

# LMCI WITH BB IMPED. (Q=1) => COMPARISON BETWEEN

- 1) GALACLIC (Vlasov solver)
- 2) SIMPLE FORMULA (2-mode approach)
- 3) BLong and SBSC (Tracking codes)

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## ◆ Parameters used

$$f_r \tau_b = 2.7$$

$$f_0 = 43350.8 \text{ Hz}$$

$$f_r = 1 \text{ GHz}$$

$$B_0 = f_0 \tau_b$$

$$\left[ \frac{Z_l}{p} \right]_{p=0} = 8.67 \Omega$$

$$V_{RF} = 6 \text{ MV}$$

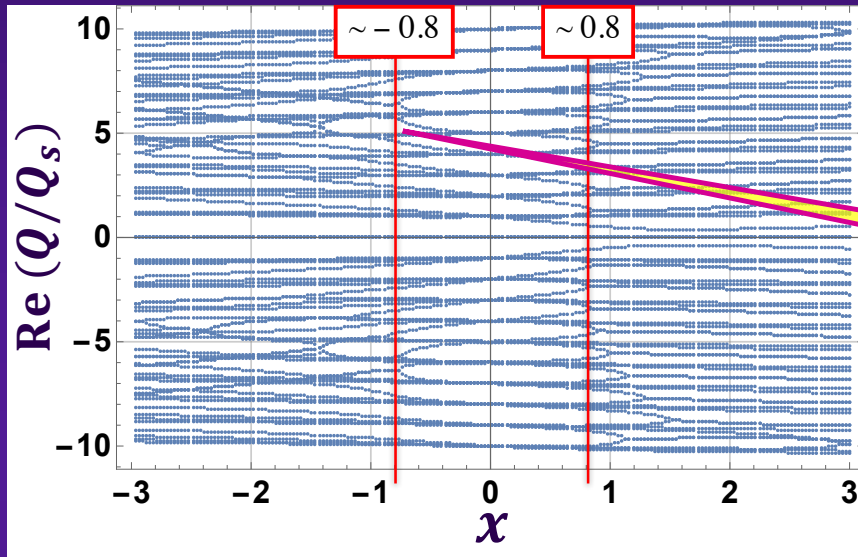
$$\omega_{s0} = 889 \text{ rad/s}$$

$$h = 462$$

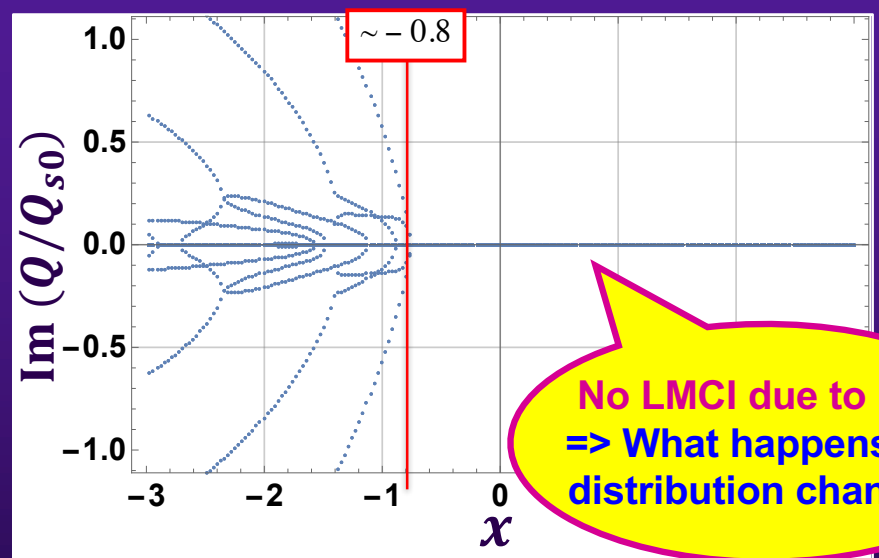
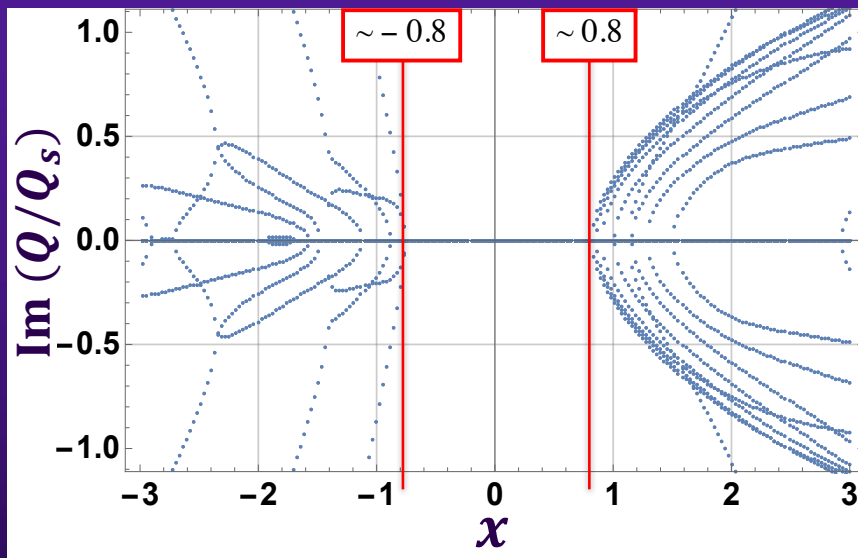
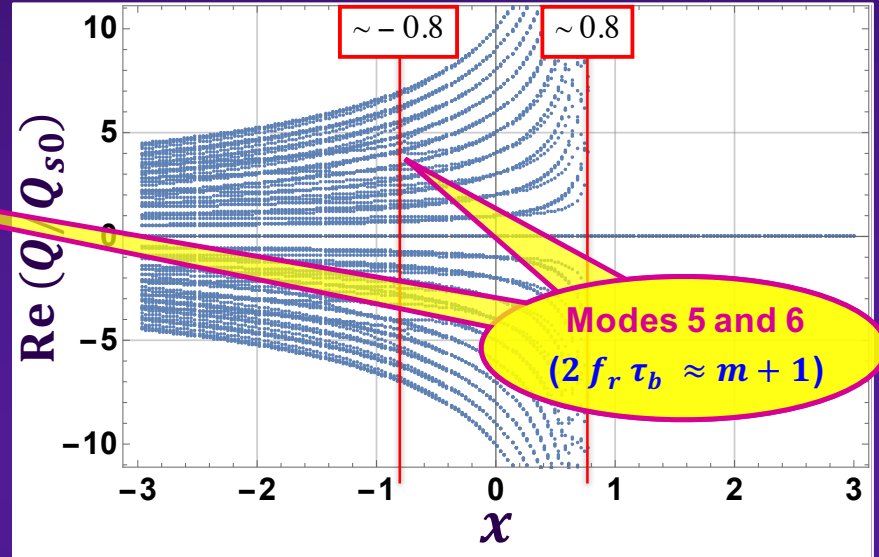
# REMINDER

GALACLIC => For PAD distribution:  $f_r \tau_b = 2.8$

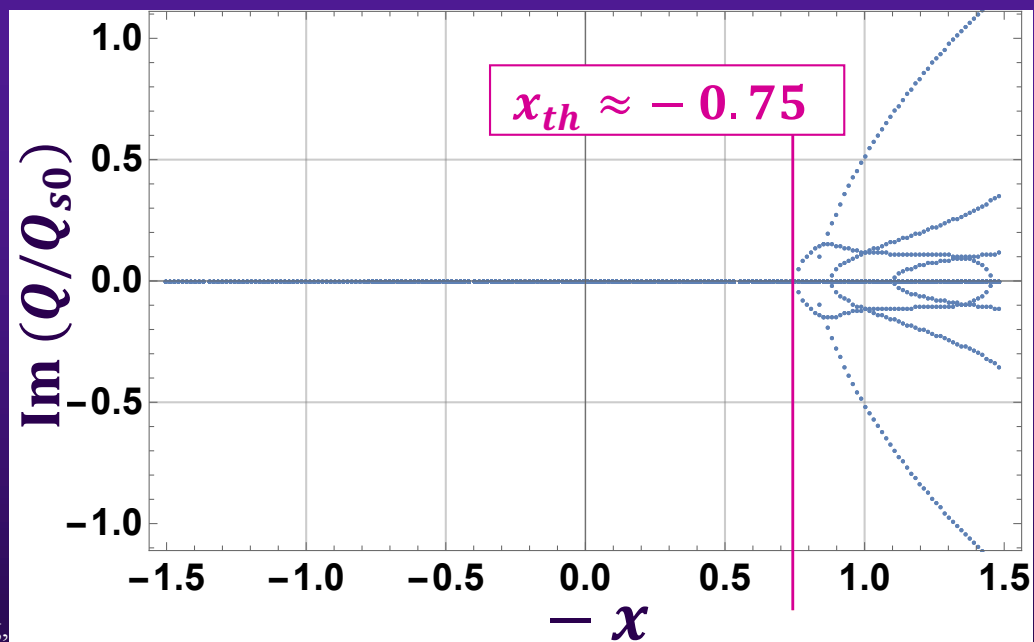
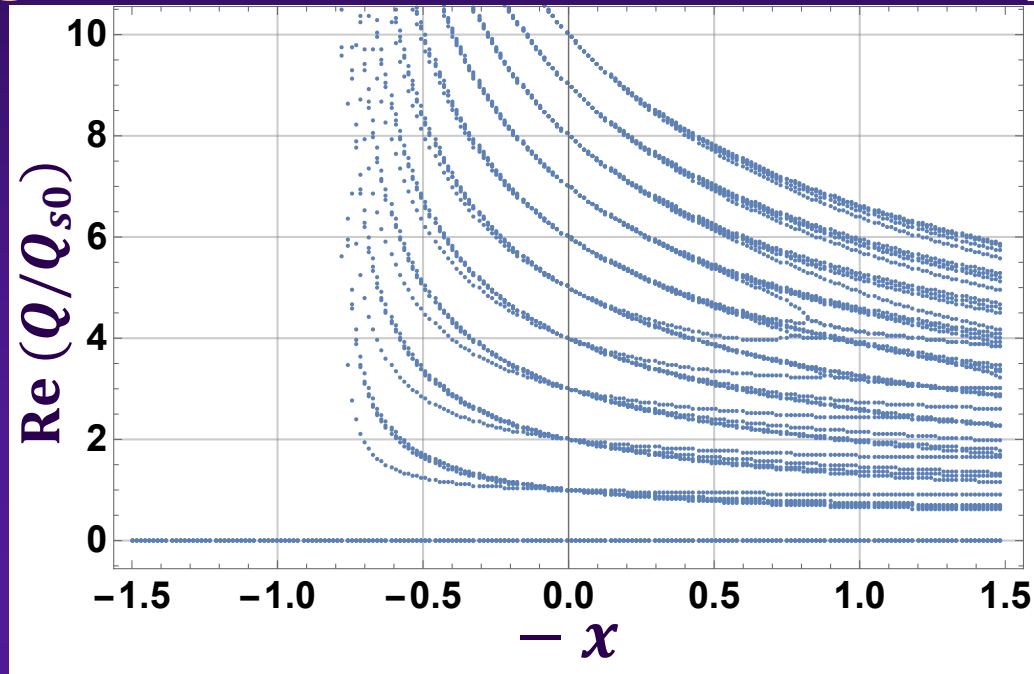
◆ GALACLIC (using  $Q_s$ )



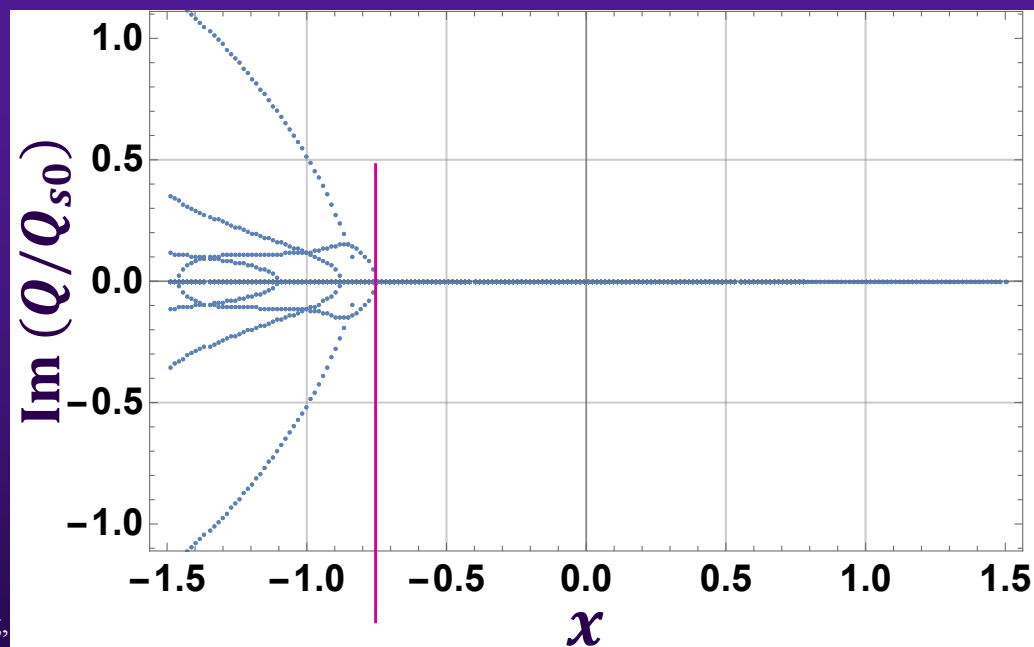
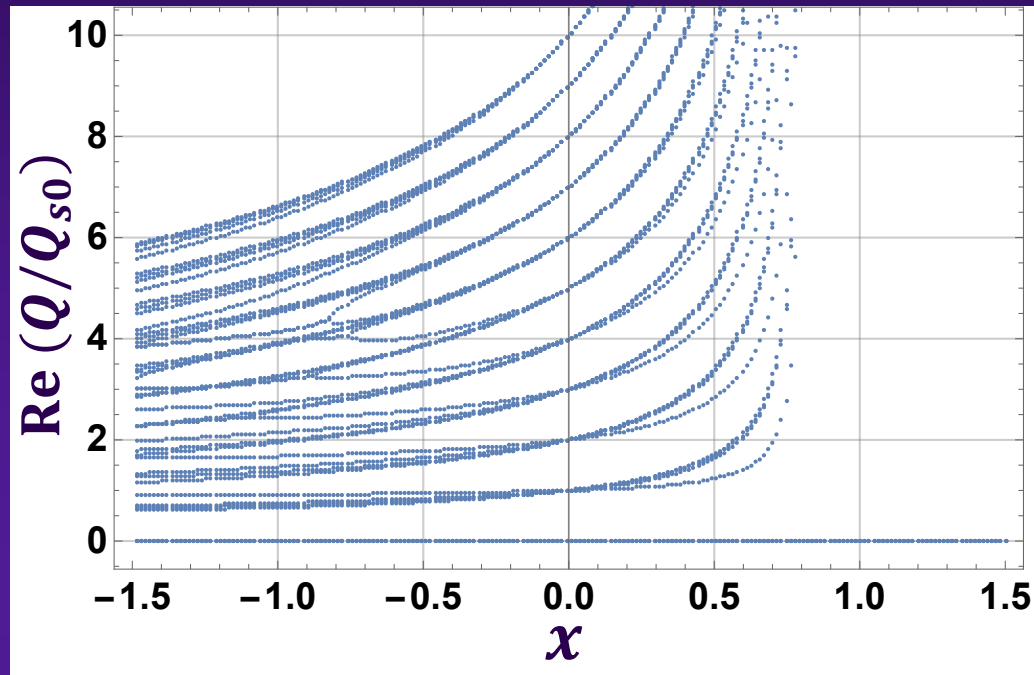
◆ GALACLIC (using  $Q_{s0}$ )



# 1) GALACLIC => For PAD distribution (& computing PWD also for PAD distribution): $f_r \tau_b = 2.7$

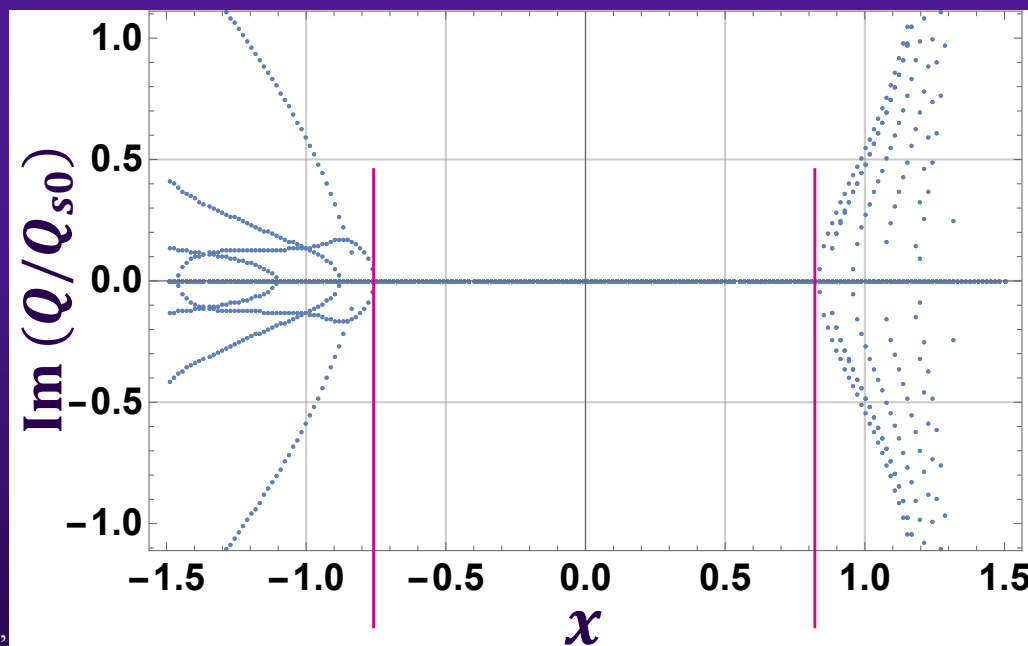
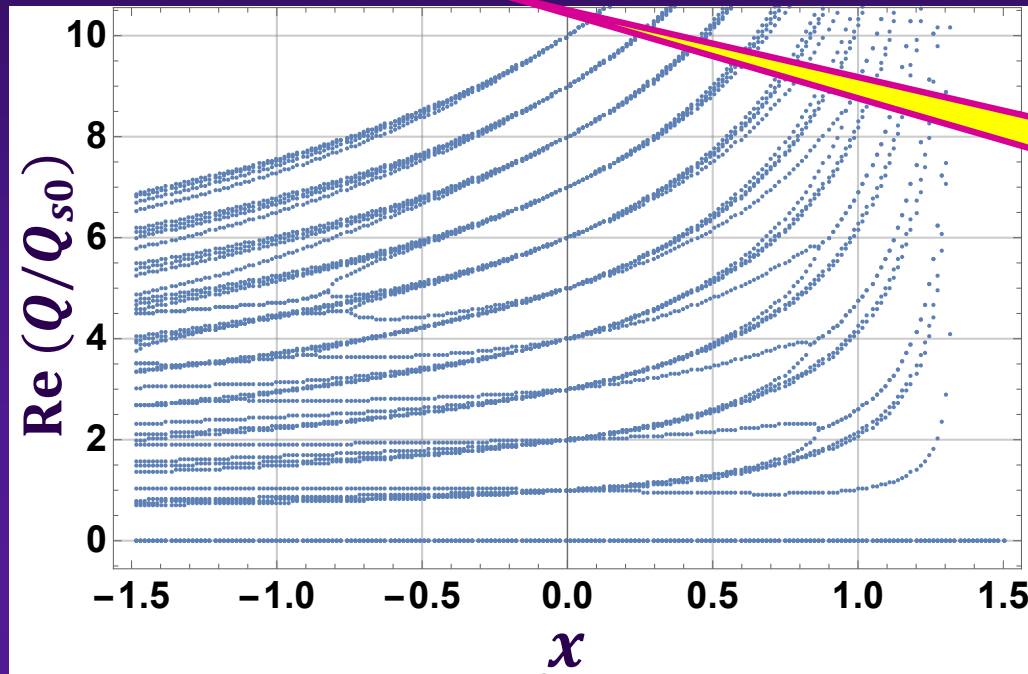


# 1) GALACLIC => For PAD distribution (& computing PWD also for PAD distribution): $f_r \tau_b = 2.7$



$$x_{th} \approx -0.75$$

# 1) GALACLIC => For PAD distribution (BUT computing PWD for PLD distribution ...): $f_r \tau_b = 2.7$



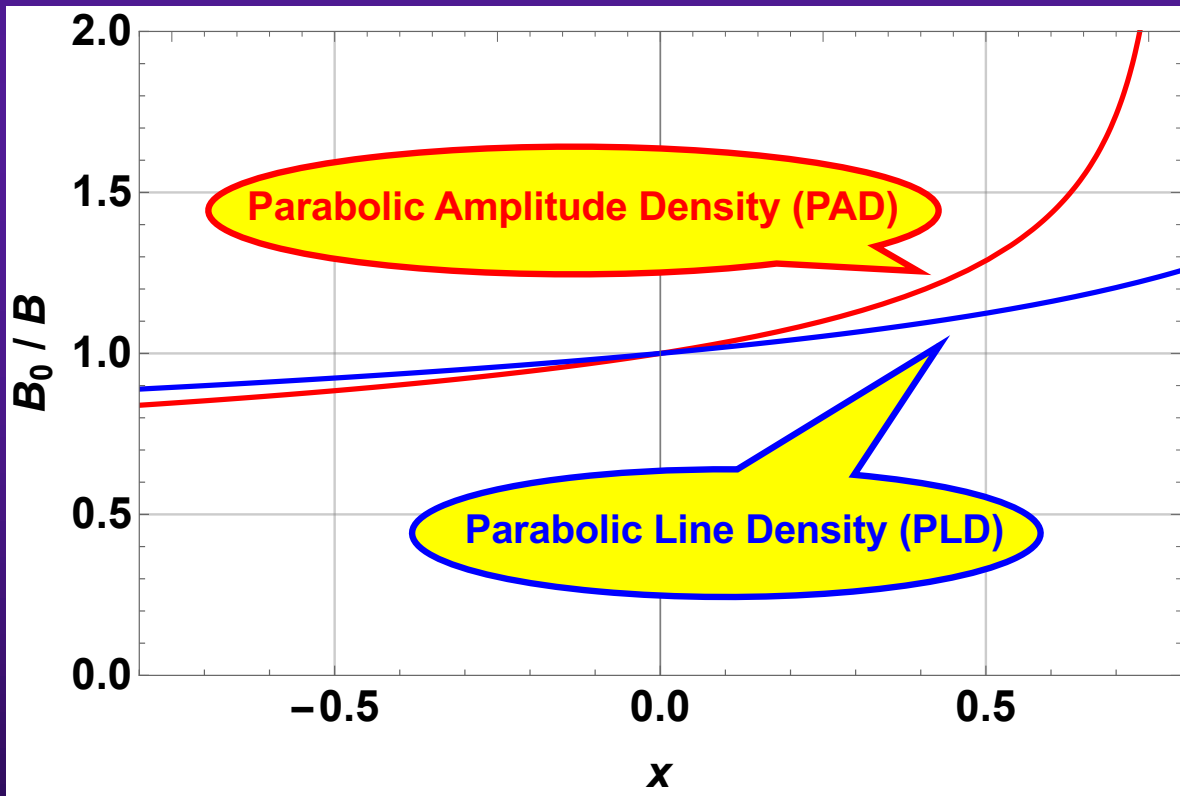
# 1) GALACLIC $\Rightarrow f_r \tau_b = 2.7$

$$N_b^{th} = \frac{|x_{th}| \pi^2}{4} \frac{B_0^3 V_{RF} h}{e f_0 \left| \frac{Z_l}{p} \right|_{p=0}} \frac{B_0}{B}$$

$$\frac{\sim 0.8 \pi^2}{4} \approx 2$$

$$\left( \frac{B_0}{B} \right)_{PAD} = \left( 1 - \frac{4}{\pi} x \right)^{-1/4}$$

$$\left( \frac{B_0}{B} \right)_{PLD} = \left( 1 - \frac{3}{4} x \right)^{-1/4}$$



Above Transition

$$N_b^{th}(-0.75)_{PAD} = 1.15 \times 10^{11} \text{ p/b}$$

$$N_b^{th}(-0.75)_{PLD} = 1.2 \times 10^{11} \text{ p/b}$$

$$N_b^{th}(+0.82)_{PAD} = \infty$$

$$N_b^{th}(+0.82)_{PLD} = 1.9 \times 10^{11} \text{ p/b} \\ \approx 1.6 N_b^{th}(-0.75)_{PLD}$$

Below Transition

## 2) SIMPLE FORMULA

- ◆ Formula based (as in transverse) on the coupling between the 2 modes overlapping the peak of the real part of the impedance and taking into account the PWD for PLD => See <http://cds.cern.ch/record/524139/files/ps-2001-063.pdf>

$$N_b^{th} = \frac{1}{0.4} \frac{B_0^3 V_{RF} h}{e f_0 \left| \frac{Z_l}{p} \right|_{p=0}} \frac{B_0}{B}$$

$$\frac{1}{0.4} \approx 2.5$$

$$\left( \frac{B_0}{B} \right)_{PLD} = \left( 1 \pm \frac{3}{4} \right)^{-1/4}$$

Above Transition

Below Transition

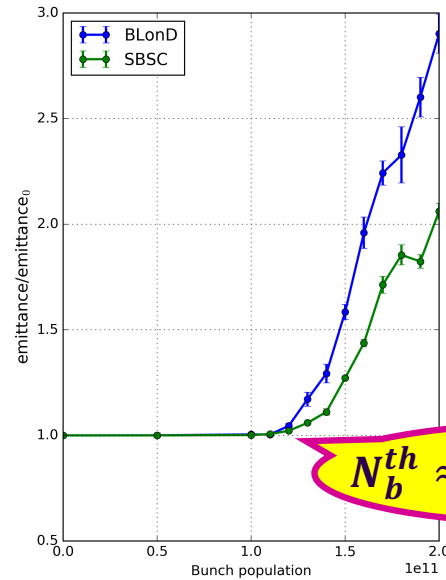
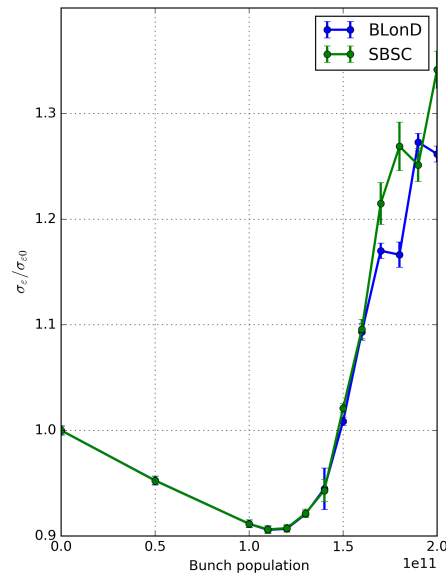
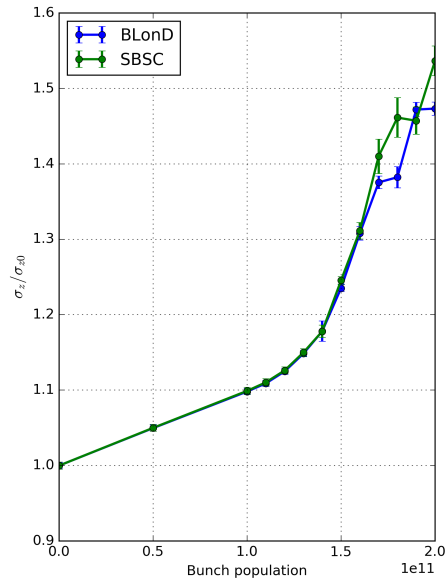
$$N_b^{th,AT} = 1.6 \times 10^{11} \text{ p/b}$$

$$N_b^{th,BT} = 2.6 \times 10^{11} \text{ p/b} \approx 1.6 N_b^{th,AT}$$

=> It is the same as with GALACLIC (PWD with PLD)  
with  $|x_{th}| = 1$  instead of  $\sim 0.8$

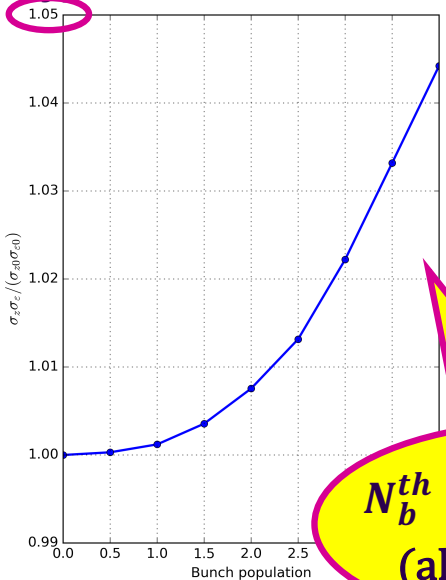
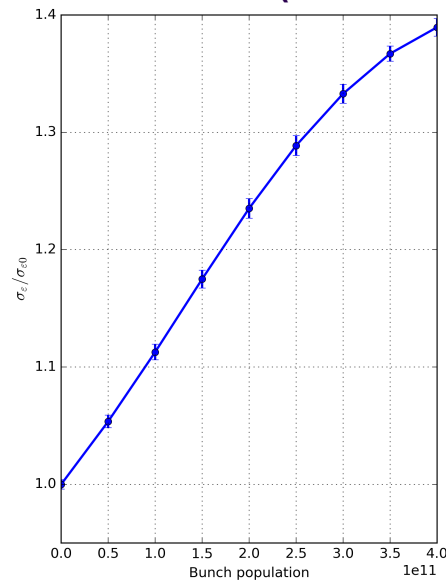
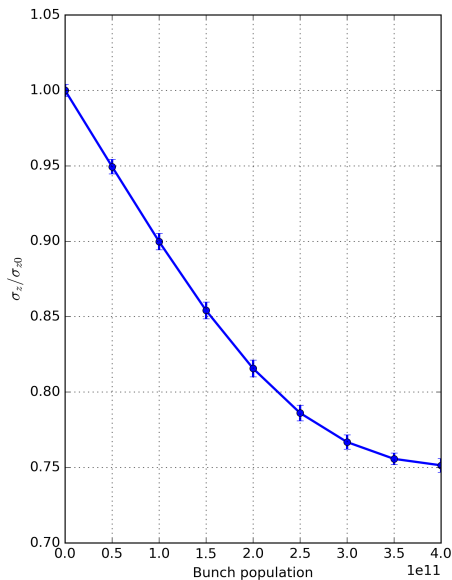
# 3) TRACKING CODES

## Above Transition



$N_b^{th} \approx 1.15 \times 10^{11}$  p/b

## Below Transition (BLonD only)



$N_b^{th} > 4 \times 10^{11}$  p/b?  
(always stable?)



# CONCLUSION (1/2)

## ◆ PWD

Bunch length variation for $10^{11}$ p/b [%]	Above Transition	Below Transition
Tracking codes	+ 10 (BLonD and SBSC)	- 10 (BLonD only)
GALACLIC (PAD)	+ 16	- 19
GALACLIC (PLD)	+ 10	- 11
Simple formula (has same scaling)	+ 10	- 11

- Very good agreement between Tracking codes, GALACLIC and simple formula **with PLD**

# CONCLUSION (2/2)

## ◆ Instability threshold

Bunch intensity threshold [ $10^{11}$ p/b]	Above Transition	Below Transition
Tracking codes	1.15 (BLonD and SBSC)	> 4 (always stable?) (BLonD only)
GALACLIC (PAD+PAD)	1.15	$\infty$
GALACLIC (PAD+PLD)	1.2	1.9 (= $1.2 \times 1.6$ )
Simple formula (has same scaling)	1.6	2.6 (= $1.6 \times 1.6$ )

- Very good agreement between Tracking codes and GALACLIC **above transition** => *Next: check mode-coupling pattern*
- Simple formula reveals same scaling but slightly larger (by ~ 30-40%) numerical factor
- Case below transition needs more analysis, checks, etc.
  - A threshold was observed in the past with HEADTAIL in good agreement with simple formula (see [http://emetral.web.cern.ch/emetral/LMCI\\_ATandBT.pdf](http://emetral.web.cern.ch/emetral/LMCI_ATandBT.pdf))
  - All analyses reveal however larger intensity threshold BT vs. AT