

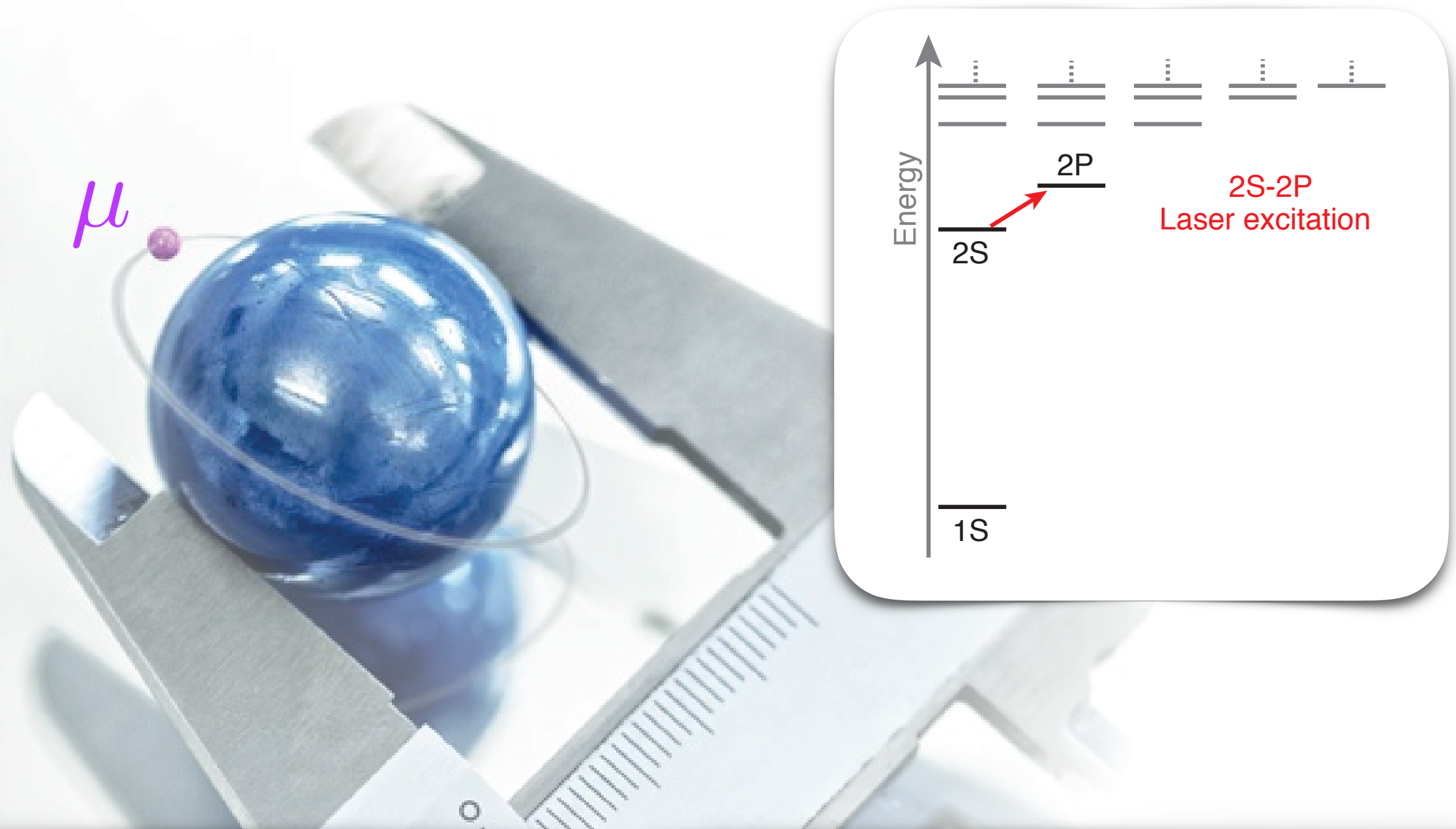
Spectroscopy of muonic atoms



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Laser spectroscopy of light muonic atoms



We measured 10
2S-2P transitions in
 μp , μd , $\mu^3\text{He}^+$, $\mu^4\text{He}^+$

+

Theoretical predictions:
QED + Nuclear structure

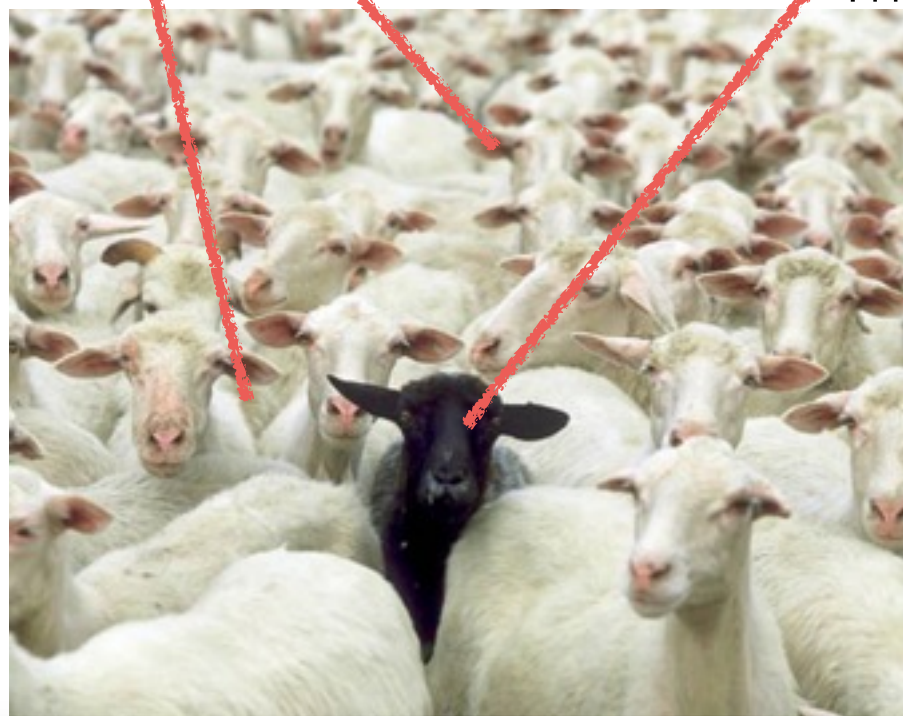


p, d, ^3He , ^4He
charge radii

Extracting the proton radius from μp

Measure 2S-2P splitting (20 ppm)
and compare with theory
→ proton radius

$$\Delta E_{2P-2S}^{\text{th}} = 206.0336(15) - 5.2275(10) r_p^2 + 0.0332(20) \text{ [meV]}$$

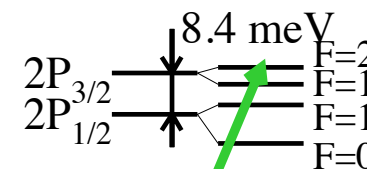


The most interesting

$$\begin{aligned} \Delta E_{\text{size}} &= \frac{2\pi(Z\alpha)}{3} r_p^2 |\Psi_{nl}(0)|^2 \\ &= \frac{2(Z\alpha)^4}{3n^3} m_r^3 r_p^2 \delta_{l0} \end{aligned}$$

$$m_\mu \approx 200 m_e$$

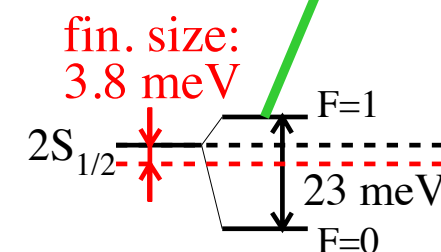
$$r_p^2 = -6 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0}$$



206 meV

50 THz

6 μm



Principle of the μp 2S-2P experiment

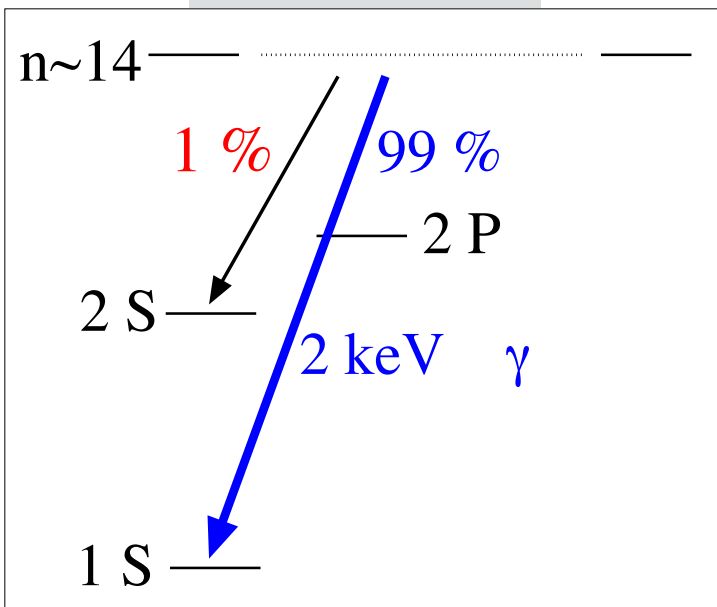
Produce many μ^- at keV energy

Form μp by stopping μ^- in 1 mbar H_2 gas

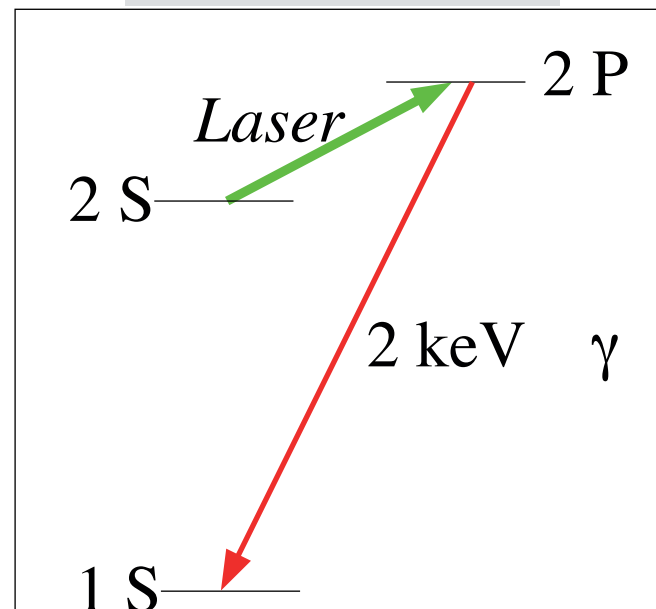
Fire laser to induce the 2S-2P transition

Measure the 2 keV X-rays from 2P-1S decay

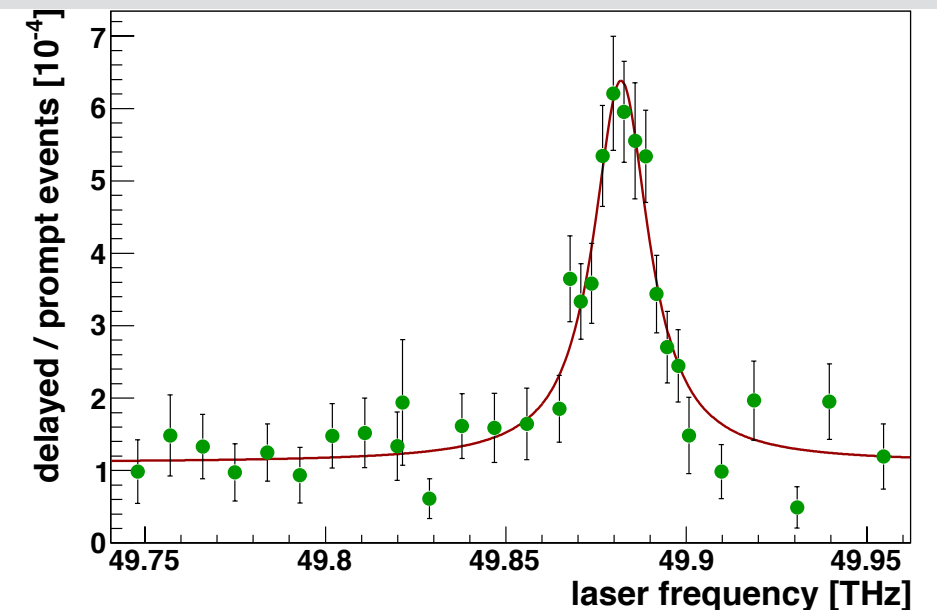
μp formation



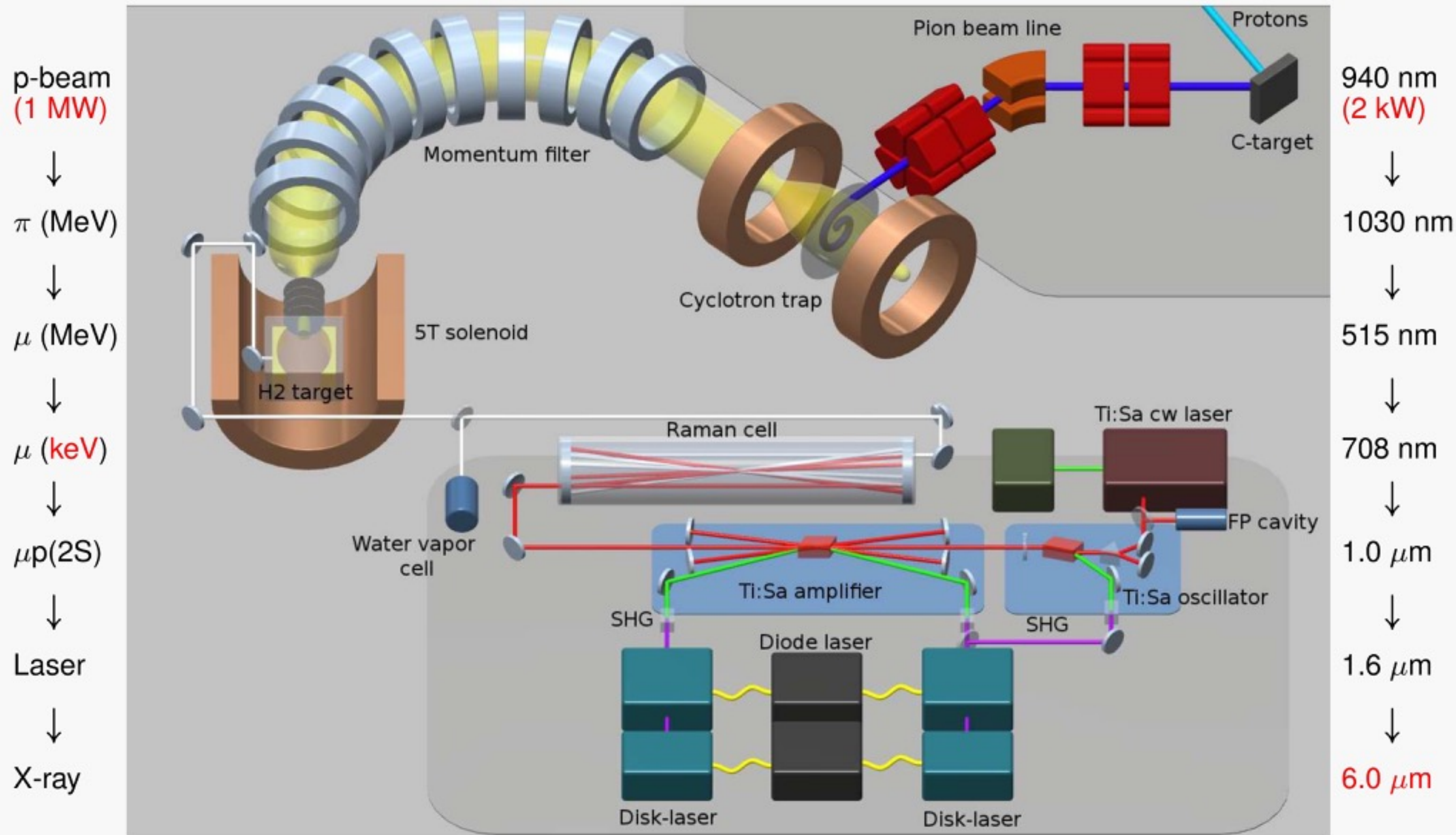
Laser excitation



Plot number of X-rays vs laser frequency

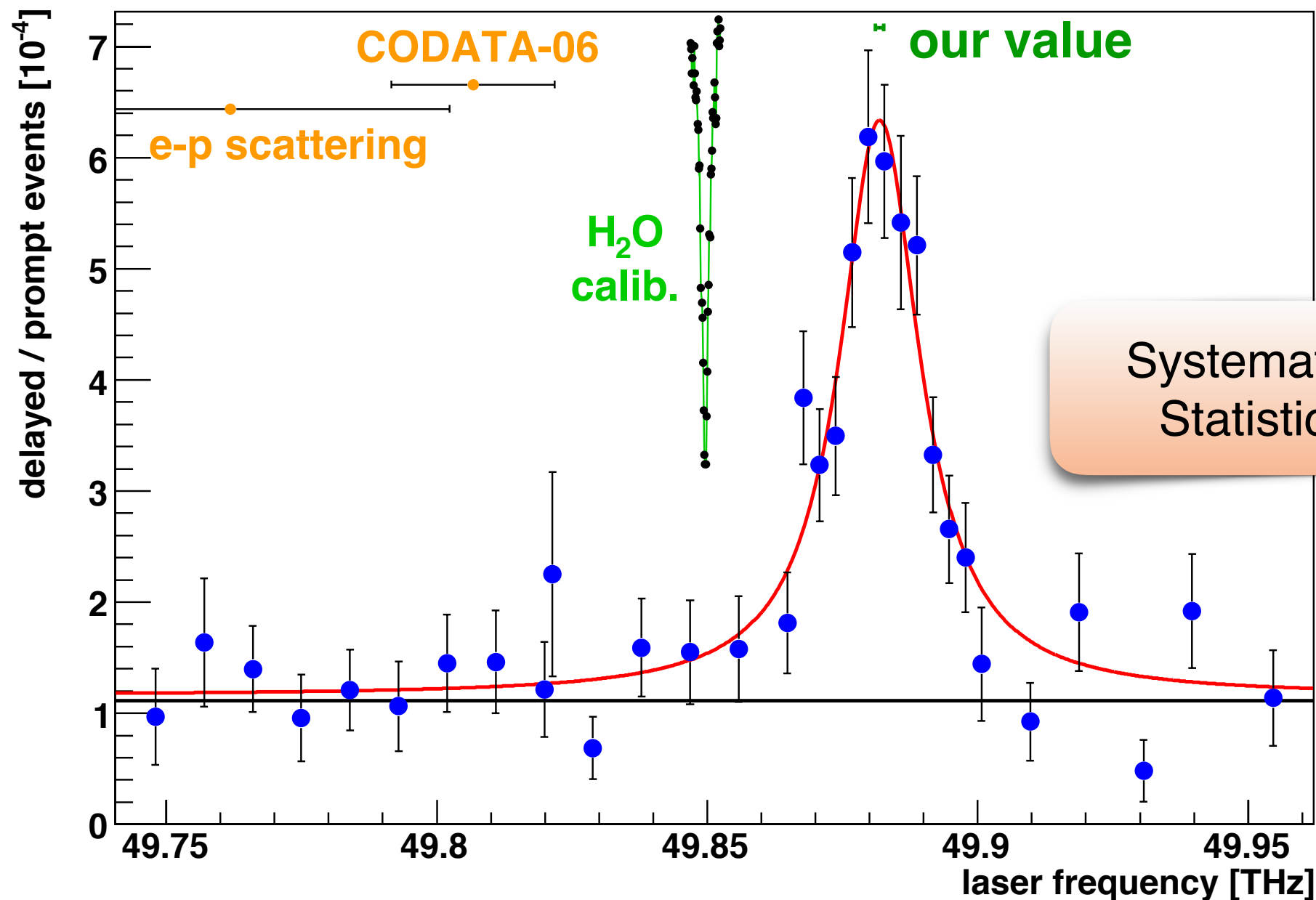


The setup at the Paul Scherrer Institute



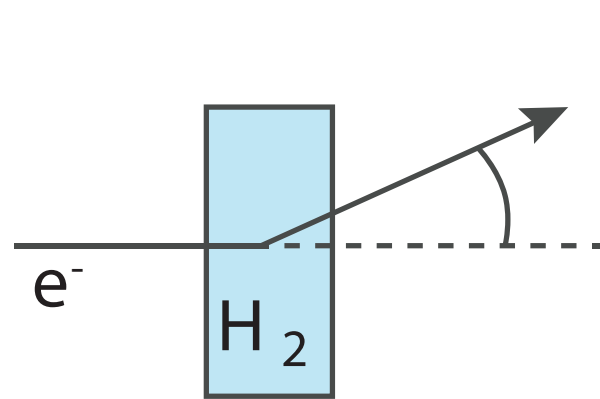
The first μp resonance (2010)

Discrepancy:
 $5.0 \sigma \leftrightarrow 75 \text{ GHz} \leftrightarrow \delta\nu/\nu = 1.5 \times 10^{-3}$

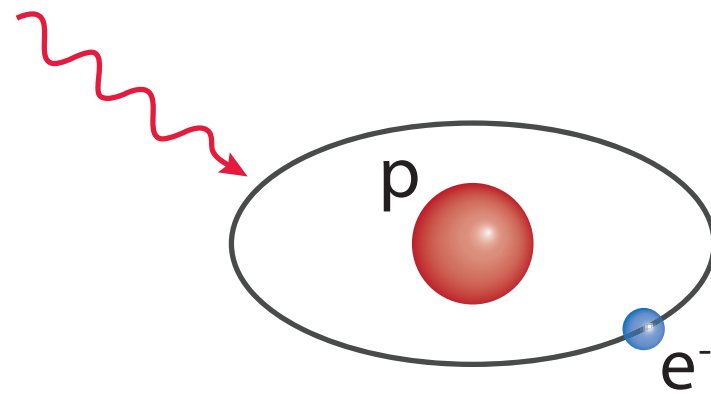


Pohl et al., Nature 466, 213 (2010)

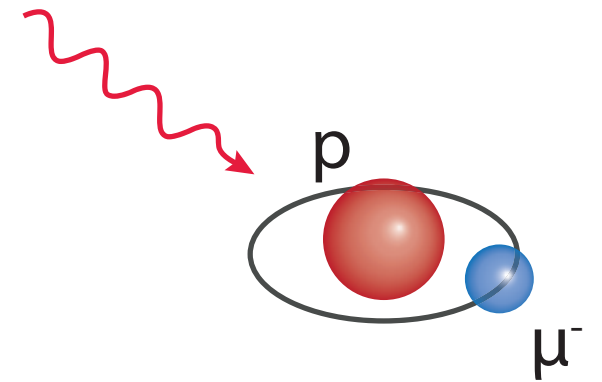
Three ways to the proton radius



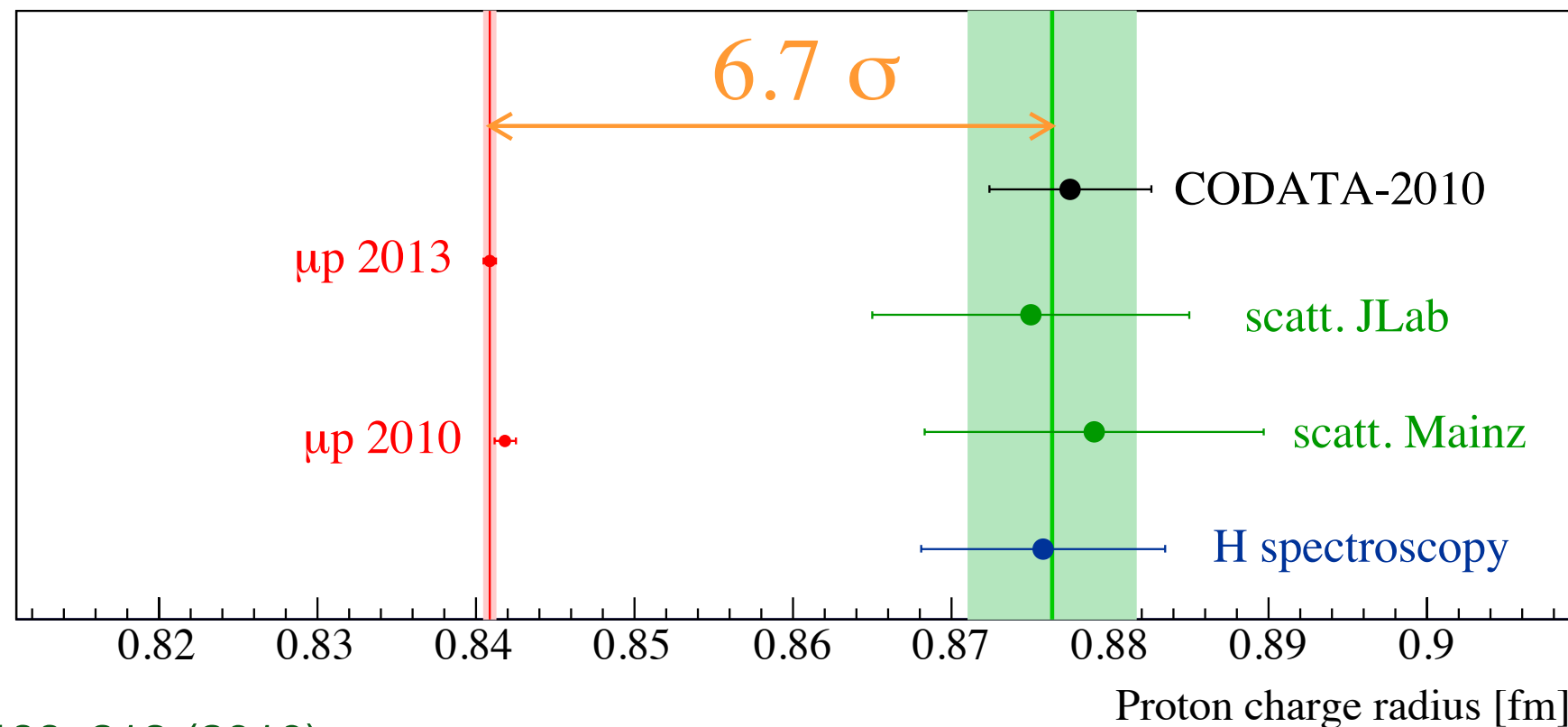
e^- -p scattering



H spectroscopy



μ p spectroscopy



Pohl et al., Nature 466, 213 (2010)

Antognini et al., Science 339, 417 (2013)

Pohl et al., Science 353, 669 (2016)

The r_p puzzle has triggered many activities



Bound-state QED

New experiments
-scattering
-spectroscopy

Effective field th.

Proton structure

New physics?

Few-nucleon

The proton radius puzzle

- μp experiment

- μp theory

- H experiments

- BSM physics

- e-p scattering

Rarely criticised since:

$$m_\mu \approx 200m_e$$

- **sensitive** to the radius

$$\sim m^3 R_p^2 \quad \checkmark$$

- **insensitive** to systematical effects

$$\sim 1/m \quad \checkmark$$

The proton radius puzzle

- μp experiment

- μp theory

- H experiments

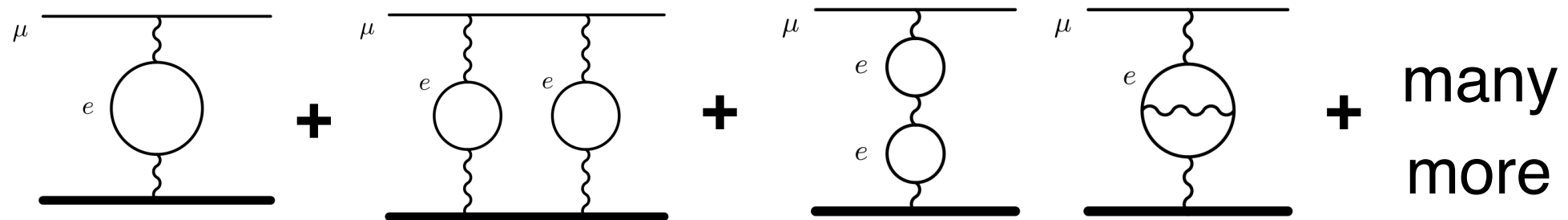
- BSM physics

- e-p scattering

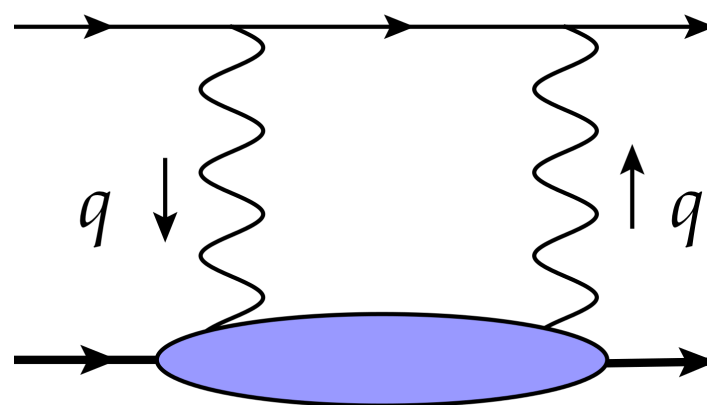
QED



Pachucki, Borie, Eides, Karschenboim,
Jentschura, Martynenko, Indelicato
Pineda, Peset, Faustov...



Two-photon exchange



Can be computed with
dispersion th. + data

But subtraction term is needed
 \Rightarrow modelling of proton

Pachucki, Carlson, Birse, McGovern, Pineda, Gorchtein, Pascalutsa,
Vanderhaeghen, Alarcon, Miller, Paz, Hill...

The proton radius puzzle

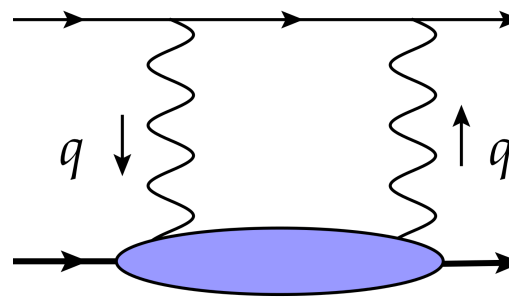
- μp experiment

- μp theory

- H experiments

- BSM physics

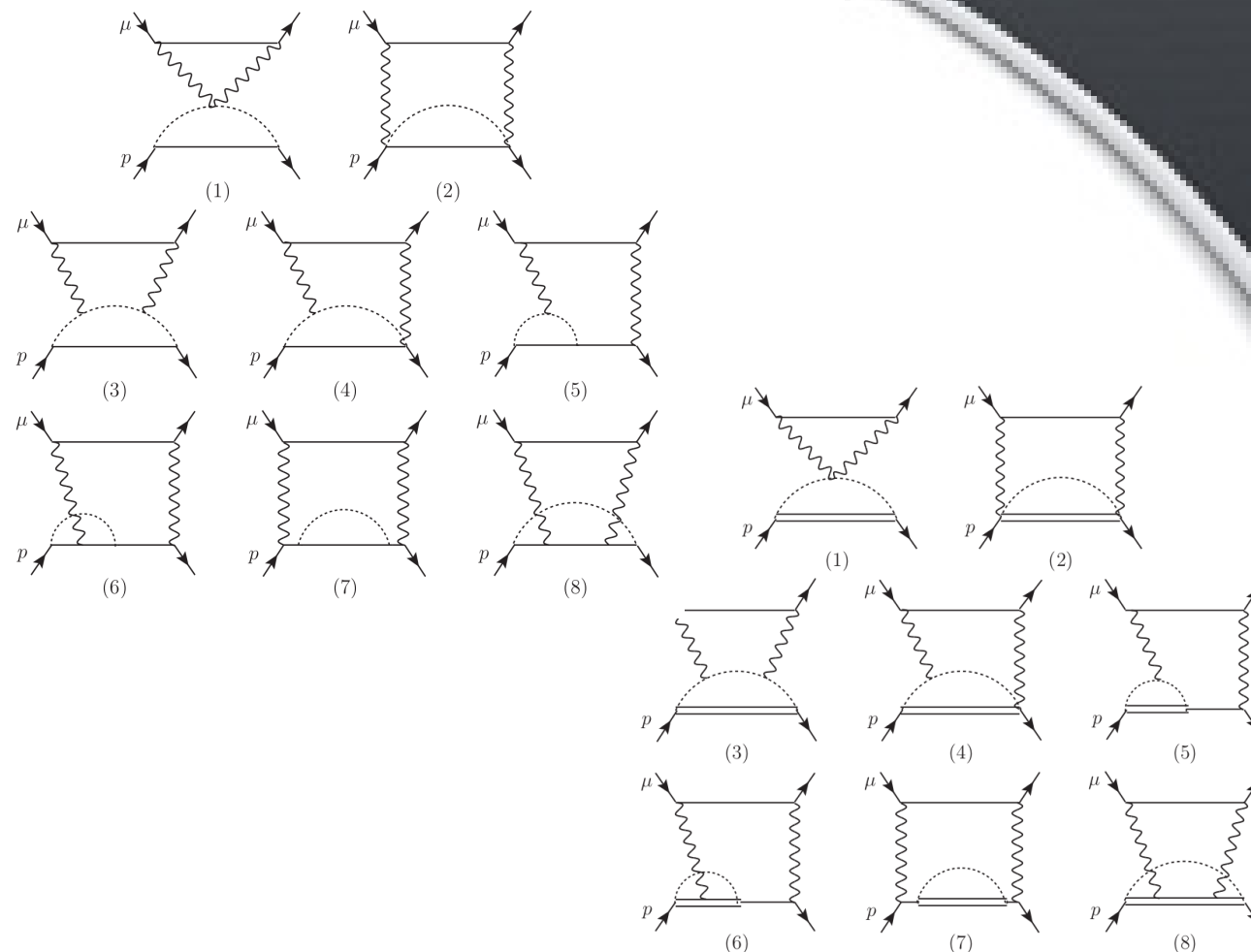
- e-p scattering



Chiral EFT

Phenomenological

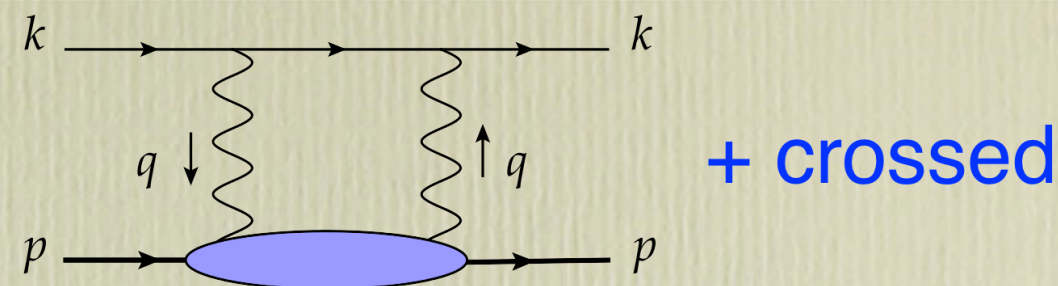
- dispersion relations
- data
- subtraction term



AGREEMENT

Technicalities on **TPE** in μp

Kinematics: 2 loop variables
 q^2 and $\nu=(pq)/M$



$$\mathcal{M} = e^4 \int \frac{d^4 q}{(2\pi)^4} \frac{1}{q^4} \bar{u}(k) \left[\gamma^\nu \frac{1}{\not{k} - \not{q} - m_l + i\epsilon} \gamma^\mu + \gamma^\mu \frac{1}{\not{k} + \not{q} - m_l + i\epsilon} \gamma^\nu \right] u(k) T_{\mu\nu}$$

Forward virtual Compton amplitude

$$\begin{aligned} T^{\mu\nu} &= \frac{i}{8\pi M} \int d^4 x e^{iqx} \langle p | T j^\mu(x) j^\nu(0) | p \rangle \\ &= \left(-g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) T_1(\nu, Q^2) + \frac{1}{M^2} \left(p - \frac{pq}{q^2} q \right)^\mu \left(p - \frac{pq}{q^2} q \right)^\nu T_2(\nu, Q^2) \end{aligned}$$

Lamb shift (nS-nP)

$$\Delta E = -\frac{\alpha^2}{2\pi m_l M_d} \phi_n^2(0) \int d^4 q \frac{(q^2 + 2\nu^2) T_1(\nu, q^2) - (q^2 - \nu^2) T_2(\nu, q^2)}{q^4 [(q^2/2m_l)^2 - \nu^2]}$$

Slide stolen from Gorchtein

Technicalities on **TPE** in μp

T_1, T_2 - the imaginary parts known (Optical theorem)

$$\begin{aligned}\text{Im}T_1(\nu, Q^2) &= \frac{1}{4M} F_1(\nu, Q^2) \\ \text{Im}T_2(\nu, Q^2) &= \frac{1}{4\nu} F_2(\nu, Q^2)\end{aligned}$$

Inelastic structure functions = data
(real and virtual photoabsorption, FF)

Real parts - from forward dispersion relation

$$F_1(\nu \rightarrow \infty, q^2) \sim \nu^{1+\epsilon} \quad \text{- subtraction needed}$$

$$F_2(\nu \rightarrow \infty, q^2) \sim \nu^\epsilon \quad \text{- no subtraction}$$

$$\text{Re}T_1(\nu, Q^2) = \bar{T}_1(0, Q^2) + T_1^{pole}(\nu, Q^2) + \frac{\nu^2}{2\pi M} \int_{\nu_0}^{\infty} \frac{d\nu'}{\nu(\nu'^2 - \nu^2)} F_1(\nu', Q^2)$$

$$\text{Re}T_2(\nu, Q^2) = T_2^{pole}(\nu, Q^2) + \frac{1}{2\pi} \int_{\nu_0}^{\infty} \frac{d\nu'}{\nu'^2 - \nu^2} F_2(\nu', Q^2)$$

Slide stolen from Gorchtein

The proton radius puzzle

- μp experiment

- μp theory

- H experiments

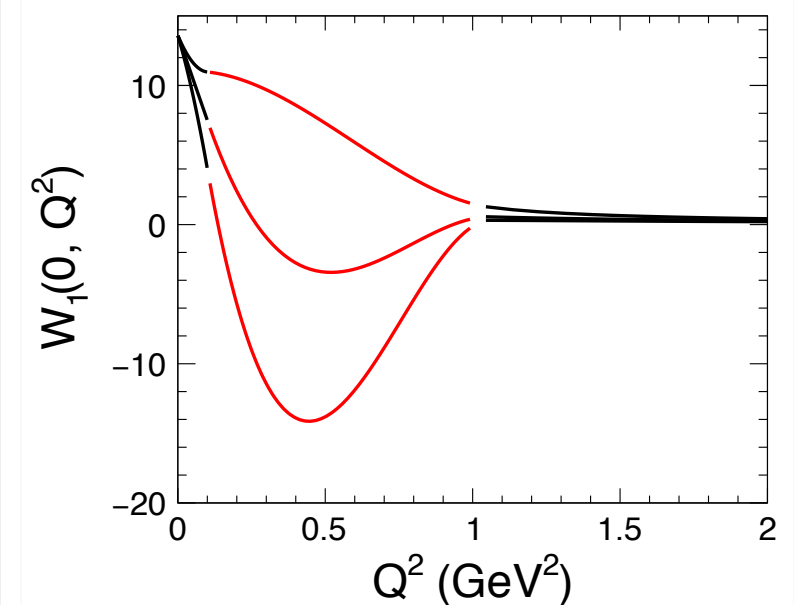
- BSM physics

- e-p scattering

Uncertainties and discrepancy

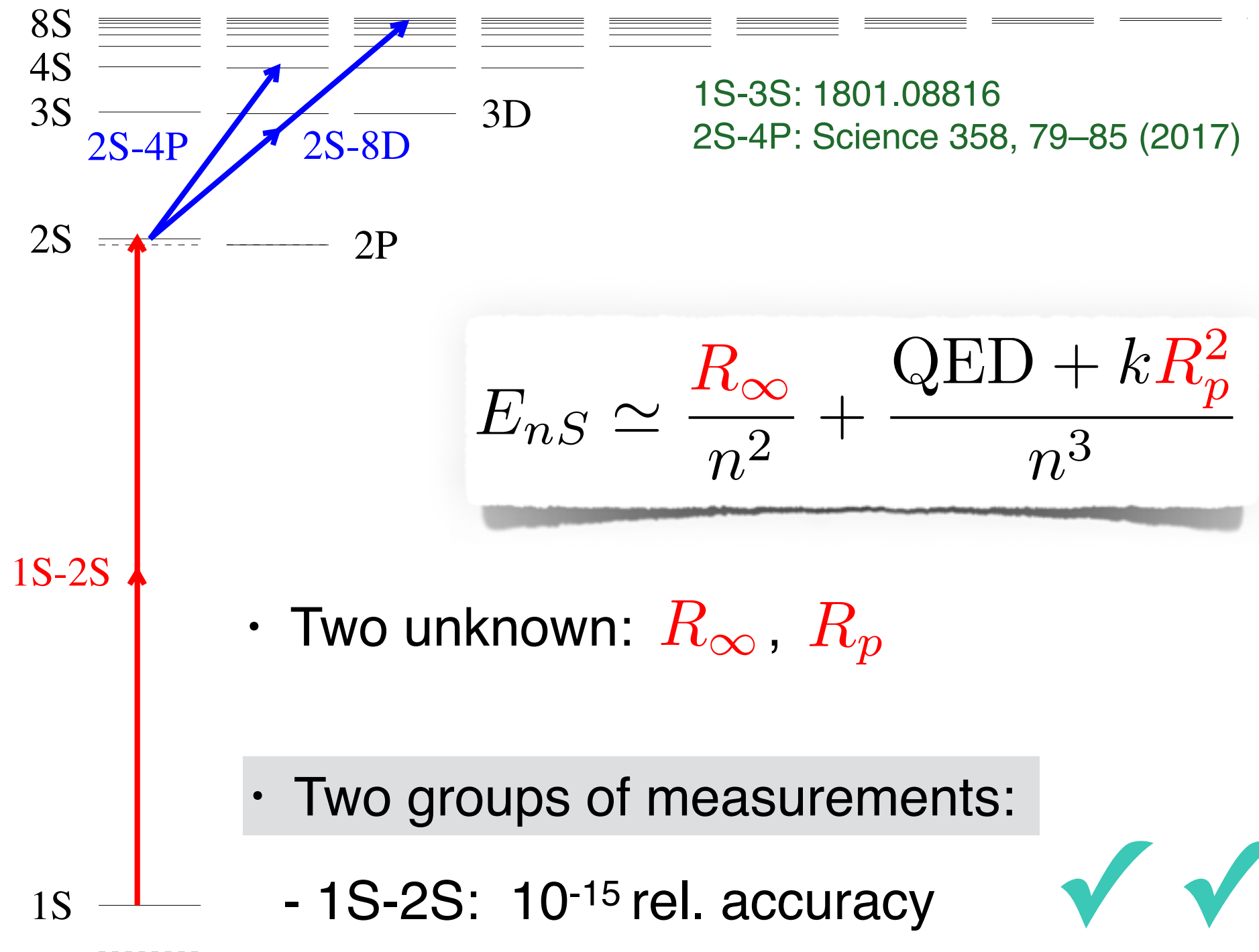
0.3	meV	Discrepancy
0.01	meV:	TPE uncertainty (conservatively, Hill and Paz)
0.0025	meV:	Polarisability-contr. uncertainty (Pascalusa)
0.0020	meV:	TPE uncertainty (McGovern, our choice)
0.0015	meV:	QED uncertainties
0.0023	meV:	Measurement uncertainty

Pachucki, Carlson, Birse,
McGovern, Pineda, Peset,
Gorchtein, Pascalutsa,
Vanderhaeghen, Tomalak,
Martynenko, Alarcon, Miller,
Paz, Hill...



The proton radius puzzle

- μp experiment
- μp theory
- H experiments
- BSM physics
- e-p scattering



- Two unknown: R_∞ , R_p

- Two groups of measurements:

- 1S-2S: 10^{-15} rel. accuracy



- others: $<10^{-13}$ rel. accuracy
and more prone to systematics



The proton radius puzzle

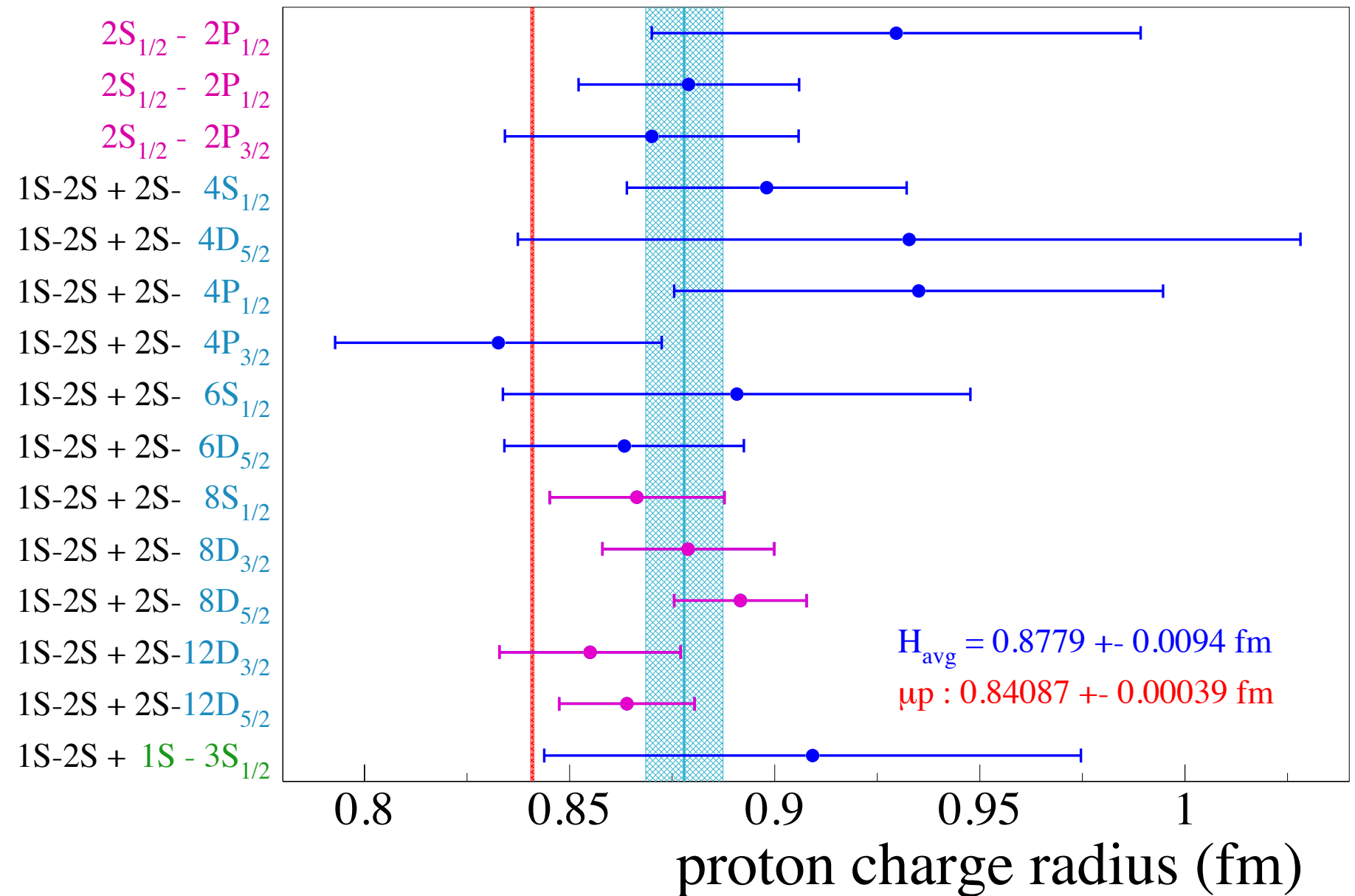
- μp experiment

- μp theory

- H experiments

- BSM physics

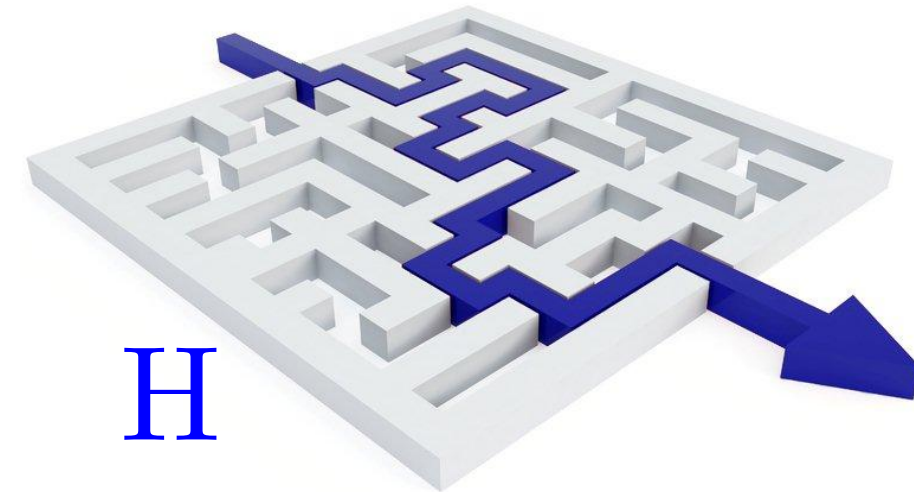
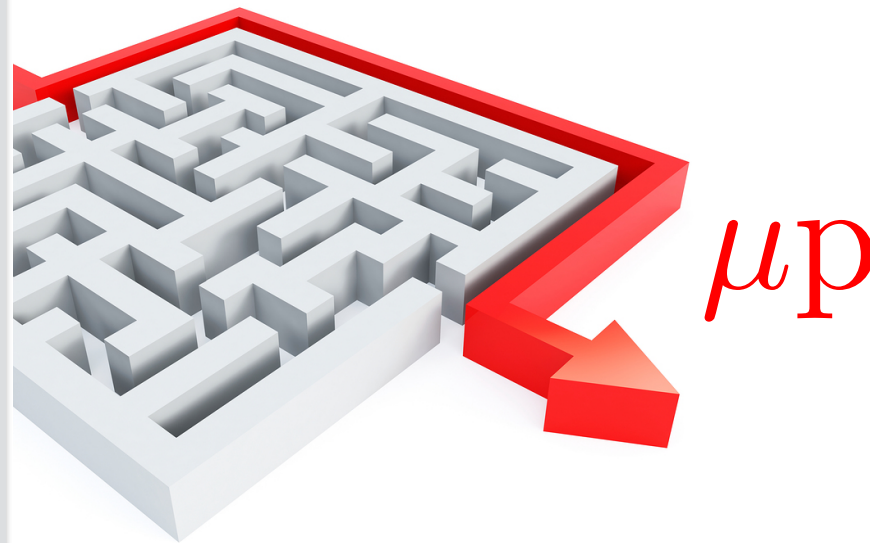
- e-p scattering



4 σ only when averaging

The proton radius puzzle

- μp experiment
- μp theory



- H experiments

Large sensitivity to r_p
 \Rightarrow requires low-precision meas.
 Large **ins**ensitivity to systematics
 But difficult to see the signal

Low sensitivity to r_p
 \Rightarrow requires high-precision
 \Rightarrow fight with systematics
 But “easy” to see the signal

- BSM physics

- e-p scattering

Explain the discrepancy by shifting the

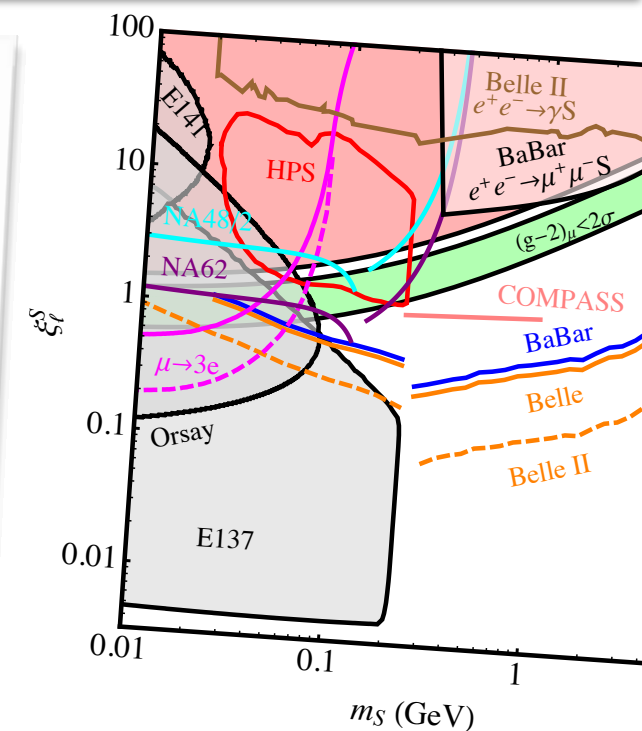
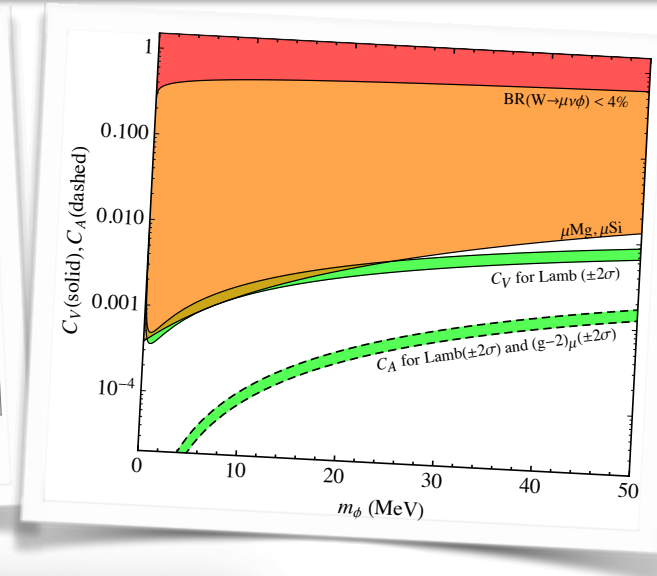
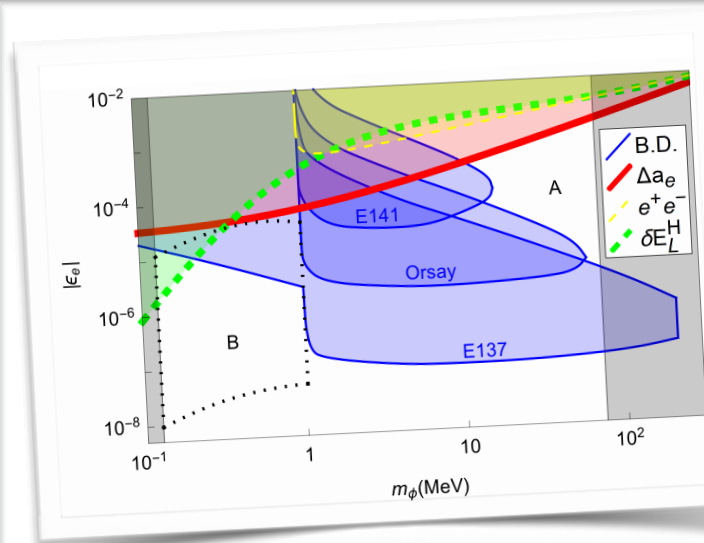
μp (2S-2P)	100 σ	75 GHz	4 Γ
H (1S-2S)	4'000 σ	40 kHz	40 Γ
H (2S-4P)	< 1.5 σ	9 kHz	$7 \cdot 10^{-4} \Gamma$
H (2S-2P)	< 1.5 σ	5 kHz	$7 \cdot 10^{-4} \Gamma$

σ : exp accuracy

Γ : line width

The proton radius puzzle

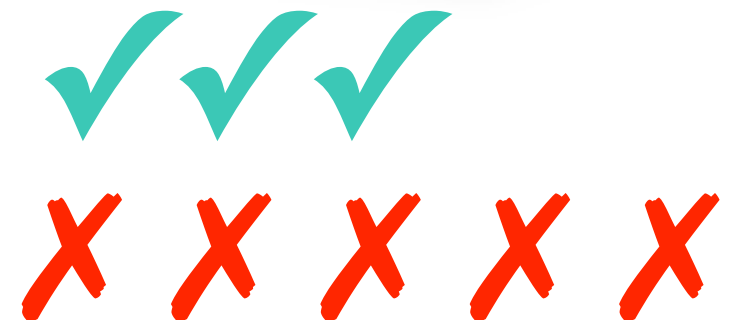
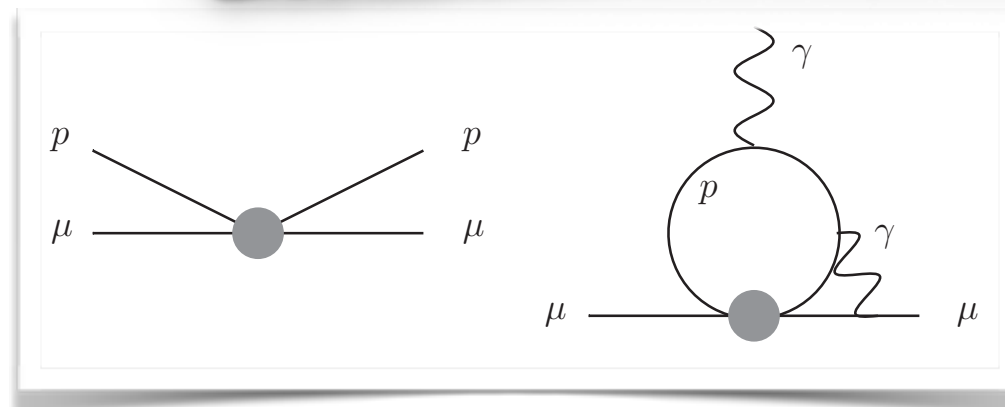
- μp experiment
- μp theory
- H experiments
- BSM physics
- e-p scattering



Some open regions for MeV force carrier still resist

Martens & Ralston (2016),
Liu, McKen & Miller (2016),
Batell et. al (2016)

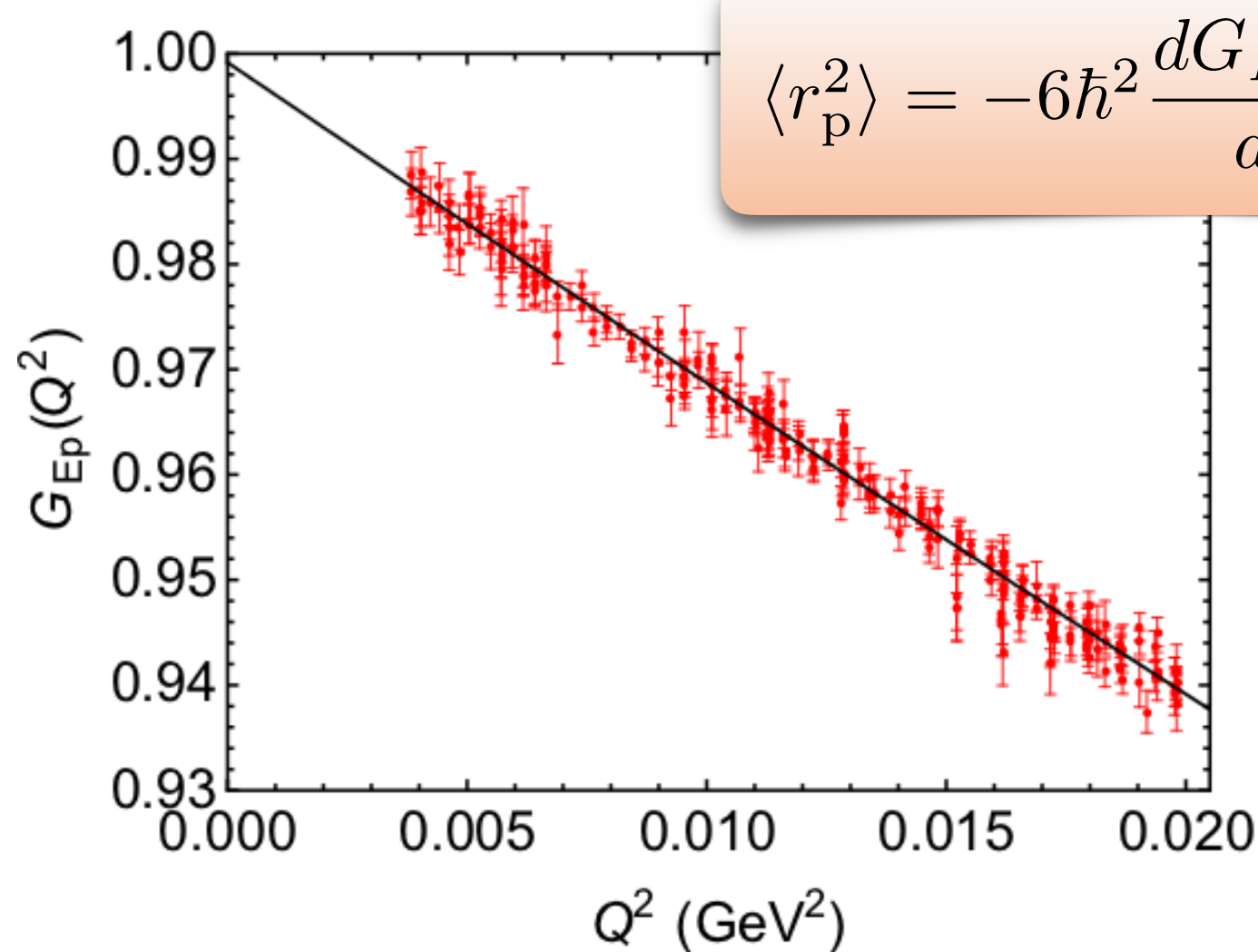
- Tuning (e.g. vector vs axial-vector)
- Preferential coupling to μ and p
- No UV completion and no full SM gauge inv.



The proton radius puzzle

- μp experiment
- μp theory
- H experiments
- BSM physics
- e-p scattering

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Ros.}} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \frac{1}{(1 + \tau)} \left(\varepsilon G_E^2(Q^2) + \tau G_M^2(Q^2) \right)$$



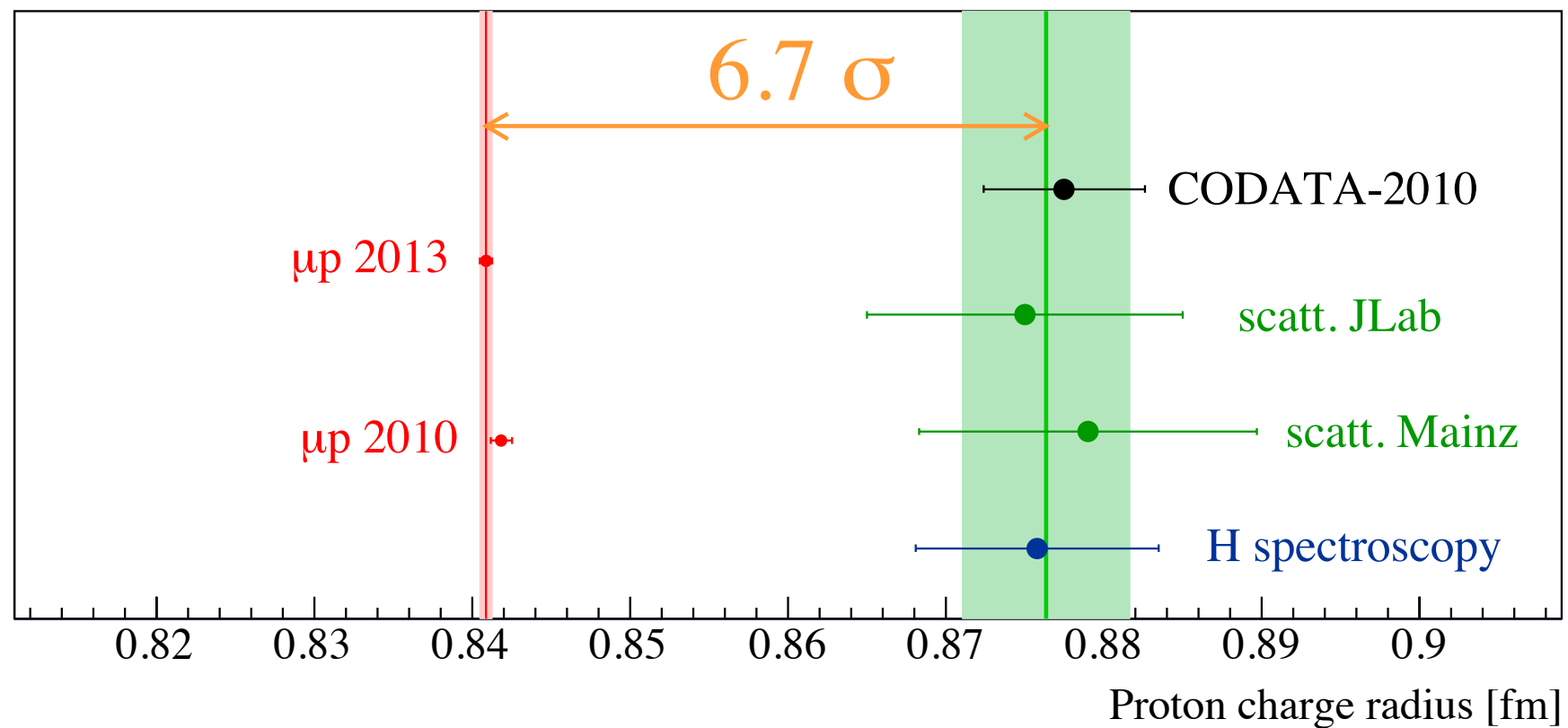
The proton radius puzzle

- μp experiment
- μp theory
- H experiments
- BSM physics
- e-p scattering

Extrapolation:

- which functionality
- analyticity
- z-expansion vs Q^2 -expansion
- coefficients with perturbative scaling
- how many degrees of freedom (under-fitting, over-fitting)
- which Q^2 range
- normalisations
- physics-motivated model (VMD, chPT, dispersion, large tails, higher-moments)
- statistical tests, χ^2 , regressions, bias
- TPE corrections

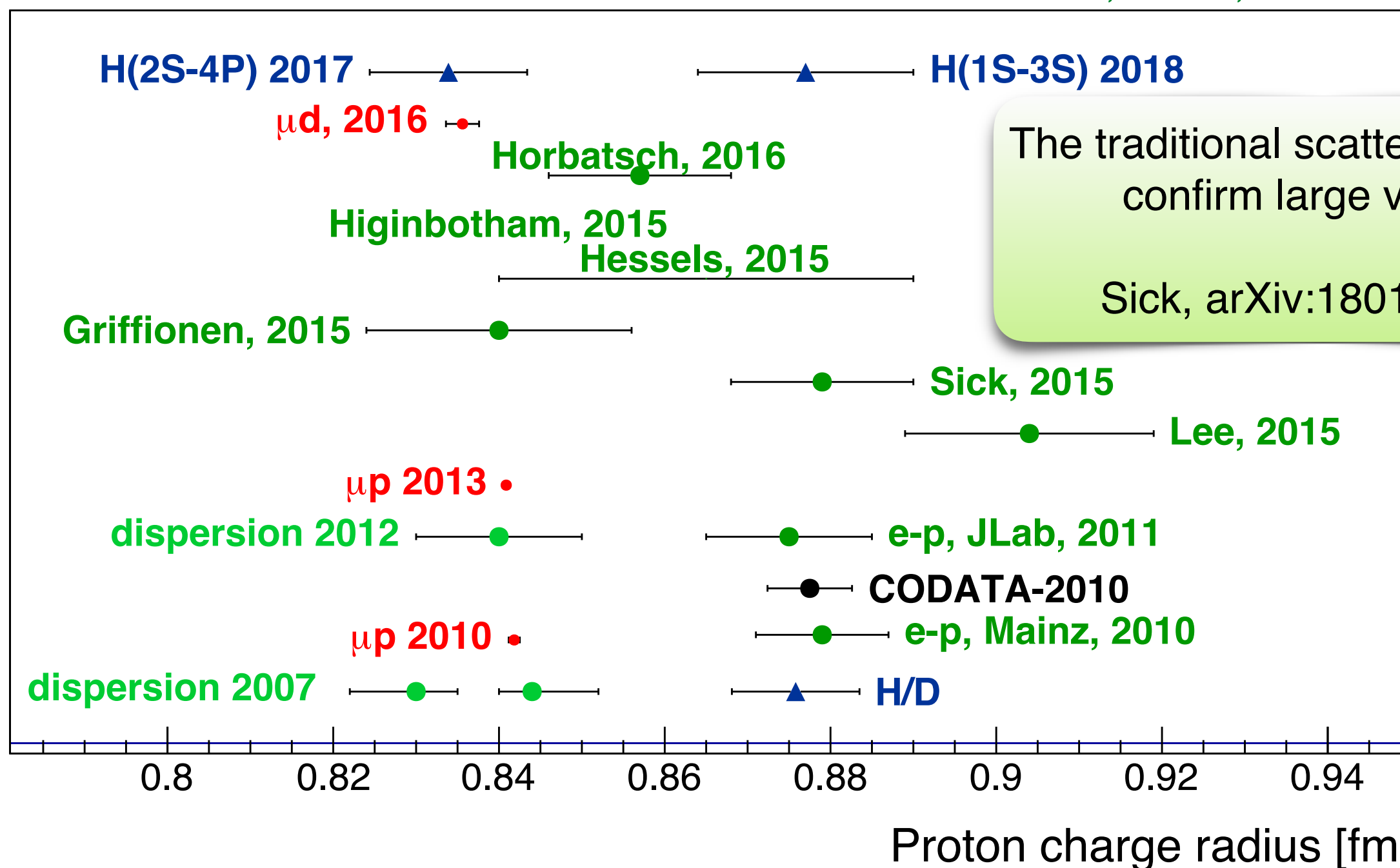
The proton charge radii



The proton charge radii

Higinbotham et al., arXiv: 1510.01293
Griffioen et al., arXiv:1509.06676
Lorenz et al., PRD 91, 014023 (2015)
Horbatsch, Hessels, Pineda, arXiv:1610.09760

Bernauer, Distler, arXiv:1606.02159
Sick, Trautmann, arXiv:1701.01809
Lee, Arrington, Hill, arXiv:1505.01489
Hoferichter et al., EPJA 52, 331 (2016)
Alarcon, Weiss, arXiv:1710.06430



The race to the proton radius solution



The race to the proton radius solution

Atomic spectroscopy

- **H(2S-2P) (Toronto)**
- **H(1S-3S) (LKB, MPQ)**
- **H(2S-4P) (MPQ)**
- H₂, H₂⁺, HD, HD⁺, HT (LKB, LaserLaB, ETH)
- He⁺ (LaserLaB, MPQ)
- He (LaserLab, MPQ)
- Li⁺ (Mainz)
- Muonium (ETH, PSI)
- Positronium (ETH, UC London)
- Rydberg states in H-like ions (NIST)
- Rydberg states in optical lattice (Ann Arbor)

New physics searches

$$K^+ \rightarrow \mu^+ \nu e^+ e^-$$

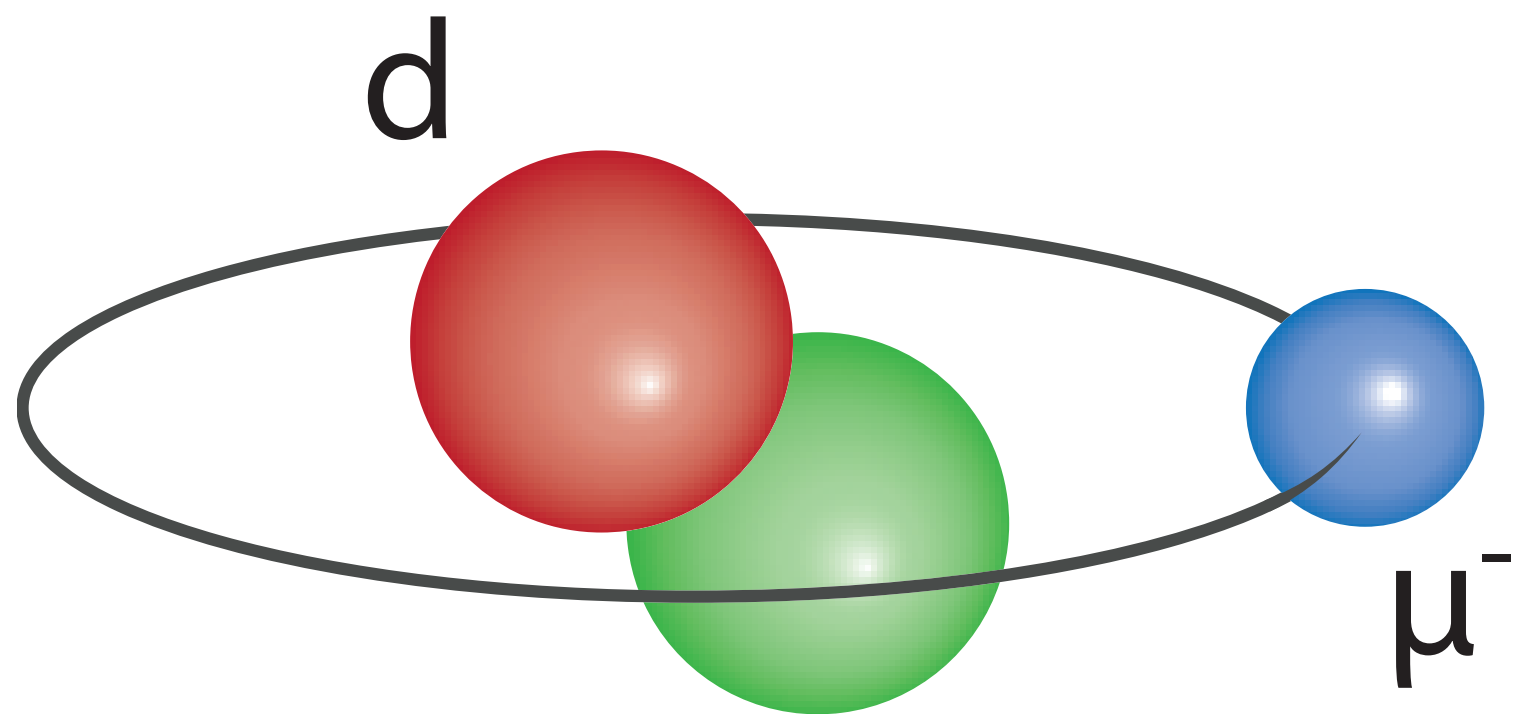
Muonic spectroscopy

- **μd**
- **$\mu^3\text{He}$, $\mu^4\text{He}$**
- μp HFS
- μLi ?

Scattering

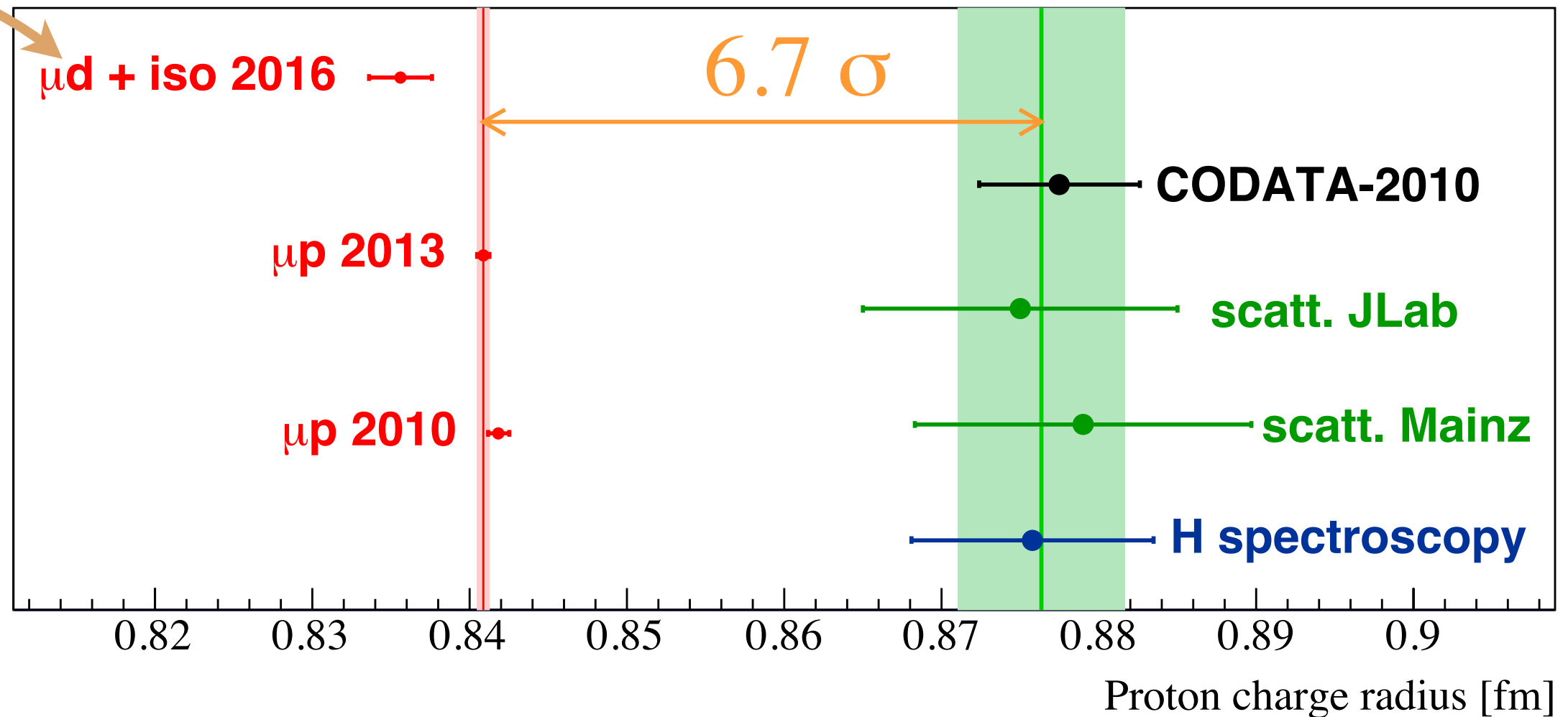
- **e-p, PRad (JLAB)**
- e-p, ISR & MAGIX (Mainz)
- μ -p, e-p, MUSE (PSI, UniBasel)
- μ -p, COMPASS (CERN)
- e-p, ProRad (Orsay)
- Tohoku, (Sendai)





The proton charge radius from **muonic deuterium**

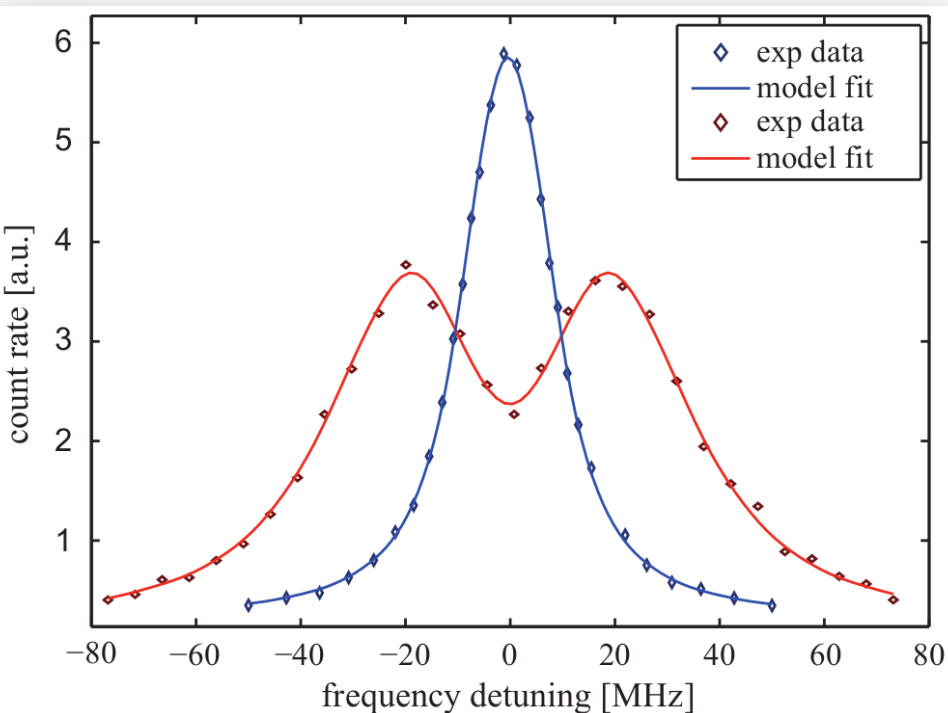
$$\left. \begin{array}{l} \text{H/D shift: } r_d^2 - r_p^2 = 3.820\,07(65) \text{ fm}^2 \\ \mu d: \quad r_d = 2.1256(8) \text{ fm} \end{array} \right\} \Rightarrow r_p = 0.8356(20) \text{ fm}$$



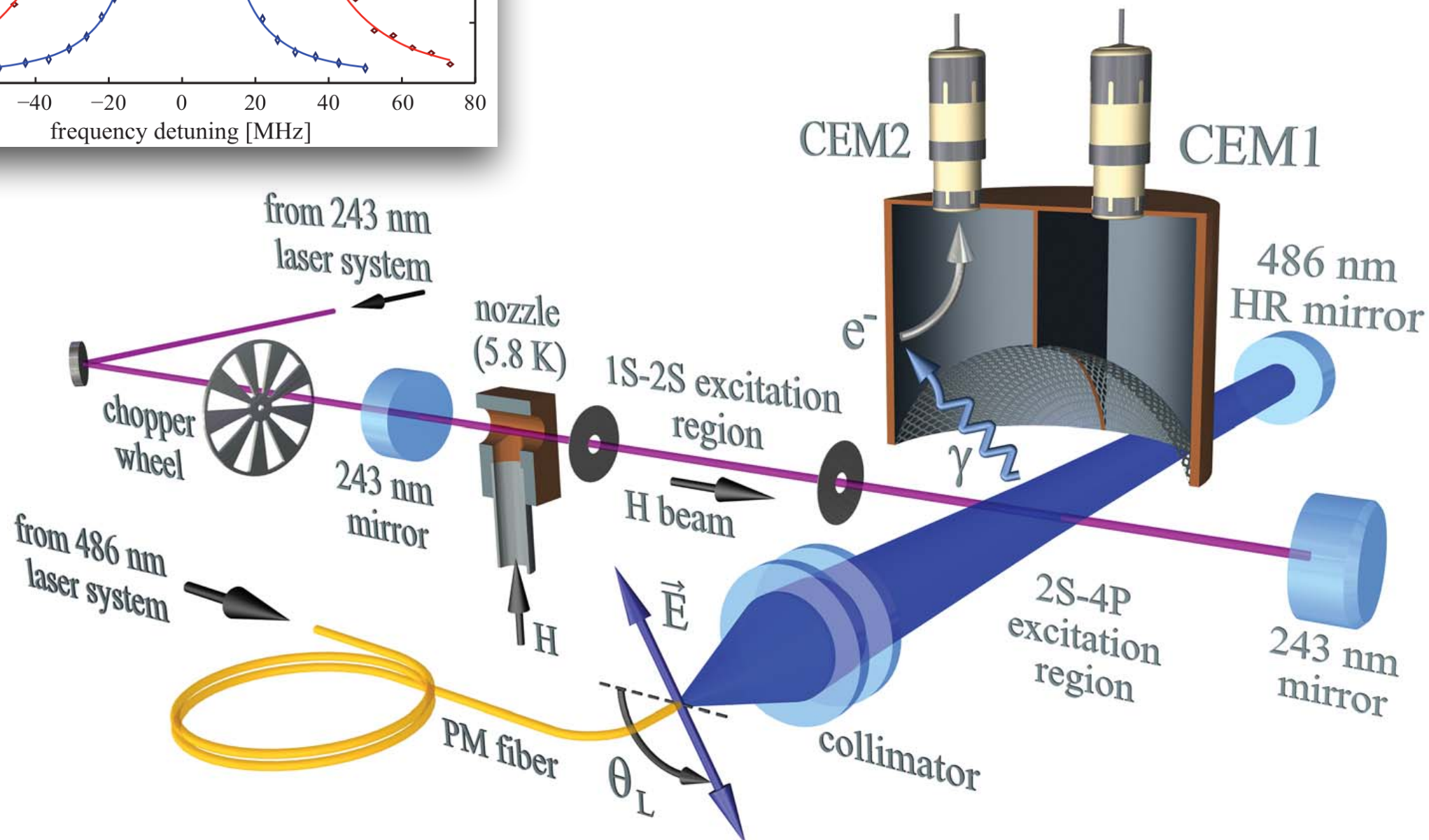
Pohl et al., Nature 466, 213 (2010)
Antognini et al., Science 339, 417 (2013)
Pohl et al., Science 353, 669 (2016)

Small value of the proton
radius is confirmed from μd

New 2S-4P measurement in H (MPQ, 2017)



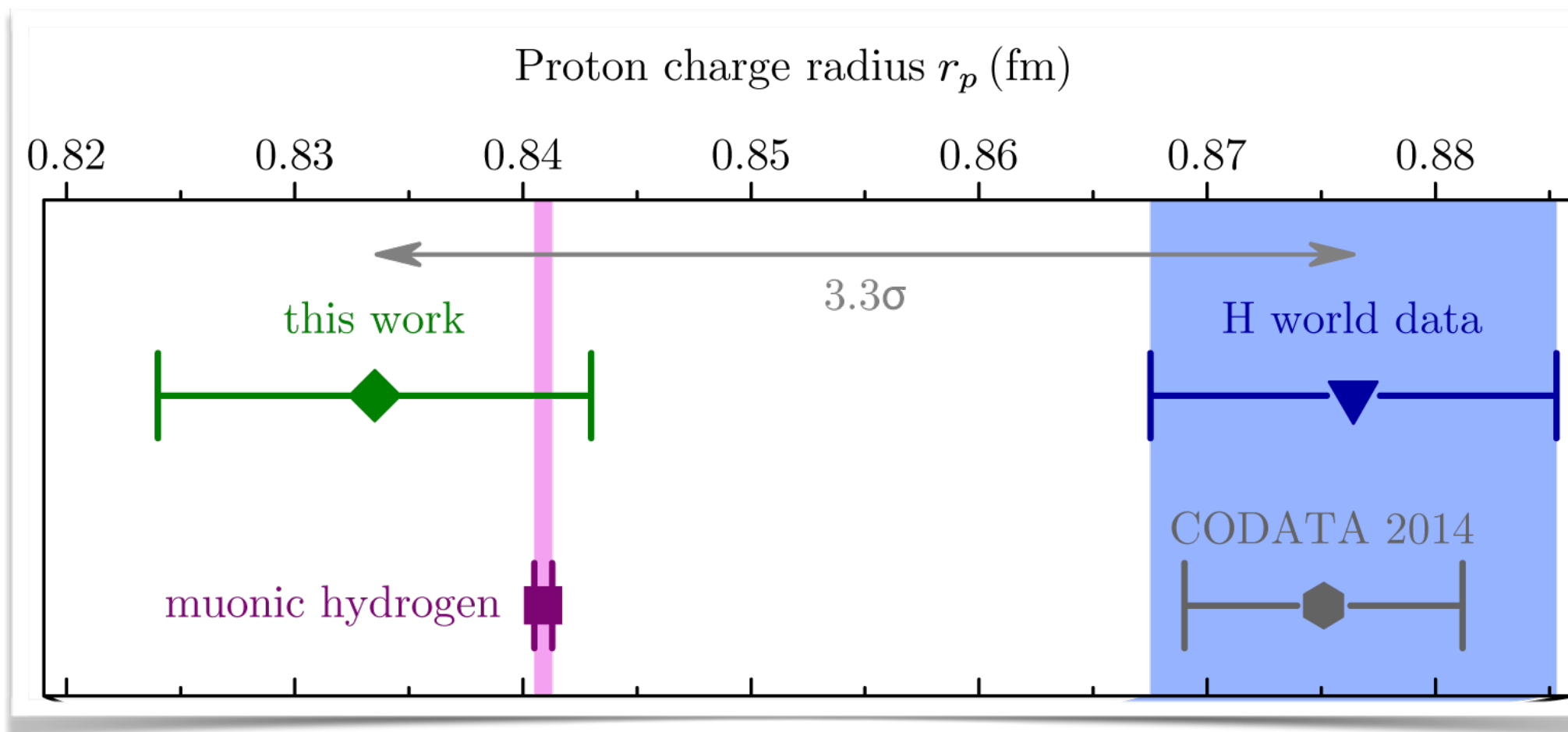
- Produce atomic H beam at cryogenic temperature
- Populate the 2S state using two-photon excitation
- Excite the 2S-4P transition
- Detect the 4P-1S decay (velocity resolved)
- Plot number of 4P-1S decays vs. laser frequency



New 2S-4P measurement in H (MPQ, Munich, 2017)

- r_p discrepancy: 9 kHz
- Line width: 20'000 kHz
- Measurement uncertainty: 3.0 kHz

⇒ split an asymmetric line to 10^{-4}



Beyer et al.,
Science 358, 79 (2017)

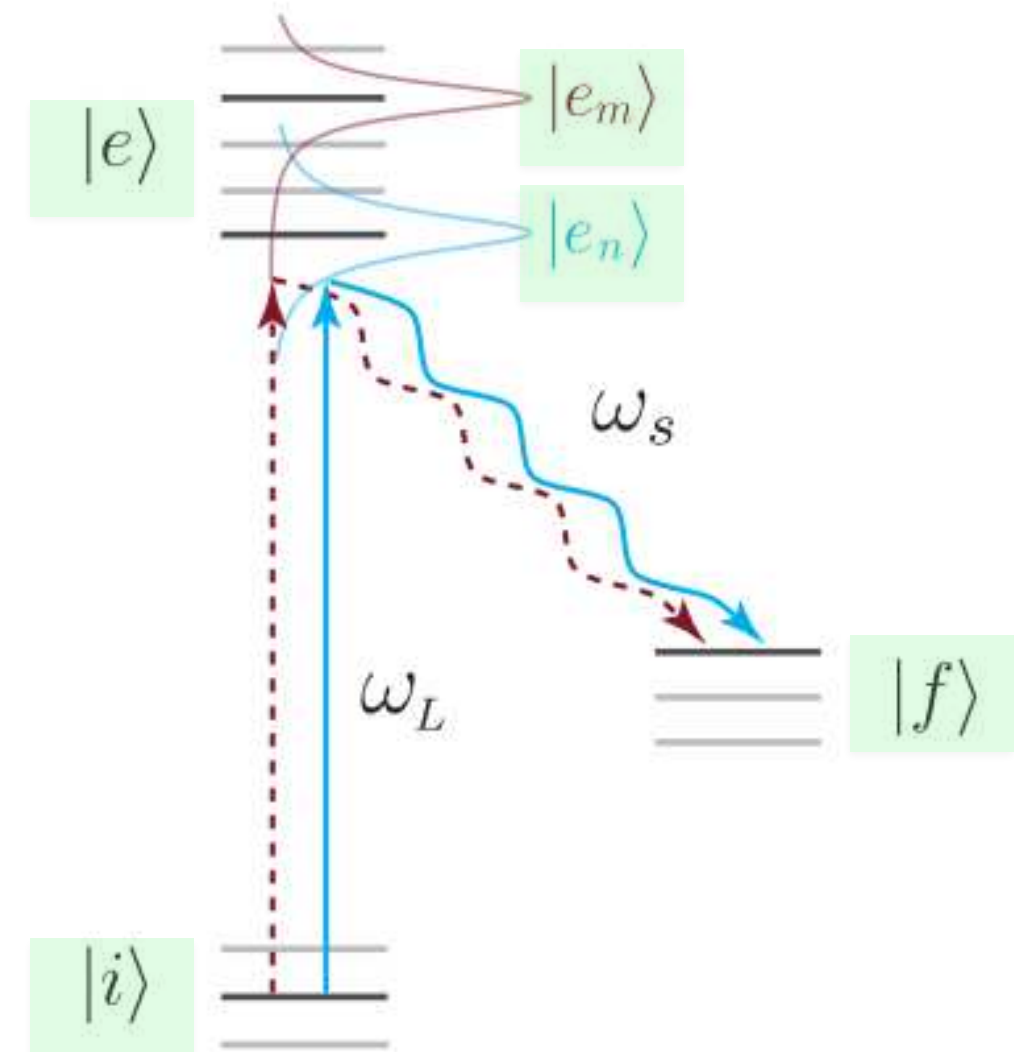
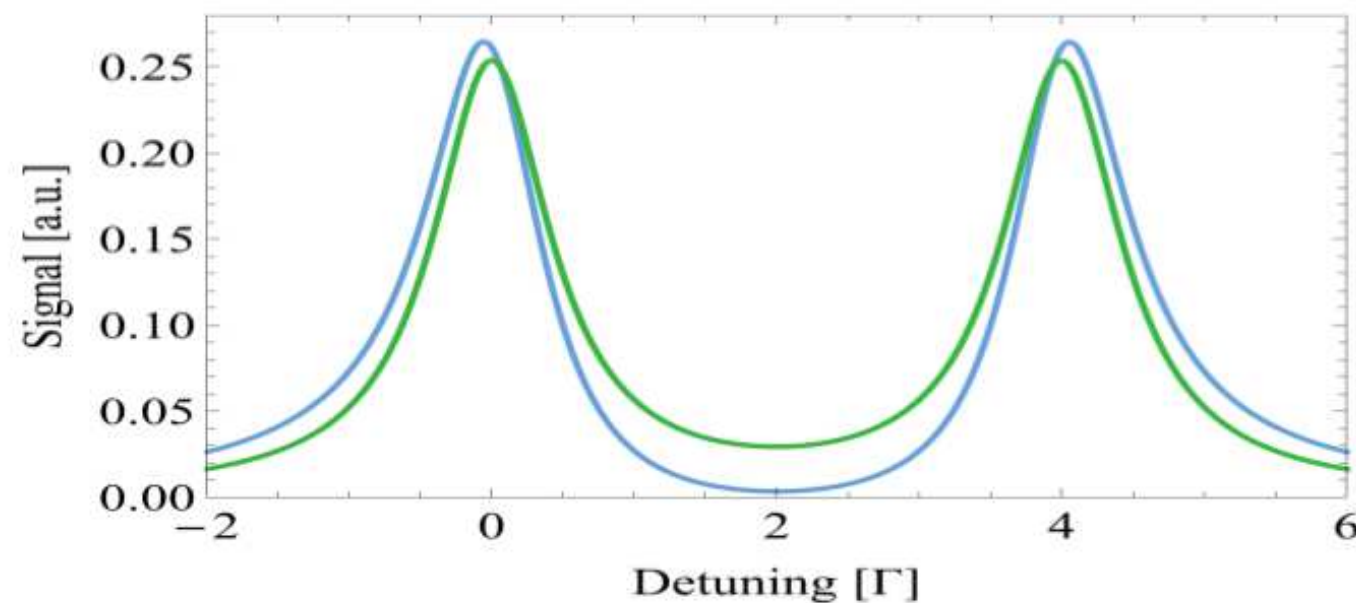
Quantum interference: an old-new systematics

Sansonetti et al., PRL 107, 023001 (2011)

Brown et al., PRA 87, 032504 (2013)

Horbatsch & Hessels, PRA 82, 052519 (2010); PRA 84, 032508 (2011)

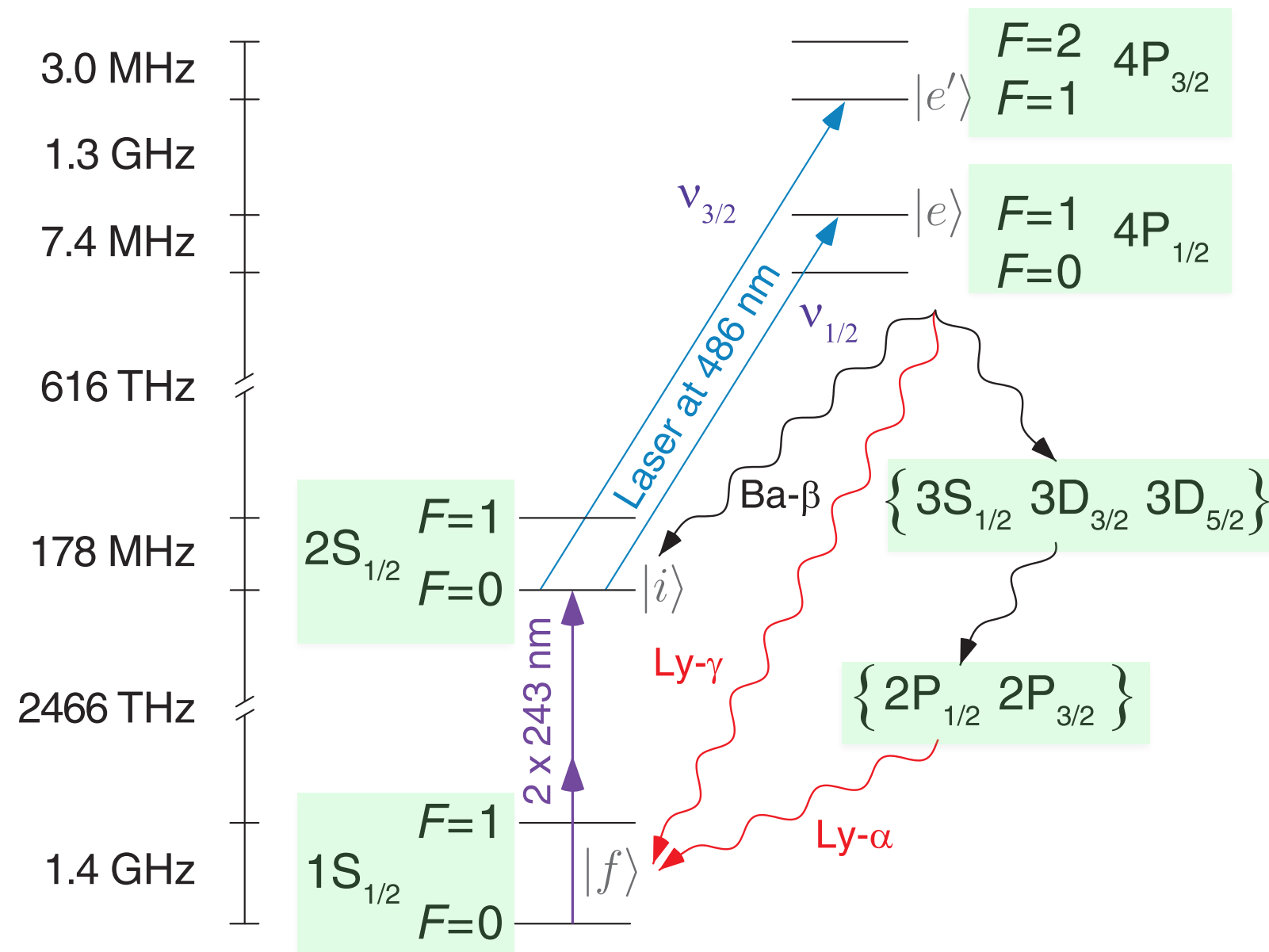
Amaro et al., PRA 92, 022514 (2015); PRA 92, 062506 (2015)



$$I(\omega) \sim \left| \frac{\vec{D} \cdot \vec{d}_1}{\omega - \omega_1 + i\Gamma_1} + \frac{\vec{D} \cdot \vec{d}_2}{\omega - \omega_2 + i\Gamma_2} \right|^2$$

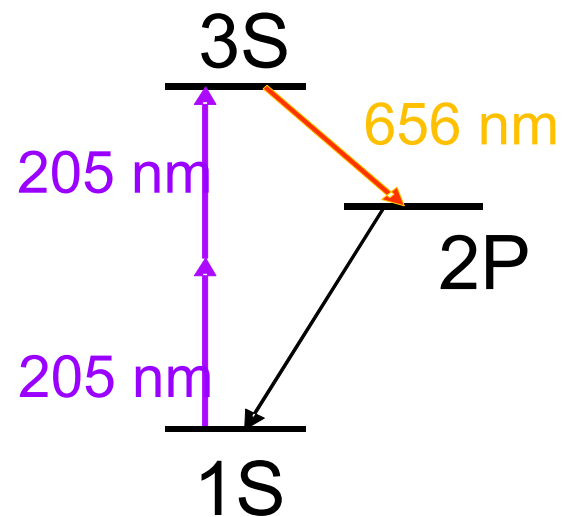
$$= \frac{(\vec{D} \cdot \vec{d}_1)^2}{(\omega - \omega_1)^2 + \Gamma_1^2} + \frac{(\vec{D} \cdot \vec{d}_2)^2}{(\omega - \omega_2)^2 + \Gamma_2^2} + 2\text{Re} \left(\frac{(\vec{D} \cdot \vec{d}_2)(\vec{D} \cdot \vec{d}_1)^*}{(\omega - \omega_1 + i\Gamma_1)(\omega - \omega_2 - i\Gamma_2)} \right)$$

Quantum interference: an old-new systematics

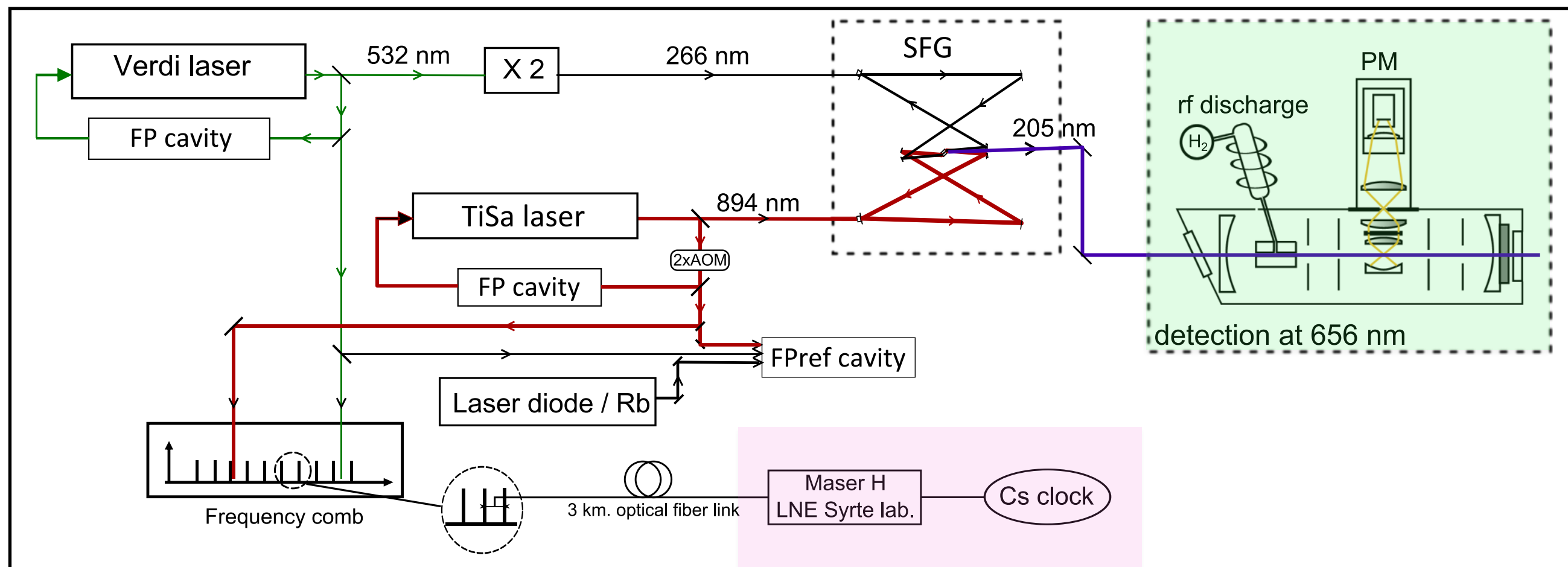


Quantum interference is complex. Its computation requires several thousands of coupled differential equations, depends on geometry, laser polarisation, detection scheme, initial state population, efficiencies etc.

New 1S-3S measurement in H (LKB, Paris)

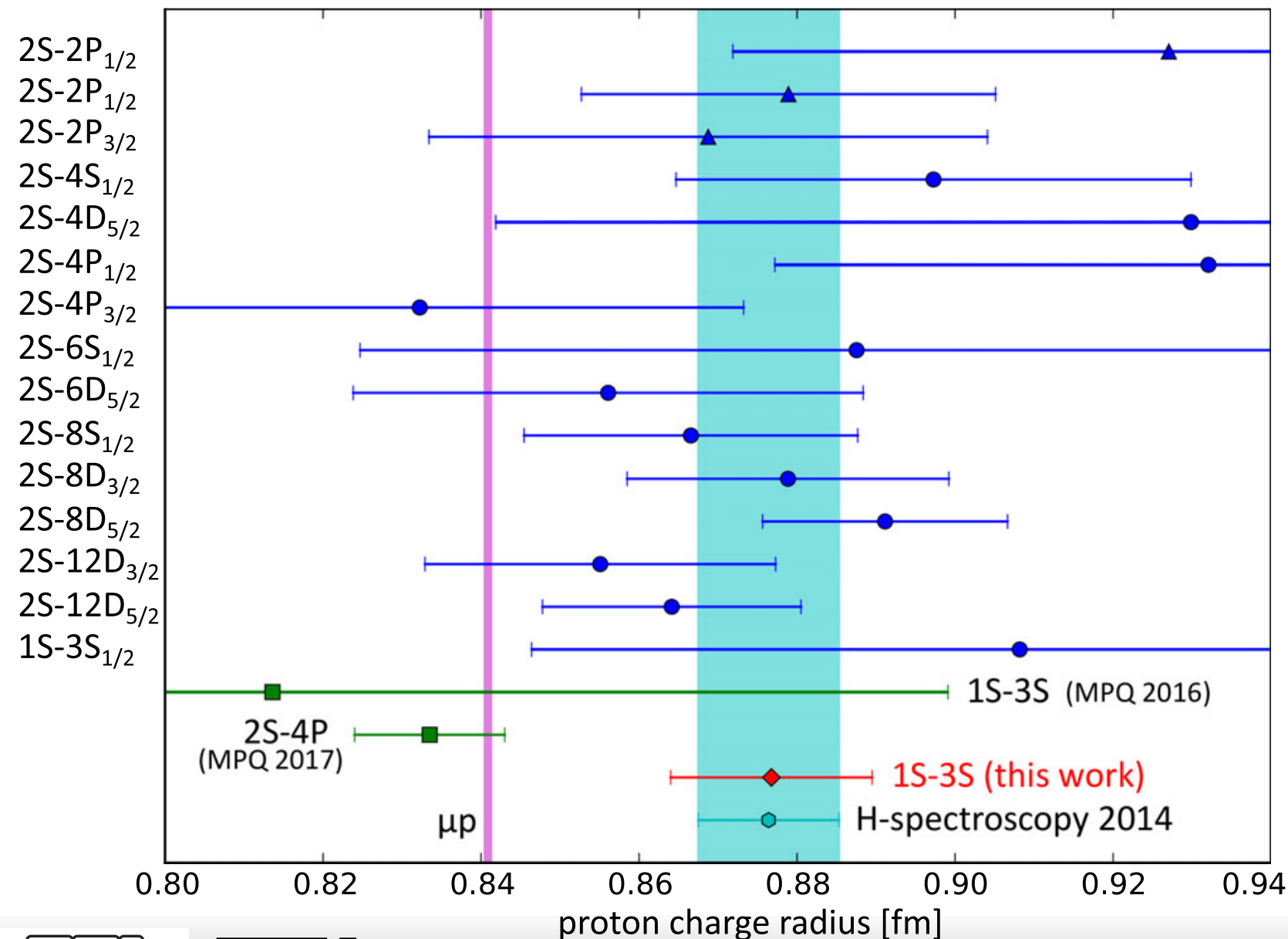


- Produce atomic H beam (room temperature)
- Excite the two-photons 1S-3S transition
- Detect the 3S-2P decay
- Plot number of 3S-2P decay vs laser frequency



New 1S-3S measurement in H (LKB, Paris, 2017)

- Line width: 1500 kHz
- Statistical uncertainty: 2.1 kHz
- Total uncertainty: 2.7 kHz
- r_p discrepancy: 9 kHz

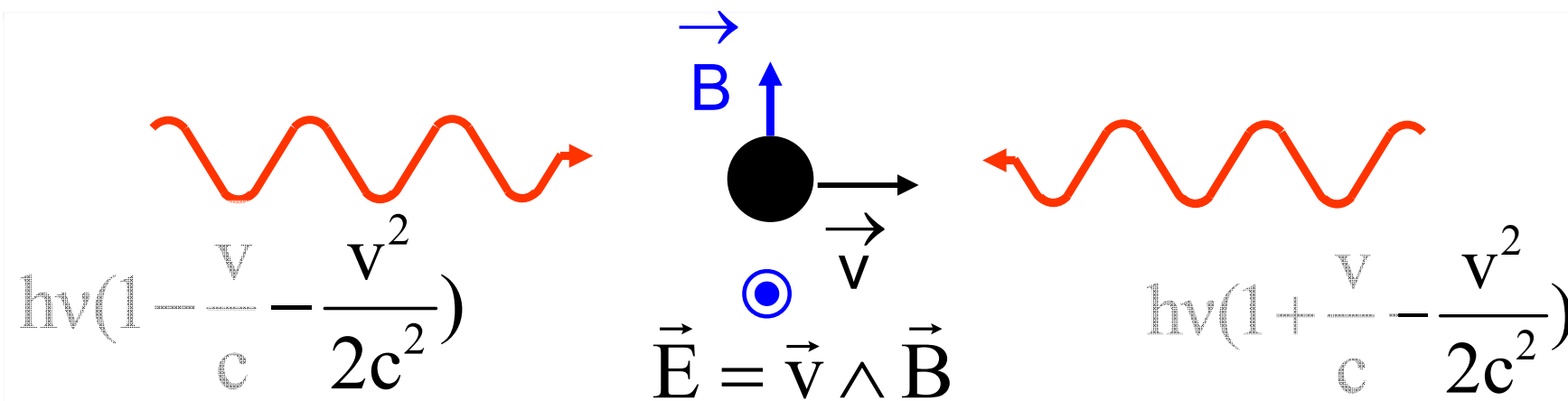


Fleurbaey et al.,
PRL120, 183001 (2018)

New 1S-3S measurement in H (LKB, Paris)

Sources of frequency shift:

- second order Doppler effect (120 kHz)
- light shift
- pressure shift

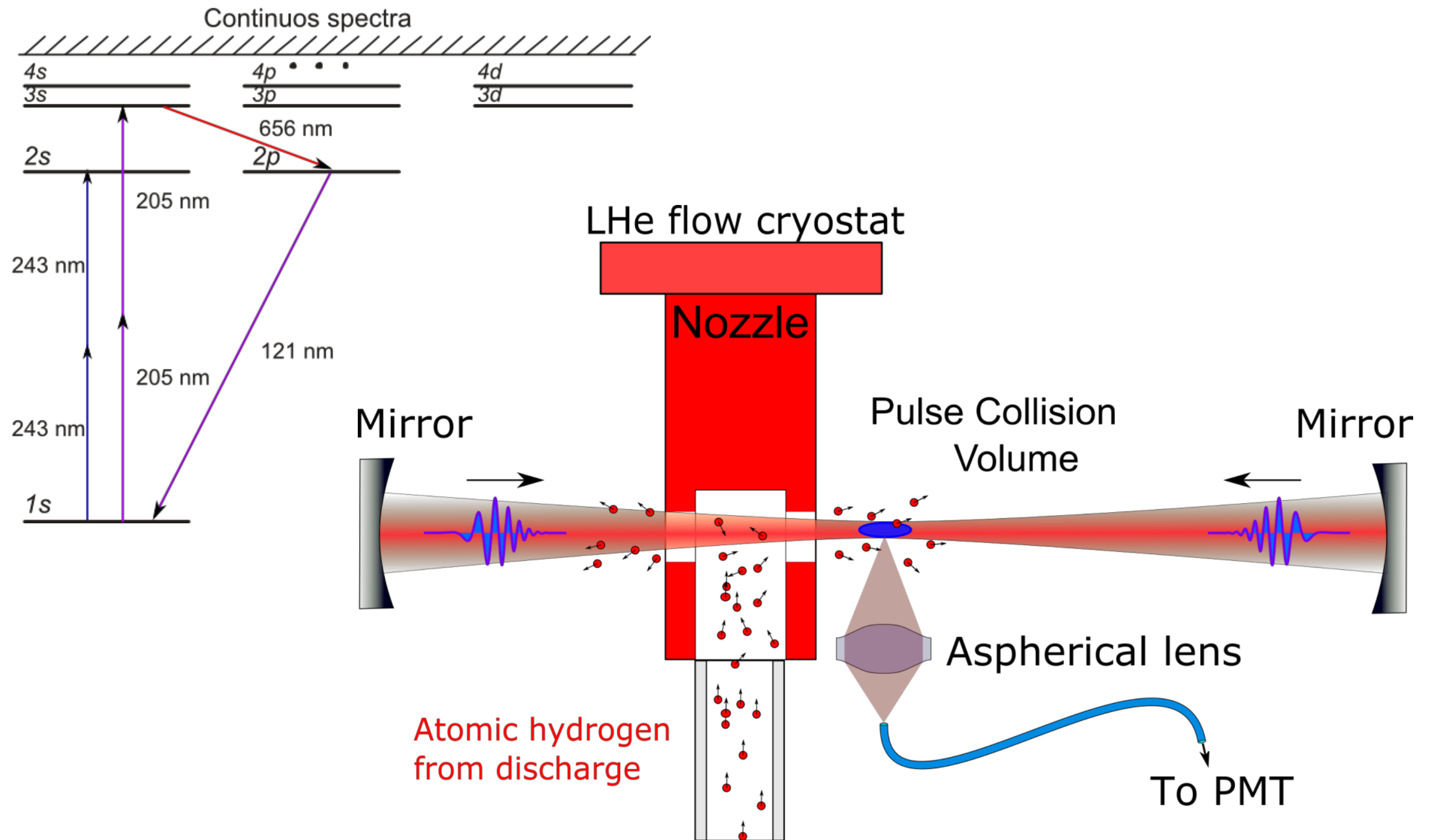


$$\delta_{\text{Stark}} = \frac{E^2}{\Delta\nu_{\text{SP}}} = \frac{v^2 B^2}{\Delta\nu_{\text{SP}}}$$

$$\delta_{\text{dop}} = -\nu_{\text{at}} \frac{v^2}{2c^2}$$

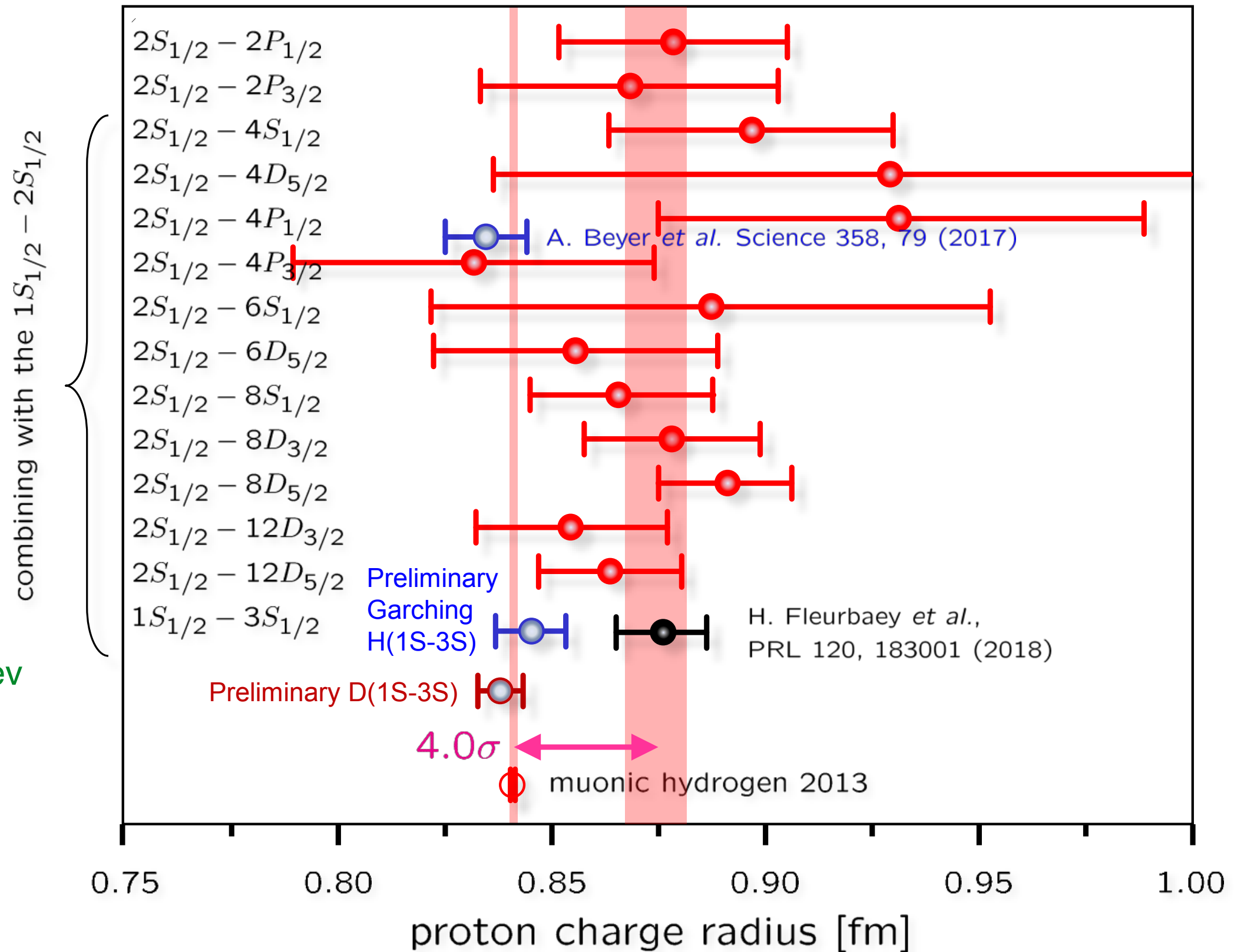
Biraben, Julien, Plon and Nez, Europhys. Lett. 15, 831 (1991)
Galtier et al., J. Phys. and Chem. Ref. Data 44, 031201 (2015)

Preliminary 1S-3S measurement in H/D (MPQ, 2018)



A. Matveev

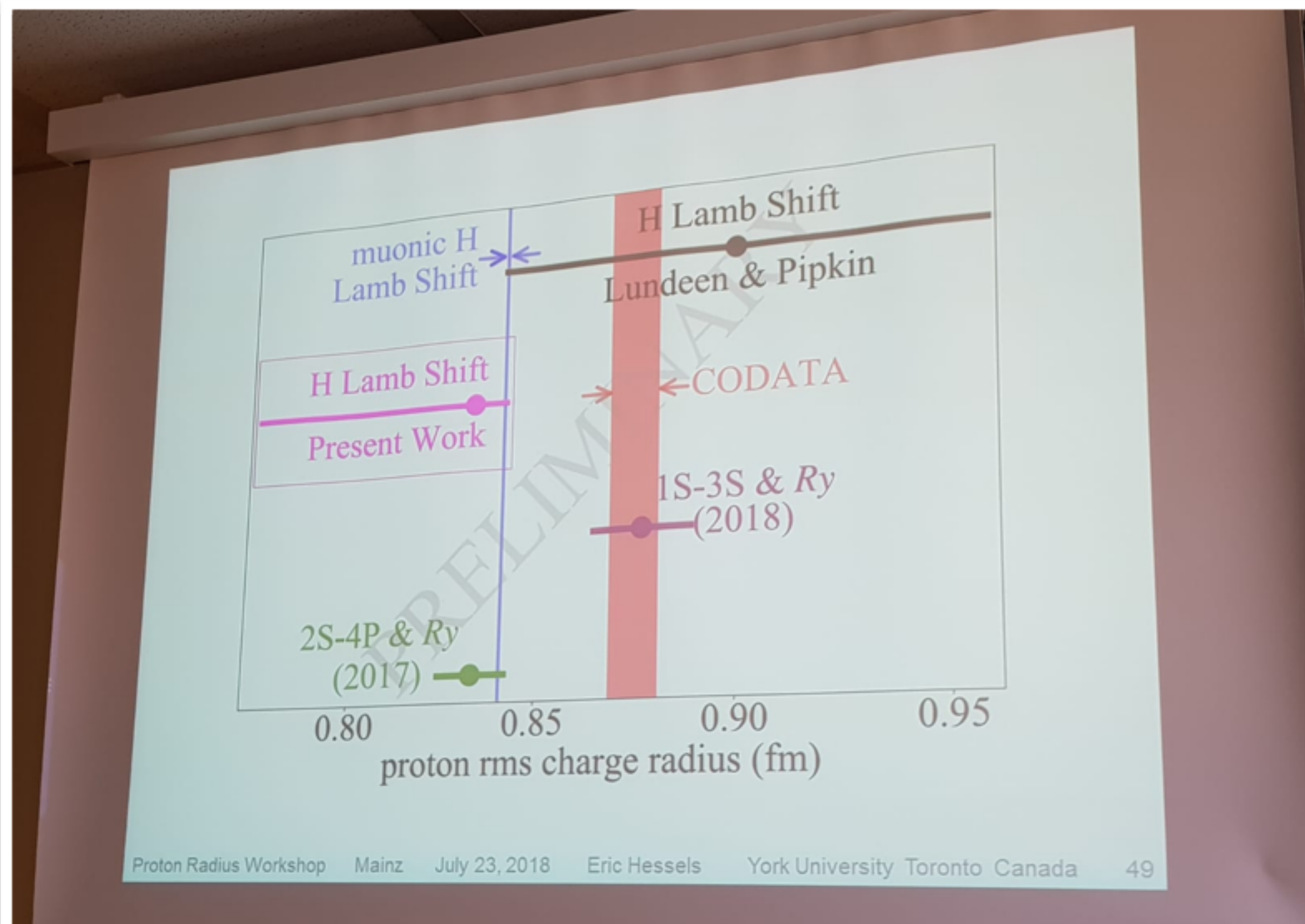
Preliminary 1S-3S measurement in H/D (MPQ, 2018)



A. Matveev

Preliminary 2S-2P measurement in H (Toronto, 2018)

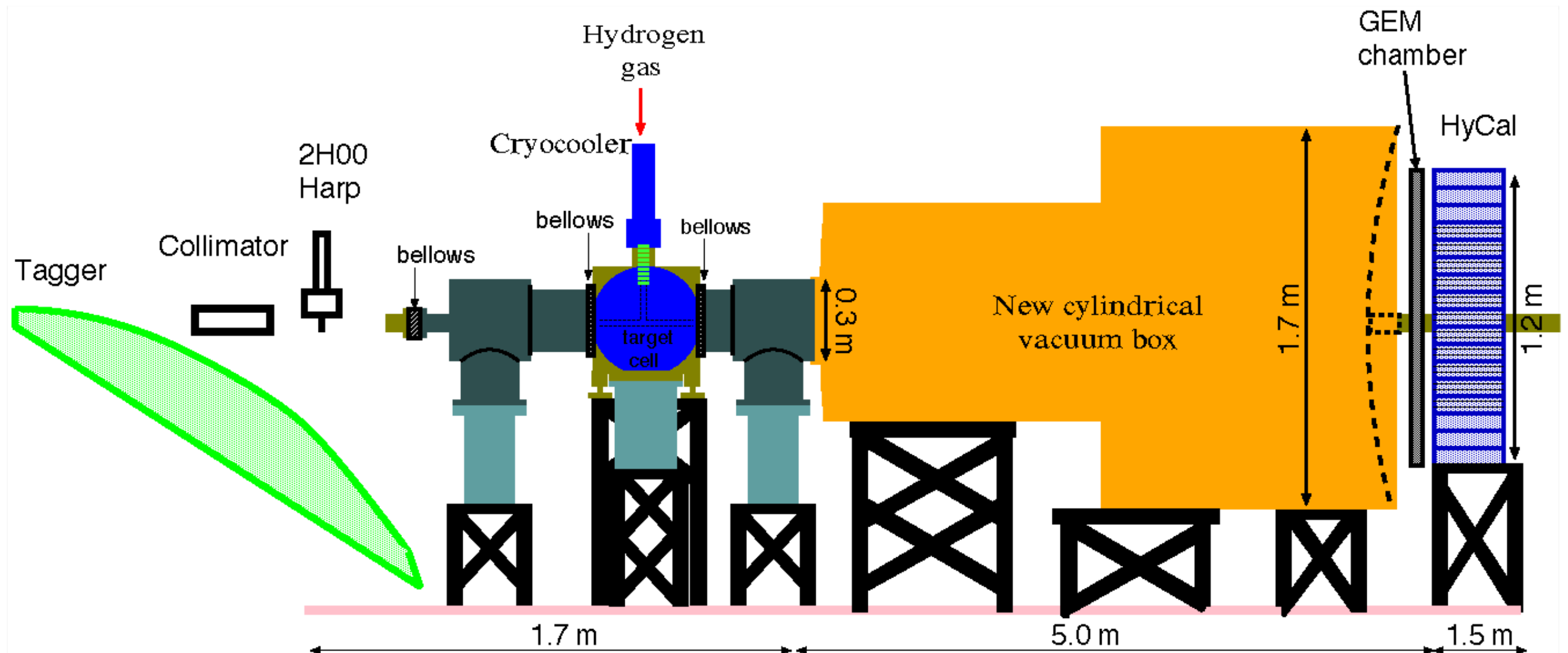
E. Hessels



Preliminary results from new e-p scattering (PRad, 2018)

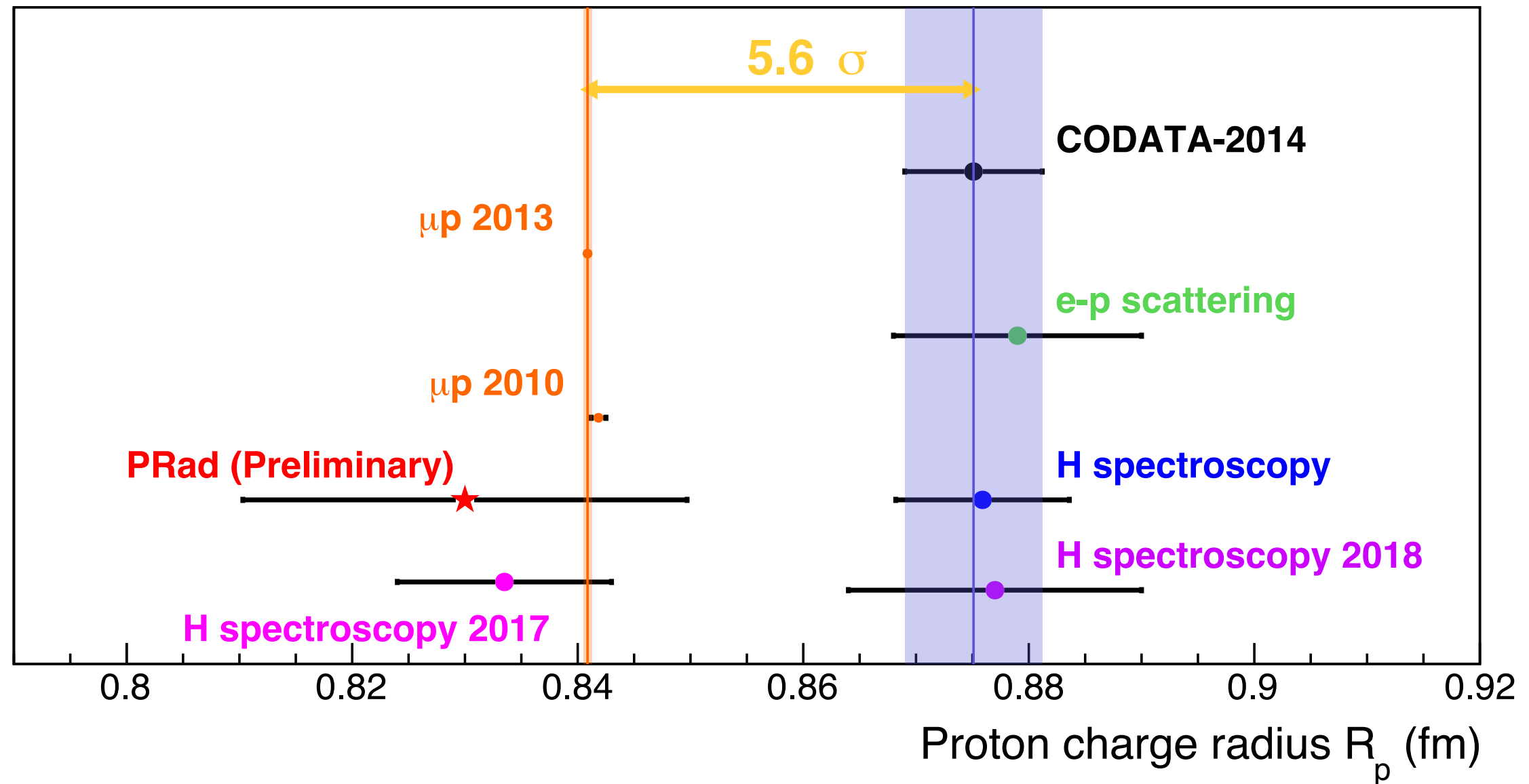
- windowless target
- non-magnetic calorimeter
- large GEM + scintillators
- Minimal angle
- Q^2_{\min} reduced by 20 to $2 \times 10^{-4} \text{ GeV}^2$
- Normalise with Møller scatt.

$$\left(\frac{d\sigma}{d\Omega} \right)_{ep} = \frac{N_{exp}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{exp}(ee \rightarrow ee)} \cdot \frac{\epsilon_{geom}^{ee}}{\epsilon_{geom}^{ep}} \cdot \frac{\epsilon_{det}^{ee}}{\epsilon_{det}^{ep}} \cdot \left(\frac{d\sigma}{d\Omega} \right)_{ee}$$

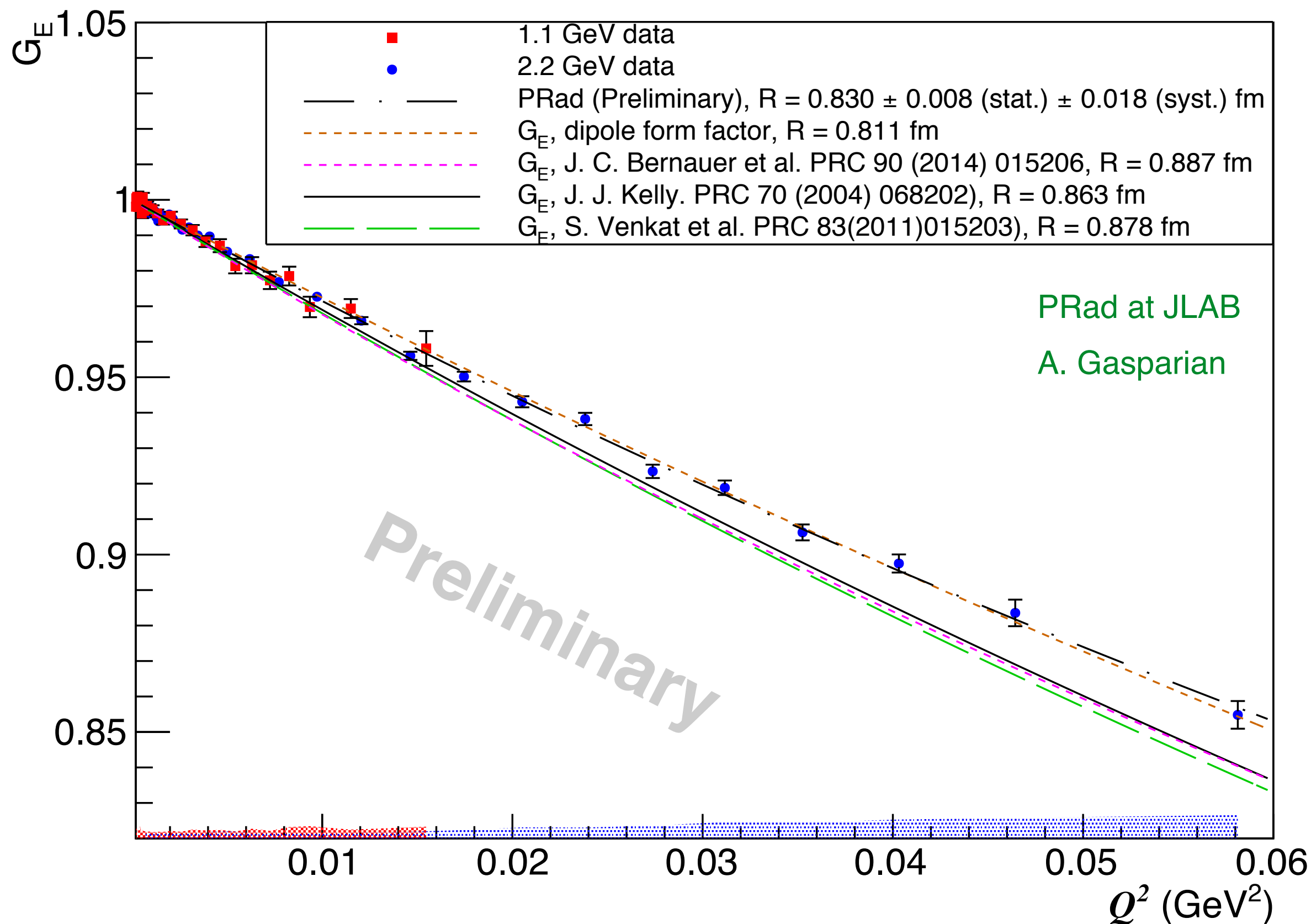


Preliminary results from e-p scattering (JLAB, 2018)

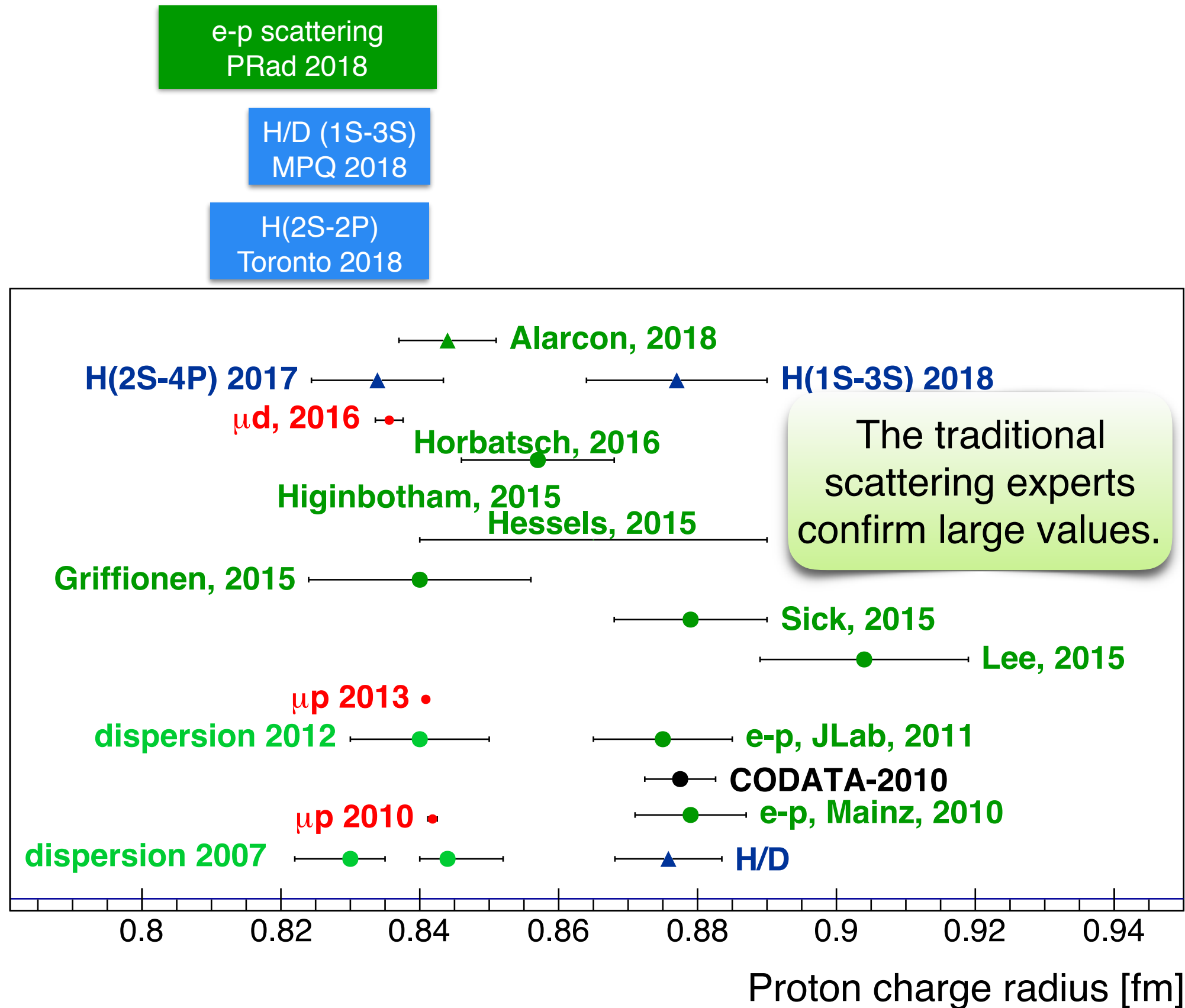
A. Gasparian

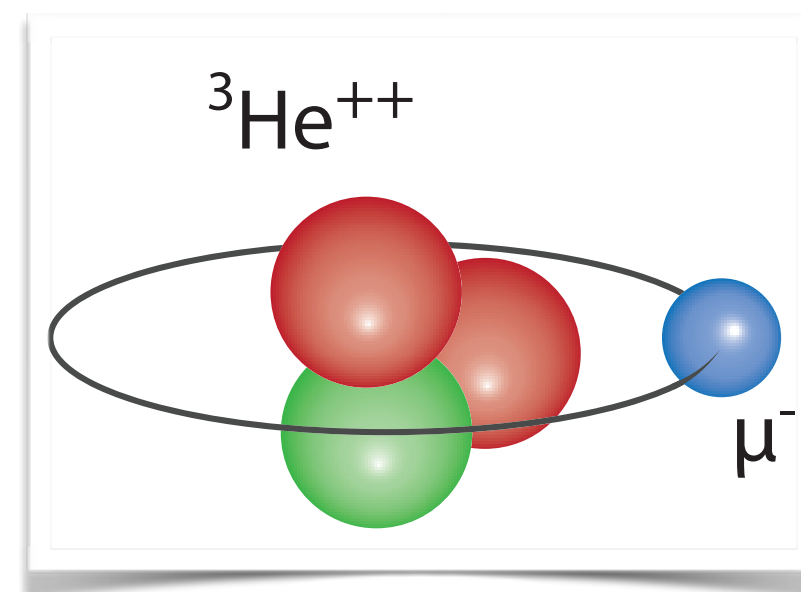
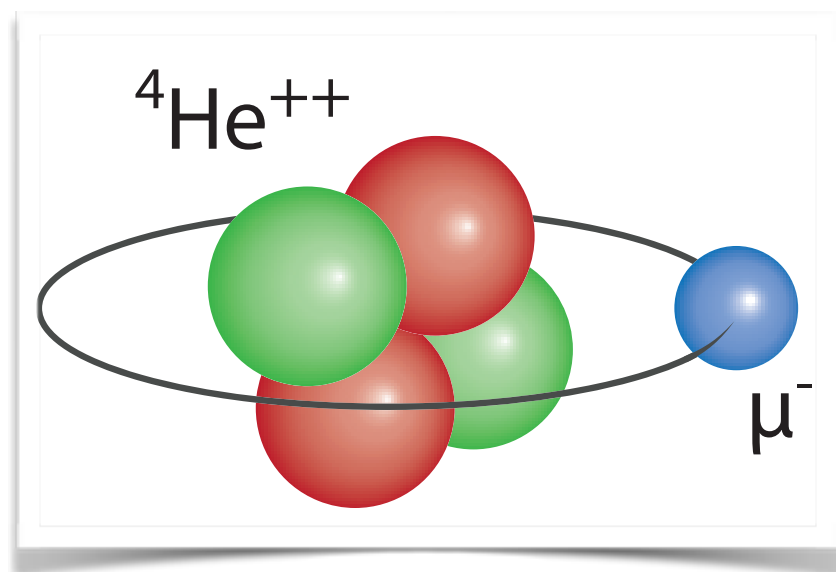


Preliminary results from e-p scattering (JLAB, 2018)

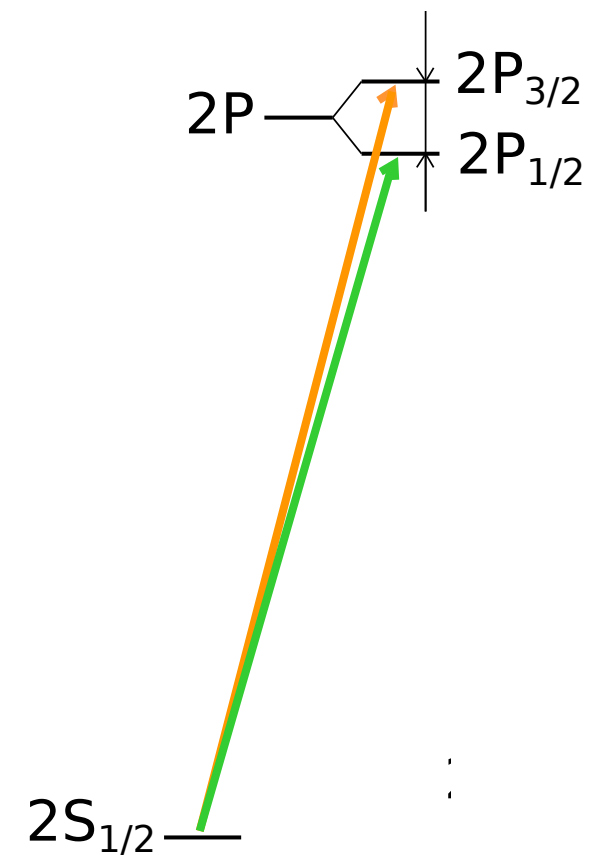
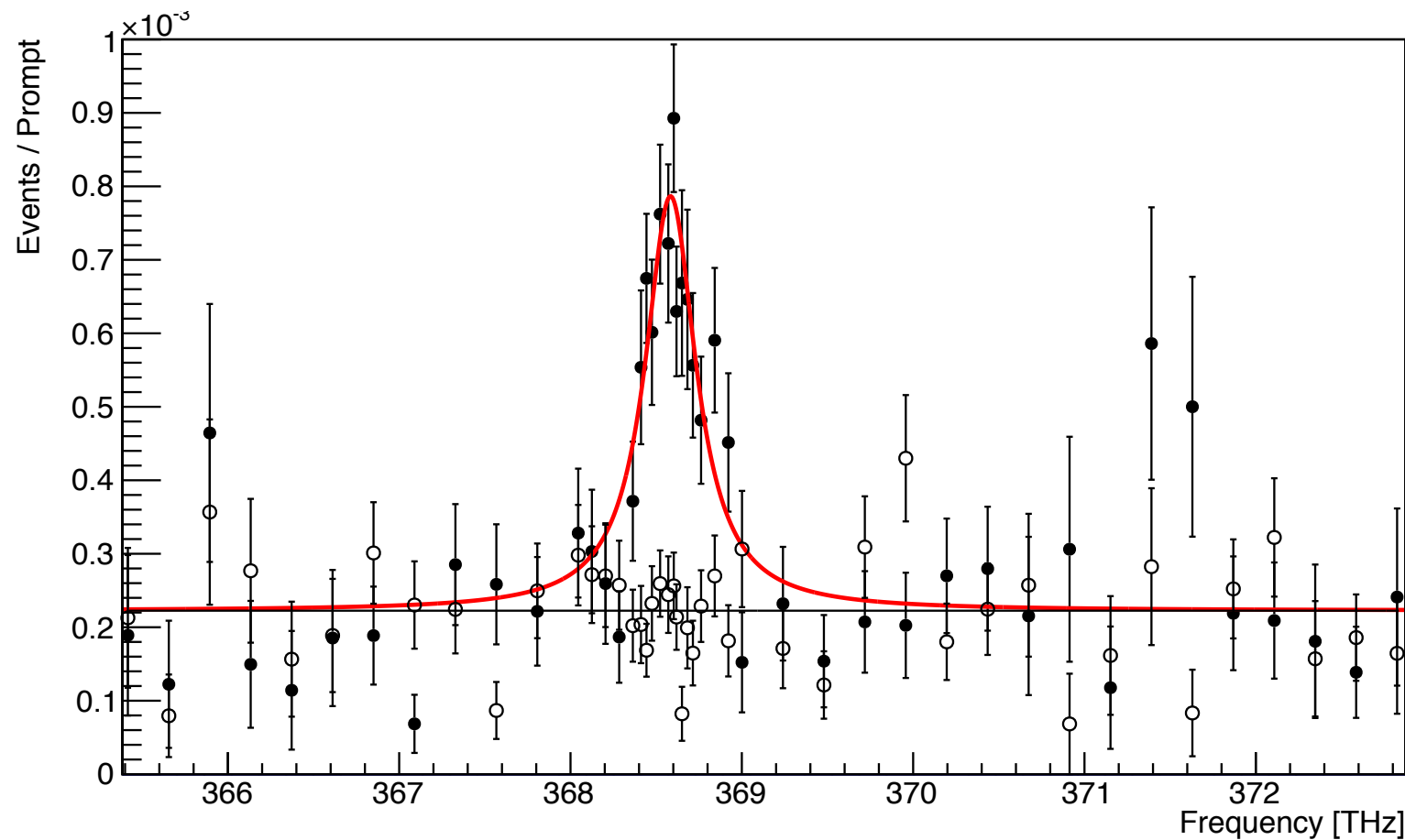


Present status





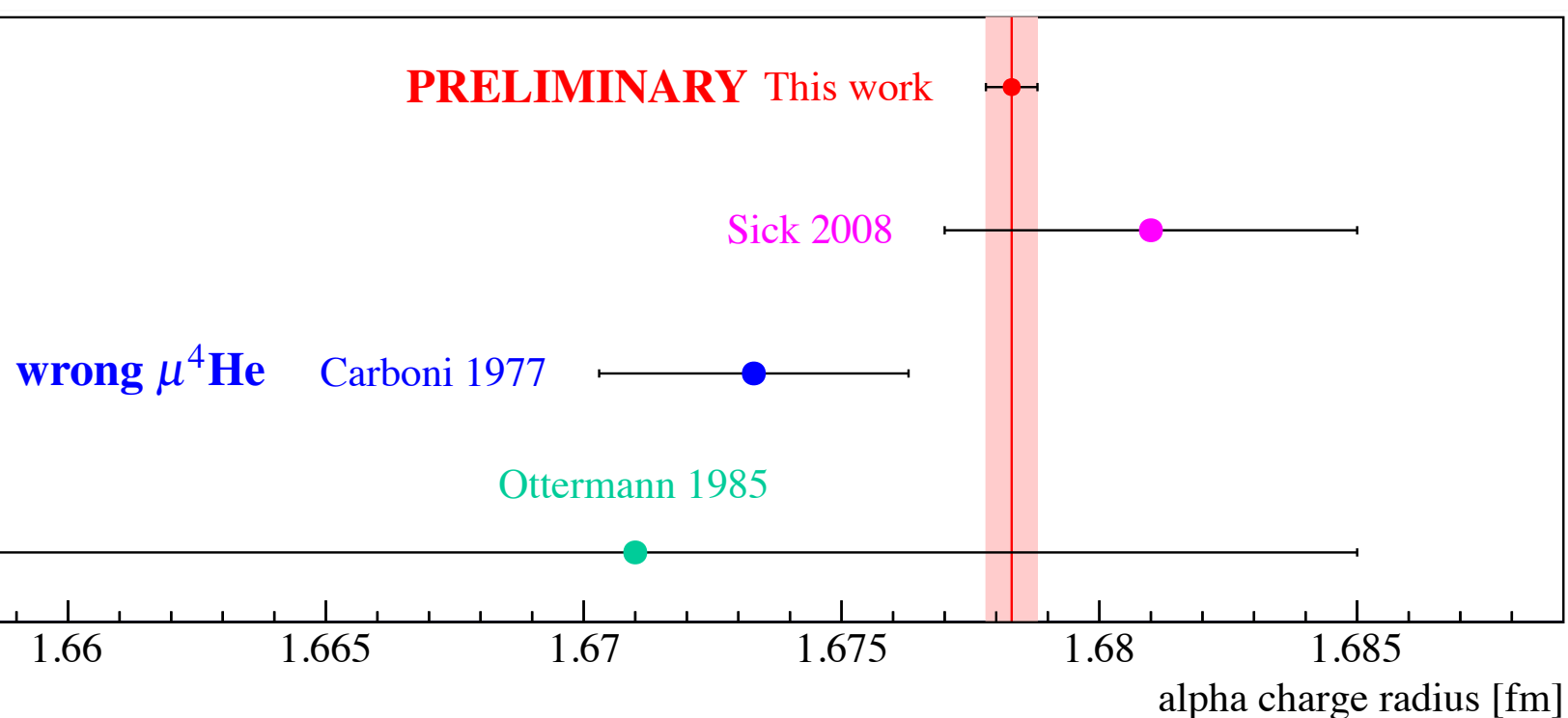
Spectroscopy of muonic Helium ($\mu^4\text{He}^+$)



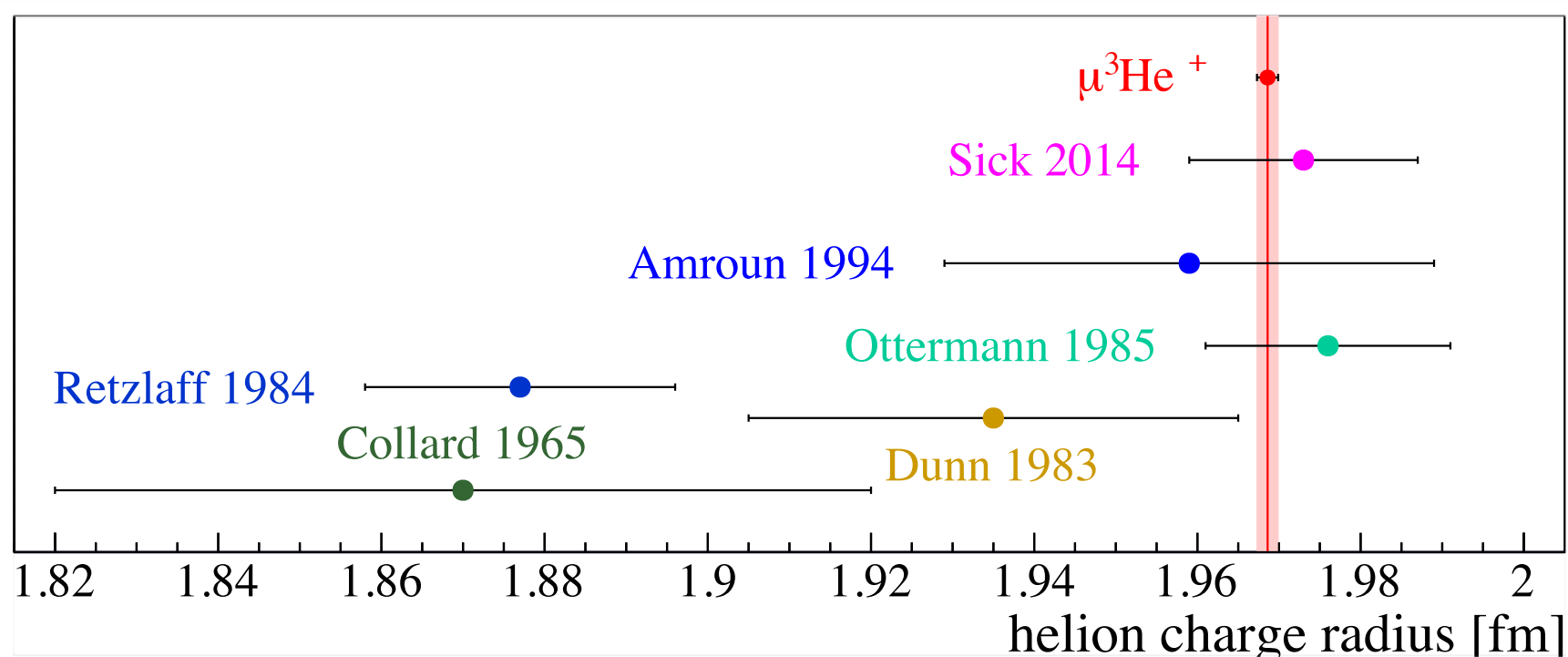
Experimental accuracy: 17 GHz (0.066 meV)
 Statistics / Laser freq. / systematics unc.: 17 GHz / 100 MHz / 10 MHz
 Theory uncertainty: 0.205 meV

$$\Delta E(2S-2P_{3/2}) = \underbrace{1668.487(14)}_{\text{QED}} - \underbrace{106.358(7)R_E^2}_{\text{finite size}} + \underbrace{6.761(77) + 3.296(189)}_{\text{TPE}} + \underbrace{146.197(12)}_{\text{fine splitting}} \text{ [meV]}$$

Alpha-particle and helion radii from μHe^+ spectroscopy



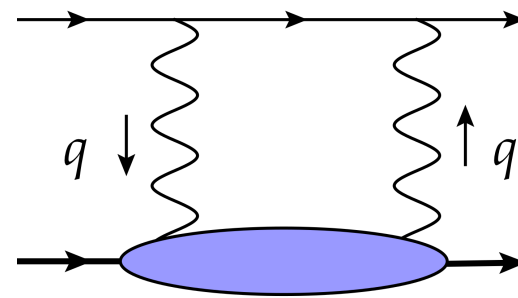
Extraction of these charge radii from muonic helium is limited by the polarisability contributions.



TPE: the key to extract precise charge radii

Dinur, Ji, Barnea,
Bacca, Hernandez

chiral EFT
few-nucleon th.



Phenomenological:

- dispersion relations
- data
- sum rules

Carlson, Gorchtein,
Vanderhaeghen

2N Force

3N Force

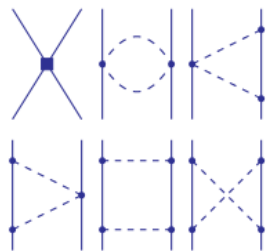
LO

$(Q/\Lambda_\chi)^0$



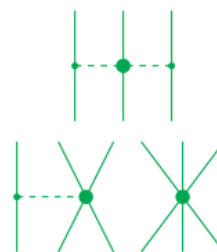
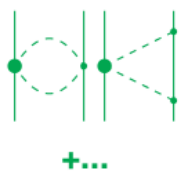
NLO

$(Q/\Lambda_\chi)^2$



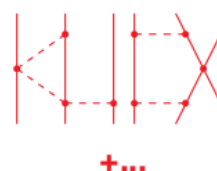
NNLO

$(Q/\Lambda_\chi)^3$



N³LO

$(Q/\Lambda_\chi)^4$



Impressive
improvement in last
years

For $\mu^3\text{He}$

Dispersion: 15.14 (49) meV
Few-nucleon th.: 15.46 (39) meV

Impact of muonic helium (μHe) measurements

Antognini et al., Can. J. Phys. 89, 47 (2011)

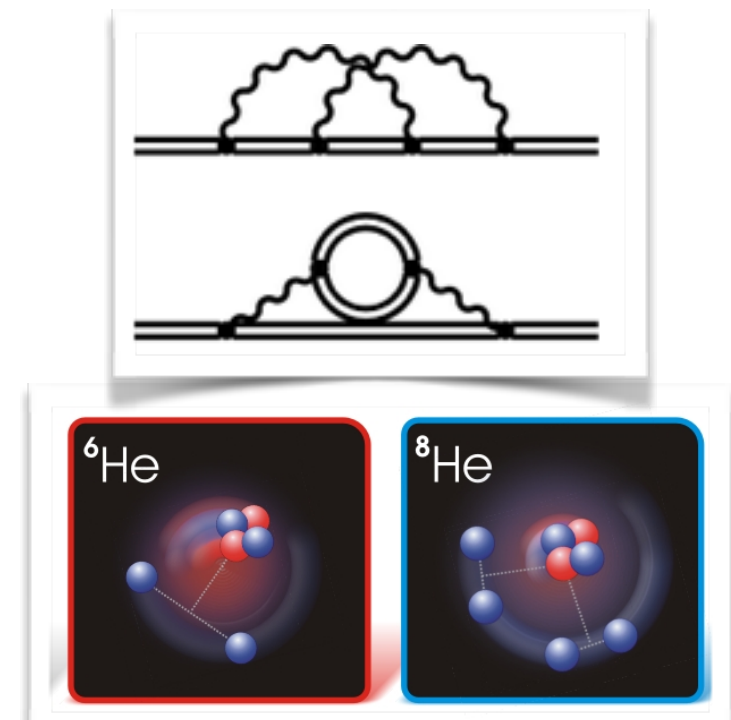
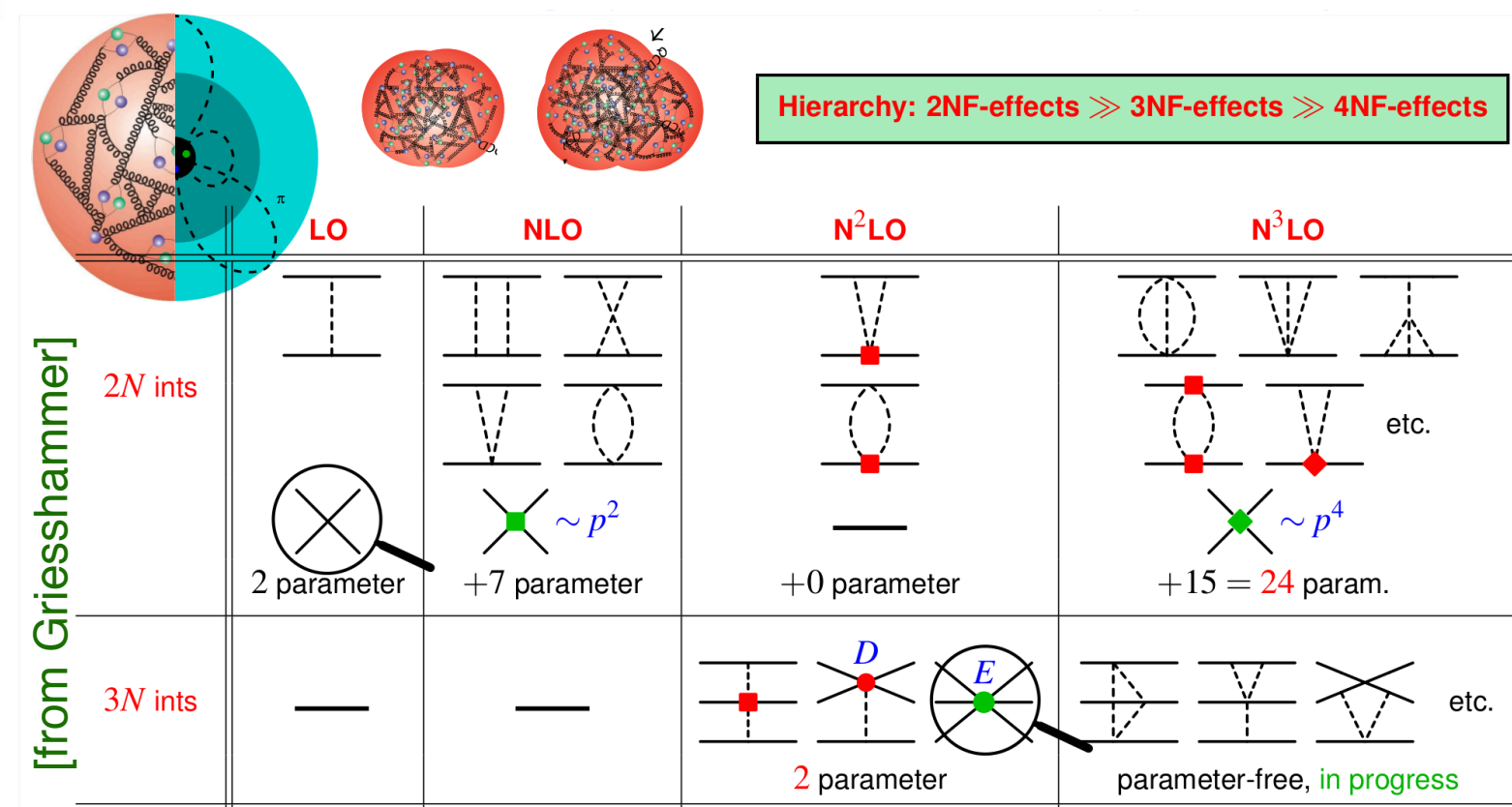
Constraints proton radius puzzle
Expose existence/absence of muonic force

Benchmark for few-nucleon theories

Improve absolute radii of ${}^6\text{He}$ and ${}^8\text{He}$

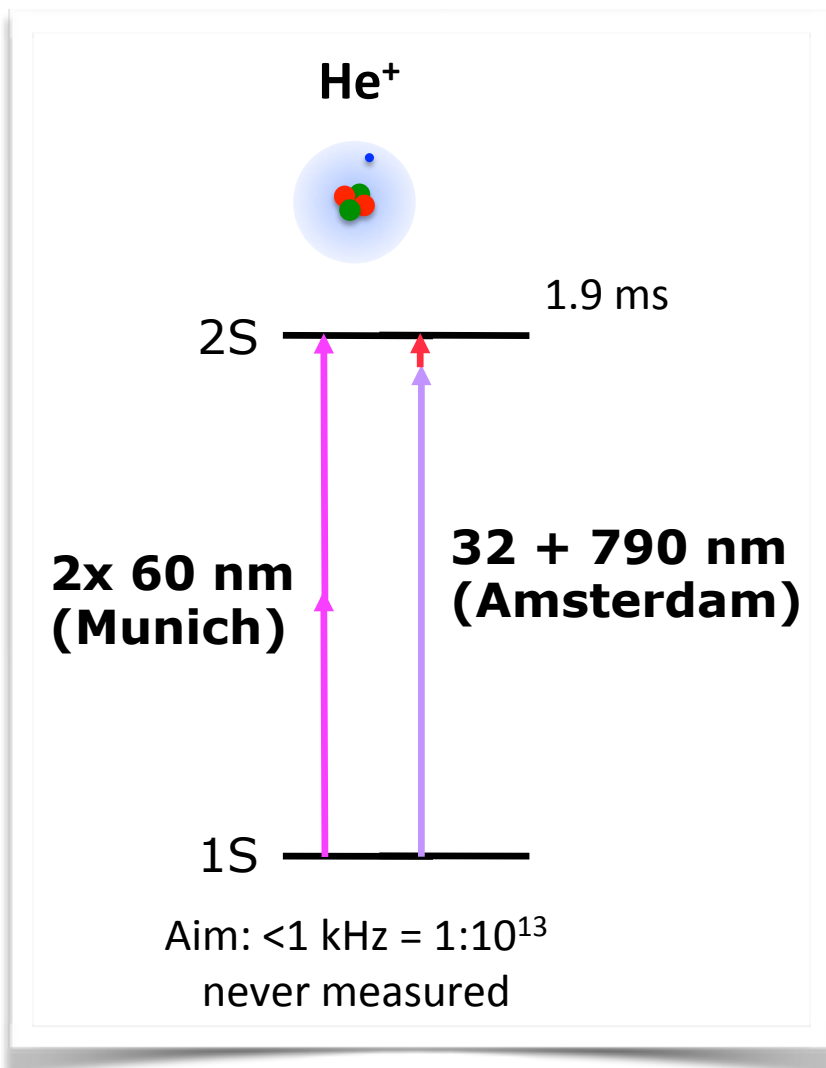
Enhanced bound-state QED test when combined with He and He^+ spectroscopy

Pachucki, Indelicato, Jentschura, Yerokhin, Eides, Karshenboim...



Lu et al., RMP 85 1383 (2013)

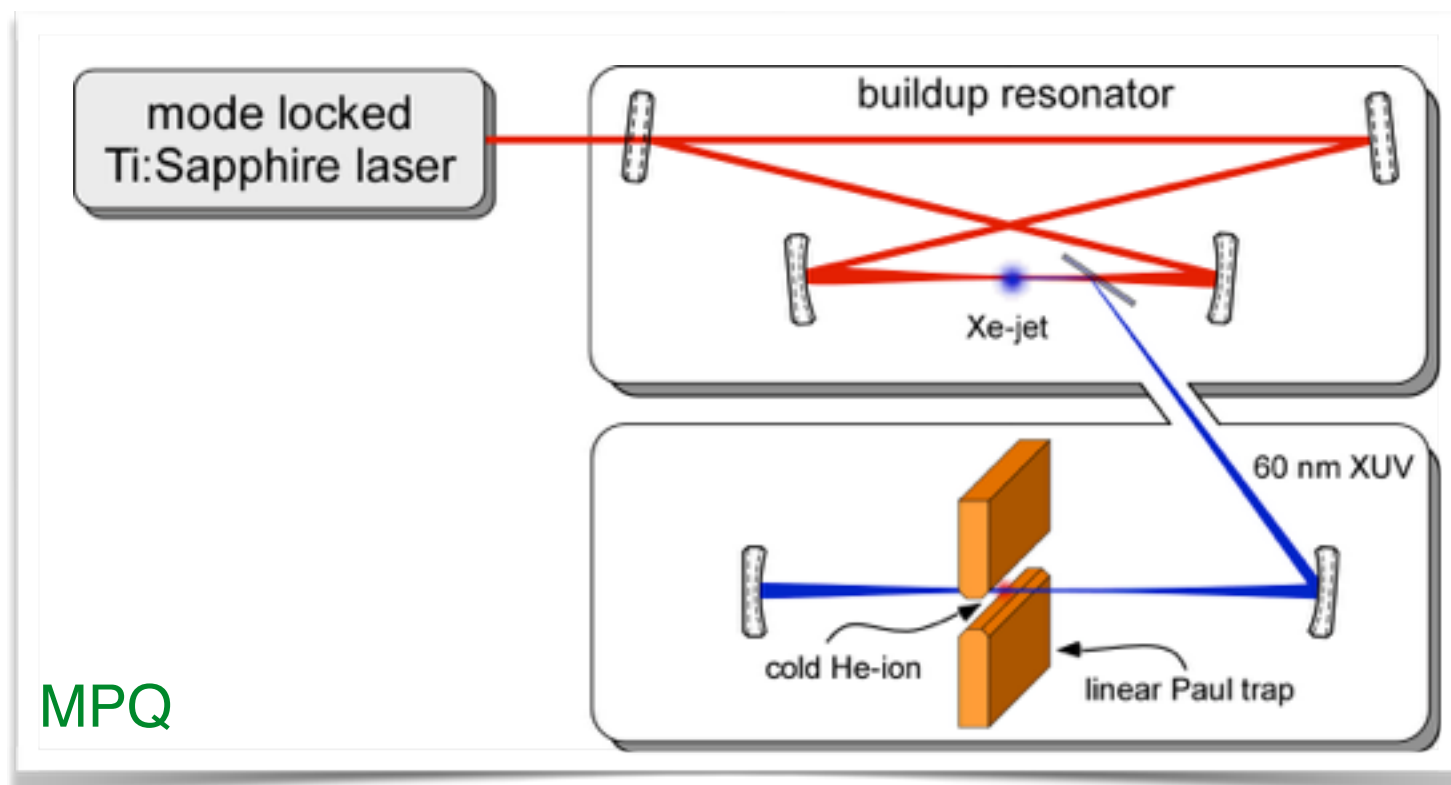
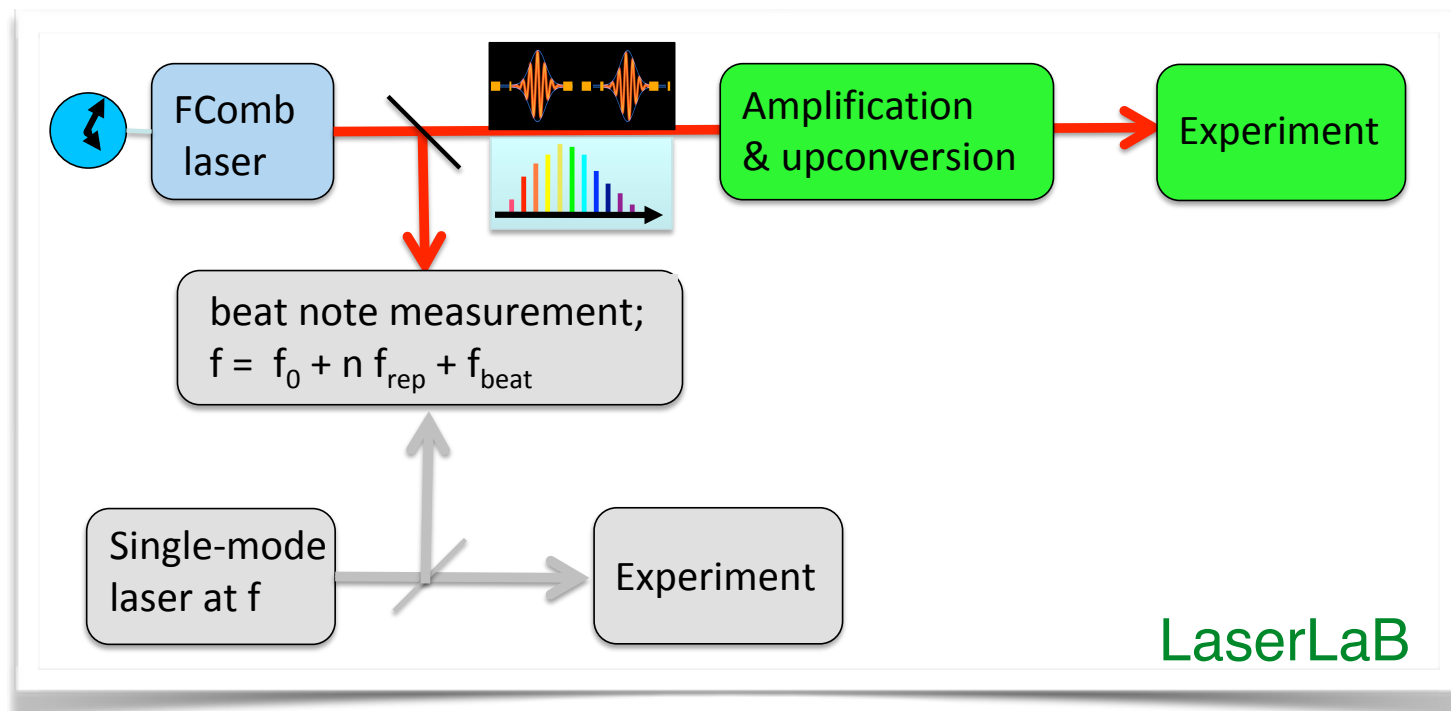
Challenging spectroscopy of He and He⁺



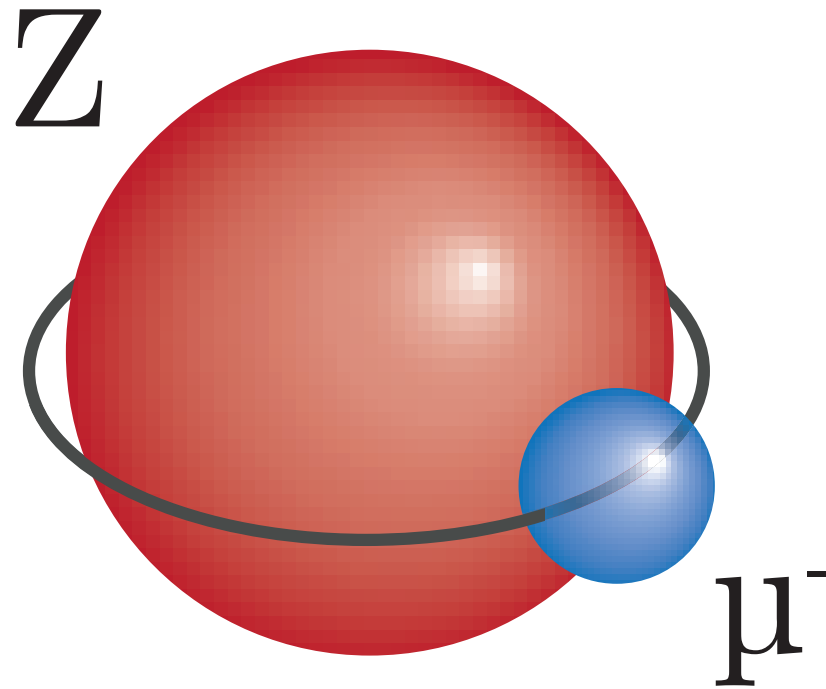
T. Udem

T.W. Hänsch

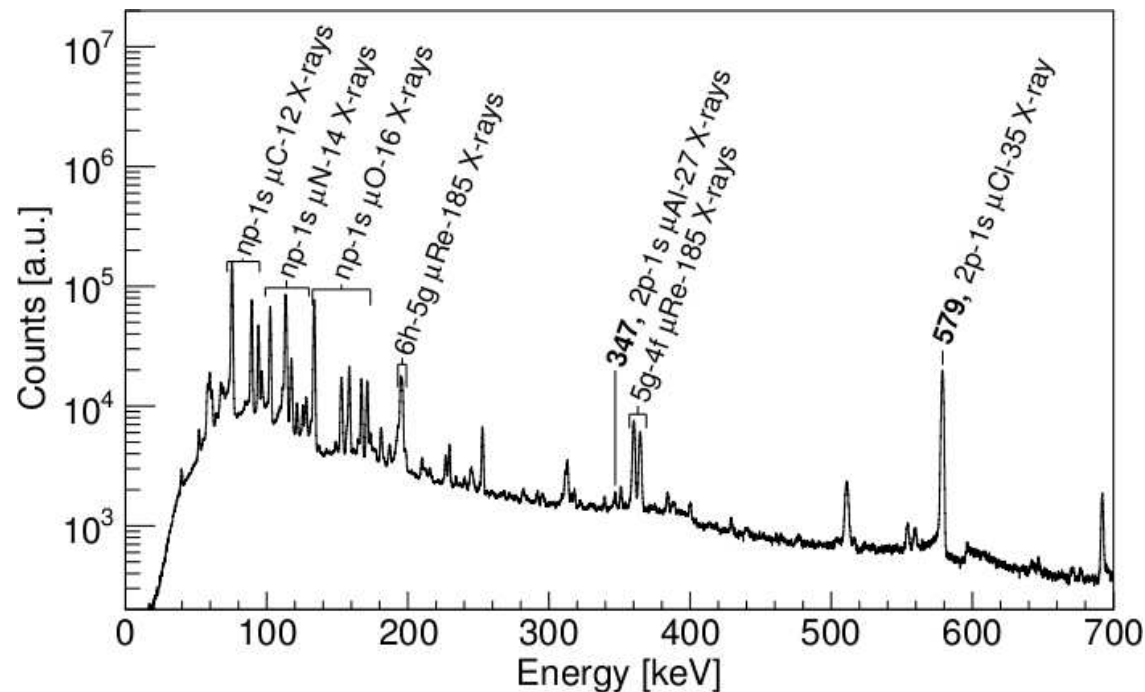
K. Eikema



The muX project (PSI, ongoing)

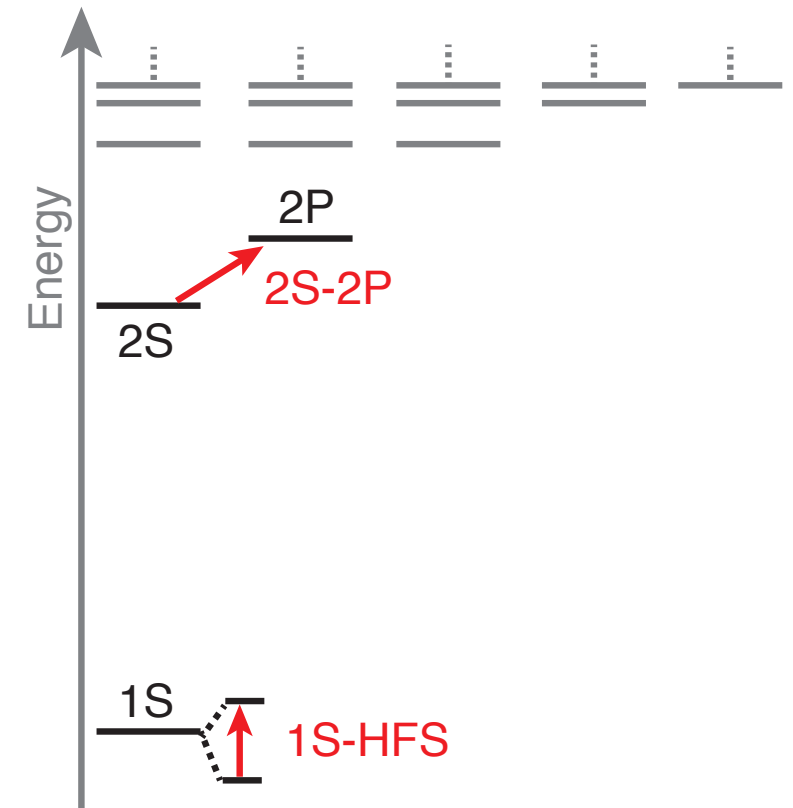
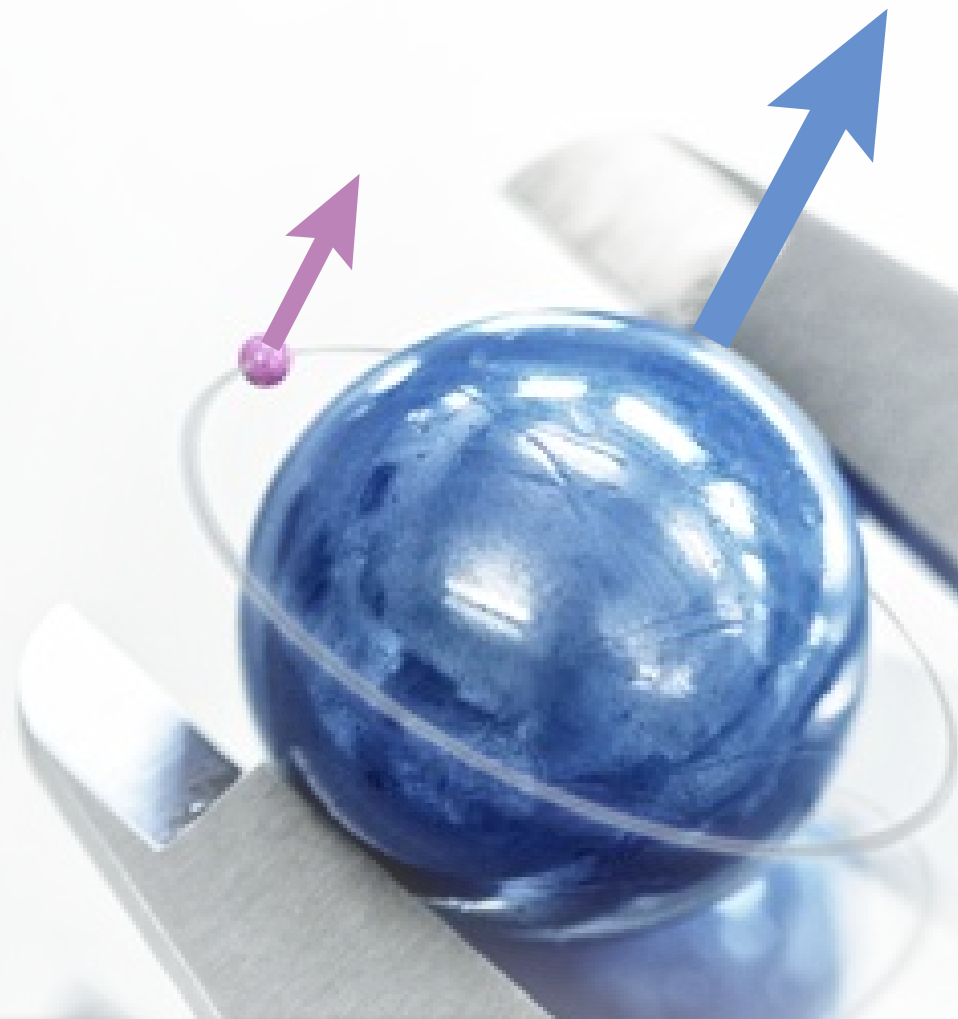


- charge radii
- quadrupole moments for radioactive nuclei



- H-like atoms
- MeV transition energies
- ΔE_{size} : MeV finite-size effects
- ΔE_{QED} : easy QED corrections
- ΔE_{el} : small atomic electron corrections
- ΔE_{pol} : difficult nuclear polarisability correc.

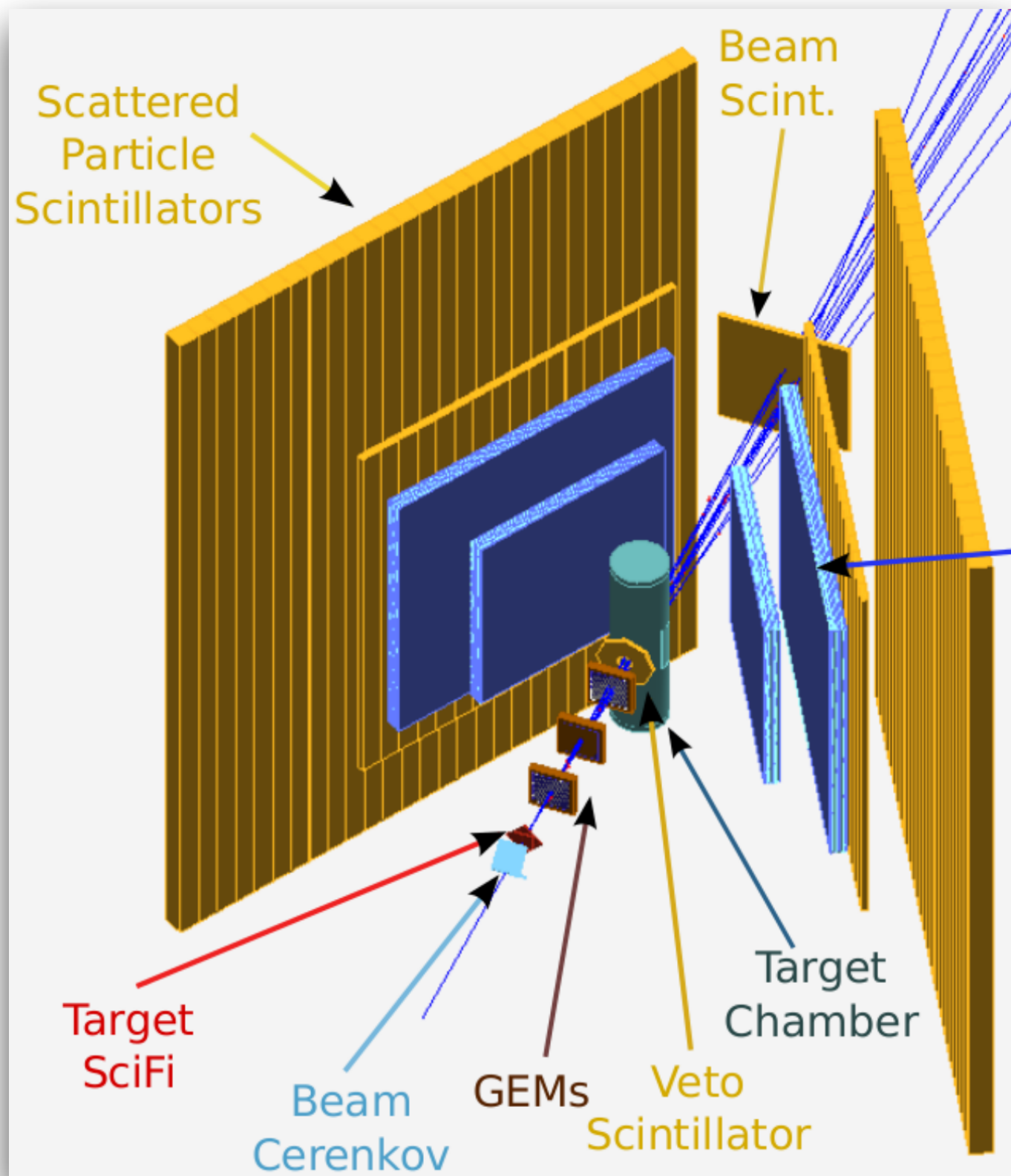
The hyperfine splitting in μp (PSI, ongoing)



- From 2S-2P
→ charge radii
- From HFS
→ magnetic (Zemach) radii

- 2S-2P μp
- 2S-2P μd
- 2S-2P $\mu^3\text{He}$, $\mu^4\text{He}$
- 1S-HFS μp

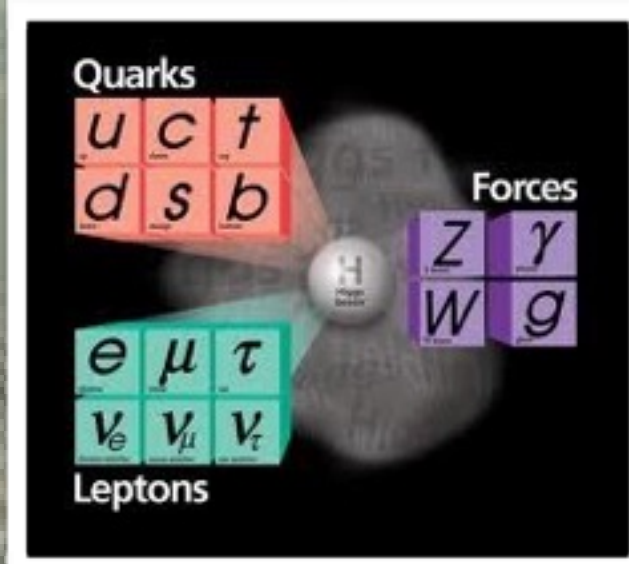
MUSE: Muon scattering (PSI, ongoing)



MUSE at PSI

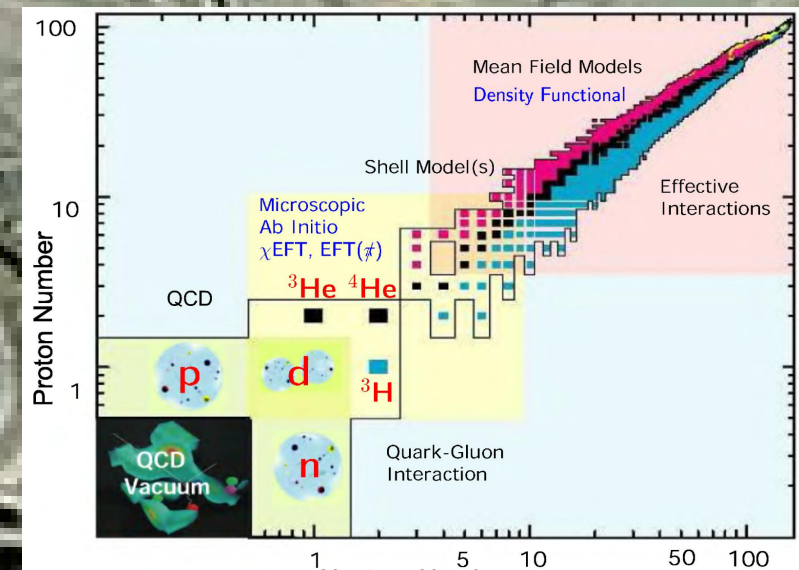
- μ^\pm -p, e^\pm -p scattering
down to $Q^2_{\min} = 2 \times 10^{-3} \text{ GeV}^2$
- Common uncertainties
 \Rightarrow precise $\Delta r = r_p^\mu - r_p^e$
- test μ -e universality
- measure TPE

arXiv:1709.09753



Test of H energy levels
Bound-state QED

BSM physics



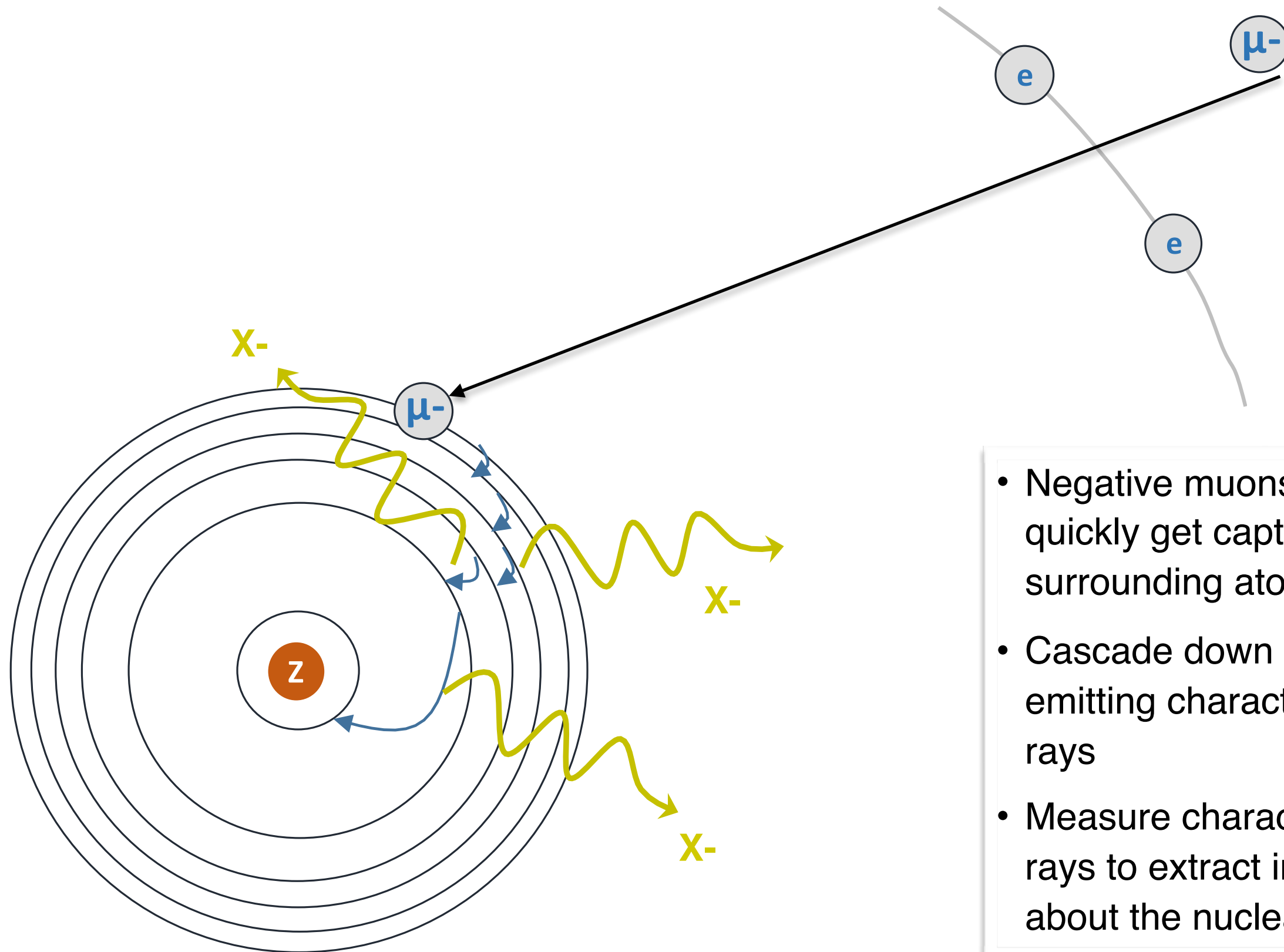
nuclear charge radii
form factors,
EFT, chiral th., lattice,
few-nucleon th.

electron scattering

H, H₂, H₂⁺, He, He⁺
spectroscopy

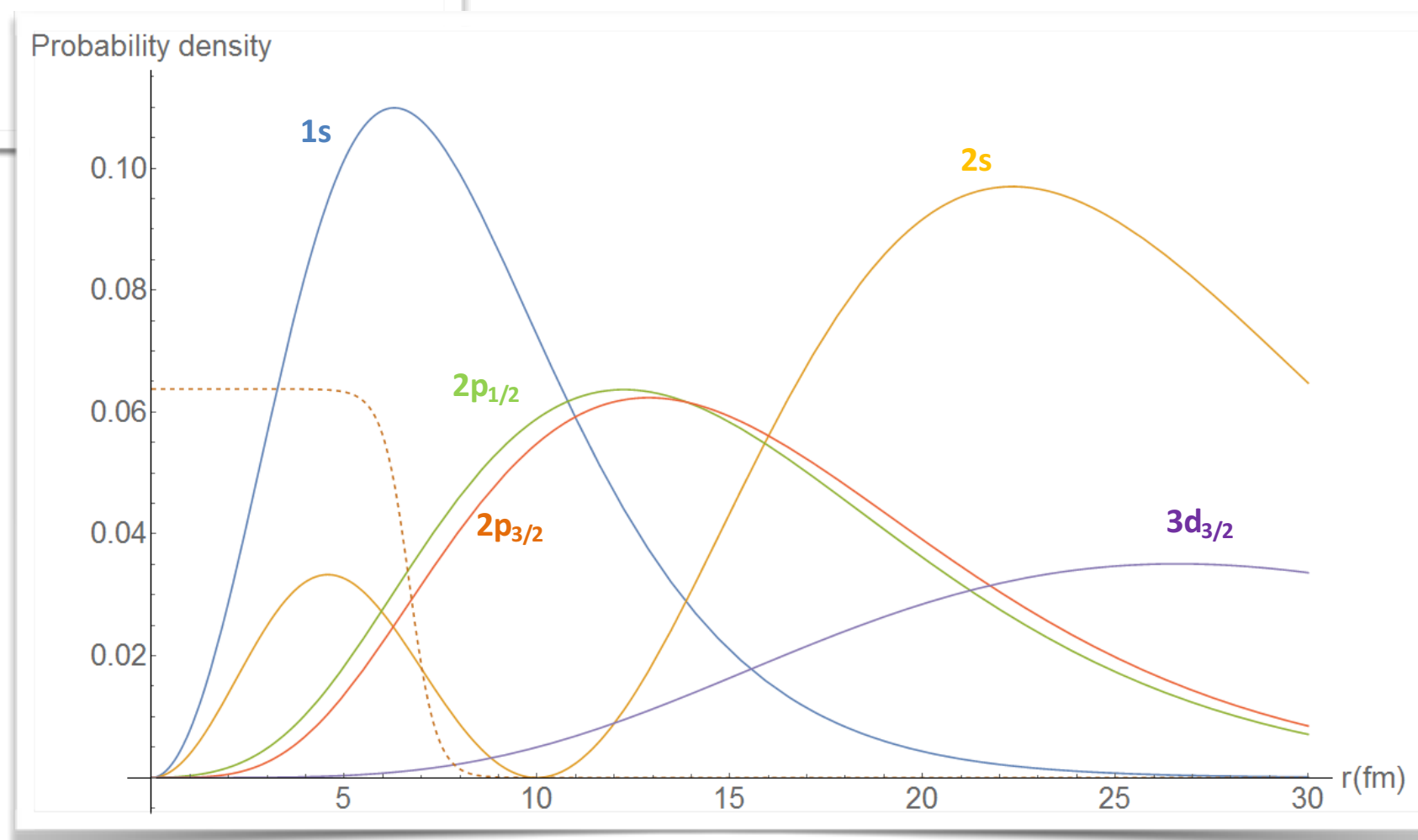
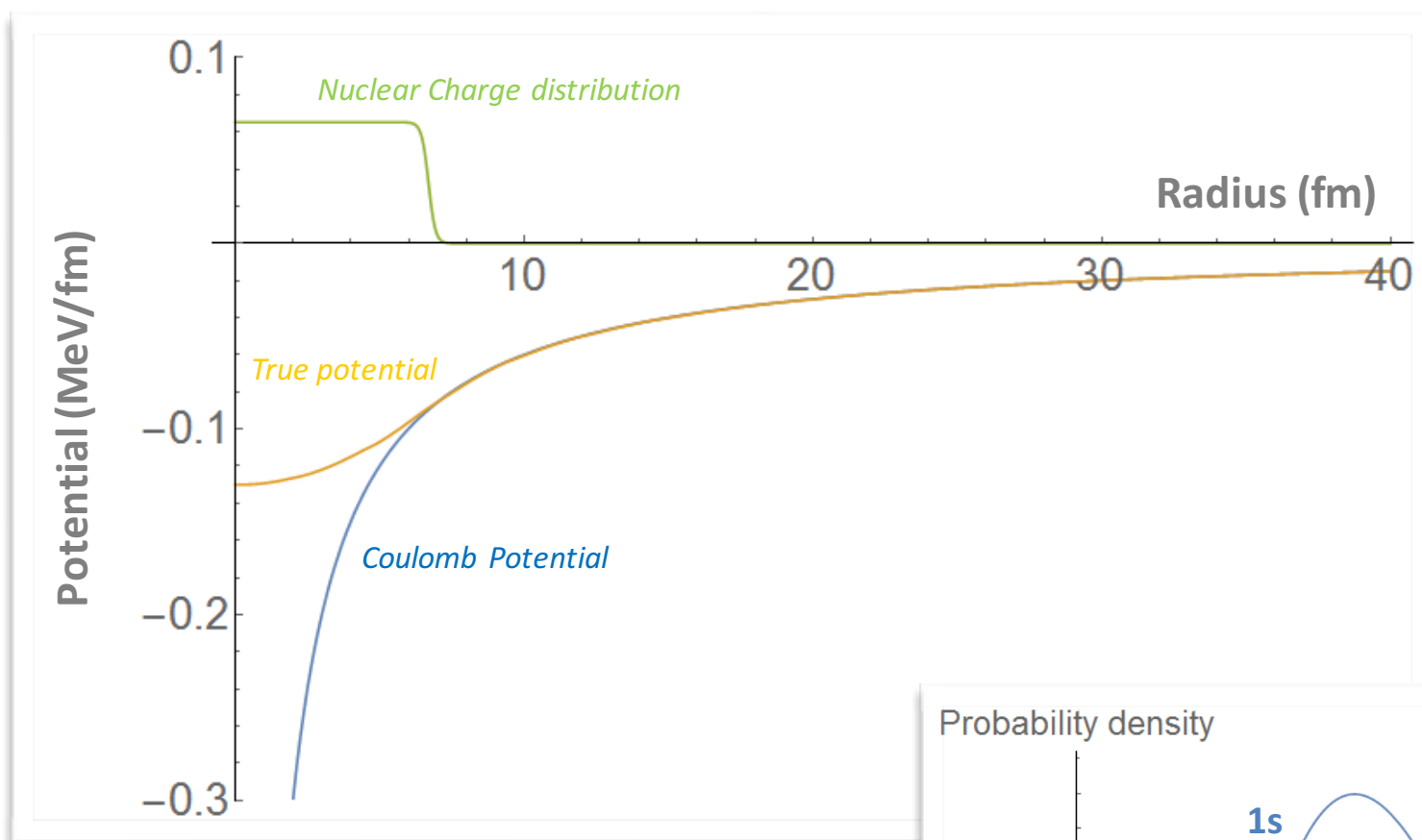
μp , μd , μHe (2S-2P)
high-Z muonic atoms
hyper-fine splitting

X-ray spectroscopy of high-Z muonic atoms



- Negative muons at rest quickly get captured by surrounding atoms
- Cascade down into 1s state emitting characteristic X-rays
- Measure characteristic X-rays to extract information about the nuclear structure

Finite size effect is huge

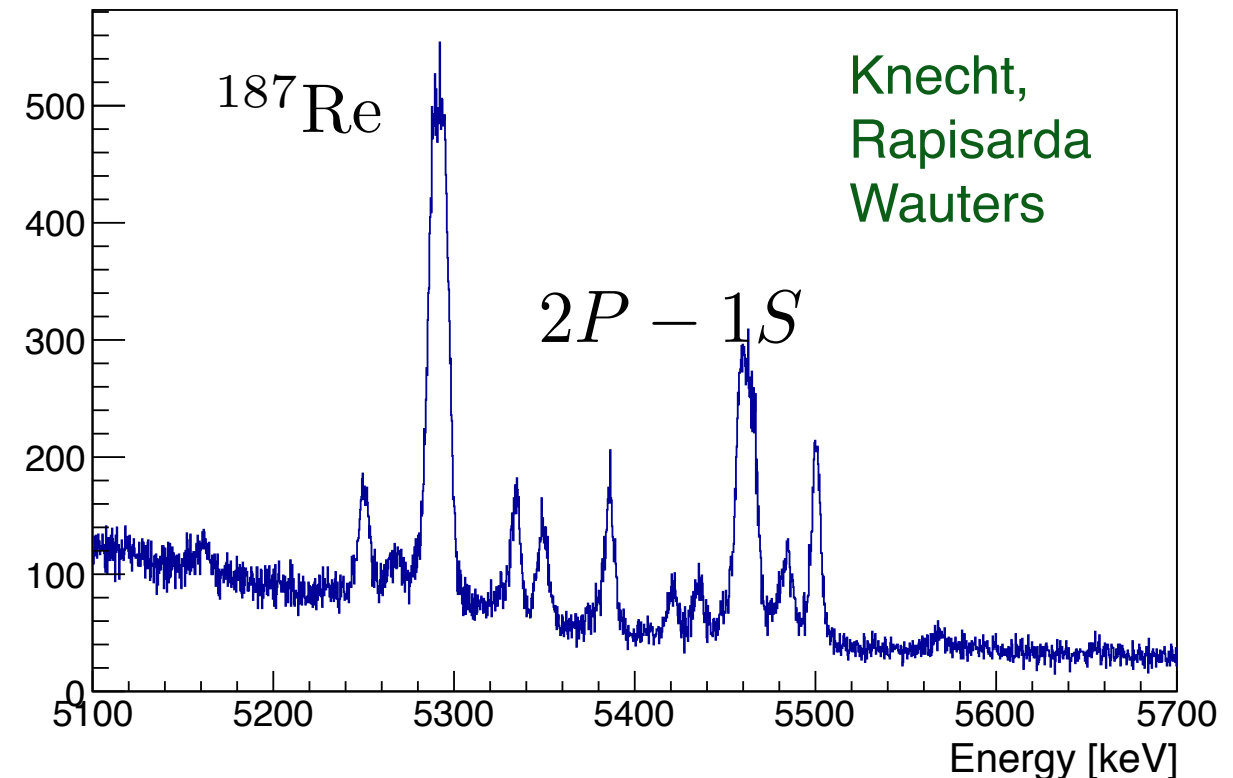


High-Z muonic ions (μZ)

$$E \simeq \frac{m_\mu}{m_e} R_\infty Z^2 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right) + \Delta E_{\text{QED}} - \Delta E_{\text{size}} + \Delta E_{\text{pol}} + \Delta E_{\text{el}}$$

- H-like atoms
- MeV transition energies
- ΔE_{size} : MeV finite-size effects
- ΔE_{QED} : easy QED corrections
- ΔE_{el} : small atomic electron corrections
- ΔE_{pol} : difficult nuclear polarisability correc.

- Measure X-rays with Ge detectors (0.1 keV acc.)
- Extract charge radii and quadrupole moments



Complications

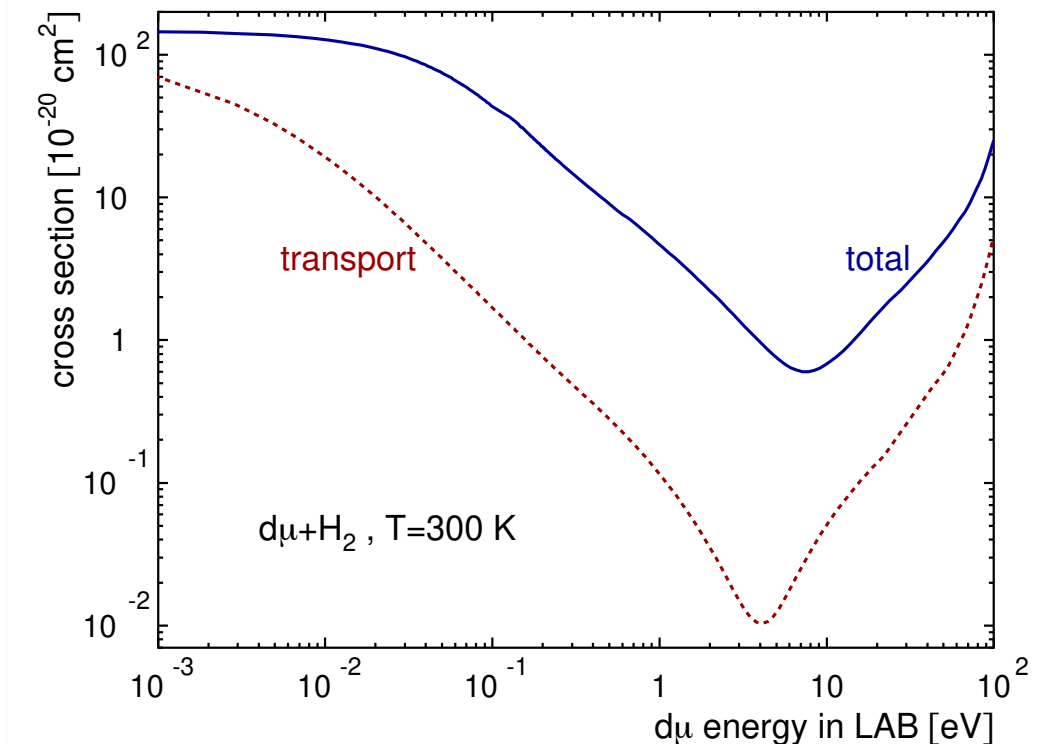
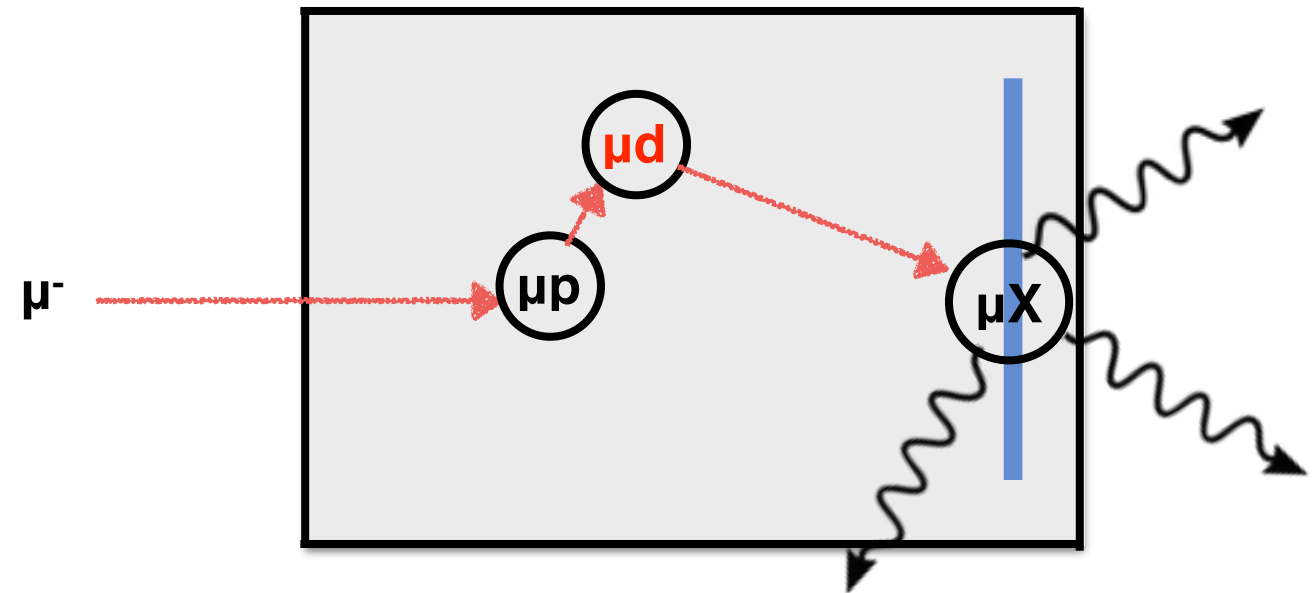
- nuclear polarisability
- nuclear excitation in final state

Natalia Oreshkina & Niklas Michel,
MPI Heidelberg

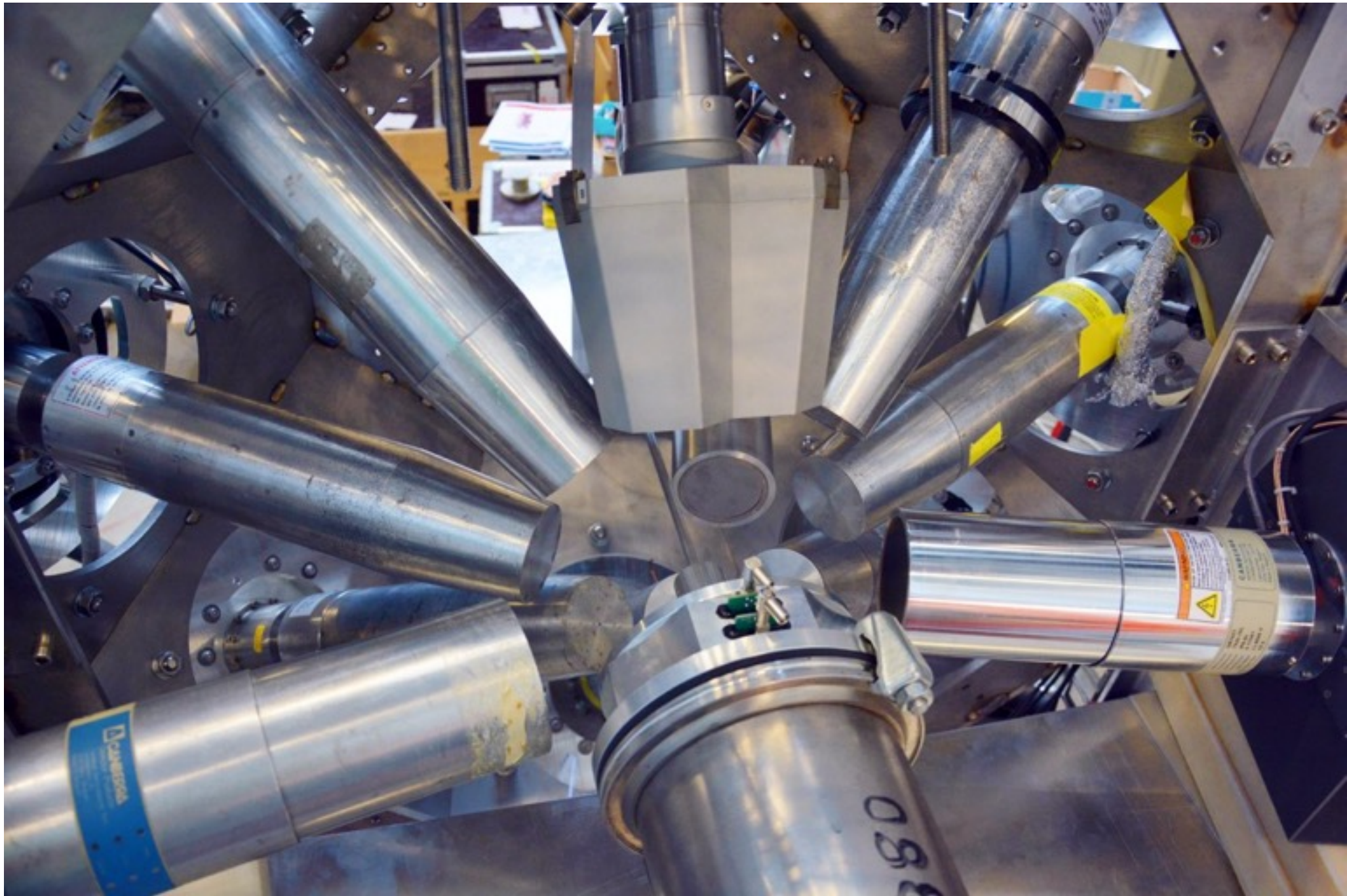
muX principle: spectroscopy for radioactive nuclei

Radioactive \Rightarrow μg material

- Stop muons in 100 bar H_2 target with 0.25% D_2 admixture
- Muonic hydrogen (μp) is formed
- In a collision ($\mu\text{p} + \text{D}_2 \rightarrow \mu\text{d} + \dots$) the muon transfers to deuterium forming μd , with kinetic energy of 45 eV
- Hydrogen gas is quasi transparent for μd at ~ 5 eV (Ramsauer-Townsend effect)
- μd reaches the X target and transfers to it to form μX^*
- μX^* de-excite emitting x-rays
- Measure x-rays with Ge-detectors

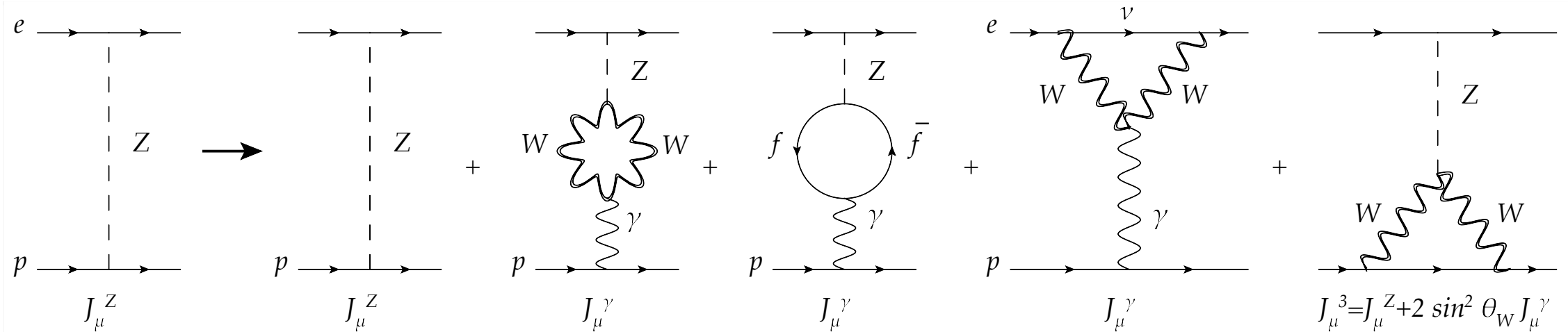


The muX setup



- 11 germanium detectors in an array from French/UK loan pool, Leuven, PSI
- First time a large array is used for muonic atom spectroscopy

Other goal of muX: Running of the Weinberg angle

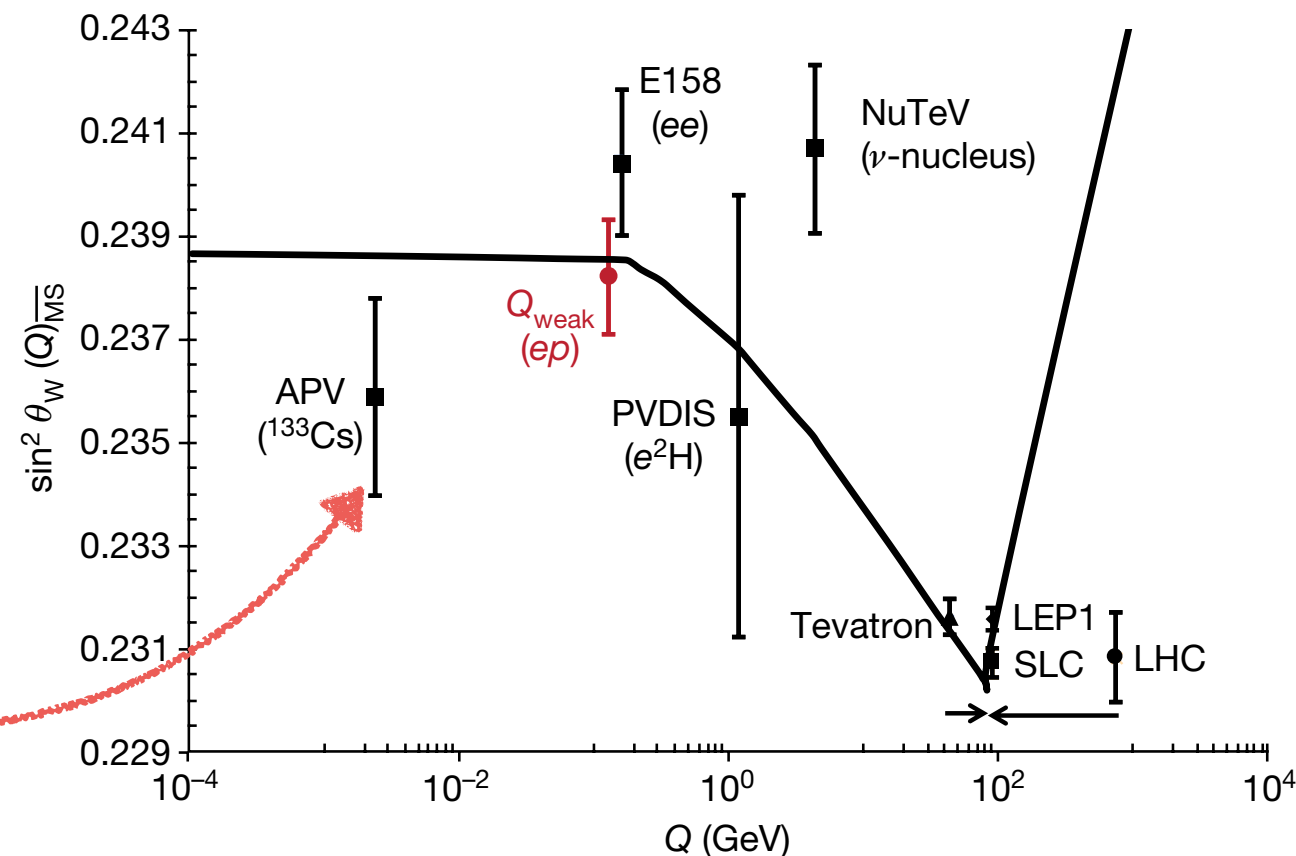


$$J_\mu^Z = J_\mu^3 - 2 \sin^2 \theta_W J_\mu^\gamma$$

Marciano, Czarnecki

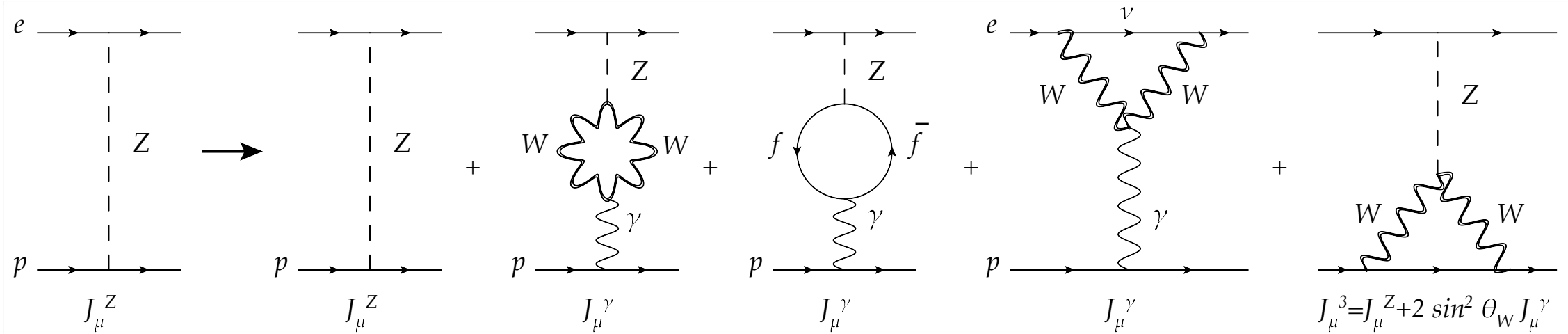
$$= \dots (J_\mu^3 - 2\kappa(Q^2) \sin^2 \theta_W J_\mu^\gamma) \equiv \dots (J_\mu^3 - 2 \sin^2 \theta_W(Q^2) J_\mu^\gamma)$$

APV (Ra)
5x better than
APV(Cs)



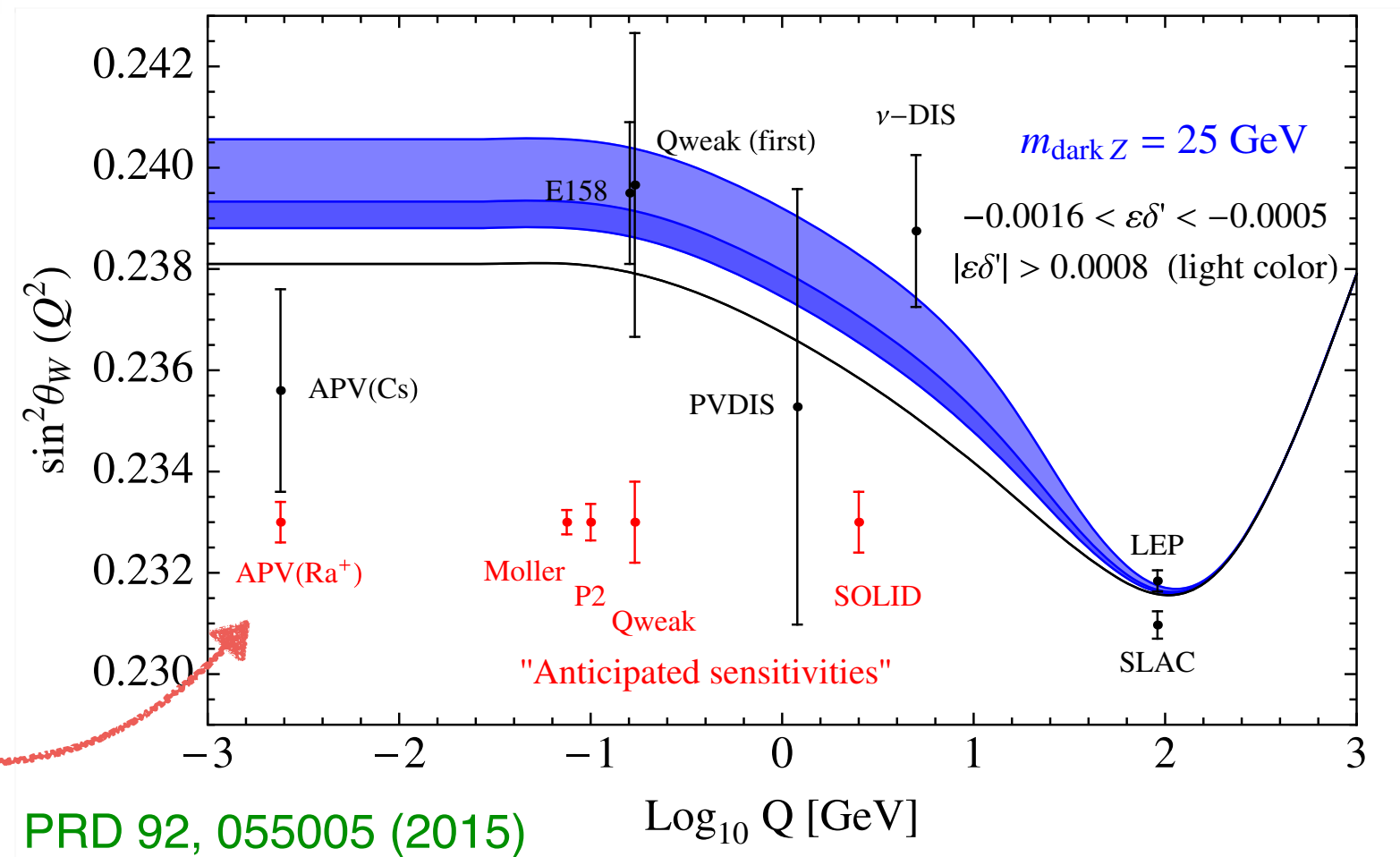
Nature 557, 207(2018)

Running of the Weinberg angle



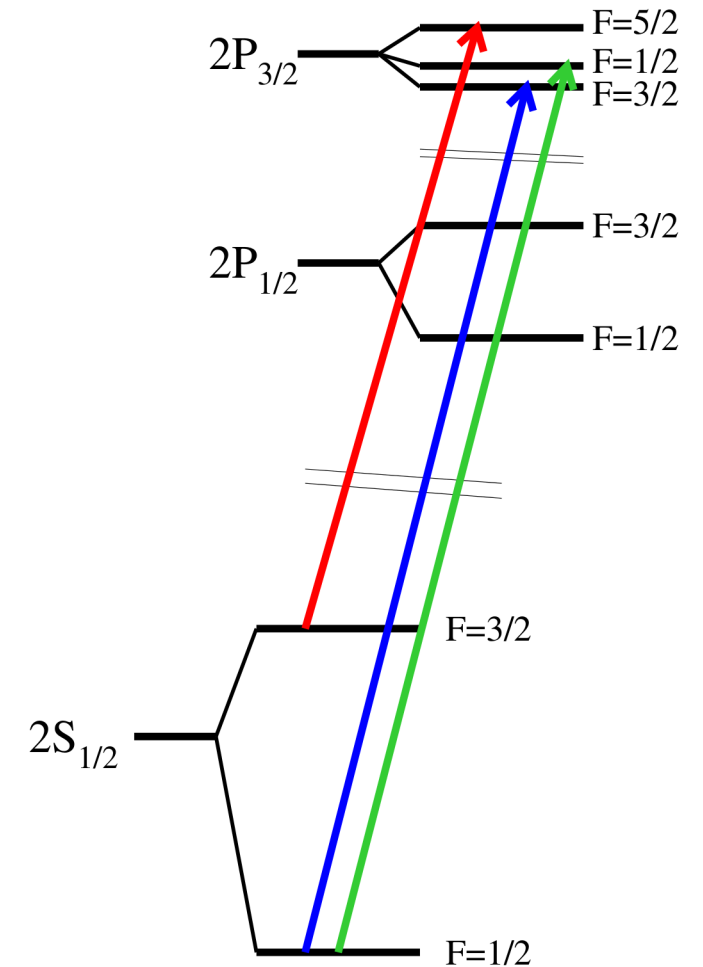
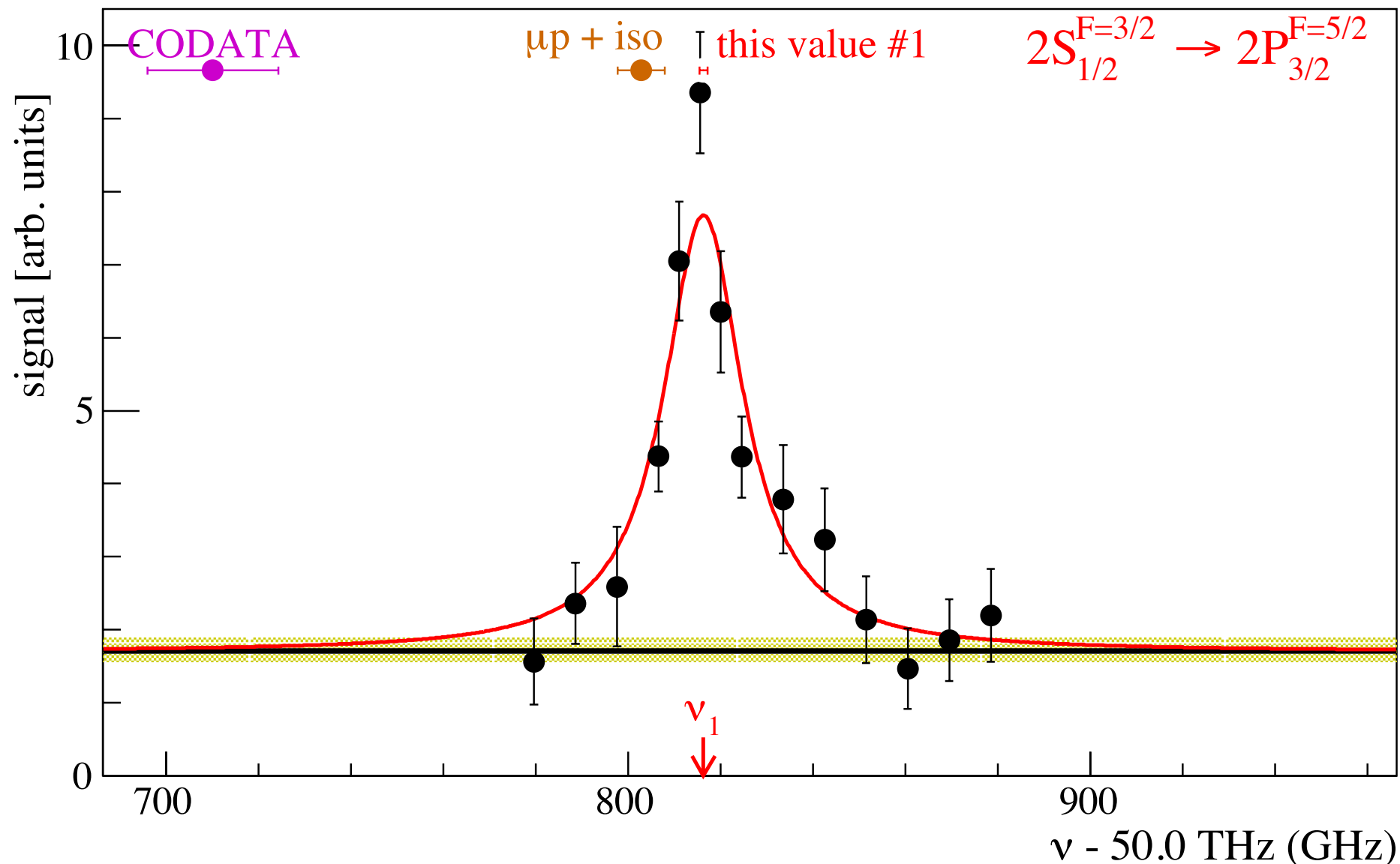
$$J_\mu^Z = J_\mu^3 - 2 \sin^2 \theta_W J_\mu^\gamma$$

$$= \dots (J_\mu^3 - 2 \kappa(Q^2) \sin^2 \theta_W J_\mu^\gamma) \equiv \dots (J_\mu^3 - 2 \sin^2 \theta_W(Q^2) J_\mu^\gamma)$$



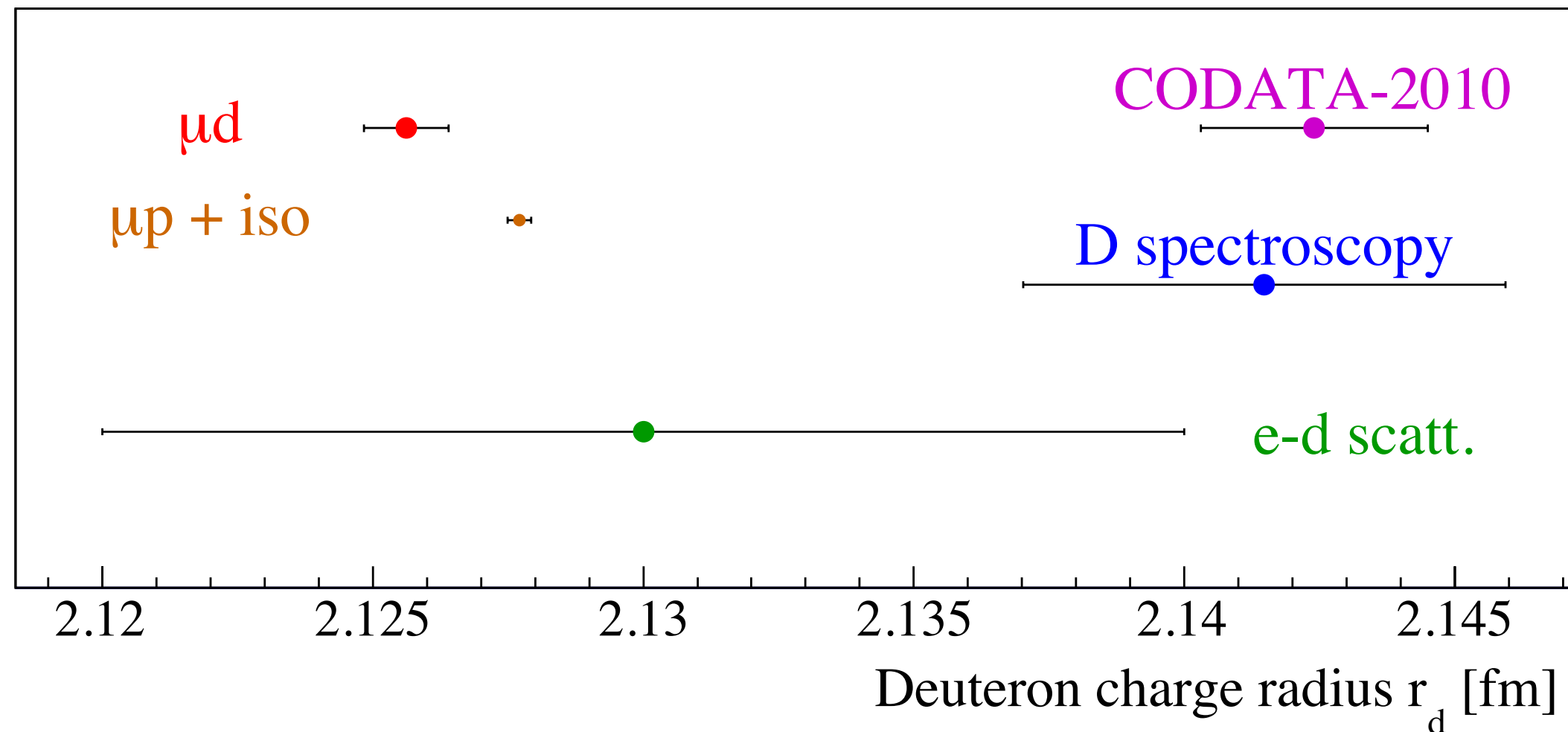
APV (Ra)
5x better than
APV(Cs)

2S-2P spectroscopy of muonic deuterium (μd)



	μp [meV]	μd [meV]	
QED	206	229	$\times 1.1$
$k\langle r^2 \rangle$	4	28	$\times 7$
TPE	0.03	1.7	$\times 56$

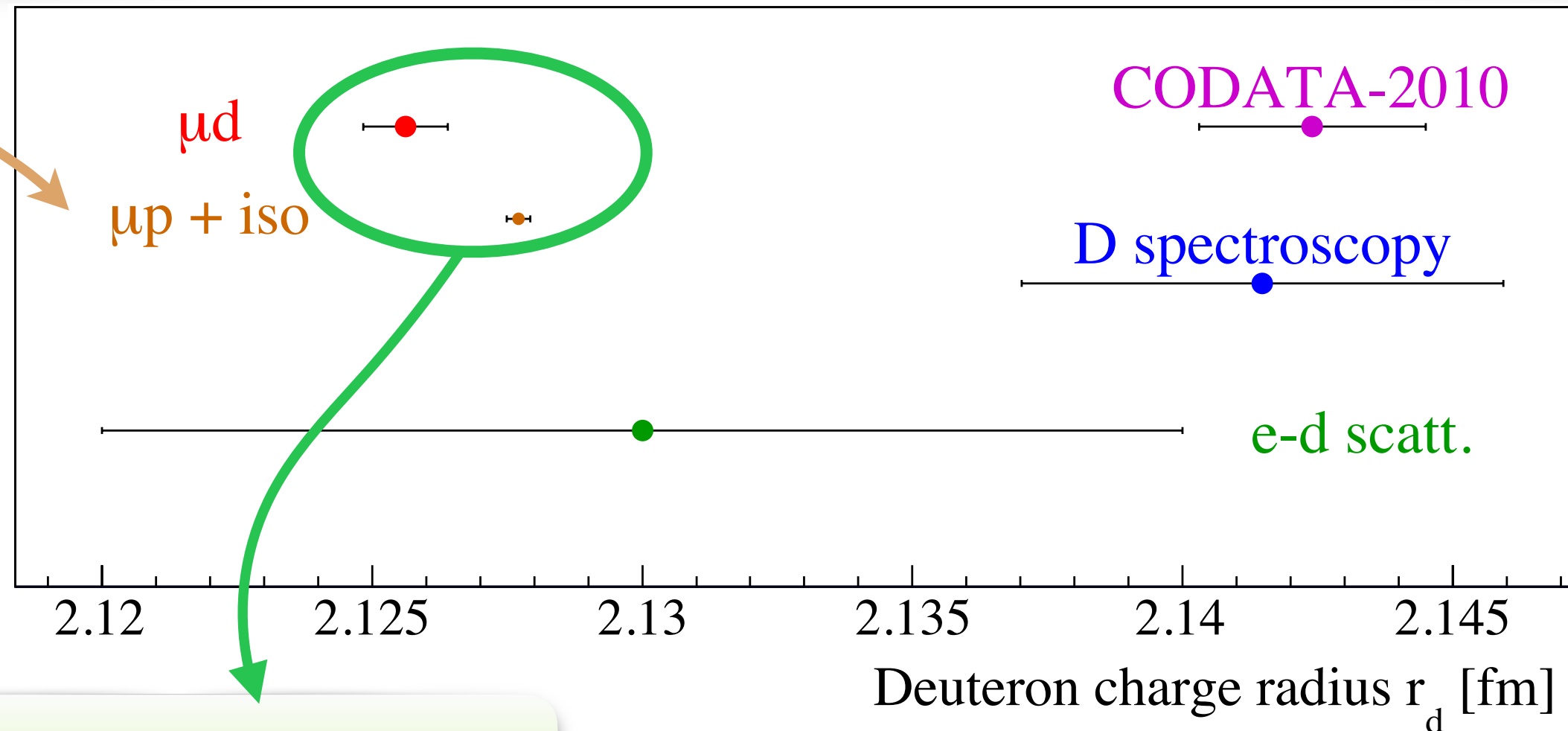
2S-2P spectroscopy of muonic deuterium (μd)



Pohl et al., Science 353, 669 (2016)
Krauth et al., Ann. Phys. 336 168 (2016)
Hernandez et. al., PLB 736, 344 (2014)
Pachucki et al., PRA 91, 040503(R) (2015)

2S-2P spectroscopy of muonic deuterium (μd)

$$\left. \begin{array}{l} \text{H/D shift: } r_d^2 - r_p^2 = 3.820\,07(65) \text{ fm}^2 \\ \mu p : \quad r_p = 0.84087(39) \text{ fm} \end{array} \right\} \Rightarrow r_d = 2.12771(22) \text{ fm}$$



Consistency of muonic results
with 1S-2S H/D isotopic-shift

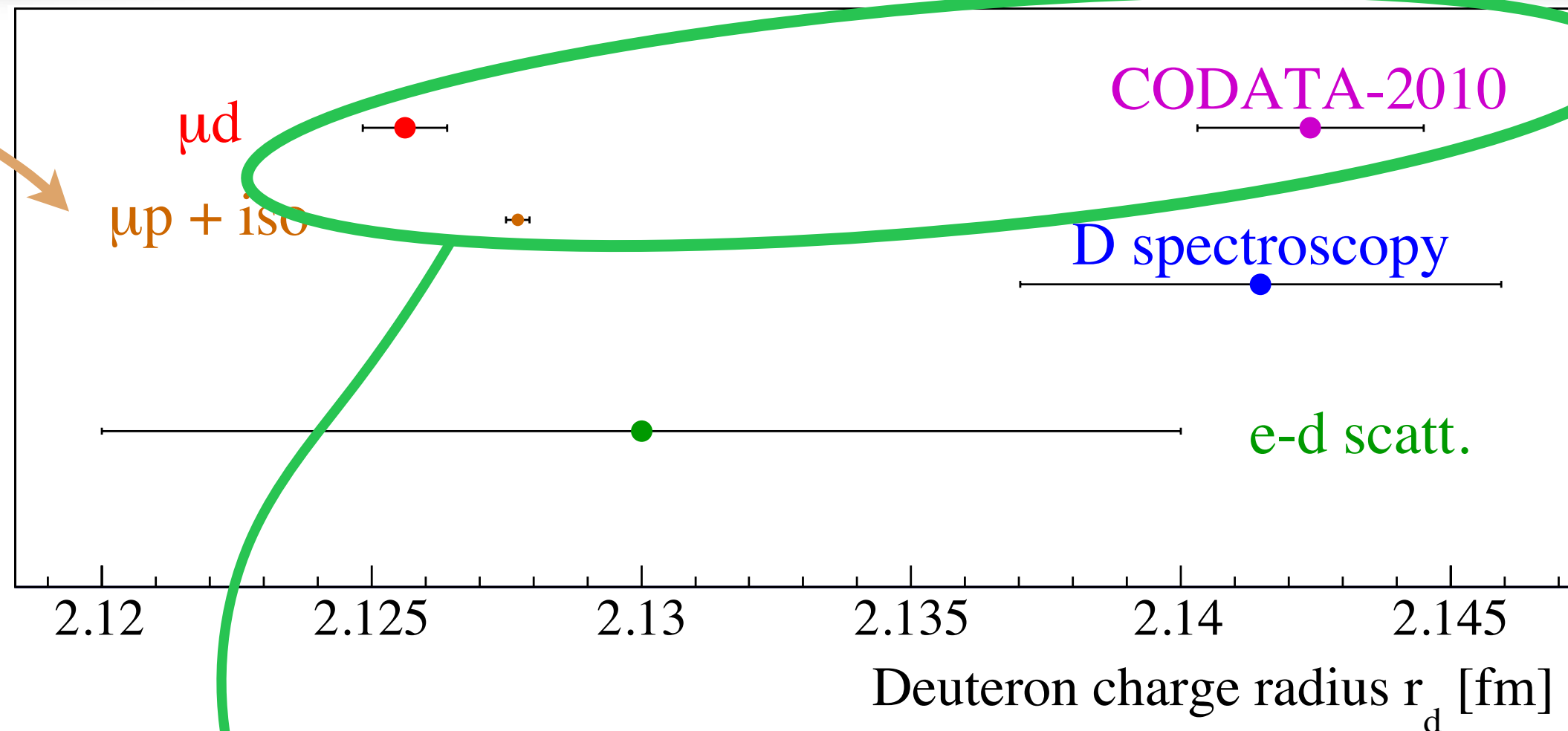
The 2.5σ difference:

- incomplete nuclear polarizability?
- BSM physics NOT coupling to n (reduced mass effect)?

Pachucki, Bacca, Barnea,
Gorchtein, Carlson....

2S-2P spectroscopy of muonic deuterium (μd)

$$\left. \begin{array}{l} \text{H/D shift: } r_d^2 - r_p^2 = 3.820\,07(65) \text{ fm}^2 \\ \mu p : \quad r_p = 0.84087(39) \text{ fm} \end{array} \right\} \Rightarrow r_d = 2.12771(22) \text{ fm}$$

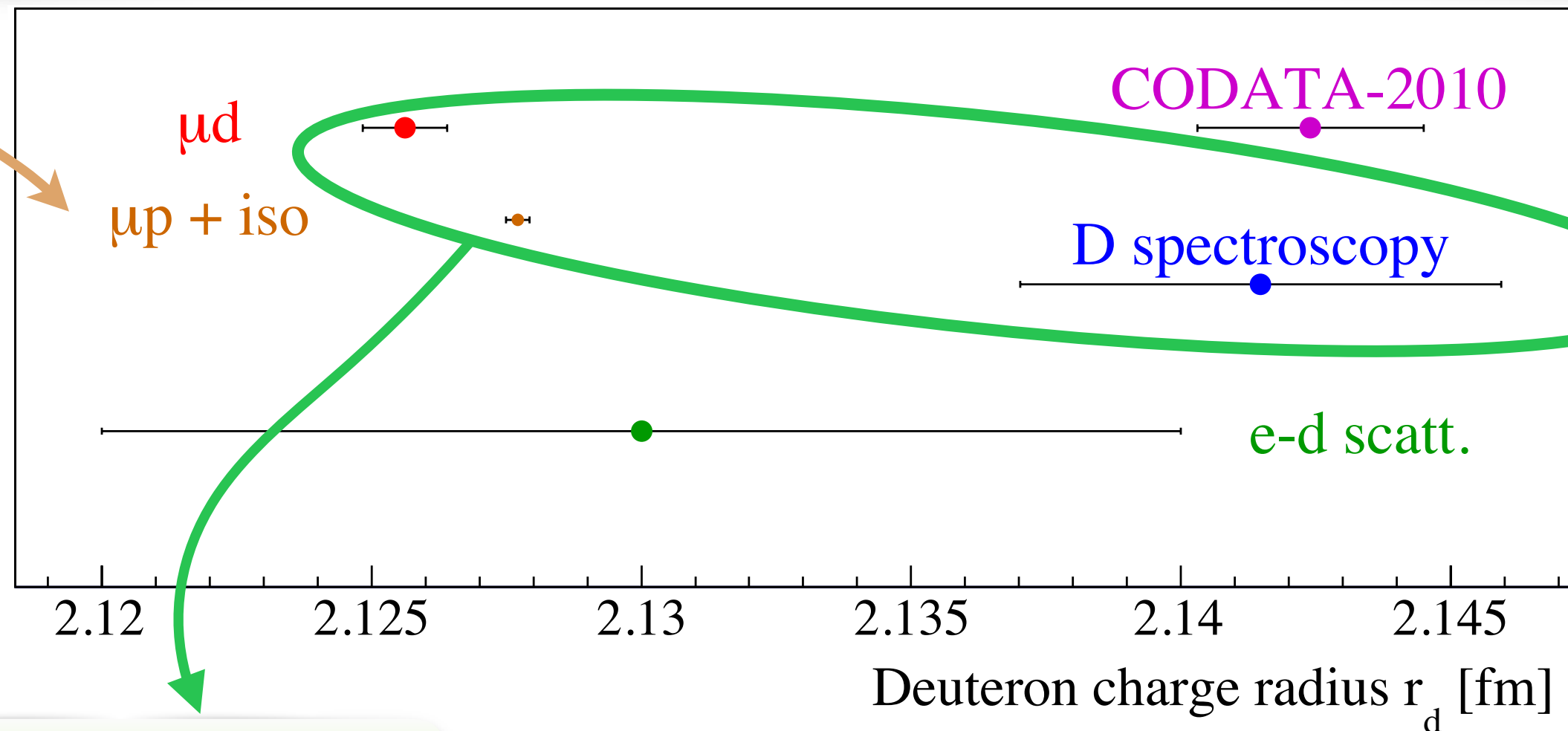


7σ from CODATA

BUT CODATA
contains proton-data

2S-2P spectroscopy of muonic deuterium (μd)

$$\left. \begin{array}{l} \text{H/D shift: } r_d^2 - r_p^2 = 3.820\,07(65) \text{ fm}^2 \\ \mu p : \quad r_p = 0.84087(39) \text{ fm} \end{array} \right\} \Rightarrow r_d = 2.12771(22) \text{ fm}$$



3.5 σ from ONLY D-data

\Rightarrow double discrepancy

- proton sector
- deuteron sector

\Rightarrow Problem with H/D exp (R_∞)?

\Rightarrow Problem with H/D th.?

\Rightarrow BSM with no coupling to n?