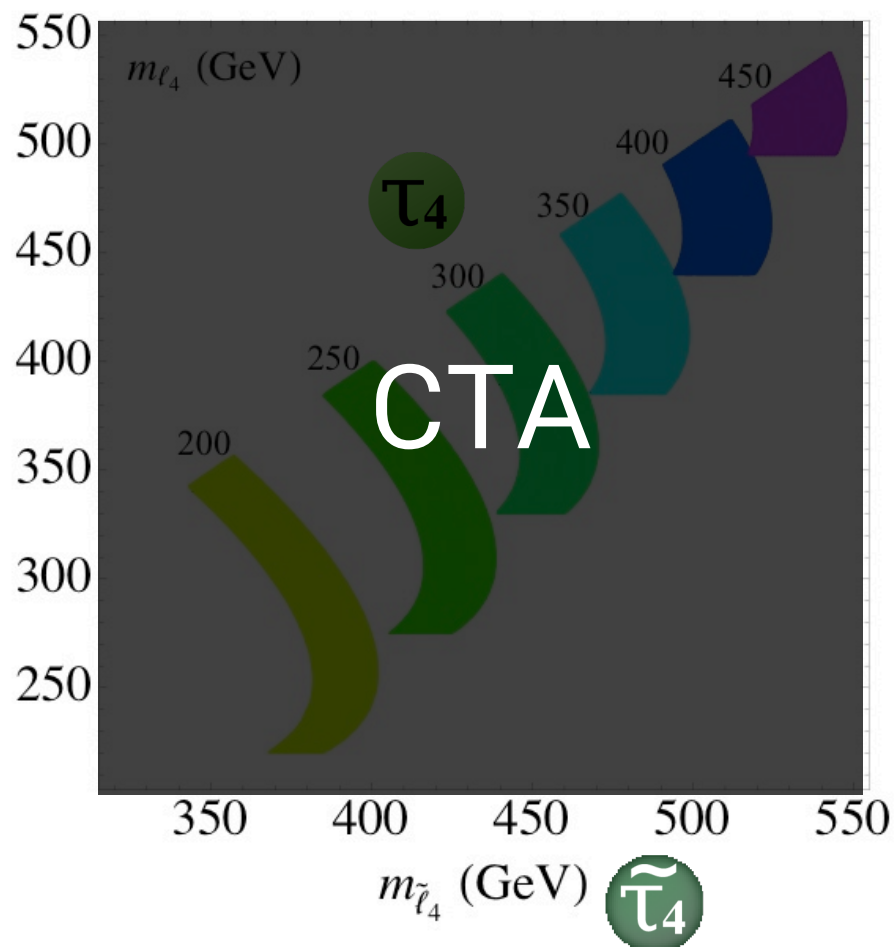
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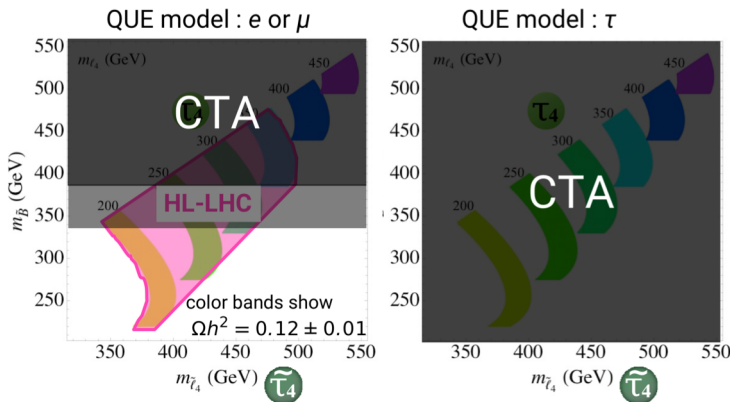
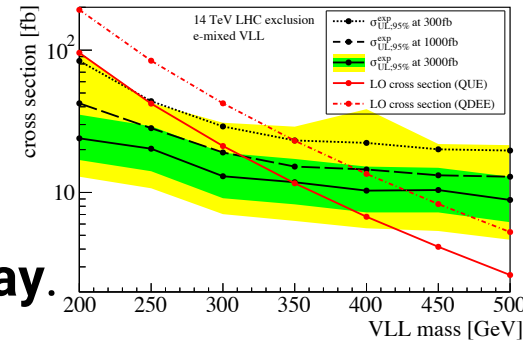
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## What I skipped

- MSSM4G is testable also by **DM-direct** and **Gamma-ray**.

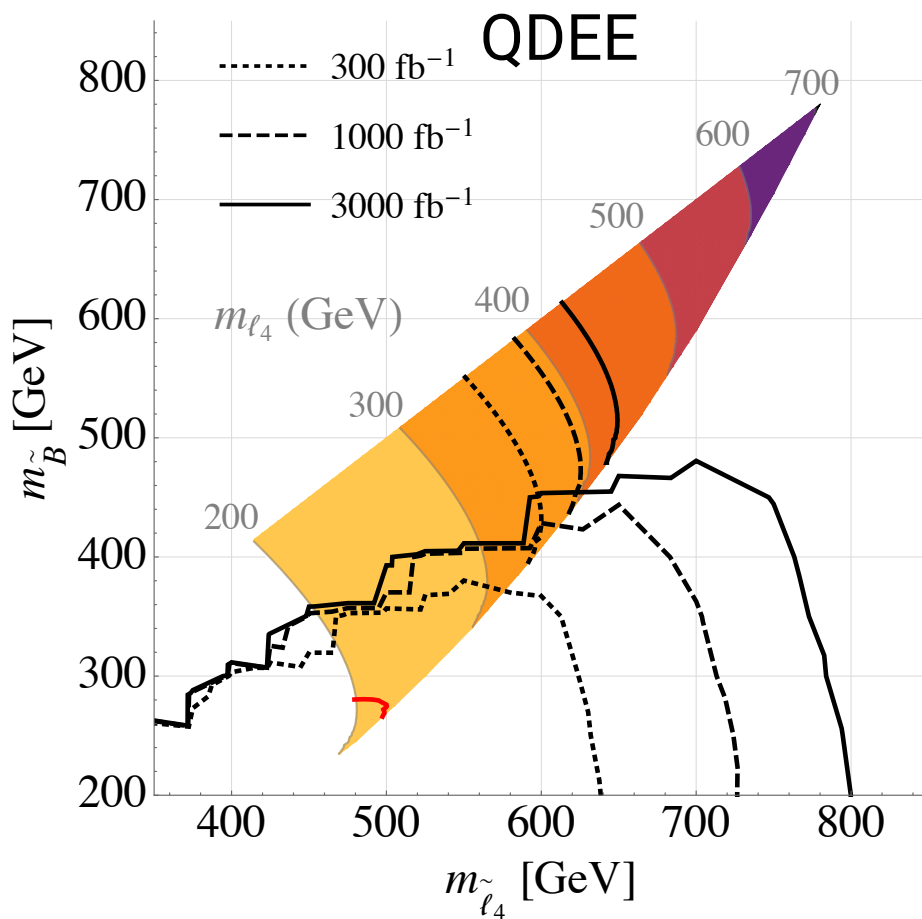
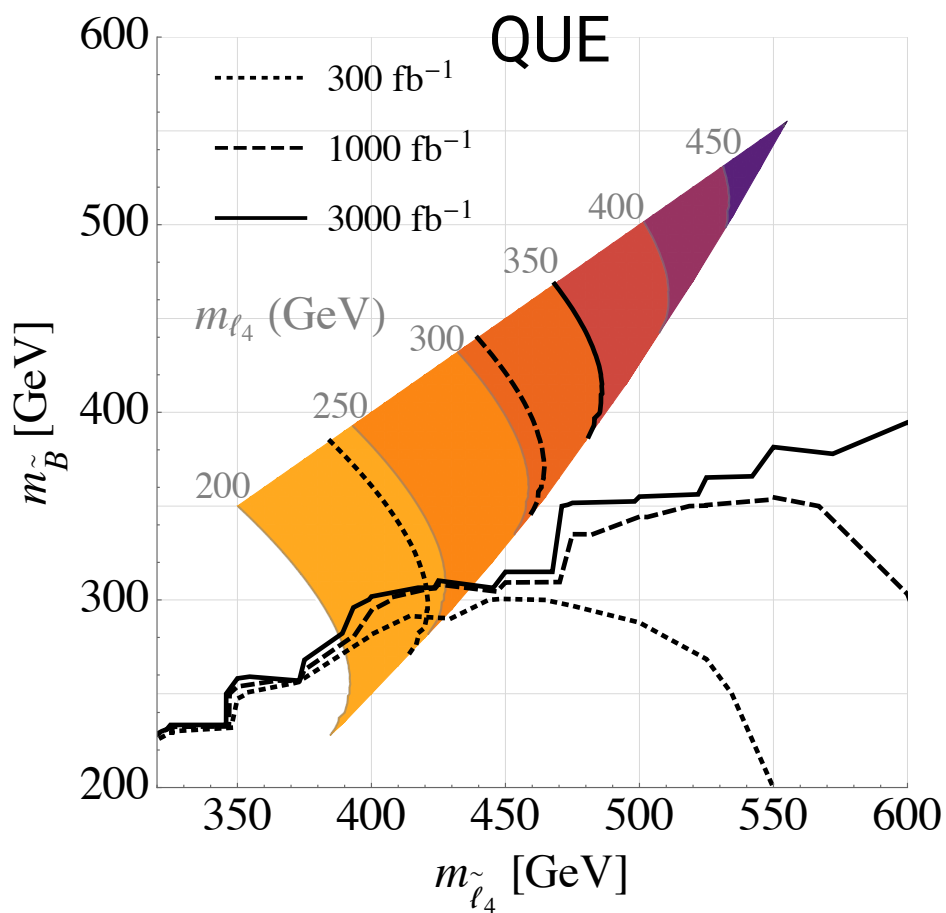


# MSSM4G "official" space

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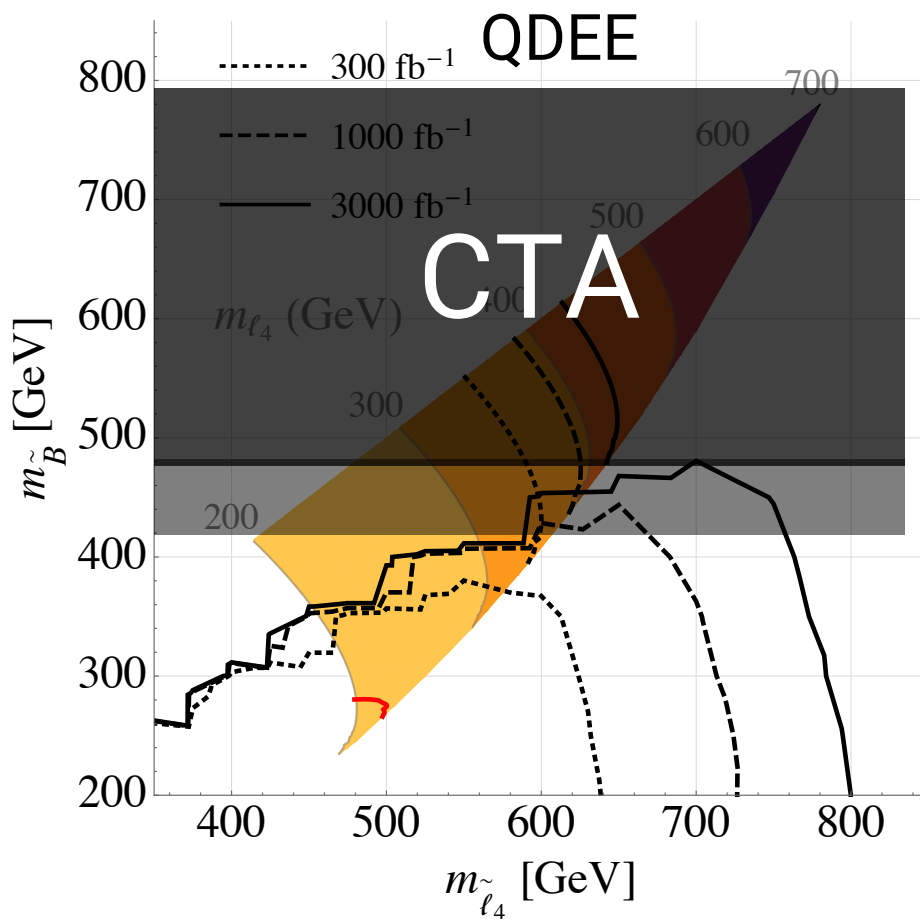
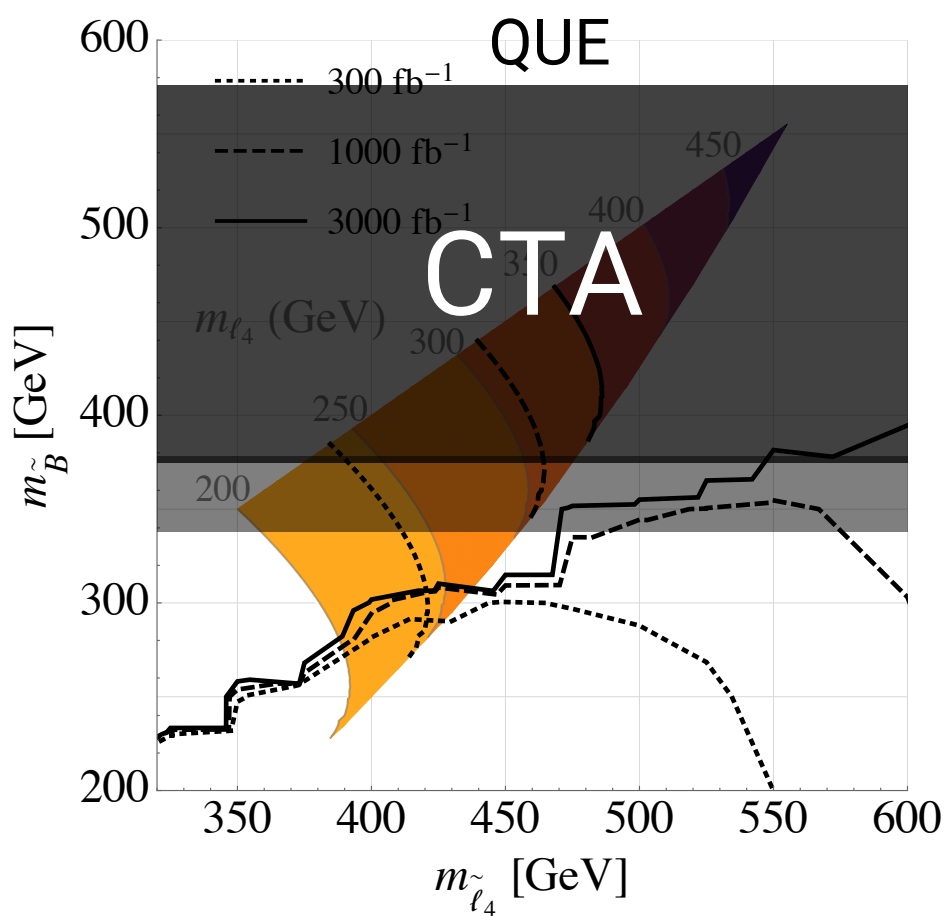
■ if 4G lepton decays to electron or muon



■ if 4G lepton decays to tau-lepton

LHC insensitive ... ( · ω · )

■ if 4G lepton decays to electron or muon



■ if 4G lepton decays to tau-lepton

LHC insensitive ... ( · ω · )

# DM indirect detection Backup

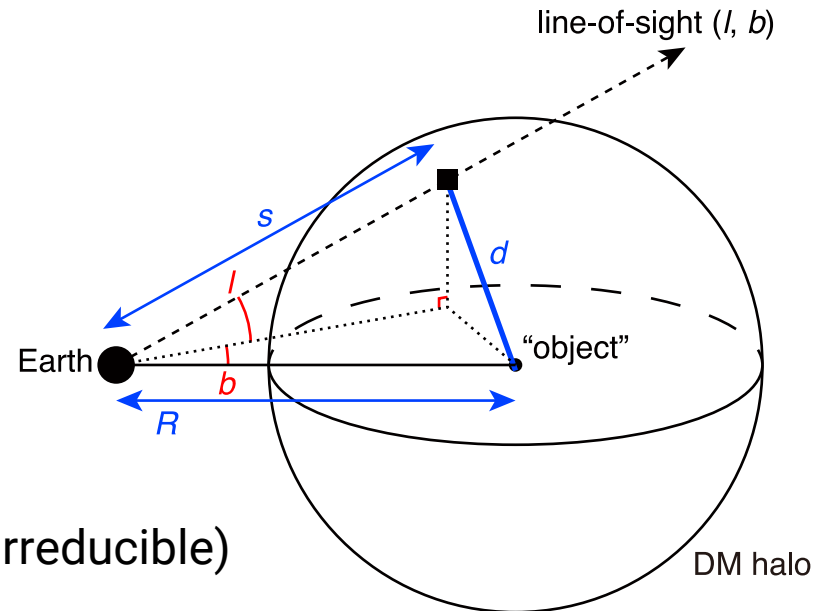
---

## ■ charged particles → diffusion

- $e$  :  $\sim 1$  kpc are observable
- $P$  :  $\sim O(10)$  kpc  $\sim$  Milky Way

## ■ neutral particles

- from (neighbor of) galactic center
  - larger density, huge BKG (miss-ID & irreducible)
  - $J \sim 10^{22}$  GeV<sup>2</sup>/cm<sup>5</sup> (NFW; cuspy)
- from dwarf spheroidals (mini-galaxies near MW)
  - DM rich, less baryon → low BKG
  - $J < 10^{19-20}$  GeV<sup>2</sup>/cm<sup>5</sup> (smaller profile dependence)



$$J = \int d\Omega_{l,b} \int_0^\infty ds \rho(d)^2$$

$$(d^2 = s^2 + R^2 - 2Rs \cos b \cos l)$$

### ■ < 100 GeV : satellites

- full-sky,  $\sim 1\text{m}^2$ , 5–10% energy resolution
- Fermi-LAT (2008) : gamma-ray to electron conversion

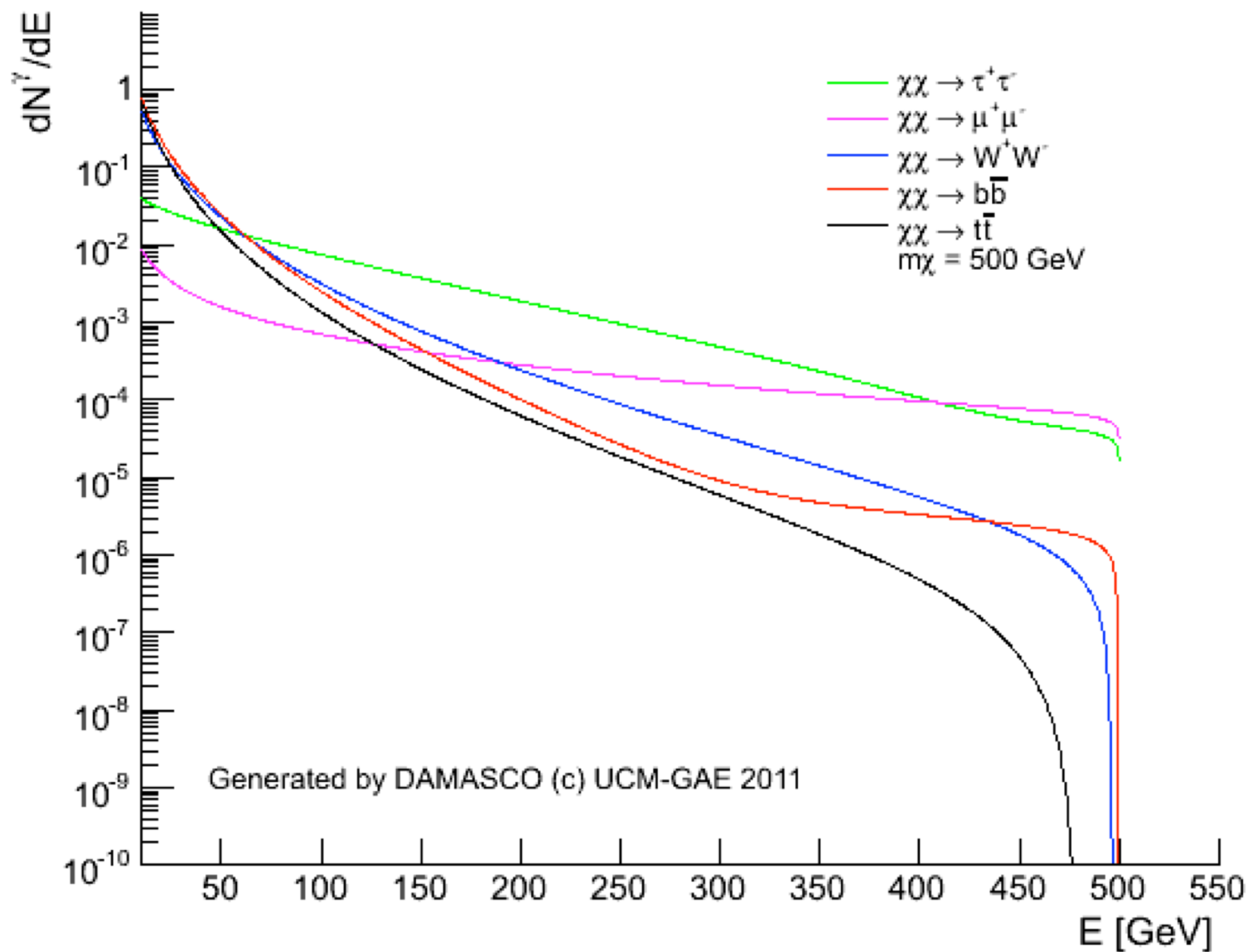
### ■ > 100 GeV : ground-based Air Cherenkov Telescopes

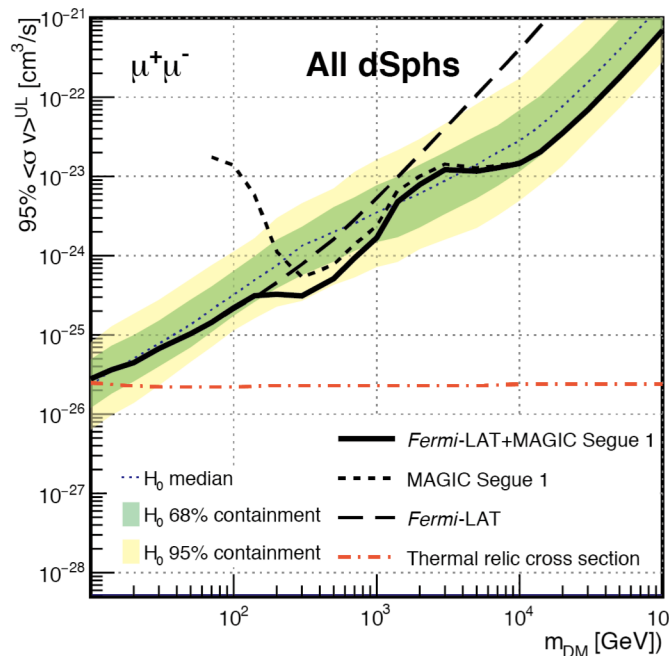
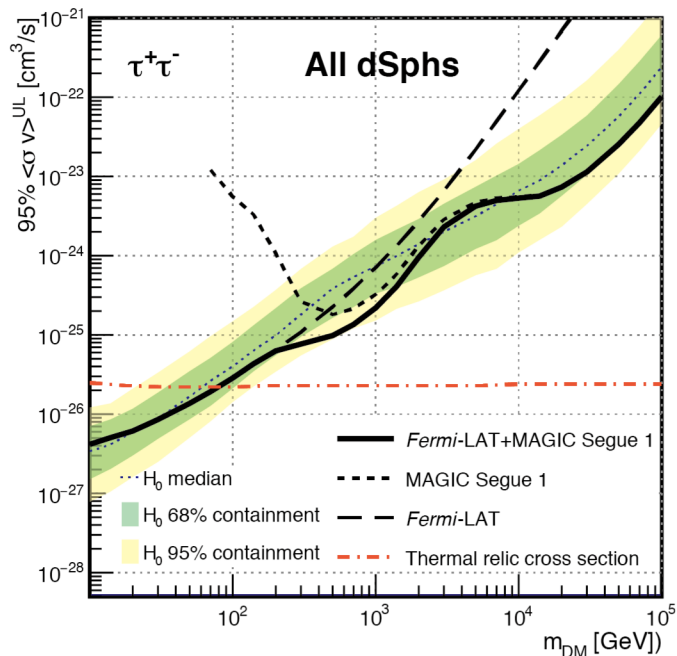
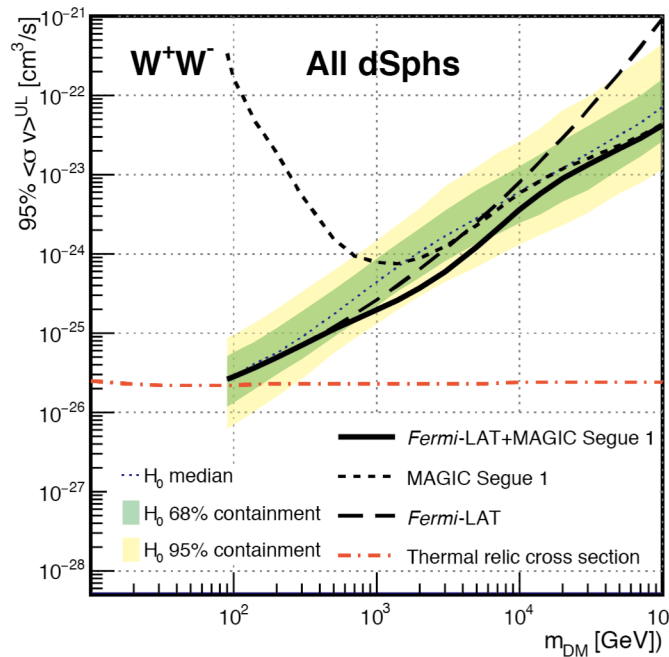
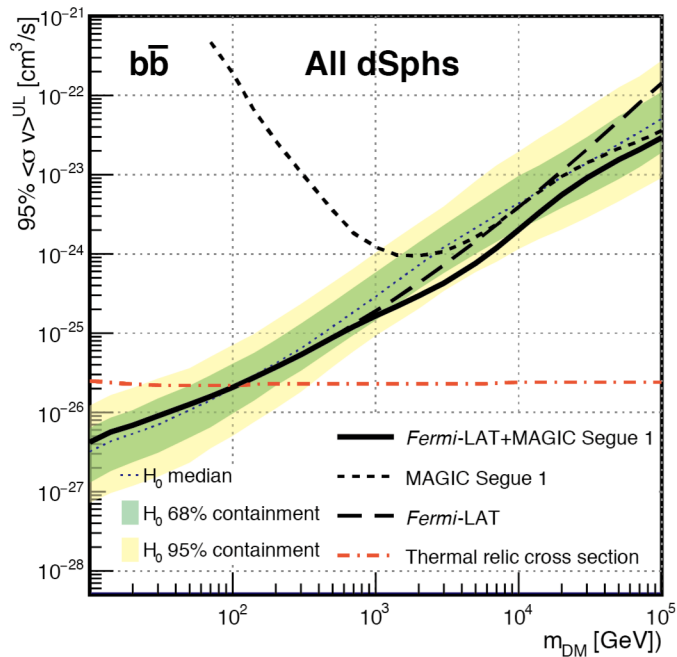
- several degree,  $10^{5-6}\text{m}^2$ ,  $\sim 20\%$  energy resolution
- VERITAS : 4x12m telescopes, Crab  $36\sigma/\sqrt{\text{hr}} = 1\%\text{Crab}$  in 35h
- MAGIC : 2x17m telescope,  $19\sigma/\sqrt{\text{hr}} = 2.2\%\text{Crab}$  in 50h
- HESS : 4x12m + 28m telescopes,  $43\sigma/\sqrt{\text{hr}}$

### ■ > 10 TeV : ground-based Water Cherenkov

- HAWC : 2/3-sky, effective area similar to ACT but worse resolution

Spectra from Cembranos et al. (PRD 83:083507)

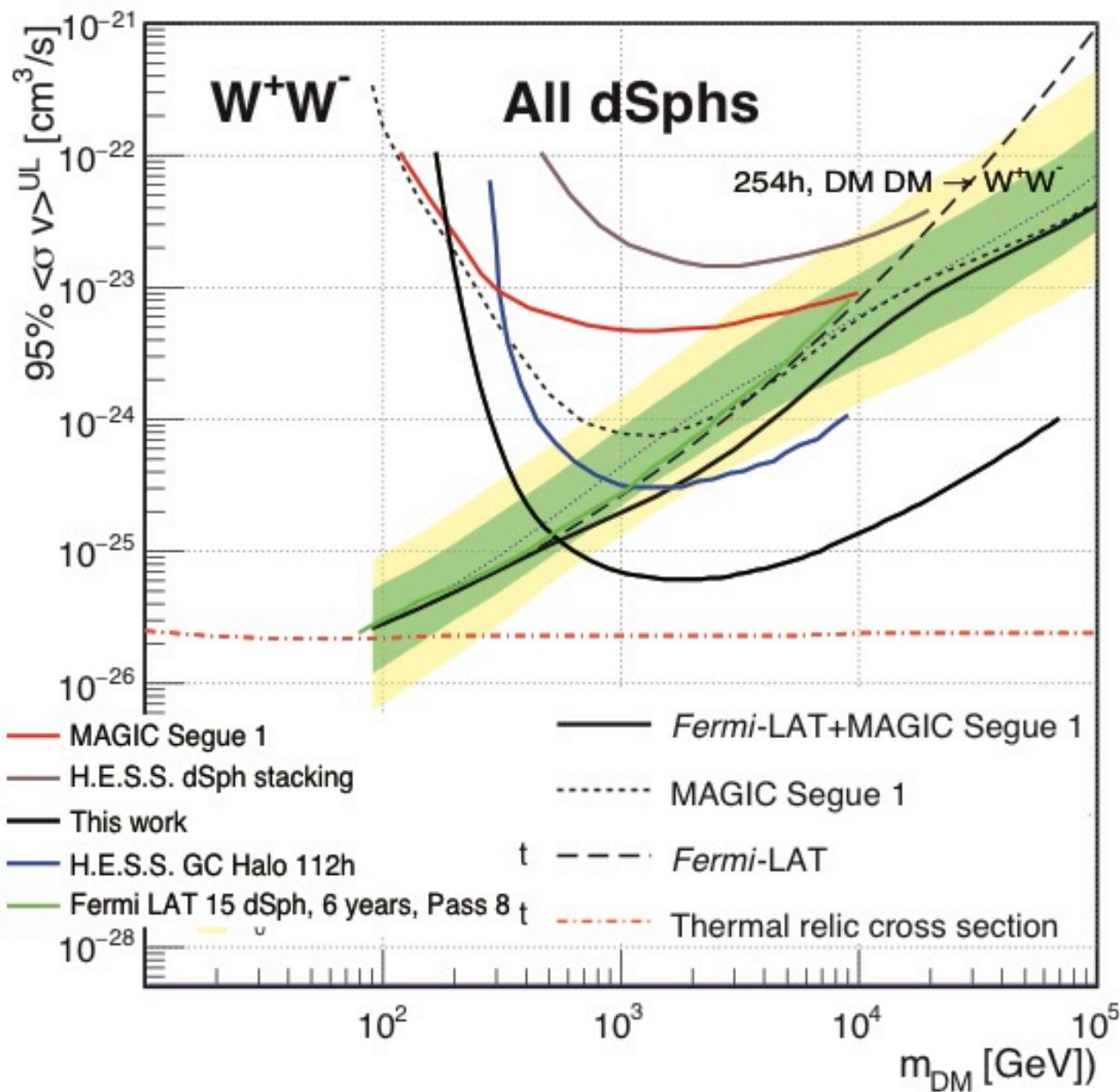
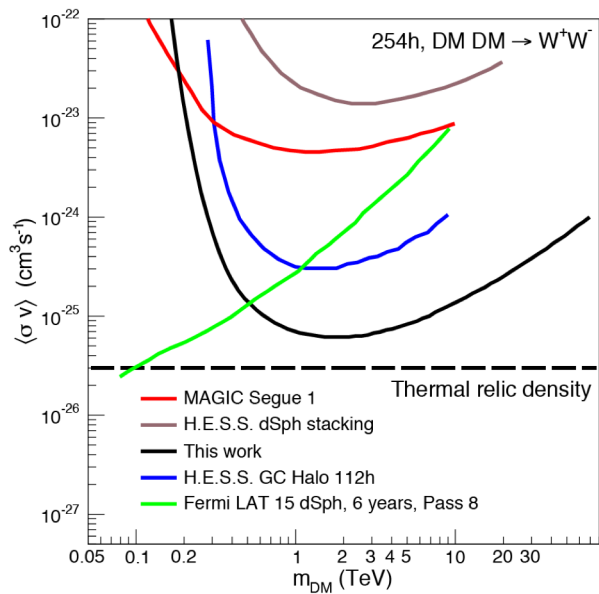
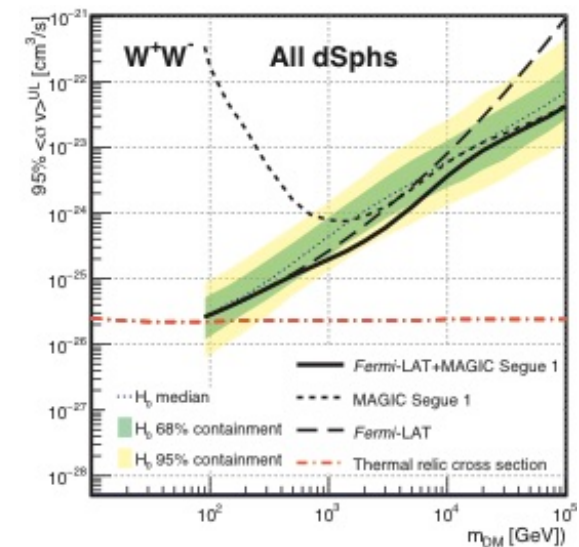




MAGIC:  
158 hr of Segue 1

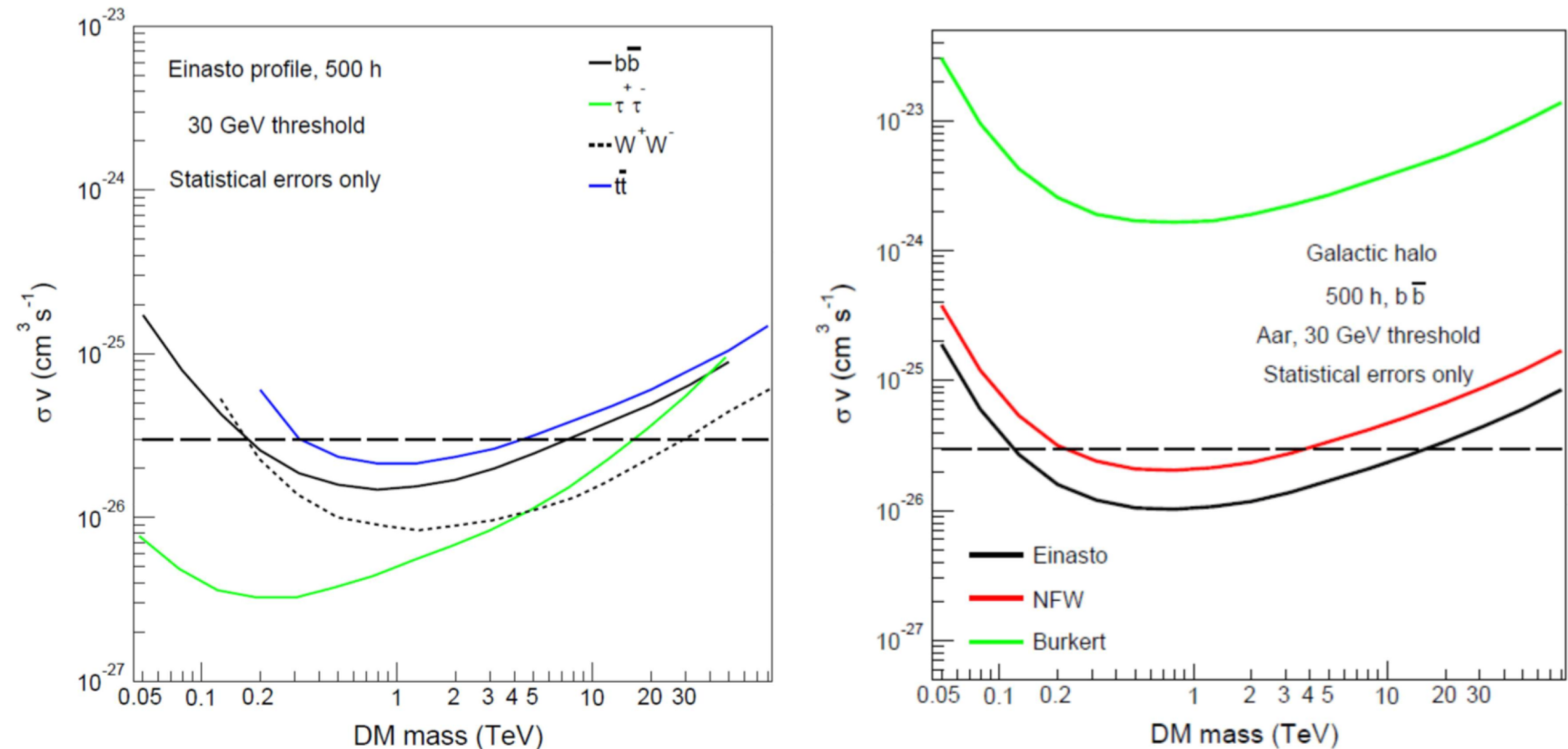
Fermi-LAT:  
6 yr of 15 dSph  
(incl. Segue 1)

DM profile: NFW



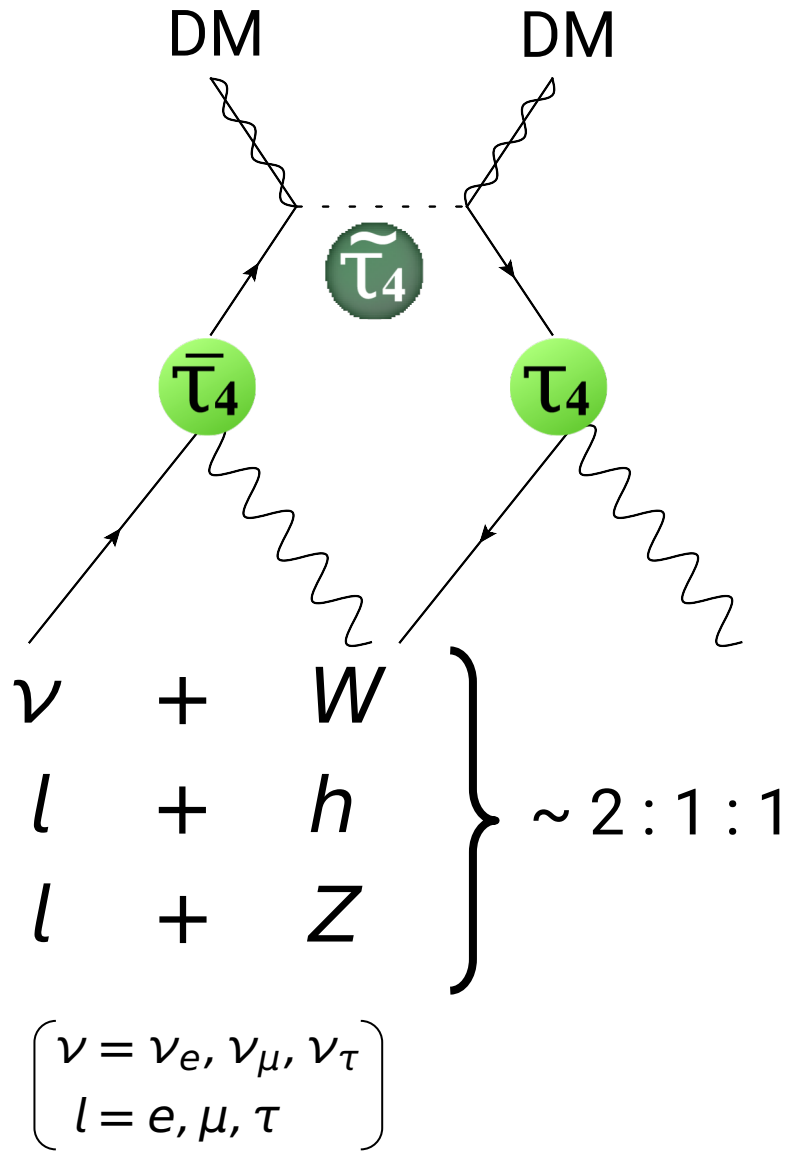
HESS assumes Einasto profile; for NFW weaker by factor  $\sim 2$ .



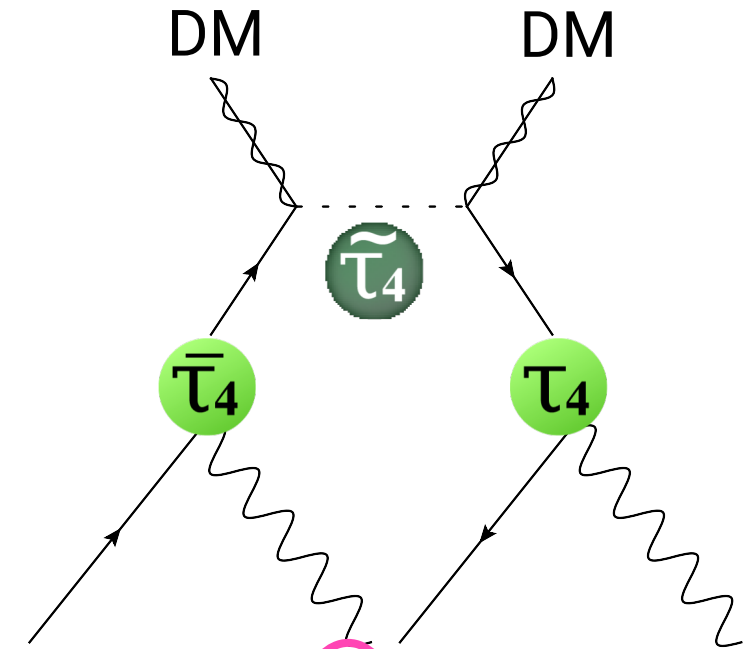


**Figure 1. Left:** Sensitivity for  $\sigma v$  from observation on the Galactic Halo with Einasto dark matter profile and for different annihilation modes as indicated. **Right:** for cuspy (NFW, Einasto) and cored (Burkert) dark matter halo profiles. For both plots only statistical errors are taken into account. The dashed horizontal lines indicate the level of the thermal cross-section of  $3 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$ .

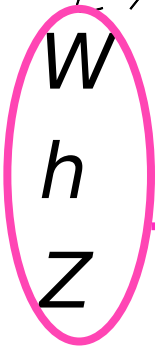
■ DM indirect detection by Gamma-ray observation



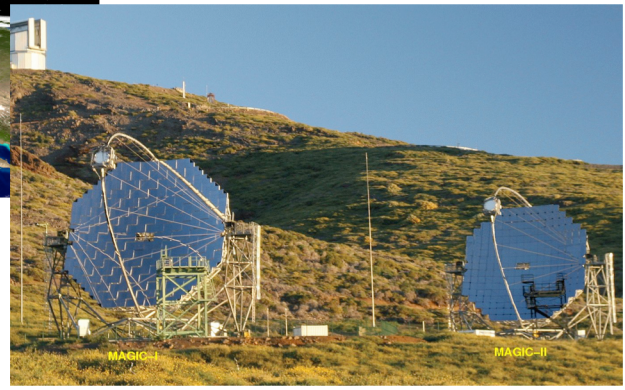
## DM indirect detection by Gamma-ray observation



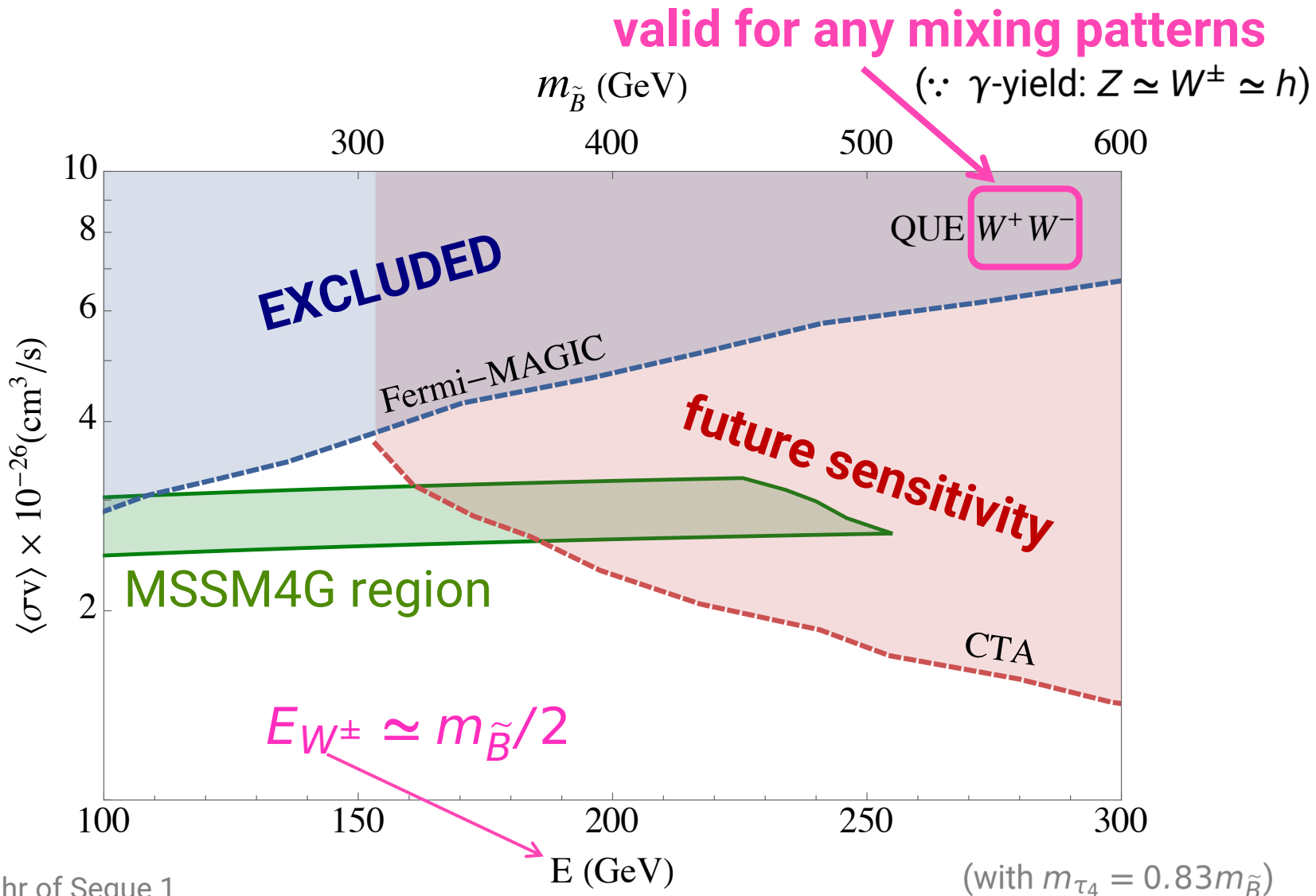
$\nu$  +  $W$   
 $l$  +  $h$   
 $l$  +  $Z$



$\left( \begin{array}{l} \nu = \nu_e, \nu_\mu, \nu_\tau \\ l = e, \mu, \tau \end{array} \right)$



- Fermi-LAT (satellite)
- MAGIC (Air Cherenkov telescope)
- CTA (future A. C. Telescope)



MAGIC: 158 hr of Segue 1

Fermi-LAT: 6 yr of 15 dSph (incl. Segue 1)

DM profile: NFW

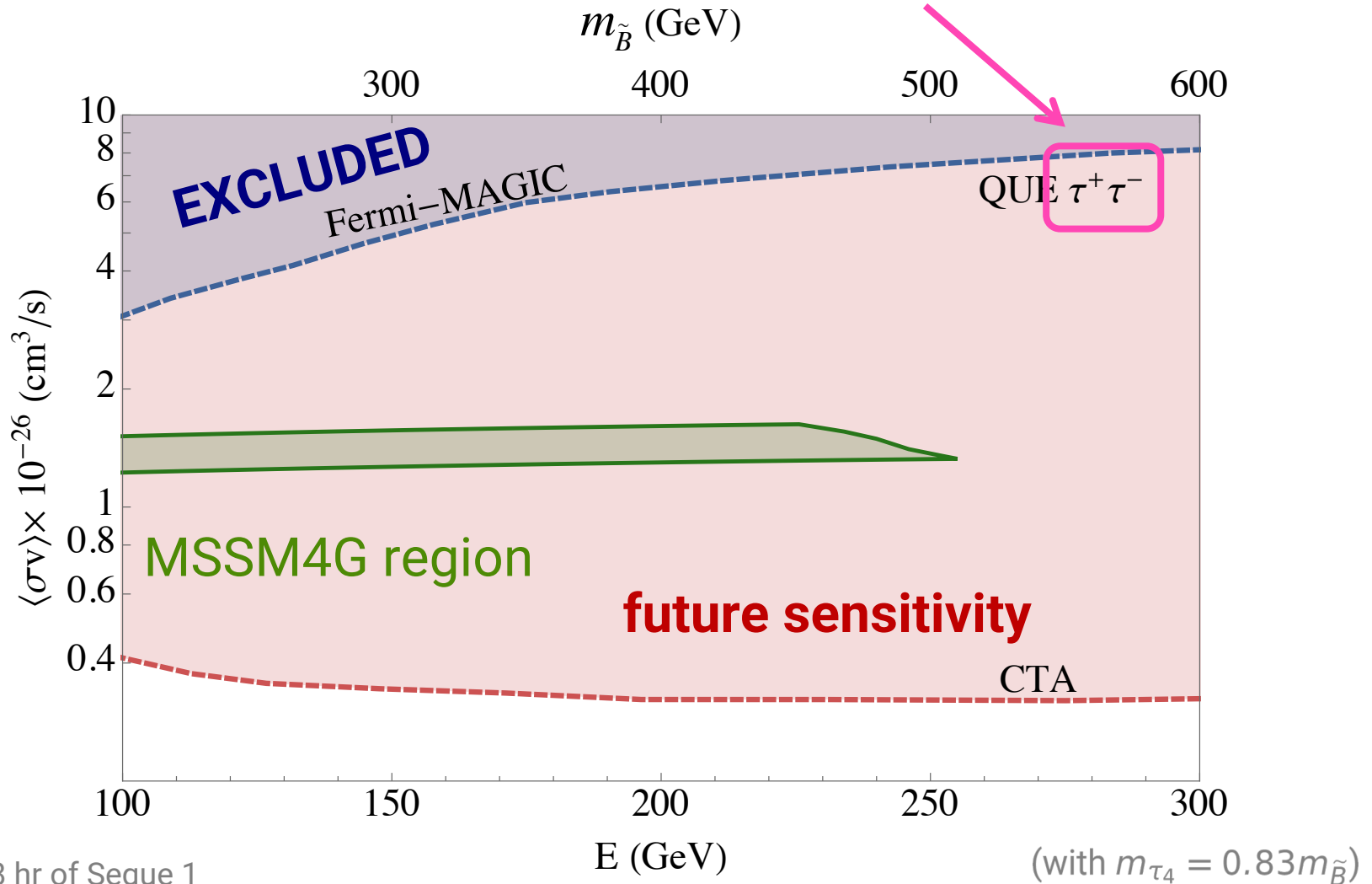
Fermi-LAT dominates MAGIC in almost all  $E$ -range.

CTA prospect : 500hr of Milky Way

DM profile: Einasto

No syst. unc. (stat only)

if 4G lepton decays to tau-lepton



MAGIC: 158 hr of Segue 1

Fermi-LAT: 6 yr of 15 dSph (incl. Segue 1)

DM profile: NFW

Fermi-LAT dominates MAGIC in almost all  $E$ -range.

CTA prospect : 500hr of Milky Way

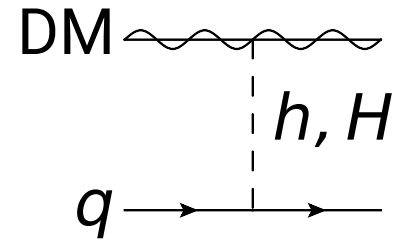
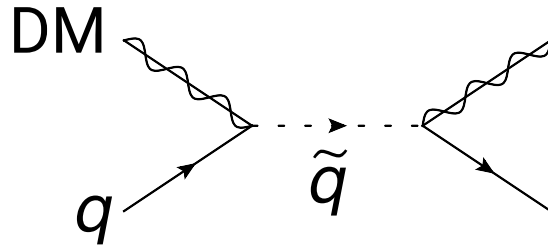
DM profile: Einasto

No syst. unc. (stat only)

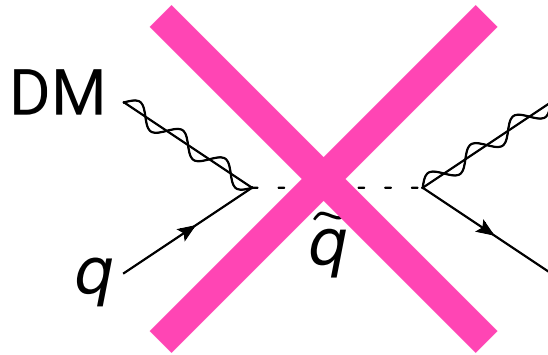
# SI direct detection constraints

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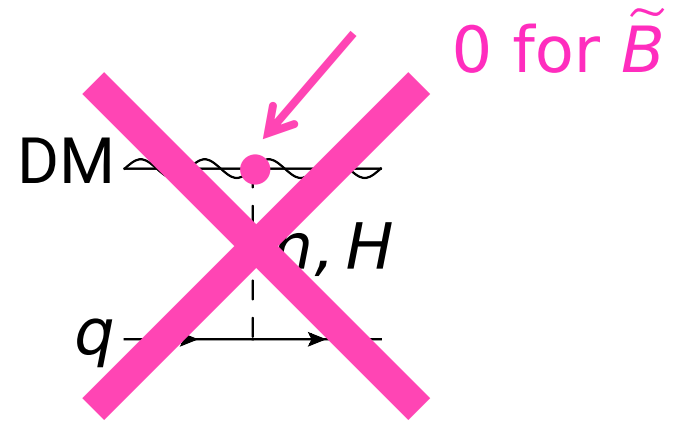
- spin-independent cross section  $\sigma_{\text{SI}}(N\tilde{\chi}_1^0 \rightarrow N\tilde{\chi}_1^0)$



- spin-independent cross section  $\sigma_{\text{SI}}(N\tilde{\chi}_1^0 \rightarrow N\tilde{\chi}_1^0)$

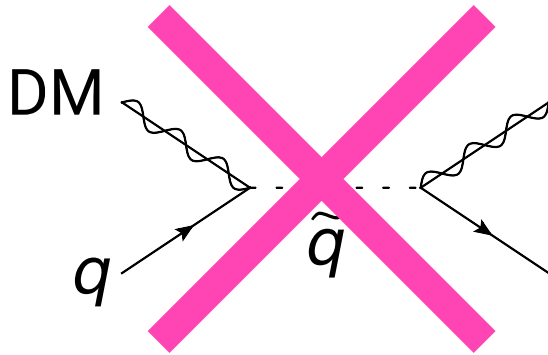


if  $\tilde{q}$  decoupled (as we assume)

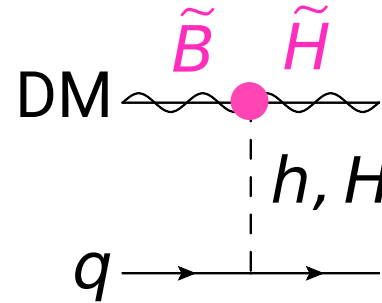




- spin-independent cross section  $\sigma_{\text{SI}}(N\tilde{\chi}_1^0 \rightarrow N\tilde{\chi}_1^0)$

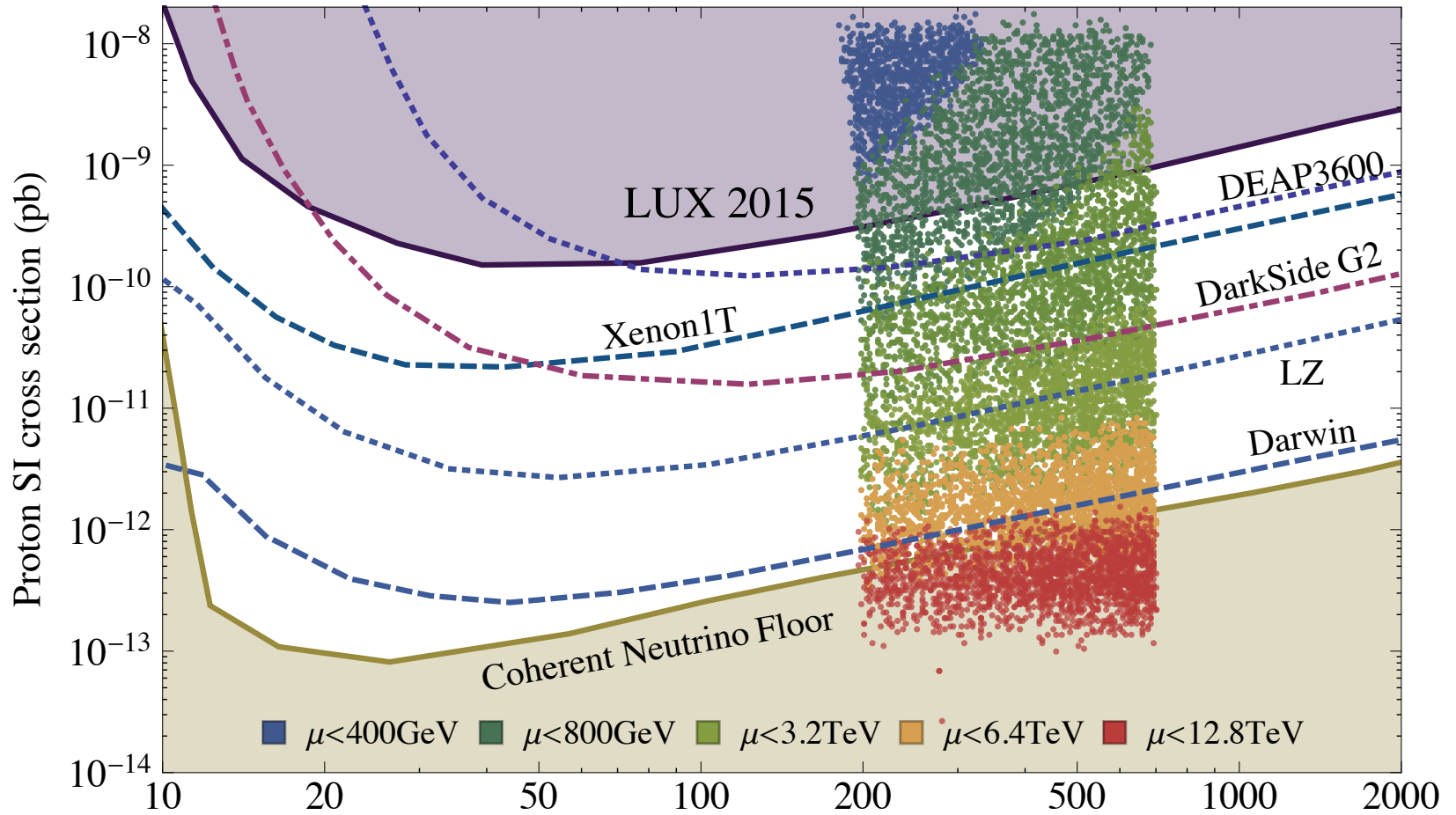


if  $\tilde{q}$  decoupled (as we assume)



$$\begin{aligned}
 \sigma_{\text{SI}} &\propto \left[ N_{41} \left( \overset{\tilde{W} \text{ in DM } (\sim 0)}{\downarrow} N_{21} - \overset{\tilde{B} \text{ in DM } (\sim 1)}{\downarrow} N_{11} \tan \theta_w \right) \frac{g^2}{4m_W m_h^2} \right]^2 \\
 &\quad \uparrow \\
 &\quad \tilde{H} \text{ in DM} \\
 &\approx \left[ \frac{M_1 m_Z s_w t_w}{\mu^2 - M_1^2 + m_Z^2 s_w^2} \frac{g^2}{4m_W m_h^2} \right]^2 \quad (M_1 \ll \mu \ll M_2, m_H)
 \end{aligned}$$

■ spin-independent cross section

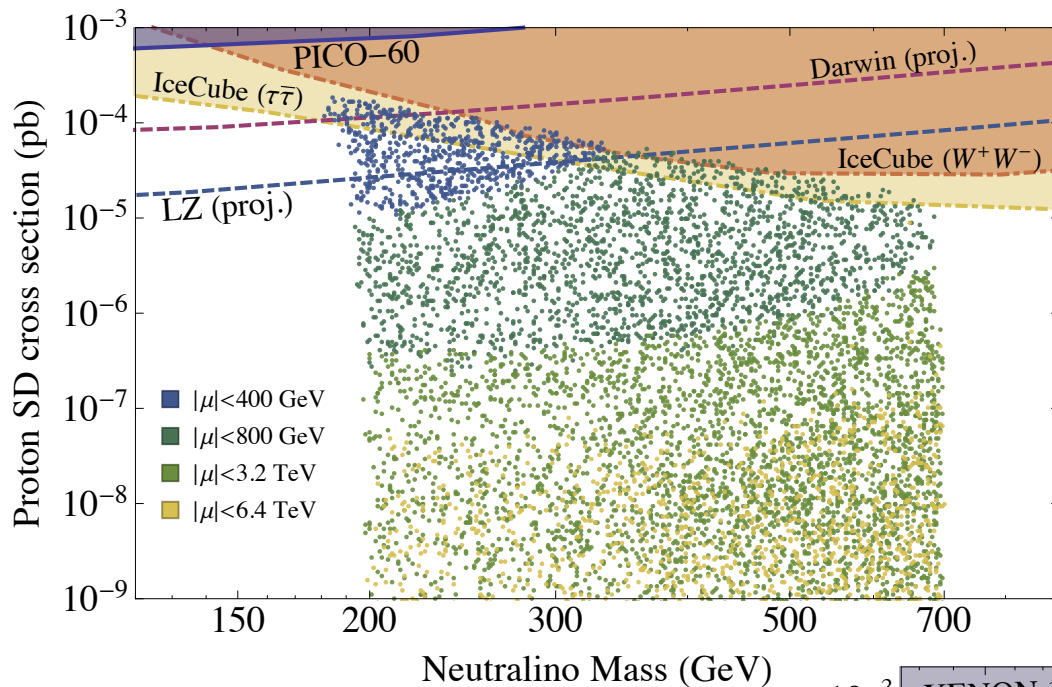


$$\approx \left[ \frac{M_1 m_Z s_w t_w}{\mu^2 - M_1^2 + m_Z^2 s_w^2} \frac{g^2}{4m_W m_h^2} \right]^2 \quad (M_1 \ll \mu \ll M_2, m_H)$$

# SD direct detection constraints

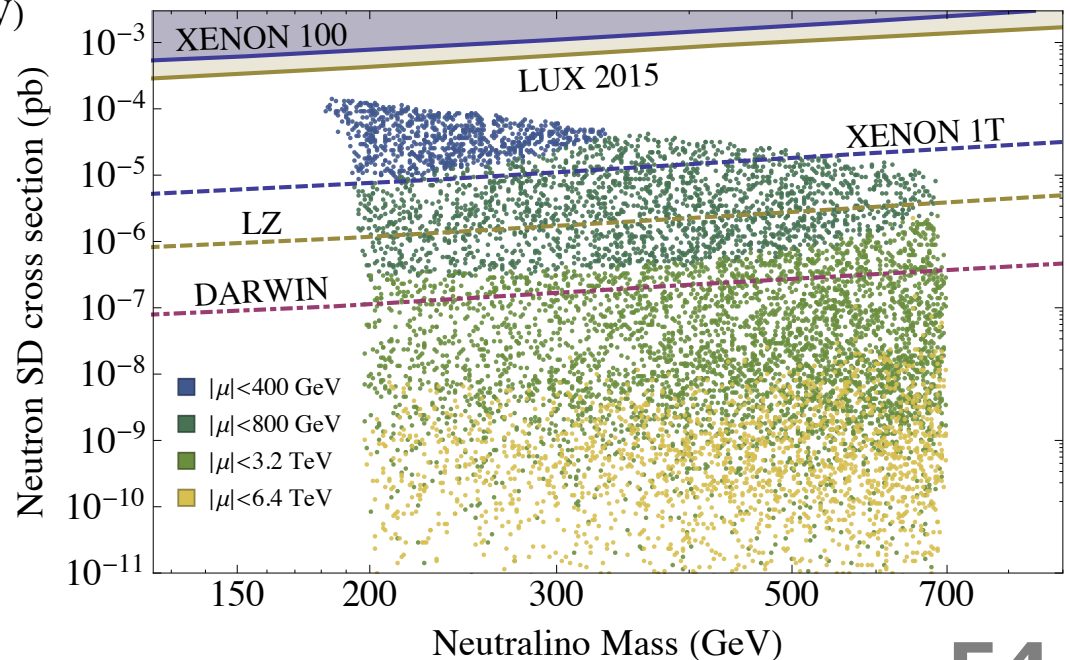
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# Spin-dependent direct detection constraints on MSSM4G scenario



## Note

DM SI/SD constraints are the same as MSSM, but the parameter space is not preferred in the MSSM because of overabundance.



# Vectorlike lepton search DATA

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**SR definition**

	$WZ(j)$	$WZ(\ell)$	$ZZ(j)$	$ZZ(\ell)$
$N_\ell$	$\geq 3$	$\geq 4$	$\geq 4$	$\geq 5$
$N_j$	$\geq 2$	$< 2$	$\geq 2$	—
$ m_{jj} - m_W $	$< 20 \text{ GeV}$	—	—	—
$ m_{jj} - m_Z $	—	—	$< 40 \text{ GeV}$	—
$\cancel{E}_T$	$> 60 \text{ GeV}$	$> 100 \text{ GeV}$	—	—
$N_{Z(\ell\ell)}$	—	—	$\geq 1$	$\geq 1$

TABLE IV: Selection flow of the background events in the vector-like lepton search. Upper bounds on the number of events in each SR,  $N_{UL}$ , are shown for three values of integrated luminosity, where systematic uncertainty of 20% as well as statistical uncertainty is included.

	background cross section [fb]				$N_{UL}$		
	di-boson	tri-boson	top	total	300 fb <sup>-1</sup>	1000 fb <sup>-1</sup>	3000 fb <sup>-1</sup>
$N_\ell \geq 3$	222	5.1	13.4	249	—	—	—
$WZ(j)^-$	0.071	0.013	0.082	0.166	25.1	70.4	200
$WZ(j)^Z$	0.643	0.071	0.183	0.898	111	359	1060
$WZ(\ell)^-$	0.014	0.025	0.017	0.056	11.9	27.4	71.1
$WZ(\ell)^Z$	< 0.001	0.005	0.003	0.008	5.1	7.9	14.5
$ZZ(j)^0$	0.194	0.016	0.058	0.268	37.2	111	321
$ZZ(j)^J$	0.064	0.007	0.022	0.093	16.4	41.8	114
$ZZ(j)^L$	0.182	0.012	0.024	0.218	31.2	91.7	263
$ZZ(j)^Z$	0.020	0.004	0.019	0.043	10.2	22.2	55.7
$ZZ(j)^{JL}$	0.060	0.005	0.009	0.075	14.2	35.3	94.3
$ZZ(j)^{JZ}$	0.008	0.001	0.008	0.017	6.7	11.9	25.6
$ZZ(j)^{LZ}$	0.020	0.004	0.019	0.043	10.2	22.2	55.9
$ZZ(j)^{JLZ}$	0.008	0.001	0.008	0.017	6.7	11.9	25.5
$ZZ(\ell)$	< 0.001	0.005	< 0.001	0.005	4.7	6.8	11.5
$ZZ(\ell)^{<2}$	< 0.001	0.003	< 0.001	0.004	4.2	5.8	9.2
$ZZ(\ell)^{<1}$	< 0.001	0.001	< 0.001	0.001	3.6	4.5	6.3

Z-flag for  $WZ(j)$ : a Z-like  $\ell\ell$  (SFOS,  $|m_{\ell\ell} - m_Z| < 10$  GeV)

Z-flag for  $WZ(\ell)$ : a Z-like  $\ell\ell$  in 3<sup>rd</sup>-leading leptons

J-flag for  $ZZ(j)$ : a Z-like  $jj$  (10 GeV)

L-flag for  $ZZ(j)$ : a Z-like  $\ell\ell$  in 2<sup>nd</sup>-leading leptons

Z-flag for  $ZZ(j)$ : leading-lepton does NOT form Z-like pairs

$ZZ(\ell)$  divided by number of jets

TABLE V: Selection flow of the signal events in searches for the  $e$ - or  $\mu$ -mixed  $\tau_4$  in the QUE model, displayed as a signal cross section in fb. SRs marked with \*, † and ‡ are the most sensitive for exclusion at  $\mathcal{L} = 300, 1000, \text{ and } 3000 \text{ fb}^{-1}$ , respectively.

$m_\tau$ [GeV], mixing	200, $e$	200, $\mu$	300, $e$	300, $\mu$	400, $e$	400, $\mu$
total	95.7	96.0	21.2	21.2	6.76	6.74
$N_\ell \geq 3$	2.23	2.42	0.634	0.671	0.231	0.230
$WZ(j)^-$	0.018	0.022	0.020	0.024	0.011	0.012
$WZ(j)^Z$	0.049	0.063	0.034	0.036	0.014	0.014
$WZ(\ell)^Z$	0.012	0.014	0.008‡	0.008	0.003	0.004‡
$ZZ(j)^0$	0.066	0.065	0.035	0.044	0.015	0.015
$ZZ(j)^J$	0.035	0.033	0.018	0.023	0.008	0.007
$ZZ(j)^L$	0.045	0.048	0.026	0.031	0.011	0.012
$ZZ(j)^Z$	0.039*	0.042*	0.025*†	0.029†	0.010*	0.012†
$ZZ(j)^{JL}$	0.025	0.025	0.013	0.016	0.006	0.006
$ZZ(j)^{JZ}$	0.021	0.022	0.013	0.015‡	0.005	0.006
$ZZ(j)^{LZ}$	0.039	0.042	0.025	0.029*	0.010†	0.012*
$ZZ(j)^{JLZ}$	0.021	0.022	0.013	0.015	0.005	0.006
$ZZ(\ell)$	0.015†‡	0.014†‡	0.005	0.007	0.003‡	0.002
$ZZ(\ell)^{<2}$	0.010	0.009	0.003	0.004	0.002	0.001
$ZZ(\ell)^{<1}$	0.004	0.003	0.001	0.002	$8 \times 10^{-4}$	$6 \times 10^{-4}$

Z-flag for  $WZ(j)$ : a  $Z$ -like  $\ell\ell$  (SFOS,  $|m_{\ell\ell} - m_Z| < 10 \text{ GeV}$ )

Z-flag for  $WZ(\ell)$ : a  $Z$ -like  $\ell\ell$  in 3<sup>rd</sup>-leading leptons

J-flag for  $ZZ(j)$ : a  $Z$ -like  $jj$  (10 GeV)

L-flag for  $ZZ(j)$ : a  $Z$ -like  $\ell\ell$  in 2<sup>nd</sup>-leading leptons

Z-flag for  $ZZ(j)$ : leading-lepton does NOT form  $Z$ -like pairs

$ZZ(\ell)$  divided by number of jets



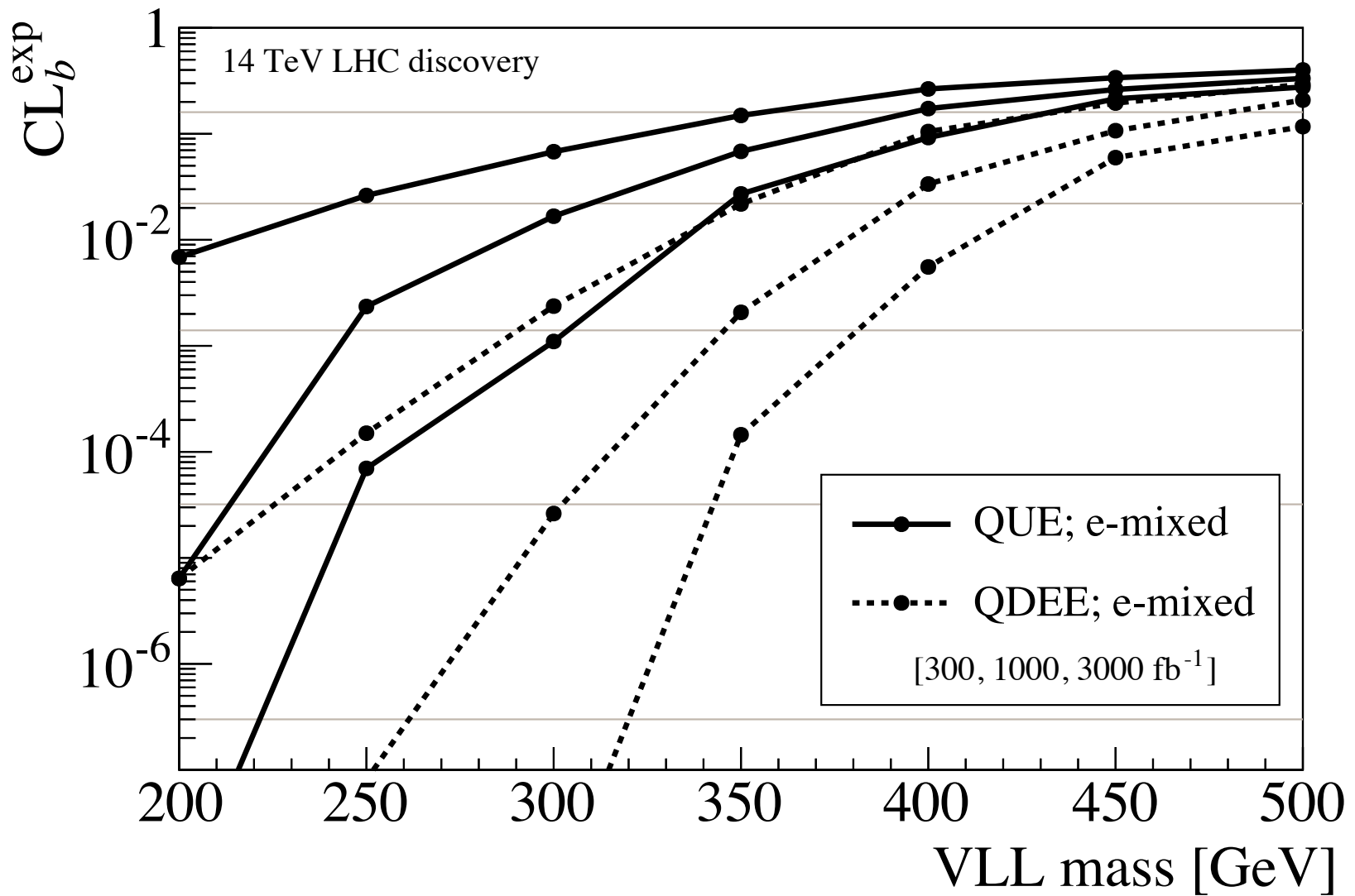
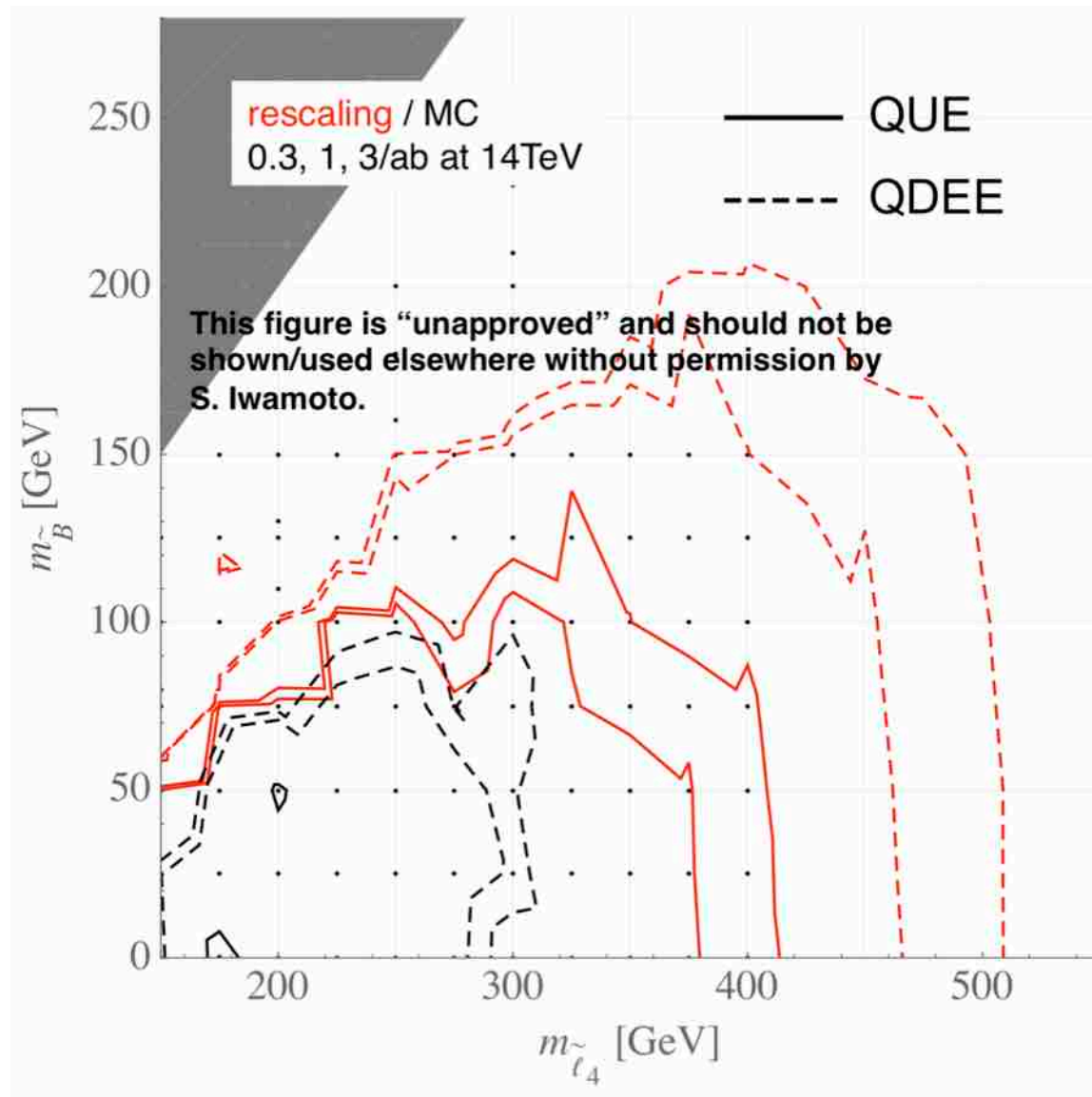


TABLE II: Future prospects for searches for vector-like leptons at the 14 TeV LHC for three values of integrated luminosity. The first table is for the QUE models, and the second for the QDEE models. We consider vector-like leptons with a mass  $m_{\ell_4} \geq 200$  GeV; the expressions  $0^{+250}$  GeV etc. show that the central value of exclusion or discovery limit is below our model points and we may achieve the limit of 250 GeV with  $1\sigma$  statistical fluctuation. In the dashed entries the upper limit is less than 200 GeV even with  $1\sigma$  statistical fluctuation. The  $CL_s$  method is used for statistical treatment, where the statistical uncertainty and a 20% systematic uncertainty for the background contribution are taken into account, while the theoretical uncertainty on the signal cross section as well as the NLO correction are not considered. See Appendix B for further details.

QUE model		300 fb <sup>-1</sup>	1000 fb <sup>-1</sup>	3000 fb <sup>-1</sup>
95% CL exclusion	<i>e</i> -mixed	240 <sup>+60</sup> GeV	310 <sup>+50</sup> <sub>-60</sub> GeV	350 <sup>+40</sup> <sub>-40</sub> GeV
	$\mu$ -mixed	270 <sup>+50</sup> GeV	330 <sup>+40</sup> <sub>-60</sub> GeV	370 <sup>+40</sup> <sub>-40</sub> GeV
3 $\sigma$ discovery	<i>e</i> -mixed	0 <sup>+250</sup> GeV	250 <sup>+60</sup> <sub>-40</sub> GeV	300 <sup>+50</sup> <sub>-50</sub> GeV
	$\mu$ -mixed	0 <sup>+280</sup> GeV	260 <sup>+70</sup> <sub>-60</sub> GeV	320 <sup>+50</sup> <sub>-40</sub> GeV
5 $\sigma$ discovery	<i>e</i> -mixed	—	0 <sup>+210</sup> GeV	220 <sup>+20</sup> <sub>-20</sub> GeV
	$\mu$ -mixed	—	0 <sup>+210</sup> GeV	240 <sup>+20</sup> <sub>-20</sub> GeV

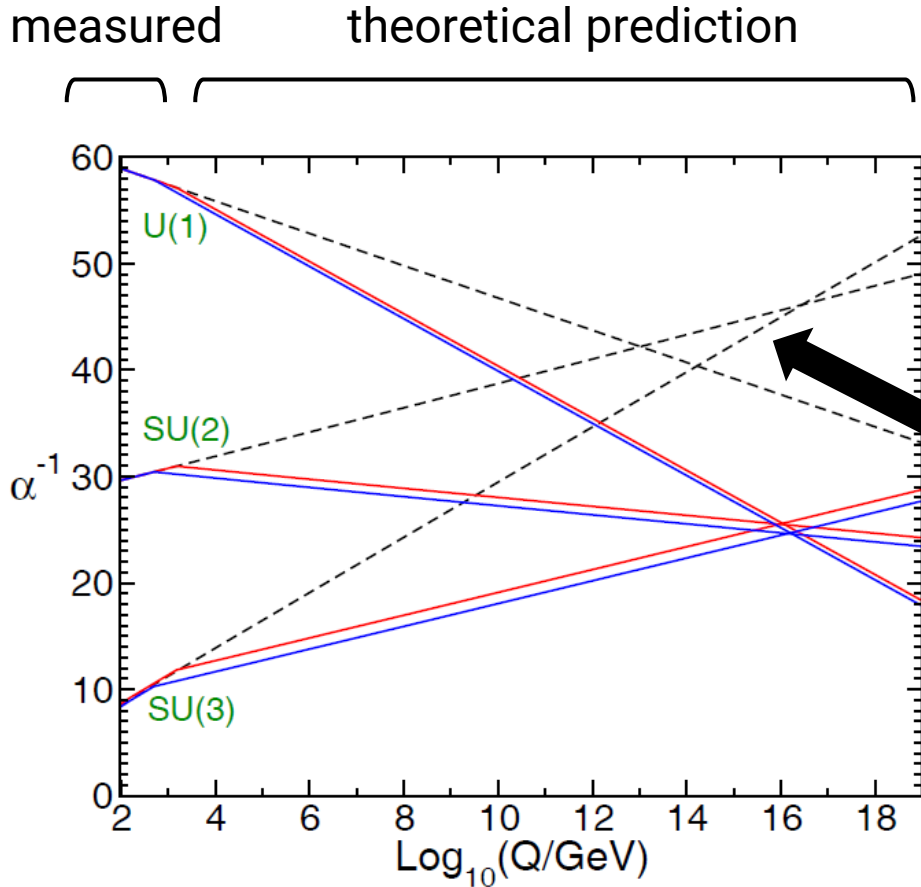
QDEE model		300 fb <sup>-1</sup>	1000 fb <sup>-1</sup>	3000 fb <sup>-1</sup>
95% CL exclusion	<i>e</i> -mixed	350 <sup>+40</sup> <sub>-50</sub> GeV	390 <sup>+40</sup> <sub>-40</sub> GeV	430 <sup>+40</sup> <sub>-40</sub> GeV
	$\mu$ -mixed	360 <sup>+40</sup> <sub>-40</sub> GeV	400 <sup>+40</sup> <sub>-40</sub> GeV	440 <sup>+40</sup> <sub>-40</sub> GeV
3 $\sigma$ discovery	<i>e</i> -mixed	290 <sup>+60</sup> <sub>-70</sub> GeV	340 <sup>+60</sup> <sub>-40</sub> GeV	380 <sup>+50</sup> <sub>-40</sub> GeV
	$\mu$ -mixed	310 <sup>+60</sup> <sub>-50</sub> GeV	360 <sup>+40</sup> <sub>-30</sub> GeV	400 <sup>+40</sup> <sub>-30</sub> GeV
5 $\sigma$ discovery	<i>e</i> -mixed	0 <sup>+200</sup> GeV	260 <sup>+40</sup> <sub>-50</sub> GeV	310 <sup>+20</sup> <sub>-30</sub> GeV
	$\mu$ -mixed	0 <sup>+260</sup> GeV	280 <sup>+30</sup> <sub>-30</sub> GeV	320 <sup>+40</sup> <sub>-20</sub> GeV



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# Gauge coupling unification

- SM  $\ni$  3 forces : U(1), SU(2), SU(3) [Why three?]



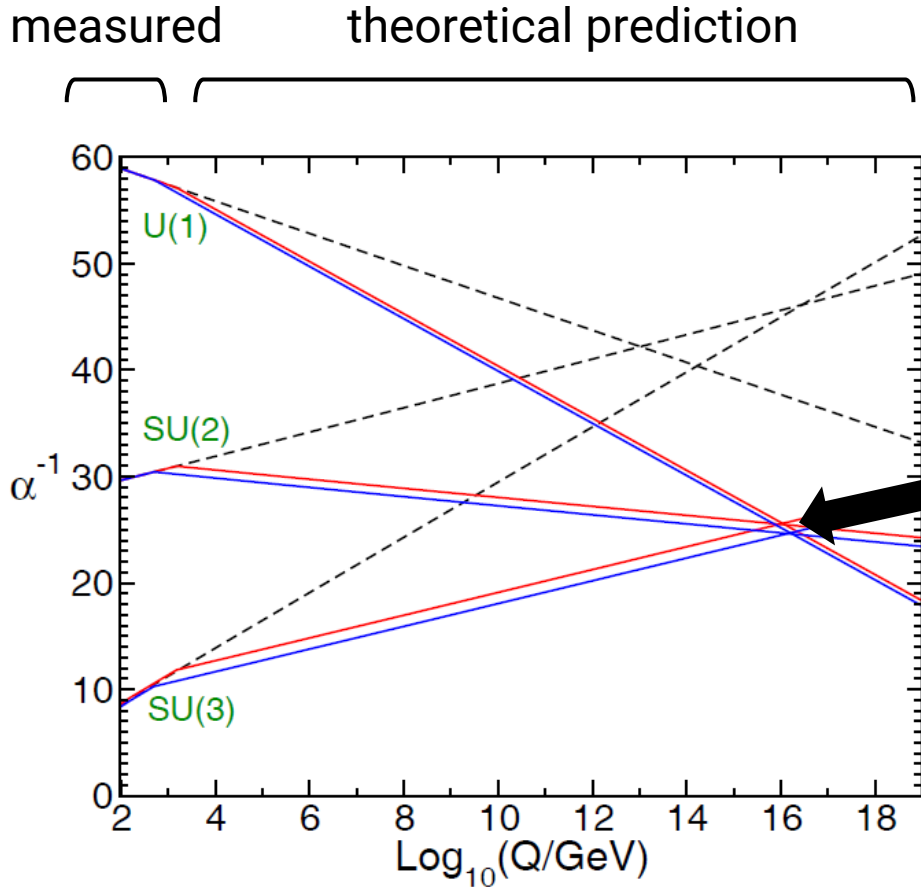
## Gauge coupling unification

	mass $\rightarrow$ $\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge $\rightarrow$ 2/3	u	c	t	g	H
spin $\rightarrow$ 1/2	up	charm	top	gluon	Higgs boson
	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	0
-1/3	d	s	b	$\gamma$	0
1/2	down	strange	bottom	photon	0
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	0	$91.2 \text{ GeV}/c^2$
-1	e	$\mu$	$\tau$	Z	0
1/2	electron	muon	tau	Z boson	1
	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	0	$80.4 \text{ GeV}/c^2$
0	$\nu_e$	$\nu_\mu$	$\nu_\tau$	W	$\pm 1$
1/2	electron neutrino	muon neutrino	tau neutrino	W boson	1

Figure from S. P. Martin, *A Supersymmetry Primer*, [hep-ph/9709356](http://hep-ph/9709356)

# Gauge coupling unification

- SM  $\ni$  3 forces : U(1), SU(2), SU(3) [Why three?]



## Gauge coupling unification

Particle	mass $\rightarrow$	charge $\rightarrow$	spin
<b>QUARKS</b>			
up ( $u$ )	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$
charm ( $c$ )	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$
top ( $t$ )	$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$
down ( $d$ )	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$
strange ( $s$ )	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$
bottom ( $b$ )	$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$
<b>LEPTONS</b>			
electron ( $e$ )	$0.511 \text{ MeV}/c^2$	$-1$	$1/2$
muon ( $\mu$ )	$105.7 \text{ MeV}/c^2$	$-1$	$1/2$
tau ( $\tau$ )	$1.777 \text{ GeV}/c^2$	$-1$	$1/2$
electron neutrino ( $\nu_e$ )	$< 2.2 \text{ eV}/c^2$	$0$	$1/2$
muon neutrino ( $\nu_\mu$ )	$< 0.17 \text{ MeV}/c^2$	$0$	$1/2$
tau neutrino ( $\nu_\tau$ )	$< 15.5 \text{ MeV}/c^2$	$0$	$1/2$
<b>GAUGE BOSONS</b>			
gluon ( $g$ )	$0$	$0$	$1$
photon ( $\gamma$ )	$0$	$0$	$1$
Z boson	$91.2 \text{ GeV}/c^2$	$0$	$1$
W boson	$80.4 \text{ GeV}/c^2$	$\pm 1$	$1$
Higgs bosons ( $H$ )	$\approx 126 \text{ GeV}/c^2$	$0$	$0$

Figure from S. P. Martin, *A Supersymmetry Primer*, [hep-ph/9709356](http://hep-ph/9709356)