A brief review of Leptogenesis

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Why Leptogenesis??

- Explain within a consistent theoretical model the mechanism for Baryogenesis.
- Need a dynamical mechanism that will start out with $Y_B = 0$ and lead to $Y_B \neq 0$.
- Can this observable be related to other physics, such as neutrinos?
  - Neutrino masses and mixings consistent with recent neutrino data can successfully give the right amount of baryon asymmetry.
- Need extension of the Standard Model (SM) and large enough CP violation in lepton sector is allowed.
- Fully exploits effects of departures from thermal equilibrium in the evolution of the early Universe!!!!!
- Focus has moved from understanding the qualitative features to detailed quantitative analysis.
Leptogenesis Basics

1. Need mixing/interference between (at least) two different states (typically flavour, CP-eigenstates,...)
2. All possible mechanisms of CP-violation can generically be implemented.
3. Important to carefully consider the dynamics in the background of an expanding Universe, then $n_B \neq n_{\bar{B}}$
4. Relevance of L and B-L conserving processes to determine the (asymmetric) densities of the different species.
5. Hard to test,....easier to falsify
Basics of CP violation in See-saw Lepton Sector

Parameter counting...low energy: \[ \mathcal{L} = -\frac{1}{2} \nu^T m_\nu \nu + h.c. \]

- 12 parameters in lepton sector: 6 masses, 3 mixing angles, 3 phases
- Have measured 7, 1 upper limit, 1 unknown mass and 3 unknown phases
- At low energy 1 Dirac phase related to flavour à la CKM. This CP violation in leptons NOT related to lepton number violation!!

Parameter counting...high energy:
\[ \mathcal{L}_{NP} = \lambda_{\alpha i} \ell_\alpha \phi N_i + h.c. + M_i N_i N_i \]

- 3 charged fermion masses, 3 RH neutrino masses + 15 parameters from complex Yukawa matrix!!!
- Cannot easily disentangle LH and RH contributions at low energy....
Leptogenesis Mechanism

Based on standard out-of-equilibrium decay of a heavy particle....(e.g. RH neutrino):

1. CP violating decay of a heavy particle through a Lepton number -violating interaction can produce a lepton asymmetry.
2. This lepton asymmetry is transformed into a baryon asymmetry through sphaleron interactions.

Fukugita, Yanagida
CP Asymmetry

- CP violation through phases in lepton sector.
- CP asymmetry produced through interference of tree and one-loop contribution of decay rate. The loop must also violate lepton number.
- CP asymmetry determined by the particle physics model that produces couplings and masses for $\nu_R$. Connection with low scale CP violating observables is model dependent.

$$\epsilon = \frac{\Gamma(N_1 \to \phi + \bar{\ell}) - \Gamma(N_1 \to \ell + \bar{\phi})}{\Gamma(N_1 \to \phi + \bar{\ell}) + \Gamma(N_1 \to \ell + \bar{\phi})}$$
Spectator effects

Consider all processes that conserve B-L. For a given T, from chemical equilibrium considerations we solve the system of equations that are derived from requiring/having:

- Total isospin, hypercharge and color must be zero
- Flavor changing interaction in the quarks are in equilibrium
- Yukawa interactions in equilibrium
- Electroweak and QCD sphalerons in equilibrium
- With SUSY additionally particles in same multiplet have $\tilde{\phi} = \phi$

Solve for $B$, $L$, $B - L$ in terms of a chemical potential, say $\ell$. However, in SUSY there are relevant mass-dependent effects from sparticles.

Chung, Garbrecht, Tulin
Relevant processes to include in the BE

Coupled system for $n_X$ and $n_{B-L}$,

\[
\frac{dn_X}{dt} + 3Hn_X = \left[ \frac{n_X}{n_X^{eq}} - 1 \right] (\gamma_D + \gamma_a)
\]

\[
\frac{dn_{B-L}}{dt} + 3Hn_{B-L} = \epsilon \left[ \frac{n_X}{n_X^{eq}} - 1 \right] \gamma_D - \frac{n_{B-L}}{n_L^{eq}} \gamma_W
\]

$\epsilon \rightarrow$ CP Asymmetry

$\gamma_W$ dissipation at $T \lesssim M$

$\gamma_D, \gamma_a$ control departure from thermal equilibrium

- $N$ decays and inverse-decays
- $\Delta L = 1$ scatterings
- $\Delta L = 2$ scatterings

- for non-singlet decaying particles must include annihilations through gauge interactions
Intuitively what should be important is the direction in flavour space into which $N_1$ decays. Given that $h_e, h_\mu, h_\tau$ are small and the lepton asymmetry is obtained from a trace in flavour space how can flavour matter? Flavour distinguishes mass eigenstates.....

- So, consider temperatures where $\Gamma_\tau, \Gamma_\mu \gg H$
  - charged lepton Yukawas have no effect of the CP asymmetry BUT
- the dynamical process of RH neutrinos decay and production and the corresponding lepton asymmetry is distributed among distinguishable flavours.
- charged lepton Yukawa interactions have the effect of projectors, asymmetries in each flavour are washed out differently, contributing with different weights in the expression for the total asymmetry.
Flavoured vs. Unflavoured

\[ \mathcal{L}_{yukawa} = \lambda_{\alpha 1}^* \bar{\ell}_\alpha N_1 \phi + h_{\alpha \beta} \bar{\ell}_\alpha e_\beta \phi + h.c. \]

Different basis give different results:

\[ \mathcal{L}_{yukawa} = \lambda_1^* \bar{l}_1 N_1 \phi + h_{i \beta} \bar{l}_i e_\beta \phi + h.c. \]

\[ \mathcal{L}_{yukawa} = \lambda_{\alpha 1}^* \bar{\ell}_\alpha N_1 \phi + h_{\alpha} \bar{\ell}_\alpha e_\alpha \phi + h.c. \]

One-flavour

\[ Y_B \approx \frac{1}{g^*} \sum \eta_\alpha \sum \epsilon_\alpha \]

\[ = \frac{1}{g^*} \eta \epsilon \]

Flavoured

\[ Y_B \approx \frac{1}{g^*} \sum \eta_\alpha \cdot \epsilon_\alpha \]
Decay rate and CP revisited

<table>
<thead>
<tr>
<th>Unflavoured</th>
<th>Flavoured</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\epsilon, \tilde{m}_1, M_1, \tilde{m}^2$</td>
<td>$\epsilon_\alpha, \tilde{m}_{1\alpha}$</td>
</tr>
<tr>
<td>$\Gamma = \frac{1}{8\pi} (\lambda \lambda^\dagger)_{11} M_1 = \frac{\tilde{m}_1 M_1^2}{8\pi v^2}$</td>
<td>$\Gamma_\alpha = \frac{1}{8\pi}</td>
</tr>
<tr>
<td>$K \equiv \frac{\Gamma}{H}</td>
<td>T=M_1 = \frac{\tilde{m}<em>1}{\tilde{m}</em>*} &lt; 1$</td>
</tr>
<tr>
<td>$\eta(\tilde{m}_1, \tilde{m}^2)$</td>
<td>$\eta_\alpha(\tilde{m}_{1\alpha})$</td>
</tr>
<tr>
<td>$\eta \propto \frac{H}{\Gamma}$</td>
<td>$\eta_\alpha \propto \frac{H}{\Gamma_\alpha}$</td>
</tr>
<tr>
<td>$M_1 \gtrsim 10^9 \text{GeV} \left( \frac{2.5 \times 10^{-3} \text{eV}^2}{\Delta m_{atm}^2} \right)^{1/2}$</td>
<td>decreases bound $M_1$</td>
</tr>
<tr>
<td>$\epsilon \leq \epsilon_{\text{max}} = \frac{3}{16\pi} \frac{M_1}{v^2} \frac{(\Delta m_{atm}^2 + \Delta m_{sol}^2)}{m_3}$</td>
<td>$\epsilon_\alpha = \leq \frac{\sqrt{3} M_1 \tilde{m}}{8\pi v^2}$ increases $\tilde{m}$</td>
</tr>
<tr>
<td>$\tilde{m} &lt; 0.15 \text{eV}$</td>
<td></td>
</tr>
</tbody>
</table>

Note: The above table contains expressions for the decay rate and CP violation in both unflavoured and flavoured cases, along with inequalities and bounds for the parameters involved.
Purely Flavoured Leptogenesis

Consider first the SM + seesaw, using the Casas-Ibarra parametrization:

$$\lambda_{\alpha k} = \frac{1}{v} \left[ U^\dagger \sqrt{m_\nu} \cdot R \sqrt{M_N} \right]_{\alpha k}$$

Flavour CP asymmetries:

$$\epsilon_\alpha = \text{Im} \left( F[m_\nu, M, R]_{ji} \times U_{j\alpha} U_{i\alpha}^* \right)$$

Total CP asymmetries:

$$\epsilon = \frac{M_1 M_k}{v^4} \text{Im} \left( \left( \sum_i m_{\nu_i} R_{i1}^* R_{ik} \right)^2 \right)$$
In the generic case it is very difficult to separate CP violating sources and it is not possible to infer in the see-saw the value of the CP asymmetry from low energy observables.

Specific models can find some correlations by minimizing the number of parameters through: family symmetries, textures, 2RHN, etc

Assuming that $R$ is real. We see,

- $\epsilon_\alpha$ will depend only on the neutrino mixing matrix $U$
- $Y_B \neq 0$ even with $\epsilon = 0$ as long as $\epsilon_\alpha \neq 0$.

→ A real R matrix implies that there is no CP violation from RH sector AND also that possible CP violation at low energy could be correlated to the CP violation that produced the BAU!! VERY MODEL DEPENDENT STATEMENT!!!!!
Purely Flavored Leptogenesis

In this type of models it is possible to generate the baryon asymmetry even in the case in which \( \sum \epsilon_\alpha = 0 \) without lepton number violation in decay.

- The BE for lepton flavour asymmetries in general present different washouts in the different flavours so.....
  \[ Y_{B-L} \propto \sum \eta_\alpha \epsilon_\alpha \neq 0 \]

- Rely on the condition that the dynamics of the different lepton flavors are decoupled at the leptogenesis temperature.

- CP violation can originate from the non leptonic sector/lepton number conserving loop

- Nice check that in the single flavour approximation \( Y_{B-L} \to 0 \)

- Case with lepton flavour violation (LFV). No need to have lepton number violation in the loop, lepton number violation only via the washout processes.
Consequences of Purely Flavor Leptogenesis

- In this type of models one can have enhancements in the CP asymmetry originating from the introduction of additional scales or couplings.
- The additional coupling can decouple the neutrino mass dependence from the out of equilibrium condition and CP-asymmetry such that leptogenesis can occur at much lower scales.

\[ \epsilon \sim \frac{h^\dagger h \lambda \lambda}{h^\dagger h} \]

This implies that either:
- Relax the tension between the neutrino masses and large enough CP violation allowing a smaller \( T (M_1) \) for leptogenesis
- Decouple the neutrino masses, out of equilibrium constraint and CP violation

However, these were precisely the issues that motivated leptogenesis!!!!
Take a flavour symmetry $U(1)_F$ such that the coupling $\bar{\ell}NH$ is not allowed.

For $M_F \gg M_N$: $\tilde{\lambda}_{\alpha k} = \left(h\frac{<S>}{M_F}\lambda^\dagger\right)_{\alpha k}$. So $m_\nu \sim \mathcal{O}(\tilde{\lambda}^2)$.

CP asymmetries:

$$\epsilon = \sum_{\alpha} \epsilon_{\alpha} = 0; \quad \epsilon_{\alpha} \neq 0 \sim \mathcal{O}(h^2) \quad (1)$$

Decoupling $\epsilon_{\alpha}$ from $\tilde{m}_{\alpha}$, $m_\nu$ allows to lower $T_{LG} \sim \text{TeV}$. 

Symmetries and Lepton number violation

D.Aristizabal, ML, E. Nardi 08, D. Aristizabal, L. Muñoz, E. Nardi 08
In the presence of LFV, fast $\ell_\alpha \rightarrow \ell_\beta$ transitions effectively eliminate all dynamical flavor effects.

If at $T_{LG}$ the LFV processes are in chemical equilibrium then there are no flavour effects and the one-flavour approximation correctly describes the production of the lepton asymmetry.

Must be included in the chemical equilibration/BEs and Spectator processes become more relevant.

In general, models of new physics have new sources of LFV, so it is not immediate that flavour effects will survive.

Some interesting examples
LFE effects in SUSY

Model with soft $m_{\alpha\beta}^2$ gives rise to new diagrams that could contribute to a lepton asymmetry via PFL à la soft leptogenesis.

Flavour CP asymmetries which are enhanced as $\propto g^2 \lambda$, but $\epsilon = \sum_{\alpha} \epsilon_{\alpha} = 0$.

Ineffective because lepton flavour densities equilibrate very fast, so ...LG described by single flavour approximation, which cannot be sourced by the type of diagram above.
Spectators again

- $T > 10^{13}$ GeV: Higgs asymmetry enhances washout-effects $\rightarrow$ Suppression of $Y_{B-L}$ by $\sim 0.4$
- $T < 10^8$ GeV: Lepton asymmetry transferred into baryons and into SU(2)-singlets $\rightarrow$ Enhancement of $Y_{B-L}$ by $\sim 0.2$

Buchmuller, Plumacher; Nardi, Nir, Racker, Roulet

- $T \lesssim 100$ TeV: With lepton flavor equilibration, in SUSY models via soft leptogenesis, $\rightarrow$ possible large enhancements ($\sim 5$) of $Y_{B-L}$ when strong washout dependence exists.

Aristizabal, Losada, Nardi
Dimension six operators and the seesaw

- **L-violating dim 5:** \((\ell \phi)^2 \rightarrow \epsilon_\alpha \propto \mathcal{I} m \left( \lambda_{j\alpha} \lambda_{i\alpha}^* \left[ \frac{3}{\sqrt{2} x_j} (\lambda \lambda^\dagger)_{j1} \right] \right)\)

- **L-conserving dim 6:**
  \[ (\bar{\ell} \phi^*) \partial (\ell \phi) \rightarrow \epsilon_\alpha \propto \mathcal{I} m \left( \lambda_{j\alpha} \lambda_{i\alpha}^* \left[ \frac{1}{x_j} (\lambda \lambda^\dagger)_{1j} \right] \right) \]

Non-unitarity in lepton mixing through dimension 6 terms.

1. enforce global U(1) to suppress dim 5 terms but **NOT** dim 6.
2. so can have PFL, with \(\epsilon_\alpha \neq 0\), but \(\sum \epsilon_\alpha \sim 0\).
3. flavour asymmetries are not strongly correlated to \(\nu\) masses so can be large.

Need hierarchy in RH \(\nu\) to be small to produce a large enough \(Y_B\). This induces fast lepton flavour violating rates. So for \(M_1 \lesssim 10^8\), LFE does not allow a large enough baryon asymmetry. \(\rightarrow\) LFE sets a lower bound on \(M_1\).
Recent Highlights/Questions in Leptogenesis

- Validity of kinetic equilibration assumption requires use of full BE $\rightarrow$ effects can enhance/suppress $Y_{B-L}$ in different scenarios.
- Quantum effects can be relevant e.g. resonant leptogenesis with MLFV.
- Possible signatures at colliders from decay of (particles with additional interactions to) heavy particle, e.g. triplet scalar: double charged Higgs decay to same sign leptons or Z’s from additional U(1).
- Separation of CP violation and lepton number violation in the decay is now possible. Lepton number violation can be introduced purely through washout effects: PFL.
- Can have strong implications in soft leptogenesis.
- Possible relevance of symmetries to induce correlations between low energy observables and LG parameters.
- Properties of R matrix can have implications on the final CP flavour asymmetries.
Summary

- Non-zero $\nu$ masses can be explained via the see-saw mechanism → has all necessary ingredients for LEPTOGENESIS
- For $T < 10^{12}$ GeV the flavour basis is fixed! → can enhance significantly the value of $Y_{B-L}$
- Possible mechanisms to enhance CP asymmetry with implications on LH and RH neutrino mass bounds
- Many corrections can significantly affect the importance of the washout processes
- Many interesting models are viable: soft, Dirac, resonant, electromagnetic, PFL
- Indirect support from neutrinoless double beta decay or CPV in neutrinos is detected
- Direct tests are extremely hard.
- Useful properties of the R matrix can be useful to determine quantitative implications for leptogenesis.
- Leptogenesis is STILL interesting.