

Binary neutron star mergers: observations and modelling in the multimessenger astronomy era

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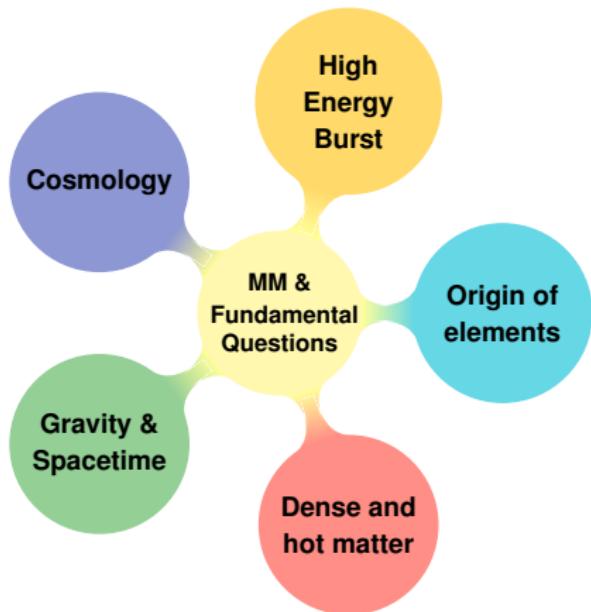
On the behalf of the Virgo Scientific Collaboration

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DISCRETE Conference, Vienna



Multimessenger astrophysics

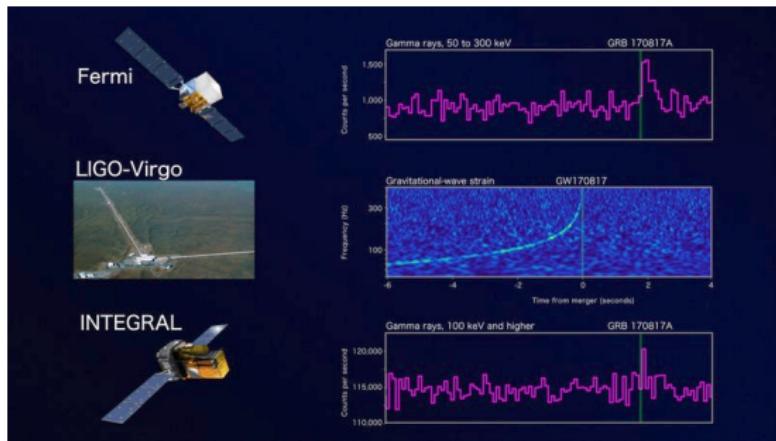
MM astrophysics: detection of different radiations from one single event or source



MM astrophysics: answers to many fundamental questions

Detections from GW170817 and its EM counterparts

GW170817: first MM detection from a compact binary merger



- ▶ GWs from an event compatible with BNS merger reported by LVC

LVC PRL 119 2017

- ▶ ~ 1.7 seconds after, γ -ray signal compatible with short GRB

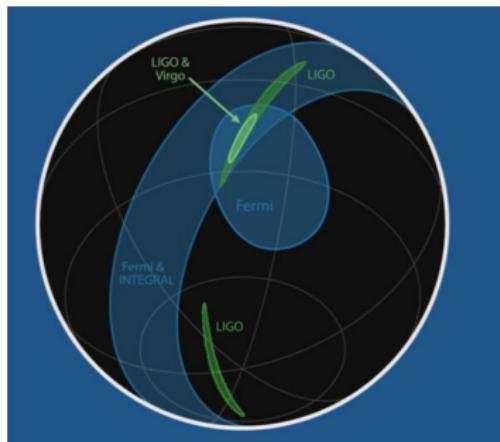
LVC, Fermi, Integral ApJ 848 L13 2017

- ▶ 11 hrs after, kilonova emission from NGC 4993 (40 Mpc): AT2017gfo

e.g., LVC+ many other astronomy and astroparticle collaborations ApJ 848 L2 2017

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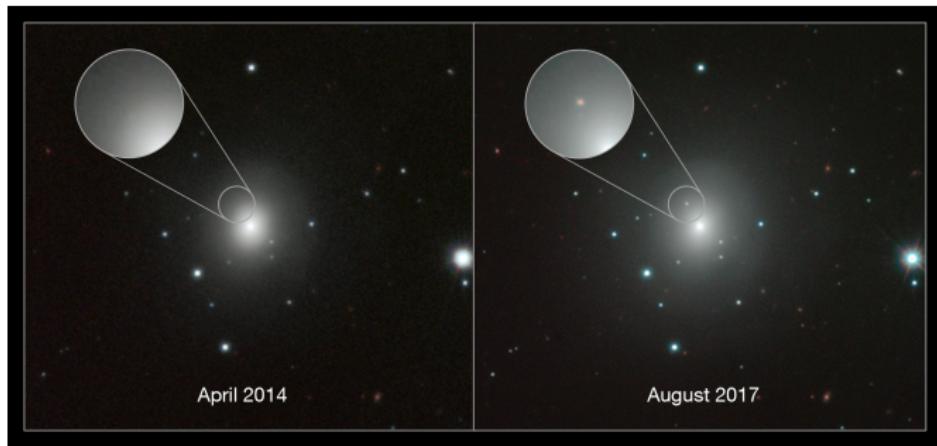
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Properties of GW170817 and its kilonova detection

- ▶ GW signal

- ▶ signal duration in GW detector network: **55 s**
- ▶ largest to date network SNR: **32.4**
- ▶ inference of many source properties

	Low-spin priors ($ \chi \leq 0.05$)	High-spin priors ($ \chi \leq 0.89$)
Primary mass m_1	$1.36\text{--}1.60 M_{\odot}$	$1.36\text{--}2.26 M_{\odot}$
Secondary mass m_2	$1.17\text{--}1.36 M_{\odot}$	$0.86\text{--}1.36 M_{\odot}$
Chirp mass \mathcal{M}	$1.188^{+0.004}_{-0.002} M_{\odot}$	$1.188^{+0.004}_{-0.002} M_{\odot}$
Mass ratio m_2/m_1	$0.7\text{--}1.0$	$0.4\text{--}1.0$
Total mass m_{tot}	$2.74^{+0.04}_{-0.01} M_{\odot}$	$2.82^{+0.47}_{-0.09} M_{\odot}$
Radiated energy E_{rad}	$> 0.025 M_{\odot} c^2$	$> 0.025 M_{\odot} c^2$
Luminosity distance D_L	$40^{+8}_{-14} \text{ Mpc}$	$40^{+8}_{-14} \text{ Mpc}$
Viewing angle Θ	$\leq 55^\circ$	$\leq 56^\circ$
Using NGC 4993 location	$\leq 28^\circ$	$\leq 28^\circ$
Combined dimensionless tidal deformability $\tilde{\Lambda}$	≤ 800	≤ 700
Dimensionless tidal deformability $\Lambda(1.4M_{\odot})$	≤ 800	≤ 1400

LVC PRL 2017. see LVC arXiv:1805.11579 for a refined analysis

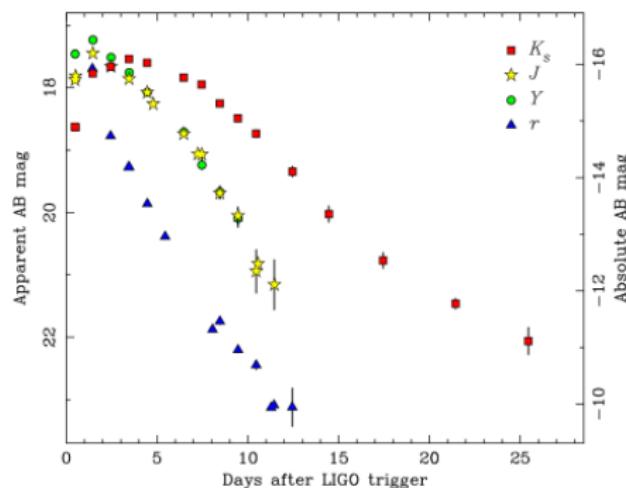
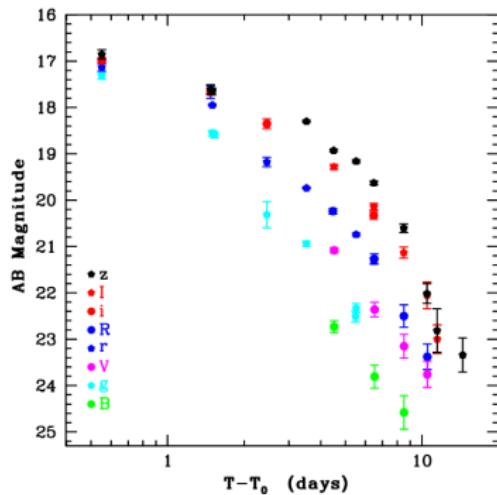
- ▶ chirp mass: $\mathcal{M}_{\text{chirp}} = (m_1 m_2)^{3/5} (m_1 + m_2)^{-1/5}$
- ▶ upper limit on E_{rad} only from BNS modelling:

$$E_{\text{rad}} \lesssim 0.126 M_{\odot} c^2$$

Zappa, Bernuzzi, Radice, Perego, Dietrich PRL 2018

Properties of GW170817 and its kilonova detection

- ▶ GW signal
- ▶ kilonova signal
 - ▶ bright, UV/O component, with a peak @ ~ 1 day (blue component)
 - ▶ rather bright, nIR component, with a peak @ ~ 5 day (red component)



Light curves; Pian, D'Avanzo *et al.* Nature 2017 (left); Tanvir *et al.* Science 2017 (right).

See also, e.g., Coulter *et al.* Science 358 2017; Troja *et al.* Nature 2017, Hallinan *et al.* Science 2017

Fundamental physics implications from GW170817 MM detection

Implications of joint GW+EM detection: v_{EM}

Speed of gravity

- if $v_{\text{EM}} \neq v_{\text{GW}}$, delay in travel time Δt :

$$\frac{v_{\text{GW}} - v_{\text{EM}}}{v_{\text{EM}}} \approx v_{\text{EM}} \frac{\Delta t}{D}$$

- arrival time difference between GW and photons from GRB

$$\Delta t_{\text{GRB}} = (1.74 \pm 0.05)\text{s}$$

- however, uncertainties on emission sequence

- if simultaneous emission ($\delta t = 0$), $\Delta t \geq \Delta t_{\text{GRB}}$ and $v_{\text{GW}} > v_{\text{EM}}$
- if EM emitted $\delta t \leq 10\text{s}$ after GW, $v_{\text{EM}} > v_{\text{GW}}$

$$-3 \times 10^{-15} \leq \frac{\Delta v}{v_{\text{EM}}} \leq 7 \times 10^{-16} \quad D = 26\text{Mpc}$$

Implications of joint GW+EM detection: $(\gamma_{\text{GW}} - \gamma_{\text{EM}})$

Test of equivalence principle

- ▶ are EM radiation and GWs affected by background potentials in the same way?
- ▶ Shapiro delay: propagation time of massless particles larger in curved spacetimes

$$\delta t_S \approx -\frac{1+\gamma}{c^3} \int_{\mathbf{r}_e}^{\mathbf{r}_o} U(\mathbf{r}(l)) dl$$

- ▶ Einstein-Maxwell minimal coupling: $\gamma_{\text{EM}} = \gamma_{\text{GW}} = 1 \rightarrow (\gamma_{\text{GW}} - \gamma_{\text{EM}}) = 0$
- ▶ conservative limit obtained by assuming:
 - ▶ $0 \leq \delta t \leq 10\text{s}$
 - ▶ measured arrival time delay $\Delta t_{\text{GRB}} = (1.74 \pm 0.05)\text{s}$
 - ▶ $U(\mathbf{r})$ caused by Milky Way for distances $> 100\text{kpc}$,

$$-2.6 \times 10^{-7} \leq (\gamma_{\text{GW}} - \gamma_{\text{EM}}) \leq 1.2 \times 10^{-6}$$

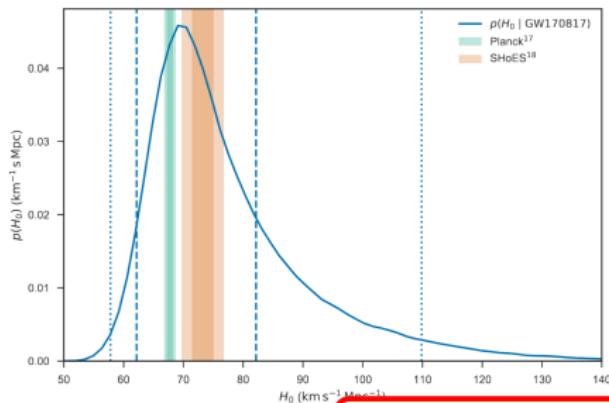
Implications of joint GW+EM detection: H_0

GW as standard sirens for H_0 measurement

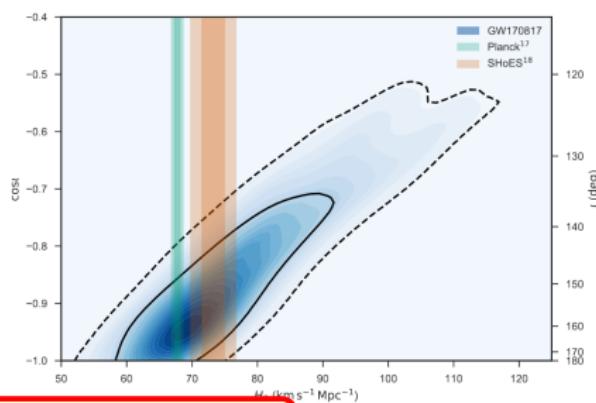
LVC, 1M2H coll, Dark Energy Camera GW-EM coll and DES coll *et al.* Nature 551 2017

- ▶ Hubble law in the local Universe: $v_H = H_0 d + \mathcal{O}(v_H/c)$
- ▶ analysis of GW signal (NGC 4993 sky location):
 - ▶ measurement of cosmological redshift of NGC 4993

$$d = 43.8^{+2.9}_{-6.9} \text{ Mpc}$$



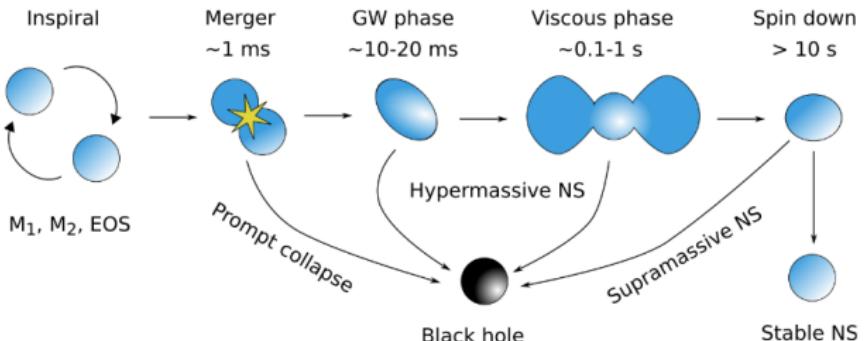
$$v_H = 3017^{+166}_{-166} \text{ km s}^{-1}$$



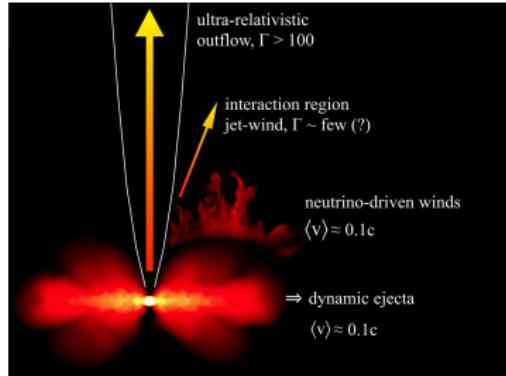
$$H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$$

BNS merger modelling and the EOS of neutron star

BNS merger in a nutshell



Credit: D. Radice



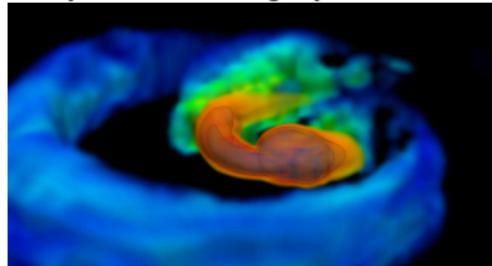
- ▶ *n*-rich matter ejected
 - ▶ *r*-process nucleosynthesis
 - ▶ different mechanisms
- ▶ decay of freshly synthesized *r*-process element: release of nuclear energy
- ▶ **kilonova:** thermal photons diffuse and are emitted at photosphere

Li & Paczynski ApJL 98, for a review: Metzger LRR 17

BNS modelling and NS equation of state (EOS)

BNS merger simulations in Numerical Relativity (NR):

necessary to model highly non-linear, strong field (post-)merger phase



Volume rendering of matter density from BNS NR simulation.

Courtesy of T. Dietrich & S. Bernuzzi

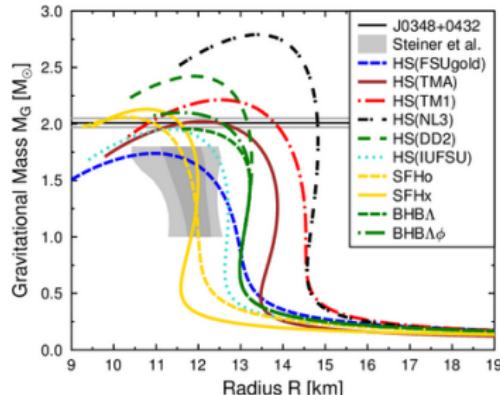
EOS of NS matter still affected by large uncertainties

e.g., Tsang *et al* 86 PRC 2012, Lattimer & Prakash Phys. Rep. 621 2016,

Örtel *et al*. RMP 89 2017 for recent reviews

- ▶ nucleon Hamiltonian
- ▶ many-body treatment
- ▶ thermodynamical degrees of freedom (hyperons, quarks?)

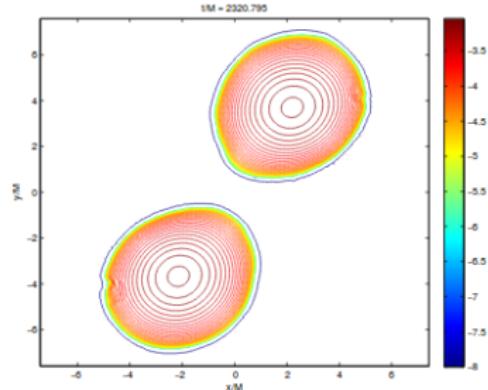
- ▶ NR: art of solving Einstein's and GR-HD equations on computer
- ▶ accurate GW waveforms, energetics, final state properties, matter dynamics
- ▶ need of NS matter EOS to close the system



Mass-radius curves for several RMF NS EOS. Courtesy of M. Hempel

Tidal deformation during the inspiral phase

NS in external, inhomogeneous gravitational field \Rightarrow tidal deformation



Bernuzzi et al PRD 2012

$$Q_{i,j} = -\lambda \mathcal{E}_{i,j}$$

$$\lambda = \left(\frac{2}{3} \frac{R^5}{G} k_2 \right)$$

- ▶ $Q_{i,j}$ quadrupolar moment
- ▶ $\mathcal{E}_{i,j} = \partial_{i,j}^2 \Phi$ tidal field
- ▶ k_2 quadrupolar tidal polarizability
- ▶ R radius of the star

- ▶ tidal deformation enhances GW emission
- ▶ $\geq 5^{th}$ PN order correction to point particle dynamics
- ▶ leading term $\propto \tilde{\Lambda}(M_A, M_B, \text{EOS})$

$$\tilde{\Lambda} = \frac{16}{13} \left[\frac{(M_A + 12M_B)M_A^4 \Lambda_2^{(A)}}{(M_A + M_B)^5} + (A \leftrightarrow B) \right]; \quad \Lambda_2^{(i)} = \left(\frac{c^2}{M_i} \right)^5 \lambda_{(i)}; \quad i = A, B$$

see, e.g., Damour, Les Houches Summer School on Gravitational Radiation 1982; Flanagan & Hinderer PRD 77 2008, Bernuzzi et al PRD 2012

NS mass, radius and EOS from GW170817

Idea:

Measure the NS tidal deformation from GW170817 inspiral signal to probe cold NS EOS above ρ_{nuc}

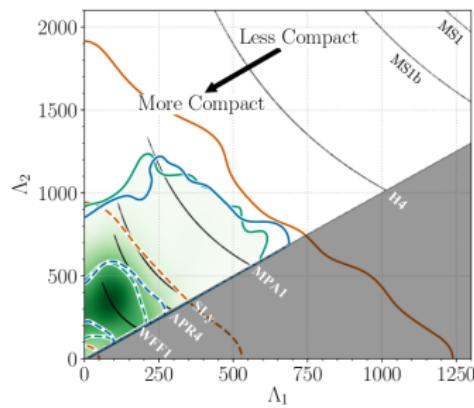
LVC PRL 121 2018

Relevant assumptions:

- ▶ same parametrized EOS for the two NSs
- ▶ $M_{\text{max,TOV}} > 1.97M_{\odot}$

e.g. Lindblom & Indik PRD 89 2014

Antoniadis *et al* Science 340 2013



- ▶ marginalized posteriors for $\Lambda_{1,2}$
- ▶ same EOS for the two NSs improves results compared with previous analysis

LVC PRL 121 2018

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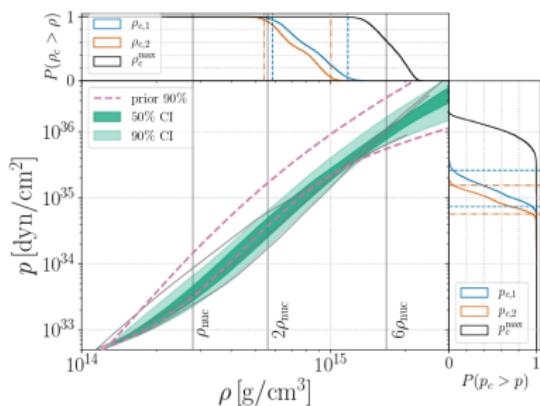
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LVC PRL 121 2018

- ▶ marginalized posteriors for $p = p(\rho)$
- ▶ GW signal favors softer EOS
- ▶ $M_{\text{TOV,max}} > 1.97M_{\odot}$: EOS stiffening at high density

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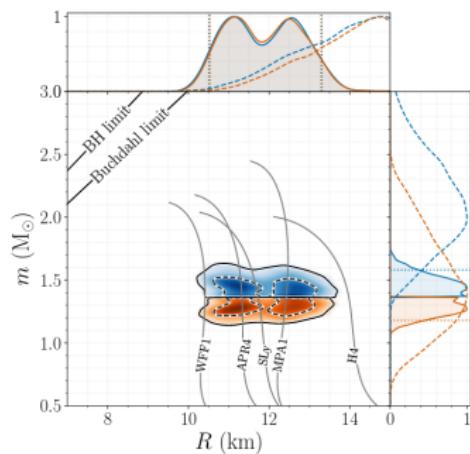
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- ▶ simultaneous NS $M - R$ measurements
- ▶ $R_1 = 11.9^{+1.4}_{-1.4} \text{ km}$
 $m_1[M_{\odot}] \in [1.36, 1.58]$
- ▶ $R_2 = 11.9^{+1.4}_{-1.4} \text{ km}$
 $m_2[M_{\odot}] \in [1.18, 1.36]$

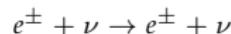
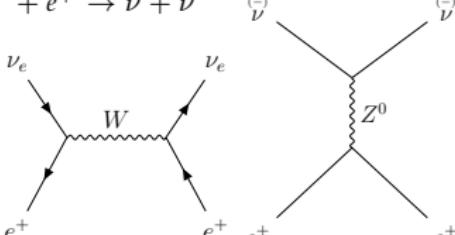
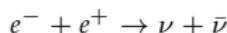
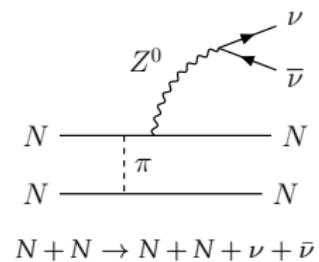
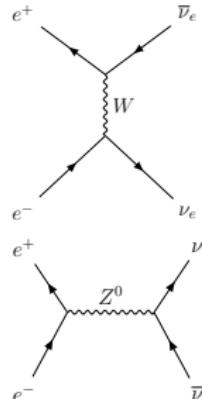
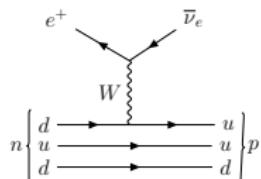
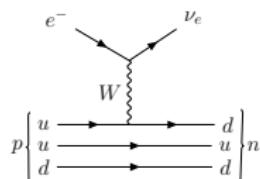
LVC PRL 121 2018

DISCRETE conference, 26/11/2018

Weak interaction in BNS merger

Weak interaction in hot and dense matter

- most relevant neutrino **production** processes (inverse: **absorption**)



Tubbs & Schramm ApJ 75; Lamb & Pethick ApJ 76; ... Burrows, Reddy

& Thompson NuPhA 06; Bacca, Hally, Liebendörfer, Perego *et al.* ApJ 12

Reaction rates in hot and dense matter

- plasma (n, p, e^\pm, γ) in thermal and NSE (NS matter EOS)
- ν production rates: boosted by high temperatures & densities

$$\lambda_{e^-} \propto n_p T^5 F_4(\mu_e/T) \quad \lambda_{e^+} \propto n_n T^5 F_4(-\mu_e/T)$$

$$\begin{aligned}\lambda_{e^-} &= \int \frac{d^3 p_\nu}{(2\pi\hbar c)^3} j_{\nu e}(E_\nu) \\ &\approx \left(\frac{n_n - n_p}{\exp\left(\frac{\mu_p - \mu_n + \Delta}{k_B T}\right) - 1} \right) \int_0^\infty \frac{4\pi\sigma_0 c}{(2\pi\hbar c)^3} \left(\frac{E + \Delta}{m_e}\right)^2 f_{e^-}(E + \Delta) E^2 dE\end{aligned}$$

$$\sigma_0 = \frac{4G_F^2(m_e c^2)^2(c_v^2 + 3c_a^2)}{\pi(\hbar c)^4} \approx 2.43 \times 10^{-44} \text{ cm}^2 \sim 2 \times 10^{-20} \sigma_{t,e}$$

$$F_k(\eta) = \int_0^\infty \frac{x^k}{1 + \exp(x - \eta)} dx$$

e.g. Bruenn ApJ 1985; Rosswog & Liebendörfer MNRAS 2003

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- ν absorption/scattering rates: neutrino diffusion

$$\ell_{\nu_e} = \frac{c}{\kappa_{\nu_e}} \approx 2.36 \times 10^3 \text{ cm} \left(\frac{\rho}{10^{14} \text{ g/cm}^3} \right)^{-1} \left(\frac{E_\nu}{10 \text{ MeV}} \right)^{-2} \ll R_{\text{NS}}$$

$$\kappa_{\nu_e}(E_{\nu_e}) = \exp \left(\frac{E_{\nu_e} - (\mu_p + \mu_e - \mu_n)}{k_B T} \right) j(E_{\nu_e}) \approx \frac{n_N \sigma_\nu}{c}$$

$$\sigma_\nu \sim \sigma_0 \left(\frac{E_\nu}{m_e c^2} \right)^2$$

⇒ Radiative transfer problem

Reaction rates in hot and dense matter

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- ▶ ν absorption/scattering rates: neutrino diffusion

$$\ell_{\nu_e} \ll R_{\text{NS}}$$

- ▶ matter composition:

- ▶ W-mediated processes can change ratio between n and p , i.e. Y_e :



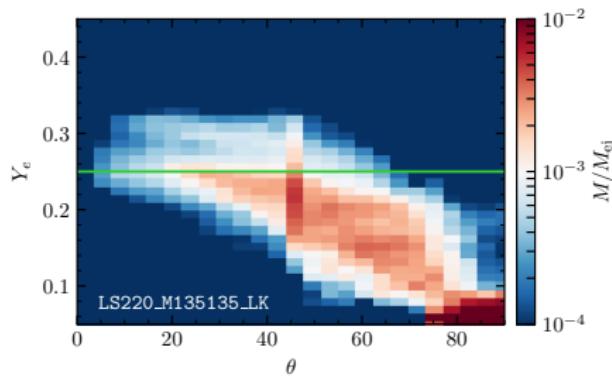
$$(Y_e = n_e/n_B \approx n_p / (n_p + n_n))$$

→ direct impact on nucleosynthesis

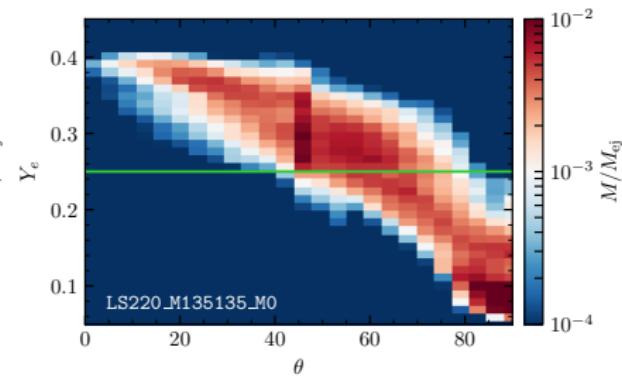
Impact of ν absorption on dynamical ejecta

- ▶ dynamical ejecta: matter promptly expelled in a BNS merger
 - ▶ $\tau_{\text{ej,dyn}} \lesssim 5 \text{ ms}$
 - ▶ $M_{\text{ej,dyn}} \lesssim 10^{-4} - 10^{-3} M_{\odot}$
 - ▶ $v_{\text{ej,dyn}} \sim 0.3c$
- ▶ in the past, ν -matter interactions assumed to be negligible
- ▶ however, ν -matter interactions increase Y_e ($n + \nu_e \rightarrow p + e^-$)

w/o neutrino absorption



w neutrino absorption

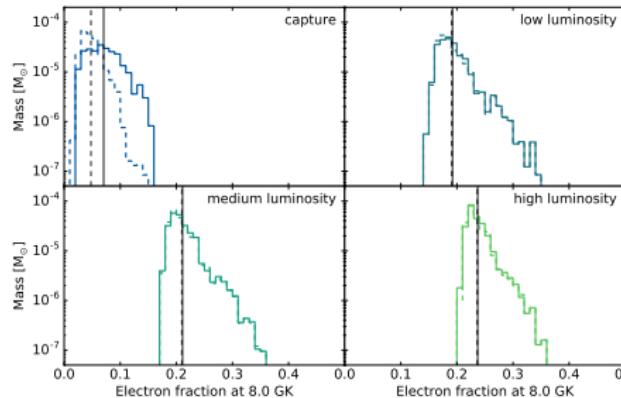


Perego, Radice, Bernuzzi ApJL 2017; Radice, Perego, Hotokezaka *et al* arXiv:1809.11161

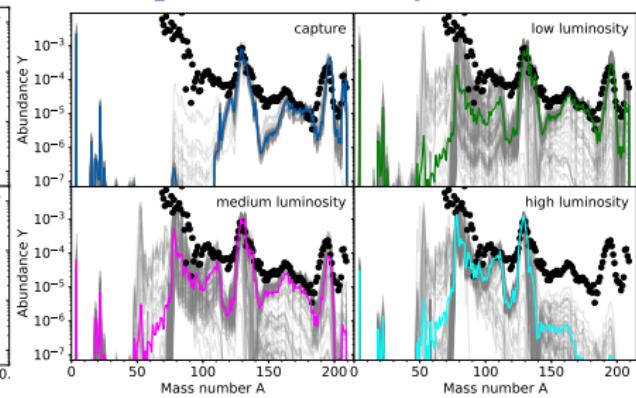
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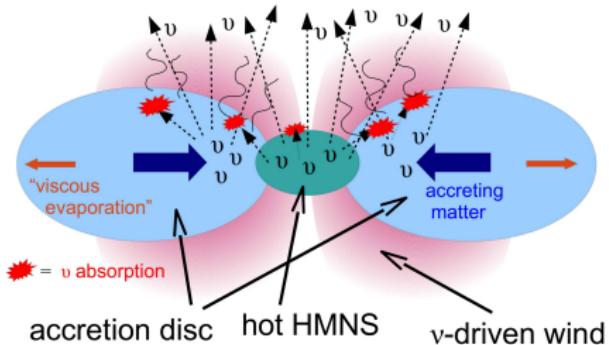
ejecta Y_e for increasing L_ν



→ r -process nucleosynthesis



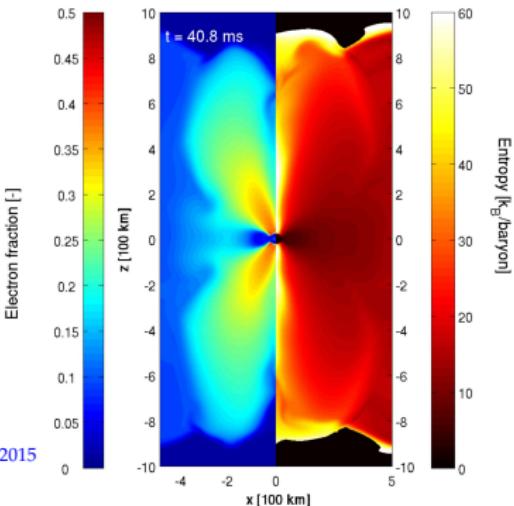
ν -driven winds from BNS merger



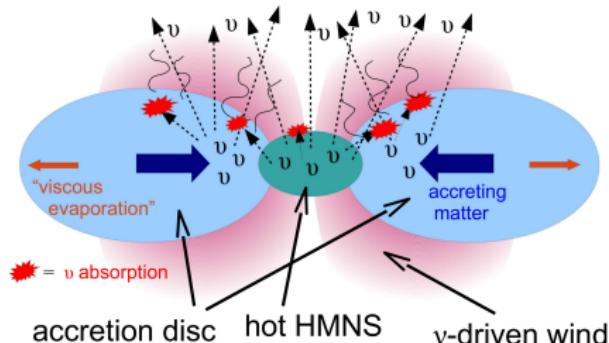
- ▶ wind ejection driven by energy & momentum deposition
- ▶ $\tau_{\text{ej,wind}} \sim \text{tens ms}$
- ▶ $M_{\text{ej,wind}} \lesssim 10^{-2} M_{\odot}$
- ▶ $v_{\text{ej,wind}} \lesssim 0.1c$

- ▶ first 3D radiation-hydrodynamics simulation
- ▶ ejecta analysis and nucleosynthesis calculations
- ▶ kilonova prediction: blue & red kilonova

Perego, Rosswog, Cabezon *et al* MNRAS 2014; Martin, Perego, Arcones *et al* ApJ 2015



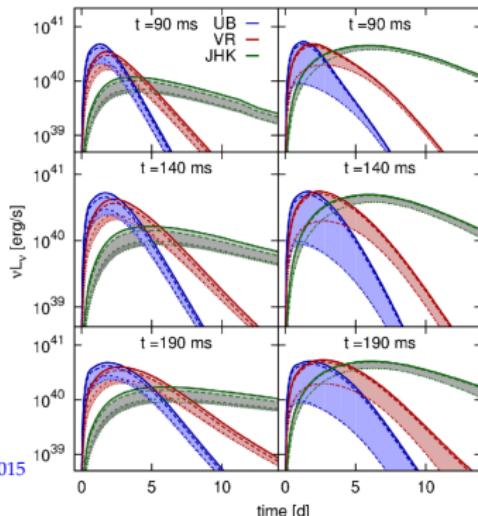
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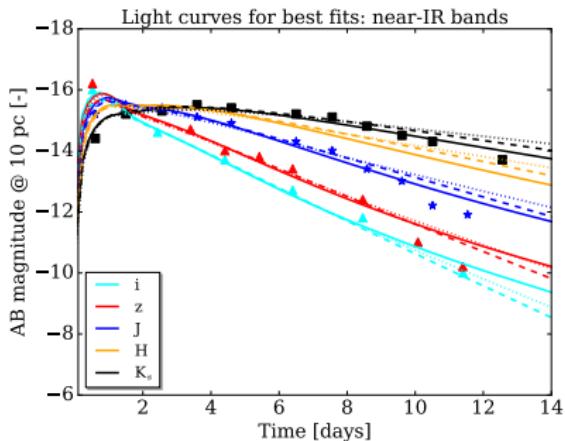
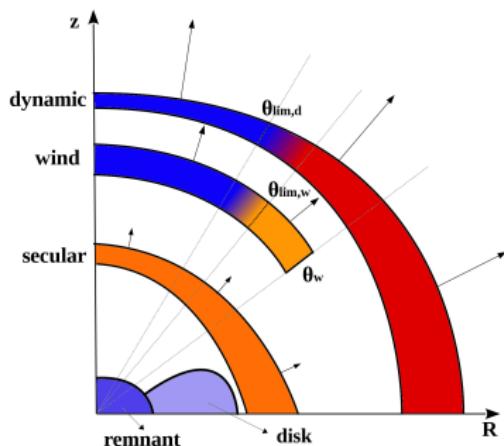
Perego, Rosswog, Cabezon et al MNRAS 2014; Martin, Perego, Arcones et al ApJ 2015



Multi-Component Anisotropic Kilonova Model

- ▶ kilonova model that includes our present knowledge about ejecta
- ▶ different ejection channels → **multi-component**
- ▶ explicit dependency on polar angle → **anisotropic & viewing angle**
- ▶ homologous expansion + γ diffusion

Perego, Radice, Bernuzzi 2017, ApJL

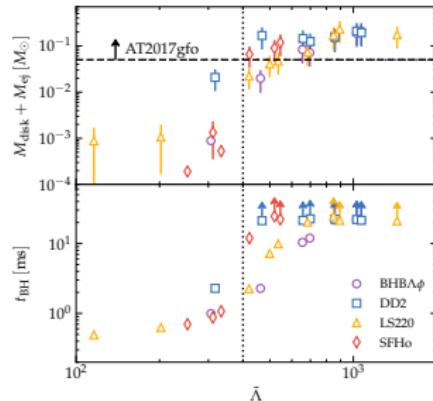


$$M_{ej,tot} \sim 0.05 M_{\odot}, \quad \theta_{obs} \approx 30^{\circ}$$

Multimessenger constraints on nuclear EOS

- ▶ can GW signal + EM signature + NR simulations constrain NS EOS?

Radice, Perego, Zappa, Bernuzzi ApJL 17

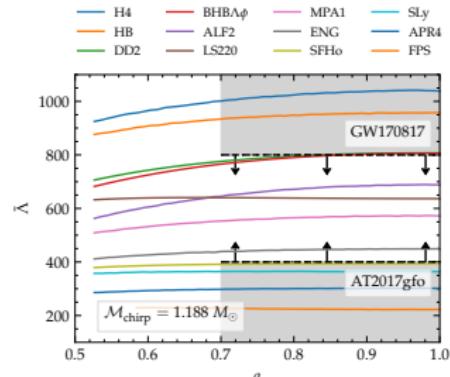


- ▶ $\tilde{\Lambda}$ describes BNS deformation:

$$\tilde{\Lambda} = \tilde{\Lambda}(\text{EOS}, M_1, M_2)$$

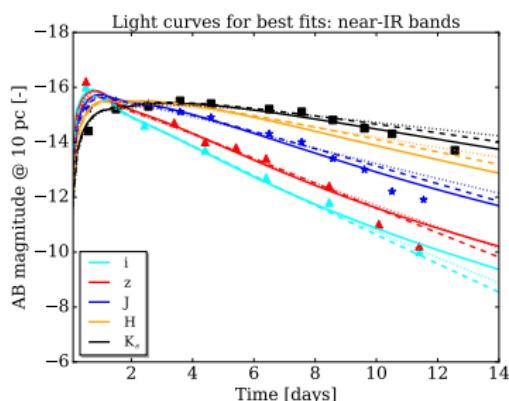
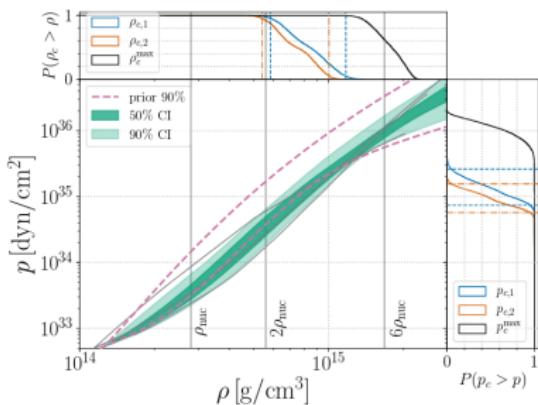
- ▶ NR results suggest $\tilde{\Lambda} \gtrsim 400$ to account for $0.05M_{\odot}$ of ejecta

- ▶ application to GW170817 / AT2017gfo
- ▶ $\tilde{\Lambda}(\text{EOS}, M_{\text{chirp}} = 1.118M_{\odot}, q)$
- ▶ calculation of $\tilde{\Lambda}$ for different EOSs
- ▶ **MM constraints from GW & EM+NR exclude very stiff & soft EOSs**

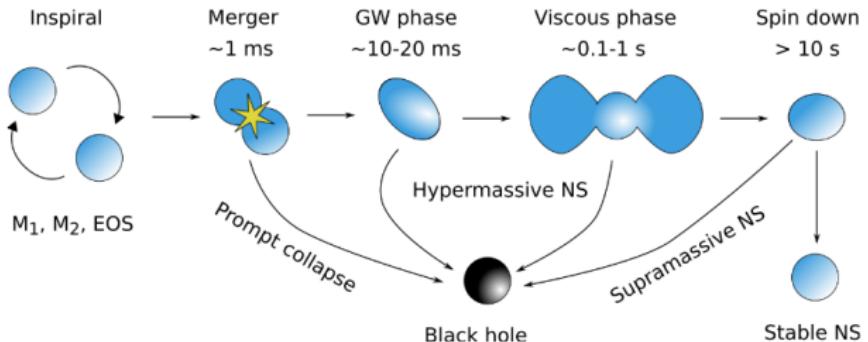


Conclusions

- MM astrophysics can answer fundamental questions: compact binary mergers as laboratory for fundamental physics
- interpretation of MM observation requires sophisticated models including all the necessary physics
- weak reactions and neutrinos play a central role in MM astrophysics
- joint GW+EM detections can set stringent limits, e.g.
 - interaction speed
 - equivalence principle
 - Hubble constant
 - EOS of nuclear matter



BNS merger in a nutshell



Credit: D. Radice; see Rosswog IJMP 2015 for a recent review

- ▶ **Massive NS ($\rightarrow \text{BH}$)**
 $\rho \gtrsim 10^{12} \text{ g cm}^{-3}$, $T \sim \text{a few } 10 \text{ MeV}$
- ▶ **thick accretion disk**
 $M \sim 10^{-2} - 0.2M_{\odot}$, $Y_e \lesssim 0.20$
 $T \sim \text{a few MeV}$
- ▶ **intense ν emission**
 $L_{\nu, \text{tot}} \sim 10^{53} \text{ erg s}^{-1}$, $E_{\nu} \gtrsim 10 \text{ MeV}$

$$(Y_e = n_e/n_B \approx n_p / (n_p + n_n))$$

NS radii and EOS from GW170817: basic idea

Idea:

Measure the NS tidal deformation from GW170817 inspiral signal to probe cold NS EOS above ρ_{nuc} , assuming the same EOS for the two NSs [LVC PRL 121 2018](#)

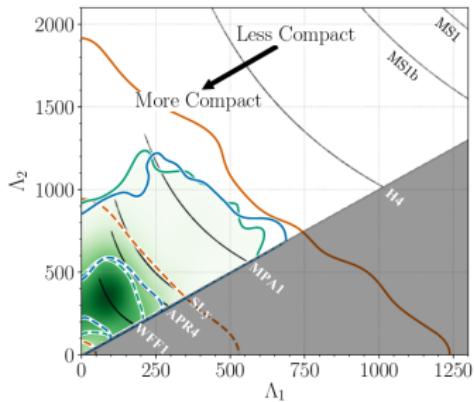
Hypothesis:

- ▶ NS mass and spin consistent with astro constraints & expectations
- ▶ same EOS for the two NSs

Methods:

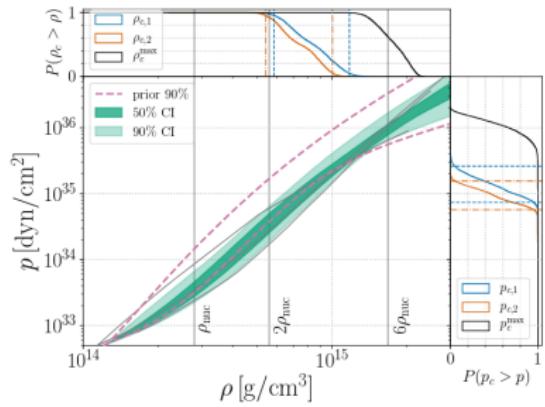
- ▶ Bayesian analysis of GW data against waveforms models generated by PhenomPNRT with different $\{\Lambda_1, \Lambda_2\}$ choices
e.g., Schmidt *et al.* PRD 86 2012; Kahn *et al.* PRD 93 2016, Dietrich, Bernuzzi, Tichy PRD 2017
- ▶ two methods to generate $\{\Lambda_1, \Lambda_2\}$:
 1. EOS-insensitive empirical relations involving $\Lambda_{1,2}$ e.g. Yanu & Yuges CQG 33 2016
 2. general, parametrized version of the NS EOS, satisfying basic constraints e.g. Lindblom & Indik PRD 89 2014
 - ▶ causality
 - ▶ thermodynamical stability
 - ▶ $M_{\text{TOV,max}} > 1.97M_{\odot}$ Antoniadis *et al* Science 340 2013

NS radii and EOS from GW170817: results



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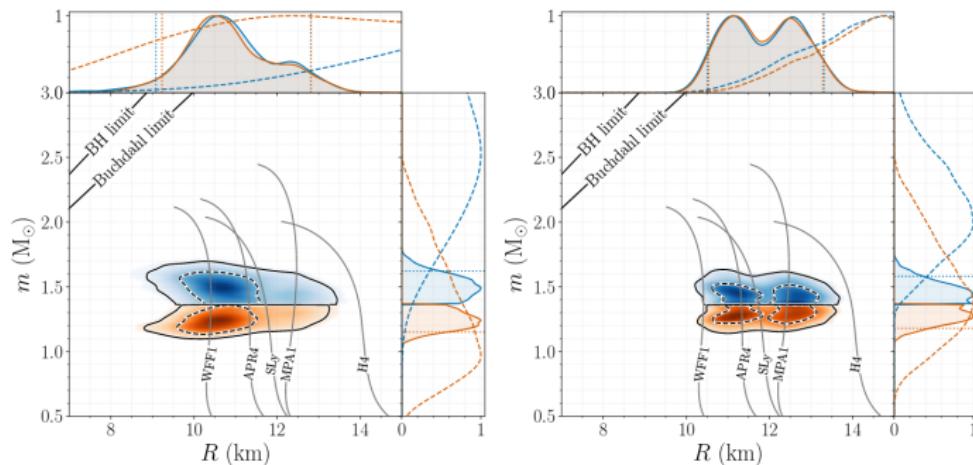
- ▶ marginalized posteriors for $\Lambda_{1,2}$
- ▶ same EOS for the two NSs improves results compared with previous analysis



- ▶ marginalized posteriors for $p = p(\rho)$
- ▶ GW signal favors softer EOS
- ▶ $M_{\text{TOV,max}} > 1.97M_\odot$: EOS stiffening at high density

NS radii and EOS from GW170817: results

- simultaneous M - R measurements



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- EOS-independent $\Lambda_{1,2}$ relations
- $R_1 = 10.8^{+2.0}_{-1.7} \text{ km}$
 $m_1[M_\odot] \in [1.36, 1.62]$
- $R_2 = 10.7^{+2.1}_{-1.5} \text{ km}$
 $m_2[M_\odot] \in [1.15, 1.36]$

- parametrized EOS
- $R_1 = 11.9^{+1.4}_{-1.4} \text{ km}$
 $m_1[M_\odot] \in [1.36, 1.58]$
- $R_2 = 11.9^{+1.4}_{-1.4} \text{ km}$
 $m_2[M_\odot] \in [1.18, 1.36]$