

# Study of Charmless Hadronic $B$ decays at $BABAR$

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Representing  
the  $BABAR$  Collaboration



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# Motivations

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- Charmless hadronic  $B$  decays are sensitive probes to investigate potential effects of new physics:
  - shift of time-dependent  $CP$ -asymmetries;
  - suppression/enhancement of branching fractions;
  - ... ;
- “Polarization puzzle”: in several  $VV$  decays (such as  $\phi K^*$  or  $\rho K^*$ ) the longitudinal polarization fraction  $f_L$  is  $\sim 0.5$ , contrary to the prediction of  $f_L \sim 0.9$  based on simple helicity arguments. Still to be fully explained;
- We can investigate new/poorly known resonances through the Dalitz Plot analysis of charmless three-body  $B$  decays;

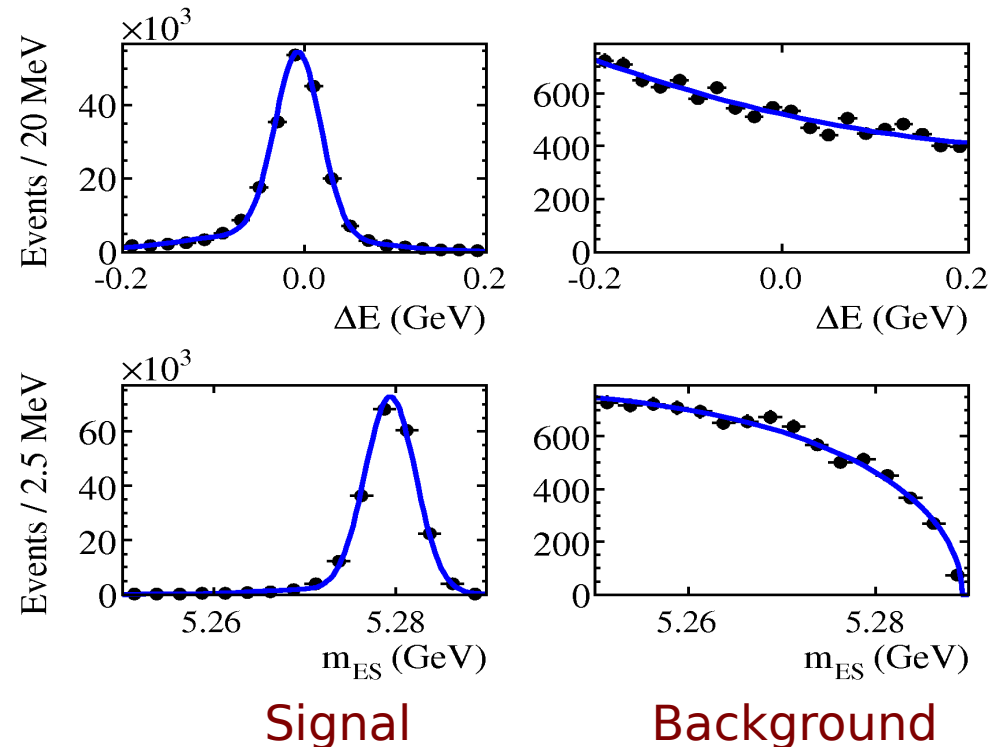
The measurements I will present today exploit the full BaBar dataset ( $\sim 465 \times 10^6$   $B\bar{B}$  pairs).

# Kinematics of $B$ decays

- Fully reconstructed  $B$  mesons: two variables are commonly used (exploiting the precise knowledge of the beam energy):

$$\Delta E = E_{meas} - E_{beam}$$

$$m_{ES} = \sqrt{E_{beam}^2 - \mathbf{p}_{meas}^2}$$



- Dominant background:  $q\bar{q}$  ( $q = u, d, s, c$ ). Reduced by means of a Fisher discriminant / Neural Network exploiting event shape variables ( $B\bar{B}$  events are spherical,  $q\bar{q}$  jet-like)

# Two-body Decays

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- Search for  $B \rightarrow \eta' \rho, \eta' f_0, \eta' K^*$ ;

arXiv:1004.0240 [hep-ex] - Accepted by PRD-RC

- Search for  $B^+ \rightarrow a_1^+ K^{*0}$ ;

arXiv:1007.2732 [hep-ex] - Submitted to PRD-RC

# Two-body: motivations

- Search for  $B \rightarrow \eta' \rho, \eta' f_0, \eta' K^*$ :

- Confirm the predicted pattern of interference for  $B \rightarrow \eta/\eta' X$  decays;

- Discrepancies among theory models in the predicted BF of  $B \rightarrow \eta' \rho^+$ . Also poor agreement between Belle's result and previous BaBar analysis;

$B^+ \rightarrow \eta' \rho^+$	Predicted $\mathcal{B}(10^{-6})$
SCET	$0.4^{+3.2}_{-0.2}$
QCDF	$6.3^{+2.8}_{-3.3}$
pQCD	$8.7^{+3.3}_{-2.5}$

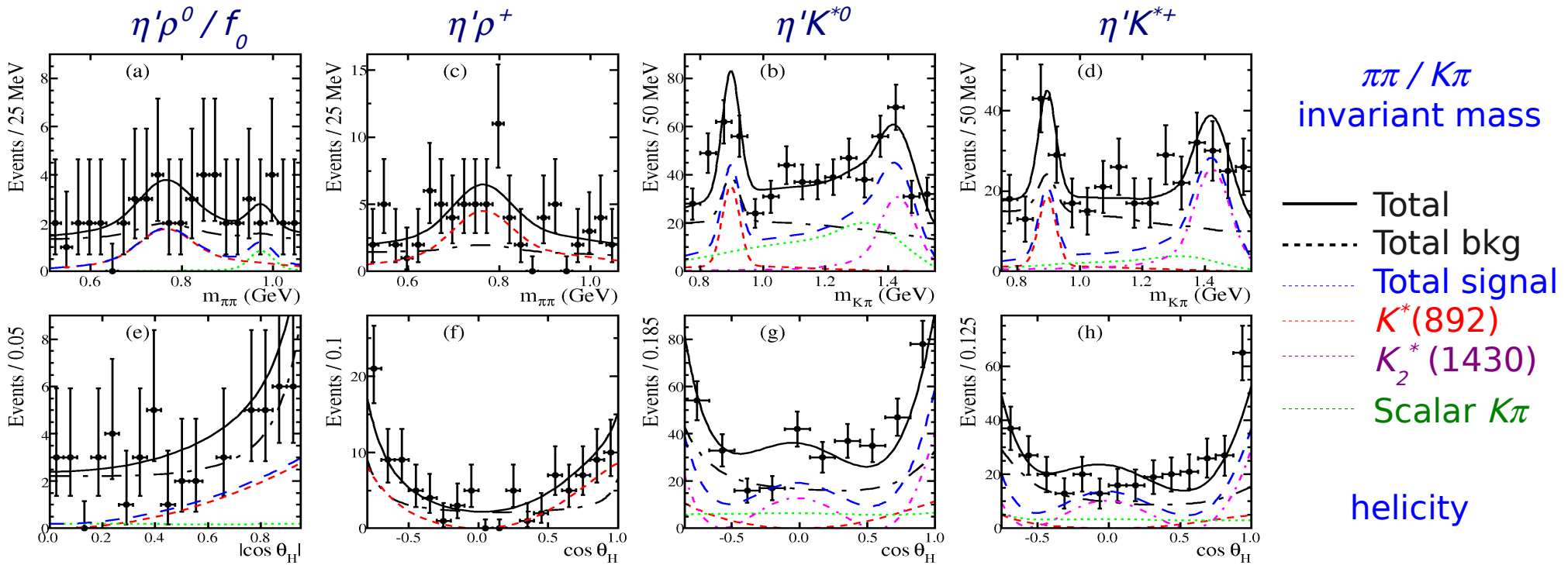
- We fit simultaneously for **three  $K^*$  components**:  $K^*(892)$ ,  $K_2^*(1430)$ , and the scalar  $K_0^*(1430)$  + non-resonant  $K\pi$  (we use the LASS parameterization) ;

- Search for  $B^+ \rightarrow a_1^+ K^{*0}$ :

- Verify and constrain theory models: QCDF predicts a BF  $\sim 11 \times 10^{-6}$ , while naïve factorization predicts  $\sim 10^{-6}$ ;

- Investigate the polarization puzzle.

# Search for $B \rightarrow \eta' \rho / \eta' f_0 / \eta' K^*$



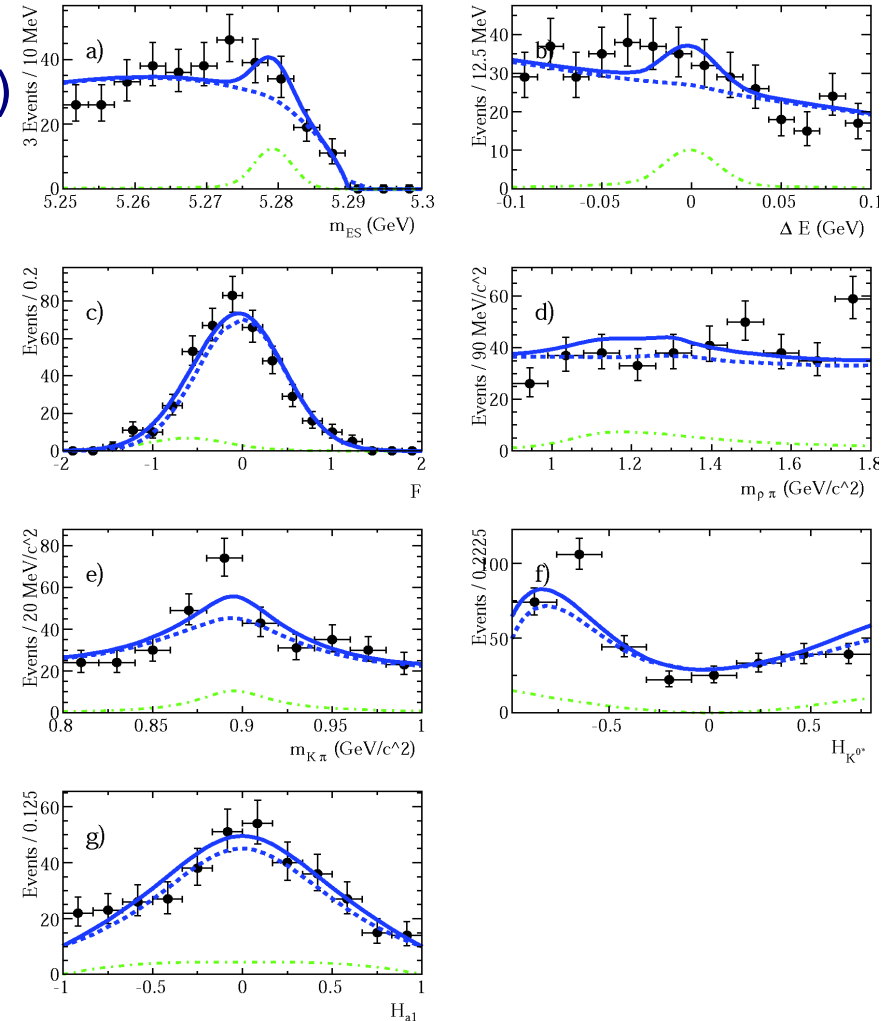
- First observation of:  $\eta' \rho^+$ ,  $\eta' K_0^*(1430)^0$ ,  $\eta' K_2^*(1430)^+$ ,  $\eta' K_2^*(1430)^0$ ;
- Evidence of:  $\eta' K^*(892)^+$ ,  $\eta' K^*(892)^0$ ,  $\eta' K_0^*(1430)^+$ ;
- Our result on  $\eta' \rho^+$  favors the predictions of pQCD and QCDF, confirmed suppression of  $\eta' K^*$  with respect to  $\eta K^*$ ;
- **Enhancement of the tensor component  $K_2^*(1430)$  over the vector  $K^*(892)$  not anticipated by the theory. This was observed also in  $\omega K^*$ , but not in  $\eta K^*$ .**

# Search for $B^+ \rightarrow a_1^+ K^{*0}$

- Maximum likelihood fit to the variables:  
 $m_{ES}$ ,  $\Delta E$ , Fisher,  $m(\rho\pi)$ ,  $m(K\pi)$ ,  $H(a_1)$ ,  $H(K^*)$
- No significant signal found, we set the upper limit:

$$\text{BF}(B^+ \rightarrow a_1^+ K^{*0}) \times \text{BF}(a_1^+ \rightarrow \pi^+ \pi^- \pi^+) < (1.8 \times 10^{-6}) \text{ (at 90\% CL)}$$

- Naïve factorization predictions favored over QCDF;
- Dominant systematic uncertainty from ignorance about  $f_L$  (nominal fit with  $f_L = 1$  to get the most conservative upper limit).



# Three-body Decays

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- Inclusive branching fraction of  $B^+ \rightarrow K^+ \pi^0 \pi^0$  ;

arXiv:1005.3717 [hep-ex] - Presented at FPCP 2010

- Observation of the rare decay  $B^0 \rightarrow K_S^0 K \pi$  ;

arXiv:1003.0640 [hep-ex] - Submitted to PRD-RC

- Amplitude analysis of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  ;

Presented at FPCP 2010

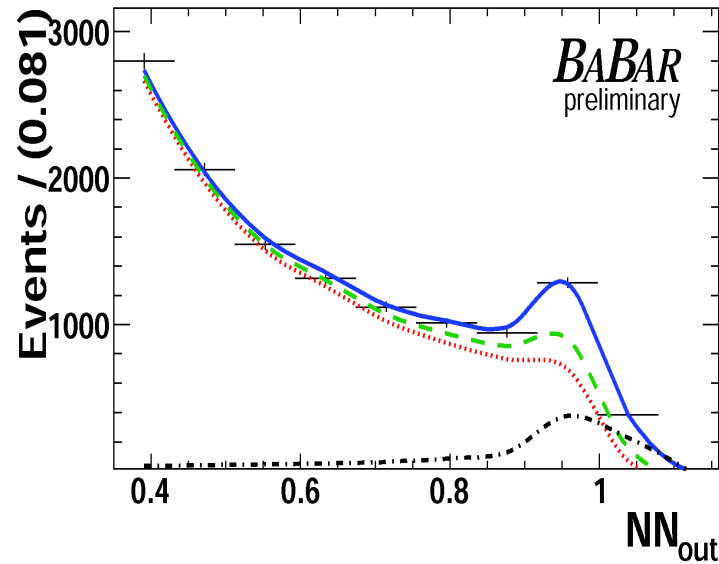
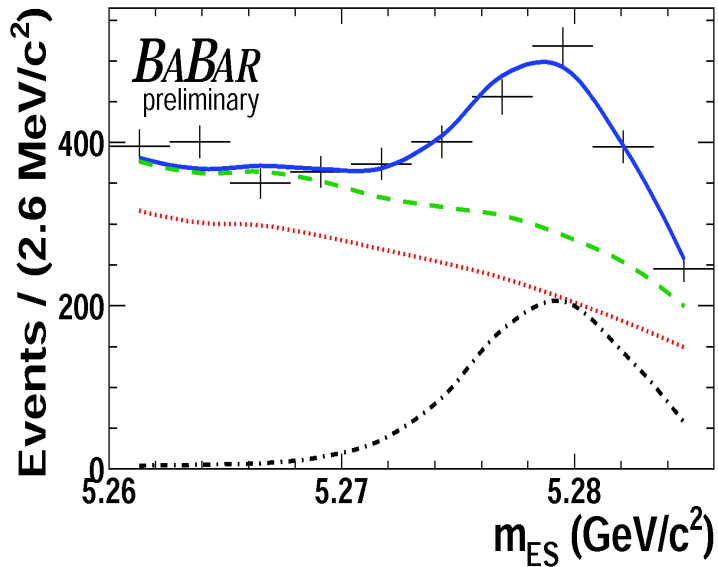


# Three-body: motivations

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- $B^+ \rightarrow K^+ \pi^0 \pi^0$  :
  - help solving the “ $K\pi$  puzzle” looking at the similar  $K^* \pi$ ;
  - Investigate the poorly known  $f_x(1300)$ , seen to decay to  $\pi^+ \pi^-$ ;
- $B^0 \rightarrow K_S^0 K \pi$  :
  - Decay proceeding through  $b \rightarrow u$  tree and  $b \rightarrow d$  penguin amplitudes;
  - Search for an isospin partner of the  $f_x(1500)$  seen decaying to  $K^+ K^-$  in  $B^+ \rightarrow K^+ K^- \pi^+$ , but not in  $B^+ \rightarrow K_S^0 K_S^0 \pi^+$ ;
- $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  :
  - First amplitude analysis of this mode;
  - Investigate the nature of the  $f_x(1500)$ .

# Inclusive BF of $B^+ \rightarrow K^+ \pi^0 \pi^0$



Fit results:

$$N_{\text{sig}} = 1220 \pm 85$$

$$f_{\text{SCF}} = 9.7 \%$$

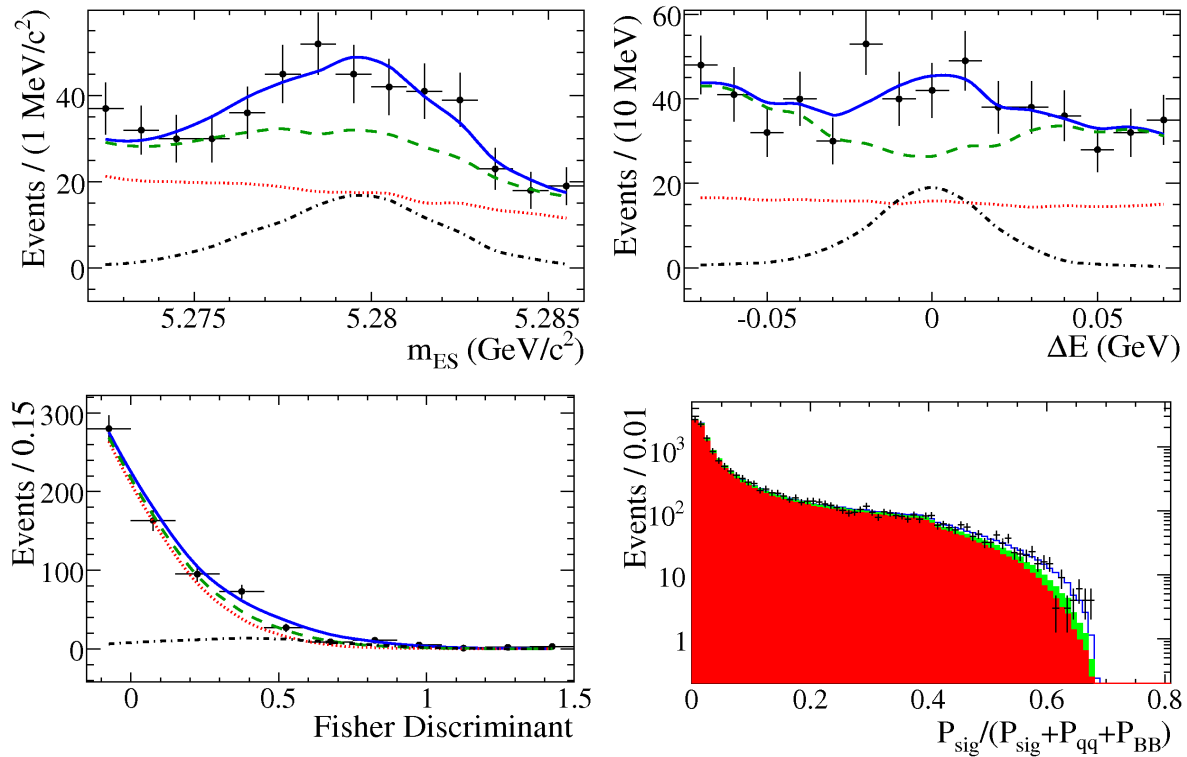
Significance  $10\sigma$   
( $15.6\sigma$  stat only)

- We measure the branching fraction:

$$\text{BF}(B^+ \rightarrow K^+ \pi^0 \pi^0) = (15.5 \pm 1.1 \pm 1.6) \times 10^{-6}$$

- Dominant systematic uncertainties:  $\pi^0$  reconstruction efficiency (6.0%),  $\text{NN}_{\text{out}}$  PDF shape (4.9%),  $\Delta E$  cut efficiency (4.0%).

# Observation of $B^0 \rightarrow K_S^0 K \pi$

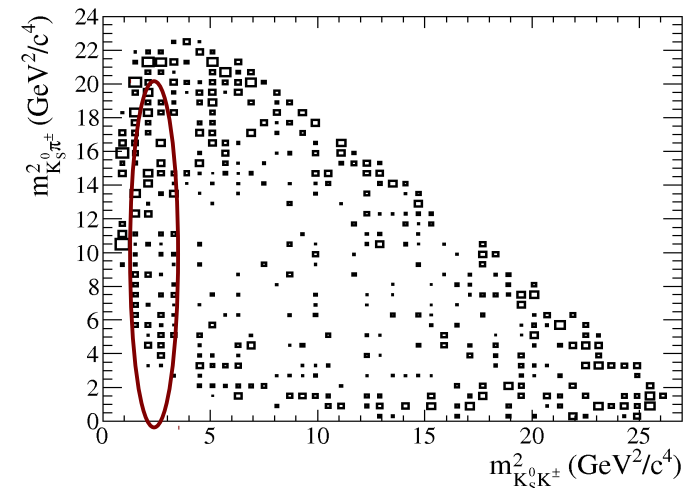


Fit results:  
 $N_{\text{sig}} = 262 \pm 47$   
 Significance  $5.2\sigma$   
 ( $6.0\sigma$  stat only)

No evidence of an isospin partner of the  $f_X(1500)$

$$\text{BF}(B^0 \rightarrow K_S^0 K \pi) = (3.2 \pm 0.5 \pm 0.3) \times 10^{-6}$$

- Dominant systematic uncertainties: signal PDF's (5.2%), corrections due to vetoes (4.1%), self-crossfeed fraction (3%).



# Amplitude analysis of $B^0 \rightarrow K_S^0 K_S^0 K_S^0$

- Three identical particles in the final state: the analysis can be done only in  $1/6^{\text{th}}$  of the Dalitz Plot. We use the variables  $s_{max}$  and  $s_{min}$ , and we move to the Squared Dalitz Plot formalism:

Standard DP

$$s_{min} = \min(s_{12}, s_{23}, s_{13})$$

$$s_{max} = \max(s_{12}, s_{23}, s_{13})$$

$$s_{xy} = m_{xy}^2$$

Squared DP

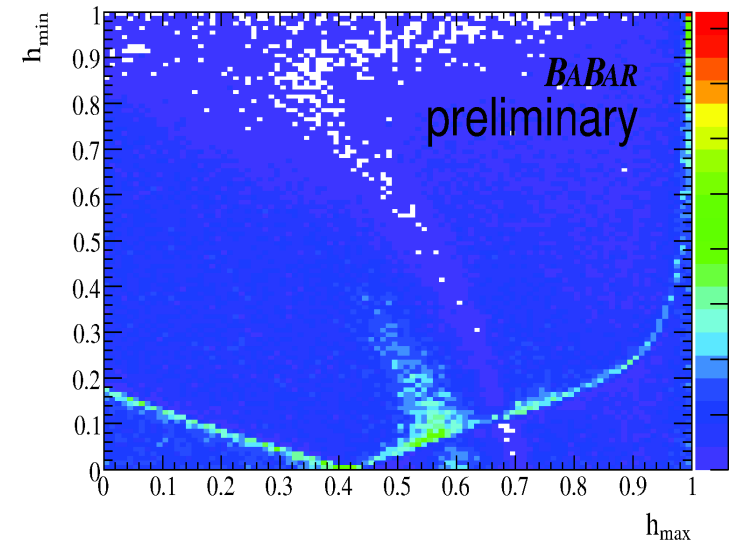
$$s_{min} \rightarrow \cos \theta_{min} \equiv h_{min}$$

$$s_{max} \rightarrow \cos \theta_{max} \equiv h_{max}$$

$$ds_{min} ds_{max} \rightarrow |\det J| dh_{min} dh_{max}$$

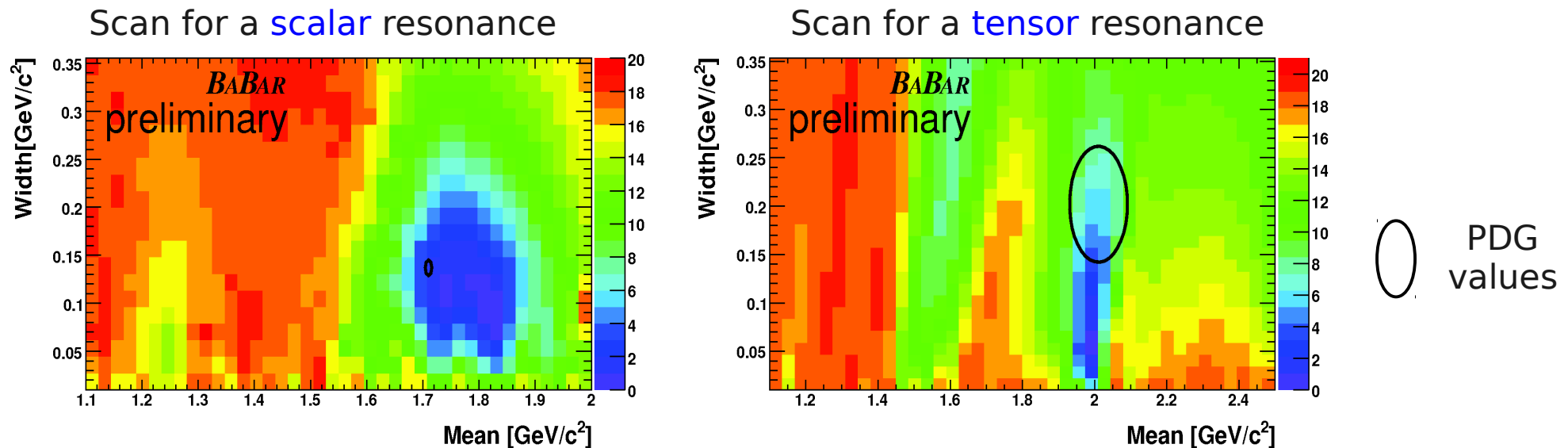
- The isobar model is used to describe the DP structure:

$$\mathcal{A}(s_{min}, s_{max}) = \sum_{j=1}^N c_j F_j(s_{min}, s_{max})$$



# Amplitude analysis of $B^0 \rightarrow K_S^0 K_S^0 K_S^0$

- $200 \pm 15$  signal events ( $305 \pm 18$   $q\bar{q}$ );
- We start with a baseline model with  $f_0(980)$ ,  $\chi_{c0}$ , and non-resonant. We add a resonance and scan the likelihood varying its mass and width;



- We only find significant contributions from  $f_0(1710)$  and  $f_2(2010)$ , **no** evidence of the  $f_x(1500)$ ;
- We measure the inclusive branching fraction:

$$\text{BF}(B^0 \rightarrow K_S K_S K_S) = (6.5 \pm 0.5 \pm 0.4) \times 10^{-6}$$

# Conclusions

Search for $B \rightarrow \eta' \rho, \eta' f_0, \eta' K^*$	Four first observations ( $>5\sigma$ ) and evidence ( $>3\sigma$ ) for three more modes. Unexpected enhancement of the tensor component over the vector in $\eta' K^*$
Search for $B^+ \rightarrow a_1^+ K^{*0}$	No signal found: upper limit sets useful constraints for theoretical models
Inclusive BF of $B \rightarrow K^+ \pi^0 \pi^0$	First measurement of the inclusive mode, next we will measure the $K^* \pi$ branching fraction
Measurement of $B^0 \rightarrow K_s^0 K \pi$	No evidence of an isospin partner of the $f_x(1500)$
Amplitude analysis of $B^0 \rightarrow K_s K_s K_s$	First amplitude analysis of this mode, no evidence of the $f_x(1500)$ decaying to $K_s K_s$

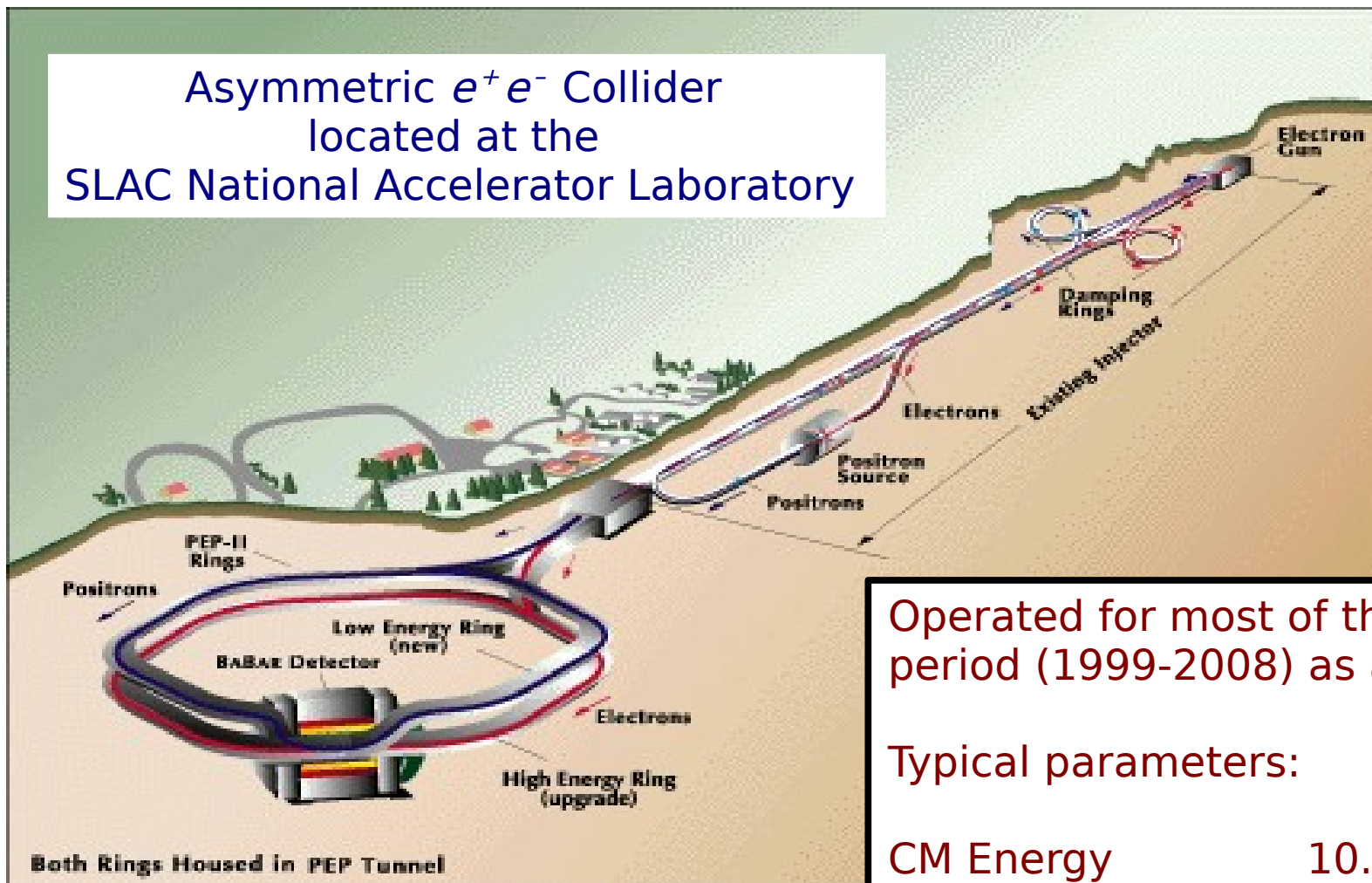
- Two years after the end of the data taking, BaBar continues to exploit its rich dataset, more results will be coming...

# Backup Slides

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# The PEP-II Collider

Asymmetric  $e^+e^-$  Collider  
located at the  
SLAC National Accelerator Laboratory



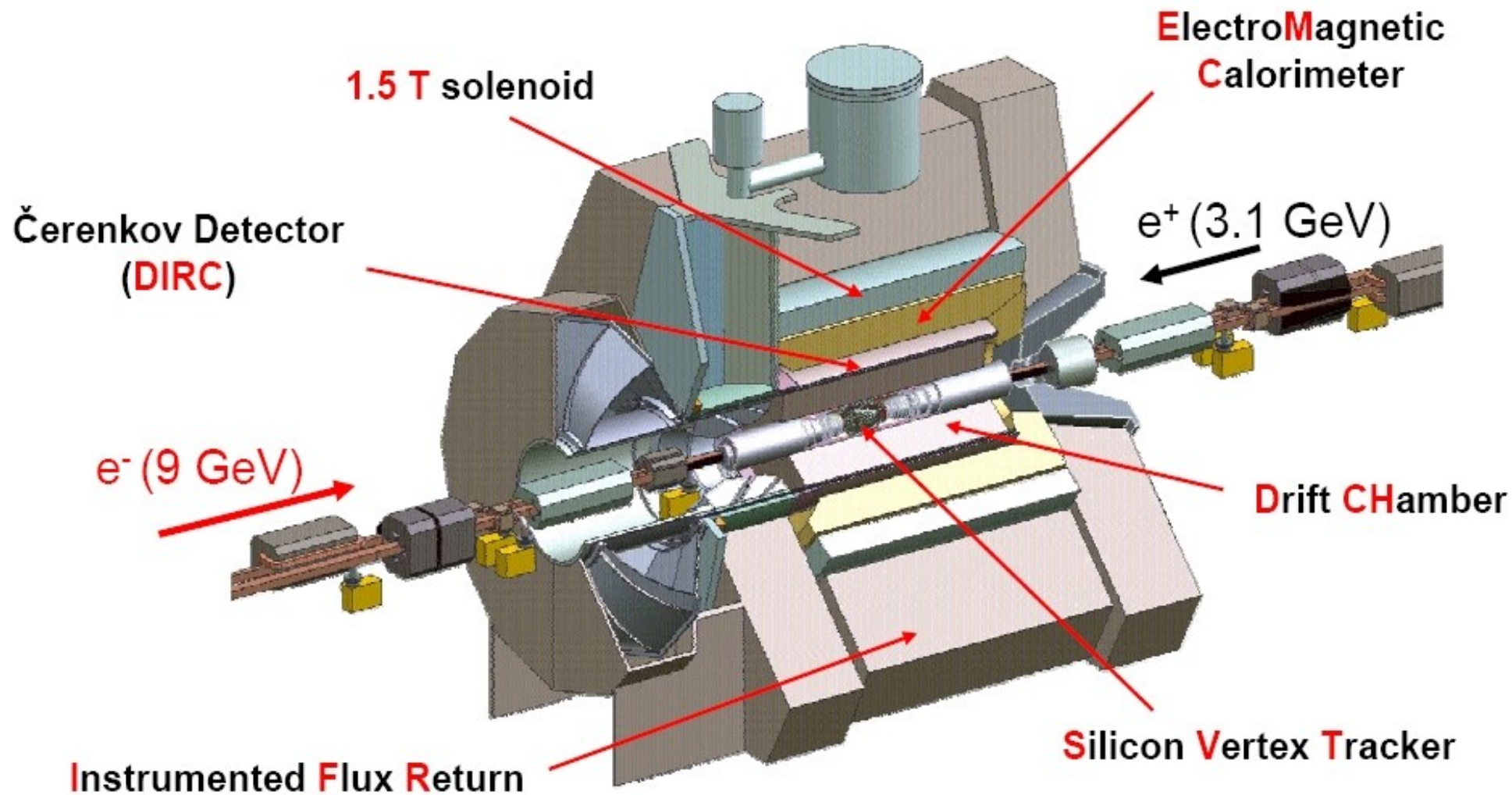
Operated for most of the data-taking period (1999-2008) as a B-factory.

Typical parameters:

CM Energy	10.58 GeV
$e^+$ Energy	3.1 GeV
$e^-$ Energy	9.0 GeV
Max Luminosity	$1.2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



# The *BABAR* detector



# Search for $B \rightarrow \eta' \rho / \eta' f_0 / \eta' K^*$

Mode	$Y$ (events)	$Y_0$ (events)	$\epsilon$ (%)	$\prod \mathcal{B}_i$ (%)	$S$ ( $\sigma$ )	$\mathcal{B}$ ( $10^{-6}$ )	$\mathcal{B}$ U.L. ( $10^{-6}$ )	$\mathcal{A}_{\text{ch}}$
$\eta' \rho^0$	37±15	9±5	23.4	17.5	2.0	1.5 ± 0.8 ± 0.3	2.8	—
$\eta' f_0$	8±8	4±2	25.9	17.5	0.5	0.2 $^{+0.4}_{-0.3}$ ± 0.1	0.9	—
$\eta' \rho^+$	128±22	15±8	14.3	17.5	5.8	9.7 $^{+1.9}_{-1.8}$ ± 1.1	—	0.26 ± 0.17 ± 0.02
$\eta' K^*(892)^0$					4.0	3.1 $^{+0.9}_{-0.8}$ ± 0.3	4.4	0.02 ± 0.23 ± 0.02
$\eta'_{\eta\pi\pi} K^*(892)^0$	28±10	4±2	18.9	11.7	2.7	2.4 $^{+1.1}_{-0.9}$ ± 0.3		-0.04 ± 0.35
$\eta'_{\rho\gamma} K^*(892)^0$	61±18	9±5	13.3	19.6	3.1	4.3 $^{+1.6}_{-1.5}$ ± 0.5		0.06 ± 0.29
$\eta' K^*(892)^+$					3.8	4.8 $^{+1.6}_{-1.4}$ ± 0.8	7.2	-0.26 ± 0.27 ± 0.02
$\eta'_{\eta\pi\pi} K^*(892)^+_{K^+\pi^0}$	14±8	2±1	11.5	5.8	2.0	3.9 $^{+3.1}_{-2.1}$ ± 0.5		-1.00 ± 0.78
$\eta'_{\rho\gamma} K^*(892)^+_{K^+\pi^0}$	26±19	6±3	9.7	9.8	1.1	4.7 $^{+4.5}_{-4.1}$ ± 1.3		0.05 ± 0.66
$\eta'_{\eta\pi\pi} K^*(892)^+_{K_S^0\pi^+}$	23±10	3±2	19.1	4.0	2.6	5.5 $^{+2.9}_{-2.4}$ ± 0.7		-0.47 ± 0.37
$\eta'_{\rho\gamma} K^*(892)^+_{K_S^0\pi^+}$	34±15	10±5	16.2	6.8	1.6	4.8 $^{+3.2}_{-2.8}$ ± 1.2		0.24 ± 0.44
$\eta' (K\pi)_0^{*0}$					5.6	7.4 $^{+1.5}_{-1.4}$ ± 0.6	—	-0.19 ± 0.17 ± 0.02
$\eta'_{\eta\pi\pi} (K\pi)_0^{*0}$	106±21	12±6	20.2	11.7	4.9	8.5 $^{+2.0}_{-1.9}$ ± 1.0		-0.39 ± 0.20
$\eta'_{\rho\gamma} (K\pi)_0^{*0}$	115±36	21±11	17.6	19.6	2.7	5.8 $^{+2.3}_{-2.2}$ ± 1.0		0.32 ± 0.31
$\eta' (K\pi)_0^{*+}$					2.9	6.0 $^{+2.2}_{-2.0}$ ± 0.9	9.3	0.06 ± 0.20 ± 0.02
$\eta'_{\eta\pi\pi} (K^+\pi^0)^{*+}$	36±15	2±1	13.9	5.8	2.4	8.8 $^{+4.2}_{-3.8}$ ± 1.3		0.00 ± 0.41
$\eta'_{\rho\gamma} (K^+\pi^0)^{*+}$	185±51	31±15	12.8	9.8	2.8	26.4 $^{+9.0}_{-8.5}$ ± 5.9		0.23 ± 0.27
$\eta'_{\eta\pi\pi} (K_S^0\pi^+)^{*+}$	18±12	1±1	18.6	4.0	1.6	5.1 $^{+3.5}_{-3.2}$ ± 0.9		0.13 ± 0.59
$\eta'_{\rho\gamma} (K_S^0\pi^+)^{*+}$	-29±22	-8±4	17.4	6.8	—	-3.8 $^{+4.0}_{-3.9}$ ± 1.5		-0.40 ± 1.48
$\eta' K_2^*(1430)^0$					5.3	13.7 $^{+3.0}_{-2.9}$ ± 1.2	—	0.14 ± 0.18 ± 0.02
$\eta'_{\eta\pi\pi} K_2^*(1430)^0$	42±13	2±1	15.1	5.8	3.7	9.8 $^{+3.4}_{-3.2}$ ± 0.9		0.58 ± 0.32
$\eta'_{\rho\gamma} K_2^*(1430)^0$	125±26	20±10	10.6	9.8	4.1	21.7 $^{+5.4}_{-5.3}$ ± 3.0		-0.05 ± 0.20
$\eta' K_2^*(1430)^+$					7.2	28.0 $^{+4.6}_{-4.3}$ ± 2.6	—	0.15 ± 0.13 ± 0.02
$\eta'_{\eta\pi\pi} K_2^*(1430)^+_{K^+\pi^0}$	42±11	5±3	9.9	2.9	3.5	27.1 $^{+8.8}_{-8.1}$ ± 4.5		0.29 ± 0.25
$\eta'_{\rho\gamma} K_2^*(1430)^+_{K^+\pi^0}$	115±28	20±10	8.5	4.9	2.9	46.2 $^{+14.4}_{-13.8}$ ± 12.2		-0.33 ± 0.24
$\eta'_{\eta\pi\pi} K_2^*(1430)^+_{K_S^0\pi^+}$	42±10	5±2	15.3	2.0	4.5	25.9 $^{+7.8}_{-7.1}$ ± 2.7		0.44 ± 0.23
$\eta'_{\rho\gamma} K_2^*(1430)^+_{K_S^0\pi^+}$	62±16	14±7	12.4	3.4	3.0	24.1 $^{+8.7}_{-8.0}$ ± 4.1		0.22 ± 0.25

# Search for $B \rightarrow \eta' \rho / \eta' f_0 / \eta' K^*$

Previous results ( $\times 10^6$ )

Mode	<i>BABAR</i>	Belle
$B^+ \rightarrow \eta' \rho^+$	$8.7^{+3.1+2.3}_{-2.8-1.3}$	$< 5.8$
$B^0 \rightarrow \eta' \rho^0$	$< 3.7$	$< 1.3$
$B^0 \rightarrow \eta' K^{*0}$	$3.8 \pm 1.1 \pm 0.5$	$< 2.6$
$B^+ \rightarrow \eta' K^{*+}$	$4.9^{+1.9}_{-1.7} \pm 0.8$	$< 2.9$

232M  $B\bar{B}$  pairs  
PRL 98, 051802 (2007)

535M  $B\bar{B}$  pairs  
PRD 75, 092002 (2007)

# Search for $B^+ \rightarrow a_1^+ K^{*0}$

$Y$	$Y_b$	$\mathcal{B}(10^{-6})$	$S$	UL ( $10^{-6}$ )
$61_{-21}^{+23}$	$34 \pm 17$	$0.7_{-0.5-1.3}^{+0.5+0.6}$	0.5	1.8

$$\mathcal{B}(B^+ \rightarrow a_1^+ K^{*0}) \times \mathcal{B}(a_1^+ \rightarrow \pi^+ \pi^- \pi^+) = (0.7_{-0.5-1.3}^{+0.5+0.6}) \times 10^{-6}$$

Source of systematic uncertainty	
Additive errors (events)	
PDF parametrization	4
$a_1$ meson parametrization	6
ML Fit Bias	17
Non resonant charmless $B\bar{B}$ background	3
$B^+ \rightarrow a_2^+ K^{*0}$ charmless background	6
Remaining charmless $B\bar{B}$ background	7
Total additive (events)	22
Multiplicative errors (%)	
Tracking efficiency	1.2
Determination of the integrated luminosity	1.1
MC statistics (signal efficiency)	0.6
Differences in selection efficiency for $a_1$ decay	3.3
Particle identification (PID)	1.4
Event shape restriction ( $\cos\theta_T$ )	1.0
Total multiplicative (%)	4.1
Variation on $f_L$ [ $\mathcal{B}(10^{-6})$ ]	+0.0 -1.2
Total systematic error [ $\mathcal{B}(10^{-6})$ ]	+0.6 -1.3

# Inclusive BF of $B^+ \rightarrow K^+ \pi^0 \pi^0$

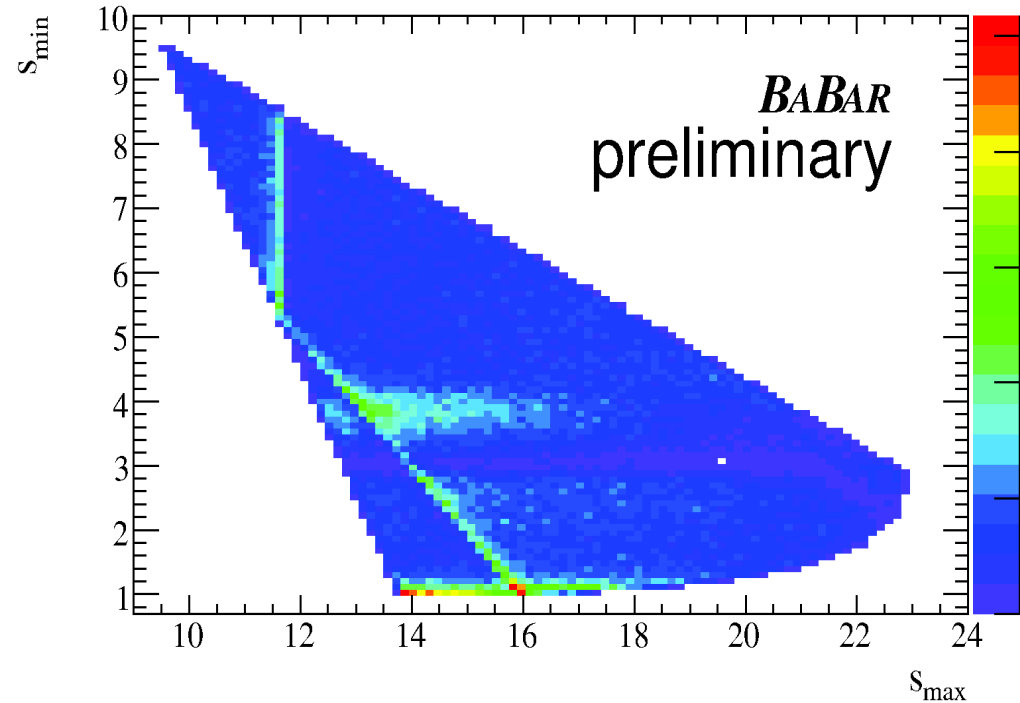
$$\mathcal{P}_j^i \equiv \mathcal{P}_j(m_{\text{ES}}^i) \mathcal{P}_j(\text{NN}_{\text{out}}^i)$$

$$\mathcal{P}_{\text{sig}}^i \equiv (1 - f_{\text{SCF}}) \mathcal{P}_{\text{CR}}(m_{\text{ES}}^i) \mathcal{P}_{\text{CR}}(\text{NN}_{\text{out}}^i) + f_{\text{SCF}} \mathcal{P}_{\text{SCF}}(m_{\text{ES}}^i) \mathcal{P}_{\text{SCF}}(\text{NN}_{\text{out}}^i),$$

Source	Uncertainty
CR signal $m_{\text{ES}}$ PDF	0.8 %
CR signal and $B\bar{B}$ background $\text{NN}_{\text{out}}$ PDFs	4.9 %
SCF signal $m_{\text{ES}}$ PDF	1.7 %
SCF signal $\text{NN}_{\text{out}}$ PDF	0.7 %
SCF fraction	2.5 %
$B\bar{B}$ background PDFs (MC statistics)	0.8 %
$B\bar{B}$ background $m_{\text{ES}}$ PDFs	1.6 %
$B\bar{B}$ background yields	1.4 %
Fit bias	1.8 %
Subtotal	6.5 %
Tracking efficiency	0.4 %
Particle identification	1.0 %
Neutral pion efficiency	6.0 %
$\Delta E$ cut efficiency	4.0 %
$\text{NN}_{\text{out}}$ cut efficiency	3.0 %
$K_S^0$ veto	2.0 %
$N_{B\bar{B}}$	0.6 %
Total	10.4 %

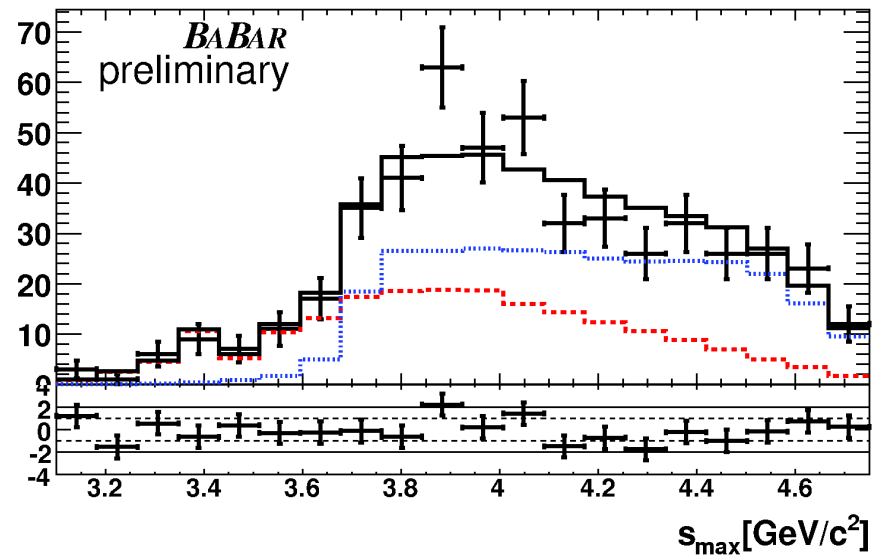
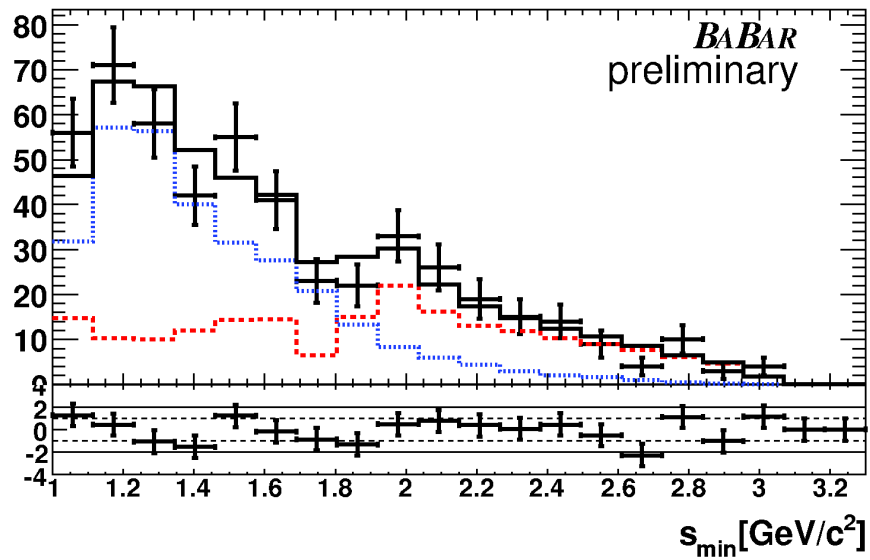
# Amplitude analysis of $B^0 \rightarrow K_S^0 K_S^0 K_S^0$

$$\begin{aligned} \mathcal{A}[B^0 \rightarrow K_S^0(1)K_S^0(2)K_S^0(3)] &= \frac{1}{2} \{ \mathcal{A}_1[B^0 \rightarrow \bar{K}^0(1)K^0(2)K^0(3)] \\ &+ \mathcal{A}_2[B^0 \rightarrow \bar{K}^0(2)K^0(3)K^0(1)] \\ &+ \mathcal{A}_3[B^0 \rightarrow \bar{K}^0(3)K^0(1)K^0(2)] \} , \end{aligned}$$

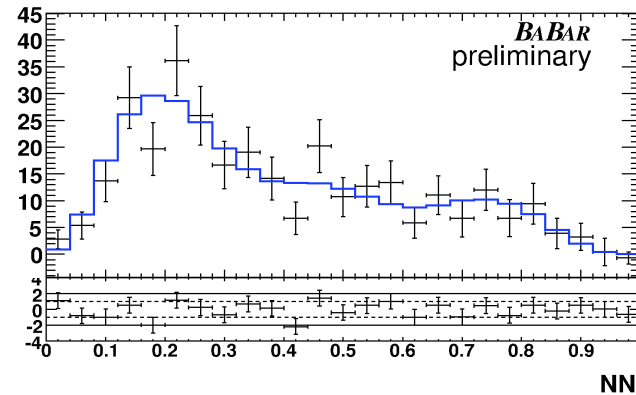
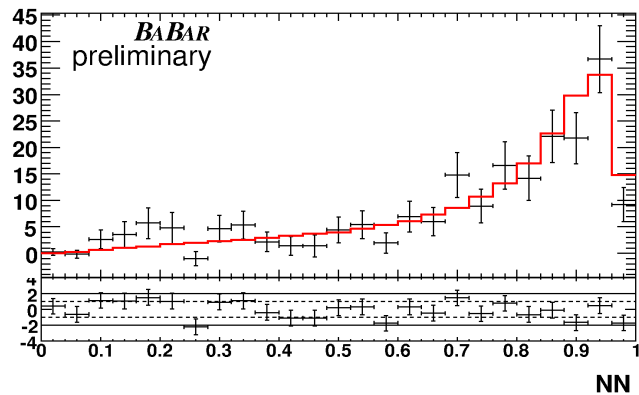
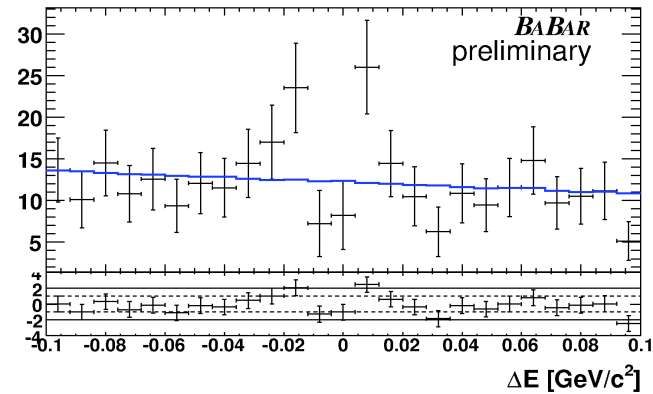
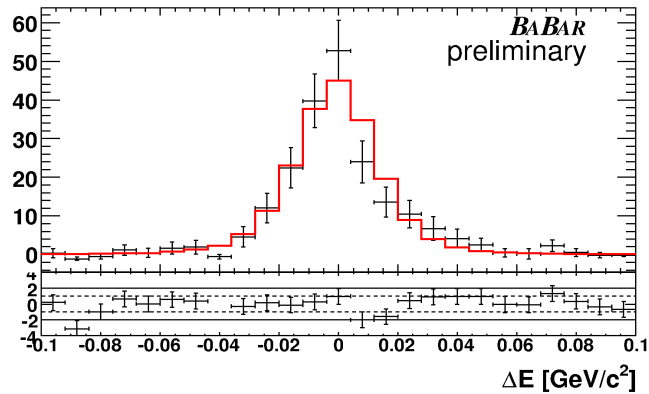
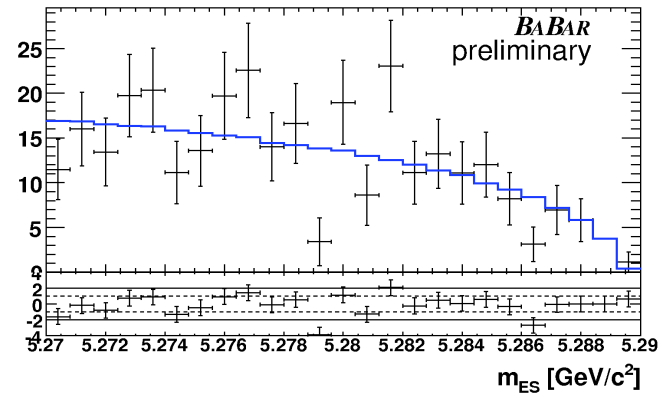
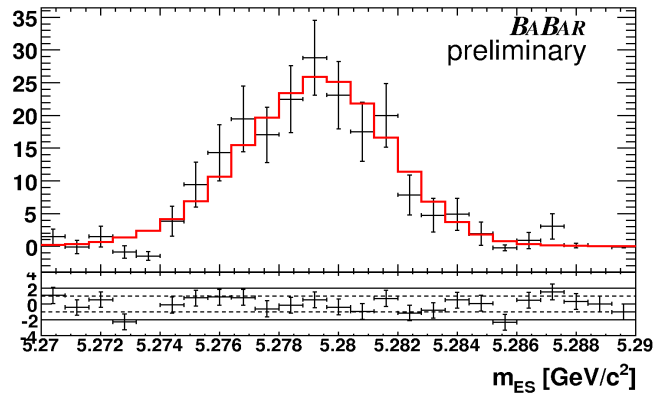


$$d\Gamma(B^0 \rightarrow K_S^0 K_S^0 K_S^0) = \frac{1}{(2\pi)^3} \frac{|\mathcal{A}|^2}{32m_{B^0}^3} ds_{\min} ds_{\max}$$

# Amplitude analysis of $B^0 \rightarrow K_S^0 K_S^0 K_S^0$



# Amplitude analysis of $B^0 \rightarrow K_S^0 K_S^0 K_S^0$





# Amplitude analysis of $B^0 \rightarrow K_S^0 K_S^0 K_S^0$

Mode	Solution 1	Solution 2
FF $f_0(980)K_S^0$	$0.44^{+0.20}_{-0.19}$	$1.03^{+0.22}_{-0.17}$
Phase [rad] $f_0(980)K_S^0$	$0.09 \pm 0.16$	$1.26 \pm 0.17$
Significance [ $\sigma$ ] $f_0(980)K_S^0$	3.3	-
FF $f_0(1710)K_S^0$	$0.07^{+0.07}_{-0.03}$	$0.09^{+0.05}_{-0.02}$
Phase [rad] $f_0(1710)K_S^0$	$1.11 \pm 0.23$	$0.36 \pm 0.20$
Significance [ $\sigma$ ] $f_0(1710)K_S^0$	3.7	-
FF $f_2(2010)K_S^0$	$0.09^{+0.03}_{-0.03}$	$0.10 \pm 0.02$
Phase [rad] $f_2(2010)K_S^0$	$2.50 \pm 0.20$	$1.58 \pm 0.22$
Significance [ $\sigma$ ] $f_2(2010)K_S^0$	3.3	-
FF $\chi_{c0}K_S^0$	$0.07^{+0.04}_{-0.02}$	$0.07 \pm 0.02$
Phase [rad] $\chi_{c0}K_S^0$	$0.63 \pm 0.47$	$-0.24 \pm 0.52$
Significance [ $\sigma$ ] $\chi_{c0}K_S^0$	4.2	-
FF NR	$2.15^{+0.36}_{-0.37}$	$1.37^{+0.26}_{-0.21}$
Phase [rad] NR	0.0	0.0
Significance [ $\sigma$ ] NR	8.2	-
Total FF	$2.84^{+0.71}_{-0.66}$	$2.66^{+0.35}_{-0.27}$