
Pattern-matching Unit for Medical Applications (PUMA)

— 22nd IEEE Real Time Conference —
Speaker: Orlando Leombruni

An interdisciplinary approach to the problem



Expertise on **highly innovative hardware solutions**

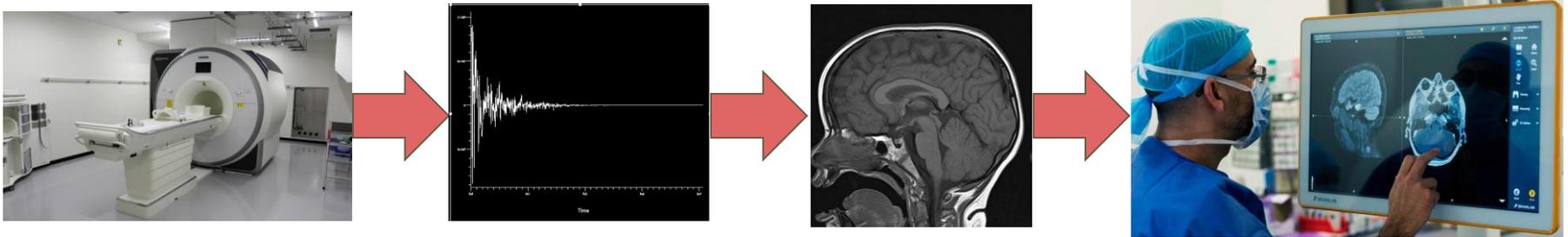
IMAGO7



Ground-breaking research on modern medical imaging techniques

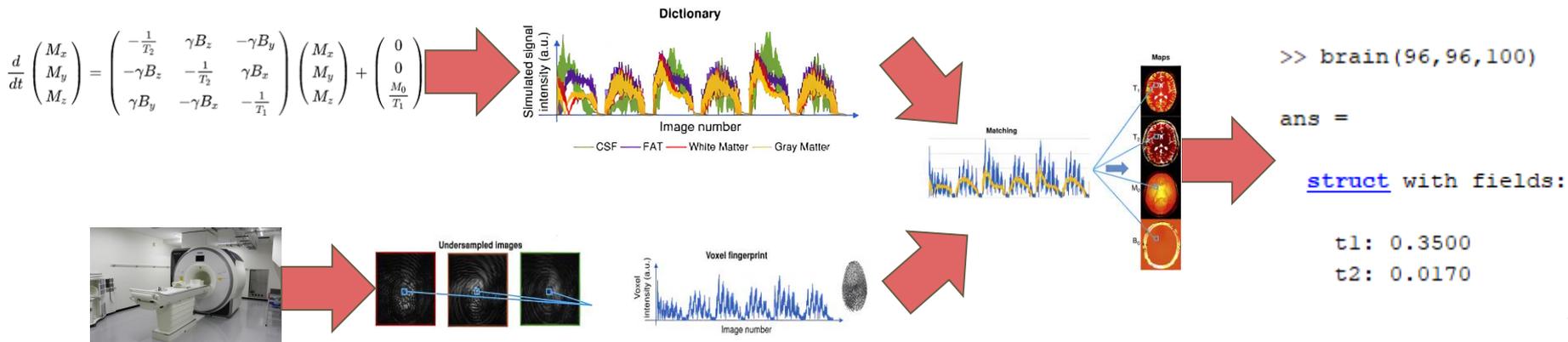
Introduction: (qualitative) MRI

- Current state-of-the-art
- MR signal acquisition done when system is in steady-state after applying magnetization
- Generate high-resolution contrast image
 - Voxels do not have a quantitative meaning
 - Image must be interpreted by a radiologist
- Quantitative reconstruction is possible by repeated acquisitions (long time)



Intro: Magnetic Resonance Fingerprinting (MRF)

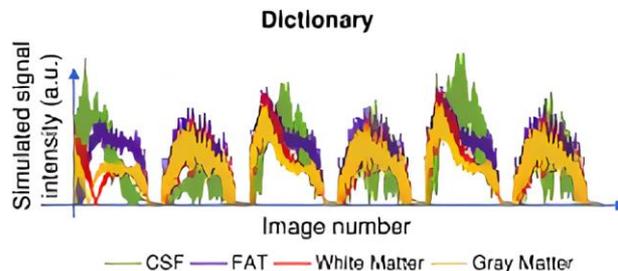
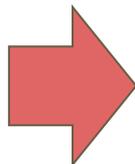
- Modern approach
- Exploit the *transient state* in-between frequent repeated acquisitions
- Extract *quantitative* information from an MRI signal in a short time
- Each point of the map is associated to specific values for the parameters
- Voxels now have a quantitative measure associated to them!



Fingerprinting state-of-the-art: the dictionary

- All current fingerprinting techniques use a *dictionary of simulated signals*
- For each possible combination of values of the chosen tissue parameters, simulate a signal
 - as close as possible to the “true” signal that would be acquired from the MR machine when it encounters a tissue with those specific values of the parameters
 - using Bloch’s equations

$$\frac{d}{dt} \begin{pmatrix} M_x \\ M_y \\ M_z \end{pmatrix} = \begin{pmatrix} -\frac{1}{T_2} & \gamma B_z & -\gamma B_y \\ -\gamma B_z & -\frac{1}{T_2} & \gamma B_x \\ \gamma B_y & -\gamma B_x & -\frac{1}{T_1} \end{pmatrix} \begin{pmatrix} M_x \\ M_y \\ M_z \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ \frac{M_0}{T_1} \end{pmatrix}$$



Fingerprinting state-of-the-art: computation

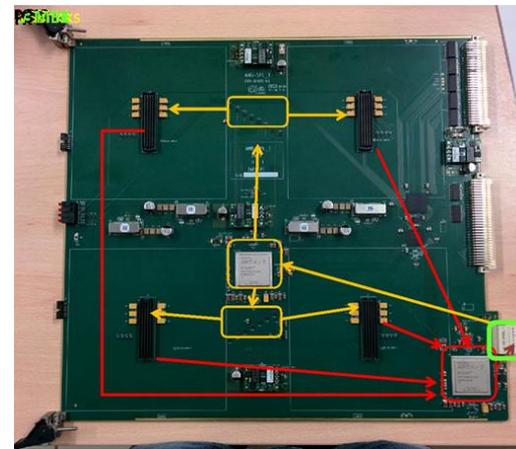
- Both signal voxels and dictionary entries are vectors of complex numbers
- for *each* voxel i , the standard method calculates the **dot product** between the i vector and the vector of ***each entry*** of the dictionary, to choose the dictionary entry that produces the **maximum dot product**
 - If entry j of the dictionary, generated from the parameters p_1^j, \dots, p_n^j , is such that $v_i \times v_j$ has the highest dot product for pixel i , then p_1^j, \dots, p_n^j are assigned as the tissue parameters of i
- Dot product is a computationally easy operation (few μ s even on general purpose processors)
- The problem is the sheer number of dot products to be computed even in simple cases!

Some numbers

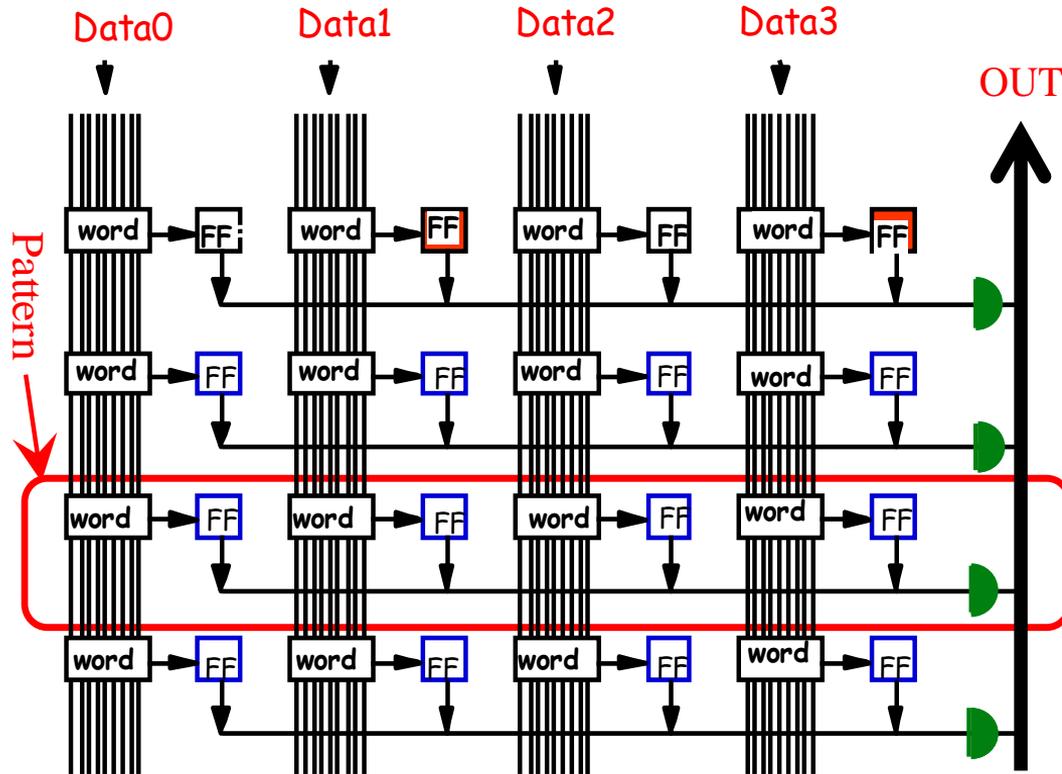
- A dictionary built from two parameters at a medium granularity has ~200k entries, a brain MR image is made by $200 \times 200 \times 200 = 8 \cdot 10^6$ voxels
 - → $1600 \cdot 10^6$ dot product operations!
 - On a fast consumer PC ($\sim 5 \mu\text{s}$ per dot product), this amounts to **8000 seconds** (>2hrs)!
 - On more powerful specialized hardware (GPGPUs): ~350 seconds
- Adding more parameters (or increasing their granularity) to the dictionary greatly increases its size
 - 4 parameters: 3M entries
 - 6 parameters: 300M entries
 - 10 parameters: 15B entries!
 - With 10 parameters, we'd take **1.5 years** for a single brain image, even with the fastest GPU!

The FTK Associative Memory

- Our idea: adapt the Associative Memory developed for High Energy Physics projects to this problem
- Capable of millions of comparisons in a single clock cycle!
- Estimated performance:
 - Using a 200k dictionary: $\sim 0.5s$
 - Using a 15B dictionary: $\sim 1h^*$



The Associative Memory



Using the Associative Memory for MRF

- If the simulated signals that compose the dictionary were “perfectly equal” to the corresponding acquired MRI signals, we could use the AM “as-is”: load the dictionary into the AM banks, then use the MRI acquisition as input
- Unfortunately, real MRI signals show acquisition defects
 - noise from the environment
 - “aliasing” effects from nearby tissues
- Therefore, we have to “pre-process” both dictionary and acquisitions

Using the AM in practice

- Both voxels of the acquired MR image and entries of the dictionary are represented by a vector of m complex numbers (often: $m = 8$)
 - each complex number is called a *component*
- In order to be loaded into the AM banks, dictionary entries must be *converted* into vectors of integers
- We employed a **binning** technique
 - Fact: components are always in the interval $[-1, 1]$
 - Divide the interval into n bins of size $2/n$
 - If the i -th component falls into the k -th bin \rightarrow assign the number k to that component

Binning: considerations

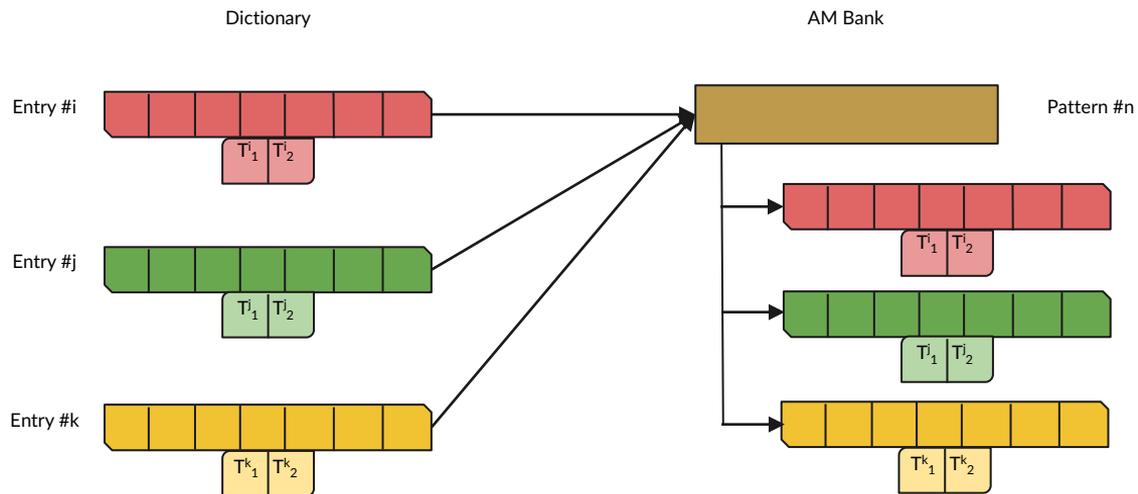
- Binning is effectively a form of *discretization*
- Multiple distinct dictionary entries could be represented by the same bin string (called *pattern* in our terminology)
- Nevertheless, if done correctly, all entries that are represented by the same pattern are “close” to each other in the dictionary space
 - i.e. they have similar values for all the parameters
- Of course, we have to perform the same binning transformation to each voxel of the acquired MR image
- The AM is then used to perform pattern matching

How to use the AM output

- The AM will output the address of the matched pattern
- Next step: associate each pattern with the list of the dictionary entries that are represented by it, then perform the dot product between the voxel and these (few) entries - **filtering!**
- Filtering requires a fine tuning of the procedure parameters
 - bin number and size
 - gaussian noise applied to dictionary entries (to simulate environmental noise)
 - ...
- «Best» parameters chosen via heuristics
 - Minimize the number of voxels with no matched pattern, while keeping the error w.r.t. the gold standard reconstruction low

Using the AM to filter “good” entries

- Each voxel of the acquired MR image is associated to a (hopefully short) list of dictionary entries
- If the AM is used correctly, the list contains the dictionary entry with the highest dot product among all entries
- Basically, the AM outputs for each voxel the list of “closest” dictionary entries
- For each voxel, must perform dot products on a subset of the dictionary after using the AM (postprocessing)



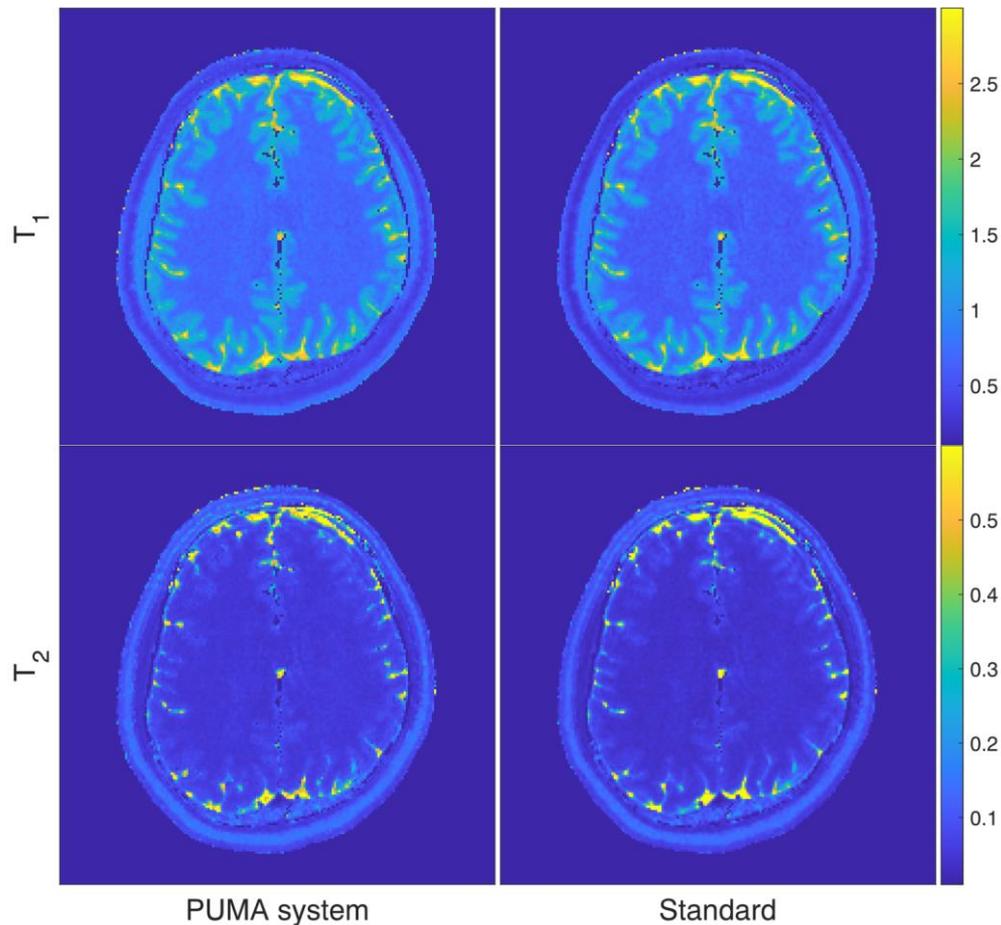
Dot-products step

- If done correctly, after filtering (step 1, see image) a few (~5000) dot products per voxel are required (step 2)
- Can be done in hardware, e.g. using FPGAs



Some results

- Extremely good results when reconstructing a brain using a dictionary with two parameters: longitudinal (T_1) and transverse (T_2) relaxation times
 - 99.97% reconstruction efficiency
 - Less than 3% error
 - **36 times** less dot products than the standard method
- Actual timing performance to be validated on real hardware (next step of the work)



Conclusions

- Highly innovative approach to a well-known problem
- «Transfer of knowledge» between High Energy Physics and Medical Imaging scenarios
- Promising preliminary results to be confirmed with tests on actual hardware

Thanks for your attention!

- Questions?
- Feel free to drop me an email: orlando.leombruni@pi.infn.it

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