

# SUSY model for muon $g-2$ anomaly and dark matter, and its implications

Norimi Yokozaki (Tohoku Univ.)

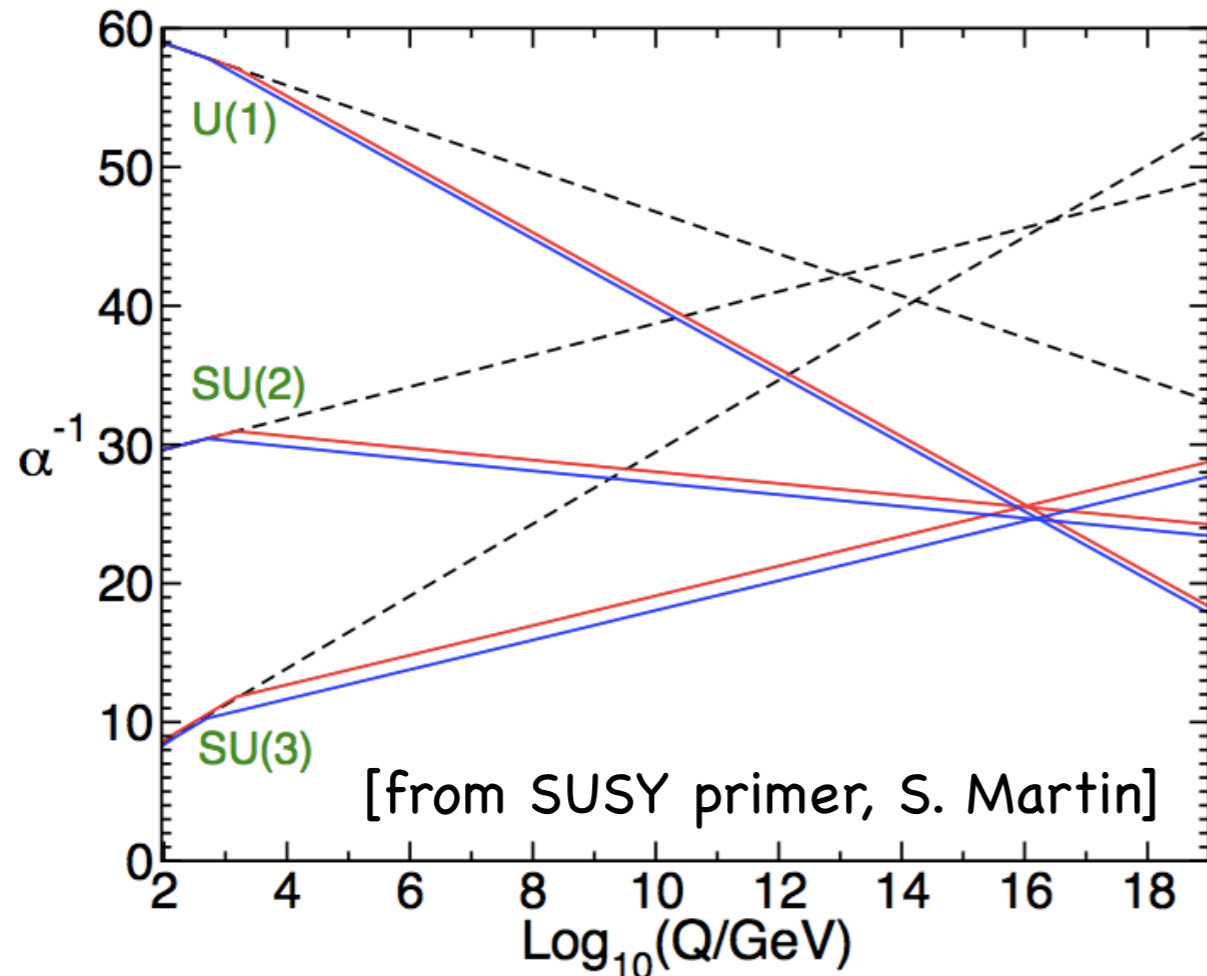
Based on

hopefully

P. Cox, C. Han, T. Yanagida and N.Y. (arXiv:1811.xxxxx)

R. Nagai and N.Y. in preparation

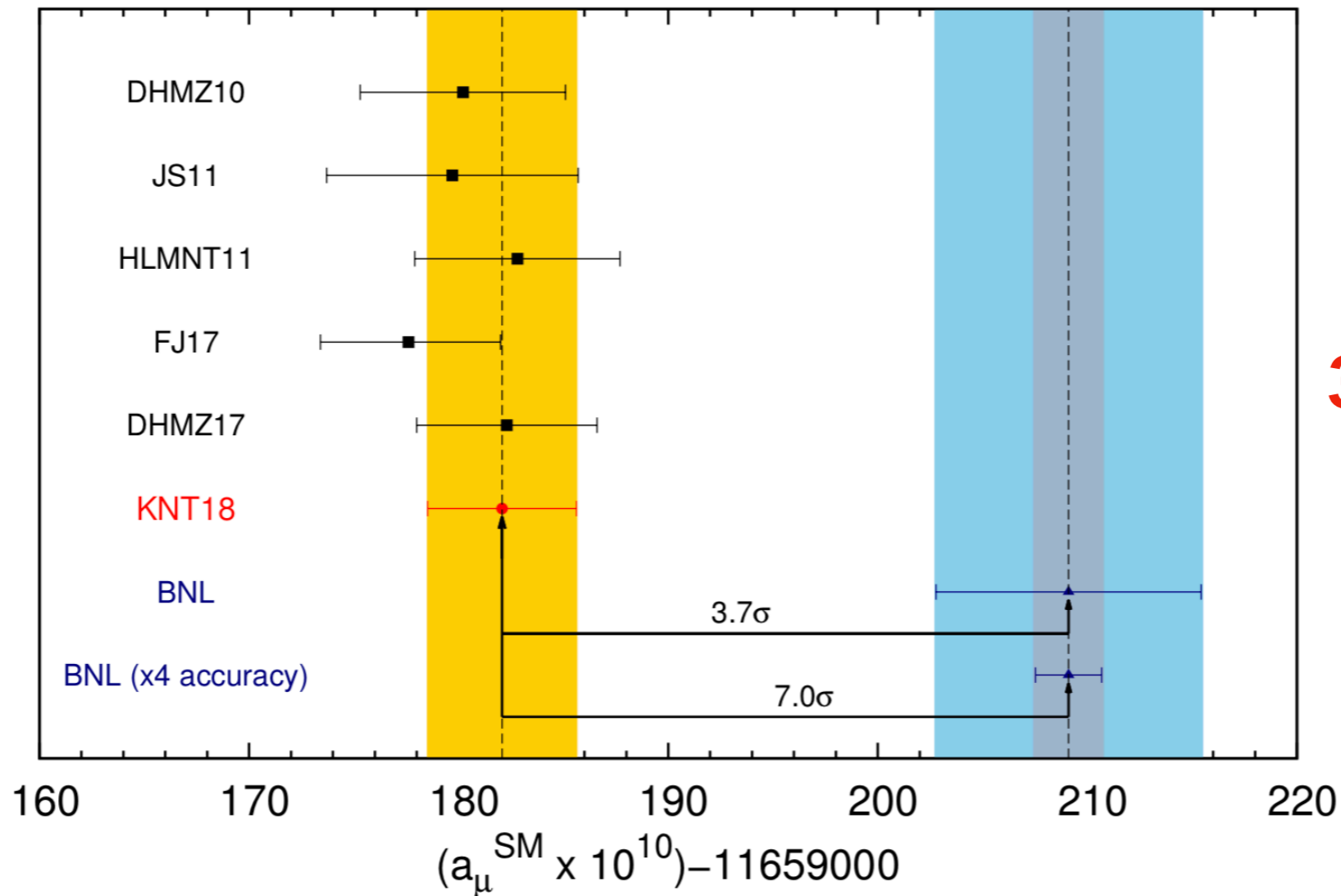
# Supersymmetry



- Gauge coupling unification  
→ Grand Unified Theory

- Absence of the quadratic divergence in the scalar potential (Higgs, PQ-breaking scalar, inflaton ...)
- Candidates for dark matter (neutralino, gravitino)
- There also exists an experimental motivation

# Muon $g-2$ anomaly



**3.7  $\sigma$  deviation**

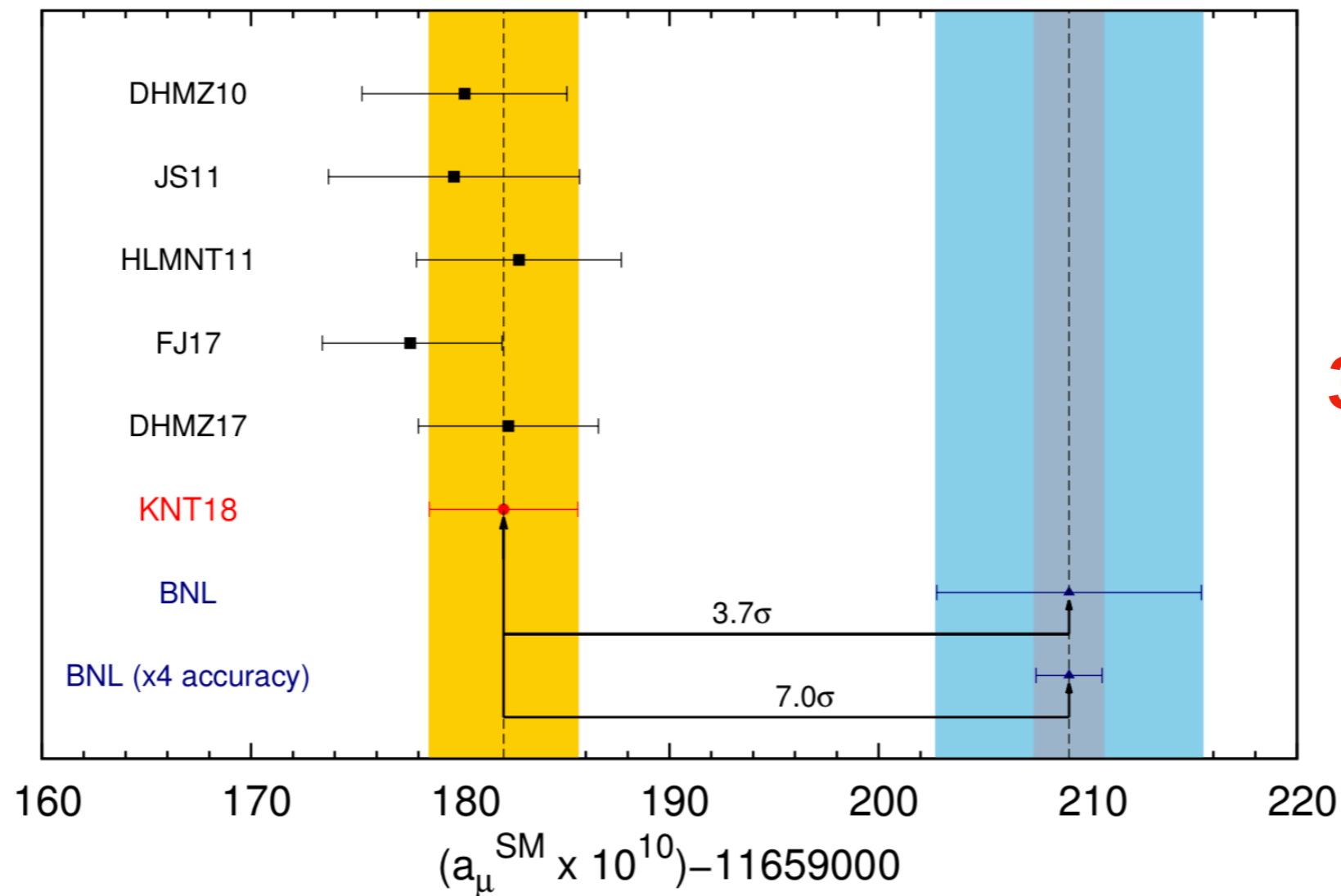
[Keshavarzi, Nomura, Teubner, 2018]

$$\mathcal{L} = \frac{e}{4m_\mu} (a_\mu)^{\text{NP}} \bar{\mu} \sigma_{\alpha\beta} \mu F^{\alpha\beta}$$

$(a_\mu)^{\text{NP}} \approx 2 \times 10^{-9}$  is required

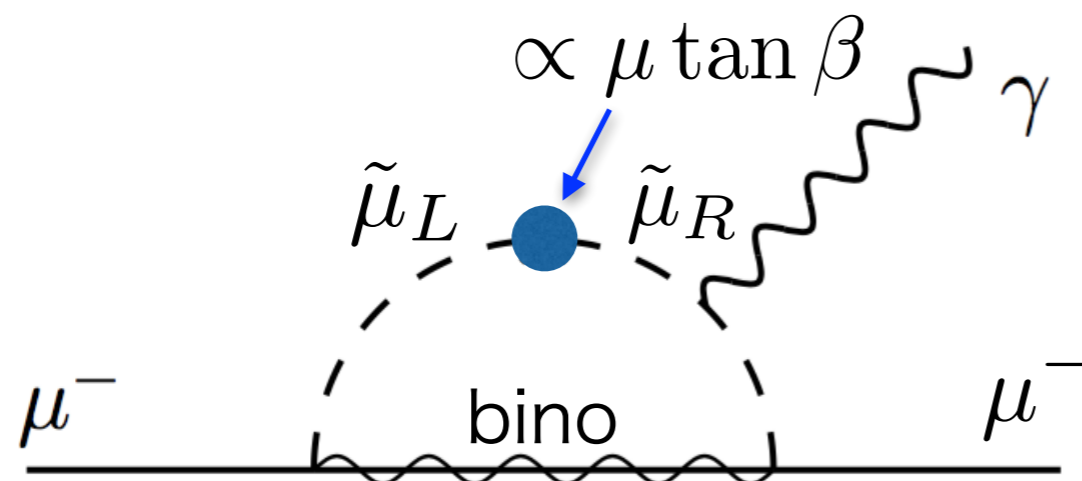
(similar to the size of W-boson contribution)

# Muon $g-2$ anomaly



**3.7  $\sigma$  deviation**

[Keshavarzi, Nomura, Teubner, 2018]

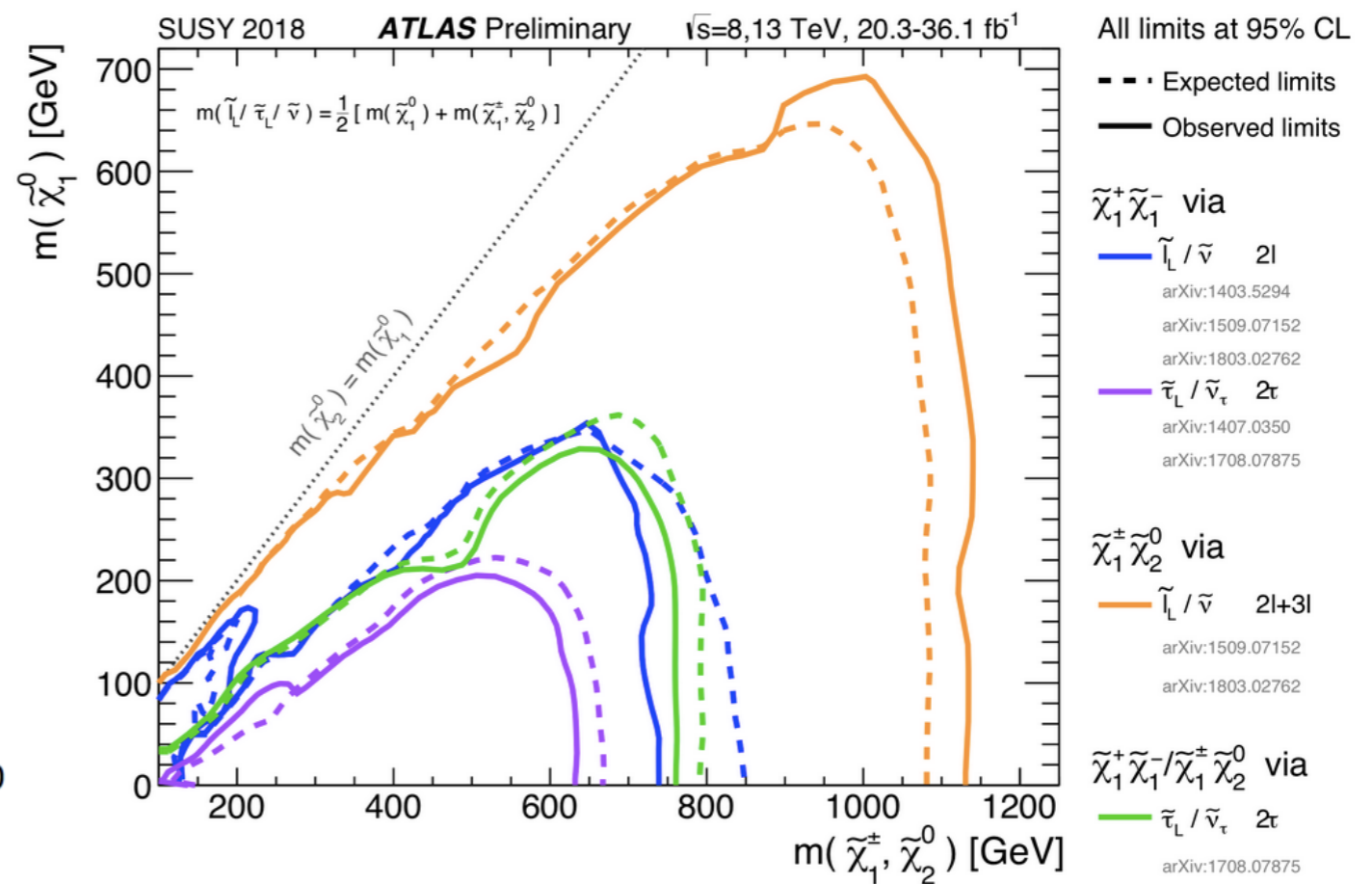
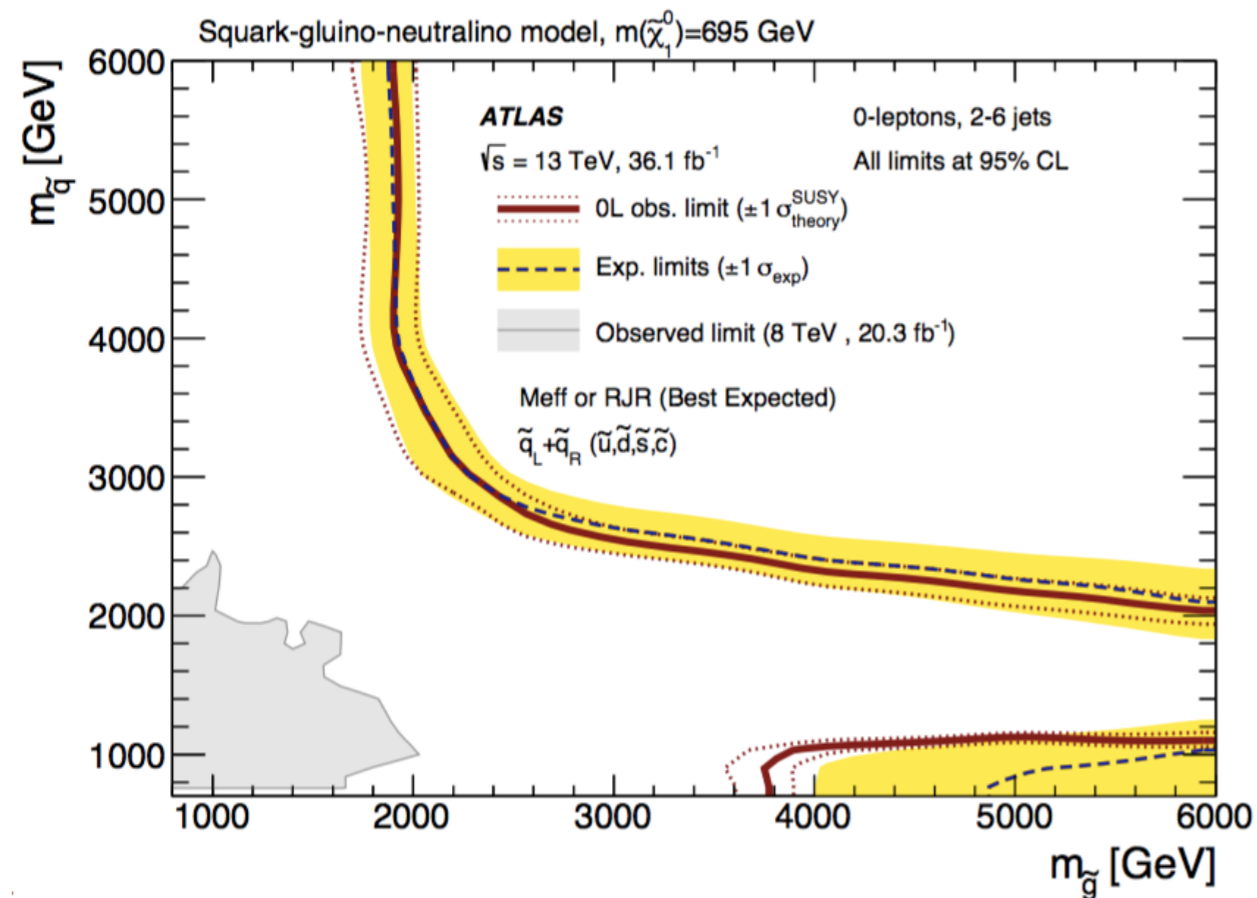


Smuons and neutralino/  
chargino are required to be  
 $O(100)\text{GeV}$

[Lopez, Nanopoulos and Wang, 1994;  
Chattopadhyay and Nath, 1996;  
Moroi, 1996]

# Difficulties

- LHC SUSY searches
  - Squarks and gluino should be heavier than  $\sim 2.5$  TeV
  - EW sector is also constrained quite severely



# Difficulties

- LHC SUSY searches
  - Squarks and gluino should be heavier than  $\sim 2.5$  TeV
  - EW sector is also constrained quite severely
- Higgs boson mass of 125 GeV
  - Stop masses are  $\sim 10$  TeV
- No signal in direct detection experiments of dark matter
  - Higgsino is heavy, i.e.  $\mu$  is large
- Vacuum instability caused by large  $\mu \tan \beta$  in the stau-Higgs potential
  - Staus need to be much heavier than smuons
- SUSY flavor problem ( $\mu \rightarrow e \gamma$ , K meson mixing  $\dots$ )

- So we want a simple model which predicts a spectrum where 3rd generation sfermions are much heavier than 1st/2nd generation sfermions **without inducing large FCNC**



Higgs(+gaugino) mediation

[Yin, Yokozaki, 2016; Yanagida, Yin, Yokozaki, 2016, 2018]

# Higgs mediation

Because of flavor constraints, we start with the sequestered Kahler potential

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + Q_i^\dagger Q_i}{3M_P^2} \right]$$

Z: SUSY breaking field [Randall, Sundrum, 1999]

$Q_i$ : MSSM field

Then, sfermions are massless

**FCNC is suppressed!**

But, of course massless sfermions are ruled out!

(If there are anomaly mediation effects, slepton masses are tachyonic)



We can couple Higgs doublets to SUSY breaking field without worrying about FCNC

$$K = -3M_P^2 \ln \left[ 1 - \frac{f(Z, Z^\dagger) + Q_i^\dagger Q_i + \Delta K'}{3M_P^2} \right]$$

$$\Delta K' = d' \frac{|Z|^2}{M_P^2} (H_u^\dagger H_u + H_d^\dagger H_d) - c_b \frac{|Z|^2}{M_P^2} H_u H_d + h.c.$$

$d'$  is assumed to be positive **so that Higgs soft masses are tachyonic**

**This is an important assumption**

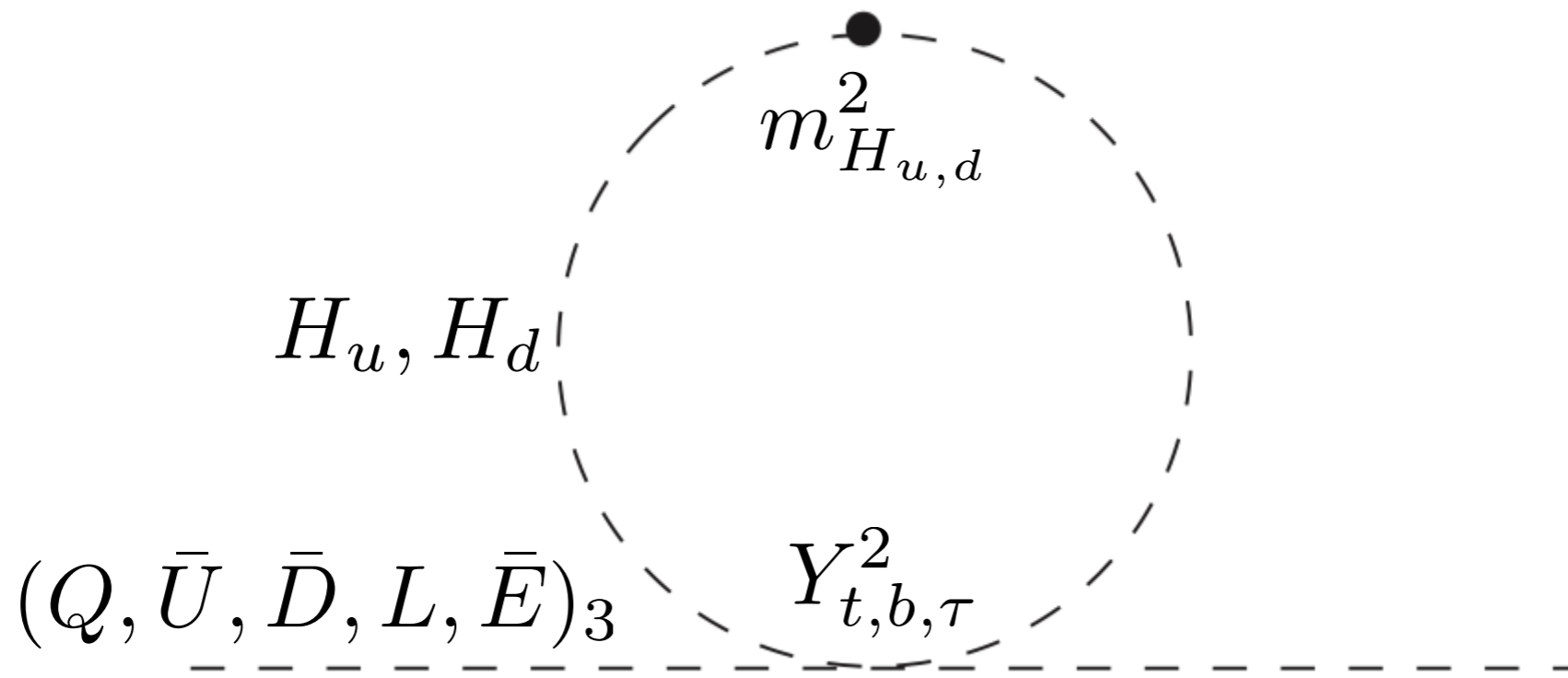
$$m_{H_u}^2 = m_{H_d}^2 = -d' \frac{|F_Z|^2}{M_P^2} = -3d' \left( \frac{\partial^2 K}{\partial Z \partial Z^\dagger} \right)^{-1} m_{3/2}^2$$

$\mathcal{O}(10^8 - 10^9) \text{ GeV}^2$

and the Higgs B-term

(D-flat direction is still safe with  $|\mu|^2$  term)

# Higgs loops



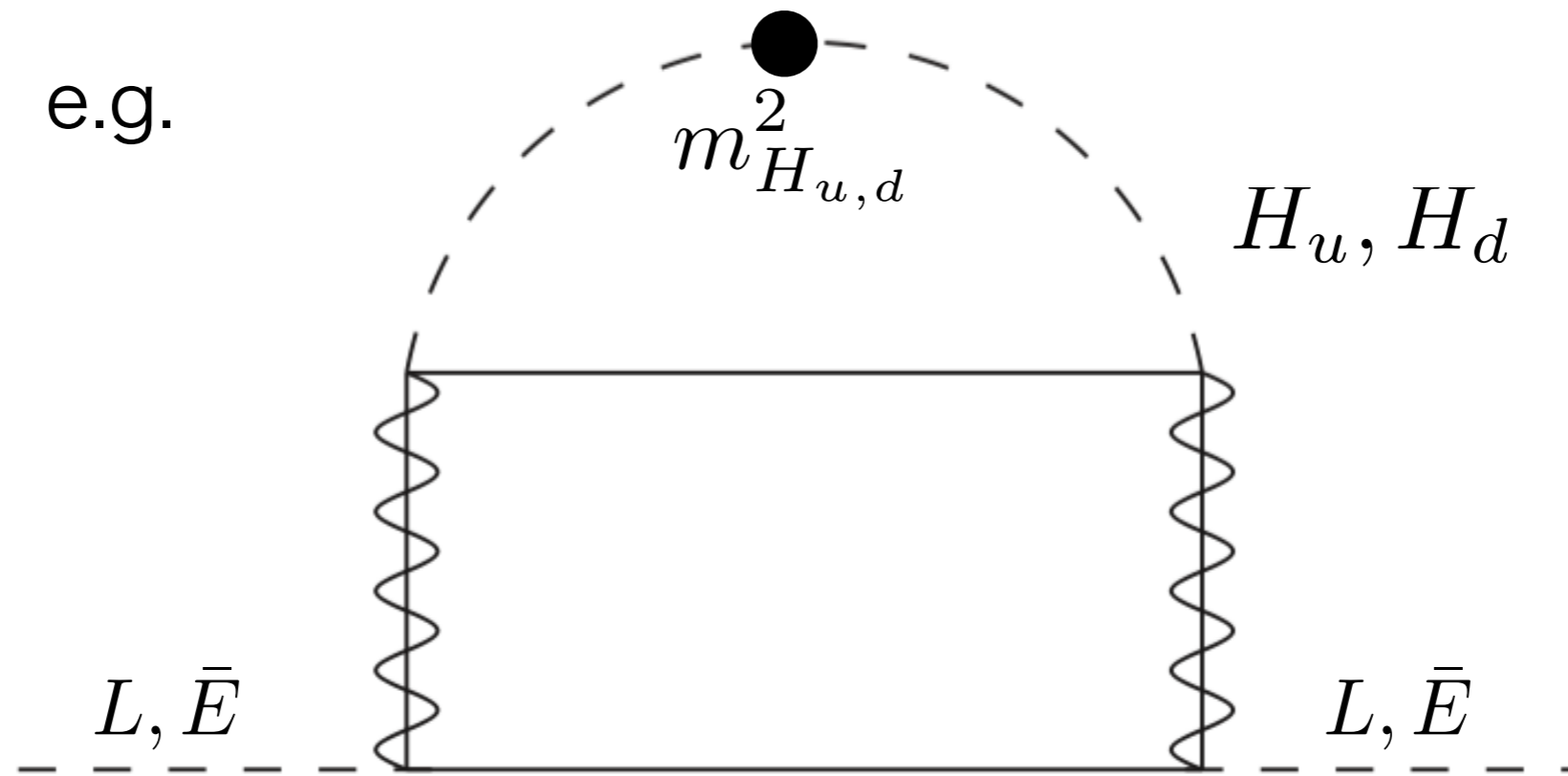
One-loop diagrams induce large positive squared masses for the third generation sfermions

$$\frac{dm_3^2}{d \ln \mu_R} \ni \frac{1}{16\pi^2} (C_t Y_t^2 m_{H_u}^2 + C_b Y_b^2 m_{H_d}^2 + C_\tau Y_\tau^2 m_{H_d}^2) < 0$$

with  $C_{t,b,\tau} \geq 0$

**$m_3$  can be as large as  $\sim 10\text{TeV}$**

# Higgs loops



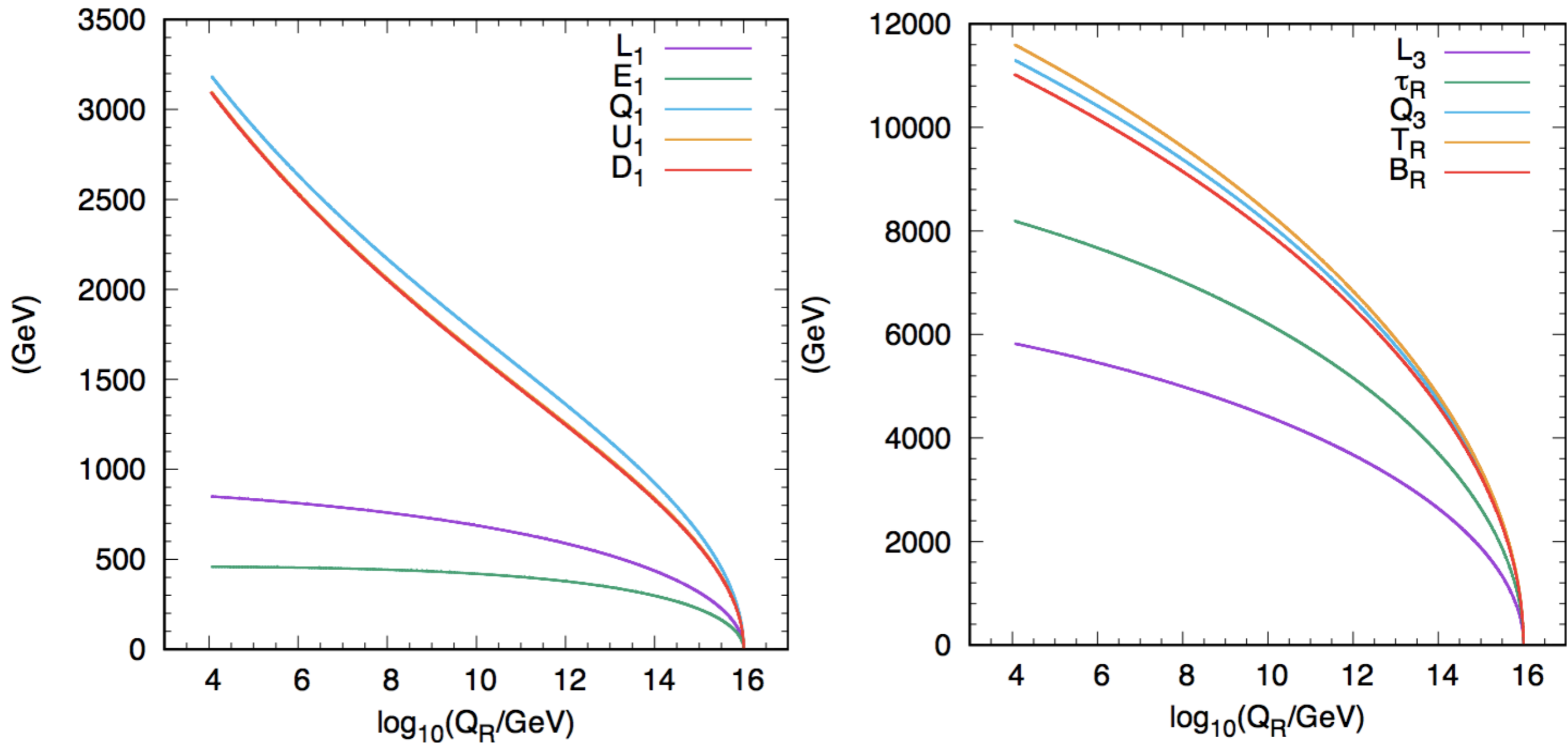
Two-loop diagrams induce positive slepton squared masses of  
 $O((100 \text{ GeV})^2)$

(if it combines with anomaly mediation, tachyonic slepton problem is solved)

Consequently hierarchical sfermion masses are generated without  
inducing too large FCNC

$$m_3 \gg m_{1,2}$$

# RGE flows in Higgs+gaugino mediation

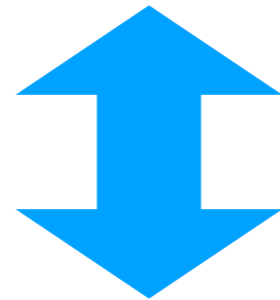


$M_1 = 440 \text{ GeV}, M_2 = 220 \text{ GeV}, M_3 = -2000 \text{ GeV}, m_{H_u}^2 = -7 \times 10^8 \text{ GeV}^2, \tan \beta = 40$   
 (mass parameters are set at the GUT scale)

# SUSY breaking mediated by Higgs-loops

- Squarks and sleptons get masses from the Higgs soft masses, and the hierarchy originates from the structure of the Yukawa couplings

Higgs  
mediation



- Quarks and leptons get masses from the Higgs VEV, and the hierarchy originates from the structure of the Yukawa couplings

Standard  
model

# Dark matter

- Because of severe constraints from direct detection experiments (LUX, PandaX), we consider the purely bino-like LSP, so that neutralino-neutralino-Higgs coupling is suppressed
- Usually, the purely bino-like neutralino is overabundant
- Correct relic abundance is obtained via **bino-wino or bino-slepton coannihilations** when their masses are close to each other
- This can be achieved with **non-universal gaugino masses** together with Higgs mediation

# Non-universal gaugino masses from product group unification

- In SUSY GUT models, there exists a serious fine-tuning problem: doublet-triplet splitting problem
- $SU(5) \times SU(3)_H \times U(1)_H$  model solves this problem elegantly  
[Yanagida, 1995; Hotta, Izawa, Yanagida, 1996]
- Non-universal gaugino masses naturally arise in this GUT model
- Gauge couplings (approximately) unify for large hidden gauge couplings

$$U(1)_Y: \quad g_1^{-2} = g_5^{-2} + \mathcal{N}^{-1} g_{1H}^{-2},$$

$$SU(2)_L: \quad g_2^{-2} = g_5^{-2},$$

$$SU(3)_C: \quad g_3^{-2} = g_5^{-2} + g_{3H}^{-2},$$

**The corrections  
can be small**

For the gaugino masses, the relevant Lagrangian is

$$\begin{aligned} \mathcal{L} = & \frac{1}{4g_5^2} \int d^2\theta \left( 1 + 2\frac{k_5}{M_P} Z \right) W_5 W_5 + h.c. \\ & + \frac{1}{4g_{3H}^2} \int d^2\theta \left( 1 + 2\frac{k_{3H}}{M_P} Z \right) W_{3H} W_{3H} + h.c. \\ & + \frac{1}{4g_{1H}^2} \int d^2\theta \left( 1 + 2\frac{k_{1H}}{M_P} Z \right) W_{1H} W_{1H} + h.c. \end{aligned}$$



$$\simeq g_5^2 / \mathcal{N}$$

**bino:**  $M_1 = (k_5 \mathcal{N} + k_{1H}) \frac{g_5^2 g_{1H}^2}{g_5^2 + \mathcal{N} g_{1H}^2} \frac{F_Z}{M_P},$

**wino:**  $M_2 = k_5 g_5^2 \frac{F_Z}{M_P}, \quad \simeq g_5^2$

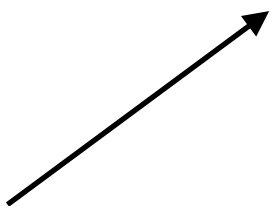
**gluino:**  $M_3 = (k_5 + k_{3H}) \frac{g_5^2 g_{3H}^2}{g_5^2 + g_{3H}^2} \frac{F_Z}{M_P},$



# Results

Free parameters are

$(M_1, M_2, M_3, m_H^2, \tan \beta)$  @ GUT scale


$$m_H^2 \equiv m_{H_u}^2 = m_{H_d}^2 < 0$$

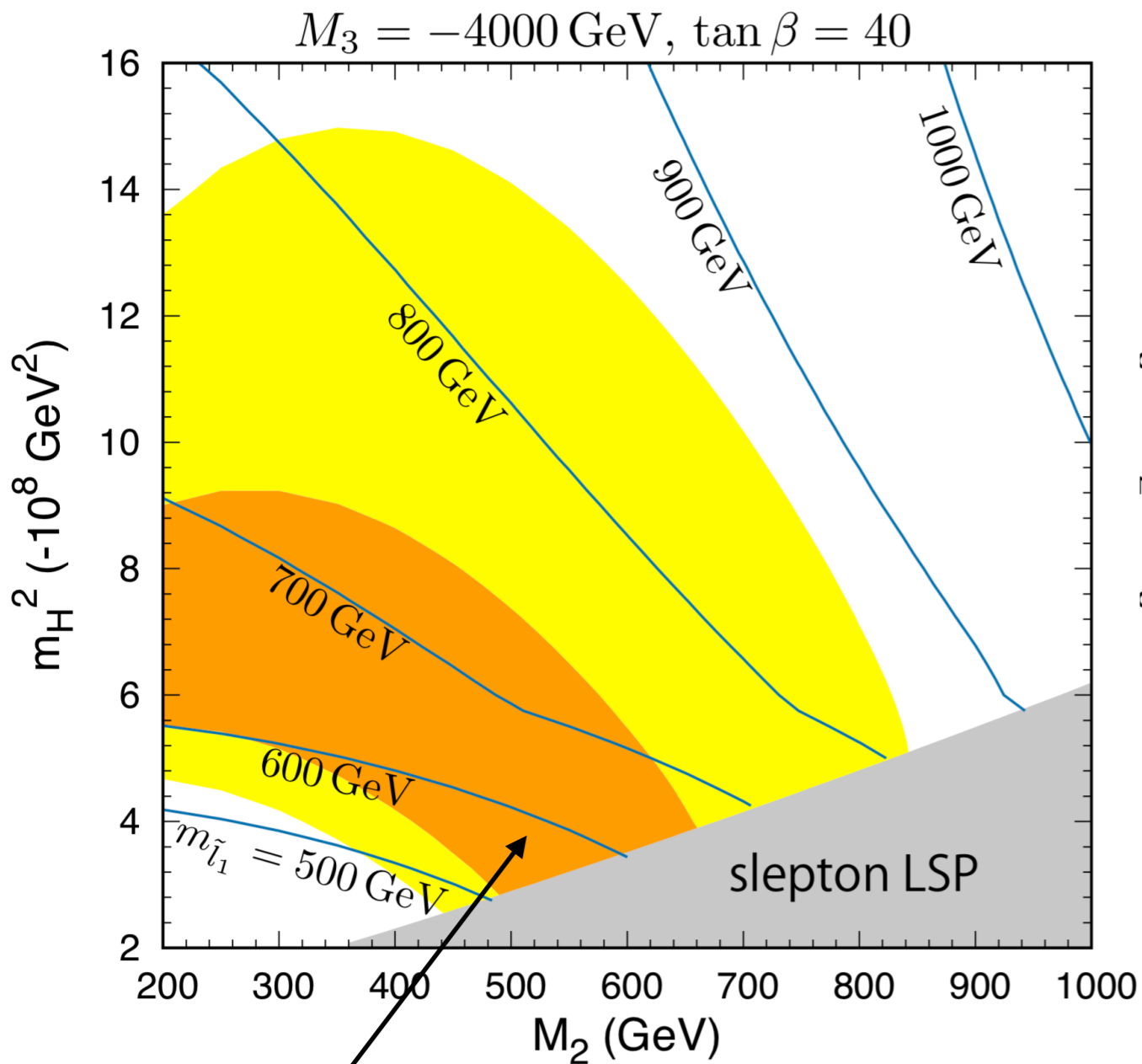
sfermions are massless at the GUT scale

We take  $\mu > 0$

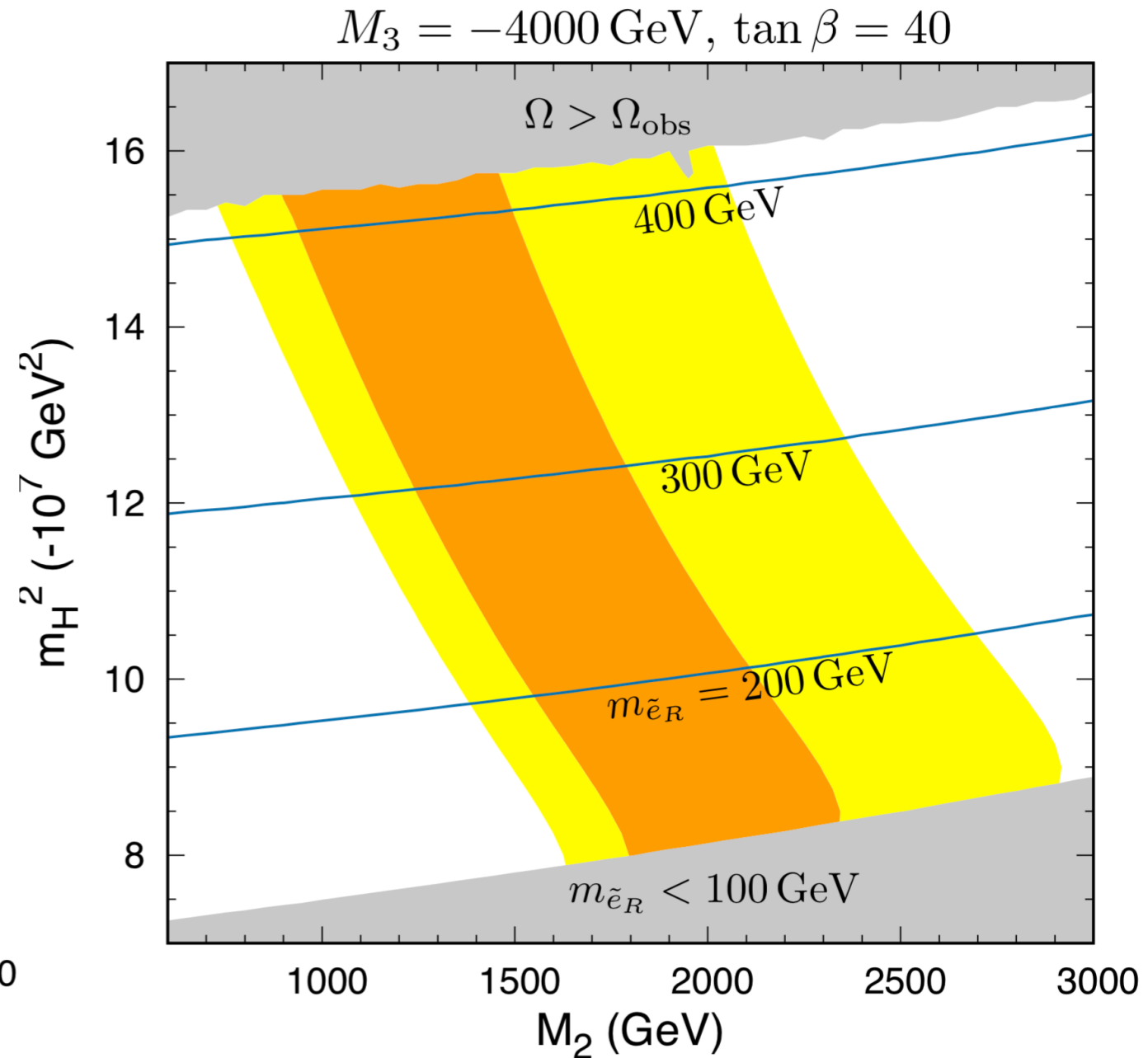
$$a_\mu^{\text{SUSY}} = \left(1 - \frac{4\alpha}{\pi} \ln \frac{m_{\tilde{\mu}}}{m_\mu}\right) \left(\frac{1}{1 + \Delta_\mu}\right) a_\mu^{\text{SUSY-1L}}$$

dominant 2-loop corrections are included

# bingo-wino coannihilation



# bingo-slepton coannihilation



$g-2$   $1 \sigma$

$M_1$  is fixed to satisfy the constraint,  $\Omega = \Omega_{\text{obs}}$

$M_1 \approx M_2$  @low-energy scale

$M_1 \approx m_{\tilde{e}_R}$

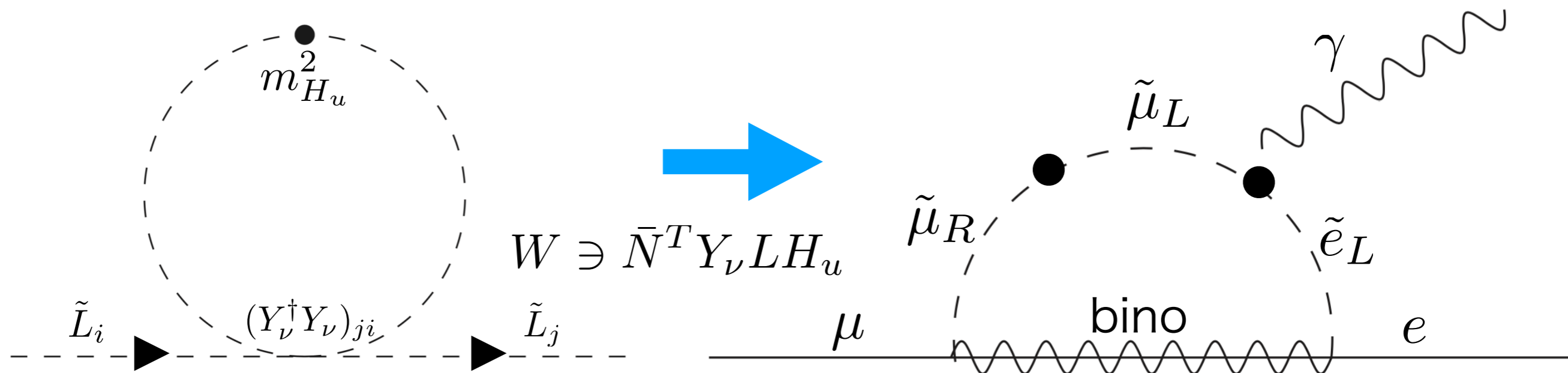
# Mass spectrum

	BP1 ( $\tilde{B} - \tilde{W}$ )	BP2 ( $\tilde{B} - \tilde{l}$ )
$M_1(M_{\text{GUT}})$	$\approx 823$	$\approx 558$
$M_2(M_{\text{GUT}})$	400	1500
$M_3(M_{\text{GUT}})$	-4000	-4000
$m_{H_u}^2 = m_{H_d}^2(M_{\text{GUT}})$	$-6.0 \times 10^8 \text{ GeV}^2$	$-1.2 \times 10^8 \text{ GeV}^2$
$\tan \beta$	40	40
$m_{\tilde{g}}$	8180	8050
$m_{\tilde{q}}$	6620	6700
$m_{\tilde{t}_1}, m_{\tilde{t}_2}$	11900, 12100	7610, 7690
$m_{\tilde{e}_L}, m_{\tilde{e}_R}$	680, 668	968, 287
$m_{\tilde{\mu}_L}, m_{\tilde{\mu}_R}$	720, 746	976, 341
$m_{\tilde{\tau}_1}, m_{\tilde{\tau}_2}$	5510, 7800	2720, 3660
$m_{\tilde{\nu}_e}, m_{\tilde{\nu}_\mu}, m_{\tilde{\nu}_\tau}$	676, 715, 5520	964, 973, 2740
$m_{\tilde{\chi}_1^0}$	404	283
$m_{\tilde{\chi}_1^\pm} \simeq m_{\tilde{\chi}_2^0}$	431	1370
$m_{\tilde{\chi}_2^\pm} \simeq m_{\tilde{\chi}_{3,4}^0}$	20900	9860
$m_A \simeq m_{H^0} \simeq M_{H^\pm}$	6800	2480
$m_h$	125.3	125.4
$\Delta a_\mu$	$2.64 \times 10^{-9}$	$2.71 \times 10^{-9}$
$\Omega_{DM} h^2$	0.119	0.119

FeynHiggs 2.14.1  
micrOMEGAs are  
used

# Lepton flavor violations with RH-neutrinos

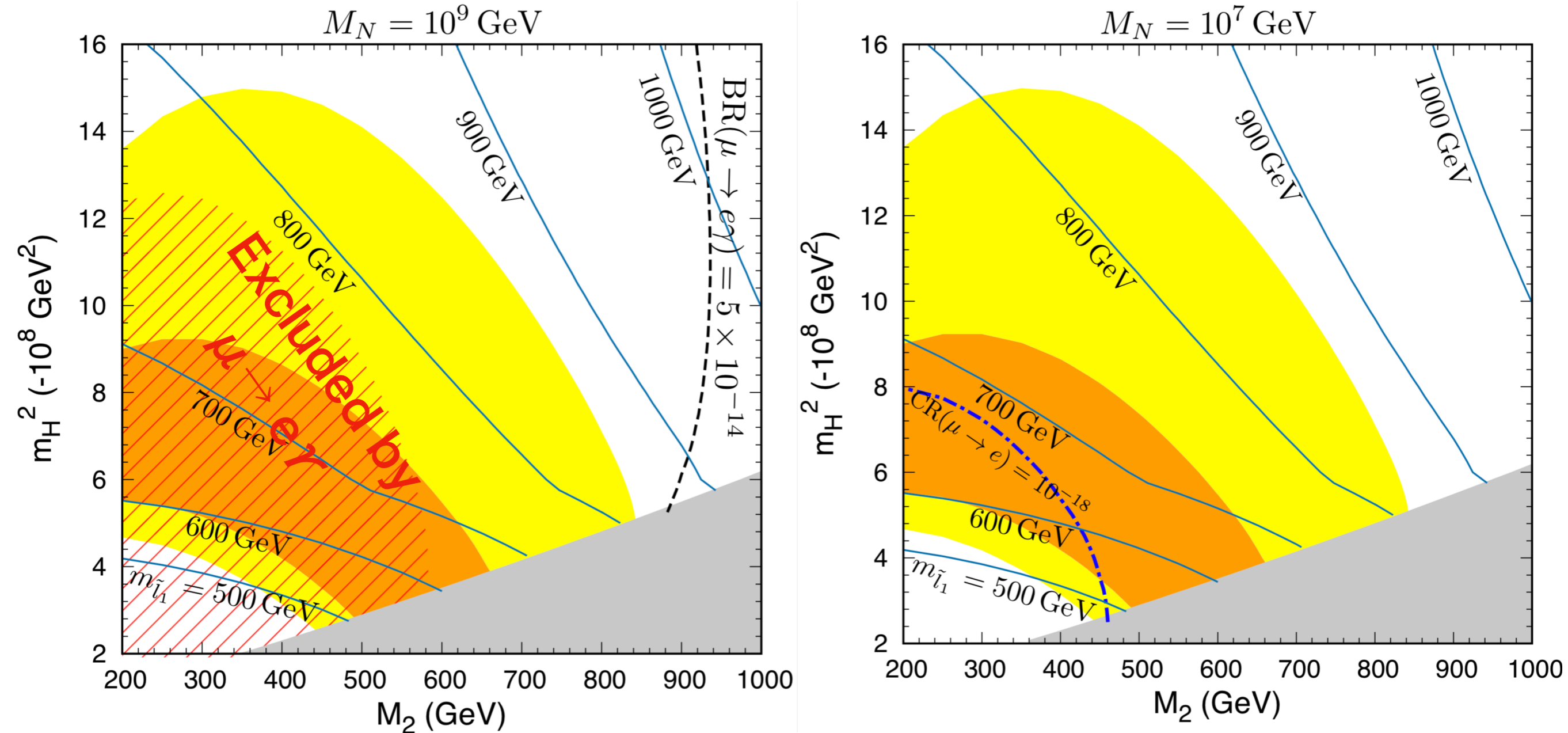
- Our scenario is flavor safe with the MSSM matter contents
- However, once RH-neutrinos are included, LFV processes are generated through slepton mass mixing



- We expect  $M_N > 10^9$  GeV to reproduce a baryon asymmetry with thermal Leptogenesis [Davidson, Ibarra, 2002]

# bino-wino coannihilation

$$M_3 = -4000\text{GeV}, \tan \beta = 40$$



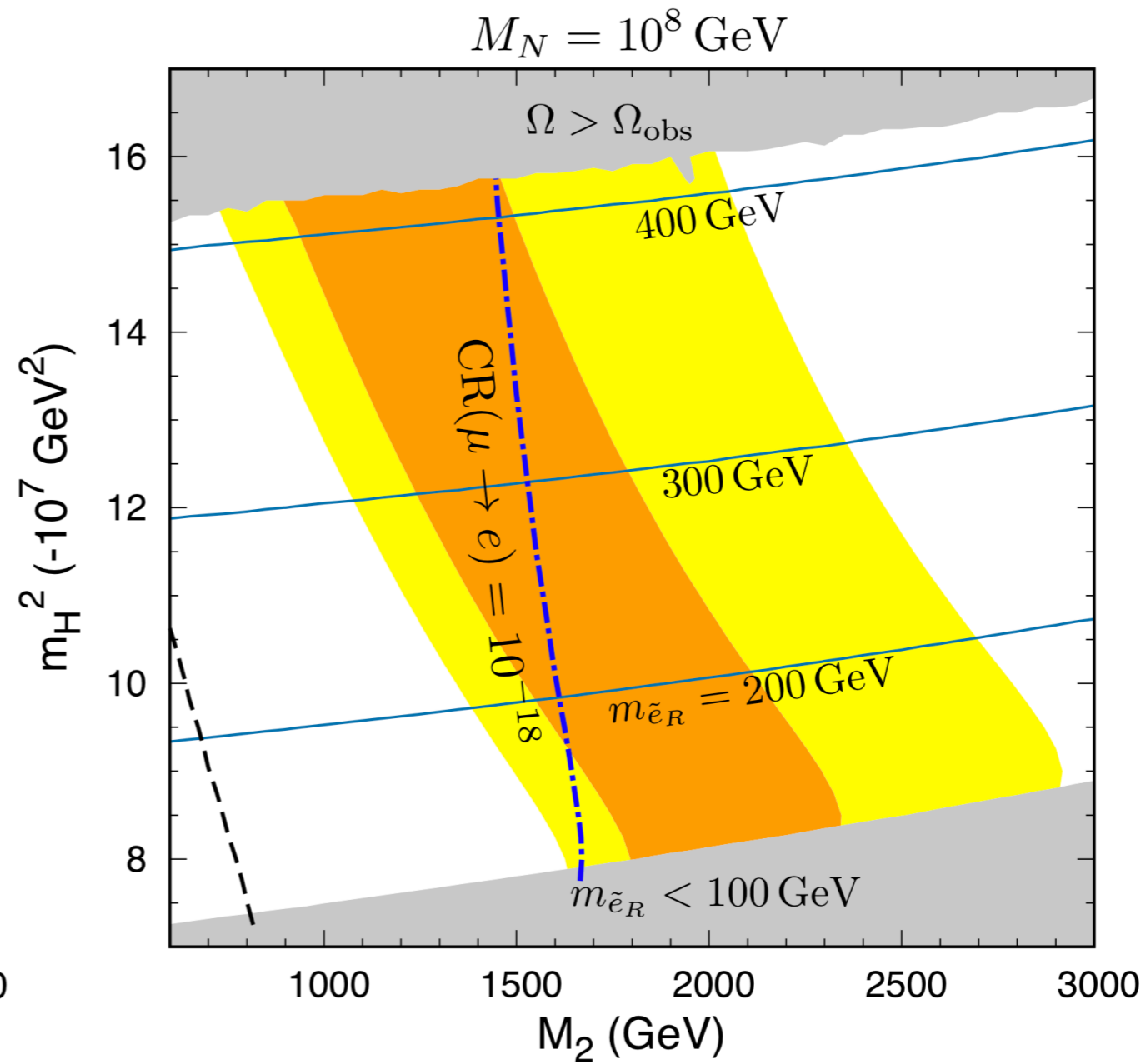
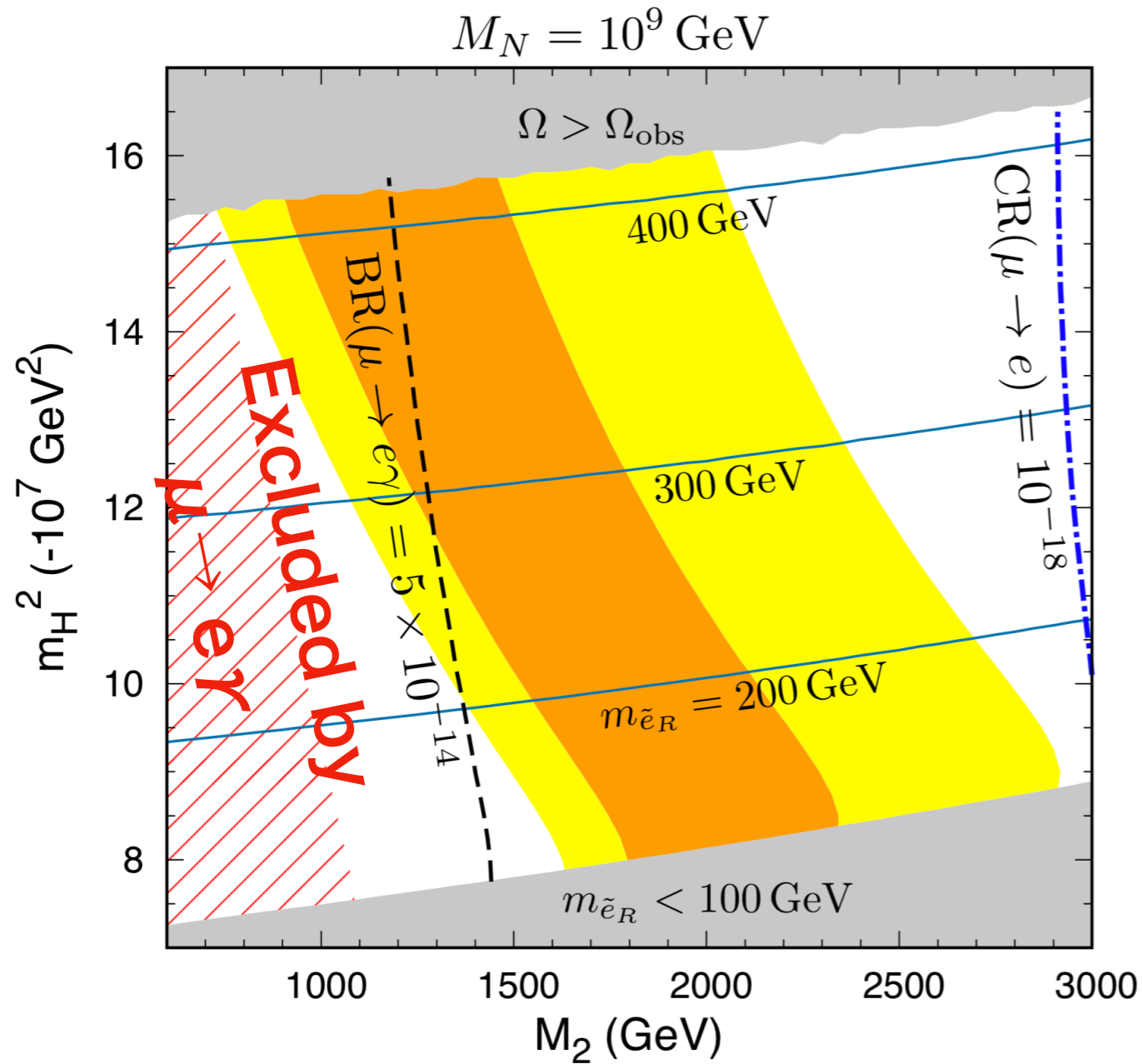
$\mu \rightarrow e \gamma$  can probe the scenario for  $M_N = 10^9 \text{ GeV}$

$\mu$ -e conversion  $\rightarrow M_N = 10^7 \text{ GeV}$

(For degenerated RH neutrino masses)

# bino-slepton coannihilation

$$M_3 = -4000\text{GeV}, \tan\beta = 40$$



$\mu$ - $e$  conversion can probe the scenario for  $M_N=10^8\text{GeV}$   
 (For degenerated RH neutrino masses)

# Summary

- In Higgs-gaugino mediation, the dark matter nature and the muon  $g-2$  anomaly are explained simultaneously
- If RH-neutrinos are included and they are responsible for baryon asymmetry, sizable lepton flavor violations are induced
- Lepton flavor violations are expected to be checked in future experiments

**Thank you for your  
attention**