

New perspectives in QCD with jet substructure

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A Model for SU(3) vacuum degeneracy using light cone coordinates

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e-Print: [hep-th/0101072](https://arxiv.org/abs/hep-th/0101072) | [PDF](#)

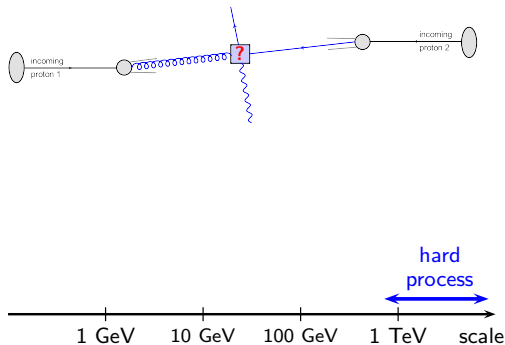
Abstract

Working in light-cone coordinates, we study the zero-modes and the vacuum in a 2+1 dimensional SU(3) gauge model. Considering the fields as independent of the transverse variables, we dimensionally reduce this model to 1+1 dimensions. After introducing an appropriate su(3) basis and gauge conditions, we extract an adjoint field from the model. Quantization of this adjoint field and field equations lead to two constrained and two dynamical zero-modes. We link the dynamical zero-modes to the vacuum by writing down a Schrodinger equation and prove the non-degeneracy of the SU(3) vacuum provided that we neglect the contribution of constrained zero-modes.

I have departed quite a bit from this topic
but let's see if we can find a way to connect...

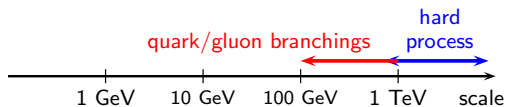
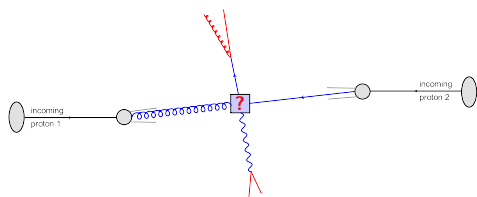
Anatomy of a high-energy collision

Colliders study fundamental interactions at high energy



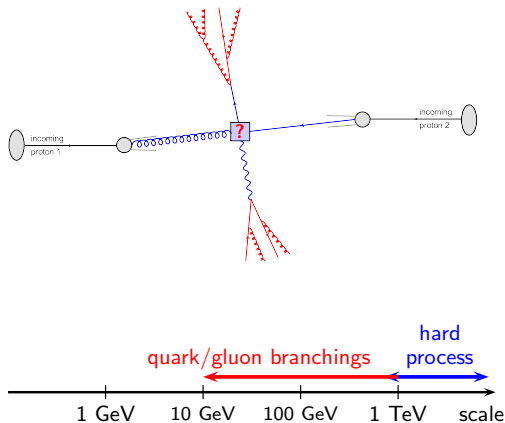
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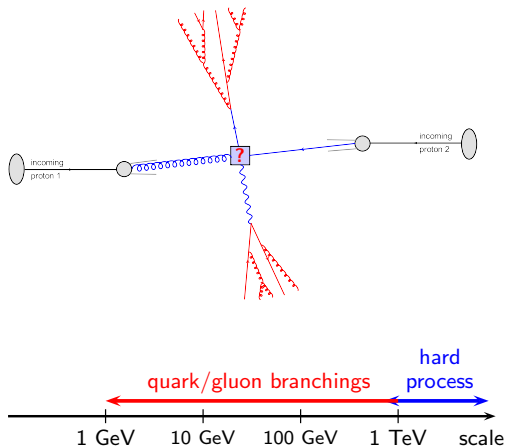
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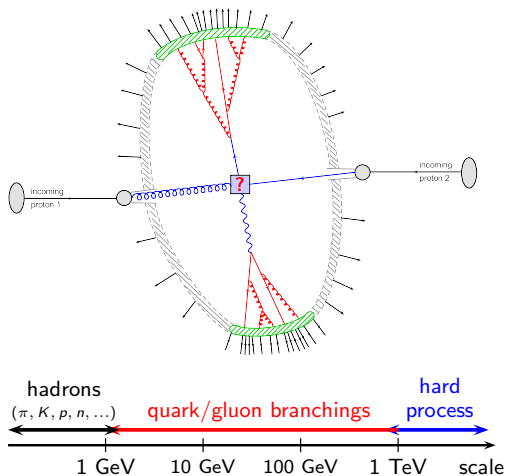
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Anatomy of a high-energy collision

Colliders study fundamental interactions at high energy



Hard + branchings

- perturbative QCD
- controlled, solid
- predictive with genuine theory uncertainties

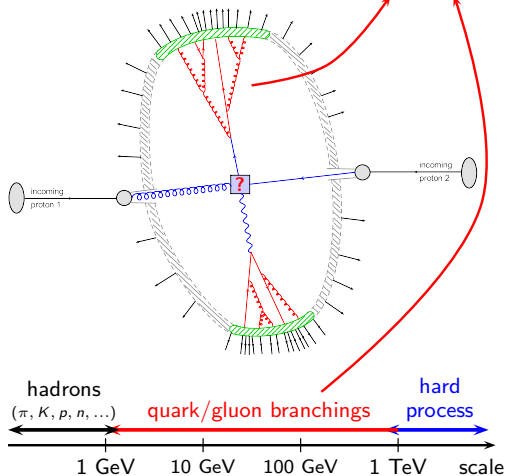
Hadronisation

- NON-perturbative
- needs modelling
- model-dependent

Anatomy of a high-energy collision

Colliders study fundamental interactions at high energy

topic #1 for this talk



Hard + branchings

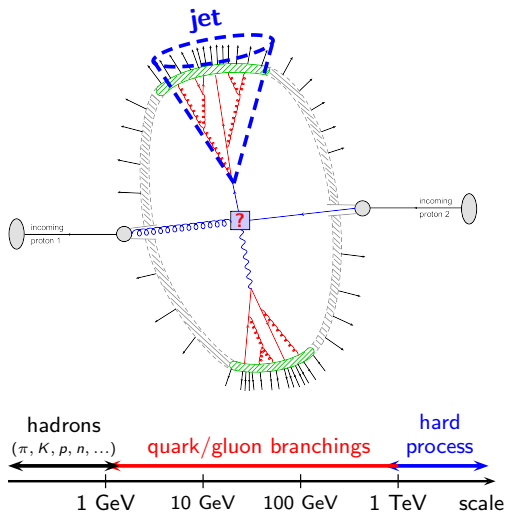
- perturbative QCD
- controlled, solid
- predictive with genuine theory uncertainties

Hadronisation

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- needs modelling
- model-dependent

Anatomy of a high-energy collision

Colliders study fundamental interactions at high energy



branchings mostly
collinear



“high-energy parton”
→ collimated shower of
particles \equiv JET

Jet \equiv proxy to
hard parton

our topic #2

Topic #1: parton showers

or “How to connect widely separated scales in pQCD?”

Generic picture:

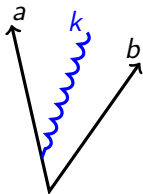
- “all-purpose” (Monte Carlo) Event generators to simulate collisions
- Most used tools in particle physics (Pythia, Herwig, Sherpa, ...)
- Central piece: parton shower (connecting hard to soft perturbative scales)

Monte Carlo generators

Generic picture:

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- Central piece: parton shower (connecting hard to soft perturbative scales)

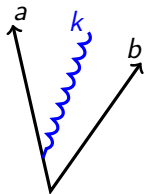
Main physics idea: gluon radiation from a $q\bar{q}$ dipole has 2 (IR) divergences



$$\text{soft: } E_k \rightarrow 0 \Rightarrow \int_{E_{\min}}^{E_{ab}} \frac{dE_k}{E_k} \alpha_s = \alpha_s \log(E_{ab}/E_{\min})$$
$$\text{collinear: } \theta_{ak} \rightarrow 0 \Rightarrow \int_{\theta_{\min}}^{\theta_{ab}} \frac{d\theta_{ak}}{\theta_{ak}} \alpha_s = \alpha_s \log(\theta_{ab}/\theta_{\min})$$

Widely disparate scales \Rightarrow logs resummed to all orders

Towards dipole showers

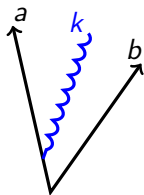


Use Sudakov parametrisation ($Q = (p_a + p_b)^2 = 2p_a \cdot p_b$):

$$k^\mu = z_a p_a^\mu + z_b p_b^\mu + k_\perp^\mu$$

$$k^2 \ll Q^2 (k^2 \approx 0) \Rightarrow z_{a,b} = \frac{k_\perp}{Q} e^{\pm\eta} \quad \text{with } \eta = \frac{1}{2} \log \frac{z_a}{z_b}$$

Towards dipole showers



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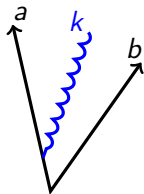
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Matrix element:

$$[dk] |\mathcal{M}|^2 \approx d\eta dk_\perp^2 \frac{d\phi}{2\pi} \frac{\alpha_s(k_\perp)}{4\pi} C_F \frac{z_a P(z_a) z_b P(z_b)}{k_\perp^2}$$

Towards dipole showers



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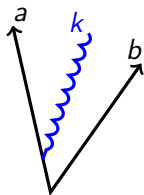
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- Soft: $k_\perp \ll Q$ ($\eta \approx 0$)
- Collinear: $z_{a,b} \rightarrow 0$ (i.e. η departs from ≈ 0)
- Soft&collinear: $k_\perp \ll Q$ and η away from 0

Towards dipole showers



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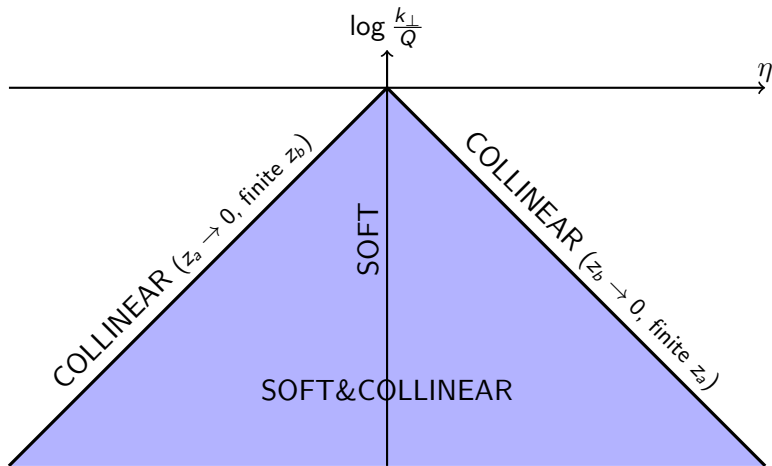
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Resummation of (leading) logarithms: $Q \gg k_{\perp 1} \gg k_{\perp 2} \gg \dots \gg k_{\perp n}$

Towards dipole showers

Convenient representation: the Lund plane



Topic #2: jets, jet substructure

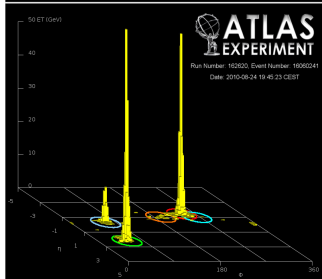
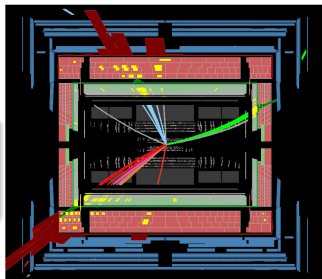
or “opening towards new phenomenology”

Central idea

Jet \equiv proxy for hard parton

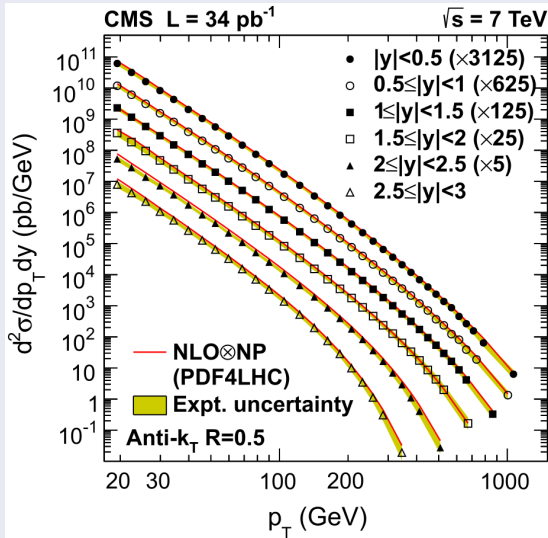
\Rightarrow carries info about the hard collision

- Ubiquitous at the LHC
used in more than 60% of the analyses
- Reconstructions of jets from particles
using dedicated **jet algorithms**
- **Calculable in perturbative QCD**
(NLO standard, sometimes NNLO)



40 years of jets for collider phenomenology

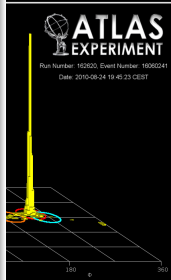
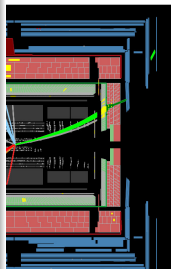
Jet cross-section at the LHC



Central idea

Jet \equiv proxy for
 \Rightarrow carries info

- Ubiquitous
used in many
- Reconstruction
using dedicated
- Calculable
(NLO standard)



Instead of using jets as “monolithic” objects
look at their internal dynamics



**JET
SUBSTRUCTURE**

Instead of using jets as “monolithic” objects
look at their internal dynamics

JET SUBSTRUCTURE

tagging
boosted
objects

machine
learning

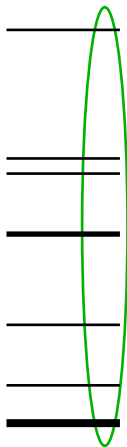
Pileup
mitigation

Heavy-ion
collisions

QCD
precision
pheno

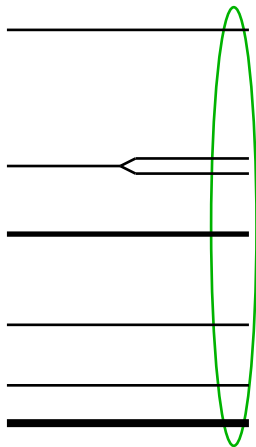
Frequent tool: Cambridge/Aachen (de-)clustering

Cambridge/Aachen: iteratively recombine the closest pair



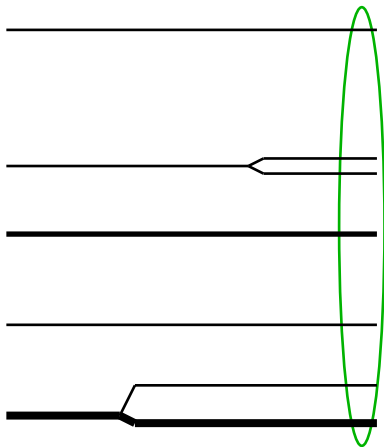
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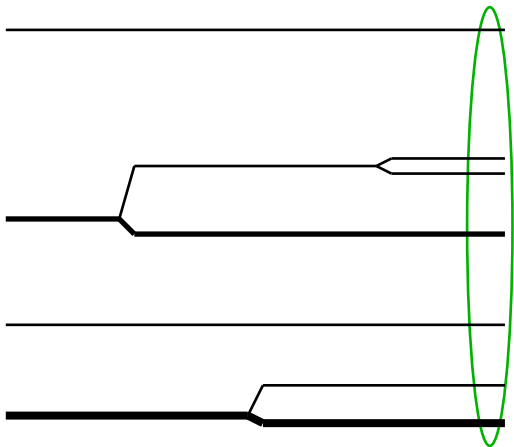
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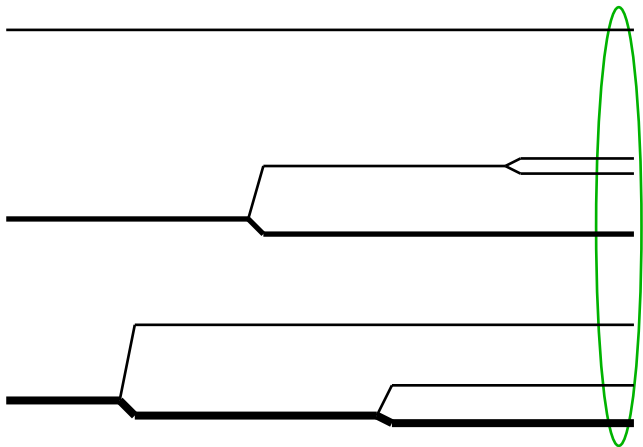
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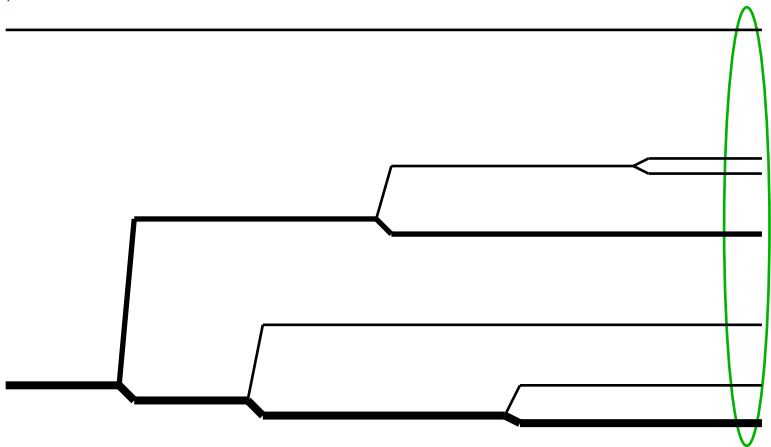
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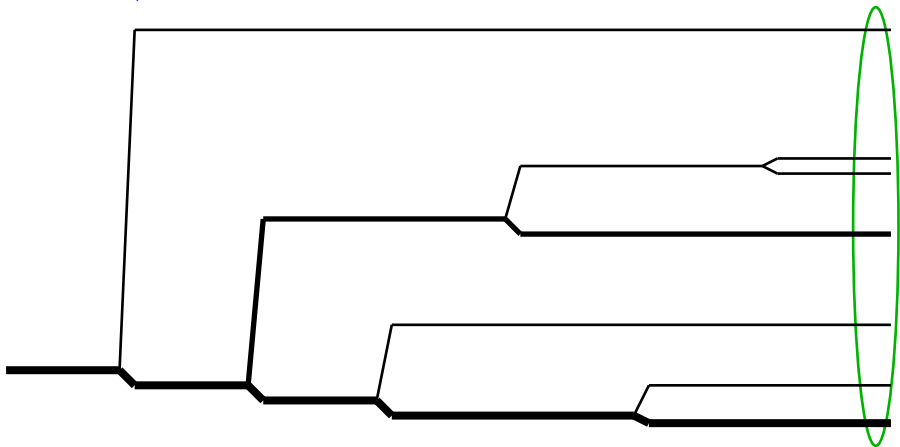
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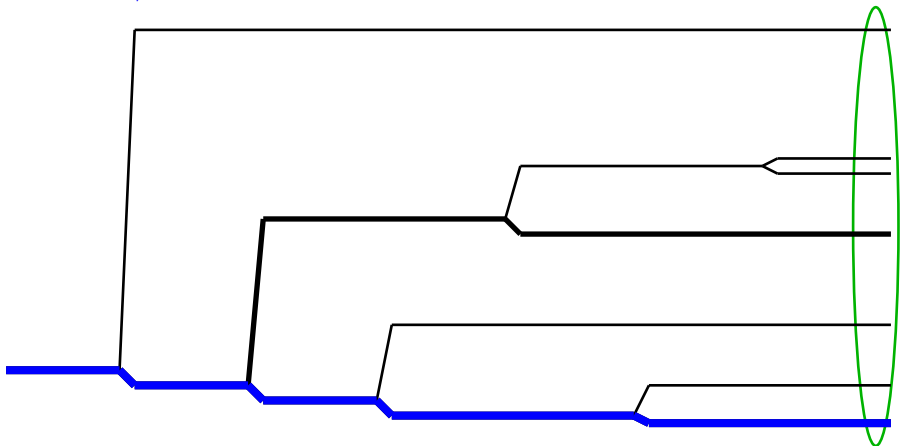
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Frequent tool: Cambridge/Aachen (de-)clustering

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Usage: iteratively undo the clustering to study internal jet dynamics

Typically: follow the hardest branch (largest p_t or z)

Instead of using jets as “monolithic” objects
look at their internal dynamics

JET SUBSTRUCTURE

tagging
boosted
objects

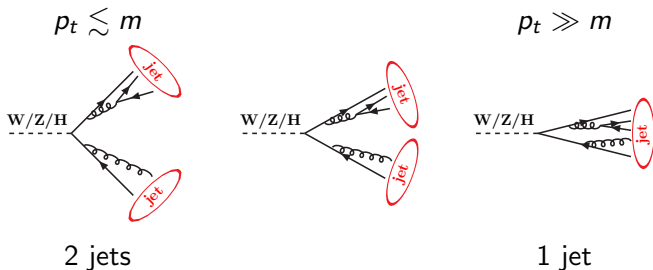
machine
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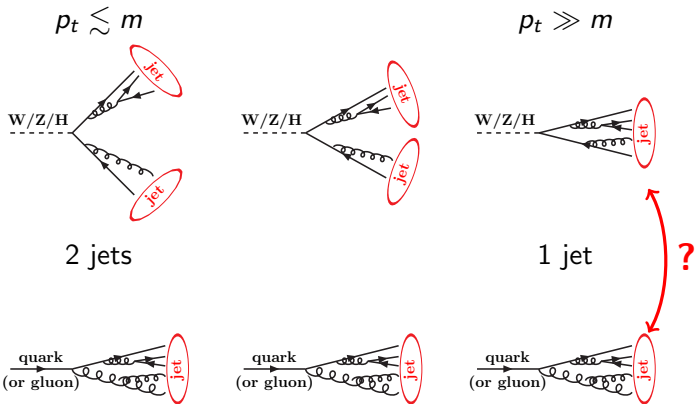
Boosted objects



(massive) objects produced boosted (energy \gg mass) are seen as 1 jet:

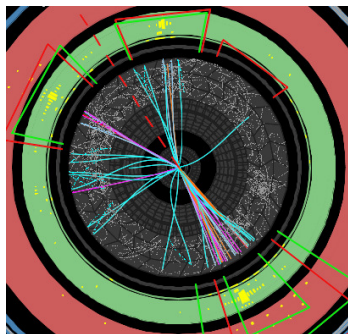
$$\theta_{q\bar{q}} \sim \frac{m}{p_t}$$

Boosted objects



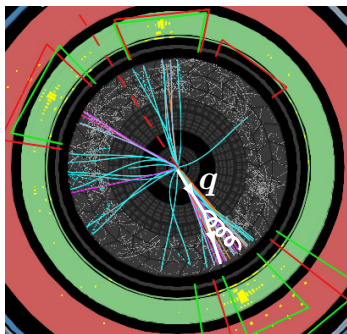
use substructure to separate from QCD jets

What jet do we have here?



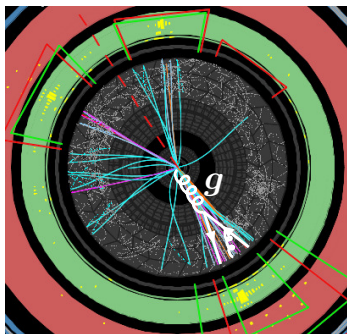
What jet do we have here?

- a quark?



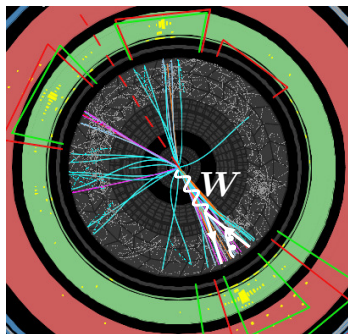
What jet do we have here?

- a quark?
- a gluon?



What jet do we have here?

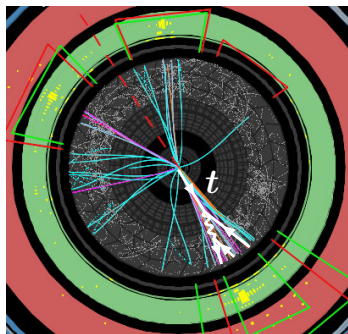
- a quark?
- a gluon?
- a W/Z (or a Higgs)?



What jet do we have here?

- a quark?
- a gluon?
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- a top quark?

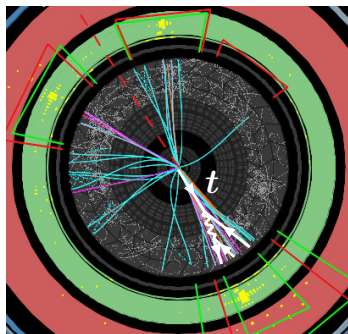
Source: ATLAS boosted top candidate



What jet do we have here?

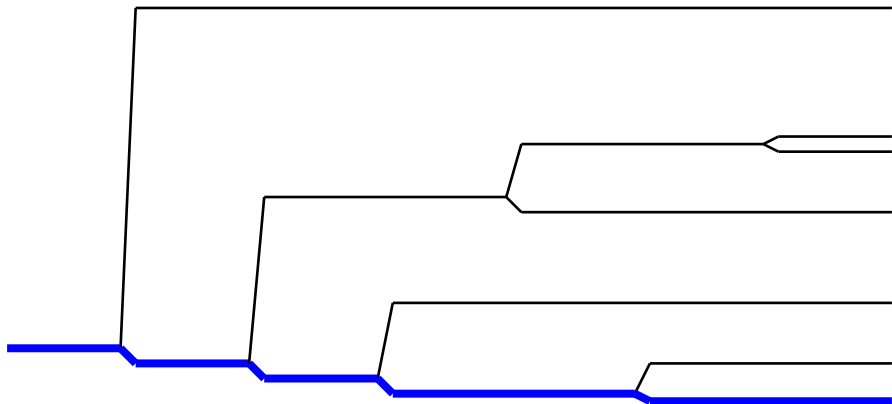
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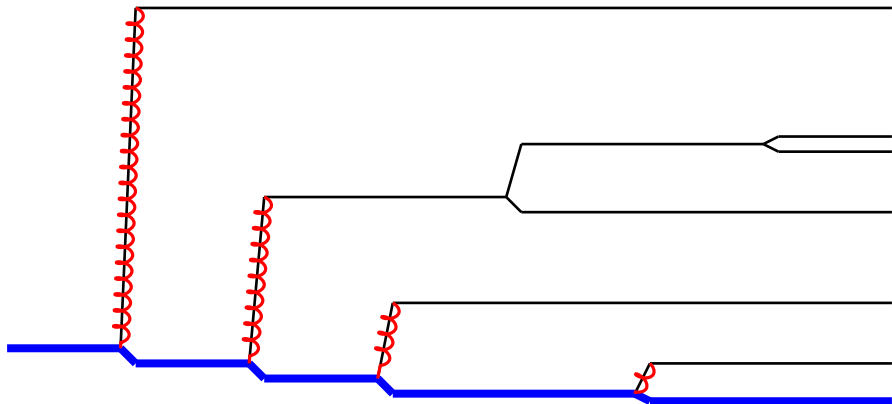


Many applications, e.g. relevant to new physics searches

Idea: look for hard branchings

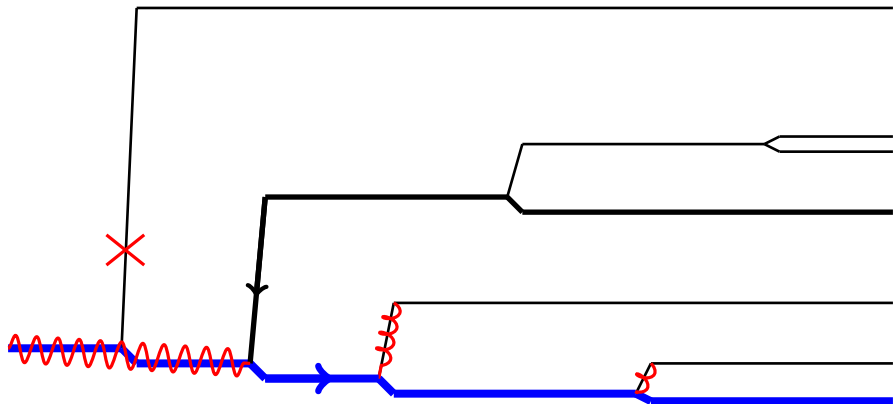


Idea: look for hard branchings



Rare hard branchings for $q/g \rightarrow q/g + g$ ($P(z) \sim 1/z$)

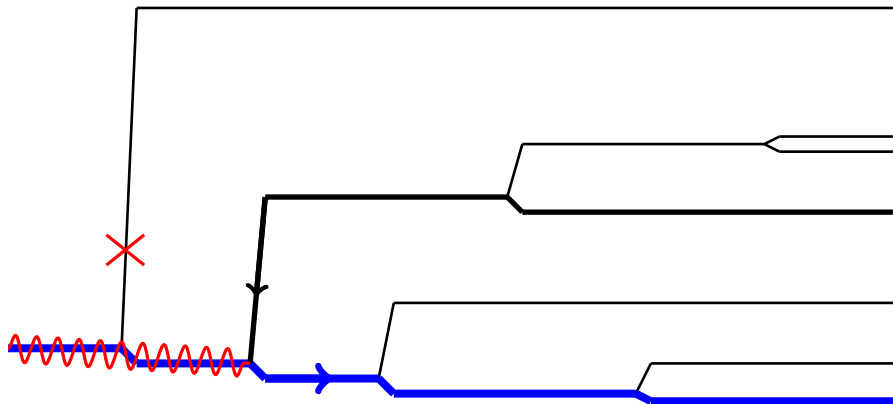
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Rare hard branchings for $q/g \rightarrow q/g + g$ ($P(z) \sim 1/z$)

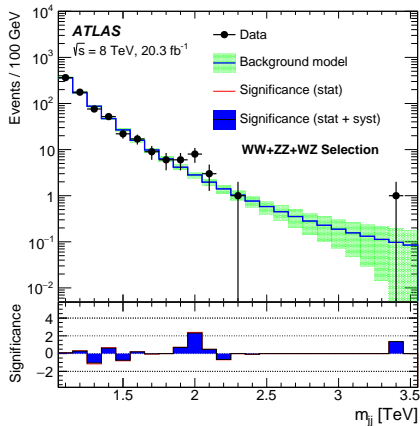
Frequent hard branchings for $W/Z/H \rightarrow q\bar{q}$ ($P(z) \sim 1$)

Idea: look for hard branchings



Method: search the first splitting with $z > z_{\text{cut}}$

Searches and measurements



(now-gone) di-boson excess (end of Run-I)

New prospects at the LHC

Instead of using jets as “monolithic” objects
look at their internal dynamics

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SUBSTRUCTURE**

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- Main idea:

Boosted jet $\Rightarrow p_t \gg m$

$$\Rightarrow \rho \equiv \frac{m^2}{p_t^2 R^2} \ll 1$$

\Rightarrow expect $\log \rho$ coming with α_s

\Rightarrow need for all-order resummation

Analytic approach to jet substructure

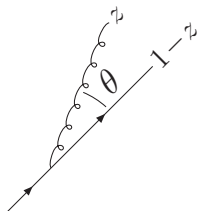
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- Example: jet mass with one (soft-and-collinear) gluon emission

$$\text{Prob}_1(> \rho) \simeq \int_0^1 \frac{d\theta^2}{\theta^2} \frac{dz}{z} \frac{\alpha_s C_R}{\pi} \Theta(z\theta^2 > \rho) \simeq \frac{\alpha_s C_R}{2\pi} \log^2(1/\rho)$$

Analytic approach to jet substructure

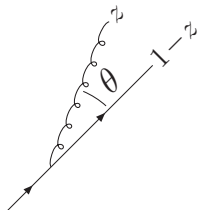
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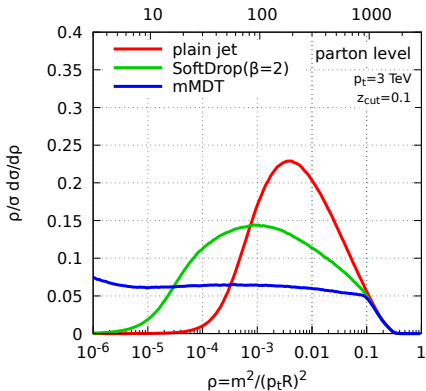
- Use the same Sudakov parametrisation as for “Monte-Carlo generators” seen earlier, but now treat things analytically

Understanding substructure tools

Breakthrough 5 years ago: jet substructure tools are calculable

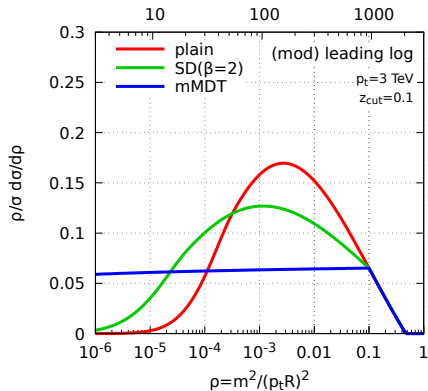
quark - Pythia (8.230)

m [GeV]



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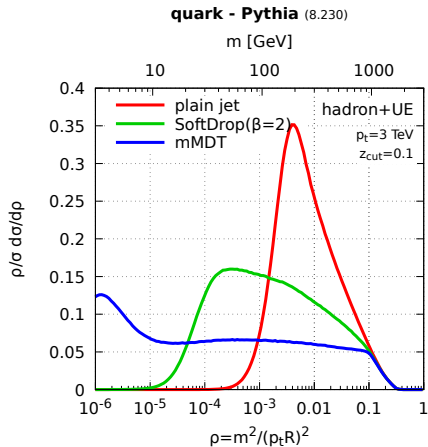
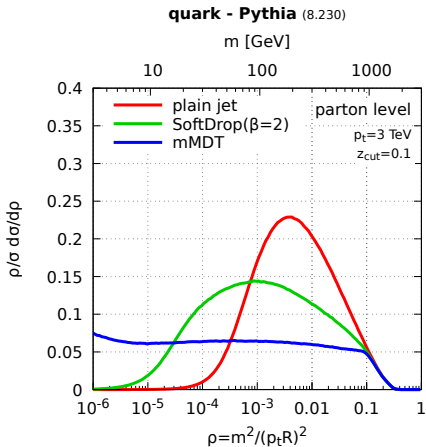
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- qualitative features reproduced and understood

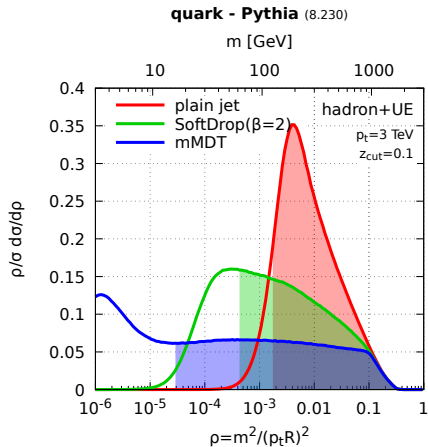
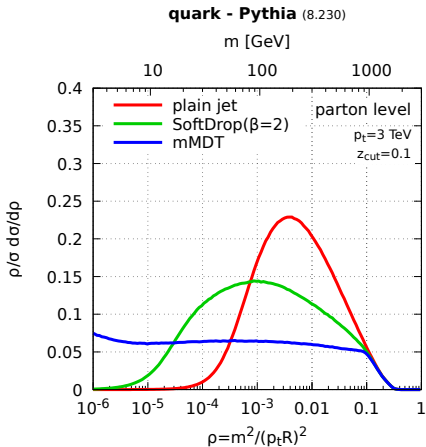
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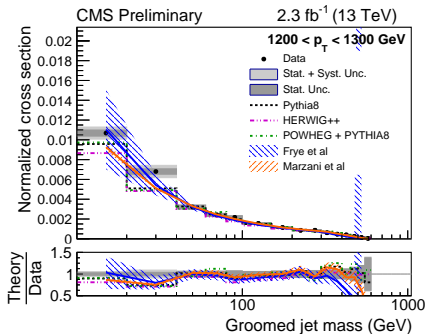
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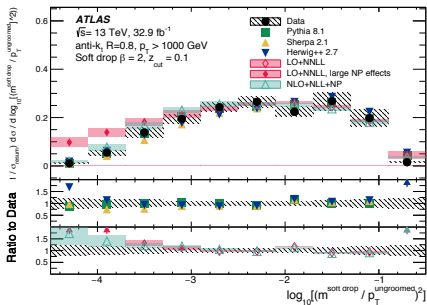
- qualitative features reproduced and understood
- substructure reduces non-perturbative effects

LHC measurements v. NLL+NLO and NNLL+LO predictions:

CMS-PAS-SMP-16-010



ATLAS(CERN-EP-2017-231)

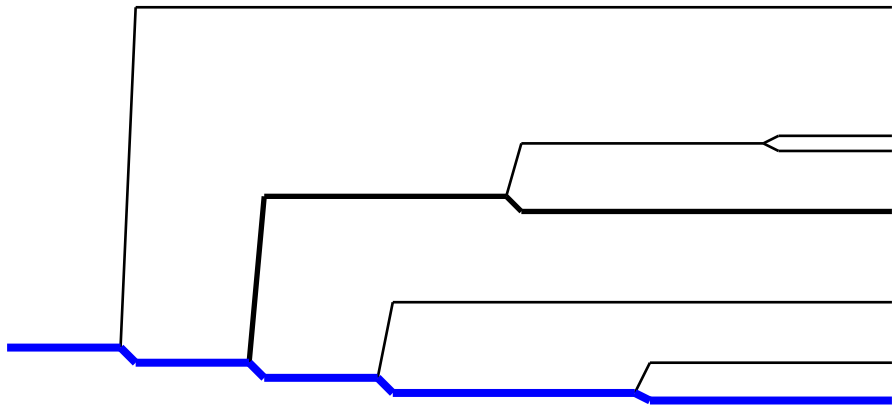


good overall agreement with the data

Precise observable, limited NP effects \Rightarrow can we extract α_s ?

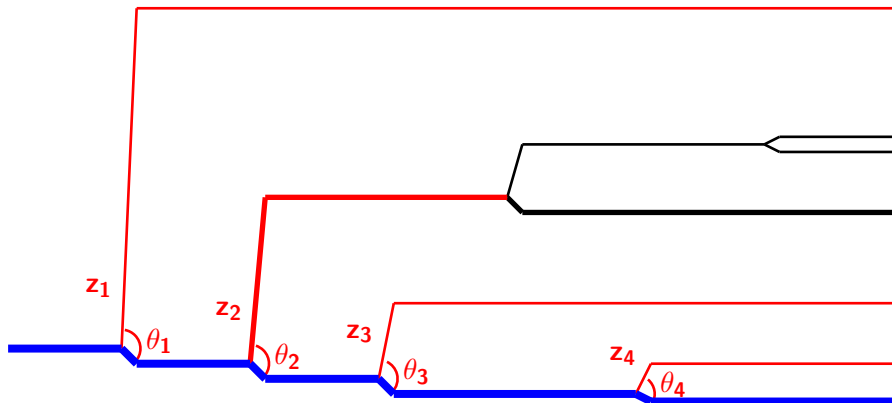
Visualising the substructure with the Lund plane

[F.Dreyer,G.Salam,GS,18]



Visualising the sustructure with the Lund plane

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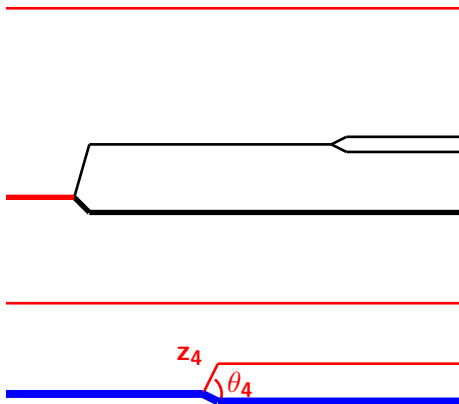
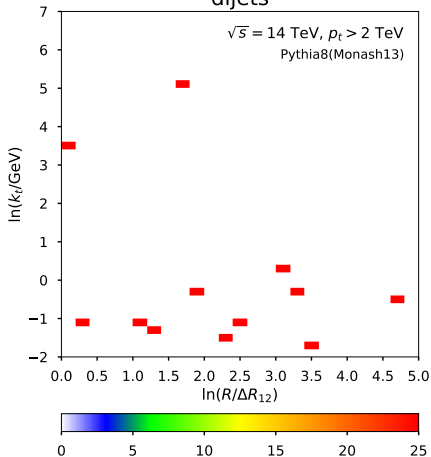


Consider all the emissions from the hardest branch

Visualising the substructure with the Lund plane

[F.Dreyer,G.Salam,GS,18]

One jet
dijets

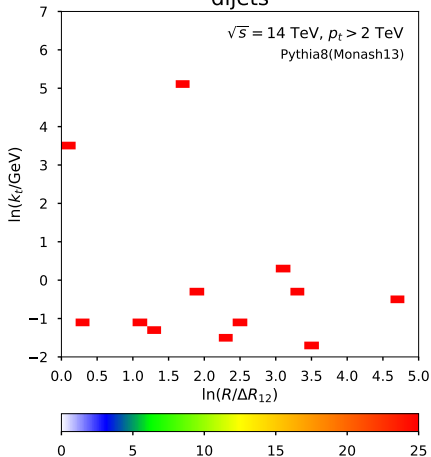


Consider all the emissions from the hardest branch
Put them in the Lund plane

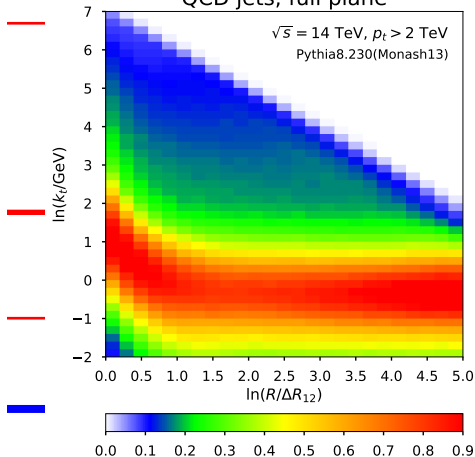
Visualising the substructure with the Lund plane

[F.Dreyer,G.Salam,GS,18]

One jet
dijets

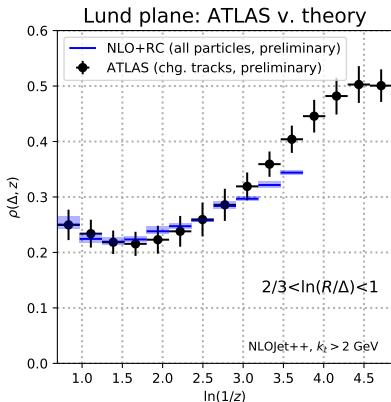
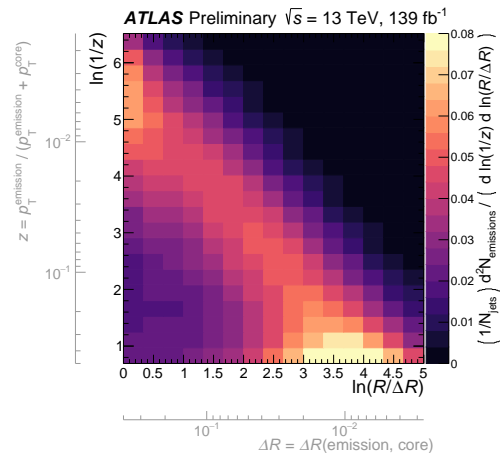


Average over jets
QCD jets, full plane



Consider all the emissions from the hardest branch
Put them in the Lund plane

Measured by ATLAS at the LHC



Instead of using jets as “monolithic” objects
look at their internal dynamics

JET SUBSTRUCTURE

tagging
boosted
objects

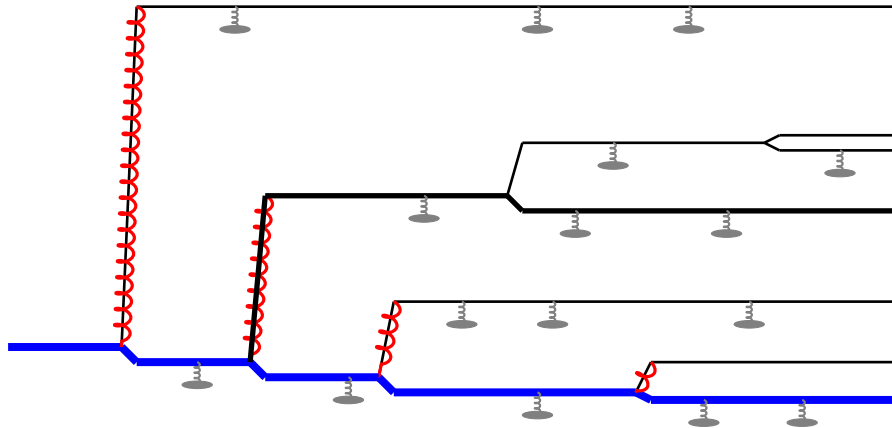
machine
learning

Pileup
mitigation

QCD
precision
pheno

Heavy-ion
collisions

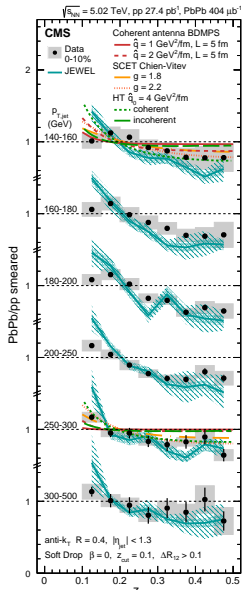
Idea: interaction with the quark-gluon plasma



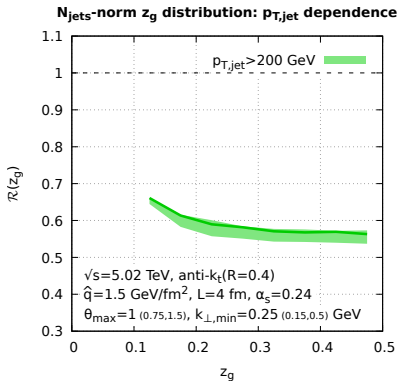
Method: look at the z fraction of the first splitting with $z > z_{\text{cut}}$

Measuring the splitting function

CMS (CMS-HIN-16-006)

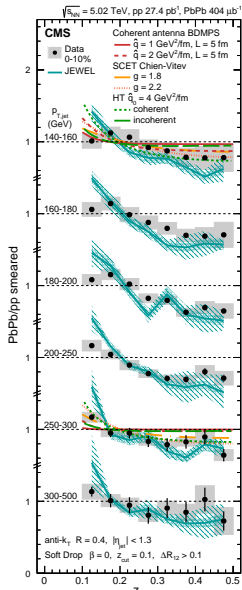


our Monte Carlo

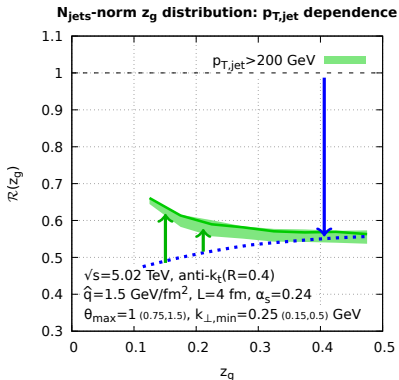


Measuring the splitting function

CMS (CMS-HIN-16-006)



our Monte Carlo



- Reduction from E loss
- Peak from extra emissions

Rich high-energy QCD pheno “close to the light-cone”

- Probe a range of widely-separated scales
- Monte-Carlo Event generators
 - ▶ Connect hard process to Λ_{QCD}
 - ▶ On-going project: improve parton-shower logarithmic accuracy
- Jets
 - ▶ Ubiquitous at colliders
 - ▶ Fast and efficient algorithms
- Jet substructure has many applications
 - ▶ boosted-object tagging (e.g. for searches)
 - ▶ QCD tools and precision physics
 - ▶ QGP/jet quenching in heavy-ion collisions
 - ▶ pileup mitigation
 - ▶ machine learning