
Top quark mass and width measurement from CDF Detector

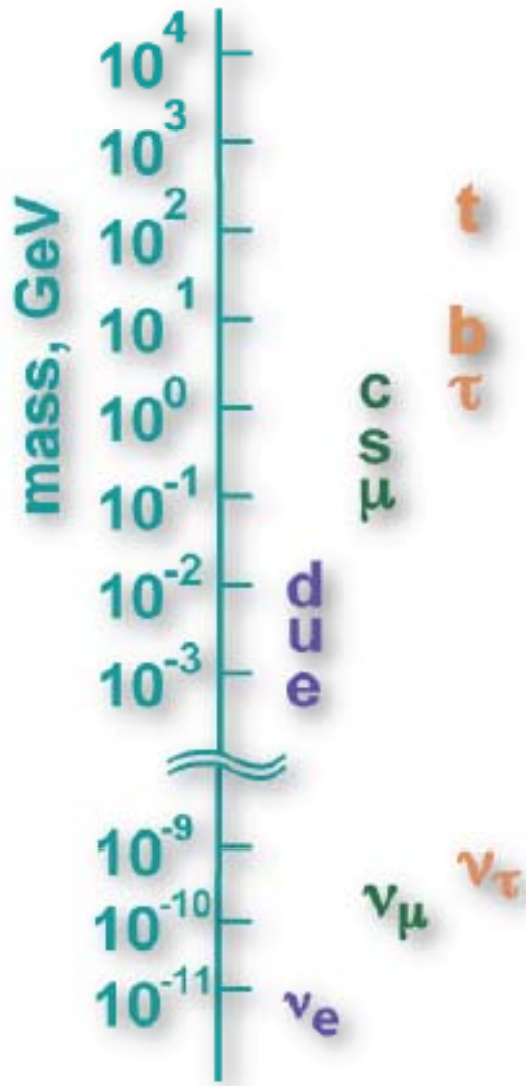


Hyunsu Lee
The University of Chicago
On behalf of the CDF collaboration

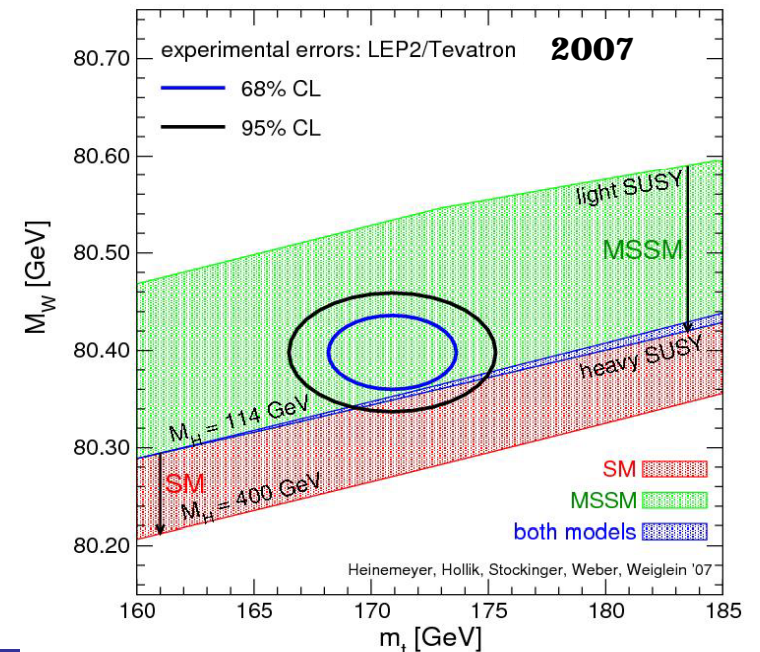
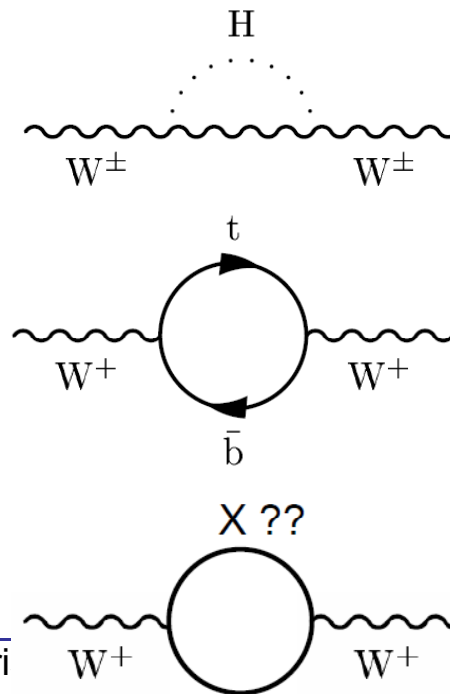


The 35th International Conference on High Energy Physics

Top quark mass

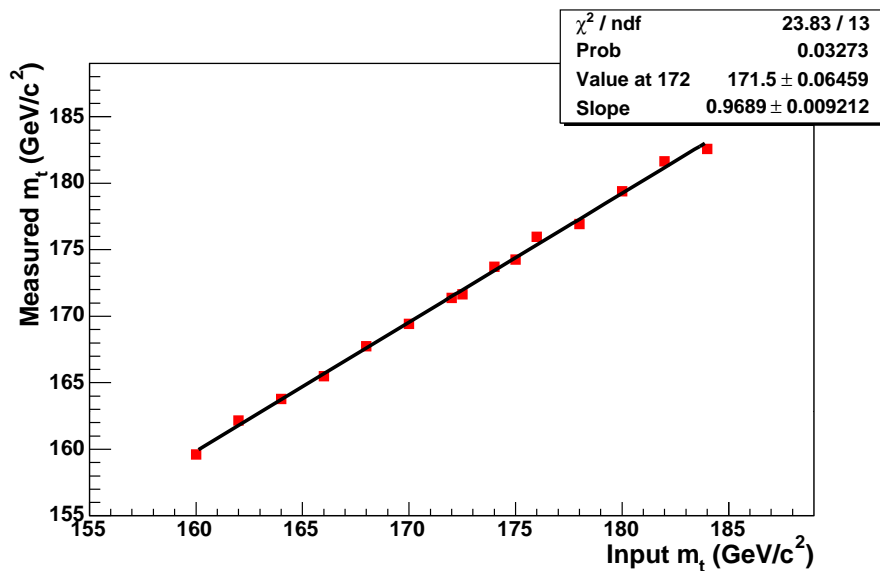
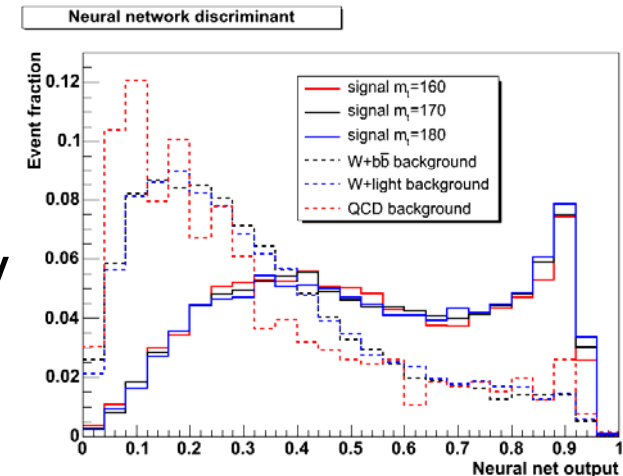


- Top quark is the heaviest known elementary particle
- Top quark mass is not predicted by SM
- Can constrain SM Higgs boson mass
 - ❖ Important contribution in radiative correction of W
 - ❖ Important test of SM

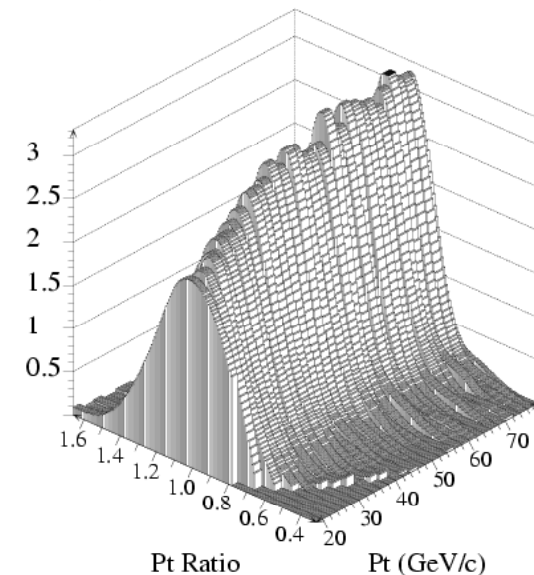


Lepton+Jets channel, Matrix Element

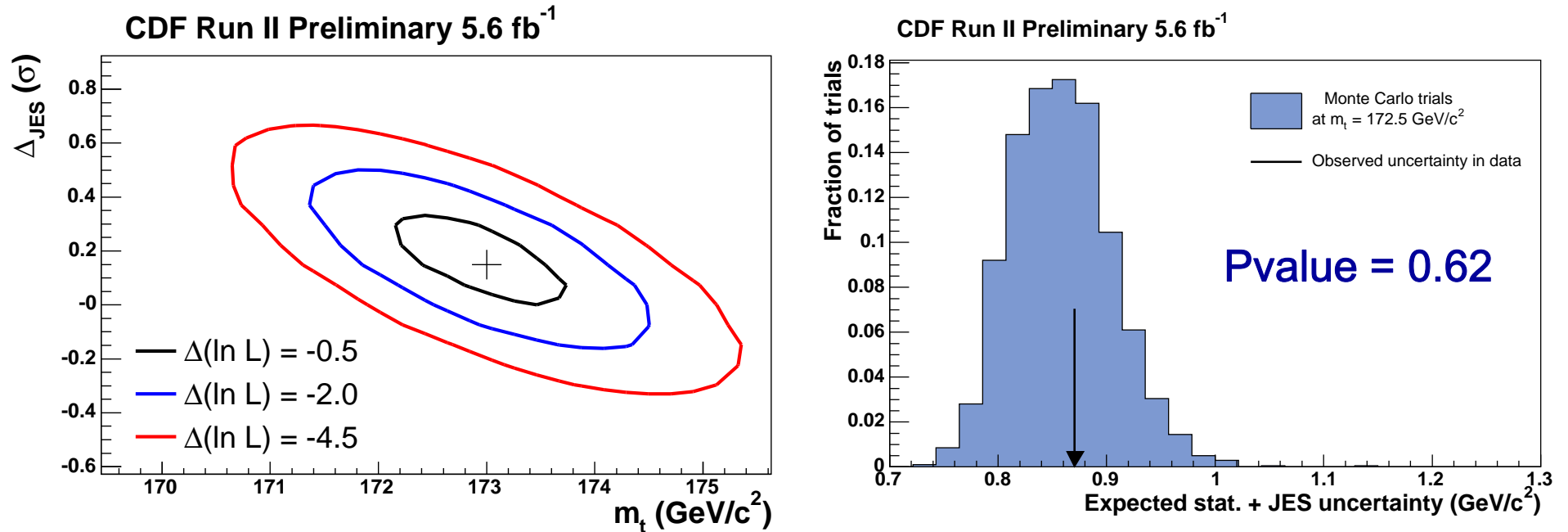
- 5.6 fb⁻¹ data – 1263 events
 - ❖ We have additional NN based selection beside topology based selection
- Transfer function was parameterized by eta and jet mass for b-jet and light jet
- *In situ* JES calibration
- MC Pseudo experiments to calibrate machinery



Transfer Function



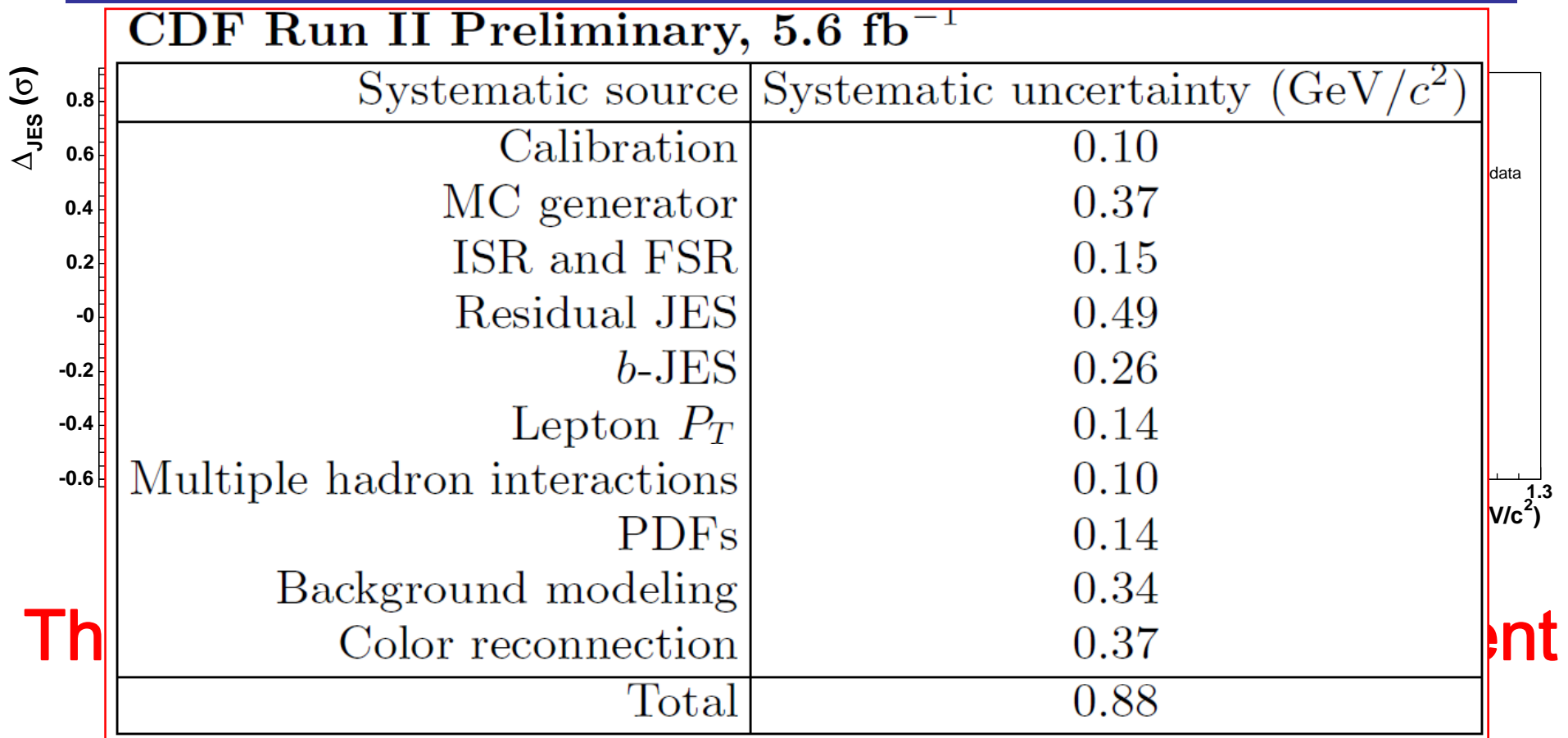
Result



**This is the best individual top mass measurement
in the world to date**

$$173.0 \pm 0.7(\text{stat}) \pm 0.6(\text{JES}) \pm 0.9(\text{syst}) \text{ GeV}/c^2 \\ = 173.0 \pm 1.2 \text{ GeV}/c^2$$

Systematic Uncertainties

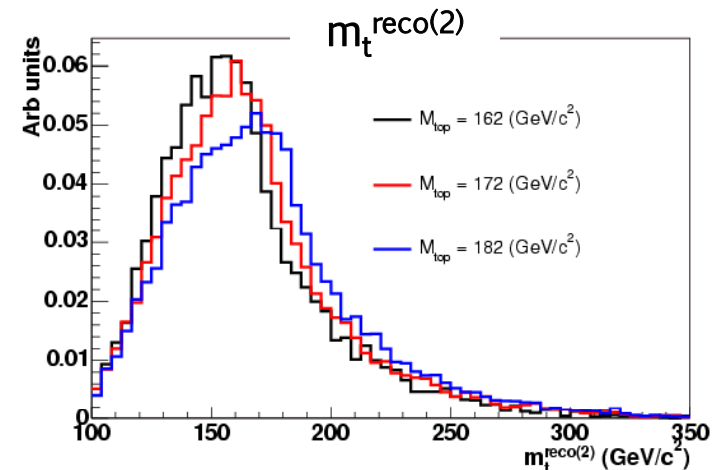
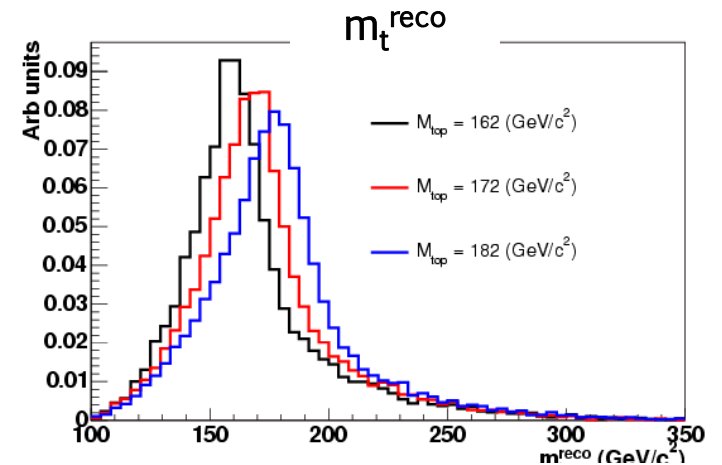


$$173.0 \pm 0.7(\text{stat}) \pm 0.6(\text{JES}) \pm 0.9(\text{syst}) \text{ GeV}/c^2$$

$$= 173.0 \pm 1.2 \text{ GeV}/c^2$$

Lepton+jets and Dilepton, Template Method

- 4.8 fb⁻¹ data – 977 Lepton+jets(LJ)
344 Dilepton(DIL)
- Fully three dimensional PDF using three observables in LJ
 - ❖ 3rd observables is reconstructed mass using kinematic fit with different combination of jet to parton assignment (2nd best fit)
- LJ only measurement
 - ❖ $172.0 \pm 1.5 \text{ GeV}/c^2$
 - ❖ Complement technique, consistent result
- Simultaneously use LJ+DIL



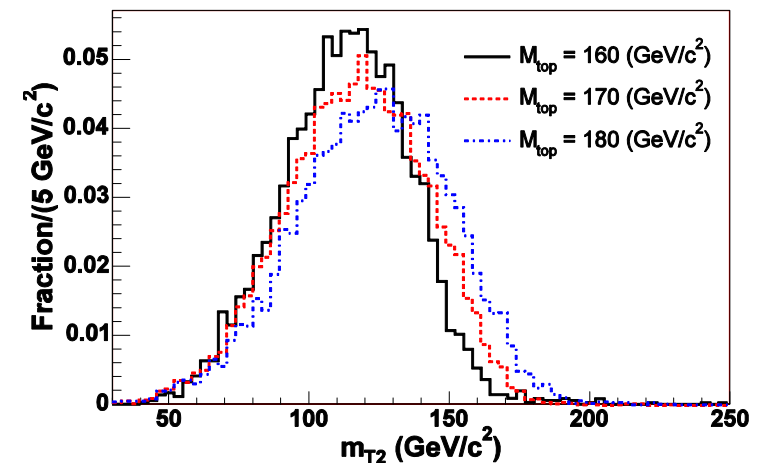
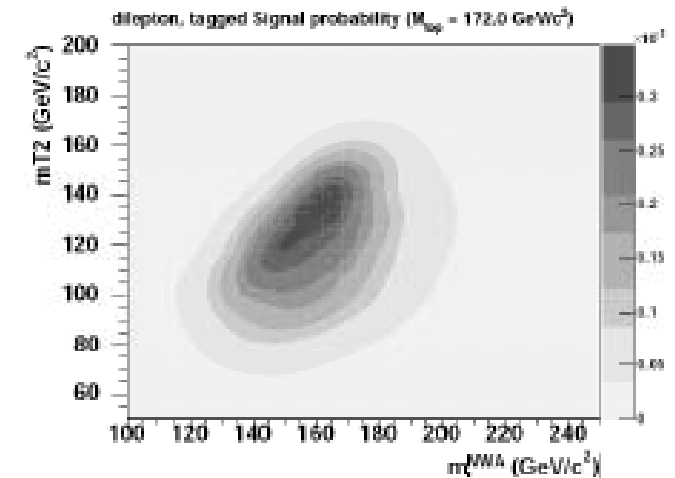
$$171.9 \pm 0.8 \text{ (stat)} \pm 0.8 \text{ (JES)} \pm 0.9 \text{ (syst)} \text{ GeV}/c^2$$
$$= 171.9 \pm 1.5 \text{ GeV}/c^2$$

Continue – Dilepton channel alone

- Two observables taking into account correlation
 - ❖ Reconstructed mass and m_{T2}
- Interesting observable m_{T2}
 - ❖ Quantity of transverse mass in two missing particle system
 - ❖ Originally introduced to measure the mass of new physics particles
A. Barr et al., J.Phys.G 29 (2003) 2343
 - ❖ CDF use m_{T2} in real data first time
Phys.Rev.D 81 (2010) 031102

$$LJ : 172.0 \pm 1.5 \text{ GeV}/c^2$$

$$170.6 \pm 2.2 \text{ (stat)} \pm 3.1 \text{ (syst)} \text{ GeV}/c^2$$
$$= 170.6 \pm 3.8 \text{ GeV}/c^2$$

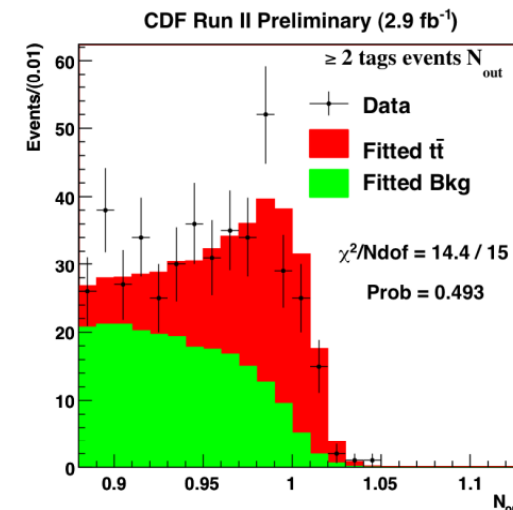
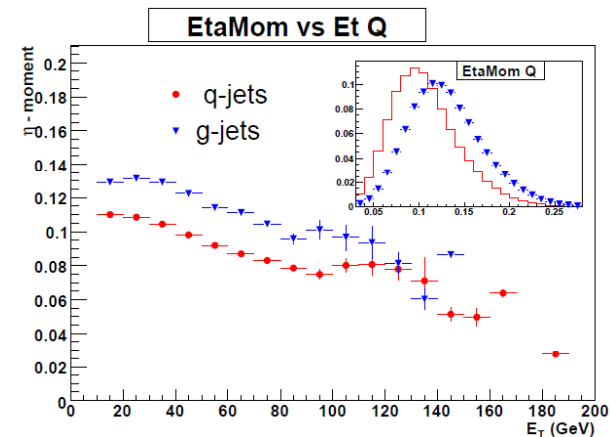


All jets channel, Template Method

- 2.9 fb⁻¹ data, template method
- Two dimensional template
 - ❖ Reconstructed top mass and reconstructed dijet mass
- NN discrimination to reduce dominant QCD backgrounds
 - ❖ Jet shape to discriminate gluon jet from quark jet

$$M_\eta \equiv \sqrt{\sum_{\text{towers}} \frac{E_T^{\text{tower}}}{E_T^{\text{jet}}} \eta_{\text{tower}}^2 - \eta_{\text{jet}}^2}$$

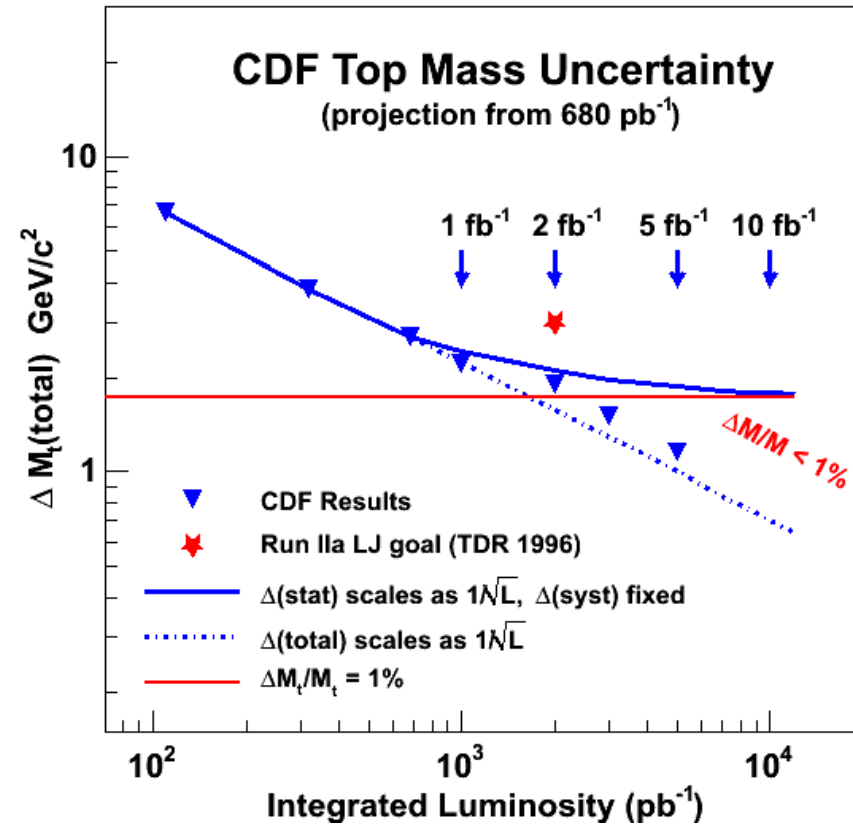
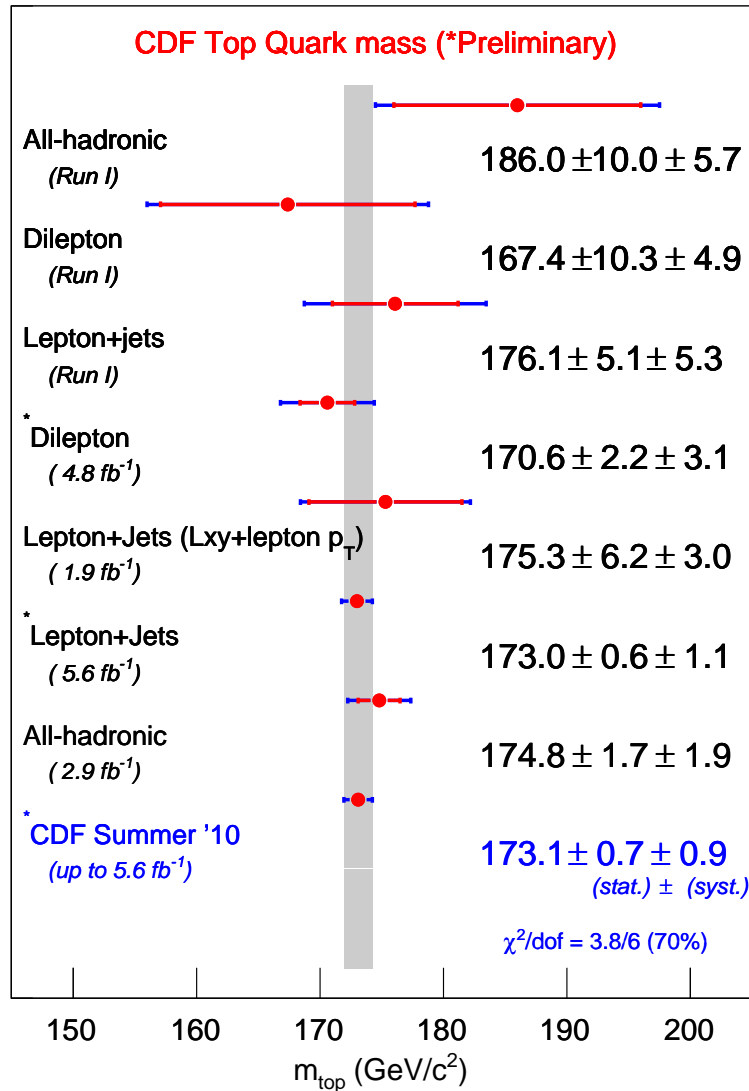
- ❖ 1btag S:B=1:4 (3452 candidates)
- ❖ 2btag S:B=1:1 (441 candidates)



$$174.8 \pm 1.7 \text{ (stat)} \pm 1.9 \text{ (JES+syst)} \text{ GeV}/c^2$$

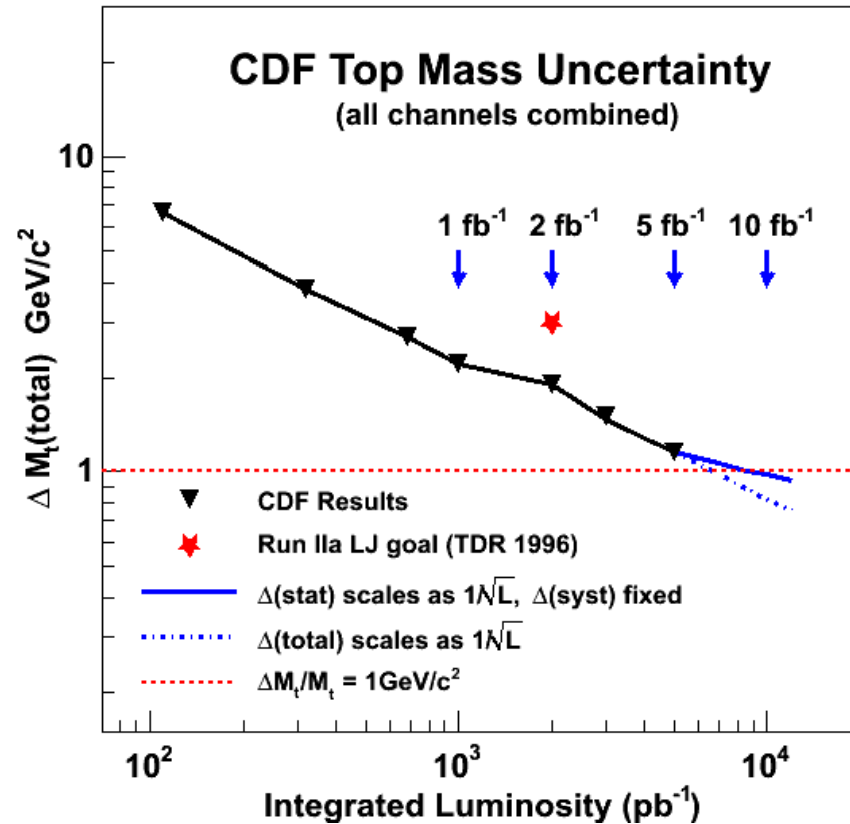
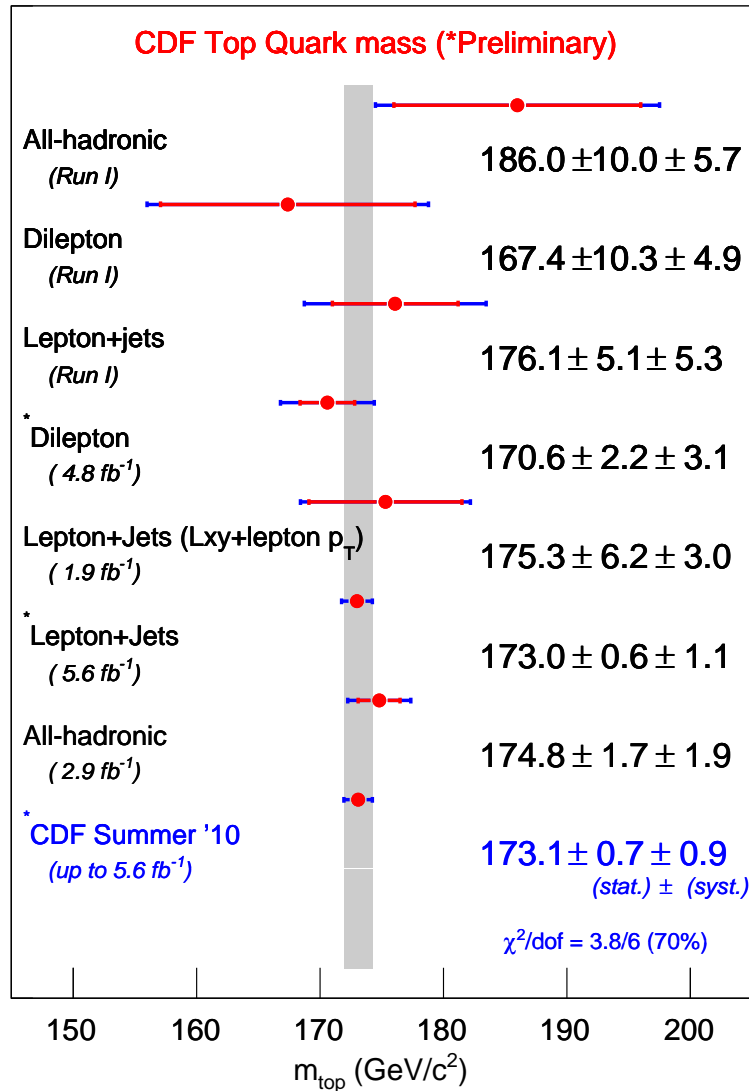
$$= 174.8 \pm 2.7 \text{ GeV}/c^2$$

CDF Top Quark mass and future



- Better than luminosity increase
- Current precision = **1.2 GeV/c²**
~0.67 %

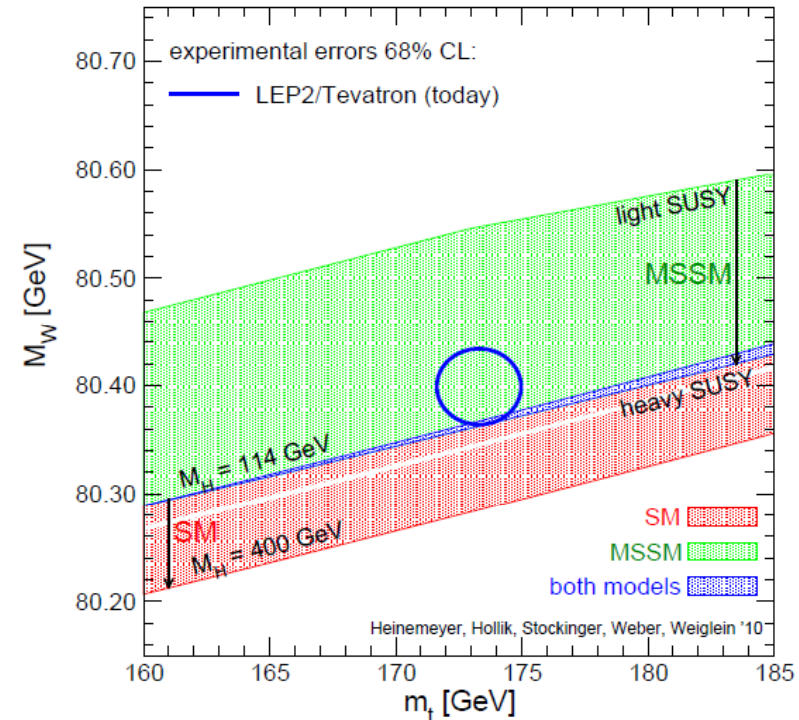
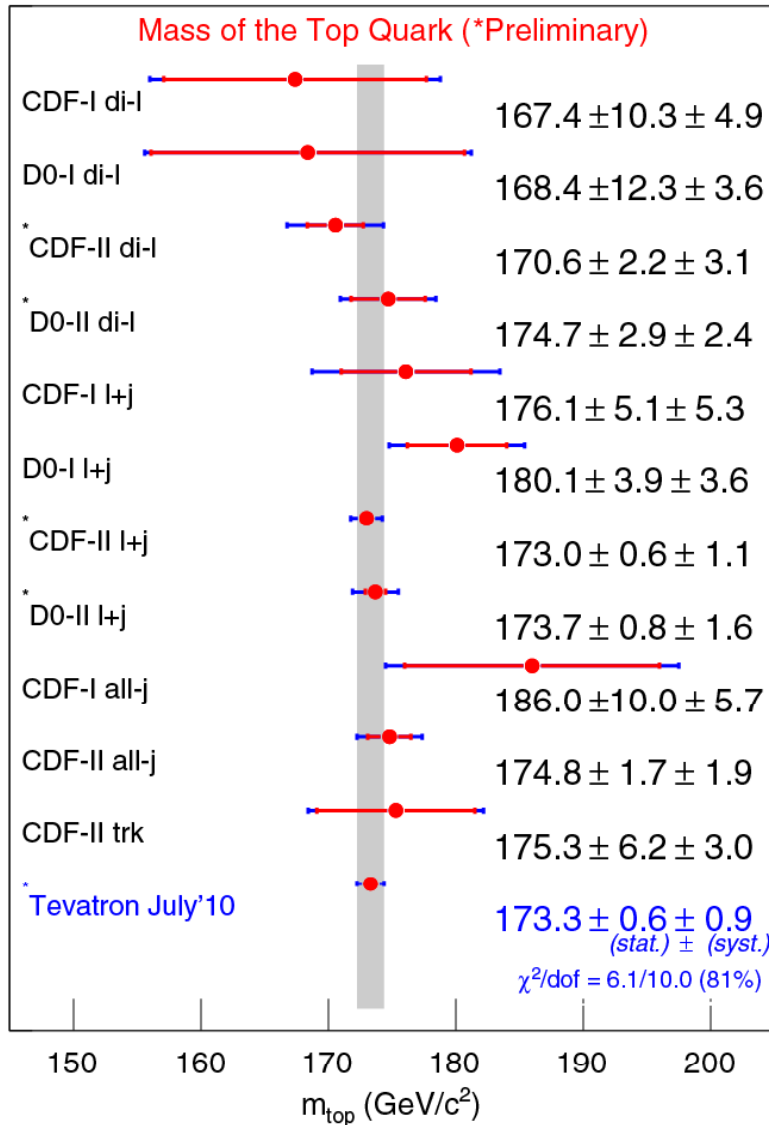
CDF Top Quark mass and future



- **1 GeV/c² precision** might be possible without any improvement at 10 fb⁻¹



Tevatron Combination



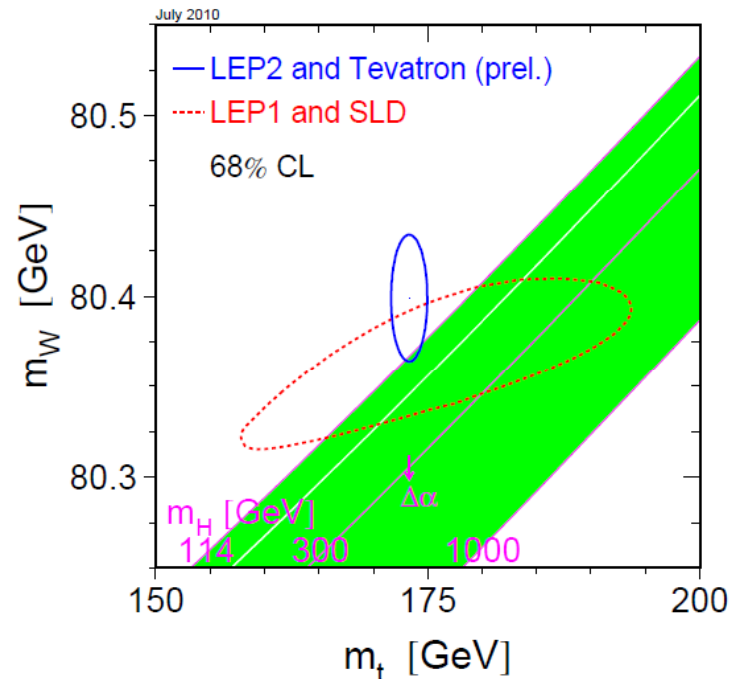
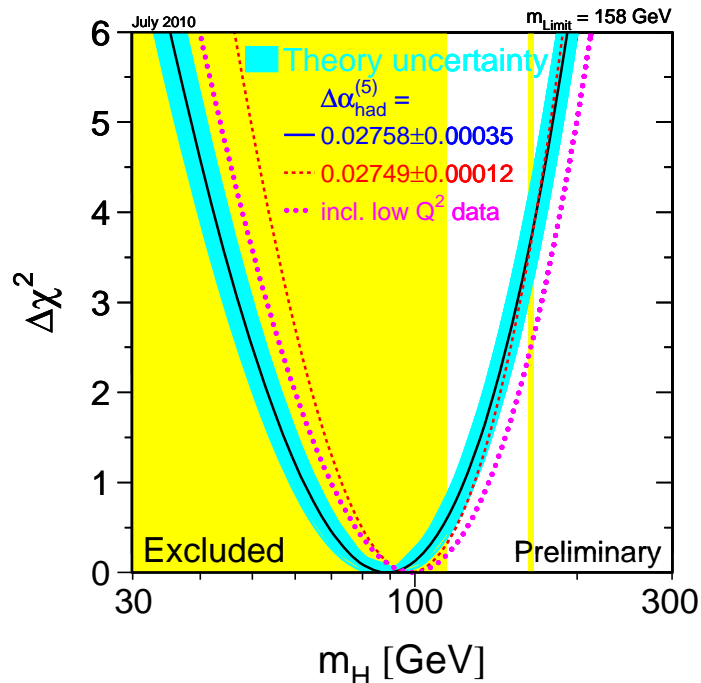
World average = 173.3 ± 1.1 GeV/c²
~0.61 % Precision

All results are consistent each others

Global EWK fit and Higgs constraints

LEP Electron Weak Working Group July 2010 Update

<http://lepewwg.web.cern.ch/LEPEWWG/>



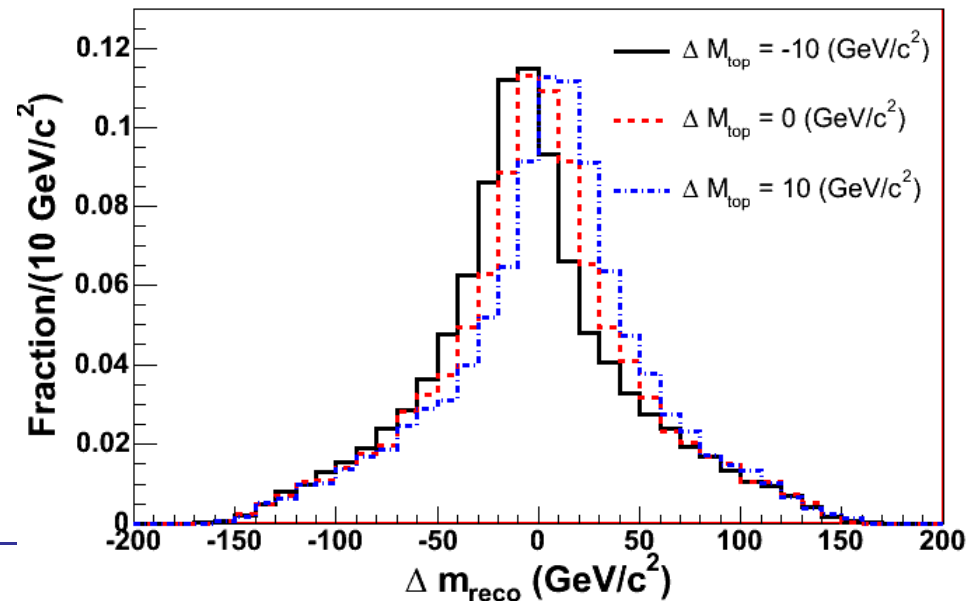
$$m_H = 89^{+35}_{-26} \text{ GeV}/c^2 \quad m_H < 158 \text{ GeV}/c^2 \text{ (95\% CL)}$$

$$m_H < 185 \text{ GeV}/c^2 \text{ (95\% CL)}$$

With direct limit from LEP II

Is top mass same with anti top quark?

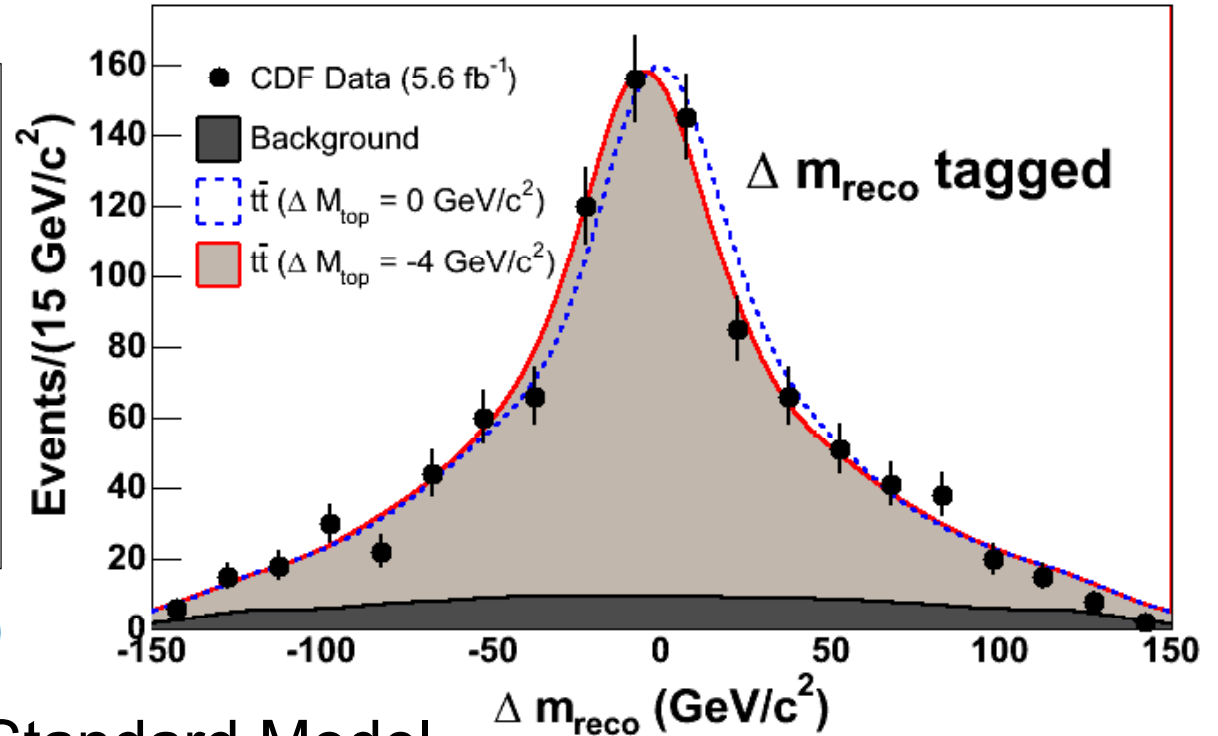
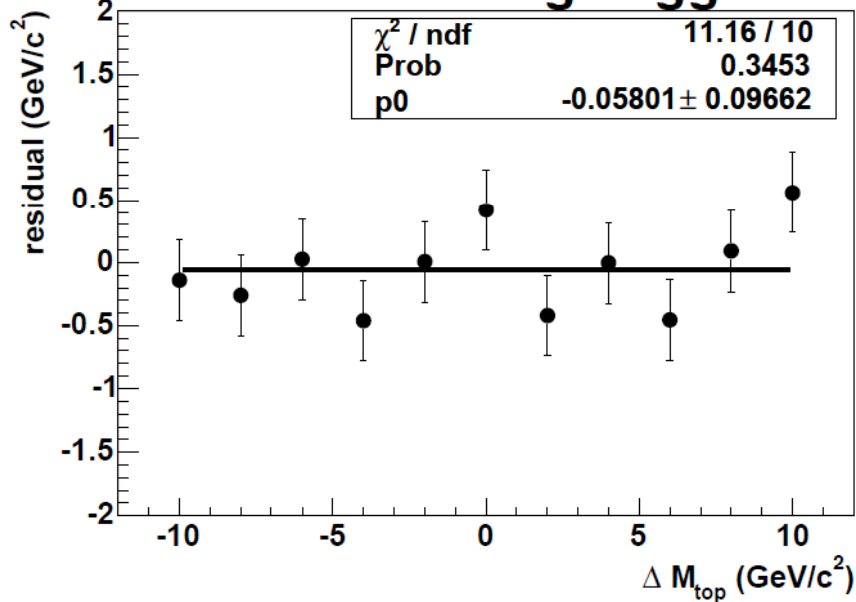
- Measured top mass precision allows us to test the mass difference top and anti-top quark
 - Good test of possible CPT violation
 - ❖ CPT violation has not very well tested on bare quarks
 - ❖ Most of test was done for relatively low mass particles
 - ❖ D0 1fb⁻¹ measurement using ME technique
- $\Delta M = 3.8 \pm 3.7 \text{ GeV}/c^2$
- We use template technique in the lepton+jets channel



Results

CDF II Preliminary

MC calibration Residuals: 0tag+tagged



- $\sim 2\sigma$ deviation from Standard Model

$$-3.3 \pm 1.4 \text{ (stat)} \pm 1.0 \text{ (syst)} \text{ GeV}/c^2$$

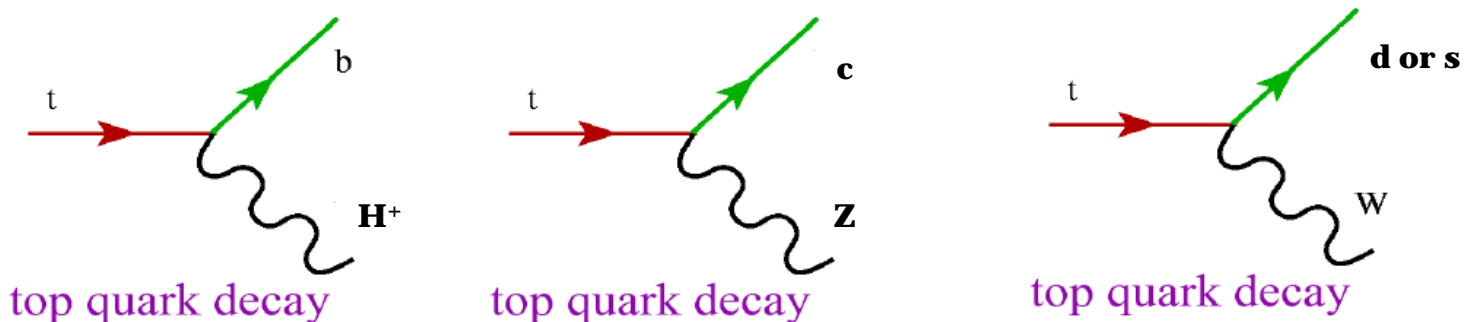
$$= -3.3 \pm 1.7 \text{ GeV}/c^2$$

Why top quark width ?

- It is intrinsic parameter of SM
 - ❖ Very precise estimation using NLO calculation ($\sim 1\%$ precision)

$$\Gamma_t = \Gamma_t^0 \left(1 - \frac{M_W^2}{m_t^2}\right)^2 \left(1 + 2 \frac{M_W^2}{m_t^2}\right) \left[1 - \frac{2\alpha_s}{3\pi} \left(\frac{2\pi^2}{3} - \frac{5}{2}\right)\right]$$

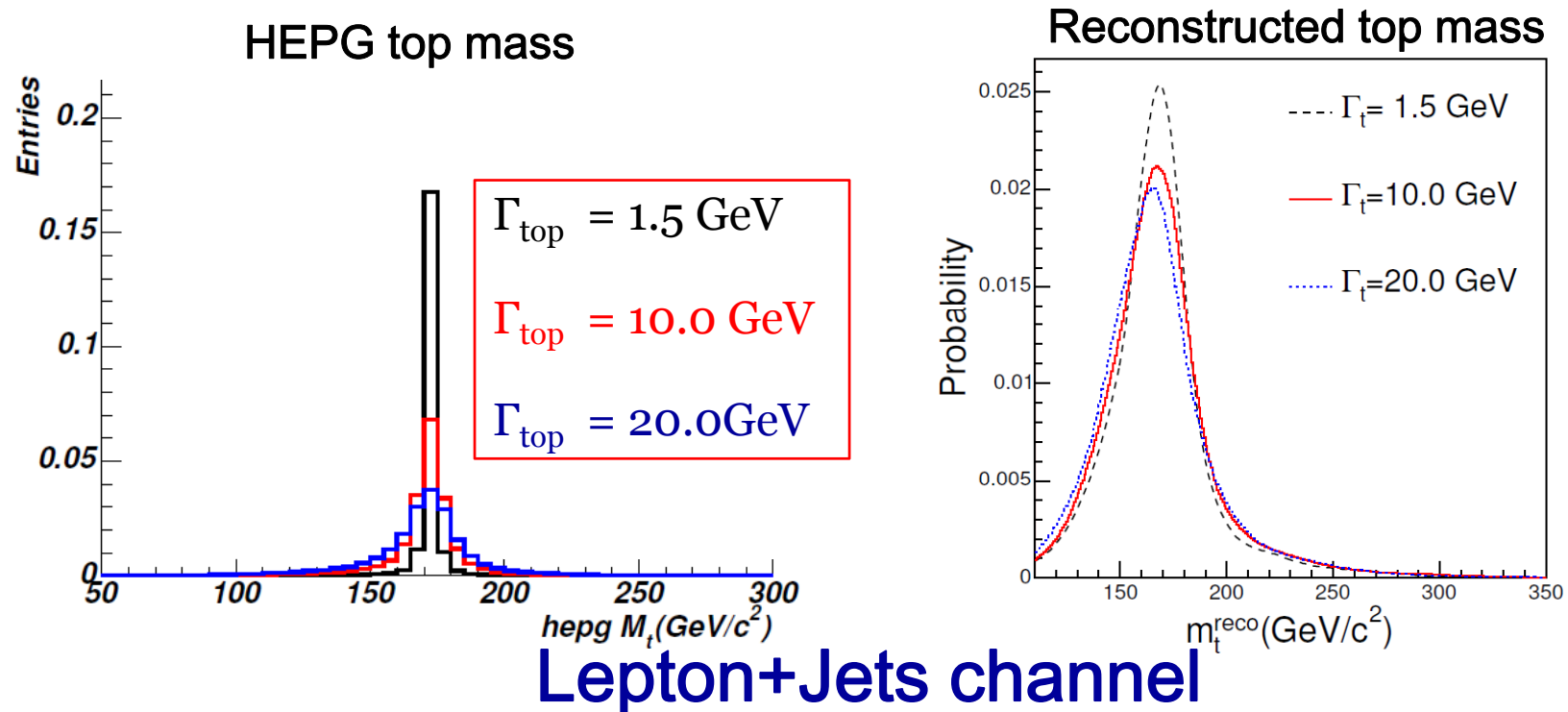
- ❖ 1.4 GeV at $M_{\text{top}} = 172.5 \text{ GeV}/c^2$
- Deviation from SM indicate new physics
 - ❖ Charged Higgs decay, FCNC, and other exotic models



- Resolving Top quark life time

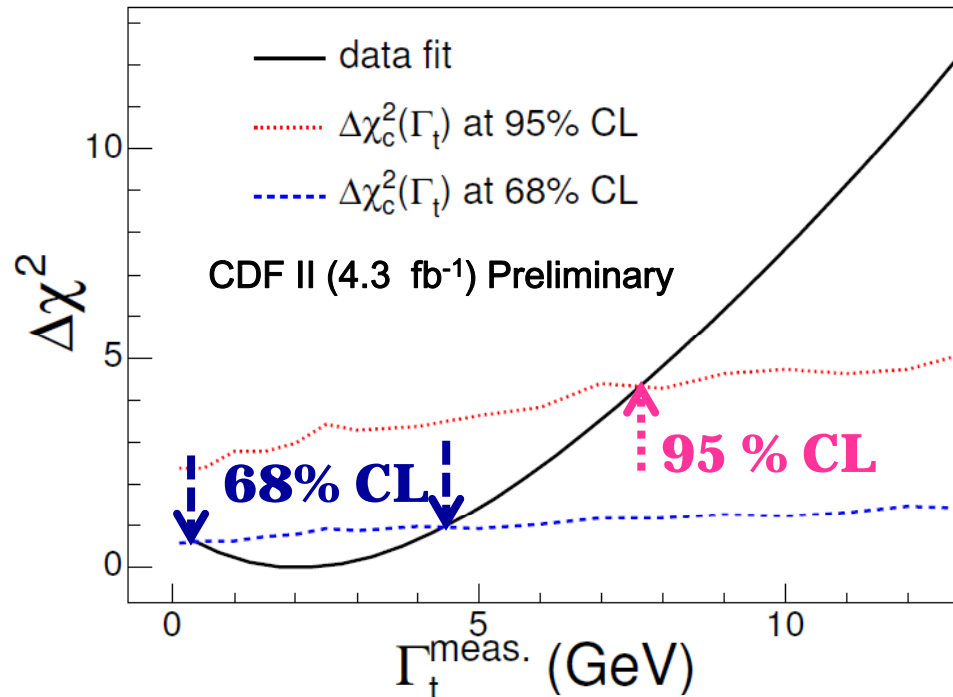
$$\tau = \frac{\hbar}{\Gamma} \quad \text{Short life time (decay before hadronization)}$$

How we can extract top width?



- Top width can make different shape of reconstructed top quark mass (RMS)
- After detector response, the effects were smeared but still we have information about top quark width

Results



- *In situ* JES calibration using 2D template (m_t^{reco} , W_{jj})

- **First direct lower bound** (68% CL) was set

$$\Gamma_{\text{top}} < 7.4 \text{ GeV @ 95\% CL}$$

$$0.3 < \Gamma_{\text{top}} < 4.4 \text{ GeV @ 68\% CL}$$

$$1.5 \text{ e}^{-25} \text{ s} < \tau_{\text{top}} < 2.2 \text{ e}^{-24} \text{ s} < \tau_{\text{had.}} \approx 3.3 \text{ e}^{-24} \text{ s}$$

Conclusion

- 0.67% (0.61%) precision of top quark mass from CDF(Tevatron)

$$M_{\text{top}} = 173.1 \pm 1.2 \text{ GeV}/c^2, \text{CDF Comb.}$$

$$M_{\text{top}} = 173.3 \pm 1.1 \text{ GeV}/c^2, \text{Tevatron Comb.}$$

- 1% resolving and observing approximately 2σ deviation (but, still consistent) of the mass difference from CDF

$$\Delta M_{\text{top}} = -3.3 \pm 1.7 \text{ GeV}/c^2$$

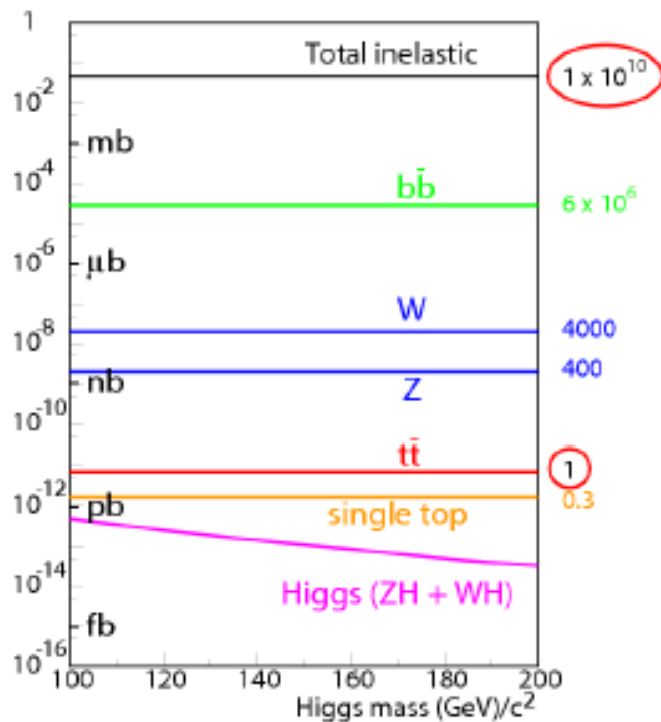
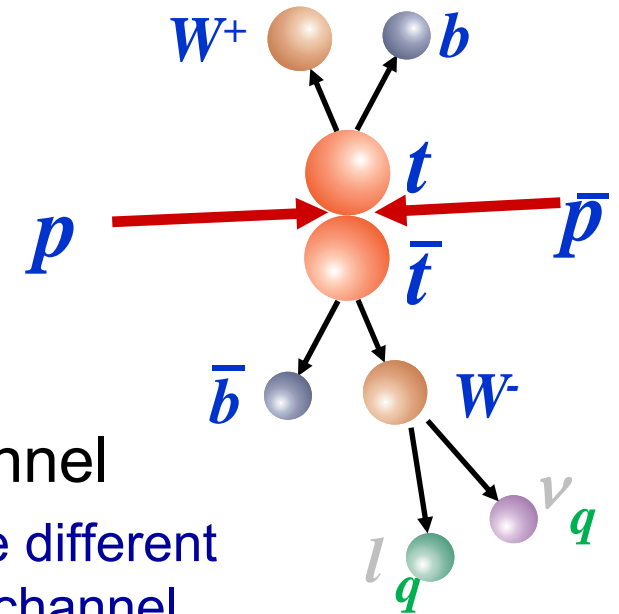
- First direct lower bound of top quark width from CDF

$$0.3 < \Gamma_{\text{top}} < 4.4 \text{ GeV} @ 68\% \text{ CL}$$

Backup

Top quark decay

- Pair production is predominated
- ~100% decay to W boson plus b quark
- Decay topologies rely on the decay of W boson
 - ❖ two jet (70%) or lepton and neutrino (30%)



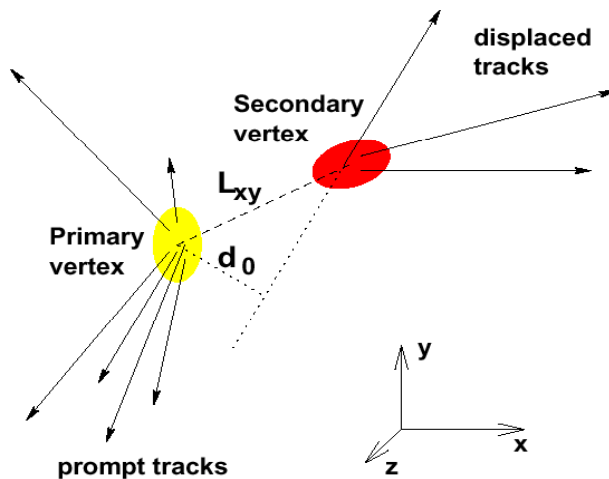
Important to look all channel

- ❖ New physics would make different phenomena for different channel

Challenge for mass measurement

- ❖ Up to six jet - Jet energy scale , jets to parton assignment
- ❖ Up to two neutrino – Missing energy – Event reconstruction
- ❖ Large QCD backgrounds

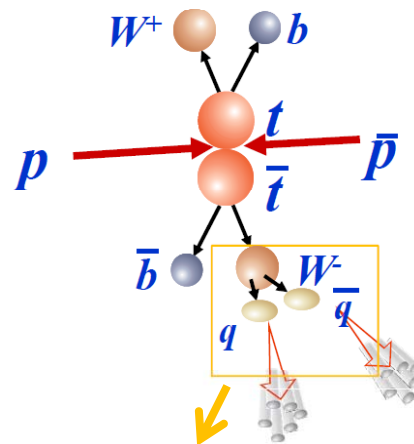
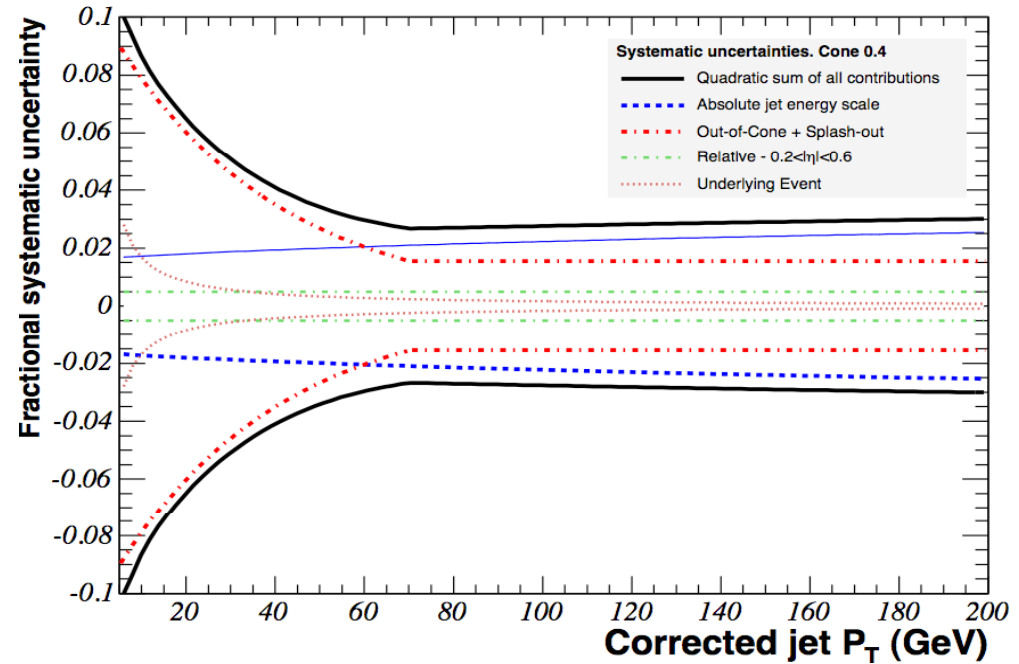
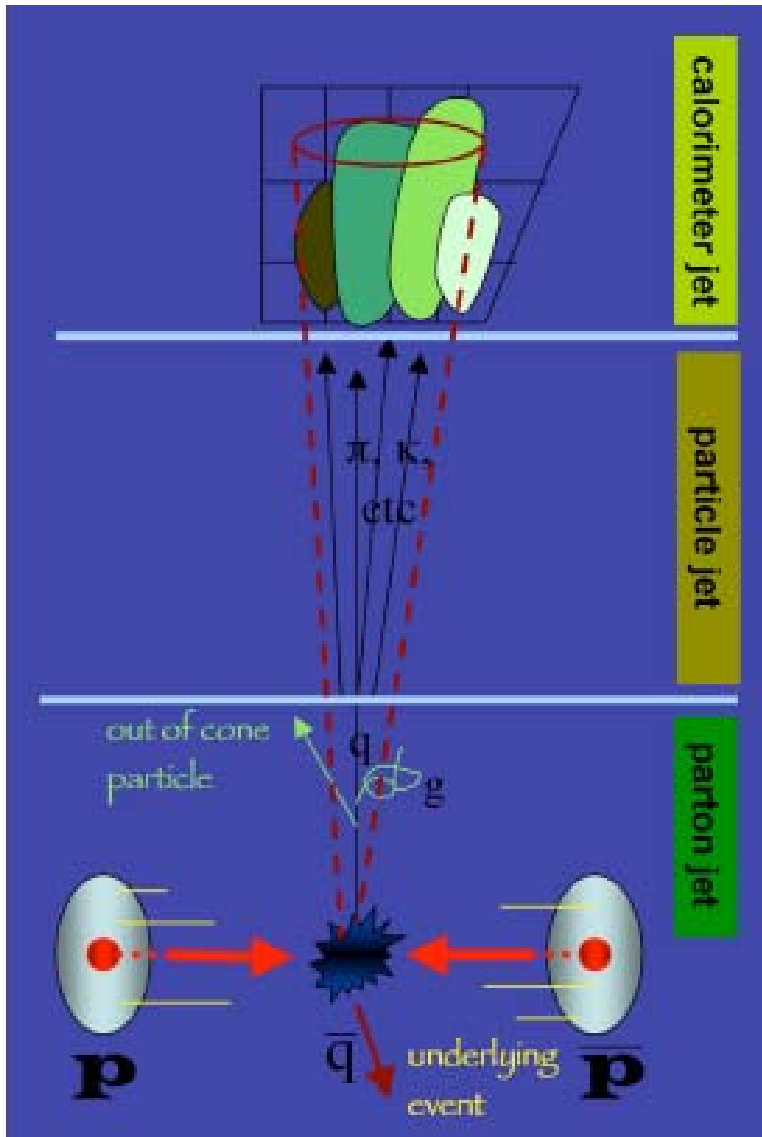
b-tagging



- B hadron can be identified by long displacement
- b tagging reduce # of jet-to-parton assign.
 - ❖ Ex) lepton+jets channel
 - ❖ 24 (0-btags), 6(1-btags), 2(2-btags)
- b tagging improve signal to background ratio significantly – 40% effi., 0.5% fake

Sample	Di-lepton (e, μ)	Lepton+jets (e, μ)	All Hadronic NN selection
0-b-tags S/B	1:1	1:4	1:20
1-b-tags S/B	4:1	4:1	1:5
2-b-tags S/B	20:1	20:1	1:1
Events in 1 fb^{-1} (≥ 1 b-tag)	25	180	150 (2 b-tags)

Jet energy scale



Measured JES uncertainty

Lepton+jets : $1.0 \text{ GeV}/c^2$

Dilepton : $2.9 \text{ GeV}/c^2$

(CDF 4.8 fb^{-1} , template method)

In situ JES calibration

Measurement technique (Matrix element technique)

- Try to extract as much information as possible from every event using theoretical prediction for ttbar production and decay
- Integrate over unknown parton energies given a measured jet energy
- For each event, we calculate probability to be ttbar with certain mass M_{top} (also JES)

**Transfer function between parton
and detector response**

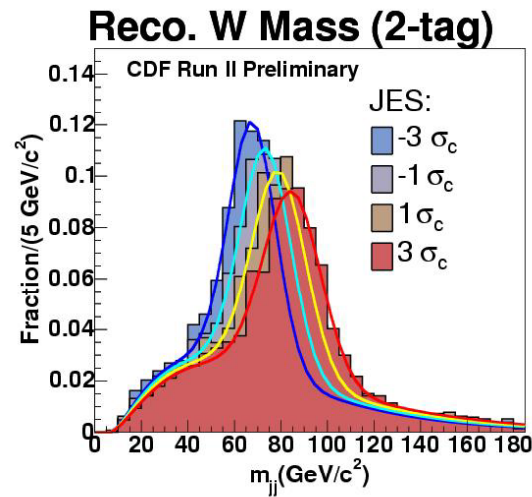
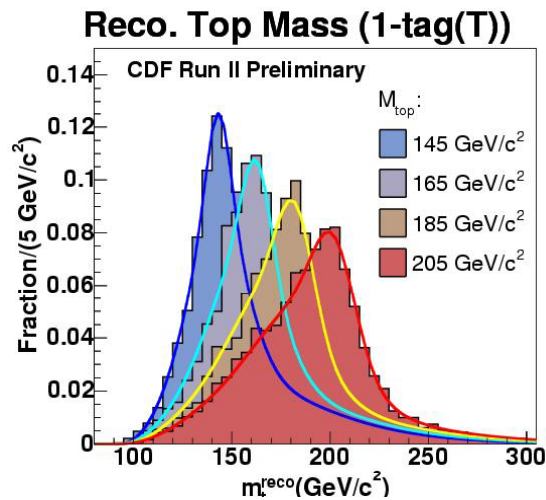
$$P(\vec{x}; M_{top}, JES) \propto \int ME \times TF \times PDF$$

ttbar Matrix element **Parton distribution
function**

- Background probability is also calculated using background matrix element
- Perform the likelihood fit using event probability

Measurement technique (template method)

- Identify variables \vec{x} sensitive to M_{top} (or JES)
- Using MC, generate signal distribution of \vec{x} as a function of M_{top} (or JES)
- Parametrize templates in terms of probability density function then assign the probability for certain mass and JES



$$P(\vec{x}; M_{top}, \Delta JES)$$

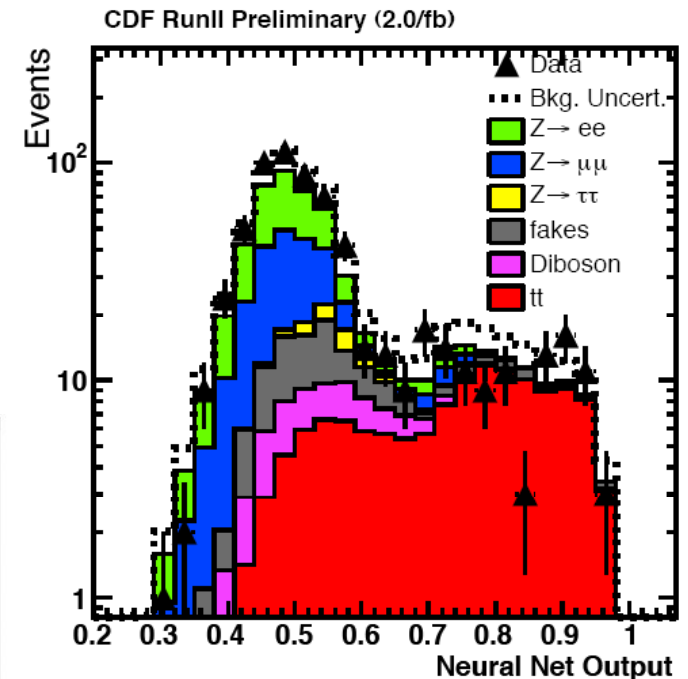
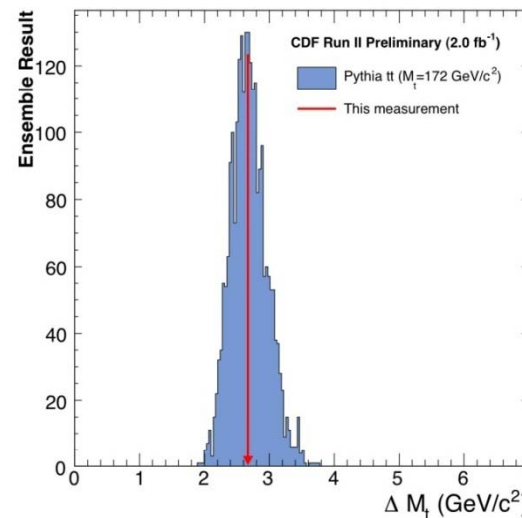
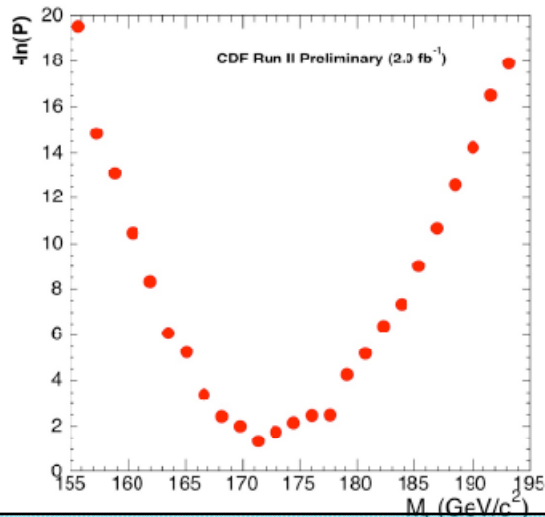
Event reconstruction
in the lepton+jets

$$\chi^2 = \sum_{i=l,4jets} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(U_j^{fit} - U_j^{meas})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{l\nu} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - m_t^{reco})^2}{\Gamma_t^2} + \frac{(M_{bl\nu} - m_t^{reco})^2}{\Gamma_t^2}$$

- Construct likelihood based on probabilities

Dilepton channel, Matrix Element

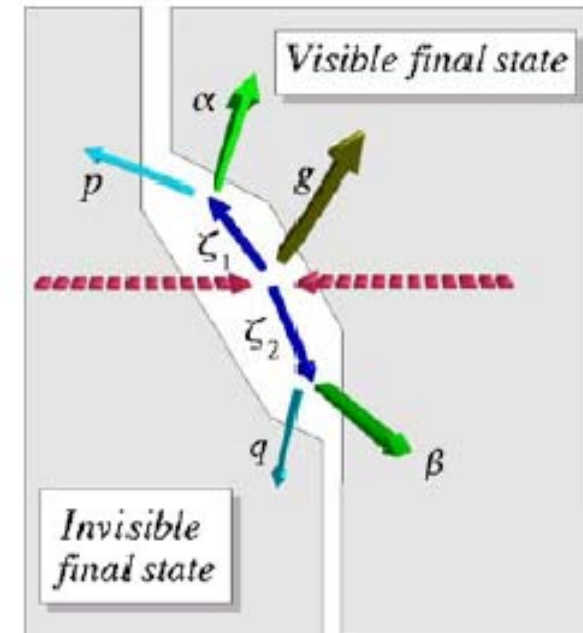
- 2.0 fb⁻¹ data, Matrix element method
- Event selection was optimized for top quark mass measurement using NN
- More sensitive analysis than template method



$$171.2 \pm 2.7 \text{ (stat)} \pm 2.9 \text{ (syst)} \text{ GeV}/c^2$$
$$= 171.2 \pm 4.0 \text{ GeV}/c^2$$

m_{T2}

- Introduced to measure the mass of new physics particle)
 - ❖ Most of new physics predict long-live stable particle – dark matter candidate
 - ❖ We expect missing particle at the final state
 - ❖ If we consider pair production of new physics particle, it will have two missing particle
- Top dilepton channel have exactly same final state



$$m_{T2} = \min[\max(m_{T(1)}, m_{T(2)})]$$
$$\mathbf{q}_T + \mathbf{p}_T = \text{missing } \mathbf{p}_T$$

Alan Barr, Christopher Lester and Phil Stephens
J. Phys. G: Nucl. Part. Phys. 29 (2003) 2343–2363

Event Reconstruction

- We modified nominal kinematic fitter to get mass difference

$$\begin{aligned} \chi^2 = & \sum_{i=\ell, 4jets} \frac{(p_T^{i,fit} - p_T^{i,meas})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(U_j^{fit} - U_j^{meas})^2}{\sigma_j^2} \\ & + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{\ell\nu} - M_W)^2}{\Gamma_W^2} \\ & + \frac{(M_{bjj} - (172.5 + dM_{reco}/2))^2}{\Gamma_t^2} + \frac{(M_{b\ell\nu} - (172.5 - dM_{reco}/2))^2}{\Gamma_t^2} \end{aligned}$$

$$\Delta m_{reco} = -Q_{lepton} \times dM_{reco}$$

- This variable is corresponding to top quark mass minus anti-top quark mass in reconstruction level