

# Loop Effects solutions to B anomalies

M. Fedele

based on [arXiv:1904.058xx](#) in collaboration with:

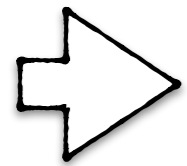
P. Arnan, A. Crivellin & F. Mescia



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BARCELONA

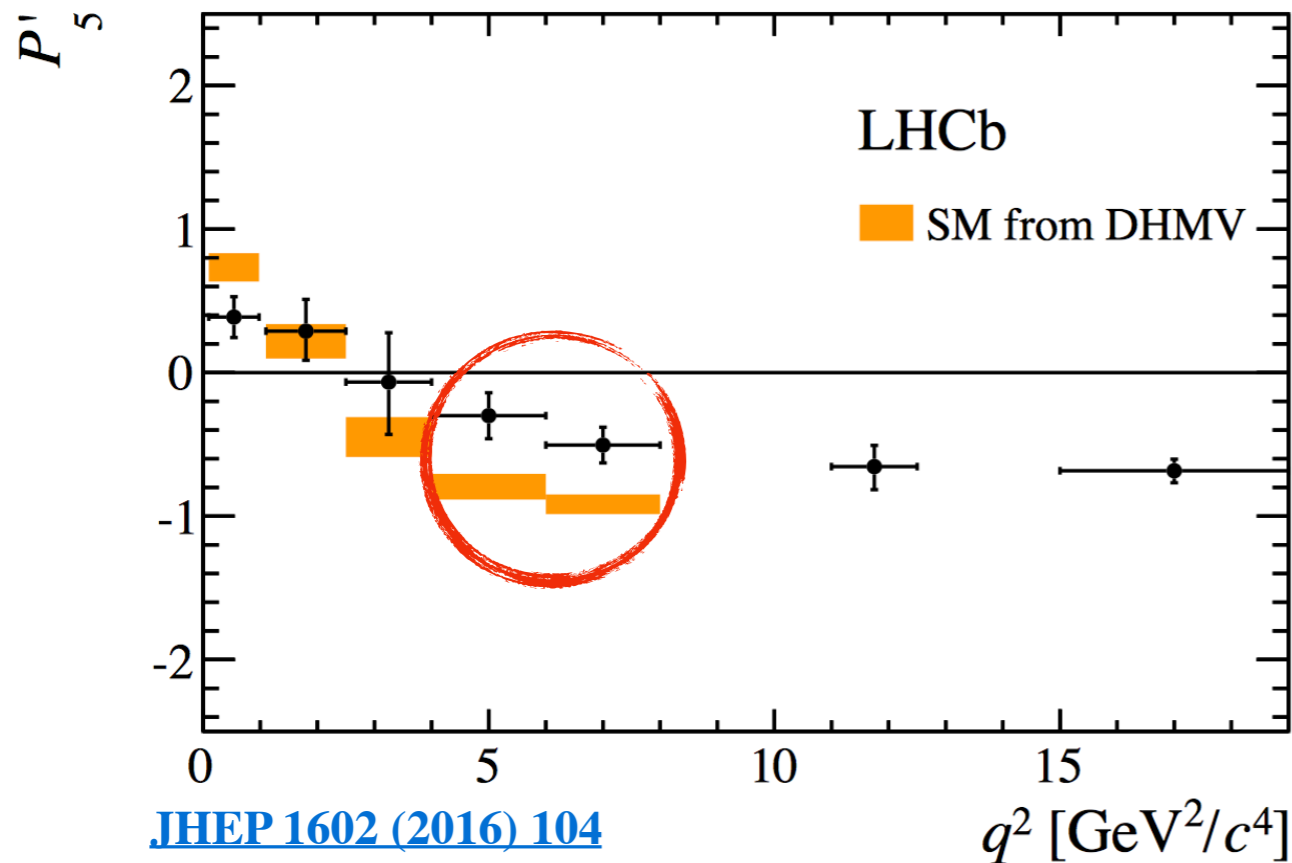
# Opportunities with Semi-Leptonic B Decays

No tree-level flavour changing neutral currents (FCNC) in the SM



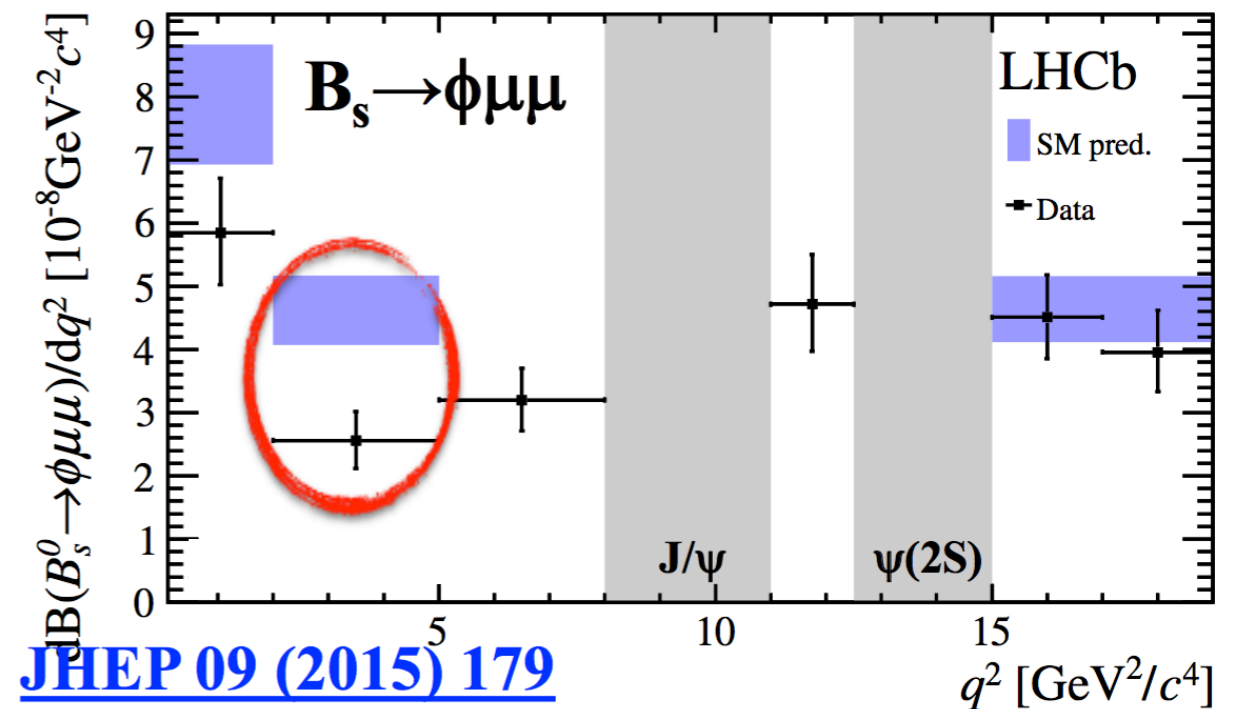
New Physics (NP) may sizably contribute in FCNC amplitudes

Intriguing set of “Anomalies” in data of exclusive B rare Decays



$\sim 3.5 \sigma$

Angular analysis of  $B \rightarrow K^* \mu \mu$  for small dilepton mass,  $4 < q^2 / \text{GeV}^2 < 8$ .

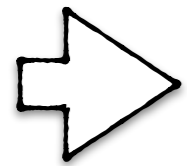


$\sim 2.5 \sigma$

$Br$  of  $B_s \rightarrow \phi \mu \mu$

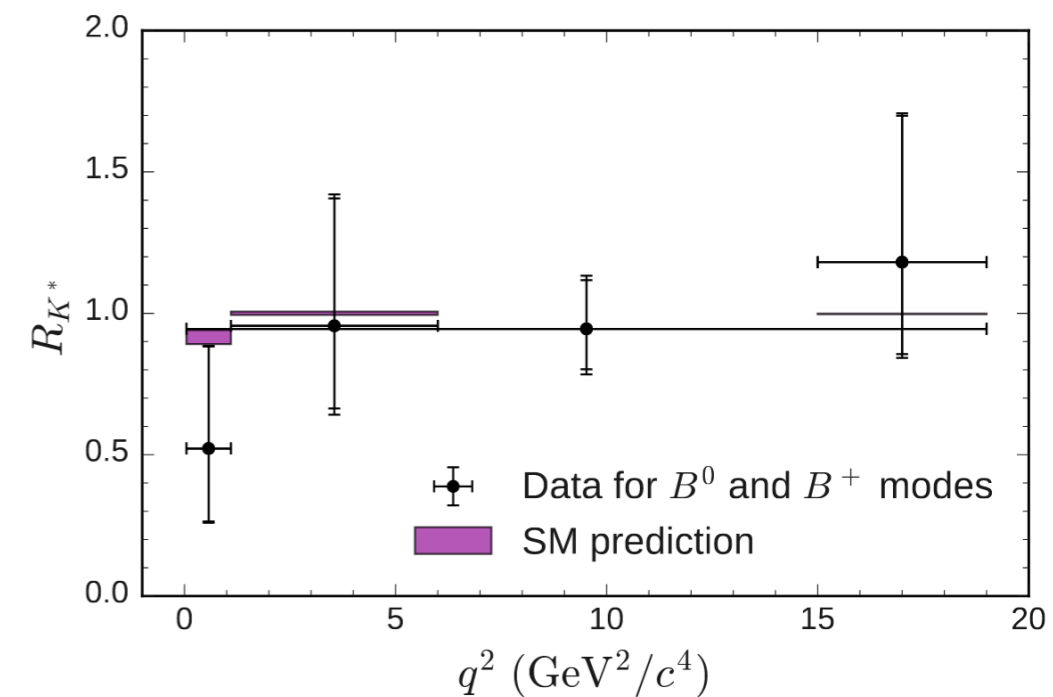
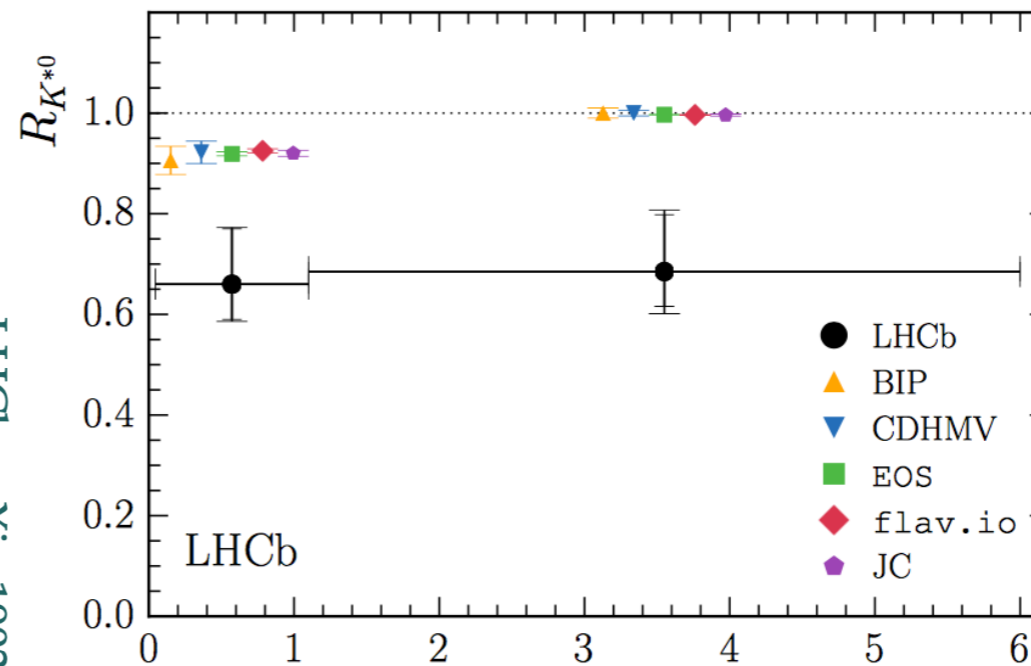
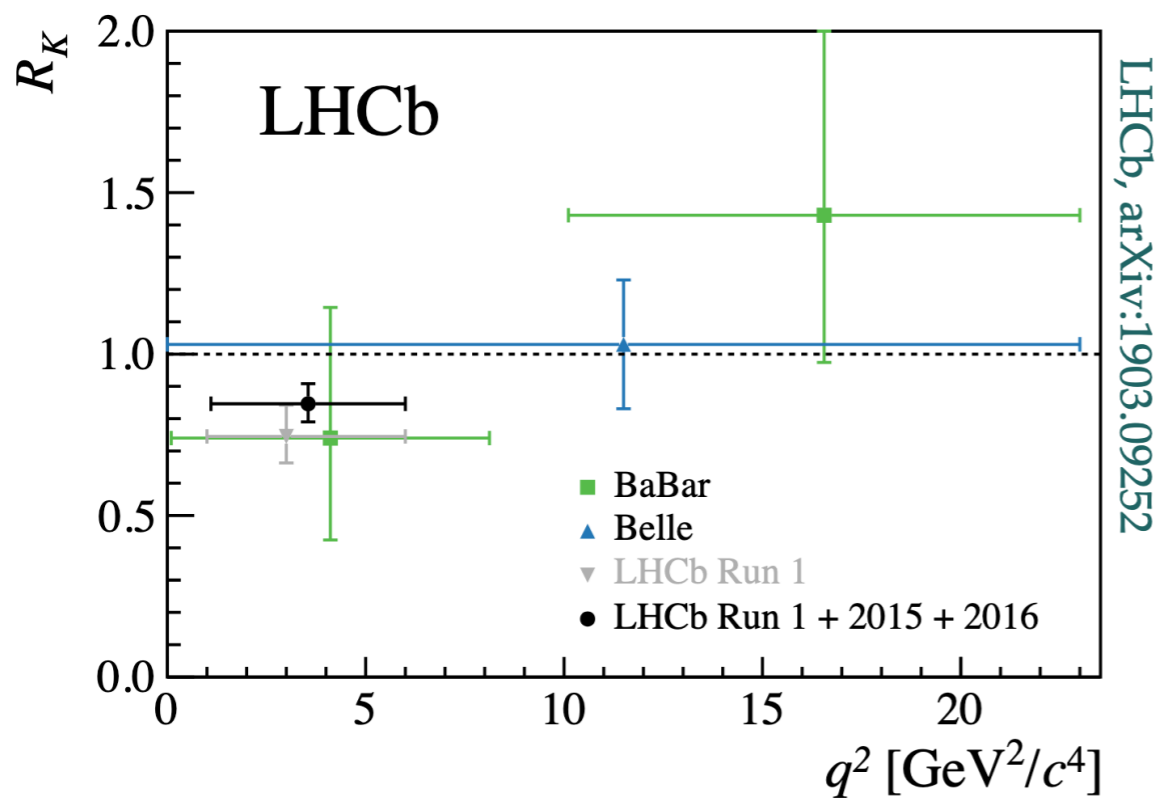
# Opportunities with Semi-Leptonic B Decays

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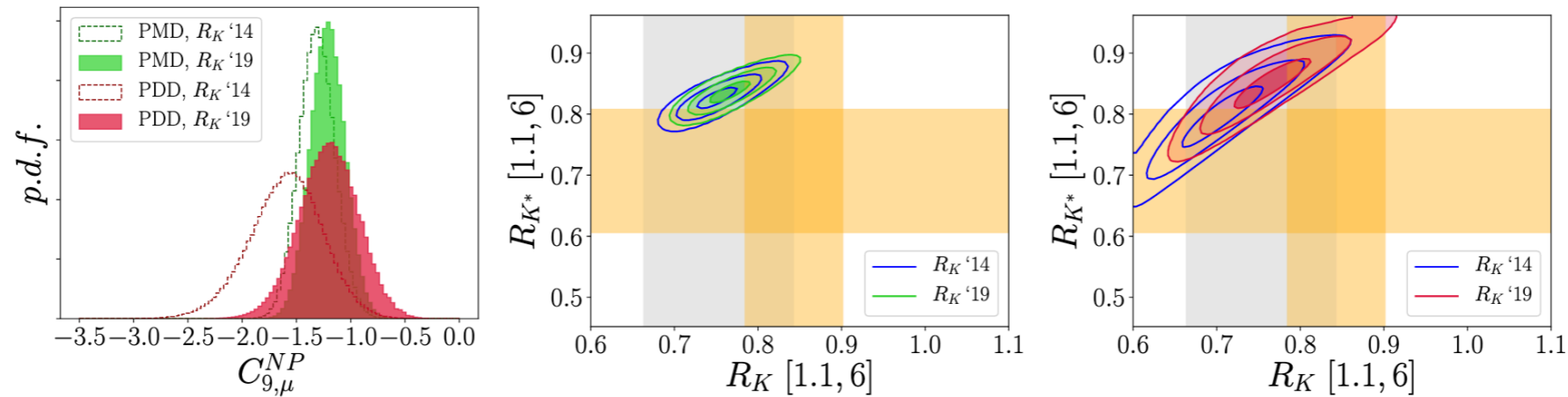
$$R_{K^{(*)}} = Br(B \rightarrow K^{(*)} ee) / Br(B \rightarrow K^{(*)} \mu\mu)$$

# Global fits after Moriond 2019

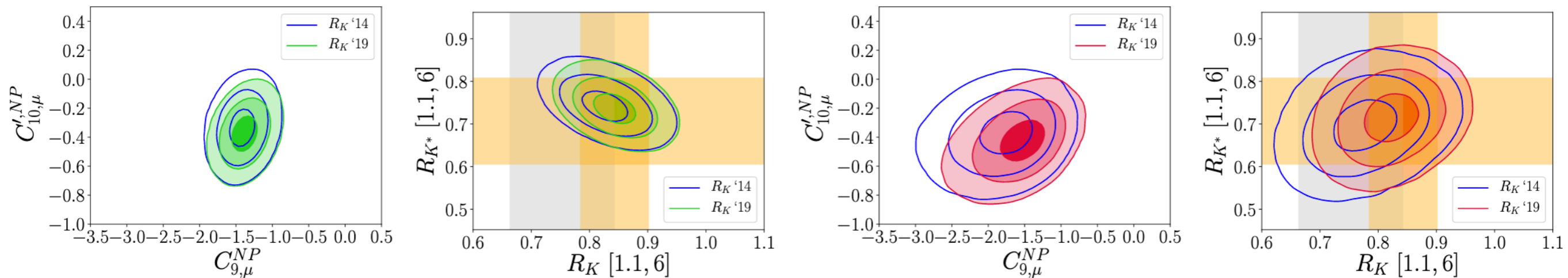
Purely left-handed solutions are no longer preferred by data:

[Ciuchini, Coutinho, MF, Franco, Paul, Silvestrini, Valli \(1903.09632\)](#)

LH:



LH + RH:

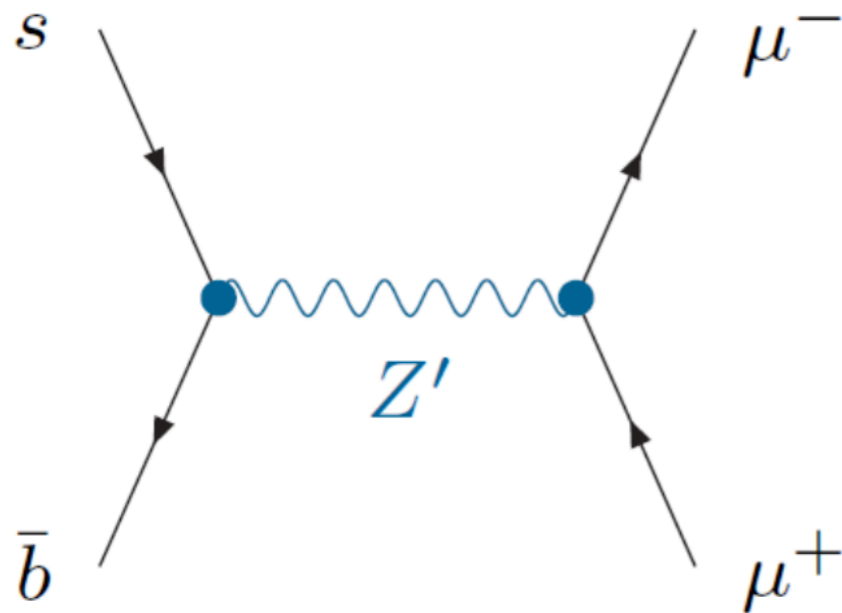


The inclusion of right-handed currents better reproduce data!

Similar findings by Algueró et al., Alok et al., Aebischer et al., Kowalska et al.

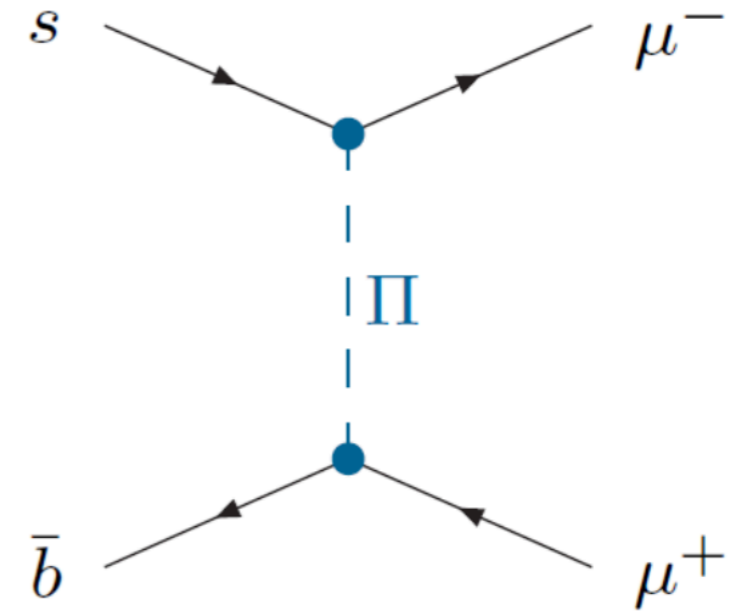
# Tree-Level Models

Many possible solutions investigated so far involve tree-level NP



***Z' models***

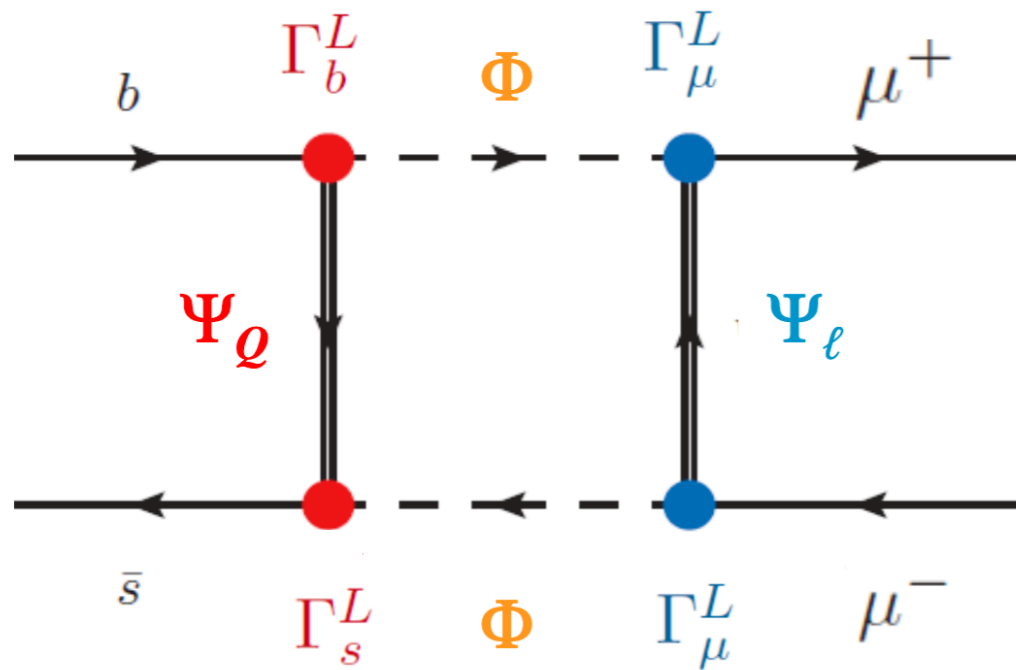
Allanach, Bordone, Buras, Crivellin, D'Ambrosio, De Fazio, Di Luzio, Falkowski, Fuentes-Martin, Gori, Isidori, Nierste, Vicente, ...



***Lepto-Quarks***

Becirevic, Bordone, Crivellin, Di Luzio, Fajfer, Faroughy, Isidori, Kosnik, Marzocca, Sumensari, ...

# Loop Models

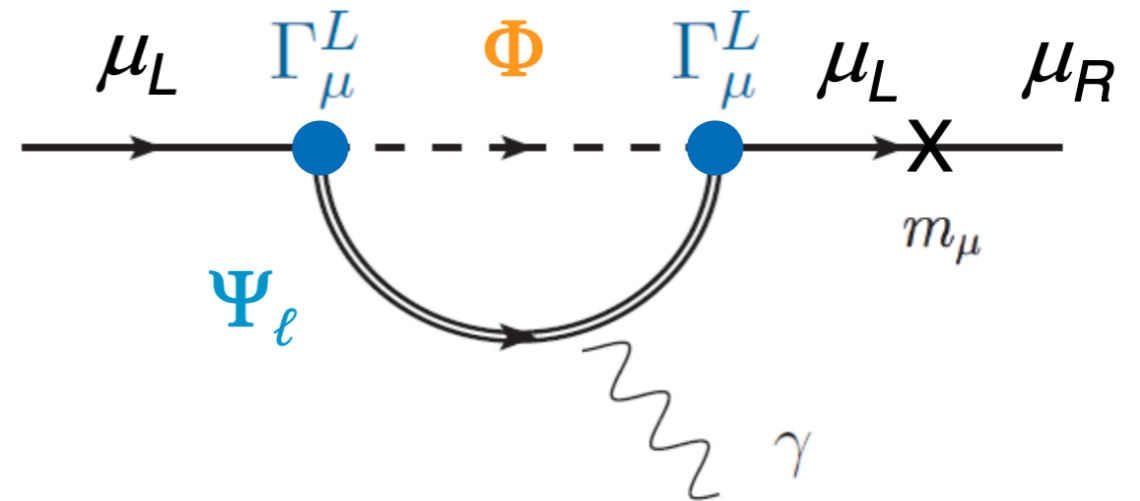
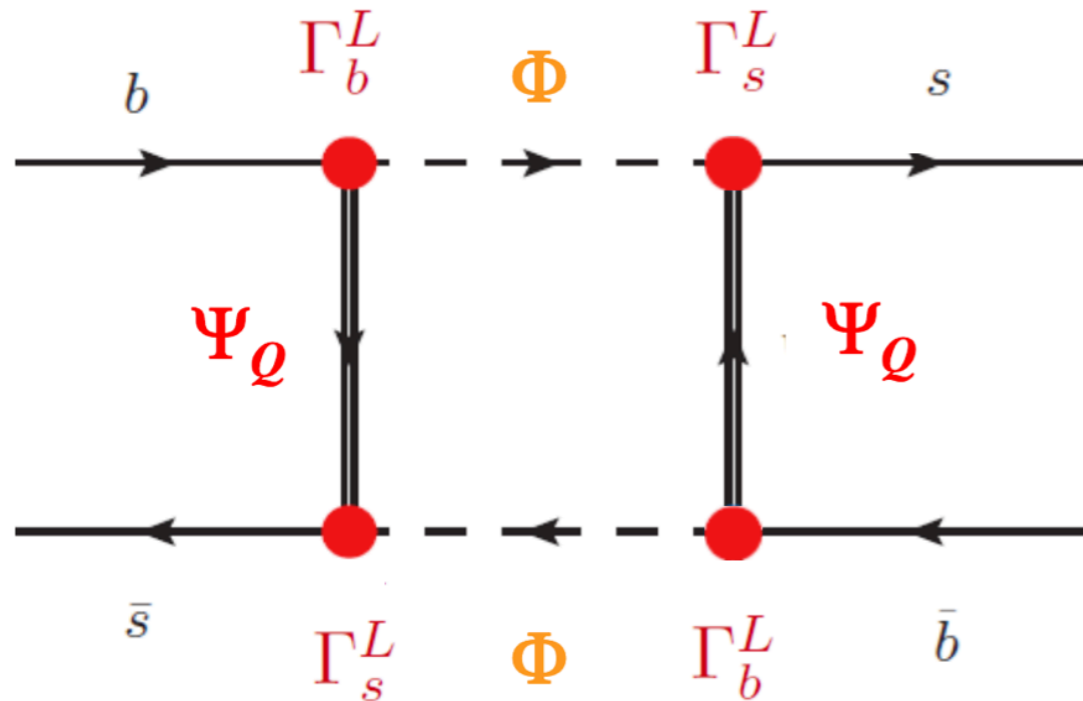


One scalar and 2 vector-like fermions (or vice versa)

$$\Rightarrow \boxed{C9 = -C10}$$

Gripaios, Nardecchia, Renner '15  
 Arnan, Crivellin, Hofer, Mescia '16

Induces contributions to  $\Delta M_s$  and muon  $g-2$



It is not possible to address everything with  $O(1)$  couplings and viable masses

# Our Generic Loop Model

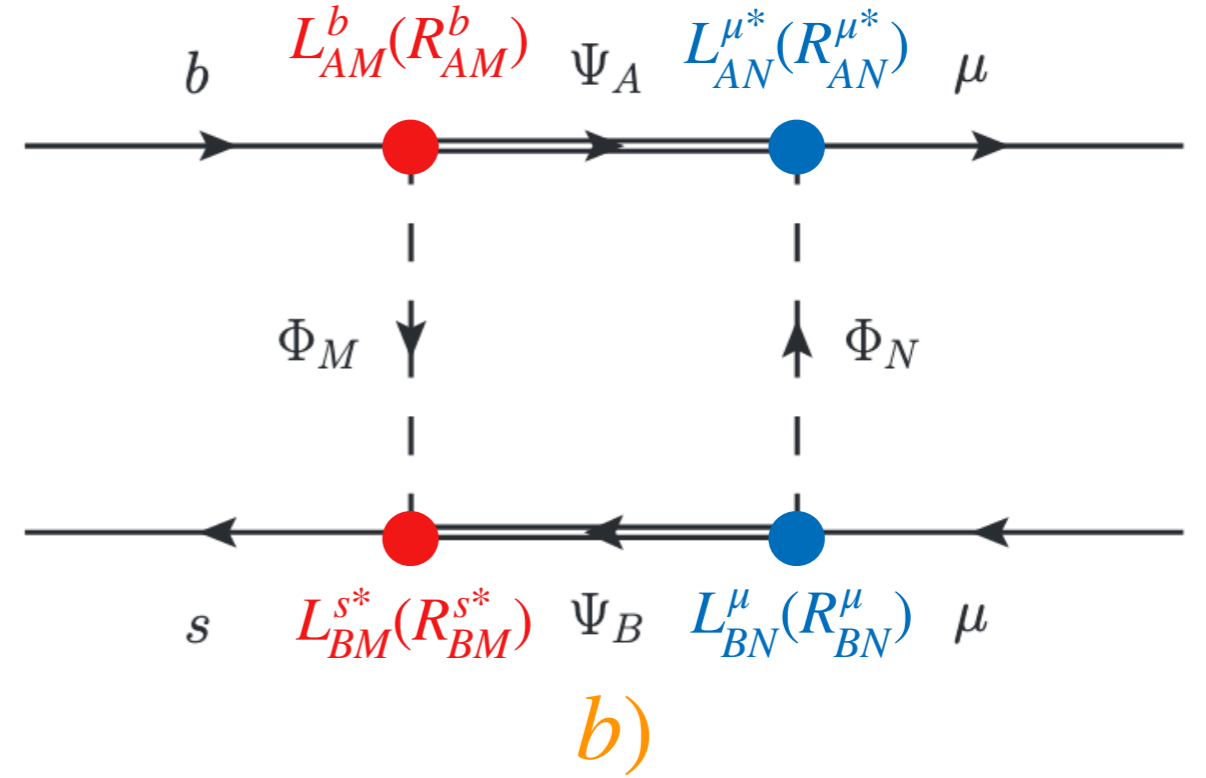
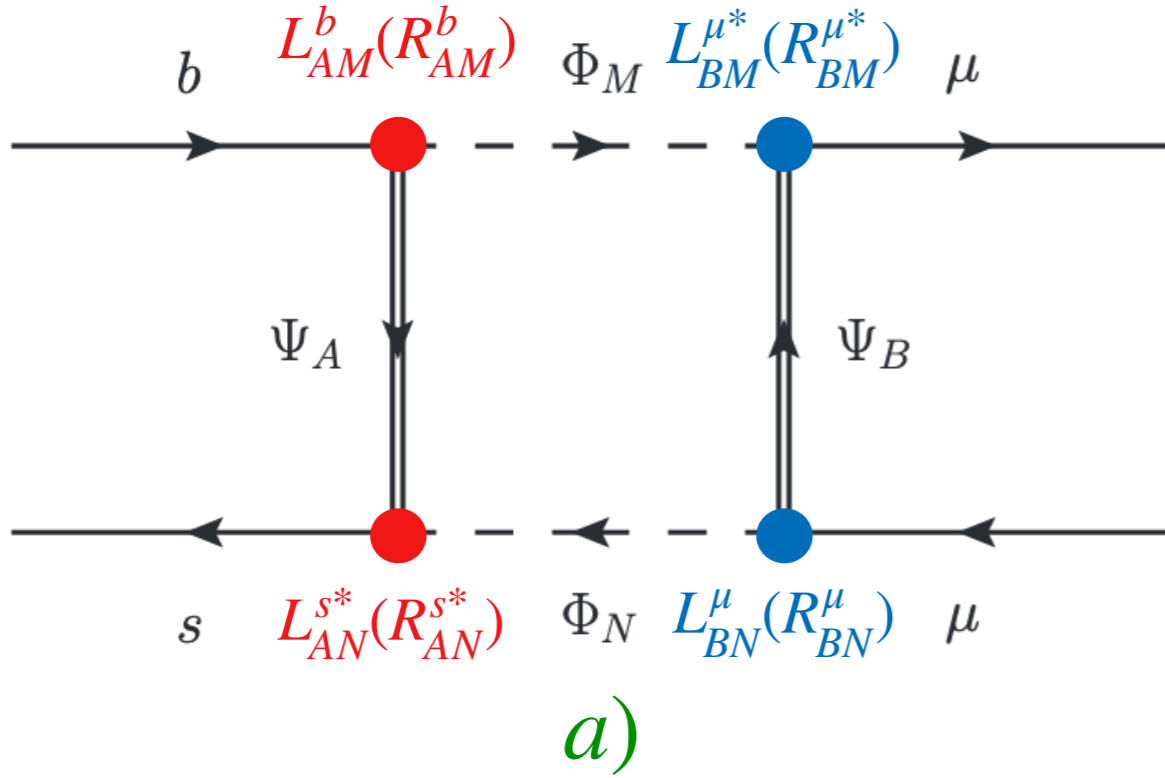
$$\mathcal{L}_{\text{int}} = \left[ \bar{\Psi}_A \left( L_{AM}^b P_L b + L_{AM}^s P_L s + L_{AM}^\mu P_L \mu \right) \Phi_M + \bar{\Psi}_A \left( R_{AM}^b P_R b + R_{AM}^s P_R s + R_{AM}^\mu P_R \mu \right) \Phi_M \right] + \text{h.c.}$$

$\Psi_A, \Phi_M$  : Generic lists containing an arbitrary number of fields

$L_{AM}^{b,s,\mu}, R_{AM}^{b,s,\mu}$  : Generic matrices in (A-M) space

- A and M also include implicitly SU(3) and SU(2) indices
- Non-vanishing entries of the coupling matrices ensure the preservation of colour and electric charge

# $b \rightarrow s \mu \mu$



Two distinct solutions, whether the fermion or the scalar is the NP field that couples to both quarks and leptons

$$C_9^{\text{box}, a) = -\mathcal{N} \frac{\chi L_{AN}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} [L_{BM}^{\mu*} L_{BN}^{\mu} + R_{BM}^{\mu*} R_{BN}^{\mu}] F(x_{AM}, x_{BM}, x_{NM})$$

$$C_{10}^{\text{box}, a) = \mathcal{N} \frac{\chi L_{AN}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} [L_{BM}^{\mu*} L_{BN}^{\mu} - R_{BM}^{\mu*} R_{BN}^{\mu}] F(x_{AM}, x_{BM}, x_{NM})$$

$$x_{AM} \equiv (m_{\Psi_A}/m_{\Phi_M})^2$$

$$C_{9(10)}^{\text{box}} = \pm C_{9(10)}^{\text{box}} (L \leftrightarrow R)$$

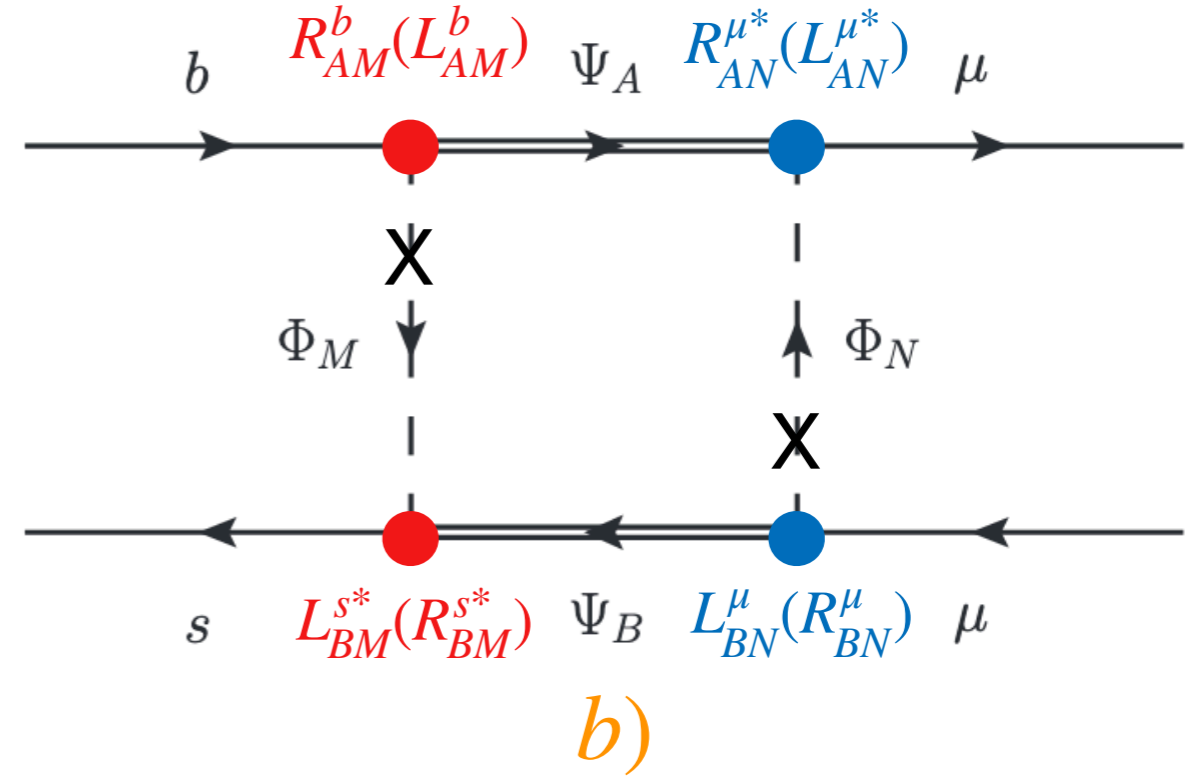
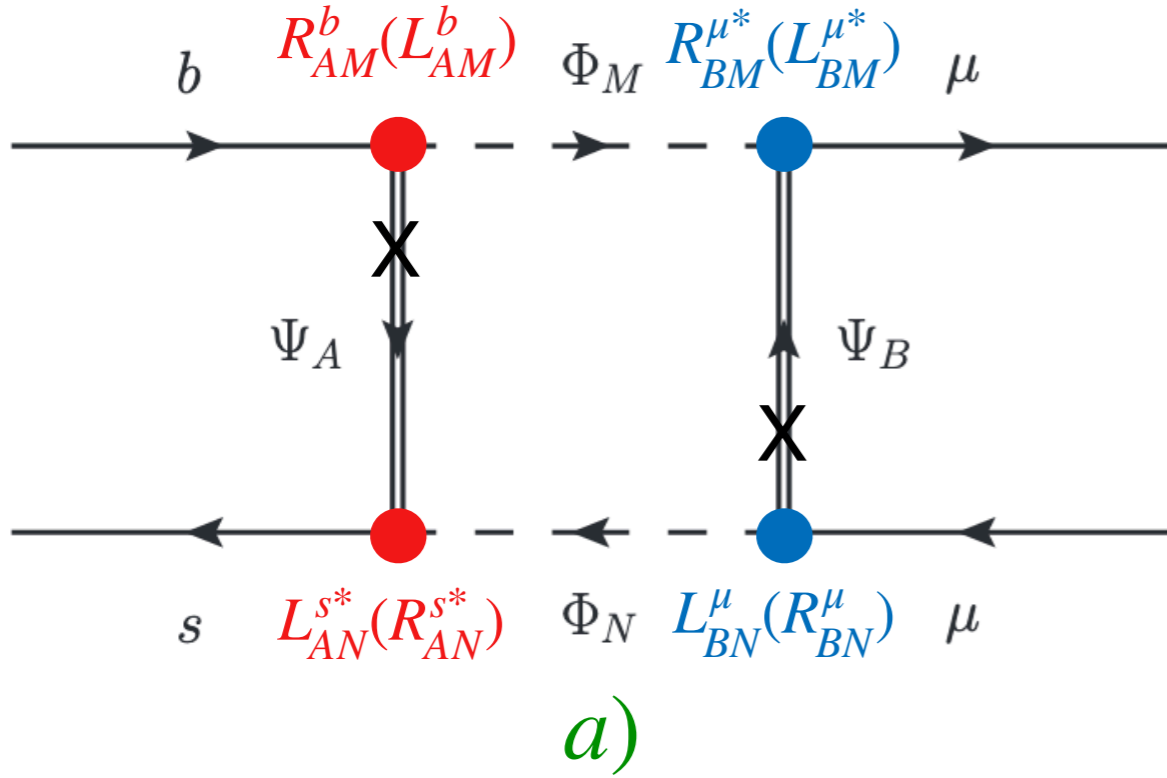
$$x_{NM} \equiv (m_{\Phi_N}/m_{\Phi_M})^2$$

$$C_9^{\text{box}, b) = -\mathcal{N} \frac{\chi L_{BM}^{s*} L_{AM}^b}{32\pi\alpha_{\text{EM}} m_{\Phi_M}^2} \left[ L_{AN}^{\mu*} L_{BN}^{\mu} F(x_{AM}, x_{BM}, x_{NM}) - R_{AN}^{\mu*} R_{BN}^{\mu} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

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# $b \rightarrow s\mu\mu$



$$C_S^{\text{box}, a) = -\mathcal{N} \frac{\chi L_{AN}^{s*} R_{AM}^b}{16\pi\alpha_{\text{EM}} m_{\Phi_M}^2} [R_{BM}^{\mu*} L_{BN}^{\mu} + L_{BM}^{\mu*} R_{BN}^{\mu}] \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM})$$

$$C_P^{\text{box}, a) = \mathcal{N} \frac{\chi L_{AN}^{s*} R_{AM}^b}{16\pi\alpha_{\text{EM}} m_{\Phi_M}^2} [R_{BM}^{\mu*} L_{BN}^{\mu} - L_{BM}^{\mu*} R_{BN}^{\mu}] \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM})$$

$$C_{S,T(P)}^{\text{box}} = \pm C_{S,T(P)}^{\text{box}} (L \leftrightarrow R)$$

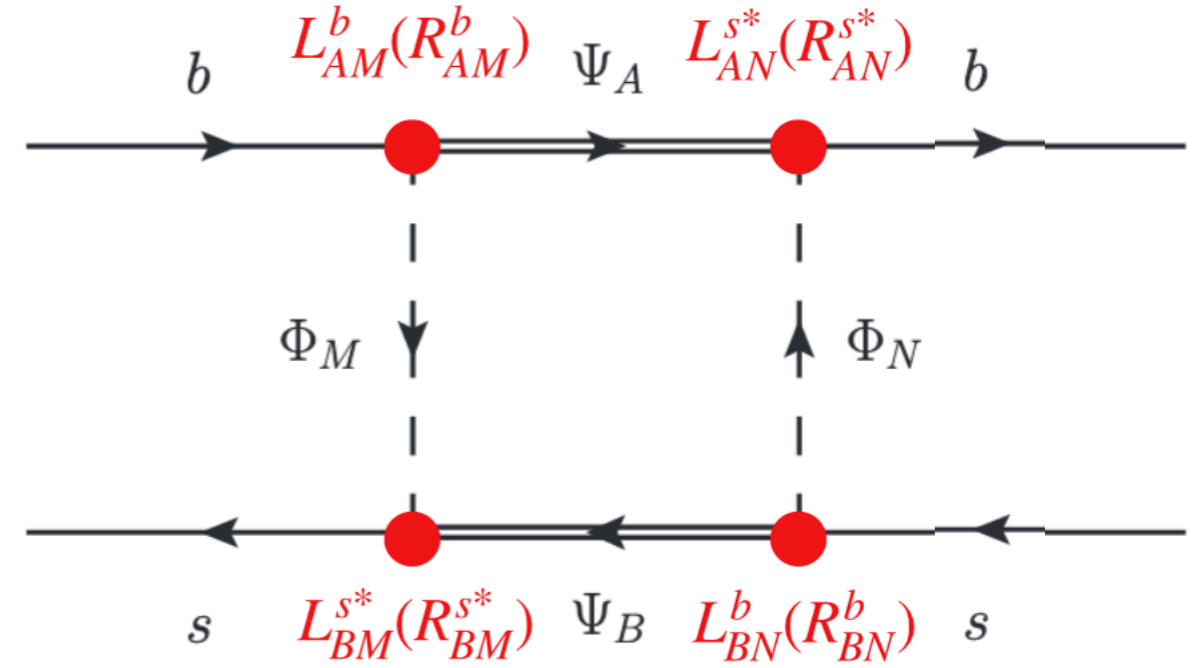
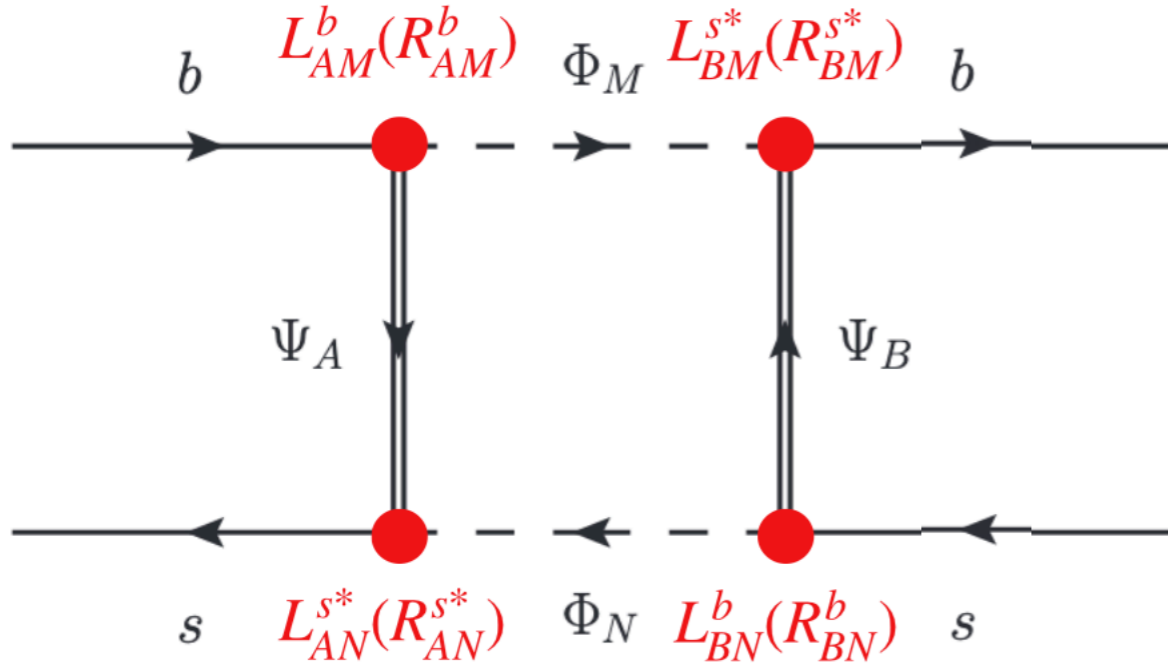
$$C_S^{\text{box}, b) = \mathcal{N} \frac{\chi L_{BM}^{s*} R_{AM}^b}{16\pi\alpha_{\text{EM}} m_{\Phi_M}^2} \left[ R_{AN}^{\mu*} L_{BN}^{\mu} F(x_{AM}, x_{BM}, x_{NM}) + L_{AN}^{\mu*} R_{BN}^{\mu} \frac{m_{\Psi_A} m_{\Psi_B}}{2m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

$$C_P^{\text{box}, b) = -\mathcal{N} \frac{\chi L_{BM}^{s*} R_{AM}^b}{16\pi\alpha_{\text{EM}} m_{\Phi_M}^2} \left[ R_{AN}^{\mu*} L_{BN}^{\mu} F(x_{AM}, x_{BM}, x_{NM}) - L_{AN}^{\mu*} R_{BN}^{\mu} \frac{m_{\Psi_A} m_{\Psi_B}}{2m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \right]$$

$$C_T^{\text{box}, b) = -\mathcal{N} \frac{\chi L_{BM}^{s*} R_{AM}^b L_{AN}^{\mu*} R_{BN}^{\mu}}{16\pi\alpha_{\text{EM}} m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM})$$

Additional WC present only in the presence of additional SU(2) breaking effects

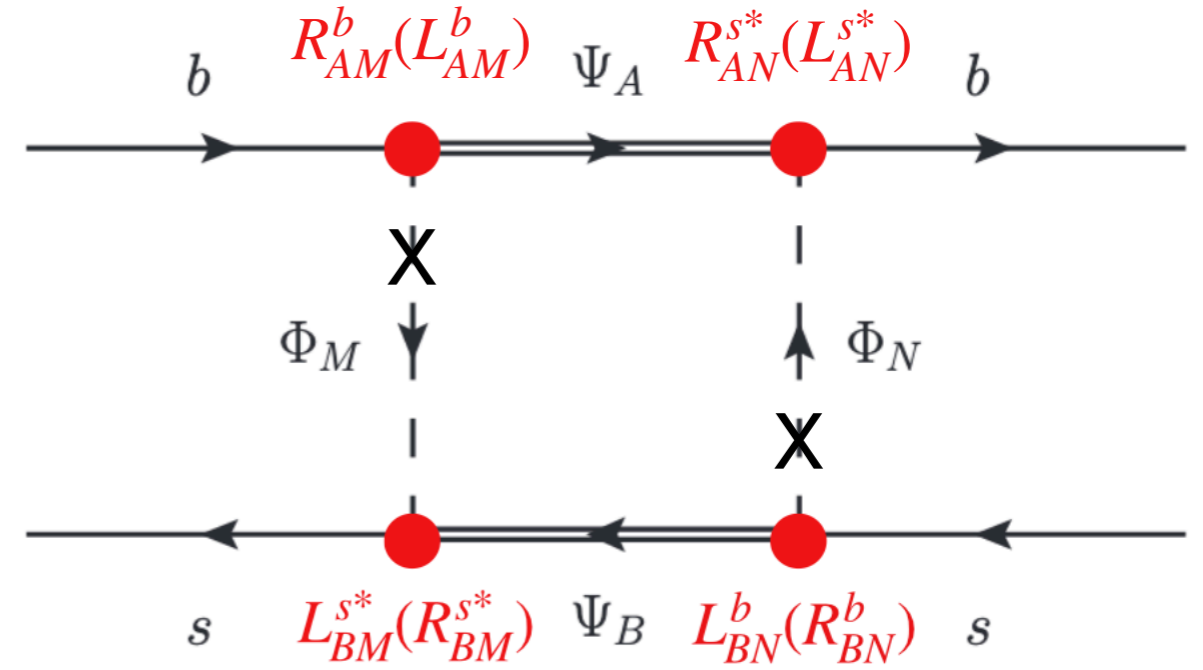
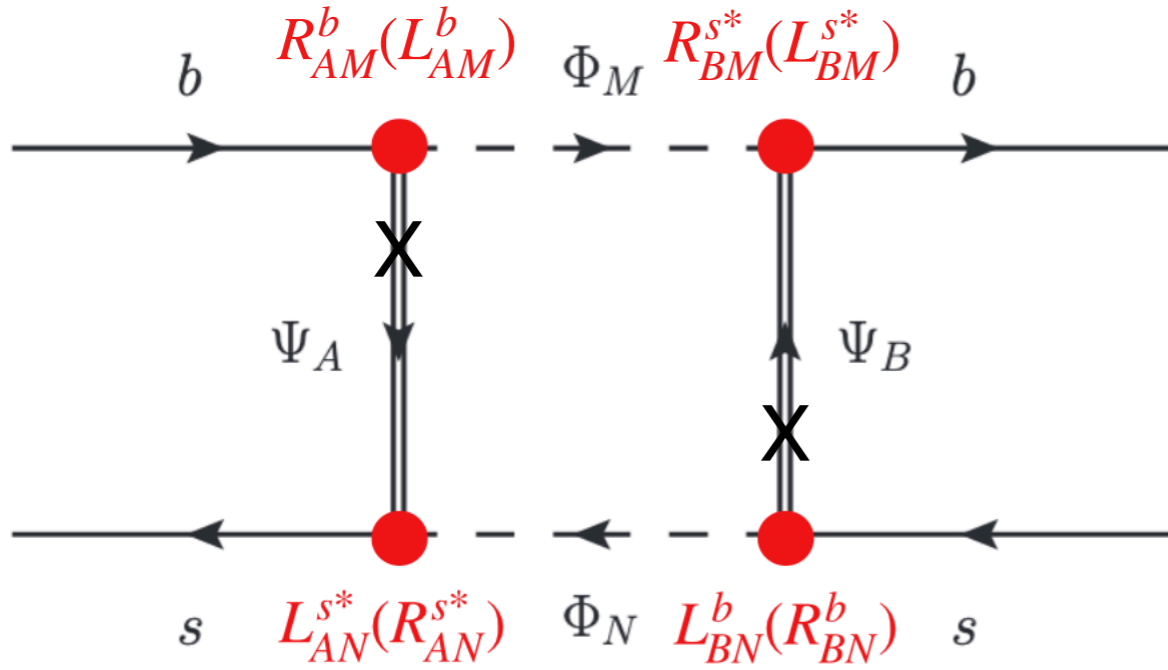
# $\Delta Ms$



Both diagrams appear, independently on  $b \rightarrow s \mu \mu$ , since no leptons are involved in this channel

$$\begin{aligned}
 C_1 &= (\chi_{BB} + \tilde{\chi}_{BB}) \frac{L_{AN}^{s*} L_{AM}^b L_{BM}^{s*} L_{BN}^b}{128\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), & C_4 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 C_2 &= \chi_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & & -\tilde{\chi}_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 C_3 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & C_5 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 & & & -\chi_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 \tilde{C}_{1,2,3} &= C_{1,2,3} (L \leftrightarrow R)
 \end{aligned}$$

# $\Delta Ms$

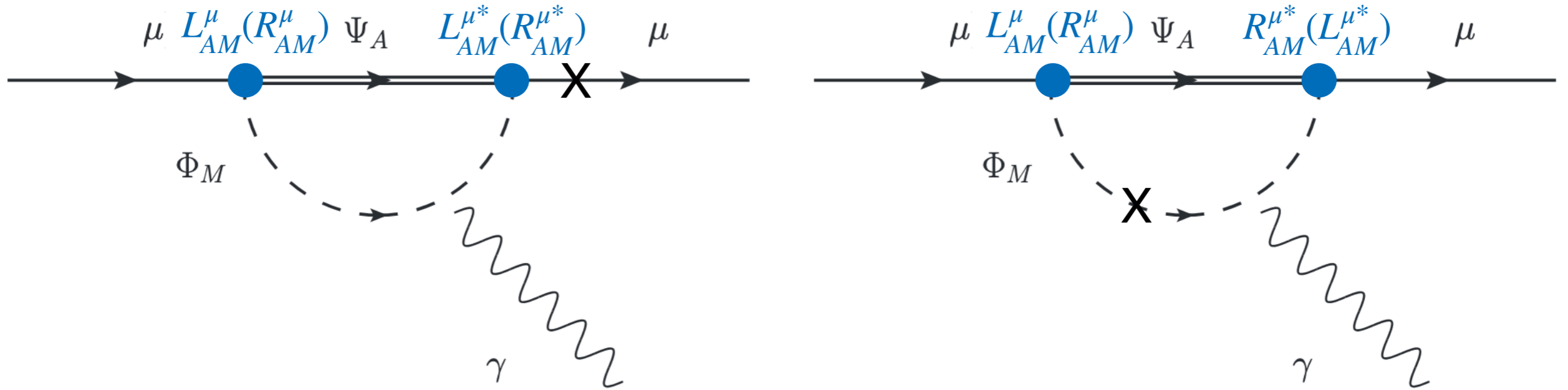


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 C_3 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b R_{BM}^{s*} L_{BN}^b}{64\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}), & C_5 &= \tilde{\chi}_{BB} \frac{R_{AN}^{s*} L_{AM}^b L_{BM}^{s*} R_{BN}^b}{32\pi^2 m_{\Phi_M}^2} \frac{m_{\Psi_A} m_{\Psi_B}}{m_{\Phi_M}^2} G(x_{AM}, x_{BM}, x_{NM}) \\
 & & & \ominus \chi_{BB} \frac{R_{AN}^{s*} R_{AM}^b L_{BM}^{s*} L_{BN}^b}{32\pi^2 m_{\Phi_M}^2} F(x_{AM}, x_{BM}, x_{NM}), \\
 \tilde{C}_{1,2,3} &= C_{1,2,3} (L \leftrightarrow R)
 \end{aligned}$$

Additional contributions to WC present in the presence of additional SU(2) breaking effects

g-2



$$\Delta a_{\mu} = \frac{\chi a_{\mu} m_{\mu}^2}{8\pi^2 m_{\Phi_M}^2} \left[ (L_{AM}^{\mu*} L_{AM}^{\mu} + R_{AM}^{\mu*} R_{AM}^{\mu}) (Q_{\Phi_M} \tilde{F}_7(x_{AM}) - Q_{\Psi_A} F_7(x_{AM})) \right. \\ \left. + (L_{AM}^{\mu*} R_{AM}^{\mu} + R_{AM}^{\mu*} L_{AM}^{\mu}) \frac{2m_{\Psi_A}}{m_{\mu}} (Q_{\Phi_M} \tilde{G}_7(x_{AM}) - Q_{\Psi_A} G_7(x_{AM})) \right]$$

Additional term induced by SU(2) breaking, and chirally enhanced

# 4th Generation Model

$$\begin{aligned}
 L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \Gamma_{u_i}^R \bar{\Psi}_u P_R u_i + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
 & + \sum_{C=L,R} \left( \lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u + \lambda_C^D \bar{\Psi}_q P_C h \Psi_d + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
 & + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
 \end{aligned}$$

We start writing down the most general Lagrangian before EWSB including a 4th vector-like generation and a neutral scalar

	$SU(3)$	$SU(2)$	$U(1)$	$U'(1)$
$\Psi_q$	3	2	1/6	$Z$
$\Psi_u$	3	1	2/3	$Z$
$\Psi_d$	3	1	-1/3	$Z$
$\Psi_\ell$	1	2	-1/2	$Z$
$\Psi_e$	1	1	-1	$Z$
$\Phi$	1	1	0	$-Z$

NB. We work in the basis with diagonal down-type quarks

# 4th Generation Model

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 & + \sum_{C=L,R} \left( \cancel{\lambda_C^U \bar{\Psi}_q P_C \tilde{h} \Psi_u} + \lambda_C^D \bar{\Psi}_q P_C h \Psi_d + \lambda_C^E \bar{\Psi}_\ell P_C h \Psi_e \right) + \text{h.c.} \\
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 \end{aligned}$$

We're interested only in couplings to bottom, strange, muon

# 4th Generation Model

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We neglect SU(2) breaking for down-type quarks  
(responsible for phenomenological un-relevant scalar/tensor operators)



# 4th Generation Model

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 \end{aligned}$$

We're interested only in couplings to bottom, strange, muon

We neglect SU(2) breaking for down-type quarks  
(responsible for phenomenological un-relevant scalar/tensor operators)

We need to diagonalize the lepton sector!



# 4th Generation Model

$$\begin{aligned}
 L^{4\text{th}} = & \sum_i \left( \Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i \right) \Phi + \text{h.c.} \\
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 & + \sum_{F=q,\ell,u,d,e} M_F \bar{\Psi}_F \Psi_F + \kappa h^\dagger h \Phi^\dagger \Phi + m_\Phi^2 \Phi^\dagger \Phi
 \end{aligned}$$

Below EWSB:

$$L_{\text{mass}}^{4\text{th}} = \begin{pmatrix} \bar{\Psi}_{\ell,2} \\ \bar{\Psi}_e \end{pmatrix}^T \begin{pmatrix} M_\ell & \sqrt{2}v\lambda_R^E \\ \sqrt{2}v\lambda_L^{E*} & M_e \end{pmatrix} P_L \begin{pmatrix} \Psi_{\ell,2} \\ \Psi_e \end{pmatrix} \Rightarrow$$

$$\begin{aligned}
 P_L \begin{pmatrix} \Psi_{\ell,2} \\ \Psi_e \end{pmatrix}_I & \rightarrow W_{IJ}^{E_L} \Psi_J^{E_L} \\
 \begin{pmatrix} \bar{\Psi}_{\ell,2} \\ \bar{\Psi}_e \end{pmatrix}_I^T P_L & \rightarrow \bar{\Psi}_J^{E_R} W_{IJ}^{E_R}
 \end{aligned}$$

# 4th Generation Model

$$L^{4\text{th}} = \sum (\Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i) \Phi + \text{h.c.}$$

$$P_L \begin{pmatrix} \Psi_{\ell,2} \\ \Psi_e \end{pmatrix}_I \rightarrow W_{IJ}^{E_L} \Psi_J^{E_L}$$

$$\begin{pmatrix} \bar{\Psi}_{\ell,2} \\ \bar{\Psi}_e \end{pmatrix}_I^T P_L \rightarrow \bar{\Psi}_J^{E_R} W_{IJ}^{E_R}$$

$$P_L \begin{pmatrix} \Psi_{q,2} \\ \Psi_d \end{pmatrix}_I \rightarrow \delta_{IJ} \Psi_J^{D_L}$$

$$\begin{pmatrix} \bar{\Psi}_{q,2} \\ \bar{\Psi}_d \end{pmatrix}_I^T P_L \rightarrow \bar{\Psi}_J^{D_R} \delta_{IJ}$$

$$L_{\text{int}}^{4\text{th}} = (L_1^b \bar{\Psi}_1^D P_L b + L_1^s \bar{\Psi}_1^D P_L s + L_I^\mu \bar{\Psi}_I^E P_L \mu) \Phi$$

$$+ (R_2^b \bar{\Psi}_1^D P_R b + R_2^s \bar{\Psi}_1^D P_R s + R_I^\mu \bar{\Psi}_I^E P_R \mu) \Phi$$

$$L_1^s = \Gamma_s^L, \quad L_1^b = \Gamma_b^L, \quad R_2^s = \Gamma_s^R, \quad R_2^b = \Gamma_b^R,$$

$$L_1^\mu = \Gamma_\mu^L \cos \theta_L, \quad L_2^\mu = -\Gamma_\mu^L \sin \theta_L, \quad R_1^\mu = \Gamma_\mu^R \sin \theta_R, \quad R_2^\mu = \Gamma_\mu^R \cos \theta_R$$

# 4th Generation Model - WC

$$\Gamma^L \equiv L_1^b L_1^{s*}, \quad \Gamma^R \equiv R_2^b R_2^{s*}$$

## ● $b \rightarrow s\mu\mu$

$$C_9^{\text{box}} = -\mathcal{N} \frac{\Gamma^L}{32\pi\alpha_{\text{EM}}m_\Phi^2} (|\Gamma_\mu^L|^2 + |\Gamma_\mu^R|^2) F(x_D, x_E)$$

$$C_{10}^{\text{box}} = \mathcal{N} \frac{\Gamma^L}{32\pi\alpha_{\text{EM}}m_\Phi^2} (|\Gamma_\mu^L|^2 - |\Gamma_\mu^R|^2) F(x_D, x_E)$$

$$C_{9(10)}^{\text{box}} = \pm C_{9(10)}^{\text{box}} (L \leftrightarrow R)$$

## ● $\Delta M_S$

$$C_1 = \frac{|\Gamma^L|^2}{128\pi^2 m_\Phi^2} F(x_D), \quad C_5 = -\frac{\Gamma^L \Gamma^R}{32\pi^2 m_\Phi^2} F(x_D), \quad \tilde{C}_1 = \frac{|\Gamma^R|^2}{128\pi^2 m_\Phi^2} F(x_D)$$

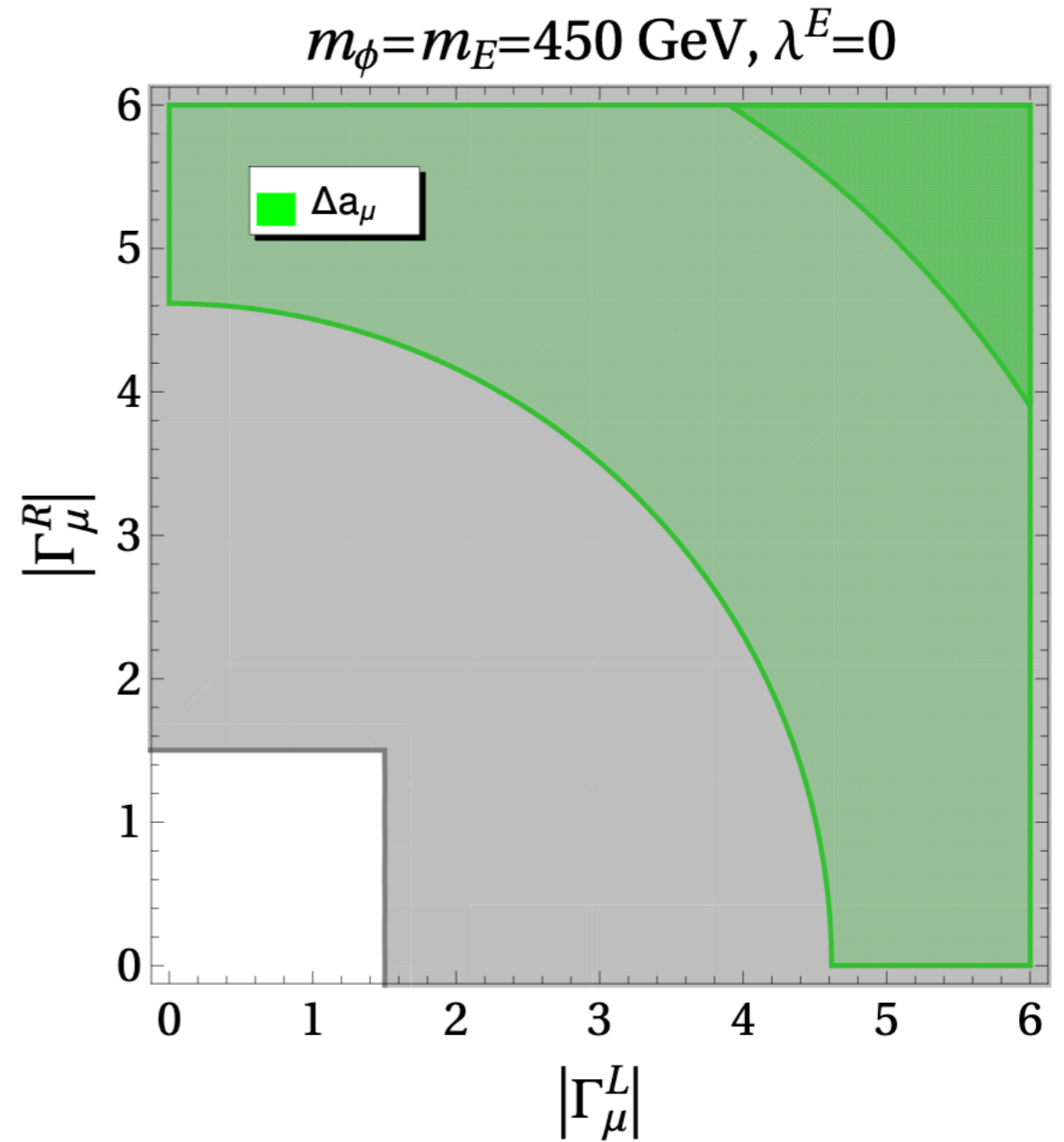
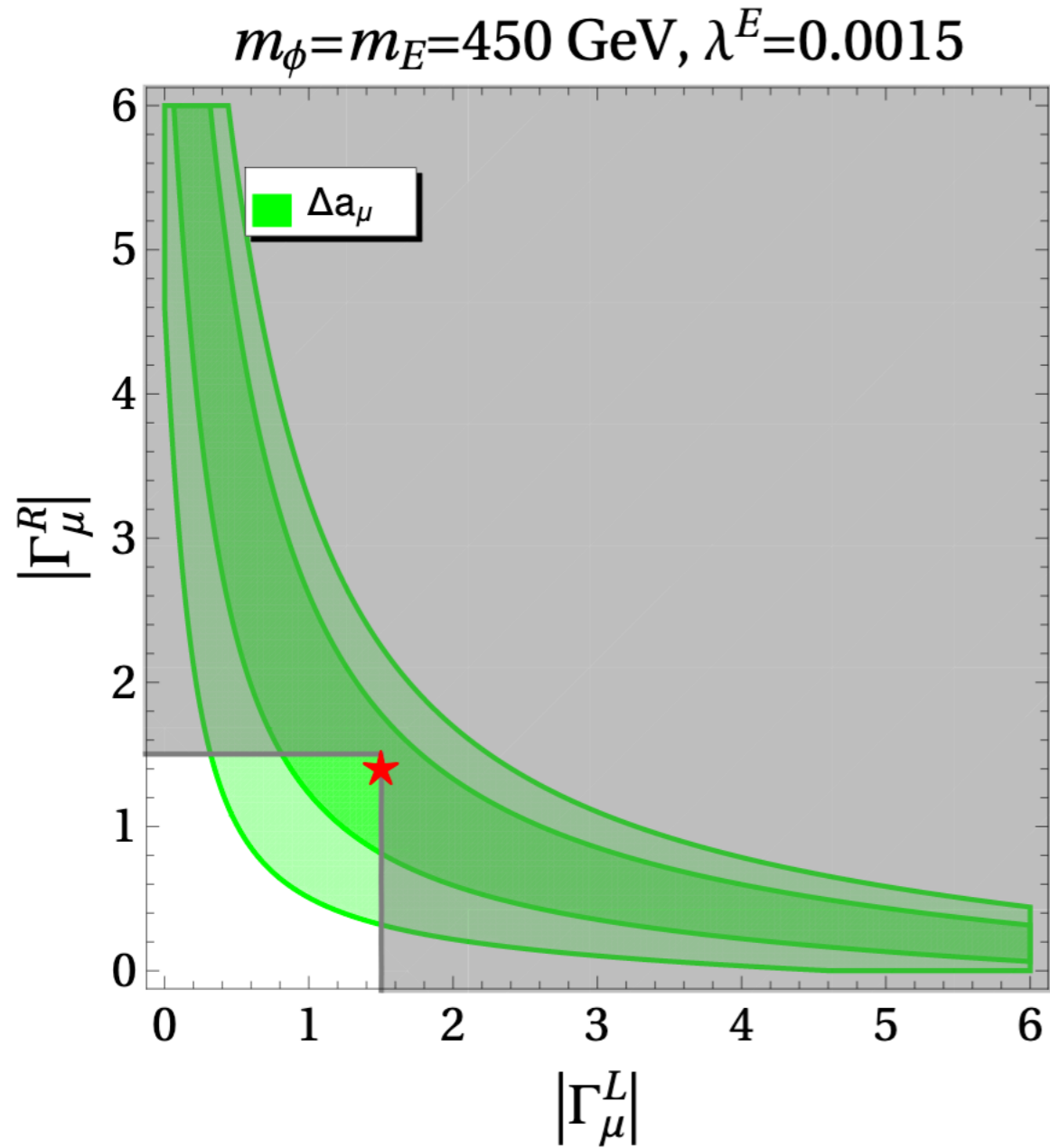
## ● g-2

$$\lambda_R^E = -\lambda_L^E \equiv \lambda^E$$

$$\Delta a_\mu = \frac{m_\mu^2}{8\pi^2 m_\Phi^2} \left[ (|\Gamma_\mu^L|^2 + |\Gamma_\mu^R|^2) F_7(x_E) + \frac{8}{\sqrt{2}} \frac{v \lambda^E}{m_\mu} \Gamma_\mu^L \Gamma_\mu^R G_7(x_E) \right]$$

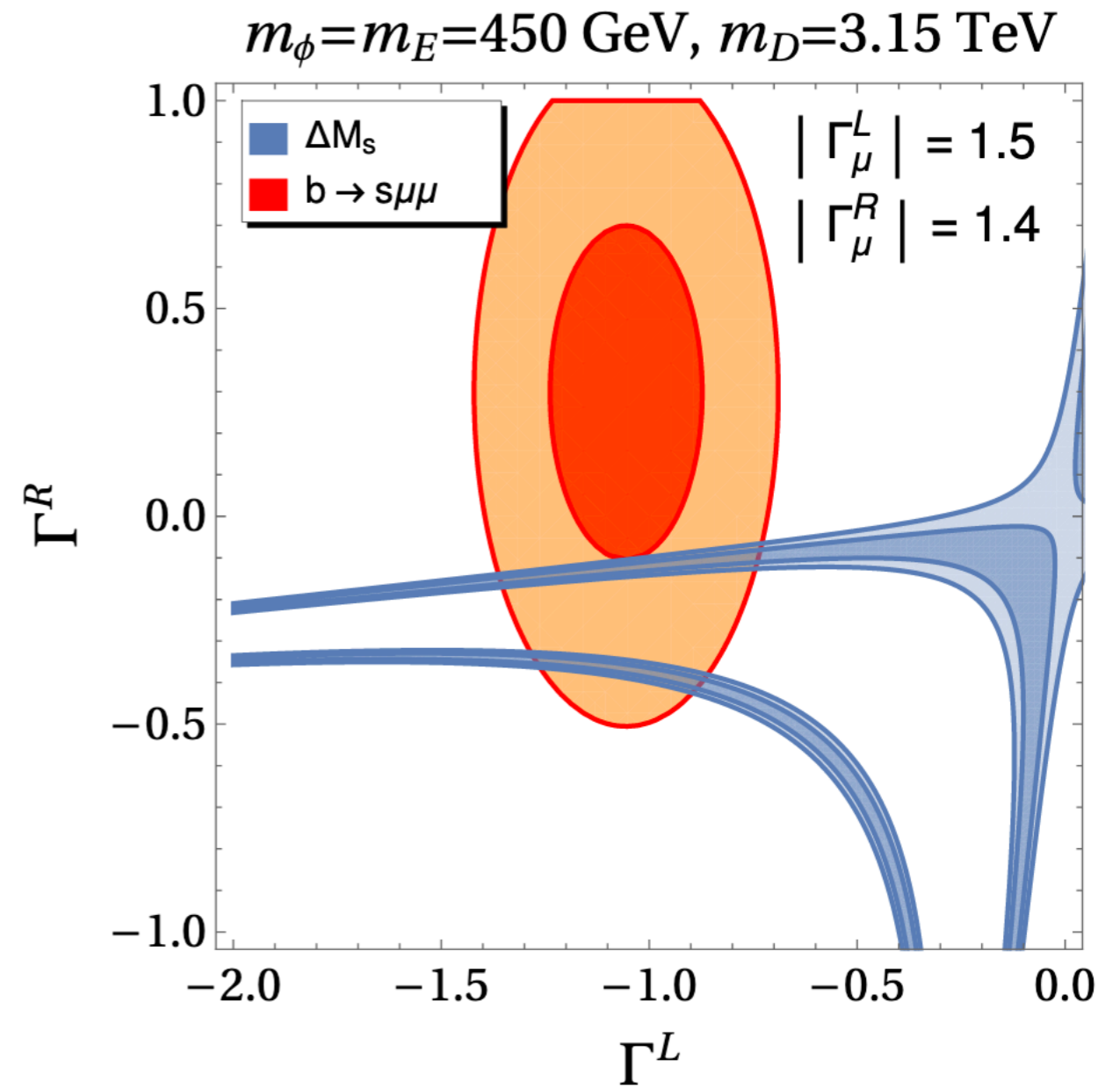
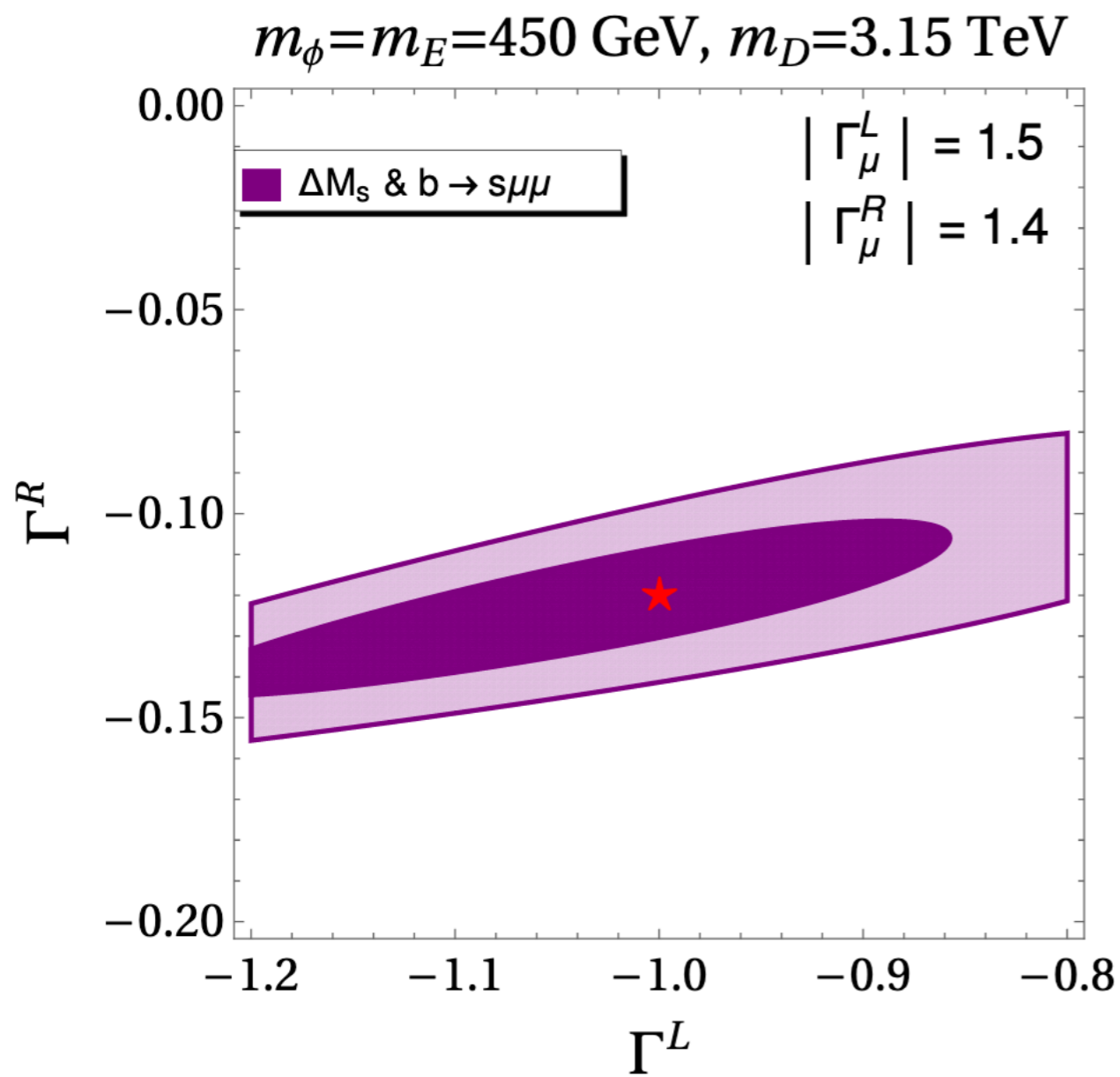
$$|\Gamma_\mu^L| = 1.5, \quad |\Gamma_\mu^R| = 1.4, \quad \lambda^E = 0.0015, \quad \Gamma^L = -1.0, \quad \Gamma^R = -0.12$$

# Fit g-2



Right-handed coupling and SU(2) breaking both fundamental!

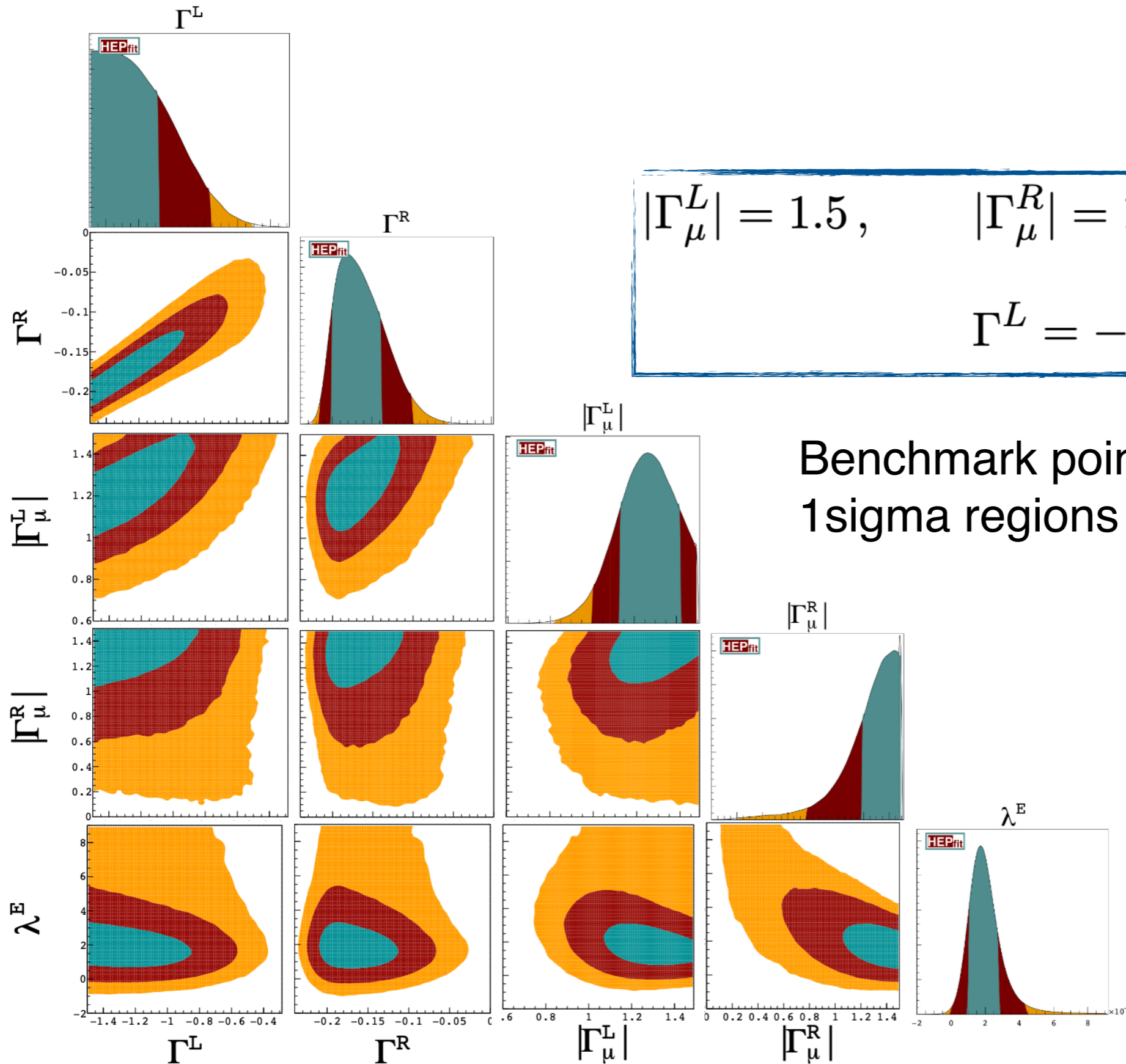
# Fit B decays



Right-handed coupling fundamental!



# Global Fit



$$|\Gamma_\mu^L| = 1.5, \quad |\Gamma_\mu^R| = 1.4, \quad \lambda^E = 0.0015$$

$$\Gamma^L = -1.0, \quad \Gamma^R = -0.12$$

Benchmark point, compatible with all 1 sigma regions of combined pdf

# Conclusions

- We have provided analytical formulae for studying B anomalies,  $B\bar{B}$  mixing and  $g-2$  in the context of general loop models
- We have investigated the additional effects provided by right-handed couplings and additional  $SU(2)$  breaking effects
- We have investigated the phenomenology in a specific model, i.e. 4th generations of vector-like fermions + neutral scalar, and addressed all the above anomalies with viable masses and  $O(1)$  couplings
- The neutral scalar is a viable (stable) DM candidate, which however require a further detailed analysis still to be addressed

# Back-up



# Colour Factors

$SU(3)$	$b \rightarrow s\ell\bar{\ell}$ type a)				$b \rightarrow s\ell\bar{\ell}$ type b)				$\chi$
	$\Psi_A$	$\Psi_B$	$\Phi_M$	$\Phi_N$	$\Psi_A$	$\Psi_B$	$\Phi_M$	$\Phi_N$	
I	3	1	1	1	1	1	$\bar{3}$	1	1
II	1	$\bar{3}$	$\bar{3}$	$\bar{3}$	3	3	1	3	1
III	3	8	8	8	8	8	$\bar{3}$	8	4/3
IV	8	$\bar{3}$	$\bar{3}$	$\bar{3}$	3	3	8	3	4/3
V	$\bar{3}$	3	3	3	$\bar{3}$	$\bar{3}$	3	$\bar{3}$	2

**Table 1.** Table of the possible  $SU(3)$  representations that can give an effect in  $b \rightarrow s\ell^+\ell^-$  or  $b \rightarrow s\nu\nu$  transitions via box diagrams.  $\chi$  denotes the resulting group factor appearing in Eqs. (2.4)-(2.8) which also enters in  $b \rightarrow s\nu\nu$  transitions.

$SU(3)$	$\Psi_A$	$\Psi_B$	$\Phi_M$	$\Phi_N$	$\chi_{BB}$	$\tilde{\chi}_{BB}$
I	3	3	1	1	1	0
II	1	1	$\bar{3}$	$\bar{3}$	0	1
III	3	3	8	8	1/36	7/12
IV	8	8	$\bar{3}$	$\bar{3}$	7/12	1/36
V	3	3	(1,8)	(8,1)	-1/6	1/2
VI	(1,8)	(8,1)	$\bar{3}$	$\bar{3}$	1/2	-1/6
VII	$\bar{3}$	$\bar{3}$	3	3	1	1

**Table 3.** Table of the different  $SU(3)$  representations that can give a non-zero effect via box diagrams to  $B_s - \bar{B}_s$  mixing.  $\chi_{BB}$  and  $\tilde{\chi}_{BB}$  denote the resulting group factors.

$SU(3)$	$\Psi_A$	$\Phi_M$	$\chi_{a_\mu}$
I	1	1	1
II	(3, $\bar{3}$ )	(3, $\bar{3}$ )	3
III	8	8	8

**Table 4.** Table of the different  $SU(3)$  representations that can give a non-zero effect to  $a_\mu$ .

# D-Dbar mixing

$$L^{4\text{th}} = \sum (\Gamma_{q_i}^L \bar{\Psi}_q P_L q_i + \Gamma_{\ell_i}^L \bar{\Psi}_\ell P_L \ell_i + \cancel{\Gamma_{u_i}^R \bar{\Psi}_u P_R u_i} + \Gamma_{d_i}^R \bar{\Psi}_d P_R d_i + \Gamma_{e_i}^R \bar{\Psi}_e P_R e_i) \Phi + \text{h.c.}$$

SU(2) + CKM  $\Downarrow$

$$L_1^u = V_{us}^* \Gamma_s^L + V_{ub}^* \Gamma_b^L, \quad L_1^c = V_{cs}^* \Gamma_s^L + V_{cb}^* \Gamma_b^L$$

Only the product of down-type coupling is constrained

$\Downarrow$

$\Gamma_b^L \gg \Gamma_s^L$  implies negligible effects due to CKM suppressions

# Fit Results for Relevant Observables

$$\begin{aligned}
 R_K[1.1, 6] &= 0.781(45), & R_{K^*}[1.1, 6] &= 0.885(39), & \bar{\mathcal{B}}(B_s \rightarrow \mu^+ \mu^-) &= 3.30(21) \cdot 10^{-9}, \\
 P'_5[4, 6] &= -0.454(69), & P'_5[6, 8] &= -0.626(59), \\
 \Delta a_\mu &= 235(87) \cdot 10^{-11}, & R_{\Delta M_s} &= -0.02(8).
 \end{aligned}$$

