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# FLAVOR CONVERSIONS OF SUPERNOVA NEUTRINOS

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# OUTLINE



**Supernovae as neutrino sources**



**MSW effect in SNe: probing shock-waves and matter turbulences**



**Self-induced SN  $\nu$  oscillations: the collective behaviour of a dense  $\nu$  gas**



**Open Issues and Conclusions**

# SUPERNOVA NEUTRINOS

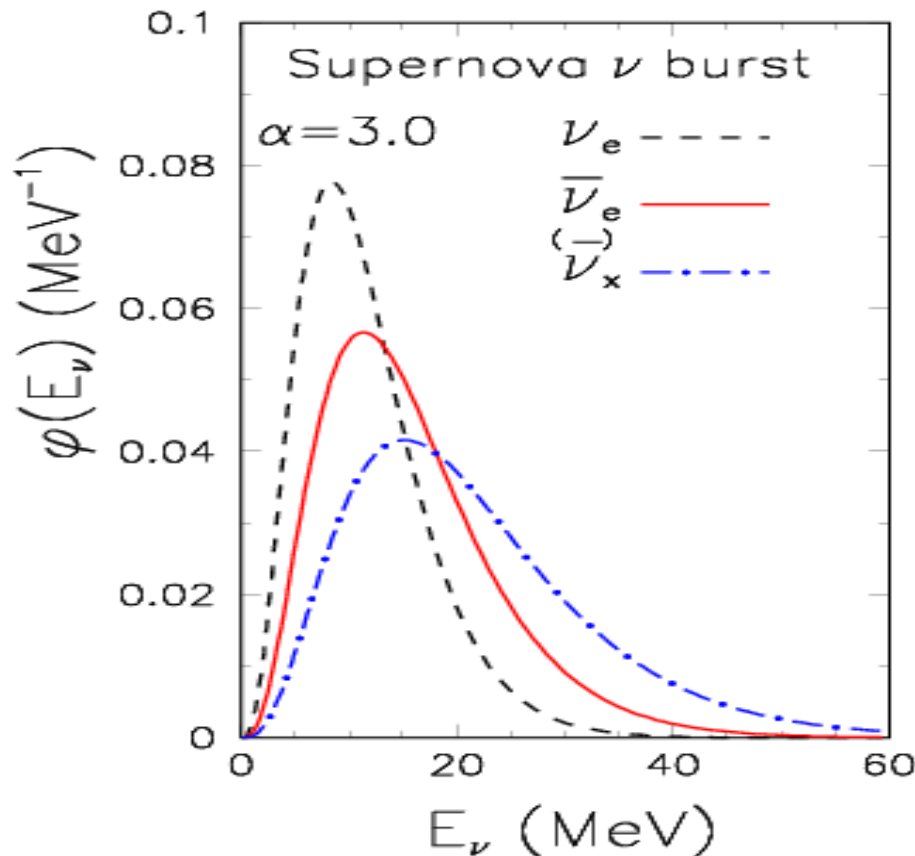
Core collapse SN corresponds to the terminal phase of a massive star [ $M \gtrsim 8 M_{\odot}$ ] which becomes unstable at the end of its life. It collapses and ejects its outer mantle in a shock wave driven **explosion**.



- **ENERGY SCALES:** 99% of the released energy ( $\sim 10^{53}$  erg) is emitted by  $\nu$  and  $\bar{\nu}$  of all flavors, with typical energies  $E \sim O(15 \text{ MeV})$ .
- **TIME SCALES:** Neutrino emission lasts  **$\sim 10 \text{ s}$**
- **EXPECTED:** **1-3 SN/century** in our galaxy ( $d \approx O(10) \text{ kpc}$ ).

# Neutrino spectra (in energy)

Time-integrated normalized  $\nu$  spectra



“quasi-thermal” spectra

Hierarchy of the spectra

$$\langle E_e \rangle \approx 9 - 12 \text{ MeV}$$

$$\langle E_{\bar{e}} \rangle \approx 14 - 17 \text{ MeV}$$

$$\langle E_x \rangle \approx 18 - 22 \text{ MeV}$$

These initial fluxes can be strongly modified by the peculiar effects of  
**FLAVOR CONVERSIONS** in SN

# SN $\nu$ FLAVOR TRANSITIONS

The flavor evolution in matter is described by the non-linear MSW equations:

$$i \frac{d}{dx} \psi_\nu = (H_{vac} + H_e + H_{\nu\nu}) \psi_\nu$$

In the standard  $3\nu$  framework

- $$H_{vac} = \frac{U M^2 U^\dagger}{2E}$$

**Kinematical mass-mixing term**

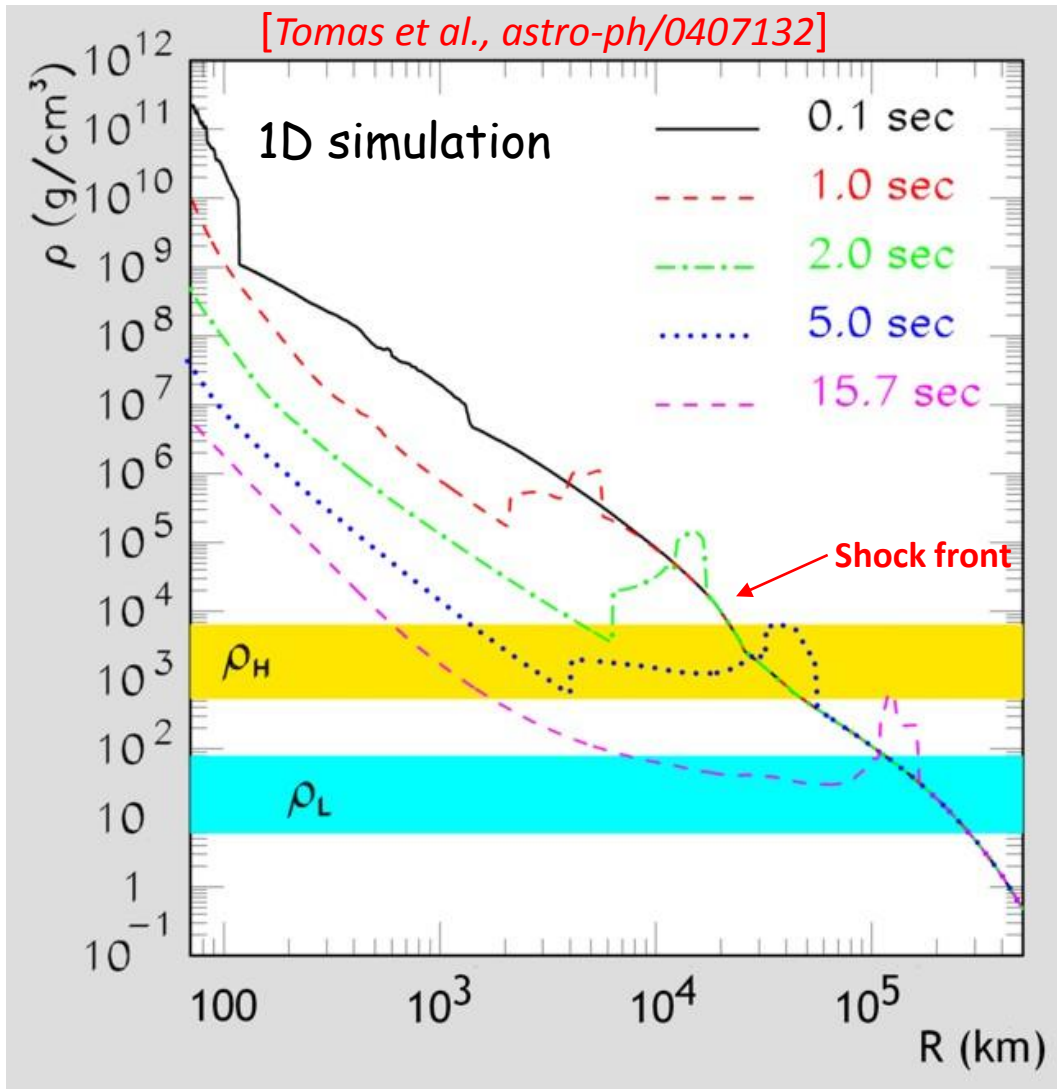
- $$H_e = \sqrt{2} G_F \text{diag}(N_e, 0, 0)$$

**Dynamical MSW term (in matter)**

- $$H_{\nu\nu} = \sqrt{2} G_F \int (1 - \cos \theta_{pq}) (\rho_q - \bar{\rho}_q) dq$$

**Neutrino-neutrino interactions term  
(non-linear)**

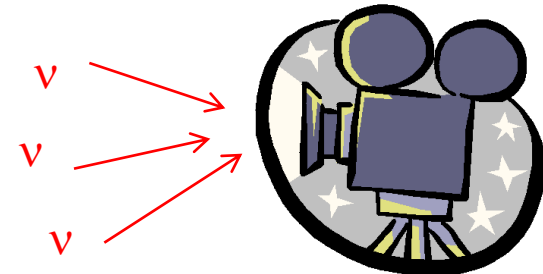
# MSW MATTER EFFECT IN SN



A few second after the core bounce, shock wave(s) can induce time-dependent matter effects in neutrino oscillations

[R.Schirato, and G. Fuller, astro-ph/0205390]

Neutrino oscillations as a “camera” for shock-wave propagation



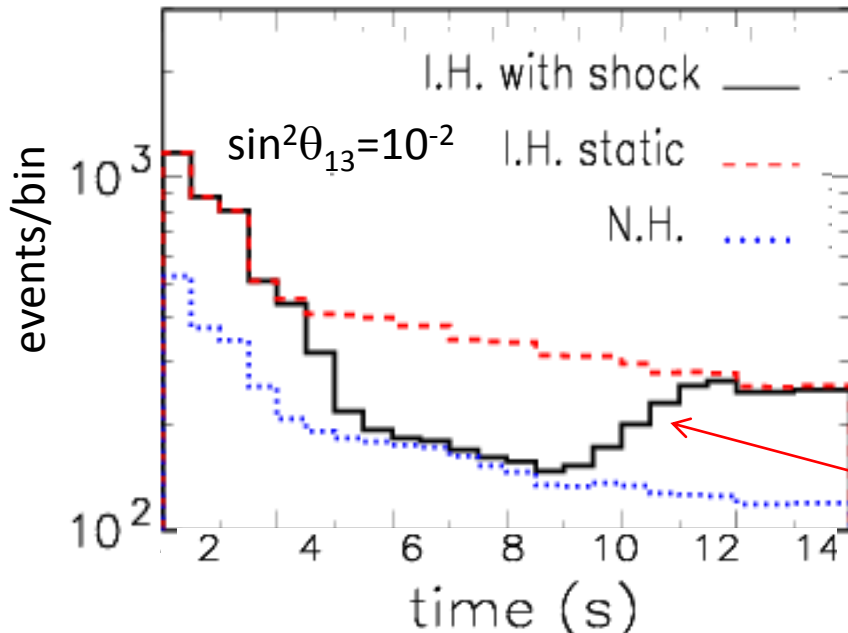
[see, e.g., Fogli, Lisi, A.M., and Montanino, hep-ph/0304056; Fogli, Lisi, A.M., and Montanino, hep-ph/0412046, Tomas et al., astro-ph/0407132, Choubey et al, hep-ph/0605255, Gava et al. 0902.0317,.... ]

# PROBING SHOCK WAVES AND MASS HIERARCHY AT LARGE $\theta_{13}$

0.4 Mton WC

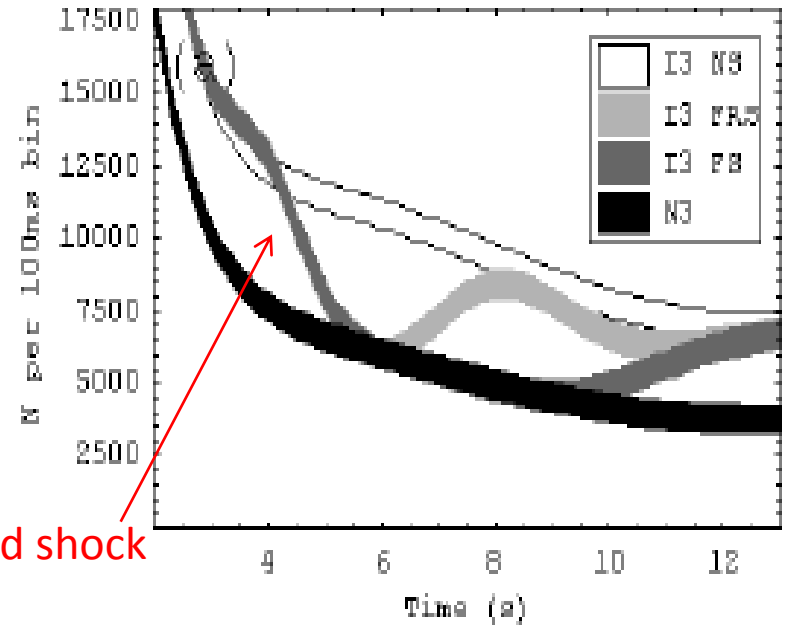


$E_{\text{POS}} = 45 \pm 5 \text{ MeV}$



[Fogli et al., hep-ph/0412046]

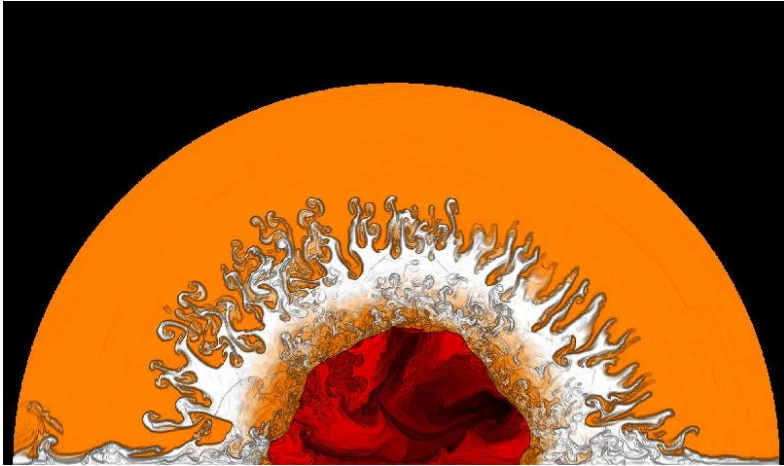
Icecube



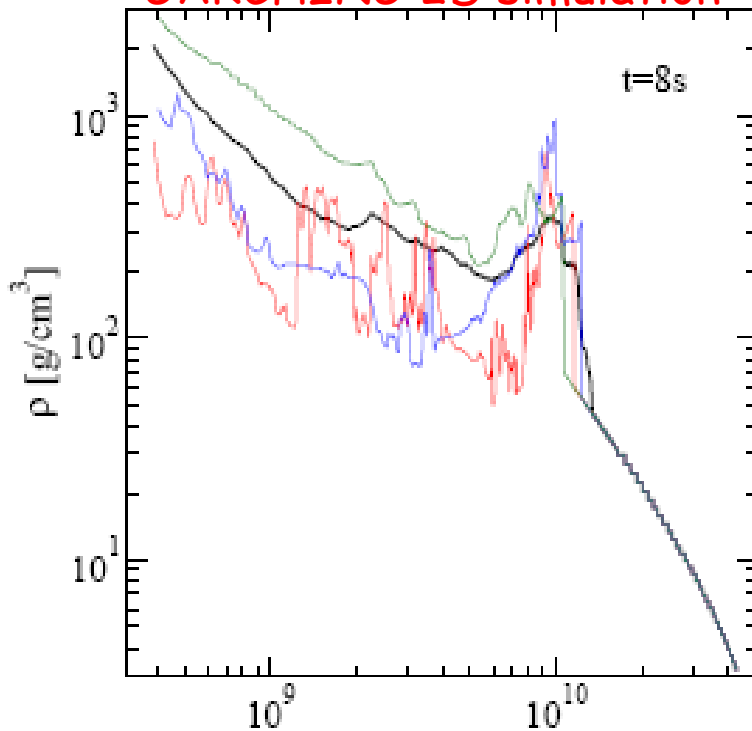
[Choubey et al, hep-ph/0605255]

In inverted hierarchy and for  $\theta_{13}$  not too small, flavor conversions along the shock-waves induce **non-monotonic** time spectra.

# STOCHASTIC DENSITY FLUCTUATIONS



GARCHING 2D simulation



Turbulent convective motions behind the shock front create a fluctuating density field in the post-shock region. A SN neutrino “beam” might thus experience stochastic matter effects while traversing the stellar envelope.

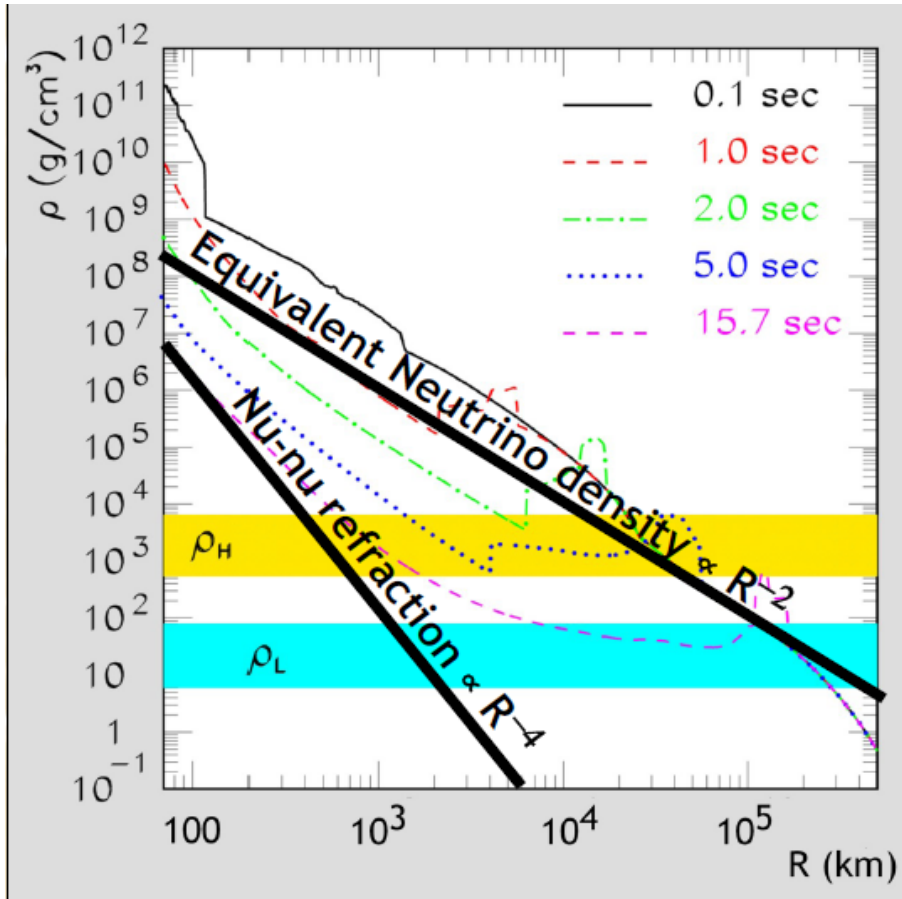
[Fogli, Lisi, A.M., Montanino, hep-ph/0603033; Friedland, astro-ph/0607244; Choubey, Harries, Ross, hep-ph/0703092, Kneller, 1004.1288, Kneller & Volpe, 1006.0913]

Depolarization ( $\langle P_{ee} \rangle \rightarrow \frac{1}{2}$ ) would replace the shock-signature when turbulence is relevant



# NEUTRINO-NEUTRINO INTERACTIONS

In the region just above the neutrino-sphere the neutrino density exceeds the ordinary electron background. Neutrinos themselves form a background medium



**$\nu$ - $\nu$  NC interactions important!**

- Matter bkg potential

$$V = \sqrt{2}G_F N_e \sim R^{-3}$$

- $\nu$ - $\nu$  potential ↙ Multi-angle effects

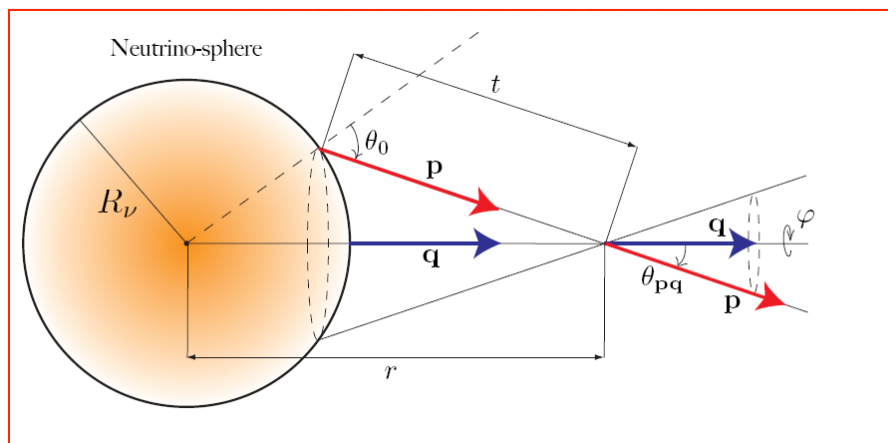
$$\mu = \sqrt{2}G_F n_\nu (1 - \cos \theta_{pq}) \sim R^{-2} \times R^{-2} = R^{-4}$$

Lesson: self-interactions ( $\mu$ ) can induce large, non-MSW flavor change at small radii, despite large matter density  $\nu$

Two seminal papers in 2006 triggered a torrent of activities

Duan, Fuller, Qian, astro-ph/0511275, Duan et al. astro-ph/0606616

# $\nu$ - $\nu$ INTERACTIONS: SINGLE-ANGLE APPROXIMATION



The structure of neutrino-neutrino interactions contains an angular modulation

"multi-angle case"

$$H_{\nu\nu} = \sqrt{2}G_F \int \frac{d^3\vec{q}}{(2\pi)^3} (1 - \cos\theta_{pq})(P_{\vec{q}} - \bar{P}_{\vec{q}})$$

Flavor polarization vectors

This makes very challenging the solution of the equations.

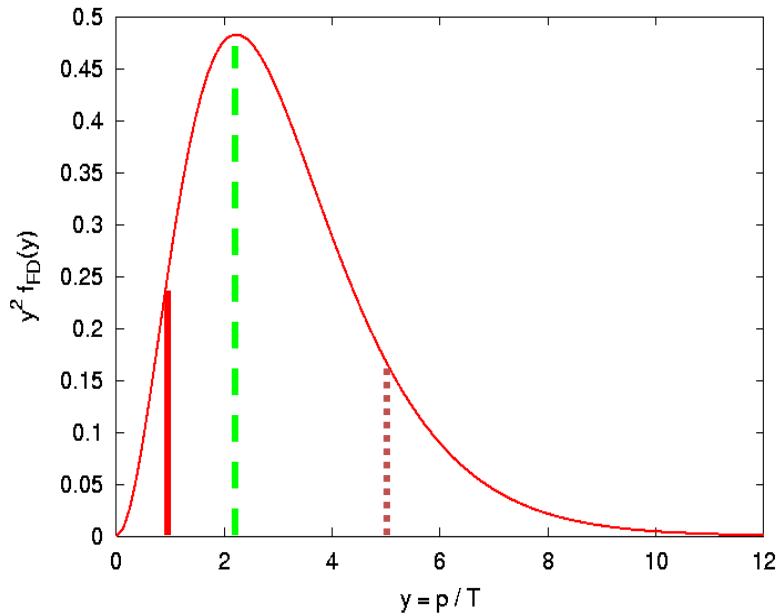
If averaged: **single-angle approximation**

$$H_{\nu\nu} = \mu \int dq (P_q - \bar{P}_q) = \mu(P - \bar{P})$$

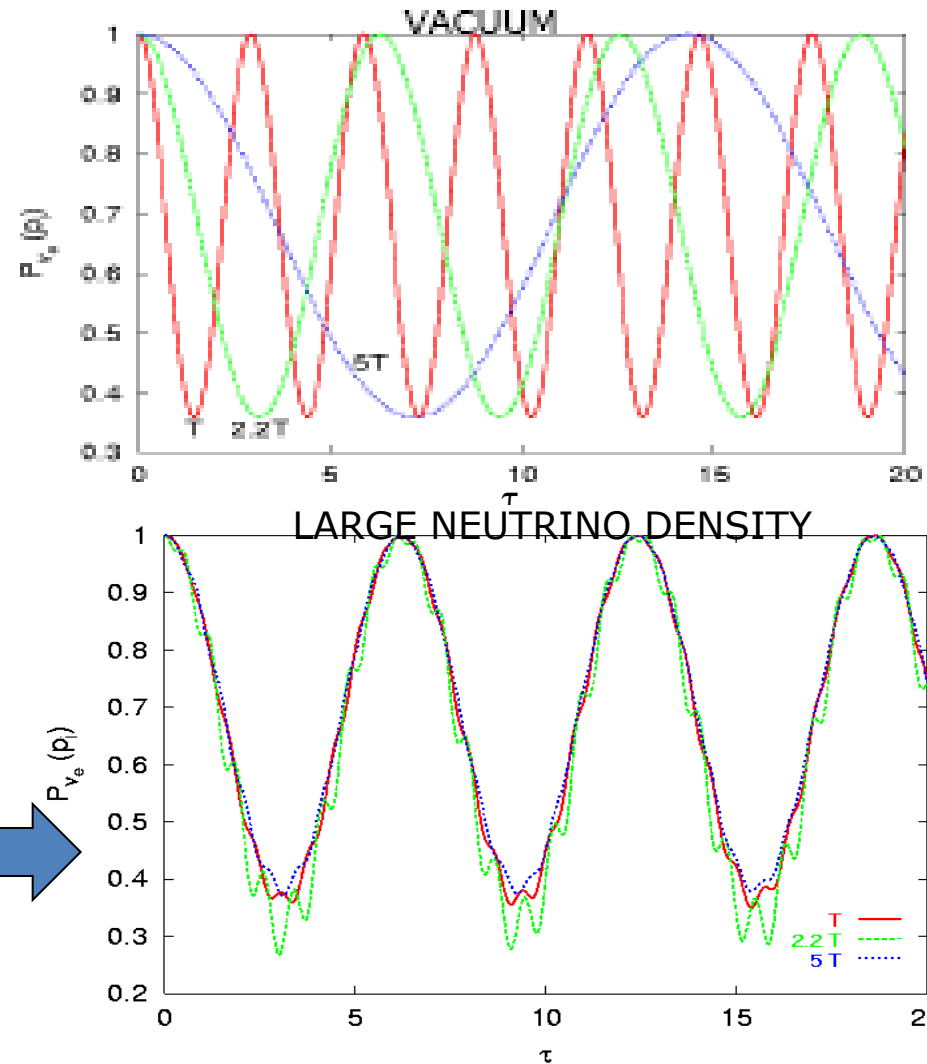
More amenable numerically. It allows for analytical interpretations.

# SYNCHRONIZED OSCILLATIONS BY NEUTRINO-NEUTRINO INTERACTIONS

Example: evolution of neutrino momenta with a thermal distribution



If neutrino density dominates, **synchronized oscillations** with a characteristic common oscillation frequency

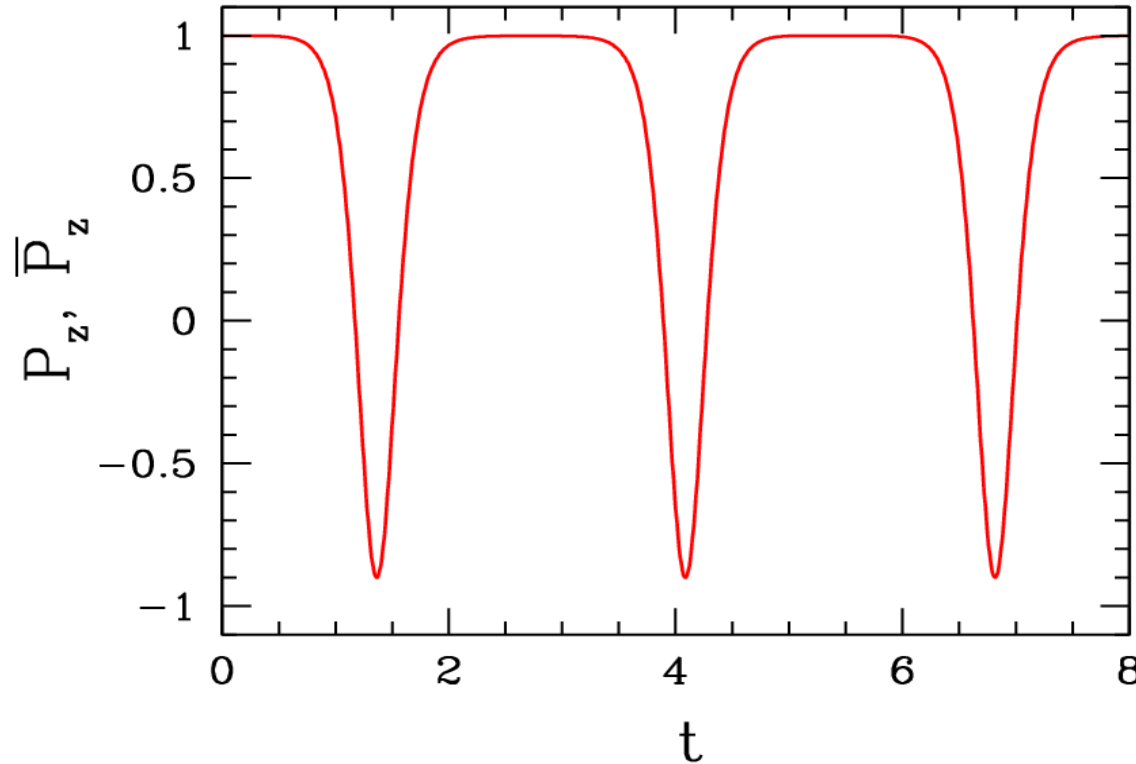


[Pastor, Raffelt, Semikoz, hep-ph/0109033]

# PENDULAR OSCILLATIONS

[Hannestad, Raffelt, Sigl, Wong, astro-ph/0608695]

Equal densities of  $\nu_e$  and  $\bar{\nu}_e$   
INVERTED HIERARCHY + small  $\theta$



In inverted hierarchy: coherent "pair conversions"  $\nu_e \bar{\nu}_e \longrightarrow \nu_\mu \bar{\nu}_\mu$

With constant  $\mu$ : periodic behaviour

# PENDULUM IN FLAVOR SPACE

[Hannestad, Raffelt, Sigl, Wong, astro-ph/0608695, Duan, Carlson, Fuller, Qian, astro-ph/0703776]

Neutrino mass hierarchy (and  $\theta_{13}$ ) set initial condition and fate

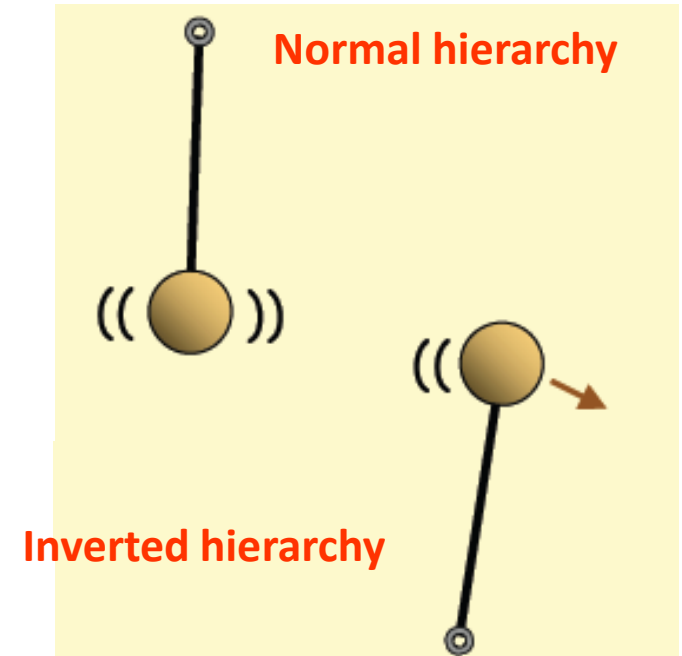
With only initial  $\nu_e$  and  $\bar{\nu}_e$ :

- **Normal hierarchy**

Pendulum starts in  $\sim$  downward (stable) positions and stays nearby. No significant flavor change.

- **Inverted hierarchy**

Pendulum starts in  $\sim$  upward (unstable) positions and eventually falls down. Significant flavor changes.



$\theta_{13}$  sets initial misalignment with vertical. Specific value not much relevant.

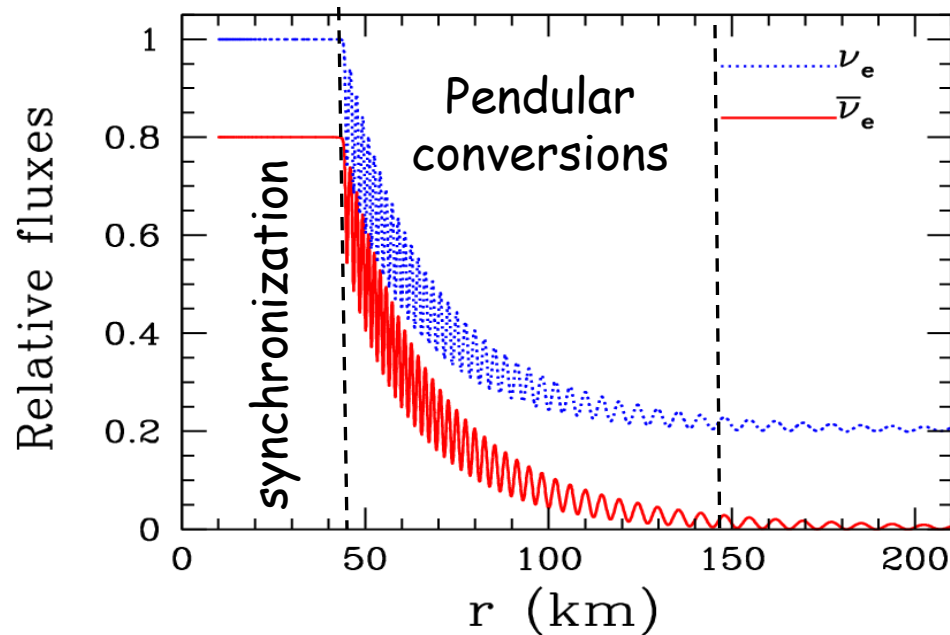
## Which mass hierarchy?

With only initial  $\nu_\mu$  and  $\bar{\nu}_\mu$  large flavor conversions in NH. The **unstable case** is when the initial ensemble consists of that flavor which is dominated by the heavier mass eigenstate.

# SUPERNOVA TOY-MODEL

[Hannestad, Raffelt, Sigl, Wong, astro-ph/0608695]

Only  $\nu_e$  and  $\bar{\nu}_e$



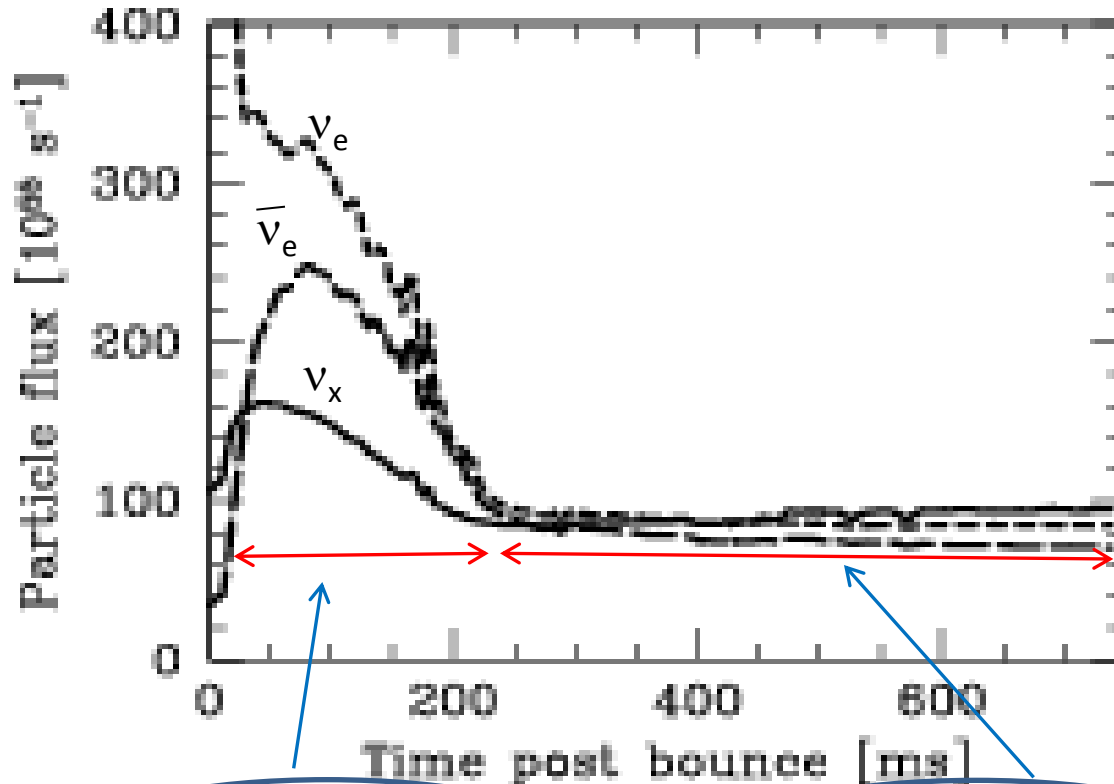
**SUPERNOVA: Non-periodic since  $\nu$  density decreases** 

**Complete flavor conversions!**

- Occurs for very small mixing angles
- Almost independent of the presence of dense normal matter
- Preserves the initial excess  $\nu_e$  over  $\bar{\nu}_e$  (lepton number conservation)

# NEUTRINO FLUX NUMBERS

[Raffelt et al. (Garching group), astro-ph/0303226]



Accretion phase

$$F_{\nu_e} > F_{\bar{\nu}_e} > F_{\nu_x}$$

Excess of  $\nu_e$  due to deleptonization

Cooling phase

$$F_{\nu_x} \geq F_{\nu_e} \geq F_{\bar{\nu}_e}$$

Moderate flavor hierarchy, possible excess of  $\nu_x$

# LARGE SCALE MULTI-ANGLE SIMULATIONS

$$H_{\nu\nu} = \sqrt{2}G_F \int \frac{d^3\vec{q}}{(2\pi)^3} (1 - \cos\theta_{pq})(P_{\vec{q}} - \bar{P}_{\vec{q}})$$

Different coupling strengths do not average in a non-isotropic medium, like  $\nu$  streaming off a SN core. Some sort of decoherence could be expected. Is the single-angle approximation a reasonable one?

## MULTI-ANGLE SIMULATIONS

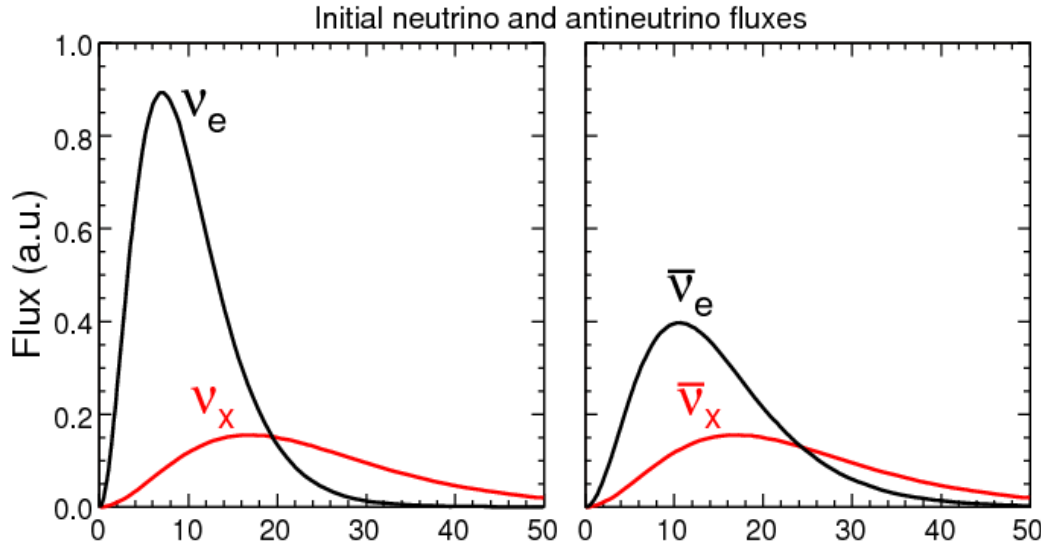
- **Accretion phase:** Duan, Fuller, Carlson & Qian, astro-ph/0606616, 0608050; Fogli, Lisi, Marrone & A.M., arXiv: 0707.1998, Fogli, Lisi, Marrone, A.M. & Tamborra, arXiv:0808.0807; Esteban-Pretel, Pastor, Tomas, Raffelt & Sigl, arXiv:0706.2498.
- **Cooling phase:** Duan & Friedland, arXiv: 1006.2359  $\longrightarrow$  See Friedland's poster
- **Neutronization burst O-Ne-Mg SNe:** Cherry et al., arXiv: 1006.2175

For typical SN  $\nu$  spectra observed an effective “quasi single-angle” behaviour  
However, how generic are these results?



# SPECTRAL SPLITS IN THE ACCRETION PHASE

[Fogli, Lisi, Marrone, *A.M.*, arXiv: 0707.1998 [hep-ph], Duan, Carlson, Fuller, Qian, astro-ph/0703776, Raffelt and Smirnov, 0705.1830 [hep-ph]]

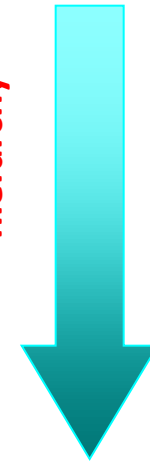


Initial fluxes at  
neutrinosphere ( $r \sim 10$  km)

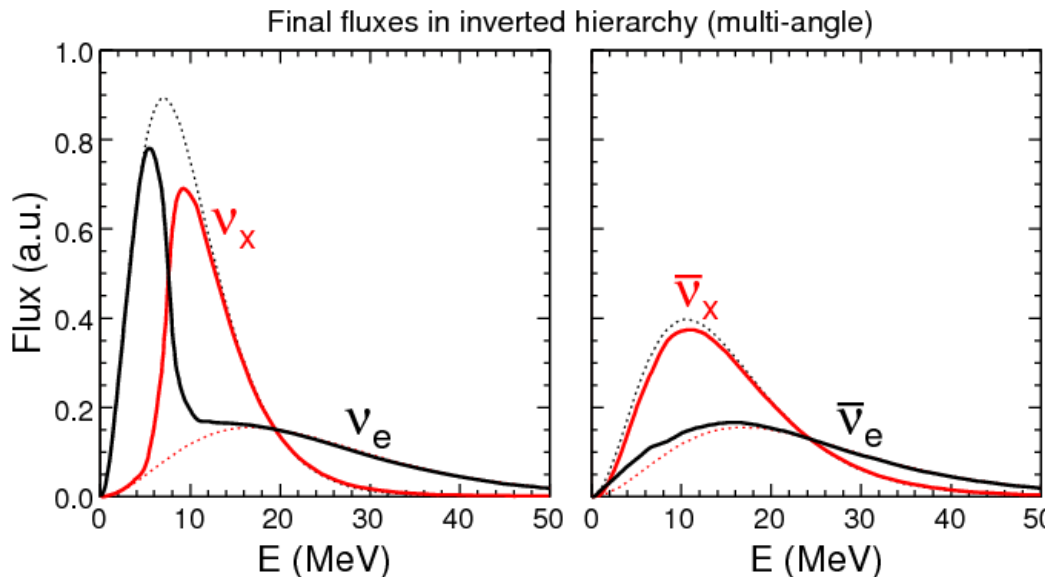
$$F_{\nu_e} : F_{\bar{\nu}_e} : F_{\nu_x} = 2.4 : 1.6 : 1.0$$

(ratio typical of accretion phase)

Inverted mass  
hierarchy



$$2\nu = (\Delta m^2, \theta_{13})$$



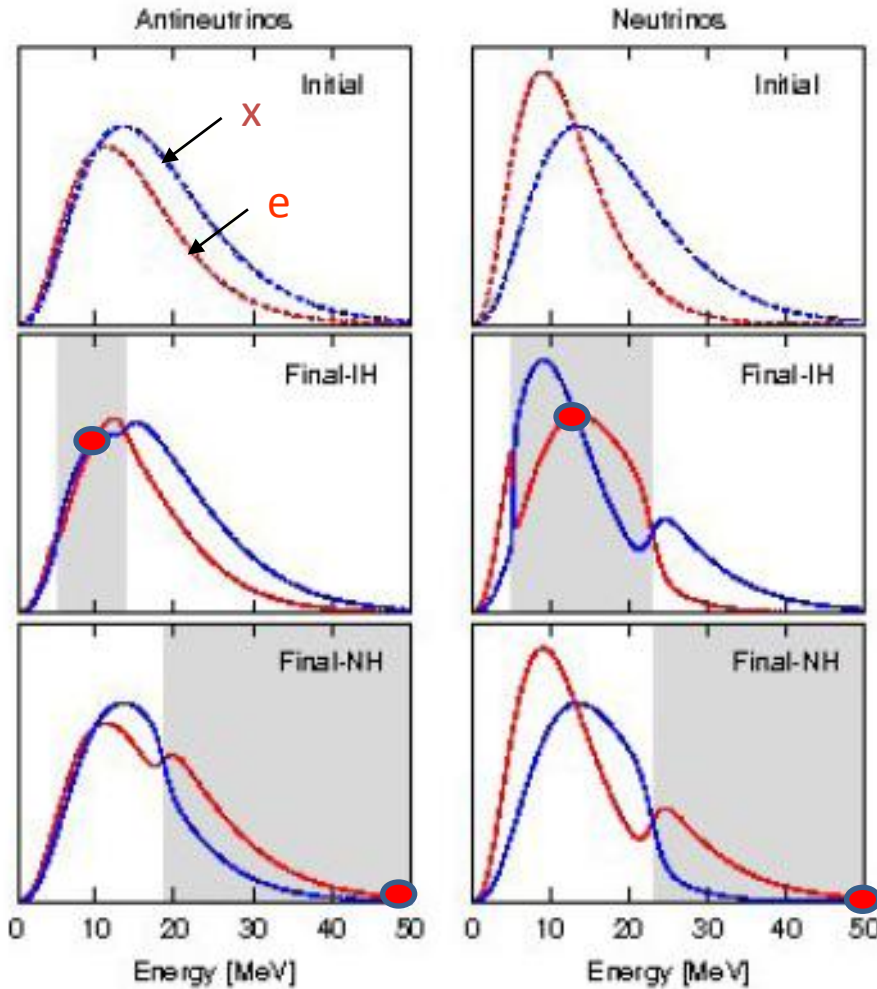
Fluxes at the end of collective  
effects ( $r \sim 200$  km)

Nothing happens in NH

# MULTIPLE SPECTRAL SPLITS IN THE COOLING PHASE

[Dasgupta, Dighe, Raffelt & Smirnov, arXiv:0904.3542 [hep-ph]]

$$2\nu = (\Delta m^2, \theta_{13})$$



$$F_{\nu e} : F_{\bar{\nu} e} : F_{\nu x} = 0.85 : 0.75 : 1.00$$

(possible during the cooling phase)

Splits possible in both normal and inverted hierarchy, for  $\nu$  &  $\bar{\nu}$ !!

Splits develops around the **crossing points** of the spectra (expect at  $E=0$ )

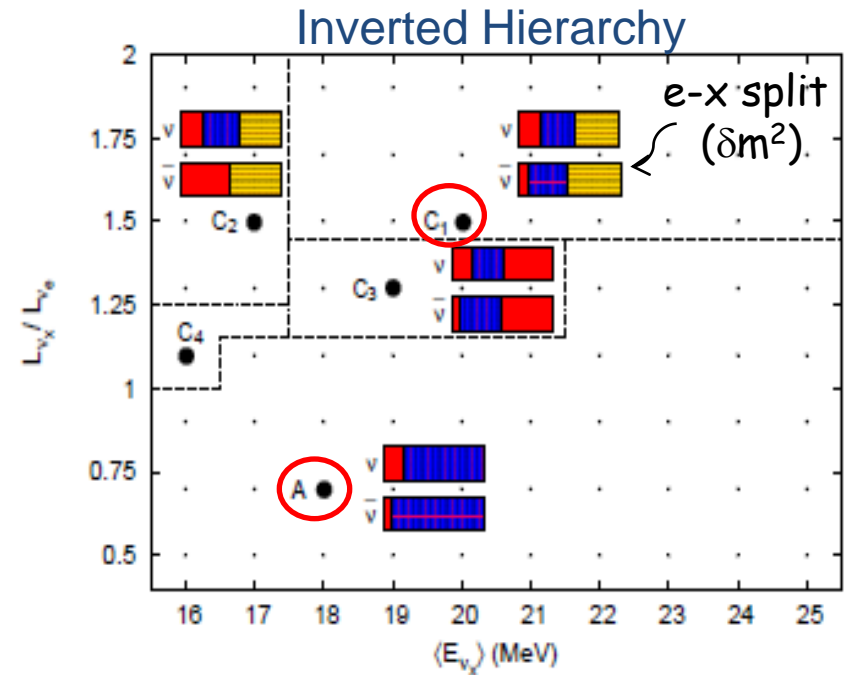
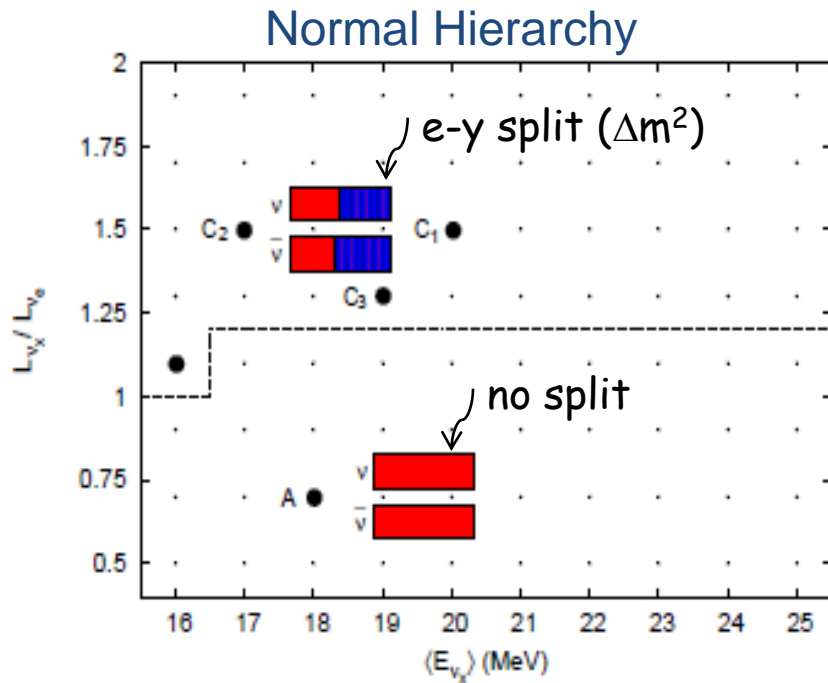
$$F_{\nu e}(E_c) - F_{\nu x}(E_c) = 0$$

THREE FLAVOR EFFECTS RELEVANT IN IH

See posters by Friedland and Tamborra

# PHASE DIAGRAM OF SPECTRAL SPLITS

[Choubey, Dasgupta, Dighe, & A.M., to appear soon]



Scan of the parameter space with  $3\nu$  simulations (S.A., 80 cases).

Abrupt changes of the split pattern btw different regions of the parameter space (in agreement with [Fogli, Lisi, Marrone, Tamborra, arXiv:0907.5115])

# OPEN ISSUES



## Theoretical issues

Robustness of the collective behavior vs. multi-angle decoherence effects. Reduced symmetries.



## Realistic SN environment

How asphericities, inhomogeneities, turbulence during the SN explosion might influence neutrino-neutrino interaction effects.



## Feedback on SN explosion simulations

Collective effects occur in a crucial region for SN dynamics and for nucleosynthesis. SN explosion simulations do not account for neutrino oscillations.



## Beyond the SM

Possible new  $\nu$ - $\nu$  interactions beyond SM might profoundly change the current picture.

# CONCLUSIONS

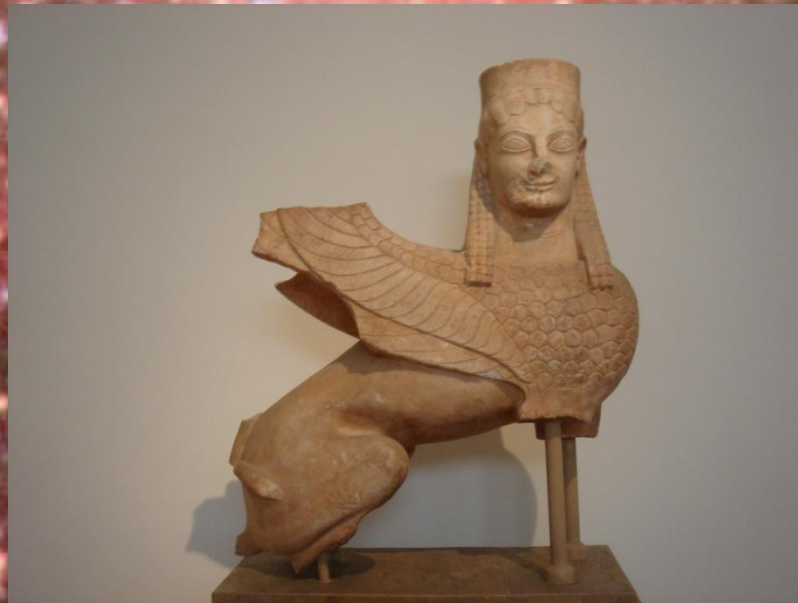
Observing SN neutrinos is the next frontiers of low-energy neutrino astronomy

The physics potential of current and next-generation detectors in this context is enormous, both for particle physics and astrophysics.

SNe provide very extreme conditions, where shock-waves, matter turbulences, neutrino-neutrino interactions prove to be surprisingly important for the  $\nu$  oscillations.

Further investigations needed to better understand neutrino flavor conversions during a stellar collapse.

Therefore, waiting the next galactic SN....



...Still lot of work to decipher the enigma