

# Modeling Neutrino-Nucleus Interactions

## Do we need a new paradigm ?

Omar Benhar


INFN and Department of Physics  
Università "La Sapienza"  
I-00185 Roma, Italy

Neutrino 2010  
Athens, June 18th, 2010

# The *paradigm*\* of electron-nucleus scattering

- Thanks to the availability of a large body of precise data, theoretical models of electron-nucleus scattering have reached a high level of accuracy


---

\*a philosophical or theoretical framework of any kind (Merriam-Webster) 

# The *paradigm*\* of electron-nucleus scattering

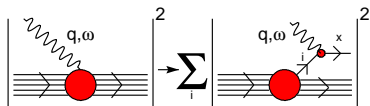
- Thanks to the availability of a large body of precise data, theoretical models of electron-nucleus scattering have reached a high level of accuracy
- The paradigm
  - ▶ Lepton kinematics fully determined
  - ▶ Elementary interaction vertex (  $d\sigma_N$  ) determined by electron-proton and electron-deuteron data (nuclear dynamics largely decoupled)

---

\*a philosophical or theoretical framework of any kind (Merriam-Webster) 

# The *paradigm*\* of electron-nucleus scattering

- Thanks to the availability of a large body of precise data, theoretical models of electron-nucleus scattering have reached a high level of accuracy
- The paradigm
  - ▶ Lepton kinematics fully determined
  - ▶ Elementary interaction vertex ( $d\sigma_N$ ) determined by electron-proton and electron-deuteron data (nuclear dynamics largely decoupled)
- The impulse approximation (IA) scheme:



$$d\sigma_A = \int d^3k dE d\sigma_N P(\mathbf{k}, E)$$

the spectral function  $P(\mathbf{k}, E)$  (from nuclear many-body theory) describes the energy and momentum distribution of the struck nucleon

\*a philosophical or theoretical framework of any kind (Merriam-Webster)

# Quasi elastic (QE) electron- & neutrino-nucleus x-sections

- QE electron scattering is usually analyzed at fixed beam energy  $E_e$  and electron scattering angle  $\theta_e$ , as a function of the energy transfer  $\omega = E_e - E_{e'}$ . Within this framework  $d\sigma_A \propto S(\mathbf{q}, \omega)$

# Quasi elastic (QE) electron- & neutrino-nucleus x-sections

- QE electron scattering is usually analyzed at fixed beam energy  $E_e$  and electron scattering angle  $\theta_e$ , as a function of the energy transfer  $\omega = E_e - E_{e'}$ . Within this framework  $d\sigma_A \propto S(\mathbf{q}, \omega)$
- The data set of MiniBooNE CCQE events provides an unprecedented opportunity to perform a similar analysis and carry out a systematic study of the (flux averaged) double differential cross section

$$\frac{d\sigma_A}{dT_\mu d\cos\theta_\mu} = \frac{1}{N} \int dE_\nu \Phi(E_\nu) \frac{d\sigma_A}{dE_\nu dT_\mu d\cos\theta_\mu}$$

# Quasi elastic (QE) electron- & neutrino-nucleus x-sections

- QE electron scattering is usually analyzed at fixed beam energy  $E_e$  and electron scattering angle  $\theta_e$ , as a function of the energy transfer  $\omega = E_e - E_{e'}$ . Within this framework  $d\sigma_A \propto S(\mathbf{q}, \omega)$
- The data set of MiniBooNE CCQE events provides an unprecedented opportunity to perform a similar analysis and carry out a systematic study of the (flux averaged) double differential cross section

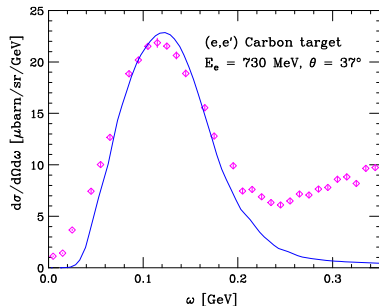
$$\frac{d\sigma_A}{dT_\mu d\cos\theta_\mu} = \frac{1}{N} \int dE_\nu \Phi(E_\nu) \frac{d\sigma_A}{dE_\nu dT_\mu d\cos\theta_\mu}$$

- Extending the paradigm of electron scattering to the analysis of the CCQE neutrino data amounts to using the nucleon axial mass  $M_A = 1.03 \text{ GeV}$ , determined by deuteron data

# Quasi elastic (QE) electron- & neutrino-nucleus x-sections

- Recall: Calculations involve *no adjustable parameters*

▶ Data: J.S. O'Connell *et al*, PRC **35**, 1063 (1987)



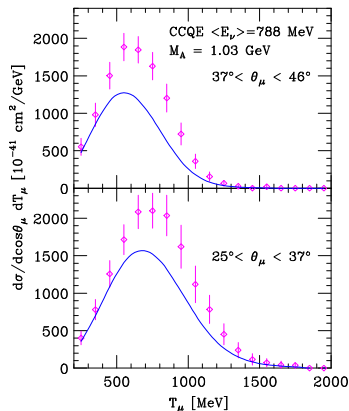
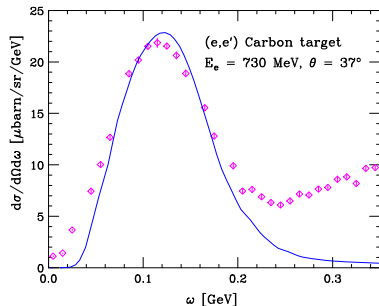


# Quasi elastic (QE) electron- & neutrino-nucleus x-sections

- Recall: Calculations involve *no adjustable parameters*

▶ Data: MiniBooNe, arXiv:1002.2680v1 [hep-ex]

▶ Data: J.S. O'Connell *et al*, PRC **35**, 1063 (1987)

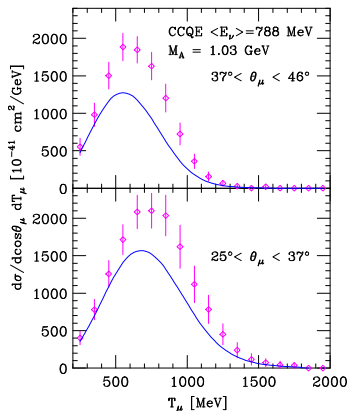
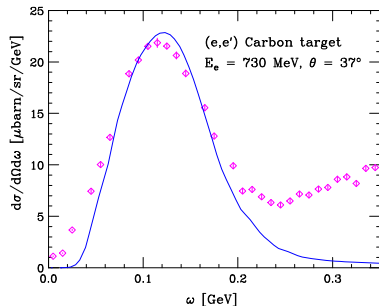


# Quasi elastic (QE) electron- & neutrino-nucleus x-sections

- Recall: Calculations involve *no adjustable parameters*

▶ Data: MiniBooNe, arXiv:1002.2680v1 [hep-ex]

▶ Data: J.S. O'Connell *et al*, PRC 35, 1063 (1987)



- The paradigm of electron scattering appears to badly fail !

# The axial mass issue

- The analyses of the CCQE data collected by K2K and MiniBooNE using a carbon target yield a value of the axial mass significantly larger than the world average. The MiniBooNE collaboration recently reported the value  $M_A = 1.35 \text{ GeV}$

# The axial mass issue

- The analyses of the CCQE data collected by K2K and MiniBooNE using a carbon target yield a value of the axial mass significantly larger than the world average. The MiniBooNE collaboration recently reported the value  $M_A = 1.35 \text{ GeV}$
- It would be tempting to interpret a large value of  $M_A$  as an *effective* axial mass, modified by nuclear effects not included in the Fermi gas model employed in data analysis

# The axial mass issue

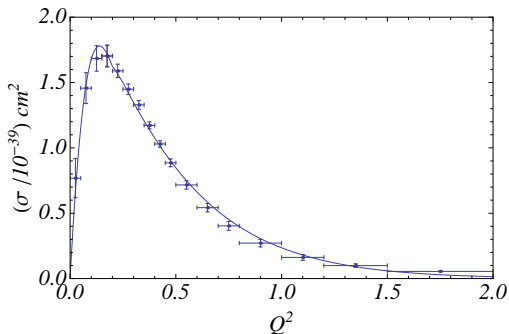
- The analyses of the CCQE data collected by K2K and MiniBooNE using a carbon target yield a value of the axial mass significantly larger than the world average. The MiniBooNE collaboration recently reported the value  $M_A = 1.35 \text{ GeV}$
- It would be tempting to interpret a large value of  $M_A$  as an *effective* axial mass, modified by nuclear effects not included in the Fermi gas model employed in data analysis
- Most existing models of nuclear effects do not appear to support the above argument (a prominent exception will be discussed later)

# The axial mass issue

- The analyses of the CCQE data collected by K2K and MiniBooNE using a carbon target yield a value of the axial mass significantly larger than the world average. The MiniBooNE collaboration recently reported the value  $M_A = 1.35 \text{ GeV}$
- It would be tempting to interpret a large value of  $M_A$  as an *effective* axial mass, modified by nuclear effects not included in the Fermi gas model employed in data analysis
- Most existing models of nuclear effects do not appear to support the above argument (a prominent exception will be discussed later)
- Using more advanced nuclear models may in fact lead to predict a value of  $M_A$  even larger than the one resulting from the MiniBooNE analysis

# Determining $M_A$ from a $\chi^2$ -fit of the $Q^2$ -distribution

- The resulting axial mass is  $M_A = 1.6$

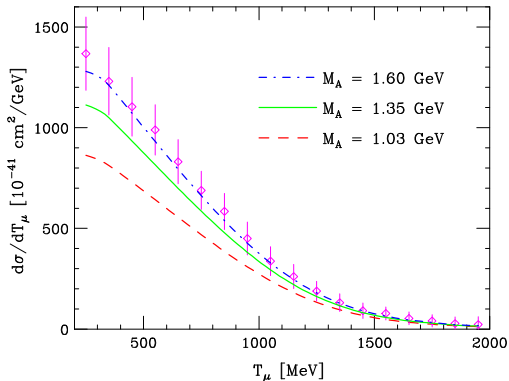


- Warning:** the  $Q^2$ -distribution is biased by the approximations needed to reconstruct the neutrino energy

$$Q^2 = 2E_\nu E_\mu \left( 1 - \frac{p_\mu}{E_\mu} \cos \theta_\mu \right) - m_\mu^2$$

# $M_A$ -dependence of the flux-integrated $T_\mu$ spectrum

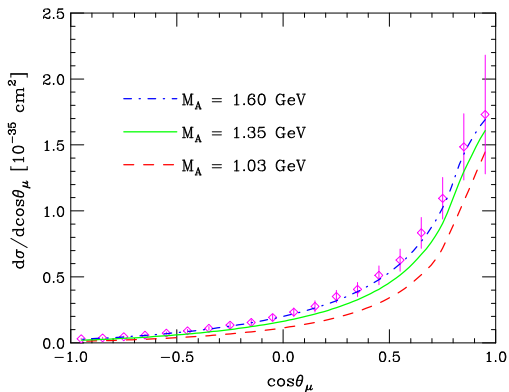
$$\frac{d\sigma_A}{dT_\mu} = \int d \cos \theta_\mu \frac{d\sigma_A}{dT_\mu d \cos \theta_\mu}$$



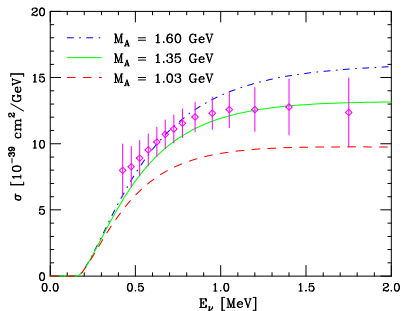


# $M_A$ -dependence of the flux-integrated $\cos \theta_\mu$ distribution

$$\frac{d\sigma_A}{d \cos \theta_\mu} = \int dT_\mu \frac{d\sigma_A}{dT_\mu d \cos \theta_\mu}$$

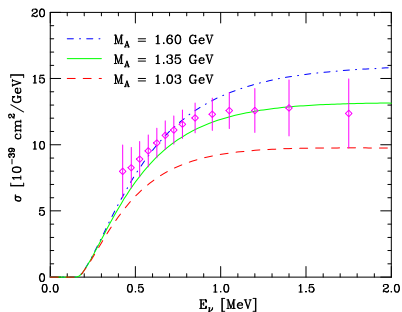


# Flux-unfolded total x-section

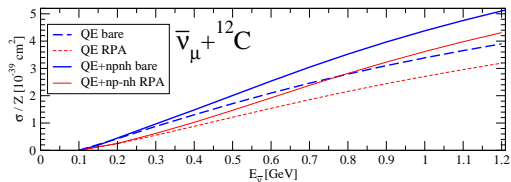
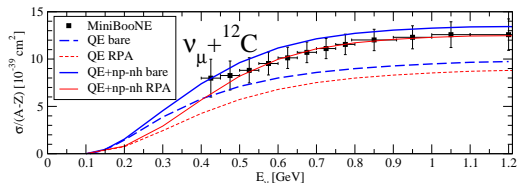


- $M_A = 1.6$  GeV does not yield the best fit to the data

# Flux-unfolded total x-section



- $M_A = 1.6 \text{ GeV}$  does not yield the best fit to the data



- Martini *et al* (2010),  $M_A = 1.03 \text{ GeV}$

# How big is the contribution of 2p-2h final states ?

- Within the model of Martini et al, the main mechanism responsible for the enhancement bringing the theoretical cross section into agreement with the data is multi nucleon knock out, leading to two particle- two hole (2p-2h) nuclear final states

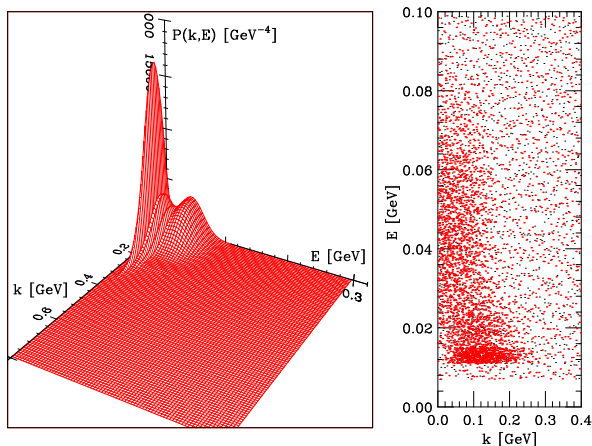
# How big is the contribution of 2p-2h final states ?

- Within the model of Martini et al, the main mechanism responsible for the enhancement bringing the theoretical cross section into agreement with the data is multi nucleon knock out, leading to two particle- two hole (2p-2h) nuclear final states
- All approaches based on *realistic* spectral functions take into account the occurrence of 2p-2h final states, arising from nucleon-nucleon correlations. In the region of the QE peak the contribution of these components, accounting for  $\sim 20\%$  of the strength (see next slide), is not large

# How big is the contribution of 2p-2h final states ?

- Within the model of Martini et al, the main mechanism responsible for the enhancement bringing the theoretical cross section into agreement with the data is multi nucleon knock out, leading to two particle- two hole (2p-2h) nuclear final states
- All approaches based on *realistic* spectral functions take into account the occurrence of 2p-2h final states, arising from nucleon-nucleon correlations. In the region of the QE peak the contribution of these components, accounting for  $\sim 20\%$  of the strength (see next slide), is not large
- In order to clarify the role of nuclear dynamics beyond the 1p-1h sector, the results of the model of Martini et al should be thoroughly tested comparing its predictions to electron scattering data

# Oxygen spectral function



- shell model states account for  $\sim 80\%$  of the strength
- the remaining  $\sim 20\%$ , lies in the region of high momentum *and* large removal energy

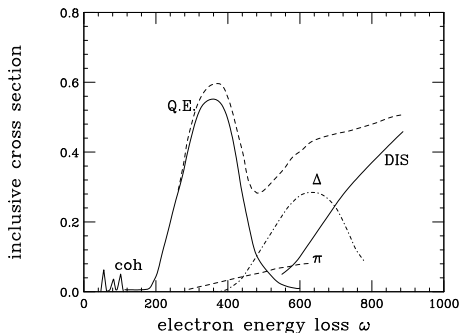
# Why should we need a new paradigm ?

- In neutrino interactions the lepton kinematics is *not* fully determined. The flux-integrated double differential cross sections picks up contributions from a variety of different kinematical regimes, in which different reaction mechanisms dominate



# Why should we need a new paradigm ?

- In neutrino interactions the lepton kinematics is *not* fully determined. The flux-integrated double differential cross sections picks up contributions from a variety of different kinematical regimes, in which different reaction mechanisms dominate
- Schematic view of the electron-nucleus cross section at beam energy in the few GeV region



- My own answer to the question raised in the title is yes, we do need a new paradigm

# Summary and outlook

- My own answer to the question raised in the title is yes, we do need a new paradigm
- More flexible models, *consistently* taking into account effects beyond the IA (two-body currents, pion production, final state interactions in the inelastic channels ...) must (and can) be developed

# Summary and outlook

- My own answer to the question raised in the title is yes, we do need a new paradigm
- More flexible models, *consistently* taking into account effects beyond the IA (two-body currents, pion production, final state interactions in the inelastic channels ...) must (and can) be developed
- State-of-the-art theoretical models must be used in the analysis of the experimental data, preferably (although not necessarily) through direct implementation in the simulation codes

# Summary and outlook

- My own answer to the question raised in the title is yes, we do need a new paradigm
- More flexible models, *consistently* taking into account effects beyond the IA (two-body currents, pion production, final state interactions in the inelastic channels ...) must (and can) be developed
- State-of-the-art theoretical models must be used in the analysis of the experimental data, preferably (although not necessarily) through direct implementation in the simulation codes