## NSTAR2019

The 12th International Workshop on the Physics of Excited Nucleons 10-14 June 2019, Bonn, Campus Poppelsdorf

EtaMAID for $\eta$ and $\eta^{\prime}$ photoproduction on nucleons
V. L. Kashevarov (Mainz University, Germany \& DLNP JINR Dubna, Russia) for Mainz - Tuzla - Zagreb Collaboration

## https://maid.kph.uni-mainz.de

 MAIDPhoto- and Electroproduction of Pions, Etas and Kaons on the Nucleon

## Institut für Kernphysik, Universität Mainz

Mainz, Germany

| MAID2007 | unitary isobar model for $\left(\mathrm{e}, \mathrm{e}^{\prime} \pi\right)$ |
| :--- | :--- |
| DMT2001 | dynamical model for $\left(\mathrm{e}, \mathrm{e}^{\prime} \pi\right)$ |
| KAON-MAID | isobar model for $\left(\mathrm{e}, \mathrm{e}^{\prime} \mathrm{K}\right)$ |
| ETA-MAID | isobar model for $\left(\mathrm{e}, \mathrm{e}^{\prime} \eta\right)$ |
| reggeized isobar model for $(\gamma, \eta)$ |  |
| Chiral MAID | new |
| chiral perturbation theory approach for $\left(\mathrm{e}, \mathrm{e}^{\prime} \pi\right)$ |  |
| 2-PION-MAID | isobar model for $(\gamma, \pi \pi)$ |
| archive | MAID2000 MAID2003 DMT2001original ETAprime2003 |

## History of MAID

The first MAID program appeared in 1998:

1. D. Drechsel, O. Hanstein, S. S. Kamalov, L. Tiator, Unitary isobar model for pion photoproduction and electroproduction on the proton up to $1-\mathrm{GeV}$, Nucl. Phys. A 645 (1999) 145.

Soon afterwards the Dubna-Mainz-Taipei (DMT) dynamical model was developed:
2. S. S. Kamalov, Shin Nan Yang,

Pion cloud and the $\mathrm{Q}^{* *} 2$ dependence of gamma* N <---> Delta transition form-factors, Phys. Rev. Lett. 83 (1999) 4494.
3. S. S. Kamalov, S. N. Yang, D. Drechsel, O. Hanstein, L. Tiator, Gamma* N ---> Delta transition form-factors: A New analysis of the JLab data ... Phys. Rev. C 64 (2001) 032201.

## History of MAID



Sabit Kamalov 15.09.1955-24.05.2019

## MTZ Collaboration

> Now MAID is part of research program of Mainz - Tuzla - Zagreb Collaboration

Mainz: Misha Gorchteyn, Victor Kashevarov, Kirill Nikonov, Michael Ostrick, Lothar Tiator

Tuzla: Mirza Hadžimehmedović, Rifat Omerović, Hedim Osmanović, Jugoslav Stahov

Zagreb: Alfred Švarc
Two more presentations of MTZ Collaboration:

1. Alfred Švarc, June 12, Wednesday, 16:30
2. Misha Gorchteyn, June 12, Wednesday, 17:30

## EtaMAID 2018

## The first version of EtaMAID:

W. T. Chiang, S. N. Yang, L. Tiator, D. Drechsel, Nucl.Phys. A 700 (2002) 429.

## photoproduction amplitudes

$$
t_{\alpha}(W)=t_{\alpha}^{B g r}(W)+t_{\alpha}^{R e s}(W)
$$

$t_{\alpha}^{B g r}: \quad$ Born $+t$-channel vector and axial-vector exchanges
$t_{\alpha}^{\text {Res }}: \quad \sum_{i=1}^{n}\{$ Breit-Wigner resonances $N, \Delta\}$
MAID2007 $(\gamma, \pi): 2 \mathrm{~S}_{11}$, for all other channels only 1 resonance N and $\Delta$ $\operatorname{EtaMAID} 2018(\gamma, \eta): 4 \mathrm{P}_{11}, 3 \mathrm{~S}_{11}, 4 \mathrm{D}_{13}, \ldots$ only N no $\Delta$

- unitarity
- fixed- $t$ analyticity
- duality
(Watson's theorem, coupled channels!) (dispersion relations!)
(problematic with Regge models!)


## EtaMAID 2018: unitarity aspects

In previous versions of EtaMAID 2002-2017 this apect was ignored.

## EtaMAID 2018:

- No unitarization for background;
- Unitarity phases for Breit-Wigner resonances do not depend on energy W and are determined from fit to data, just like in pion photoproduction above two-pion thresold.

$$
t_{\gamma, \eta}^{\alpha}(W)=t_{\gamma, \eta}^{\alpha, B o r n}(W)+t_{\gamma, \eta}^{\alpha, V M(\text { Regge })}(W) \cdot F_{d}(W)
$$

$$
\begin{aligned}
& +\sum_{j=1}^{N_{\alpha}} t_{\gamma, \eta}^{\alpha, B W, j}(W) \cdot e^{i \Phi_{j}} \\
& \text { phenomenological phase } \\
& \text { taken as a free parameter }
\end{aligned}
$$

## EtaMAID 2018: duality

from quark-hadron duality it is known:
sum over all $s$-channel resonances is equivalent to sum over all t-channel resonances therefore: keeping both leads to double counting

$$
\begin{aligned}
M & =\sum_{i=1}^{\infty} M_{s}^{R e s_{i}}=\sum_{i=1}^{\infty} M_{t}^{R e s_{i}}=\sum_{i=1}^{N} M_{s}^{R e s_{i}}+\left[\sum_{i=1}^{\infty} M_{t}^{R e s_{i}}-\sum_{i=1}^{N} M_{s}^{R e s_{i}}\right] \\
& \approx \sum_{i=1}^{N} M_{s}^{R e s_{i}}+M^{R e g g e} \cdot F_{d}(W) \quad \text { :our approach }
\end{aligned}
$$

## Regge + Resonances

## Duality: $\quad \sum$ Resonances $=\sum$ Reggeons

A. Sibirtsev, J. Haidenbauer, S. Krewald, U. G. Meissner, and A. W. Thomas, EPJA 41, 71 (2009)


## EtaMAID 2018: modelling the background

- Born terms in s and u channels + Regge trajectories in t channel
- Energy dependence coupling constants for Born terms:

$$
\mathrm{g} \rightarrow \mathrm{~g} *\left(\mathrm{~W}_{\mathrm{thr}} / \mathrm{W}\right)^{* *} \text { parB, fit parameter parB }=4.51(\eta), 3.95(\eta \text { ' })
$$

- Regge $\rightarrow$ Regge $*$ damping factor $f_{d}(\mathrm{~W})$
fit parameter $\Lambda=970 \mathrm{MeV}(\eta), 440 \mathrm{MeV}(\eta$ ')



## EtaMAID 2018

total number of data points: 10,700 - our overall $\chi^{2} /$ data in the fit is 2.46

|  |  | Observable | Reaction | used | $W$ [MeV] | $N$ | $\chi^{2}$ | $\chi^{2} / N$ | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\eta \mathrm{P}$ | 00000200000 | $\sigma_{0}$ | $p(\gamma, \eta) p$ | - | 1488-1870 | 2880 | 9502 | 3.3 | A2MAMI-17 (Run I) |
|  |  | $\sigma_{0}$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1488-1891 | 2712 | 4437 | 1.6 | A2MAMI-17 (Run II) |
|  |  | $\sigma_{0}$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1888-1957 | 288 | 329 | 1.1 | A2MAMI-17 (Run III) |
|  |  | $\sigma_{0}$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1965-2795 | 634 | 2276 | 3.6 | CLAS-09 |
|  |  | $\sigma_{0}$ | $p(\gamma, \eta) p$ | - | 1588-2370 | 680 | 8640 | 13. | CBELSA/TAPS-09 |
|  |  | $\Sigma$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1496-1908 | 150 | 394 | 2.6 | GRAAL-07 |
|  |  | $\Sigma$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1700-2080 | 214 | 617 | 2.9 | CLAS-17 |
|  |  | $T$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1497-1848 | 144 | 246 | 1.7 | A2MAMI-14 |
|  |  | $F$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1497-1848 | 144 | 246 | 1.7 | A2MAMI-14 |
|  |  | $E$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1525-2125 | 73 | 155 | 2.1 | CLAS-16 |
|  |  | $E$ | $p(\gamma, \eta) p$ | $\sqrt{ }$ | 1505-1882 | 135 | 255 | 1.9 | A2MAMI-17 |
| $\eta \mathrm{n}$ | $\begin{aligned} & \infty \\ & 0 \\ & 0 \\ & \text { n } \end{aligned}$ | $\sigma_{0}$ | $n(\gamma, \eta) n$ | $\sqrt{ }$ | 1492-1875 | 880 | 3079 | 3.5 | A2MAMI-14 |
|  |  | $\sigma_{0}$ | $n(\gamma, \eta) n$ | - | 1505-2181 | 322 | 2986 | 9.3 | CBELSA/TAPS-11 |
|  |  | $\Sigma$ | $n(\gamma, \eta) n$ | $\sqrt{ }$ | 1504-1892 | 99 | 177 | 1.8 | GRAAL-08 |
|  |  | $E$ | $n(\gamma, \eta) n$ | $\sqrt{ }$ | 1505-1882 | 135 | 209 | 1.5 | A2MAMI-17 |
| $\eta^{\prime} \mathrm{p}$ | $\begin{aligned} & \text { ๗ } \\ & \text { O } \\ & \sim \\ & \sim \end{aligned}$ | $\sigma_{0}$ | $p\left(\gamma, \eta^{\prime}\right) p$ | $\sqrt{ }$ | 1898-1956 | 120 | 198 | 1.7 | A2MAMI-17 |
|  |  | $\sigma_{0}$ | $p\left(\gamma, \eta^{\prime}\right) p$ | $\sqrt{ }$ | 1925-2795 | 681 | 2013 | 3.0 | CLAS-09 |
|  |  | $\sigma_{0}$ | $p\left(\gamma, \eta^{\prime}\right) p$ | - | 1934-2351 | 200 | 278 | 1.4 | CBELSA/TAPS-09 |
|  |  | $\Sigma$ | $p\left(\gamma, \eta^{\prime}\right) p$ | $\sqrt{ }$ | 1903-1913 | 14 | 35 | 2.5 | GRAAL-15 |
|  |  | $\Sigma$ | $p\left(\gamma, \eta^{\prime}\right) p$ | $\sqrt{ }$ | 1904-2080 | 62 | 85 | 1.4 | CLAS-17 |
| $\eta^{\prime} \mathrm{n}$ | - | $\sigma_{0}$ | $n\left(\gamma, \eta^{\prime}\right) n$ | $\sqrt{ }$ | 1936-2342 | 170 | 191 | 1.1 | CBELSA/TAPS-11 |

## Regge model for background

Diff. cross sections and polarisation observables for $\gamma p \rightarrow \eta p$ at high energies comparison with different Regge models
__ our favoured Regge-cut model

V. L. Kashevarov, M. Ostrick, L. Tiator , Phys. Rev. C96 (2017) 045207

## Fit results: total cross sections

$$
\gamma N \rightarrow \eta^{\prime} N
$$



$$
\gamma N \rightarrow \eta N
$$

Lines: full solution for $\gamma p$ (red) and $\gamma \mathrm{n}$ (black) channels.

$$
\begin{array}{ll}
\gamma p \rightarrow \eta p: \chi^{2}=238.6 / 125 \approx 1.91 ; & Y p \rightarrow \eta^{\prime} p: \chi^{2}=9.46 / 12 \approx 0.79 \text { (A2MAMI) } \\
\gamma n \rightarrow \eta n: \chi^{2}=120.6 / 44 \approx 2.74 ; & Y n \rightarrow \eta^{\prime} n: \chi^{2}=10.9 / 17 \approx 0.64
\end{array}
$$

## $\gamma p \rightarrow \eta p$

## Fit results: $\mathrm{d} \sigma / \mathrm{d} \Omega$



$$
\chi^{2}=2265 / 634 \approx 3.57
$$

Data: CLAS-09
Lines: red - full solution; solid black - Regge+Born; dashed - Regge ; dotted - Born terms

Fit results: partial contribution of resonances



Black dashed line - Regge + Bonrn contribution

## Fit results: partial waves contribution (no bgr)


$\mathrm{S}_{11}$ - black solid;
$\mathrm{P}_{11}$ - magenta solid; $\quad \mathrm{P}_{13}$ - magenta dashed
$\mathrm{D}_{13}$ - green solid; $\quad \mathrm{D}_{15}$ - green dashed
$\mathrm{F}_{15}$ - blue solid; $\quad \mathrm{F}_{17}$ - blue dashed
G 17 - cyan solid

## $\gamma p \rightarrow \eta p$

Fit results: $\Sigma$


Data: black - GRAAL-07;

$$
X^{2}=531.8 / 150 \approx 3.55
$$

green - CBELSA/TAPS preliminary

$$
X^{2}=694.1 / 214 \approx 3.24
$$

$$
X^{2}=309.5 / 156 \approx 1.98
$$

## $\gamma p \rightarrow \eta p$

## Fit results: $\Sigma$

Partial contributions of resonances

$N(2120) 3 / 2^{-}$and $N(2060) 5 / 2^{-}$interference explains the shape of the angular distributions.
Overall status for both resonances in PDG-2019:
But status for $(\eta \mathrm{N})$ : 0 for $\mathrm{N}(2120) 3 / 2^{-}$and $*$ for $N(2060) 5 / 2^{-}$
Should be updated!
Excluding $\mathrm{N}(2000) 5 / 2+$ or $\mathrm{N}(1990) 7 / 2+$ from the fit practically does not affect the quality of $\Sigma$ data description.

## $\gamma n \rightarrow \eta n$

Fit results: $d \sigma / d \Omega$


Data: A2MAMI-14
Lines: full solution

## $\gamma n \rightarrow \eta n$

## Legendre coefficients



Partial wave content of Legendre coefficients, $\quad l_{\max }=3$

\[

\]

Data: A2MAMI-17;
Red lines: full solution

## Other PWA groups analyzing $(\gamma, \eta)$ and $\left(\gamma, \eta^{\prime}\right)$ data

BnGa: Bonn-Gatchina group:
A.V. Anisovich, E. Klempt, V.A. Nikonov, A.V. Sarantsev, and U. Thoma. Multi-channel K-matrix model and N/D dispersion approach.
Predictions up to $\mathrm{W}=2500 \mathrm{MeV}$ for 3 channels:

$$
\mathbf{p}(\gamma, \eta) \mathbf{p}, \mathbf{n}(\gamma, \eta) \mathbf{n}, \text { and } \mathbf{p}\left(\gamma, \eta^{\prime}\right) \mathbf{p}
$$

JüBo: Jülich-Bonn group:
D. Rönchen, M. Döring, H. Haberzettl, J. Haidenbauer, U.-G. Meißner, and K. Nakayama.
Covariant multi-channel dynamical model.
Predictions up to $\mathrm{W}=2380 \mathrm{MeV}$ for 1 channel: $\mathbf{p}(\gamma, \eta) \mathbf{p}$
KSU: Kent State University group:
B.C. Hunt and D.M. Manley.

Multi-channel K-matrix model.
Predictions for 2 channels: $\mathbf{p}(\gamma, \eta) \mathbf{p}$ up to $W=1990 \mathrm{MeV}$, $\mathbf{n}(\gamma, \eta)$ n up to $W=1870 \mathrm{MeV}$

Comparison with other new PWA



Red line: EtaMAID2018
Cyan line: BnGa
Blue line: KSU
Black line: JüBo

## $\gamma p \rightarrow \eta p$

Polarization observables T and F


Cyan line: BnGa
Blue line: KSU
Black line: JüBo
Data: A2MAMI-14
$\mathrm{T}: \chi^{2}=255.3 / 144 \approx 1.77 ; \quad \mathrm{F}: \chi^{2}=253.3 / 144 \approx 1.76$

## $\gamma n \rightarrow \eta n$

Beam asymmetry $\Sigma$












Red line: EtaMAID2018
Cyan line: BnGa
Blue line: KSU
$X^{2}=238.5 / 99 \approx 2.41$
Data: GRAAL-08

## $\gamma n \rightarrow \eta n$

Helicity beam asymmetry E


## Narrow resonance $\mathrm{S}_{11} / \mathrm{D}_{13}$ in $\mathrm{p}\left(\gamma, \eta^{\prime}\right) \mathrm{p}$ EtaMAID vs. BNGA


$\Sigma$ and d $\sigma / \mathrm{d} \Omega$ data can well be fitted with a very narrow resonance at $\mathrm{W}_{\mathrm{R}}=1900 \mathrm{MeV}$. In the total cross section such a resonance is invisible.
It shows up in interferences between $S-F$ or $P-D$ resonances

Narrow resonance $\mathrm{S}_{11} / \mathrm{D}_{13}$ in $\mathrm{p}\left(\gamma, \eta^{\prime}\right) \mathrm{p}$ EtaMAID vs. BNGA


## Narrow resonance in $\gamma \mathrm{p} \rightarrow \eta^{\prime} \mathrm{p}$ ?

Legendre fit with Lmax = 2 (black dashed) and Lmax $=3$ (red solid)


A2MAMI data from threshold up to $\mathrm{W}=1908.26$ are shown for each tagger bin

## Narrow resonance in $\gamma \mathrm{p} \rightarrow \eta^{\prime} \mathrm{p}$ ?

Legendre coefficients from fit with Lmax = 3


Red line at $\mathrm{W}=1.904 \mathrm{GeV}$

## Narrow resonance in $\gamma \mathrm{p} \rightarrow \eta^{\prime} \mathrm{p}$ ?



New EtaMAID solution for narrow resonance:

F15(1900)
$\mathrm{M}=1901 \mathrm{Mev}$
$\mathrm{G}=1.2 \mathrm{MeV}$


## Predictions for $\gamma \mathrm{p} \rightarrow \eta^{\prime} \mathrm{p}$



Red lines: EtaMAID 2018
Black lines: BnGa 2017

Black points: CBELSA/TAPS-09
Cyan points: CLAS-09

An Isobar Model for Eta and Etaprime Photoproduction on the Nucleon
Victor Kashevarov and Lothar Tiator

| Reference: |
| :---: |
| $\frac{\text { L. Tiator, M. Gorchtein, V.L. Kashevarov, K. Nikonov, M. Ostrick (Mainz), }}{\text { M. Hadzimehmedovic, R. Omerovic, H. Osmanovic, J. Stahov (Tuzla), }}$ |
| $\frac{\text { and A. Svarc (Zagreb),arXiv:1807.04525, }}{\text { Eur. Phys. J. A (2018) } 54: 210}$ |

- Electromagnetic Multipoles ( $\mathrm{E}_{\mathrm{l}}, \mathbf{M}_{l \pm}$ )
- CGLN and Helicity Amplitudes ( $\mathrm{F}_{1}, \ldots, \mathrm{~F}_{4}, \mathrm{H}_{1}, \ldots, \mathrm{H}_{4}$ )
- Observables (with beam, target and recoil polarization)
- Total Cross Sections


## Summary and conclusions

1. New version of EtaMAID for $\eta$ and $\eta$ ' photoproduction on protons and neutrons is finished and available on the MAID webpage.
2. The well-known duality problem is addressed in a new approach with a damping factor removing most of Regge background in the resonance region.
3. Unitarization was done by adding a phase for each resonance as free parameter.
4. New EtaMAID2018 describes all data very well and explains most of them: - cusp in eta total cross section, in connection with steep rise of the $\eta^{\prime}$ total cross section from its threshold, is explained by a strong coupling of $\mathrm{N}(1895) 1 / 2^{-}$to both channels;

- narrow bump in ( $\eta \mathrm{n}$ ) and dip in ( $\eta \mathrm{p}$ ) channels have different origin: the first is a result of interference of a few resonances, and the second is a threshold effect due to opening $K \Sigma$ decay channel of $\mathrm{N}(1650) 1 / 2^{-}$resonance;
- angular dependence of $\Sigma$ asymmetry for $\gamma \mathrm{p} \rightarrow \eta \mathrm{p}$ at $\mathrm{W}>2 \mathrm{GeV}$ is explained by an interference of $\mathrm{N}(2120) 3 / 2-$ and $\mathrm{N}(2060) 5 / 2^{-}$resonances.

5. The near threshold behavior of $\Sigma$ for $\gamma \mathrm{p} \rightarrow \eta^{\prime} \mathrm{p}$ is still an open question.
6. Possible narrow resonance with $M=1726 \mathrm{MeV}$ observed both in $\gamma p \rightarrow \eta p$ and $\gamma n \rightarrow \eta n$ reaction channels for $\sigma_{1 / 2}$ needs further investigation.
7. Next step: adding $\pi \mathrm{N}, \omega \mathrm{N}, \mathrm{K} \Lambda$, and $\mathrm{K} \Sigma$ channels.

## $\gamma p \rightarrow \eta p \quad$ Fit results: differential cross sections



Data: A2MAMI-17;
Lines: red - full solution; solid black - Regge+Born; dashed - Regge ; dotted - Born terms
$\gamma p \rightarrow \eta p$
Differential cross sections

$$
\chi^{2}=4679 / 2928 \approx 1.60
$$



Data: A2MAMI-17;
Lines: red - full solution; solid black - Regge+Born; dashed - Regge ; dotted - Born terms
$\gamma p \rightarrow \eta p$
Polarization observables: $\Sigma$



Red line: EtaMAID2018
Cyan line: BnGa
Blue line: KSU
Black line: JüBo
Data: black - GRAAL-07
red - CLAS-17
green - CBELSA/TAPS preliminary
$\gamma P \rightarrow \eta p \quad$ Polarization observables: E


Data: black - CLAS-16;

$$
X^{2}=170.6 / 73 \approx 2.34
$$

red - A2MAMI-17 " $p$ ";
$X^{2}=272.3 / 135 \approx 2.02$
green - CBELSA/TAPS preliminary

$$
X^{2}=395.5 / 93 \approx 4.25
$$



Data: CLAS-09
Lines: red - full solution;
solid black - Regge+Born; dashed - Regge ; dotted - Born terms
$\gamma \mathrm{n} \rightarrow \eta^{\prime} \mathrm{n}$
Differential cross sections
$X^{2}=279.9 / 170 \approx 1.64$


Data: CBELSA/TAPS-11
Lines: red - full solution;
solid black - Regge+Born; dashed - Regge ; dotted - Born terms 39

## EtaMAID 2018

amplitudes $A_{1 / 2}^{p(n)}$ for proton (neutron). The first row for each resonance gives a parameter set of the presented EtaMAID solution. The parameters indicated without errors were fixed during the fit. The second row indicate an overall status of the resonance and lists the corresponding parameters estimated by PDG [1] (NE means "No Estimates" given by PDG). The effective $\eta^{\prime} N$ branching ratios according to ref. [75] for the $N(1880) 1 / 2^{+}$and $N(1895) 1 / 2^{-}$are $(6.3 \pm 2) \%$ and $(19.5 \pm 5) \%$, respectively.

| Resonance $J^{P}$ | $M_{B W}[\mathrm{MeV}]$ | $\Gamma_{B W}[\mathrm{MeV}]$ | $\beta_{\eta N}[\%]$ | $A_{1 / 2}^{p}\left[10^{-3} \mathrm{GeV}^{-1 / 2}\right]$ | $A_{1 / 2}^{n}\left[10^{-3} \mathrm{GeV}^{-1 / 2}\right]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $N(1535) 1 / 2^{-}$ | $1522 \pm 8$ | $175 \pm 25$ | $34 \pm 5$ | +115 | $-102 \pm 8$ |
| $* * * *$ | $1530 \pm 15$ | $150 \pm 25$ | $42 \pm 13$ | $+105 \pm 15$ | $-75 \pm 20$ |
| $N(1650) 1 / 2^{-}$ | $1626_{-5}^{+10}$ | $133 \pm 20$ | $19 \pm 6$ | +55 | $-25 \pm 20$ |
| $* * * *$ | $1650 \pm 15$ | $125 \pm 25$ | $25 \pm 10$ | $+45 \pm 10$ | $-10_{-30}^{+40}$ |
| $N(1710) 1 / 2^{+}$ | $1670 \pm 20$ | $63_{-18}^{+55}$ | $12 \pm 4$ | 5.5 | $-42_{-12}^{+16}$ |
| $* * * *$ | $1710 \pm 30$ | $140 \pm 60$ | $30 \pm 20$ | NE | NE |
| $N(1880) 1 / 2^{+}$ | $1882 \pm 24$ | $90_{-30}^{+70}$ | $43_{-20}^{+10}$ | 60 | $-7_{-60}^{+60}$ |
| $* * *$ | $1880 \pm 50$ | $300 \pm 100$ | NE | NE | NE |
| $N(1895) 1 / 2^{-}$ | $1894.4_{-15}^{+5}$ | $71_{-13}^{+25}$ | $3.3 \pm 1.5$ | -32 | $+43_{-50}^{+30}$ |
| $* * * *$ | $1895 \pm 25$ | $120_{-40}^{+80}$ | $25_{-10}^{+15}$ | NE | NE |

However, our goal for nucleon resonance analysis is to get the pole positions and residues and error analysis for these more fundamental $\mathrm{N}^{*}$ properties.

