

# New Results in Strangeness Production with Polarization Observables

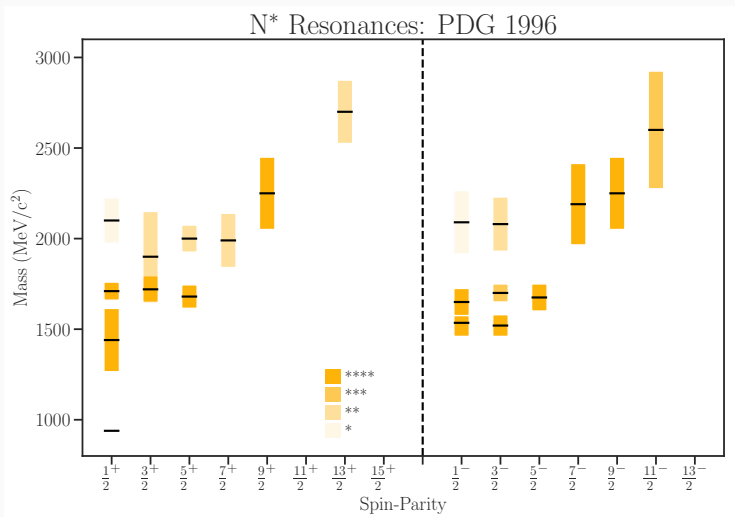
NSTAR 2019

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**D.G. Ireland**

13 June, 2019

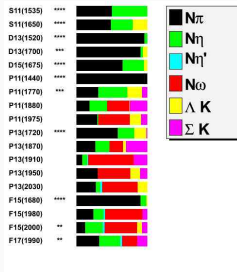
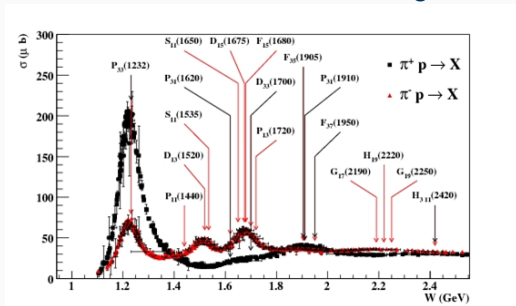
# Light Baryon Spectrum - PDG 1996<sup>1</sup> List of $N^*$ Resonances



<sup>1</sup>R.M. Barnett et al. In: *Phys. Rev. D* 54 (1996), p. 1.

# Resonance Hunting

Resonances found from  $\pi N$  scattering...



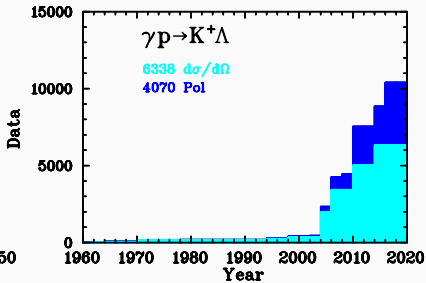
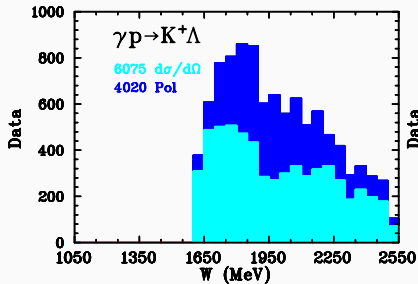
Coupling to other channels<sup>2</sup>?

<sup>2</sup>Simon Capstick and W. Roberts. "Strange decays of nonstrange baryons". In: *Phys. Rev. D* 58 (1998), p. 074011.

# Kaon Photoproduction

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# Kaon Photoproduction - $K\Lambda$ Experimental Database

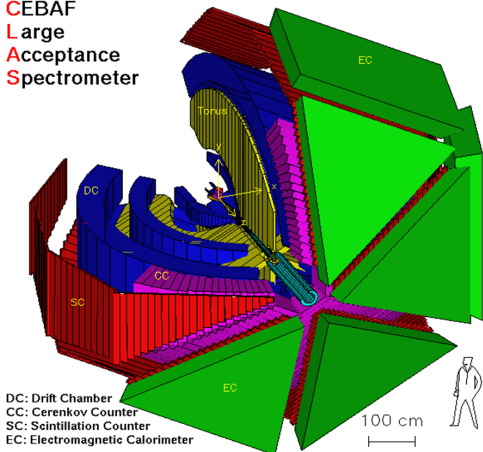


Accumulated  $K\Lambda$  data points

# Recent Experimental Data



**C**EBAF  
**L**arge  
**A**cceptance  
**S**pectrometer



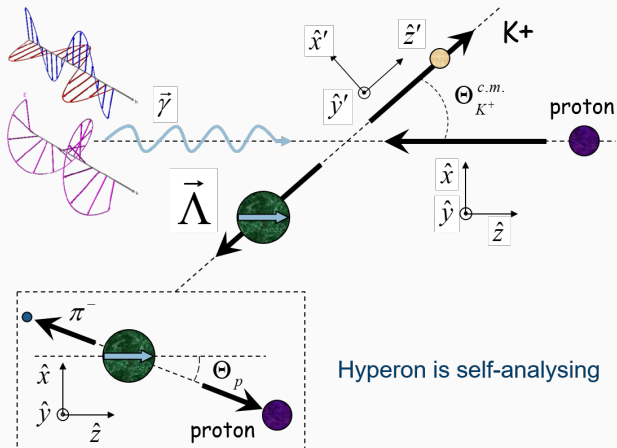
DC: Drift Chamber  
CC: Cerenkov Counter  
SC: Scintillation Counter  
EC: Electromagnetic Calorimeter

100 cm  
|-----|

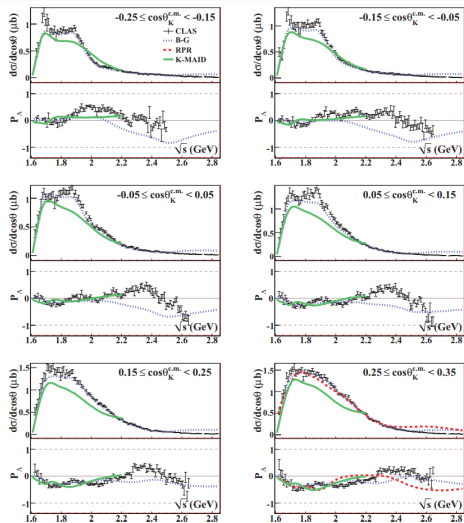


Data also from ELSA, GRAAL, LEPS, MAMI,...

# Kaon Photoproduction - $K\Lambda$ example



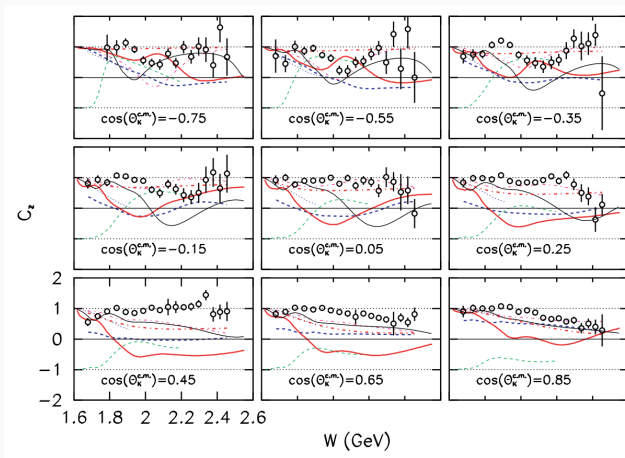
# $\gamma p \rightarrow K^+ \Lambda$ : Cross-sections and Recoil Polarizations<sup>3</sup>



<sup>3</sup>M. E. McCracken et al. "Differential cross section and recoil polarization measurements for the  $\gamma p \rightarrow K^+ \Lambda$  reaction using CLAS at Jefferson Lab". In: *Physical Review C* 81 (2010), p. 025201.

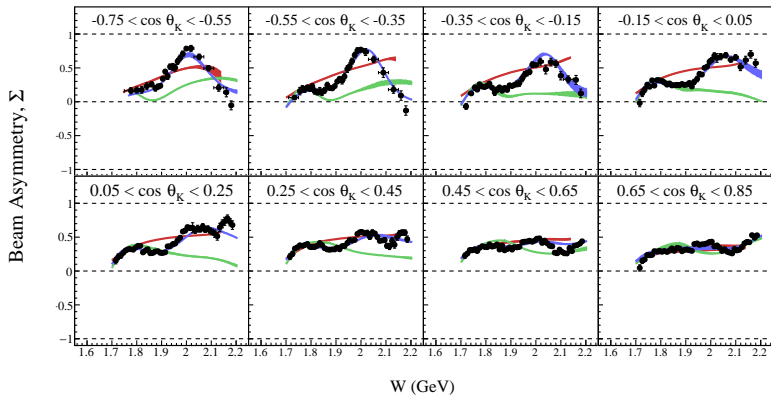


# $\gamma p \rightarrow K^+ \Lambda$ : Circular Beam-Recoil Observables<sup>4</sup>



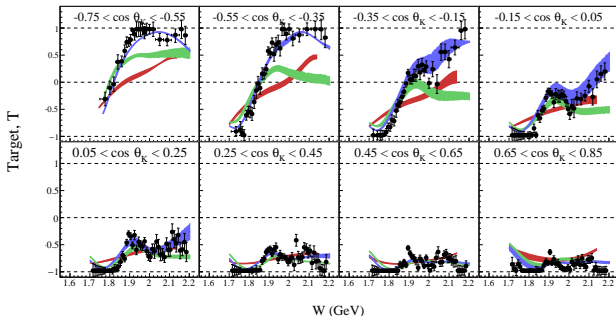
<sup>4</sup>RK Bradford et al. "First measurement of beam-recoil observables  $C_x$  and  $C_z$  in hyperon photoproduction". In: *Physical Review C* 75.3 (2007), p. 035205.

# $\gamma p \rightarrow K^+ \Lambda$ : Beam Asymmetry<sup>5</sup>



<sup>5</sup>C. A. Paterson et al. "Photoproduction of  $\Lambda$  and  $\Sigma^0$  hyperons using linearly polarized photons". In: *Phys. Rev. C* 93 (2016), p. 065201.

# $\gamma p \rightarrow K^+ \Lambda$ : Comparison with Models

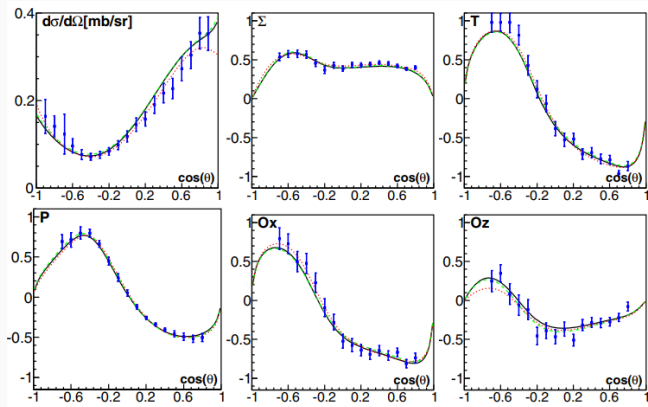


- Data Points: CLAS results;
- Red: ANL-Osaka calculations<sup>6</sup> (prediction);
- Green: Bonn-Gatchina 2014 fit<sup>7</sup> (BG2014-02, prediction);
- Blue: Bonn-Gatchina full re-fit with CLAS results;

<sup>6</sup>H. Kamano et al. "Nucleon resonances within a dynamical coupled-channels model of  $\pi N$  and  $\gamma N$  reactions". In: *Phys. Rev. C* 88 (2013), p. 035209.

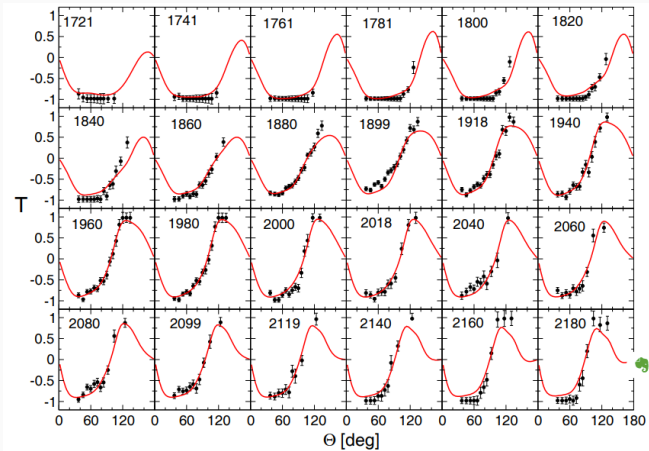
<sup>7</sup>E. Gutz et al. "High statistics study of the reaction  $\gamma p \rightarrow p\pi^0\eta$ ". In: *Eur. Phys. J. A* 50 (2014), pp. 1–27.

# $\gamma p \rightarrow K^+ \Lambda$ : L+P Model<sup>8</sup>



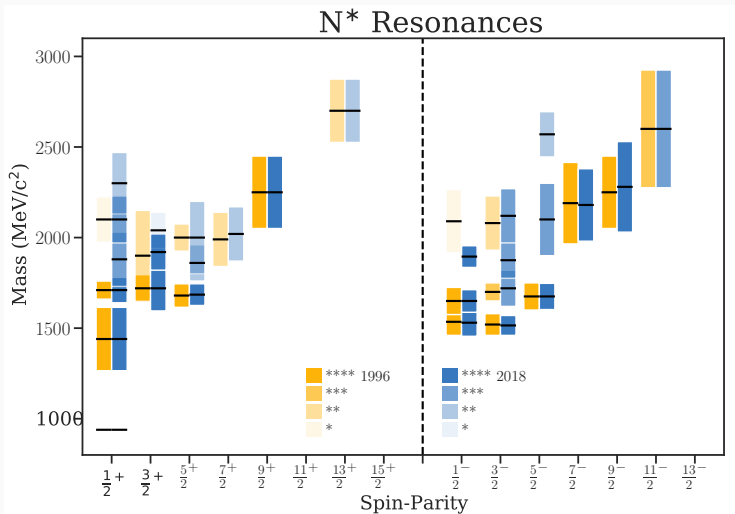
<sup>8</sup>A. V. Anisovich et al. "Strong Evidence for Nucleon Resonances near 1900 MeV".  
In: *Phys. Rev. Lett.* 119.6 (2017), p. 062004.

# $\gamma p \rightarrow K^+ \Lambda$ : Jülich-Bonn Coupled Channels<sup>9</sup>



<sup>9</sup>D. Rönchen, M. Döring, and U. -G. Meißner. “The impact of  $K + \Lambda$  photoproduction on the resonance spectrum”. In: *Eur. Phys. J. A* 54 (2018), p. 110.

# Light Baryon Spectrum - PDG 2018<sup>10</sup> List of $N^*$ Resonances



<sup>10</sup>(Particle Data Group) Tanabashi, M. et al. "Review of Particle Physics". In: *Phys. Rev. D* 98.3 (Aug. 2018), p. 030001.

## The Recent BESIII Result

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nature  
physics

Letter | Published: 06 May 2019

## Polarization and entanglement in baryon-antibaryon pair production in electron-positron annihilation

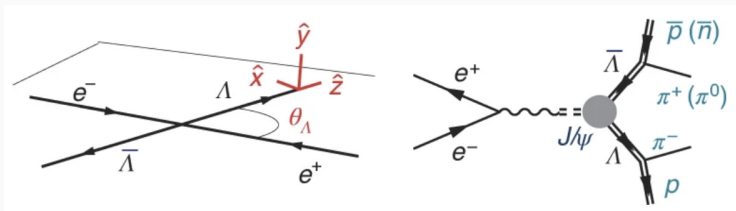
The BESIII Collaboration

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<sup>11</sup>M. Ablikim et al. “Polarization and entanglement in baryon-antibaryon pair production in electron-positron annihilation”. In: *Nature Physics* (May 2019), p. 1.



# $\Lambda\bar{\Lambda}$ Production

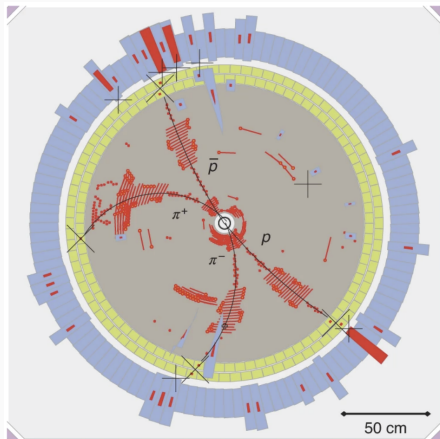


$\Lambda\bar{\Lambda}$  production process.

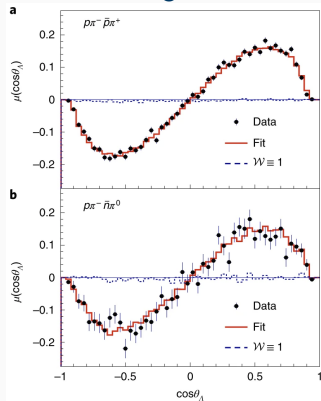
$$\begin{aligned}
 & \mathcal{W}(\xi; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_+) \\
 &= 1 + \alpha_\psi \cos^2 \theta_\Lambda + \alpha_- \alpha_+ \left[ \sin^2 \theta_\Lambda (n_{1,x} n_{2,x} - \alpha_\psi n_{1,y} n_{2,y}) \right. \\
 & \quad \left. + (\cos^2 \theta_\Lambda + \alpha_\psi) n_{1,z} n_{2,z} \right] \\
 &+ \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (n_{1,x} n_{2,z} + n_{1,z} n_{2,x}) \\
 &+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (\alpha_- n_{1,y} + \alpha_+ n_{2,y})
 \end{aligned}$$

$\Lambda\bar{\Lambda}$  intensity distribution

BES  $\Lambda - \bar{\Lambda}$  event



Polarization signal...



$$\mu(\cos \theta_{\Lambda}) = \frac{\alpha_- - \alpha_2}{2} \frac{1 + \alpha_{\psi} \cos^2 \theta_{\Lambda}}{3 + \alpha_{\psi}} P_y(\theta_{\Lambda})$$

**Table 1 | Summary of the results**

Parameters	This work	Previous results
$\alpha_\psi$	$0.461 \pm 0.006 \pm 0.007$	$0.469 \pm 0.027$ (ref. <sup>14</sup> )
$\Delta\Phi$	$42.4 \pm 0.6 \pm 0.5^\circ$	-
$\alpha_-$	$0.750 \pm 0.009 \pm 0.004$	$0.642 \pm 0.013$ (ref. <sup>6</sup> )
$\alpha_+$	$-0.758 \pm 0.010 \pm 0.007$	$-0.71 \pm 0.08$ (ref. <sup>6</sup> )
$\bar{\alpha}_0$	$-0.692 \pm 0.016 \pm 0.006$	-
$A_{CP}$	$-0.006 \pm 0.012 \pm 0.007$	$0.006 \pm 0.021$ (ref. <sup>6</sup> )
$\bar{\alpha}_0/\alpha_+$	$0.913 \pm 0.028 \pm 0.012$	-

# $\Lambda$ Weak Decay Parameter- BES Results

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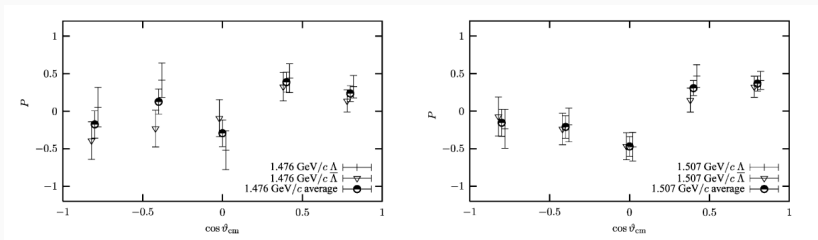
**>  $5\sigma$  difference between new result and PDG<sup>12</sup>.**

<sup>12</sup>(Particle Data Group) Tanabashi, M. et al. "Review of Particle Physics". In: *Phys. Rev. D* 98.3 (Aug. 2018), p. 030001.

**So What?**

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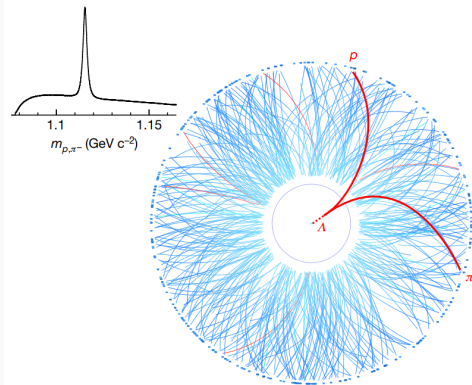
# $p\bar{p} \rightarrow \Lambda\bar{\Lambda}$ Polarization<sup>13</sup>



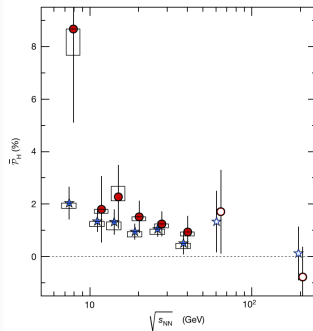
<sup>13</sup>E. Klempt et al. “Antinucleon nucleon interaction at low energy: Scattering and protonium”. In: *Phys. Rept.* 368 (2002), pp. 119–316.

# Global $\Lambda$ hyperon polarization in nuclear collisions<sup>14</sup>

STAR Au-Au collision



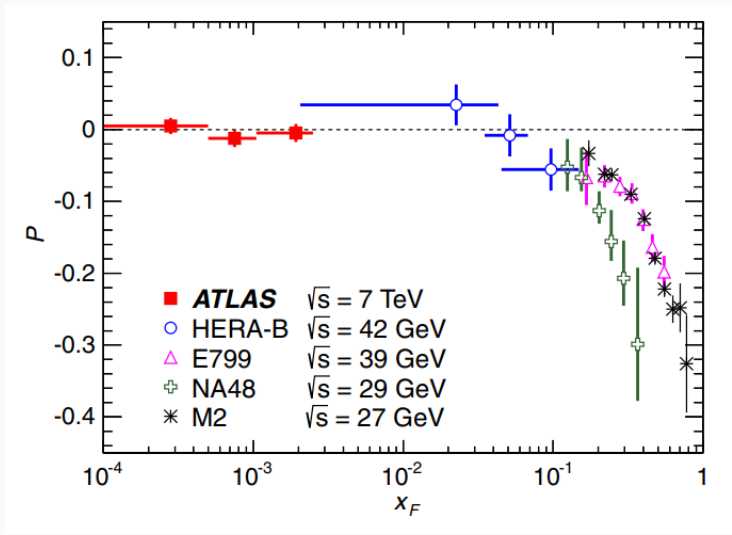
Average  $\Lambda$  ( $\bar{\Lambda}$ ) polarization in collisions...



<sup>14</sup>The STAR Collaboration. "Global  $\Lambda$  hyperon polarization in nuclear collisions". In: *Nature* 548.7665 (2017), pp. 62–65.



# $\Lambda(\bar{\Lambda})$ Transverse Polarization with ATLAS<sup>15</sup>



<sup>15</sup>ATLAS Collaboration, G. Aad, et al. "Measurement of the transverse polarization of  $\Lambda$  and  $\bar{\Lambda}$  hyperons produced in proton-proton...". In: *Phys. Rev. D* 91 (2015),

# Decay Parameters of Higher Mass States<sup>16</sup>

## $\Omega^-$ DECAY PARAMETERS

### $\alpha(\Omega^-) \alpha_-(\Lambda)$ FOR $\Omega^- \rightarrow \Lambda K^-$

Some early results have been omitted.

VALUE	EVTS
$0.0115 \pm 0.0015$	<b>OUR AVERAGE</b>

## $\Xi^0$ DECAY PARAMETERS

See the "Note on Baryon Decay Parameters" in

### $\alpha(\Xi^0) \alpha_-(\Lambda)$

This is a product of the  $\Xi^0 \rightarrow \Lambda \pi^0$  and  $\Lambda \rightarrow p \pi^-$  asy

VALUE	EVTS
$-0.261 \pm 0.006$	<b>OUR AVERAGE</b>

<sup>16</sup>(Particle Data Group) Tanabashi, M. et al. "Review of Particle Physics". In: *Phys. Rev. D* 98.3 (Aug. 2018), p. 030001.

## **Consequences for Kaon Photoproduction Observables?**

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# Fierz Identity for LUY plus CUY

## Intensities for Experimental Polarization Configurations:

**LUY:** Linear photon beam; unpolarized target; measured recoil

$$1 + \alpha_- \cos \theta_y \mathbf{P} - \{ \Sigma + \alpha_- \cos \theta_y \mathbf{T} \} P_L^\gamma \cos 2(\alpha - \phi) \\ + \{ \alpha_- \cos \theta_x \mathbf{O}_x + \alpha_- \cos \theta_z \mathbf{O}_z \} P_L^\gamma \sin 2(\alpha - \phi)$$

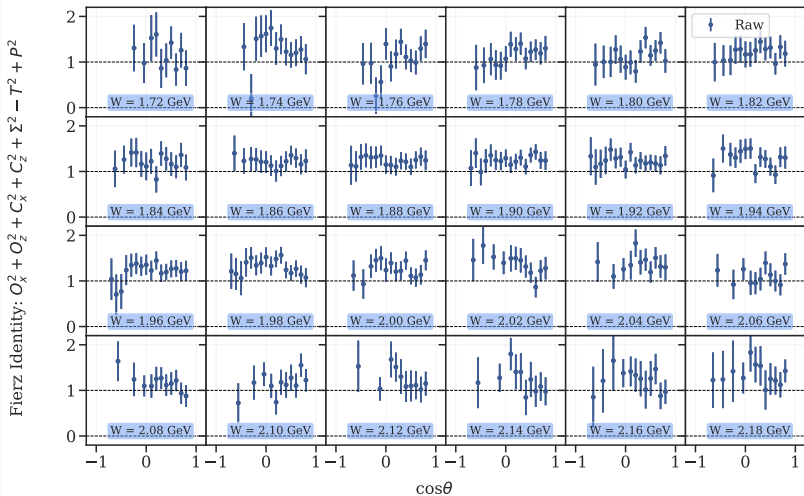
**CUY:** Circularly photon beam; unpolarized target; measured recoil

$$1 + \alpha_- \cos \theta_y \mathbf{P} + (\alpha_- \cos \theta_x \mathbf{C}_x + \alpha_- \cos \theta_z \mathbf{C}_z) P_C^\gamma$$

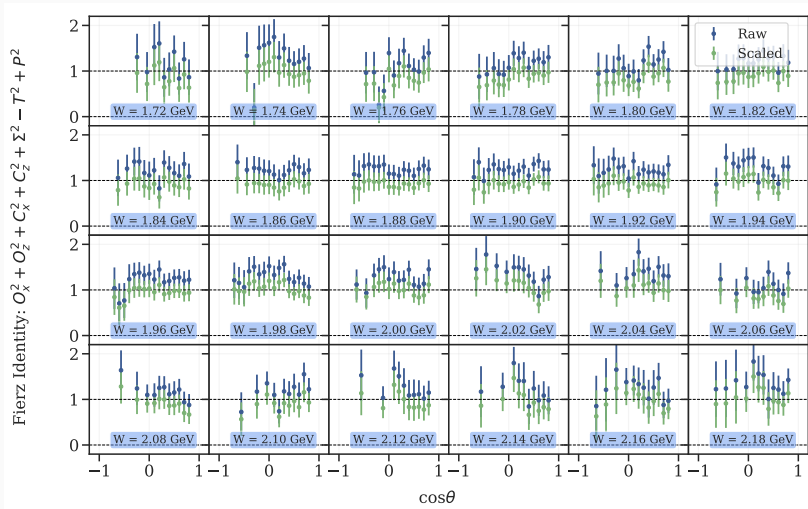
## Fierz identities connecting two experiments:

$$\mathbf{O}_x^2 + \mathbf{O}_z^2 + \mathbf{C}_x^2 + \mathbf{C}_z^2 + \Sigma^2 - \mathbf{T}^2 + \mathbf{P}^2 = 1 \\ \Sigma \mathbf{P} - \mathbf{C}_x \mathbf{O}_z + \mathbf{C}_z \mathbf{O}_x - \mathbf{T} = 0 .$$

# Fierz Identity Values for Original Data



# Fierz Identity Values for Scaled Data



# Fierz Identities as a Statistical Ensemble

Generate **pseudodata**:

- Pick random point in amplitude space
- Calculate observables from amplitudes
- Treat observables as independent and adjust value by a random number sampled from  $\mathcal{N}(0, \sigma)$ ,
- Single polarization observables have  $\sigma \in [0.01, 0.05]$
- Double polarization observables have  $3 \times \sigma$

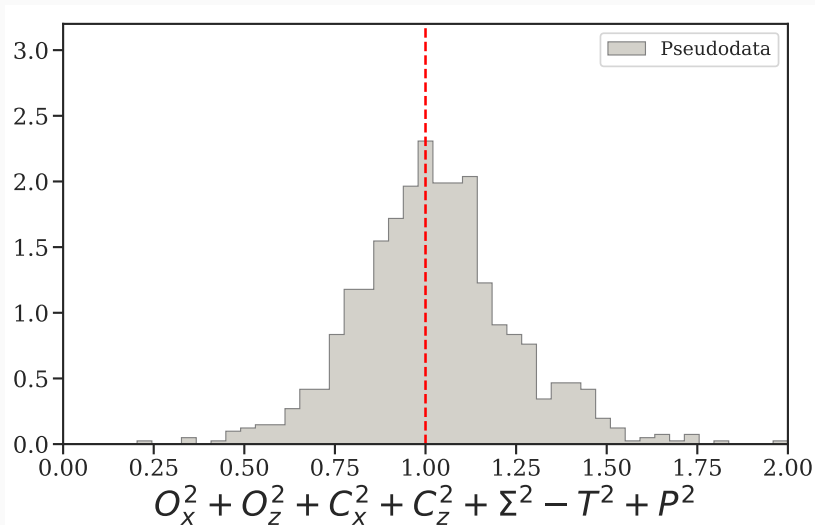
Writing

$$\mathcal{F} = \mathbf{O}_x^2 + \mathbf{O}_z^2 + \mathbf{C}_x^2 + \mathbf{C}_z^2 + \mathbf{\Sigma}^2 - \mathbf{T}^2 + \mathbf{P}^2$$

Also define **pull** as

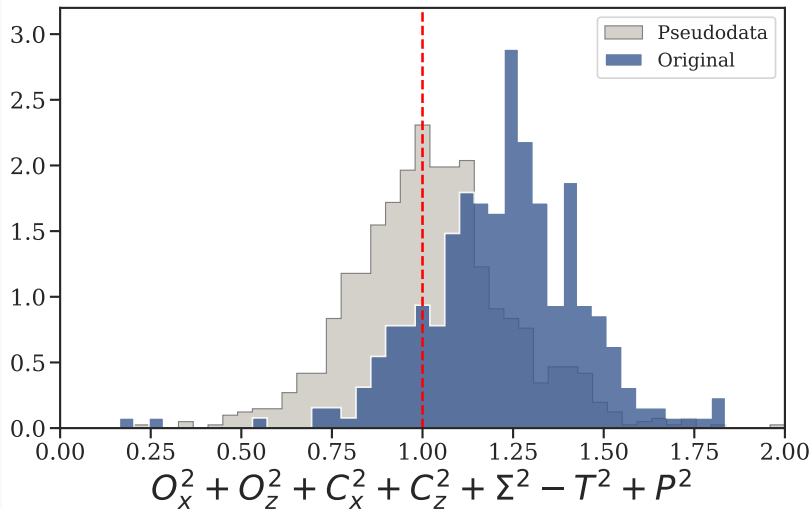
$$\frac{\mathcal{F} - 1}{\sigma_{\mathcal{F}}}$$

## Key Result: Histogram of Fierz Identities

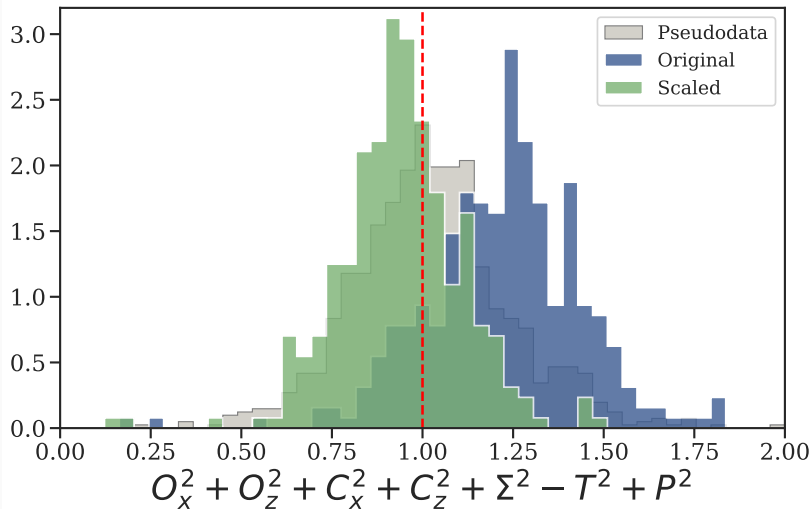




# Key Result: Histogram of Fierz Identities



# Key Result: Histogram of Fierz Identities



**Estimate  $\alpha_-$  from  $K\Lambda$  data?**

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## Infer $\alpha_-$ from $K\Lambda$ data

with: M. Döring, D. I. Glazier, J. Haidenbauer, R. Murray-Smith, M. Mai and D. Rönchen<sup>17</sup>.

## Fierz Identities as Random Variables

$$\begin{aligned}\mathcal{F}_i^{(1)} &= a^2 l^2 (\mathcal{O}_{x,i}^2 + \mathcal{O}_{z,i}^2 - \mathcal{T}_i^2) + a^2 c^2 (\mathcal{C}_{x,i}^2 + \mathcal{C}_{z,i}^2) + l^2 \Sigma_i^2 + a^2 \mathcal{P}_i^2, \\ \mathcal{F}_i^{(2)} &= a l [\Sigma_i \mathcal{P}_i - \mathcal{T}_i - a c (\mathcal{C}_{x,i} \mathcal{O}_{z,i} - \mathcal{C}_{z,i} \mathcal{O}_{x,i})],\end{aligned}$$

where  $a = \alpha_-^{\text{PDG}} / \alpha_-$  and  $c, l$  are **relative calibrations** (i.e. systematics) for circular and linear photon polarization, resp.

Instances of  $\mathcal{F}_i^{(1)}$  and  $\mathcal{F}_i^{(2)}$  for given  $a, c$  and  $l$  are  $f_i^{(1)}$  and  $f_i^{(2)}$

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<sup>17</sup>D. G. Ireland et al. In: *arXiv:1904.07616* (2019).

## Likelihood Function

$$p_i(\mathfrak{D}_i|a, l, c) \propto \exp \left[ - \left( \frac{f_i^{(1)} - 1}{\sigma_{\mathcal{F}_i^{(1)}}} \right)^2 - \left( \frac{f_i^{(2)}}{\sigma_{\mathcal{F}_i^{(2)}}} \right)^2 \right],$$

assuming observables are independent and identically distributed (gaussian).  $\mathfrak{D}_i = \cup_{j=1}^7 \mathcal{O}_{j,i}$  represents observables at point  $i$

For observables from  $N$  bins:

$$\mathcal{P}(\mathfrak{D}|a, l, c) \propto \prod_{i=1}^n p_i(\mathfrak{D}_i|a, l, c)$$

where  $\mathfrak{D} = \cup_{i=1}^n \mathfrak{D}_i$  represents entire data set.

i.e. the probability that the observables obey Fierz identity

## Include knowledge of calibrations

Calculate posterior PDF from likelihood and prior:

$$\mathcal{P}(a, l, c|\mathcal{D}) \propto \mathcal{P}(\mathcal{D}|a, l, c)\mathcal{P}(l, c) .$$

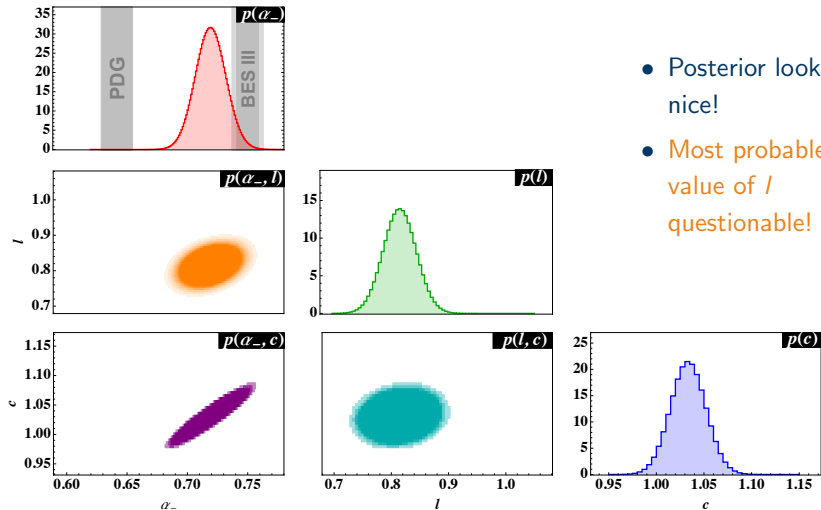
- Impose  $\alpha_- \geq 0$
- Quoted systematic uncertainties in  $P_\gamma^L$  are 3-6% (use 5)
- Quoted systematic uncertainties in  $P_\gamma^C$  are 2% (use 2%)
- Which PDF to use? Gaussian  $\mathcal{N}(1, \sigma)$ ? Uniform  $\mathcal{U}(1 - \sigma, 1 + \sigma)$ ?

## Posterior PDF

Function of  $a$ ,  $c$  and  $l$ ,  $\mathcal{P}(a, l, c|\mathcal{D})$ , calculations done by

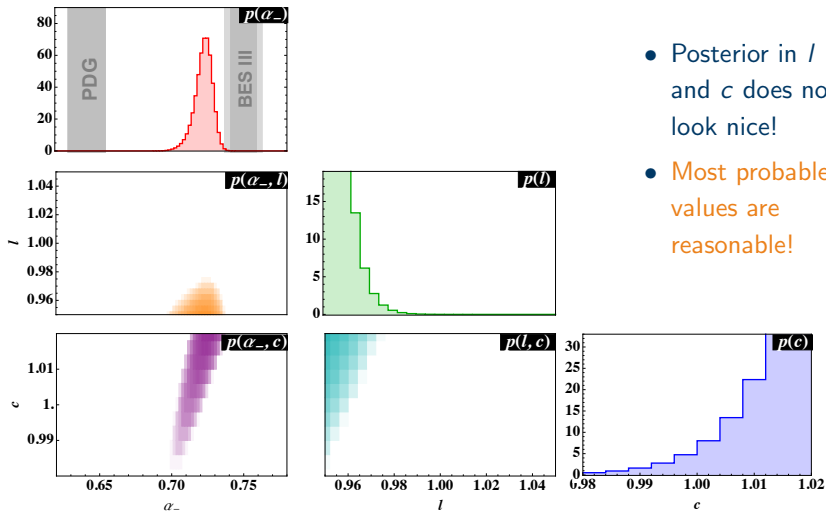
1. Markov Chain Monte Carlo (MCMC)
2. Direct calculation on  $a - c - l$  grid

# Gaussian Prior



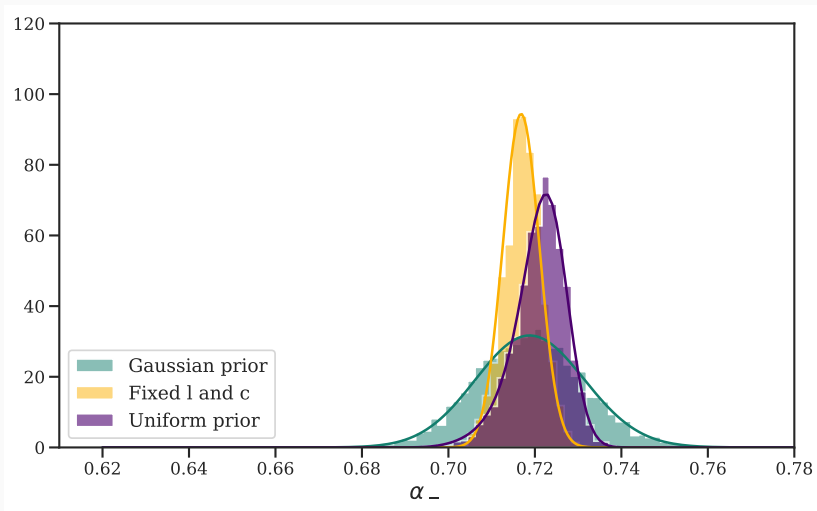
- Posterior looks nice!
- Most probable value of  $l$  questionable!

# Uniform Prior

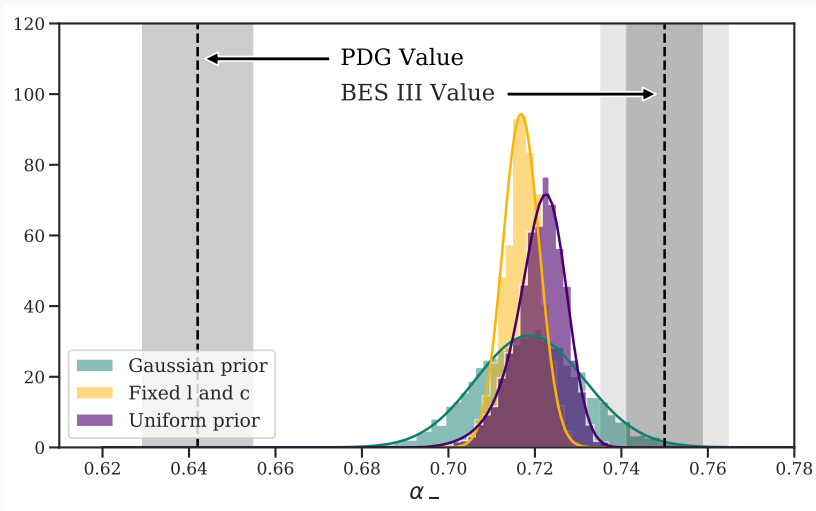




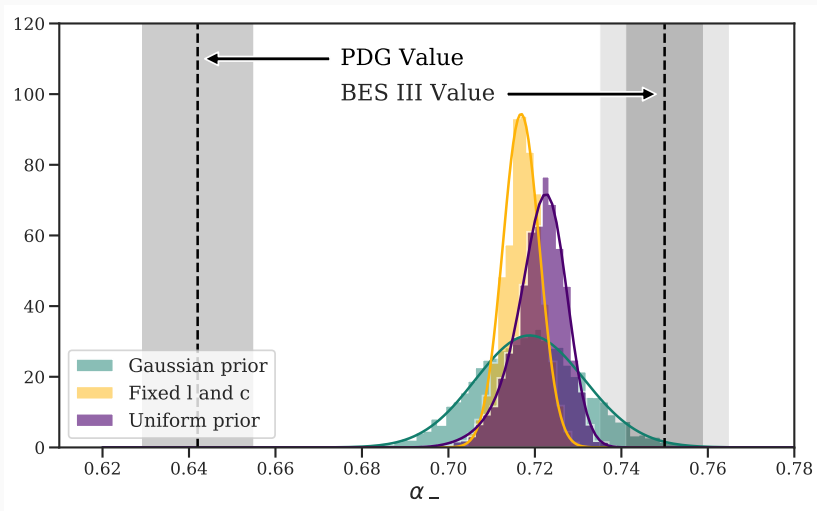
## Posterior PDFs for $\alpha_-$ - Summary of results



# Posterior PDFs for $\alpha_-$ - Summary of results



# Posterior PDFs for $\alpha_-$ - Summary of results



$$\alpha_- = 0.721 \pm 0.006 \text{ (stat.)} \pm 0.005 \text{ (sys.)}$$

## Estimates of $\alpha_-$ - Summary of results

Source	Value	Prior Assumption $P_{\gamma}^L, P_{\gamma}^C$
PDG	$0.642 \pm 0.013$	
BES III	$0.750 \pm 0.009 \pm 0.004$	
CLAS	$0.719 \pm 0.013$	$\mathcal{N}(1.0, 0.05^2), \mathcal{N}(1.0, 0.02^2)$
	$0.721 \pm 0.006$ (*)	$\mathcal{U}(0.95, 1.05), \mathcal{U}(0.98, 1.02)$
	$0.727 \pm 0.007$	$\mathcal{U}(0.90, 1.10), \mathcal{U}(0.96, 1.04)$
	$0.717 \pm 0.004$	Both fixed at 1.0
	$0.721 \pm 0.006 \pm 0.005$	Summary of our result

## **Consequences for Fitting Kaon Photoproduction Observables?**

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# Refit of JüBo Coupled Channels Model

Observable (# data points)	$\chi^2/n$ (Refits)		
	$\alpha_- = 0.642$	0.75	0.721
$d\sigma/d\Omega$ (421)	1.11	1.03	0.95
$\Sigma$ (314)	2.55	2.61	2.56
$T$ (314)	1.75	1.74	1.69
$P$ (410)	1.84	1.66	1.62
$C_x$ (82)	2.15	1.72	1.34
$C_z$ (85)	1.58	1.83	1.62
$O_x$ (314)	1.44	1.53	1.51
$O_z$ (314)	1.34	1.58	1.49
all (2254)	1.67	1.66	1.59

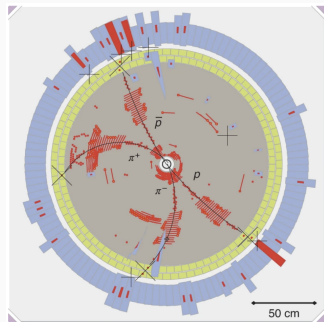
**Improved fit!**

## Conclusions

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# Summary

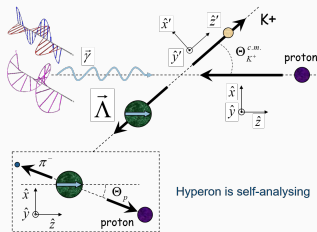
- New BES III result for  $\alpha_-$  is 17% higher than PDG value





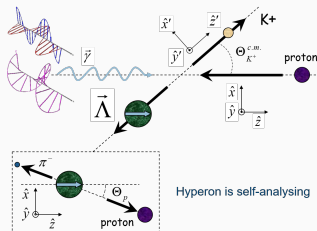
# Summary

- New BES III result for  $\alpha_-$  is 17% higher than PDG value
- Affects **all recoil observables** relying on  $\Lambda$  weak decay



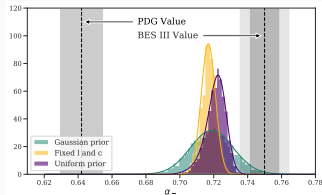
# Summary

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- Kaon photoproduction data can **independently** determine  $\alpha_-$



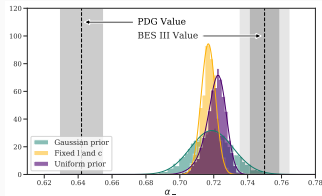
# Summary

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- Other analyses will have to be reviewed!

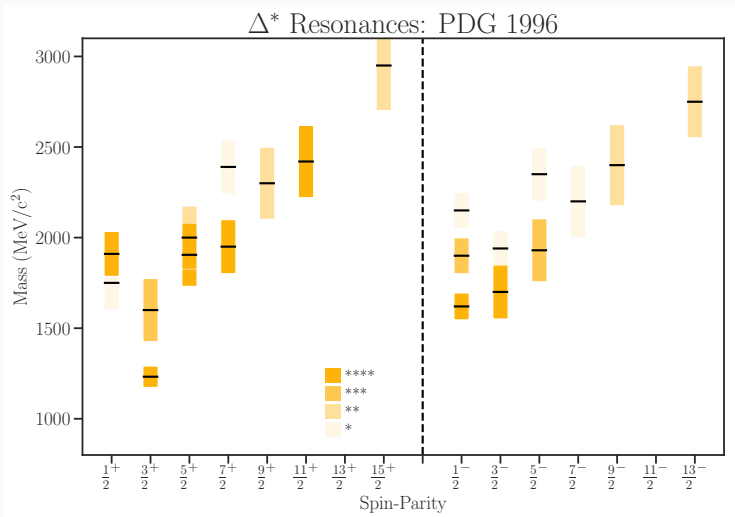


Details posted on arXiv<sup>18</sup>

<sup>18</sup>D. G. Ireland et al. In: *arXiv:1904.07616* (2019).

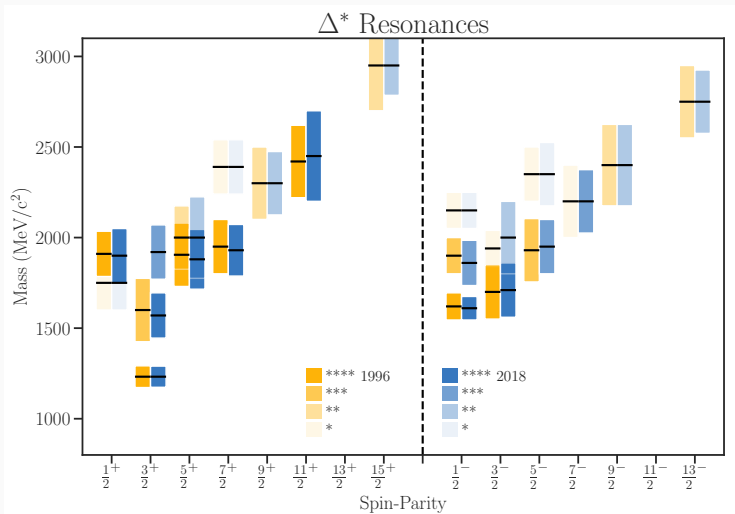
Backup Slides

# Light Baryon Spectrum - PDG 1996<sup>19</sup> List of $\Delta$ Resonances



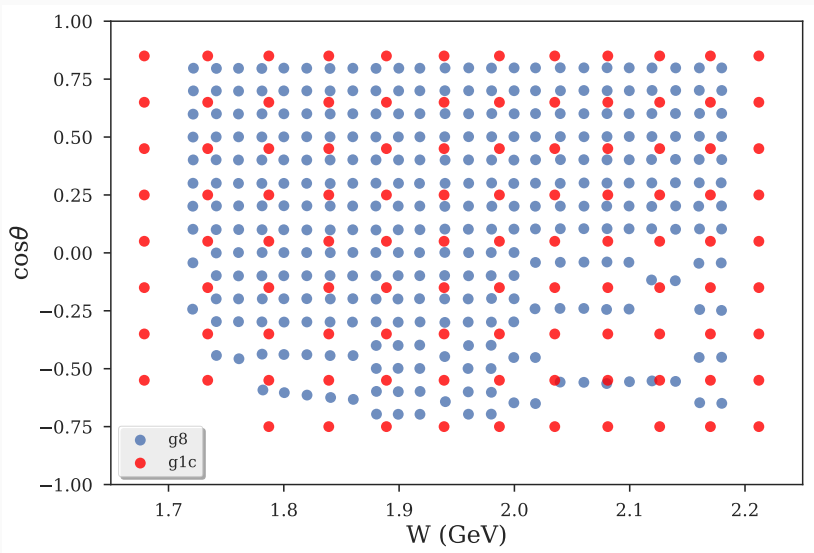
<sup>19</sup>R.M. Barnett et al. In: *Phys. Rev. D* 54 (1996), p. 1.

# Light Baryon Spectrum - PDG 2018<sup>20</sup> List of $\Delta$ Resonances



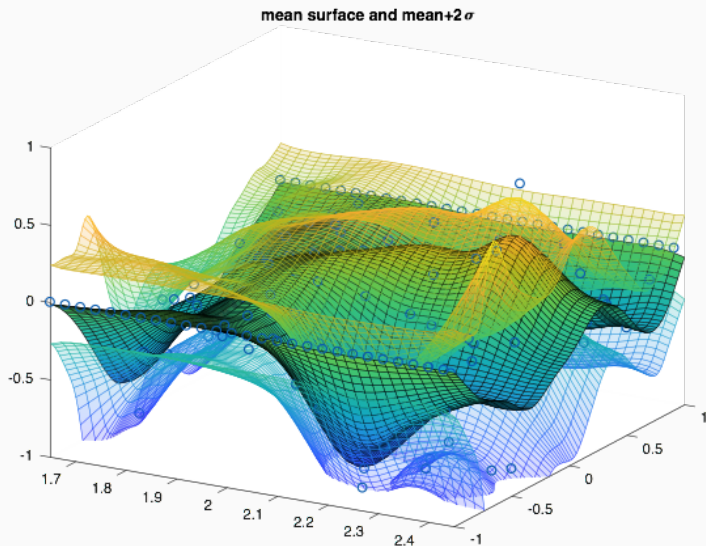
<sup>20</sup>(Particle Data Group) Tanabashi, M. et al. "Review of Particle Physics". In: *Phys. Rev. D* 98.3 (Aug. 2018), p. 030001.

# g8 $K - \Lambda$ Coverage

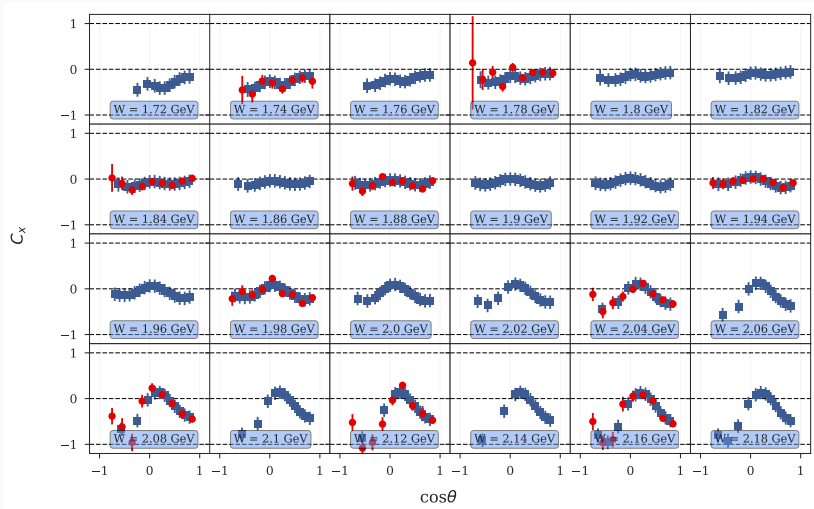




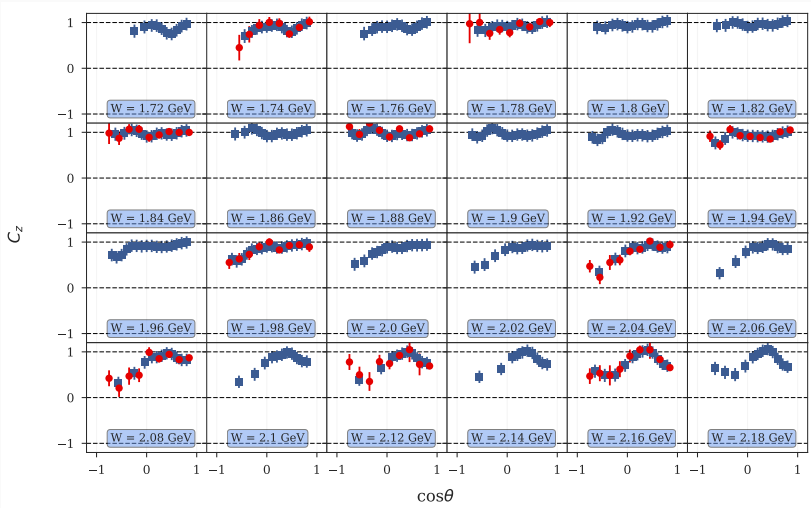
# Gaussian Process Interpolation



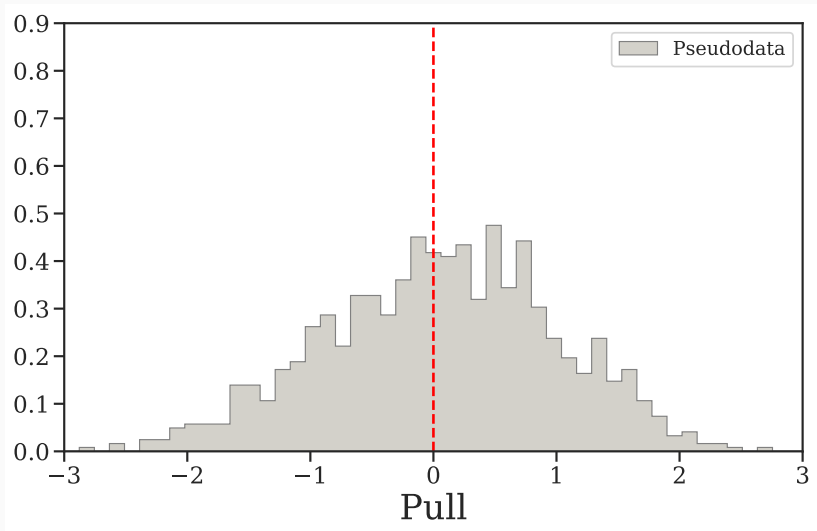
# Using Gaussian Process to Interpolate g1c to g8 Bins: $C_x$



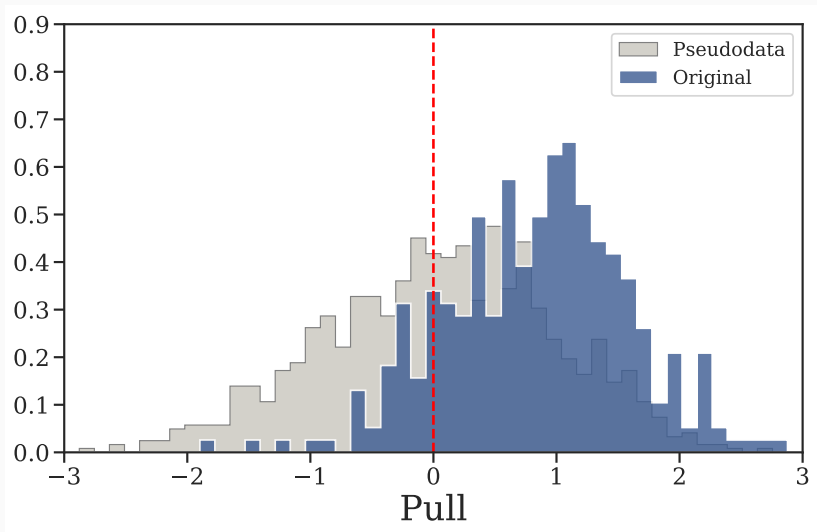
# Using Gaussian Process to Interpolate g1c to g8 Bins: $C_z$



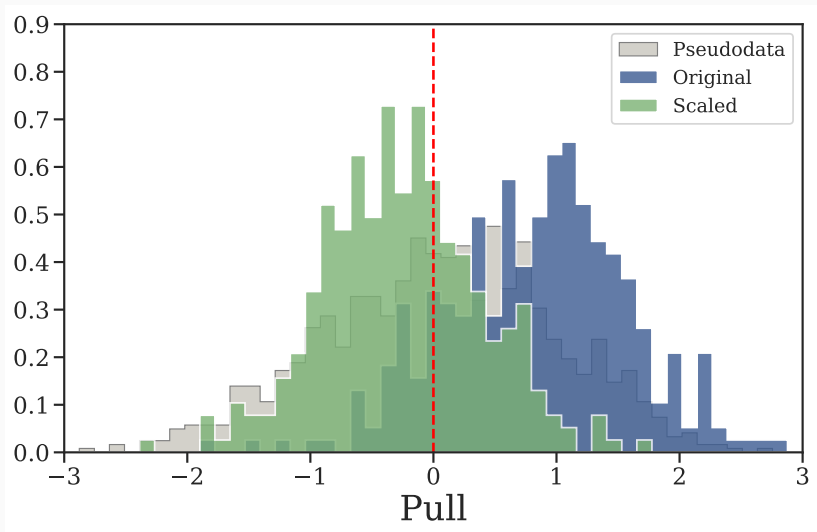
## Key Result: Pulls of Fierz Identities



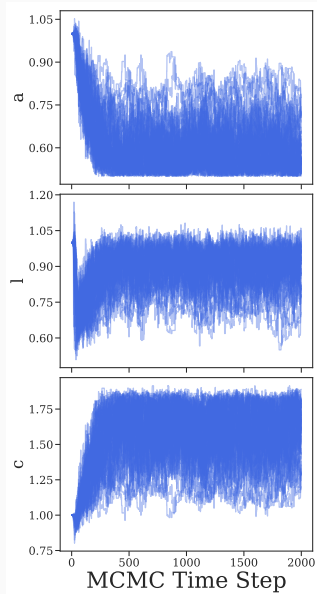
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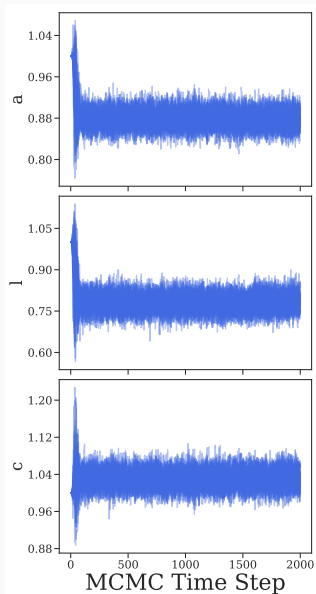
## Key Result: Pulls of Fierz Identities



# MCMC Chain - no prior



# MCMC Chain - gaussian prior





# MCMC Chain - uniform prior

