



Hadronic $b \rightarrow c$ decays at Belle

($B^+ \rightarrow D^{(*)}K$ Dalitz, $B^0 \rightarrow D_s^{(*)}h$, $B^- \rightarrow \bar{p}\Lambda D$)

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Outline

Efforts put

- in the direct determination of φ_3
 - $B^\pm \rightarrow D^{(*)}K^\pm$ Dalitz or GGSZ (ref: [Giri et al, Phys. Rev. D, 68, 054018 \(2003\)](#))
- towards indirect determination of φ_3
 - $B^0 \rightarrow D_s^{(*)}h$ in $B^0 \rightarrow D^{(*)}\pi$ TCPV (ref: [Dunietz et al, Phys. Rev. D, 65, 054025 \(2002\)](#))
- in testing of the *generalized factorization*
 - $B^- \rightarrow \bar{p}\Lambda D$ (ref: [C. Chen, Phys. Rev. D, 78, 054016 \(2008\)](#))

CKM matrix and Φ_3 (γ) Angle

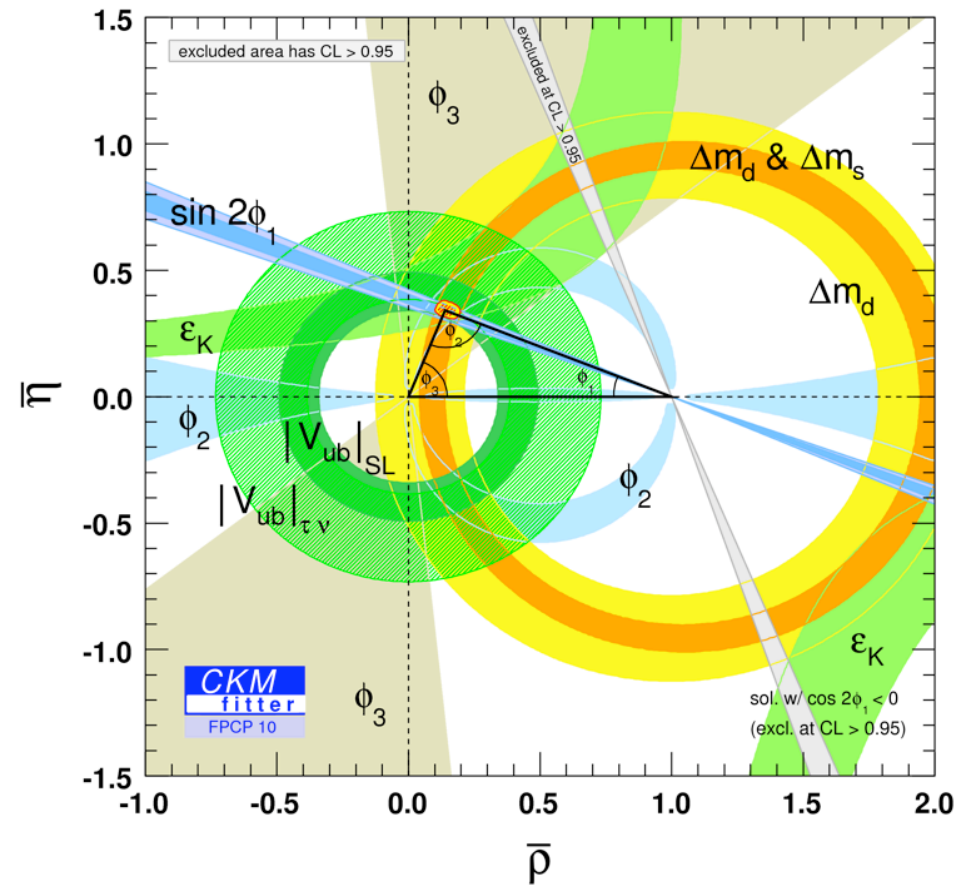
- Current CKM picture, as shown in FPCP10 by the *CKMfitter* group

$$\phi_1 = (21.15^{+0.90}_{-0.88})$$

$$\phi_2 = (89.0^{+4.4}_{-4.2})$$

$$\phi_3 = (70^{+14}_{-21})$$

(in degree)



Angle φ_3 needs more efforts and is more difficult to estimate

Event Selection

- charged tracks:
 - $|dr| < 0.2 \text{ cm}$, $|dz| < 4 \text{ cm}$
- photon:
 - $E_\gamma > 100 \text{ MeV}$
- charged hadron (K/ π):
 - $\mathcal{L}_{\text{Total}} = \mathcal{L}_{\text{CDC}} \times \mathcal{L}_{\text{TOF}} \times \mathcal{L}_{\text{ACC}}$
 - $\mathcal{L}(\text{K}/\pi) > 0.6$ for a kaon
 - efficiency $\sim 85\%$, fake rate $\sim 10\%$
- K_S^0 :
 - reconstructed from $\pi^+\pi^-$
 - quality check based on vertex topology
 - $|M(K_S^0) - M_{\text{PDG}}| < 10 \text{ MeV}/c^2$

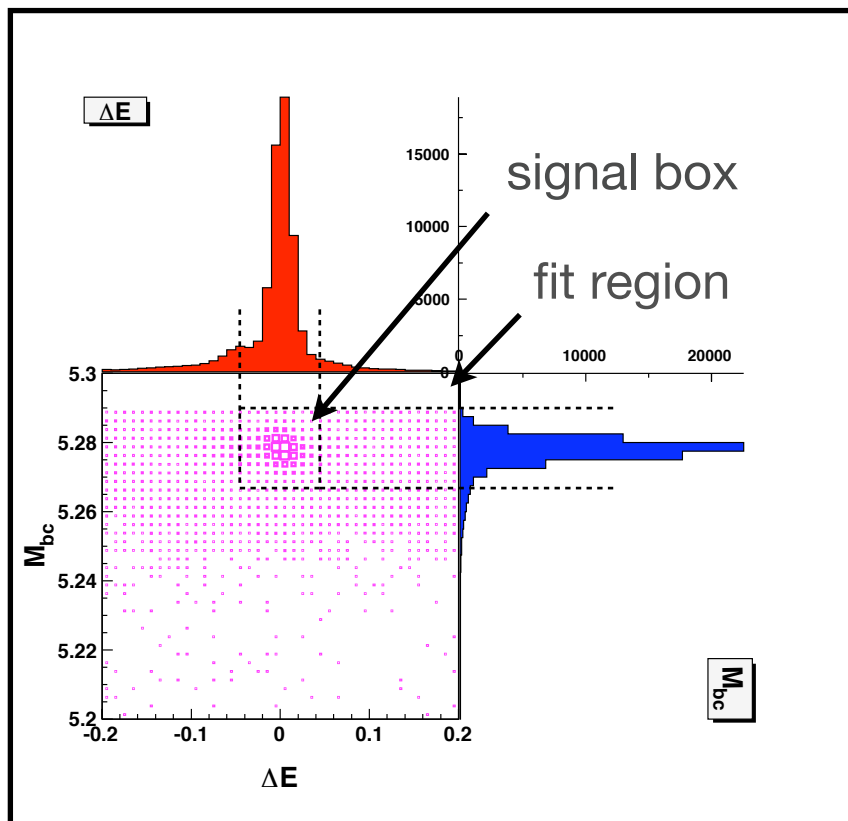
Continuum suppression:

Likelihood based on event topology

- Fisher \mathcal{F} ,
- B meson thrust angle $\cos\theta_{\text{th}}$,
- B meson polar angle $\cos\theta_B$

B meson Reconstruction:

- B^0 candidate selection based on kinematically uncorrelated ΔE and M_{bc} variables



$$M_{bc} = \sqrt{E_{\text{beam}}^2 - \left(\sum_i p_i^*\right)^2}$$
$$\Delta E = \sum_i E_i^* - E_{\text{beam}}$$

where,

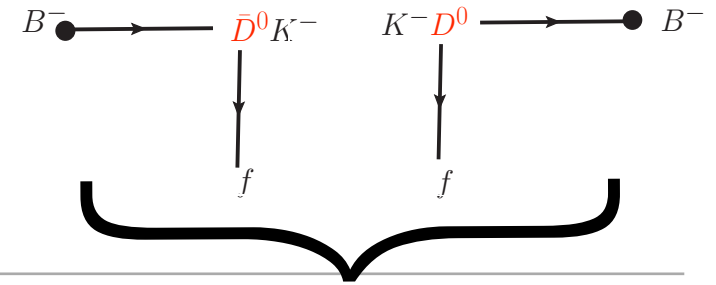
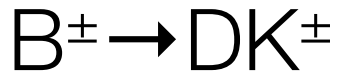
(E_i^*, p_i^*) are the i^{th} final-state 4-momentum in the center-of-mass frame, and

E_{beam} is the beam energy

All results on 657 M $B\bar{B}$ events!

$$\underline{B^\pm \rightarrow D^{(*)} K^\pm}$$

(Dalitz)



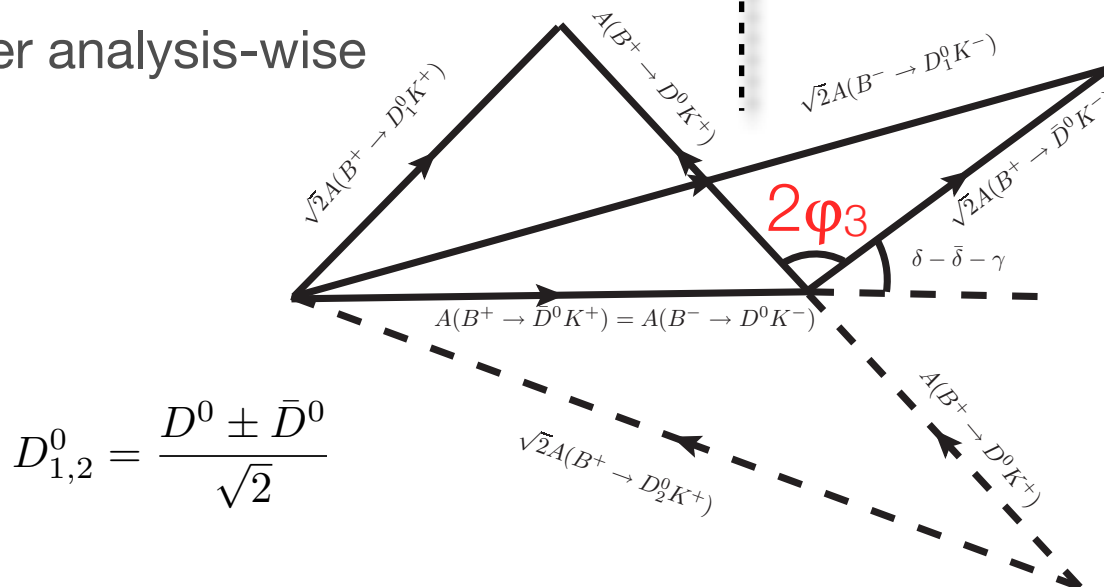
interfere

ADS

- $f = K^+\pi^-$
- col. sup. x Cabibbo allowed \sim col. allowed x Cabibbo sup.
- no control over strong phases
- statistically limited
- simpler analysis-wise

Dalitz

- $f = K_S^0\pi^+\pi^-$
- Cabibbo allowed modes
- large strong phases due to resonances
- most sensitive
- needs Dalitz analysis



$$D_{1,2}^0 = \frac{D^0 \pm \bar{D}^0}{\sqrt{2}}$$

model dependent/
independent
dependency:
D⁰ decay model
(Isobar, BW)

B → D^(*)K Dalitz (model dependent)

- Amplitude for B[±] → DK[±] process can be expressed as

$$M_{\pm} = f(m_{\pm}^2, m_{\mp}^2) + r_{\pm} e^{\pm i\phi_3 + i\delta} f(m_{\mp}^2, m_{\pm}^2)$$

$$m_{\pm}^2 = m_{K_S^0 \pi^{\pm}}^2$$

amplitude of D⁰ → K_S⁰ π⁺ π⁻ decay :

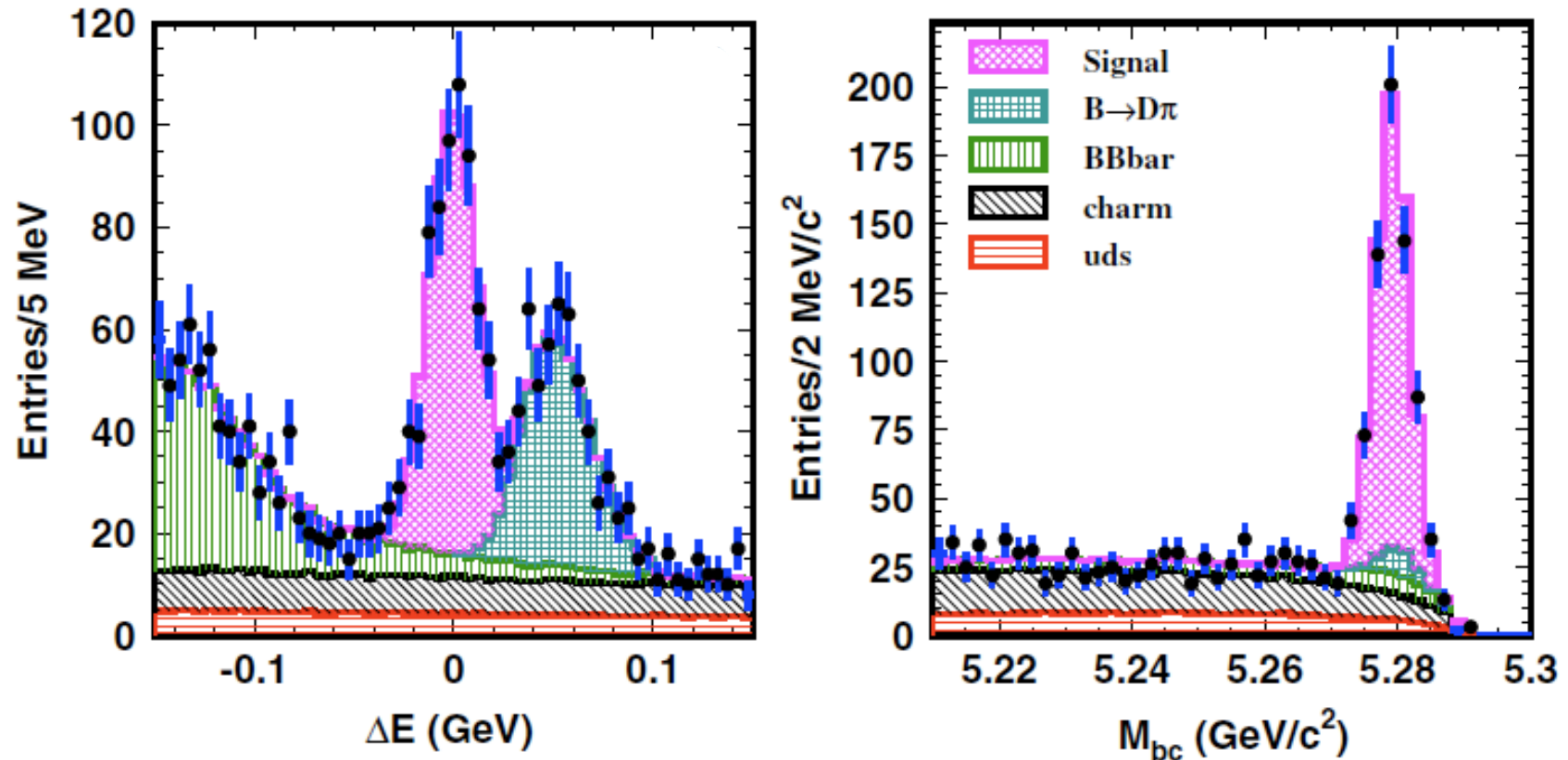
- determined from Dalitz plot of large continuum data,
- flavor-tagged by soft pion charge in D^{*±} → D π_S[±]
- assuming isobar model, BW shapes for resonances

Analysis procedure:

- first step: background fractions are obtained from ΔE-M_{bc} 2D unbinned maximum likelihood (UML) fit
- Second step: Dalitz, with likelihoods (continuum separation) inside the fit using $x_{\pm} = r_{\pm} \cos(\pm\phi_3 + \delta)$ and $y_{\pm} = r_{\pm} \sin(\pm\phi_3 + \delta)$

$B \rightarrow DK \Delta E - M_{bc}$

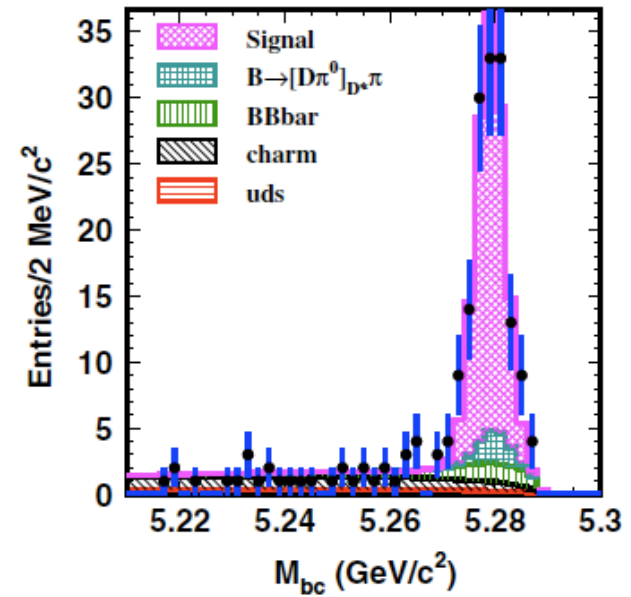
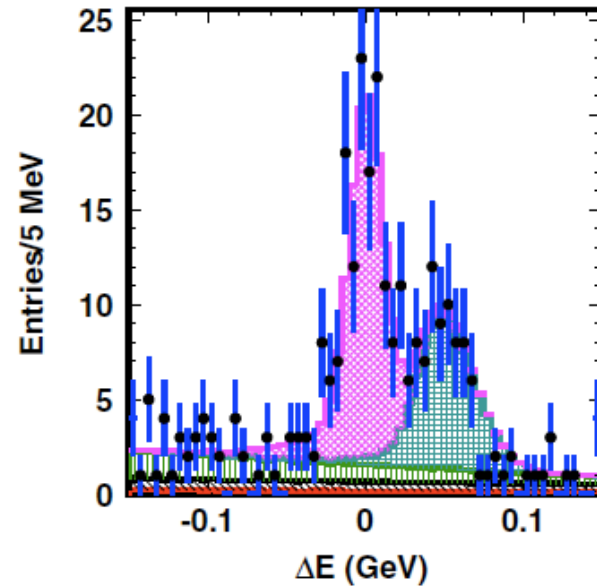
A 2D UML fit with free parameters: background relative fractions



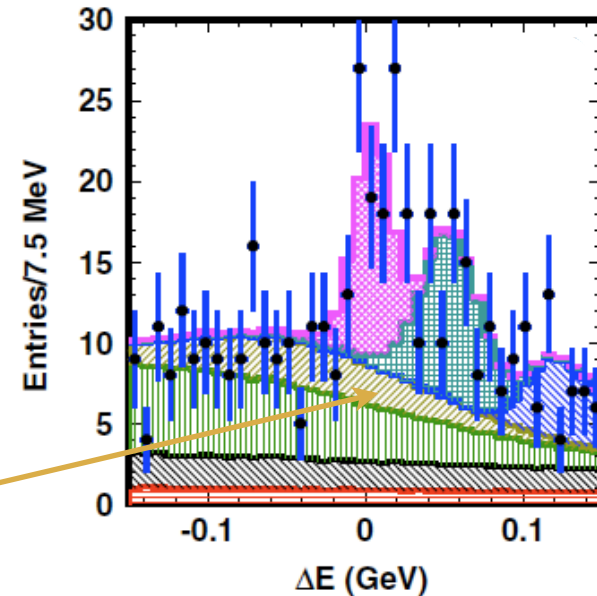
Note: continuum background is separated into **charm** and **u,d,s** components

$B \rightarrow D^* K \Delta E - M_{bc}$

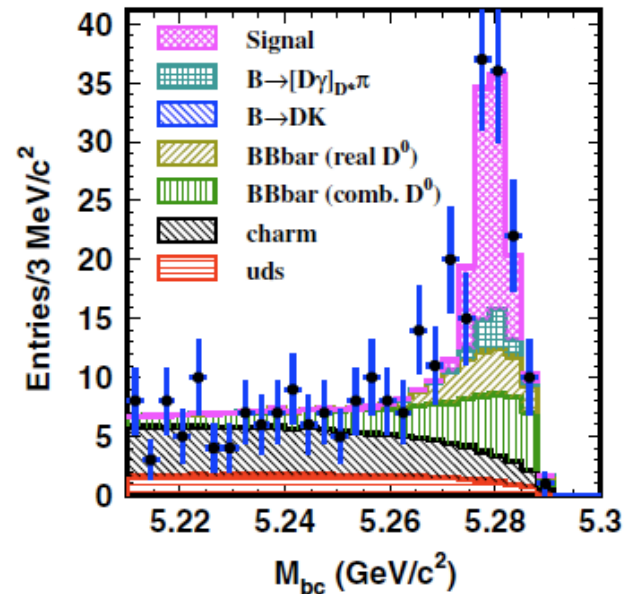
• $D^* \rightarrow D\pi^0$



• $D^* \rightarrow D\gamma$

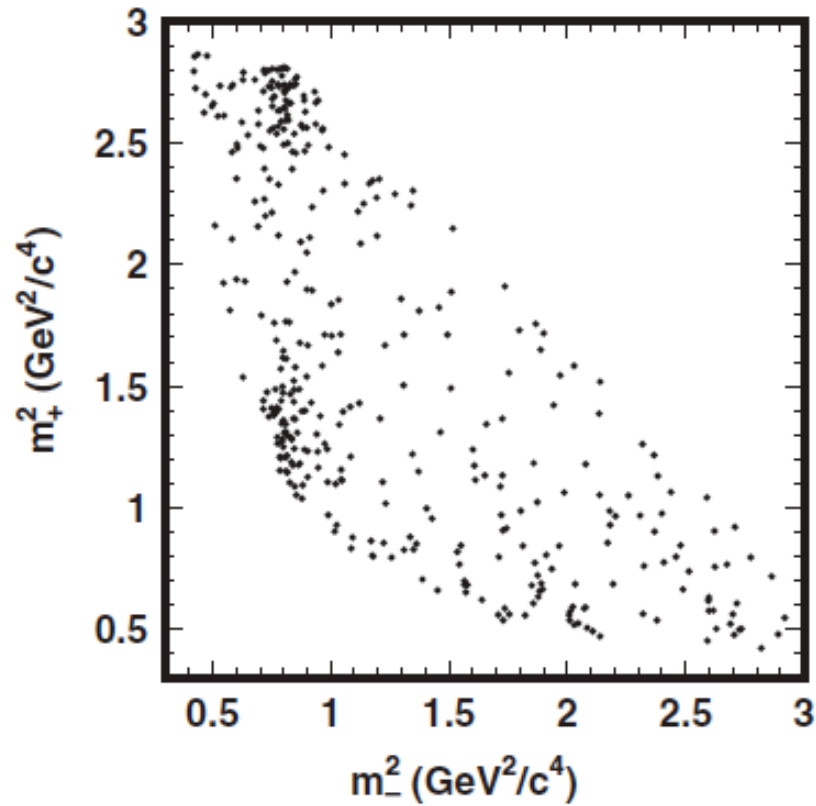


photon
cross-feed

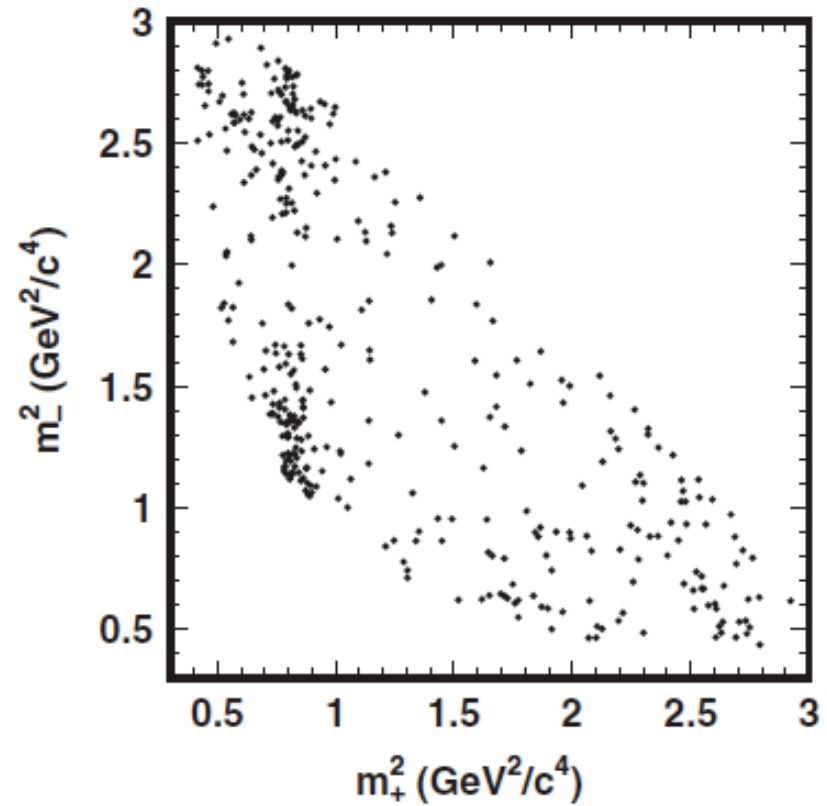


B → DK Dalitz

$B^+ \rightarrow DK^+$

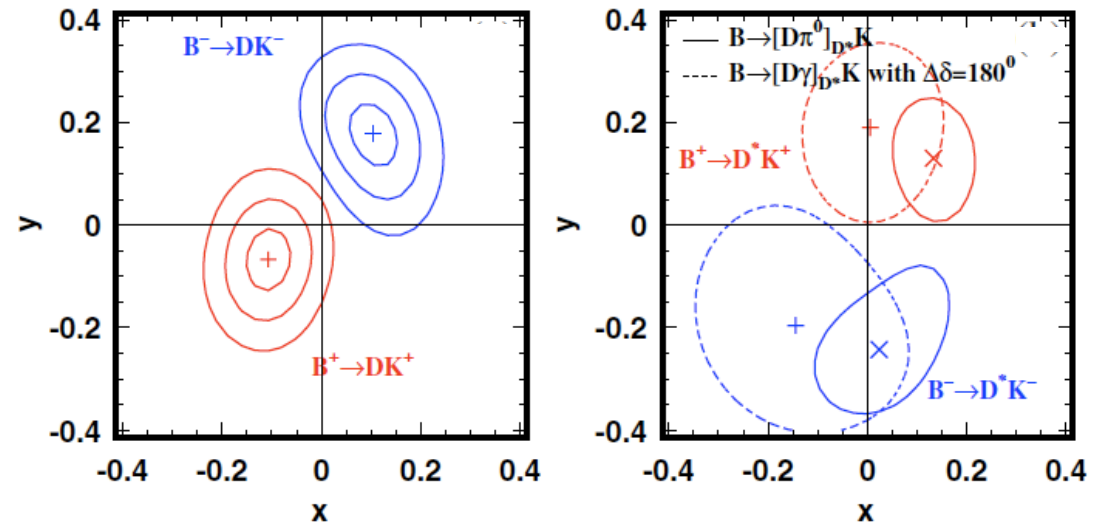


$B^- \rightarrow DK^-$



$B \rightarrow D^{(*)}K$ Dalitz (model dependent)

To improve sensitivity,
combine various
 $B^\pm \rightarrow D^{(*)}K^\pm$ modes



- combined $B^\pm \rightarrow D^{(*)}K^\pm$ results:

Parameter	1σ interval	2σ interval	Systematic error	Model uncertainty
ϕ_3	$(78.4^{+10.8}_{-11.6})^\circ$	$54.2^\circ < \phi_3 < 100.5^\circ$	3.6°	8.9°
r_{DK}	$0.160^{+0.040}_{-0.038}$	$0.084 < r_{DK} < 0.239$	0.011	$+0.050 - 0.010$
r_{D^*K}	$0.196^{+0.072}_{-0.069}$	$0.061 < r_{D^*K} < 0.271$	0.012	$+0.062 - 0.012$
δ_{DK}	$(136.7^{+13.0}_{-15.8})^\circ$	$102.2^\circ < \delta_{DK} < 162.3^\circ$	4.0°	22.9°
δ_{D^*K}	$(341.9^{+18.0}_{-19.6})^\circ$	$296.5^\circ < \delta_{D^*K} < 382.7^\circ$	3.0°	22.9°

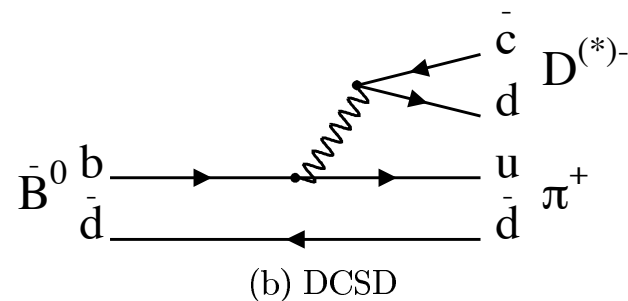
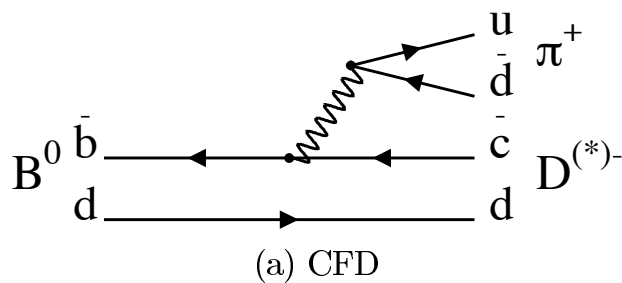
possible to remove model uncertainty:
perform a fit in the momentum-binned Dalitz plot
(much along the original idea of GGSZ)

$$\mathbf{B} \rightarrow \mathbf{D}_s^{(*)} \mathbf{h}$$
$$(\mathbf{h} = \mathbf{K}/\pi)$$

Time dependent CP Analysis

$$B^0 \rightarrow D^{(*)\mp} \mp \pi^\pm$$

- theoretically cleanest method of extracting the $\sin(2\phi_1 + \phi_3)$ and hence the ϕ_3
- Initial state B^0 can be found in the state $D^{*\mp}\pi^\pm$ state in two ways: either through CFD or via mixing followed by DCSD



- The DCSD involves $b \rightarrow u$ transition, and the phase ϕ_3 shows up due to the interference between the two as,

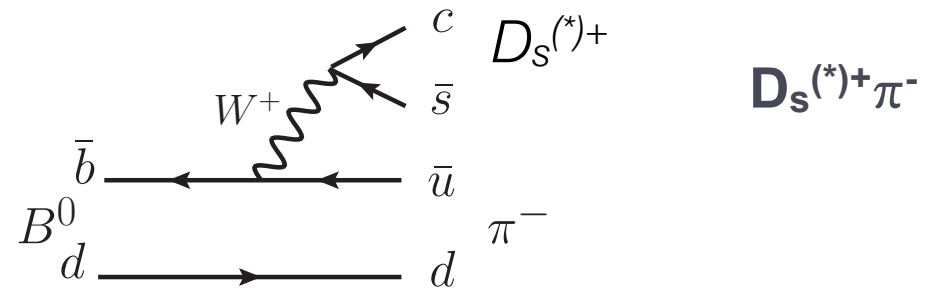
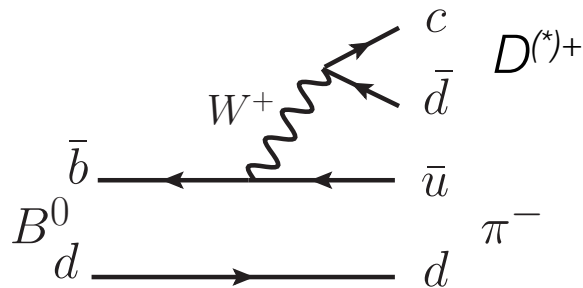
$$R_{D^{(*)}\pi} \sin(2\phi_1 + \phi_3)$$

where, $R_{D^{*\pi}}$ is the ratio of magnitude of DCSD and CFM amplitude and must be provided externally.

$B^0 \rightarrow D_s^{(*)} h$

- $B^0 \rightarrow D_s^{*+} \pi^-$ is related to $B^0 \rightarrow D^{*+} \pi^-$ (DCSD) by SU(3) symmetry

DCSD



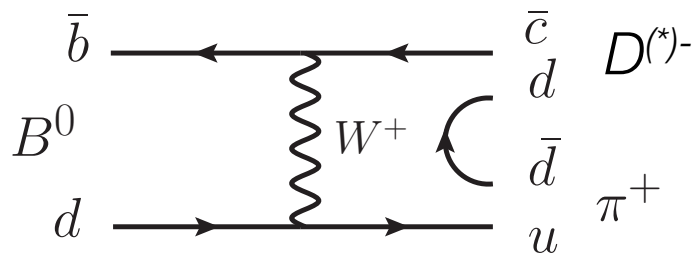
which means, $\mathcal{R}_{D^{(*)}\pi} = \tan \theta_C \frac{f_{D^{(*)}}}{f_{D_s^{(*)}}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{(*)+} \pi^-)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \pi^+)}}$

Theory predicts

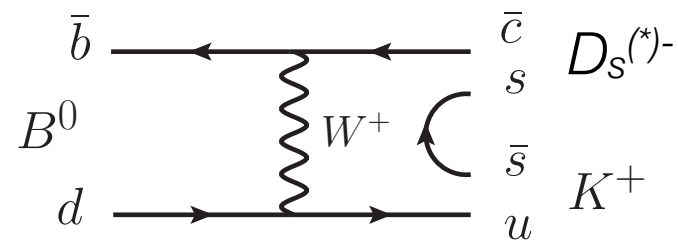
$$\mathcal{R}_{D^{(*)}\pi} \sim 2\%$$

$B^0 \rightarrow D_s^{(*)} h$

- $B^0 \rightarrow D_s^{*-} K^+$ is related to CFD W -exchange by SU(3) symmetry



CFD W -exchange



$B^0 \rightarrow D_s^{*-} K^+$

- $B^0 \rightarrow D_s^{*-} K^+$ is expected to be enhanced due to re-scattering effects \Rightarrow needs check!

(ref: Phys. Rev. Lett., **78**, 3999 (1997)
 Phys. Lett. B, **666**, 185 (2008))

$B^0 \rightarrow D_s h$

A ΔE - M_{D_s} 2D UML fit is performed

- signal is reconstructed in three D_s^+ decay channels: $\phi\pi$, $K^*(892)^0 K$, $K_S^0 K$
- $B^0 \rightarrow D_s^+ \pi^-$ and $B^0 \rightarrow D_s^+ K^-$ cross-feed each other
- data fitted simultaneously in 3 x 2 mutually exclusive samples

We obtained,

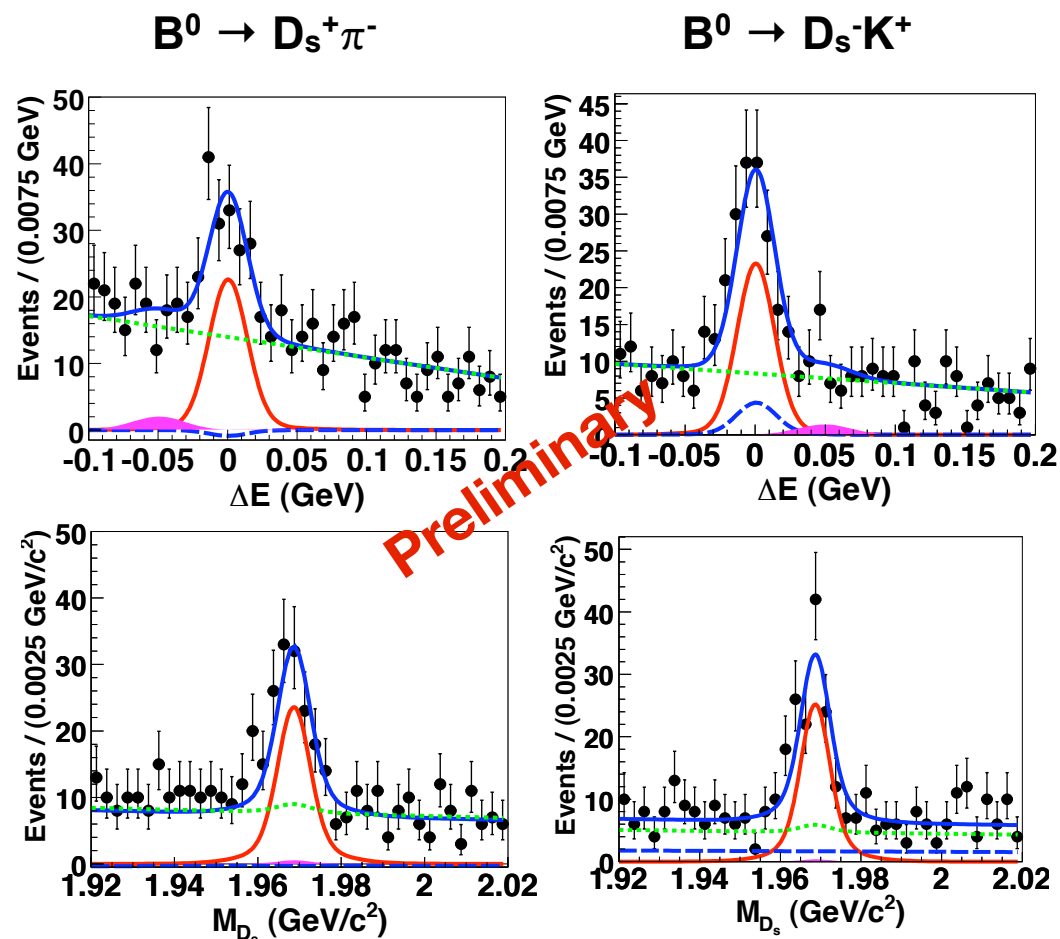
$$\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (1.99 \pm 0.26 \pm 0.18) \times 10^{-5}$$

and

$$\mathcal{B}(B^0 \rightarrow D_s^- K^+) = (1.91 \pm 0.24 \pm 0.17) \times 10^{-5}$$

with significances 8.0σ and 9.2σ , respectively.

$$\mathcal{R}_{D\pi} = [1.71 \pm 0.11(\text{stat}) \pm 0.09(\text{syst}) \pm 0.02(\text{th})]\%$$



$$B^0 \rightarrow D_s^* h$$

An UML fit to ΔE is performed to six exclusive samples

$$|M_{D_s} - M_{PDG}| < 15 \text{ MeV}/c^2$$

$$132 \text{ MeV}/c^2 < \Delta M < 168 \text{ MeV}/c^2$$

We obtain,

$$\mathcal{BR}(B^0 \rightarrow D_s^{*+} \pi^-) = (1.75^{+0.32}_{-0.34}) \times 10^{-5}$$

and

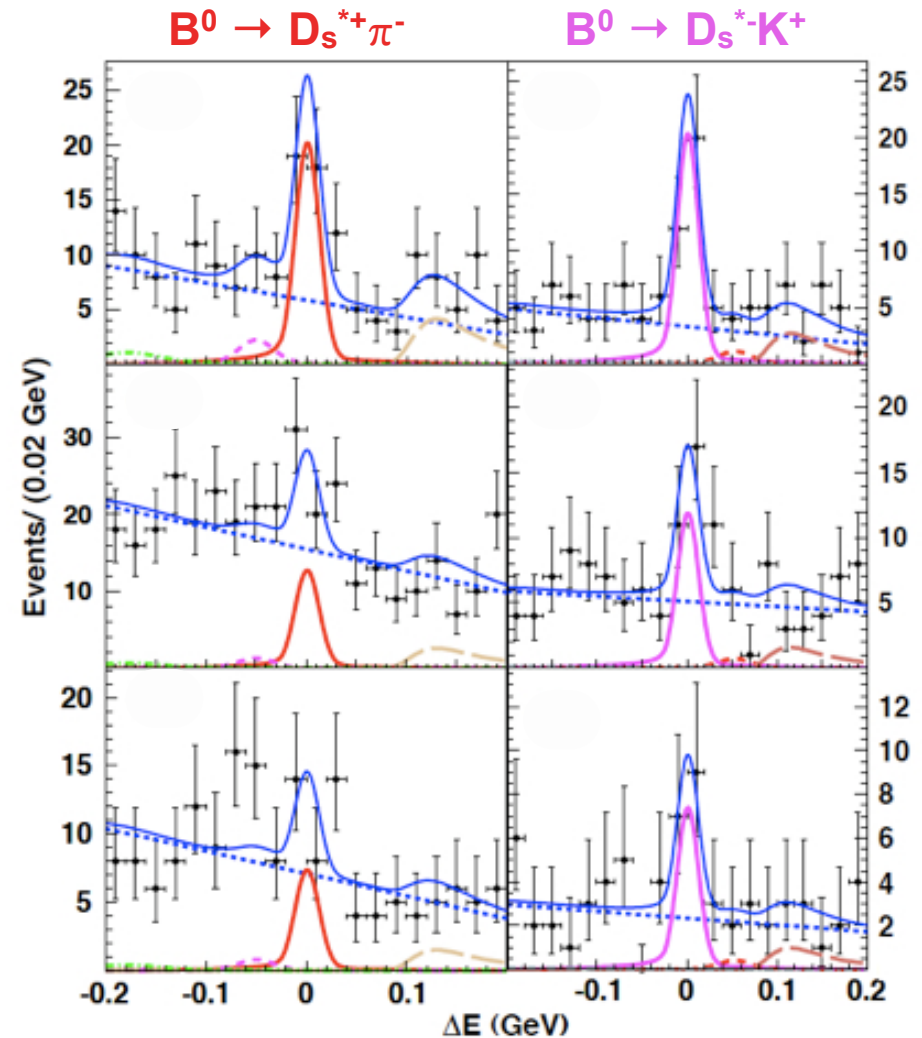
$$\mathcal{BR}(B^0 \rightarrow D_s^{*-} K^+) = (2.02^{+0.33}_{-0.31}) \times 10^{-5}.$$

with significances 6.1σ and 8.0σ , respectively

$$D_s^+ \rightarrow \phi \pi^+$$

$$D_s^+ \rightarrow K^{*0} K^+$$

$$D_s^+ \rightarrow K_S^0 K^+$$



$$\mathcal{R}_{D^* \pi} = [1.58 \pm 0.15(\text{stat}) \pm 0.10(\text{syst}) \pm 0.03(\text{th})]\%$$

$$\mathbf{B^- \rightarrow \bar{p} \Lambda D}$$

$B^- \rightarrow \bar{p} \Lambda D$: A test for *generalized factorization*

- The vertex (and the penguin correction thereof) of the hadronic matrix elements of four quark operators can be absorbed in the effective Wilson coefficients c^{eff} , so that the momentum dependence is smeared out

- Under generalized factorization:

three body amplitudes

1. current type
2. transition type
3. hybrid

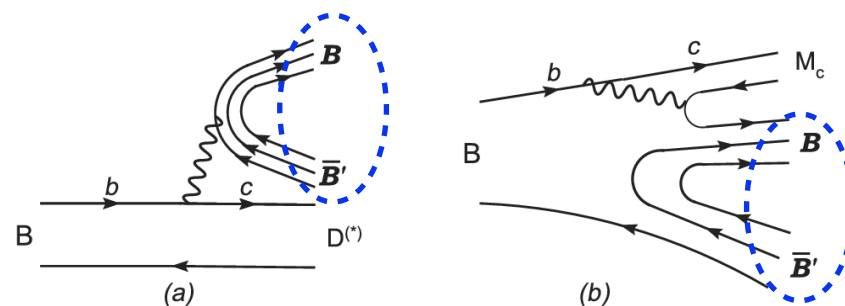


FIG. 1. Two types of the $B \rightarrow \mathbf{B}\bar{\mathbf{B}}'M_c$ decay process: (a) current type and (b) transition type.

- Under generalized factorization approximation, one predicts the decay amplitude

$$\mathcal{B}(B^- \rightarrow \bar{p} \Lambda D^0) \sim 1.1 \times 10^{-5}$$

proceeding via **threshold** enhancement.

$B^- \rightarrow \bar{p} \Lambda D^0$

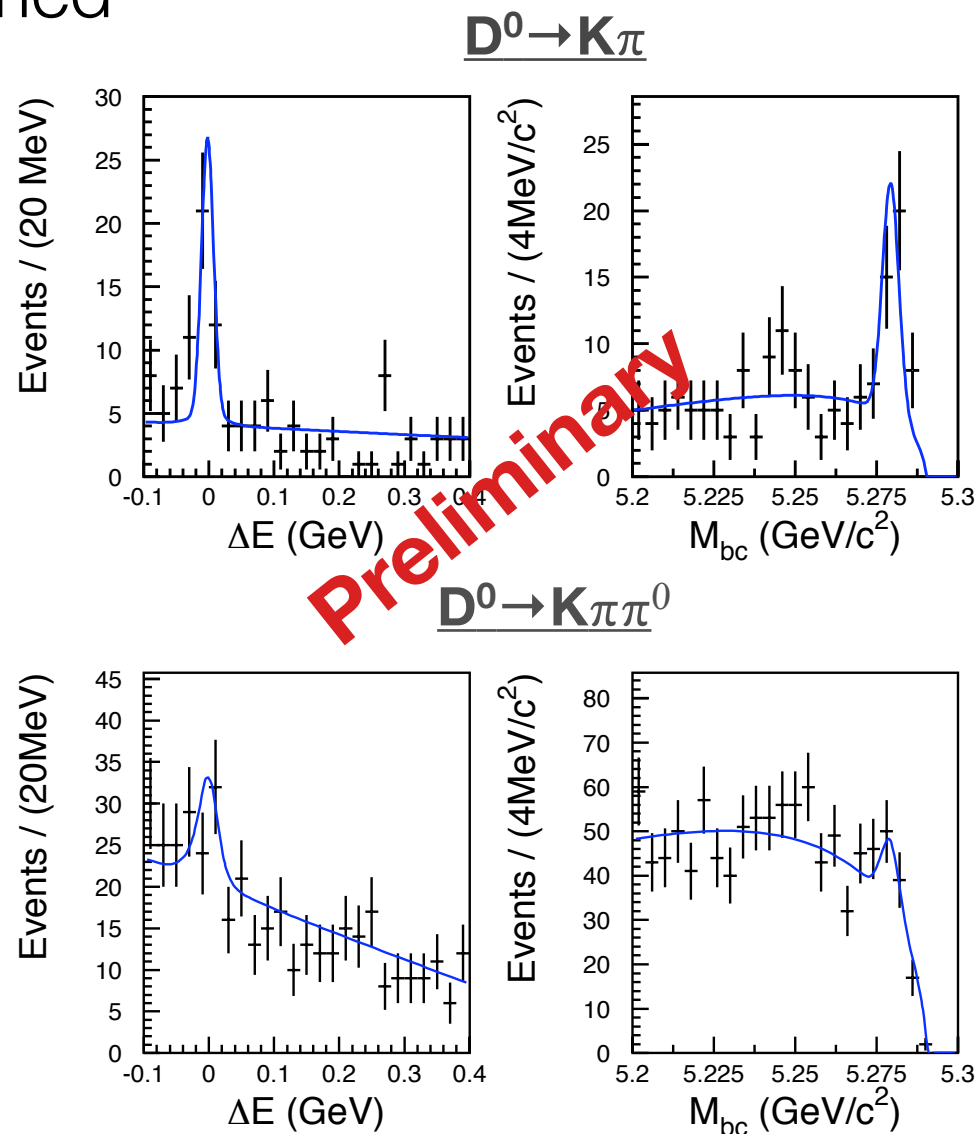
An UML fit to ΔE - M_{bc} is performed

- $\mathcal{L}(p/h) > 0.6$ for a proton
- Λ selection
 1. quality check vertex topology
 2. $1.111 \text{ GeV}/c^2 < M_\Lambda < 1.121 \text{ GeV}/c^2$
- D meson is reconstructed in two decay channels
 1. $D^0 \rightarrow K\pi$
 2. $D^0 \rightarrow K\pi\pi^0$

We report,

$$\mathcal{B}(B^- \rightarrow \bar{p} \Lambda D^0) = (1.40^{+0.27}_{-0.24} \pm 0.16) \times 10^{-5}$$

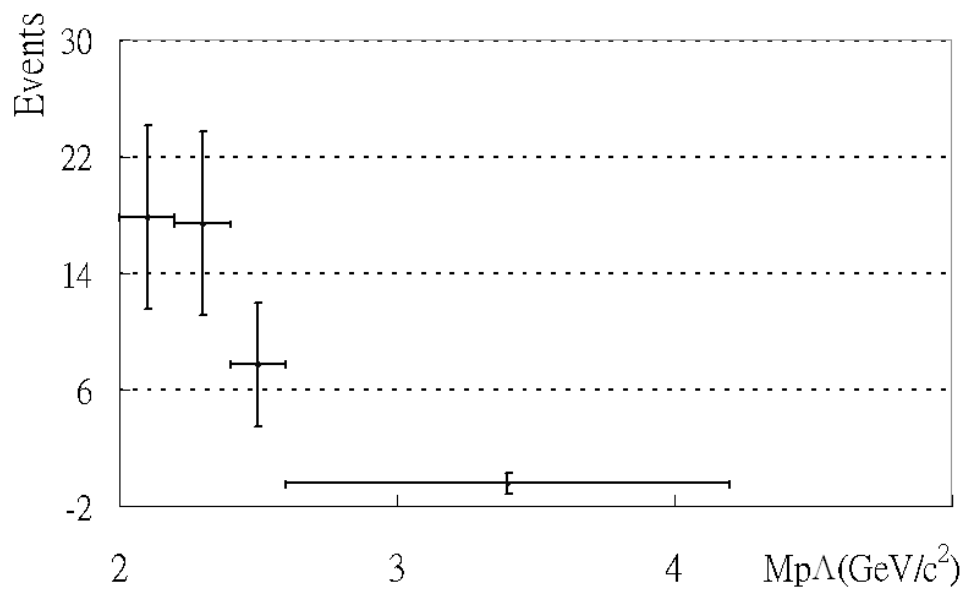
with a significance of 8.6σ .



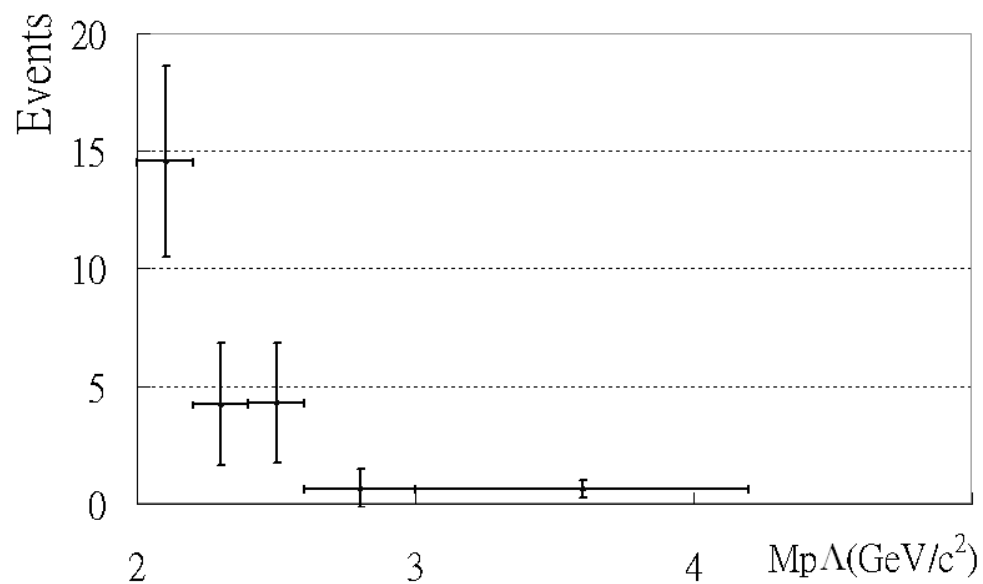
$B^- \rightarrow p \Lambda D$

We also observe $p\Lambda$ threshold enhancement near $2 \text{ GeV}/c^2$

$D^0 \rightarrow K\pi$



$D^0 \rightarrow K\pi\pi^0$



Conclusion

- We report results from $B^\pm \rightarrow D^{(*)}K^\pm$ Dalitz analysis done using isobar model, as

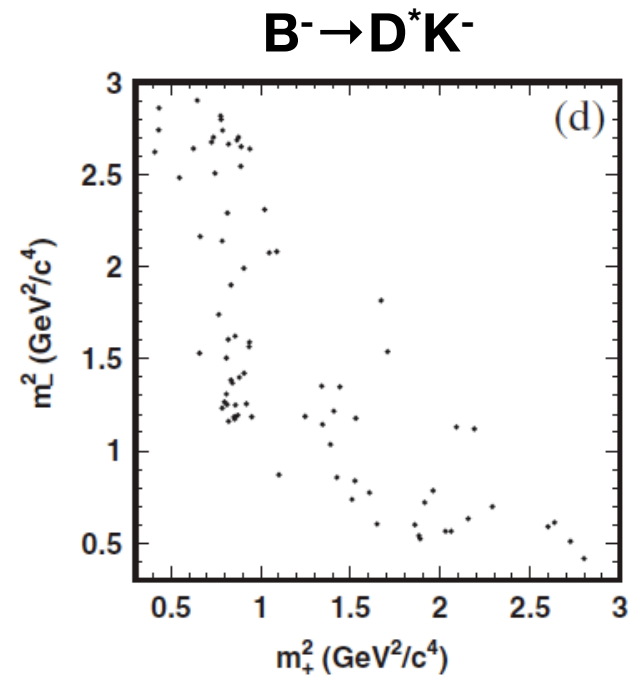
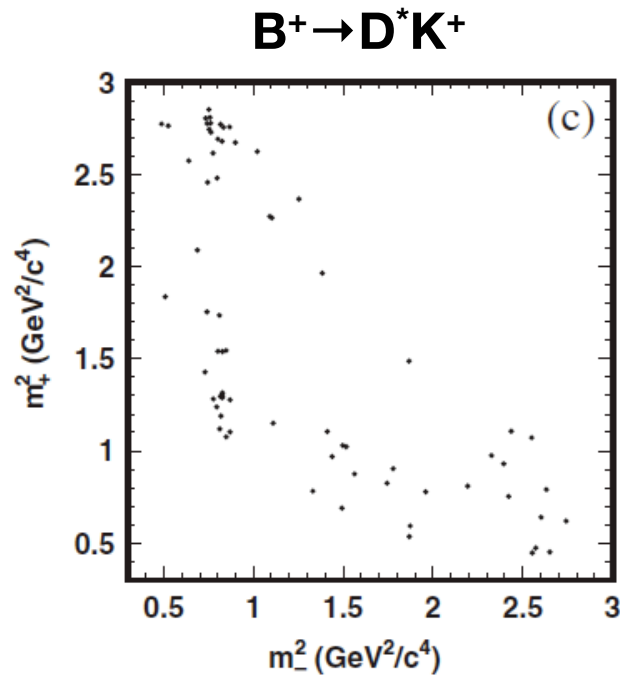
$$\phi_3 = (78.4^\circ_{-11.6^\circ}^{+10.8^\circ} \pm 3.6^\circ(\text{syst}) \pm 8.9^\circ(\text{model}))$$

- A model-independent study is undertaken to reduce the model-uncertainties.
- $B^0 \rightarrow D_s h$ measurements yield $R_{D\pi} = [1.71 \pm 0.11(\text{stat}) \pm 0.09(\text{syst}) \pm 0.02(\text{th})]\%$, consistent with the theoretical predictions of 2%
- $B^0 \rightarrow D_s^* h$ measurements yield $R_{D^*\pi} = [1.58 \pm 0.15(\text{stat}) \pm 0.10(\text{syst}) \pm 0.03(\text{th})]\%$
- $B^- \rightarrow p\Lambda D^0$ study shows agreement with the expectations from the *generalized factorization* approach

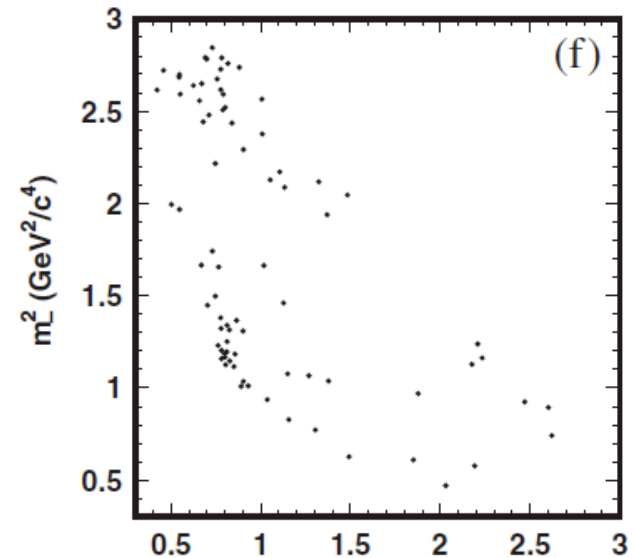
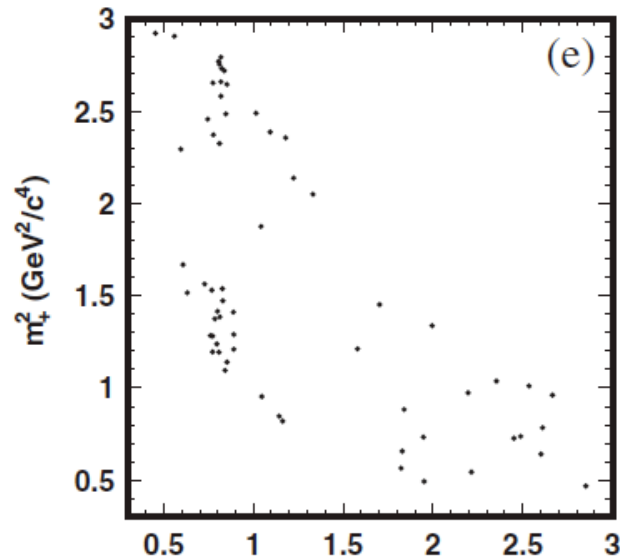
Back up

$B \rightarrow D^* K$ Dalitz

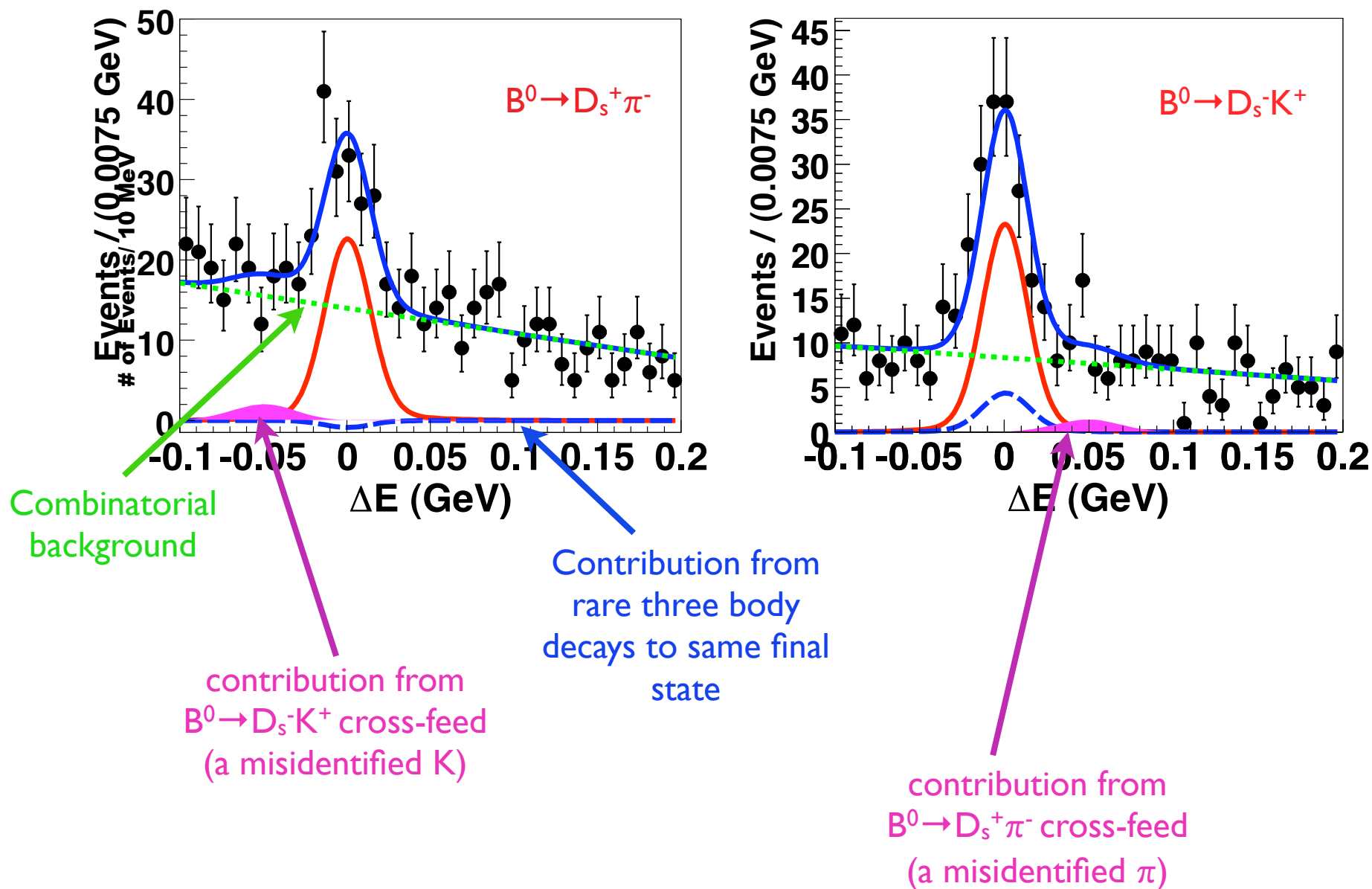
$D^* \rightarrow D\pi^0$



$D^* \rightarrow D\gamma$



Result: Fit Explained

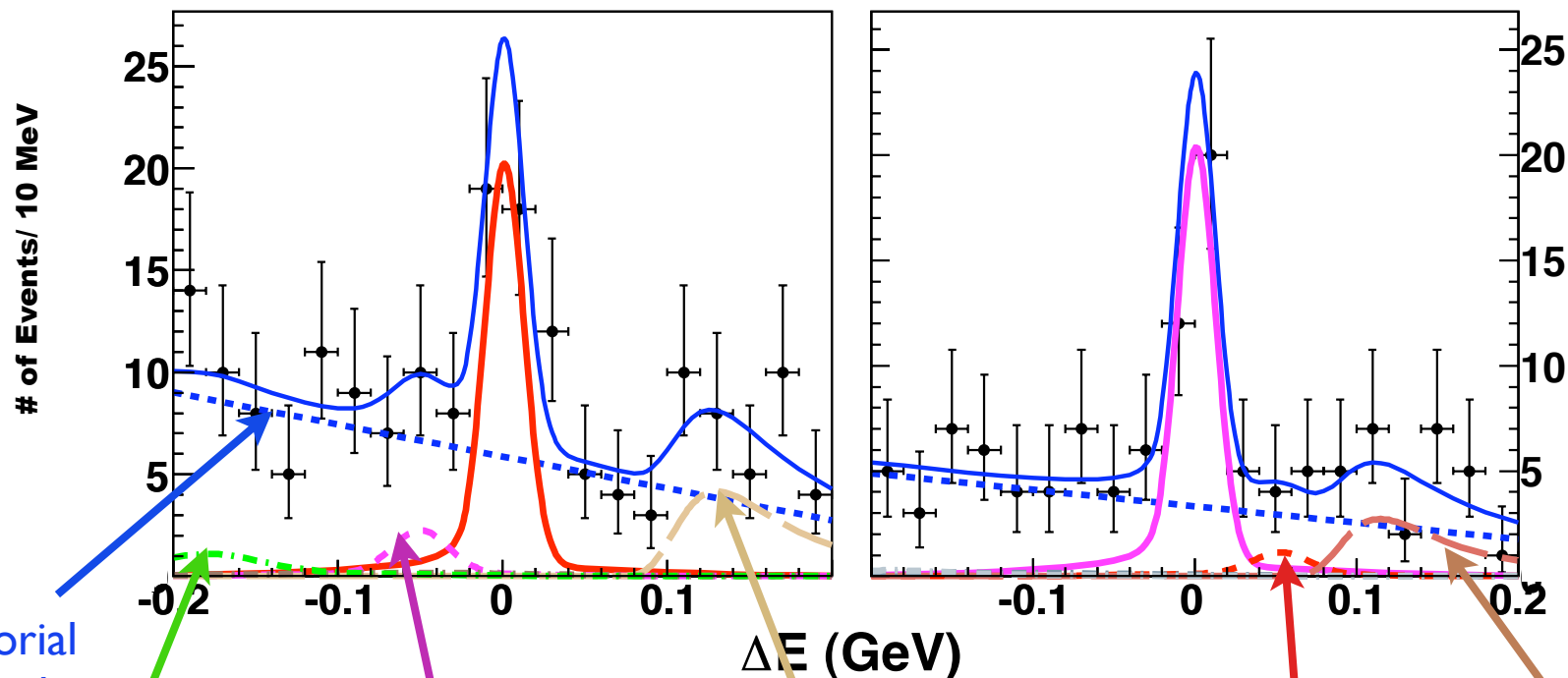


Result: Fit Explained

$B^0 \rightarrow D_s^{*+} \pi^-$

$\phi\pi$ mode

$B^0 \rightarrow D_s^{*+} K^+$



Combinatorial background:
1st order polynomial

contribution from $B^0 \rightarrow D_s^{(*)+} \rho^-$ with a missing π^0

contribution from $B^0 \rightarrow D_s^{*-} K^+$ crossfeed (a misidentified K)

contribution from $B^0 \rightarrow D_s^{*+} \pi^-$ (additional γ)

contribution from $B^0 \rightarrow D_s^{*+} \pi^-$ crossfeed (a misidentified π)

contribution from $B^0 \rightarrow D_s^- K^+$ (additional γ)

Individual branching fractions of $B^- \rightarrow p \Lambda D$

$D^0 \rightarrow K \pi$

$$\mathcal{B}(B^- \rightarrow \bar{p} \Lambda D^0 (K \pi)) = (1.43_{-0.30}^{+0.34} \pm 0.14) \times 10^{-5}$$

with a significance of 7.70σ .

$D^0 \rightarrow K \pi \pi^0$

$$\mathcal{B}(B^- \rightarrow \bar{p} \Lambda D^0 (K \pi \pi^0)) = (1.35_{-0.40}^{+0.44} \pm 0.18) \times 10^{-5}$$

with a significance of 3.85σ .